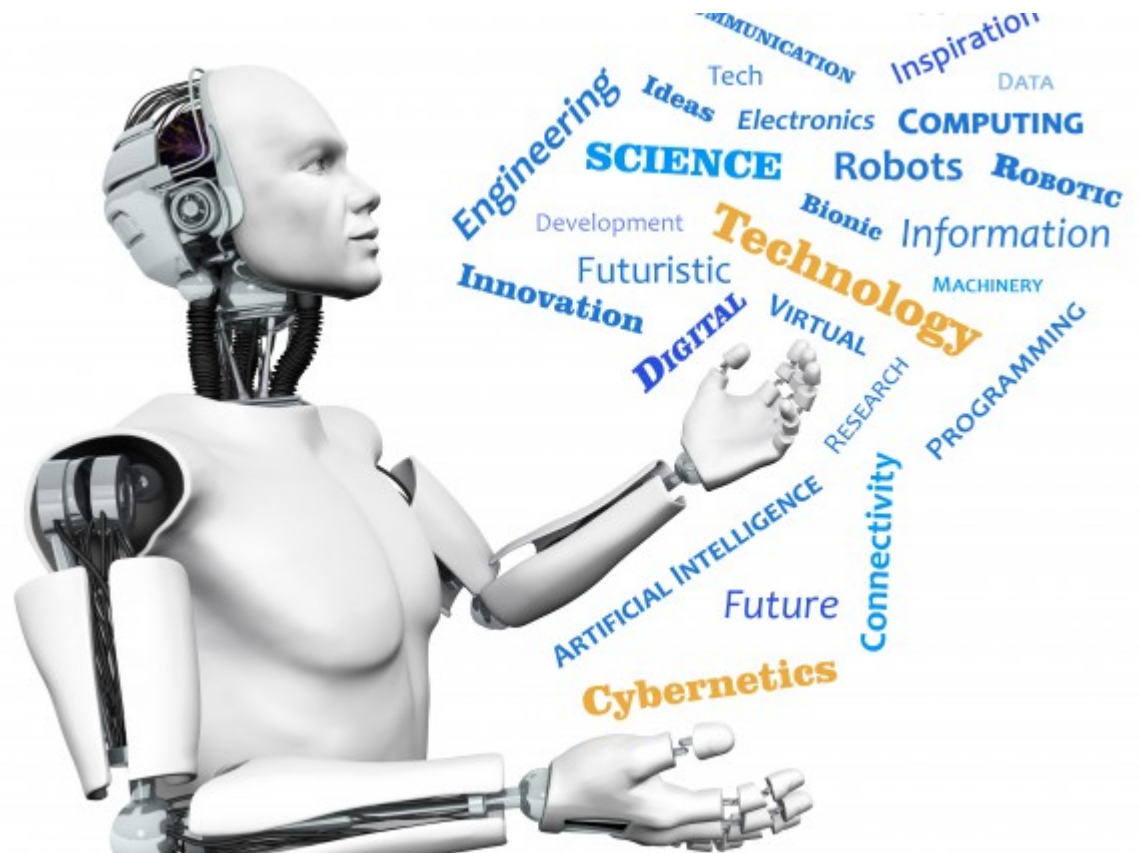


15-494/694: Cognitive Robotics

Dave Touretzky

Lecture 7:

The World Map



Outline

- Why have a world map?
- What's in Cozmo's native world map?
- Cozmo localization
- Object pose: quaternions
- Designing our own world map
- Obstacle detection

Why Have A World Map?

- Represent objects available to the robot.
- Landmarks to be used for localization.
- Obstacle avoidance during path planning.

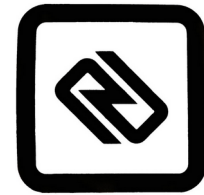
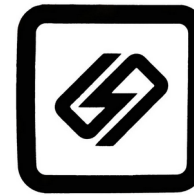
What's In Cozmo's Native World Map?

- Cozmo himself
- The light cubes, once seen
- The charger, once sensed or seen
- Faces that have been detected
- Custom markers that have been detected
- To access the world map:
 - `robot.world` is a `cozmo.world.World` object
 - components: `robot.world.light_cubes`, etc.

Light Cube Markers

“Paperclip”

1:



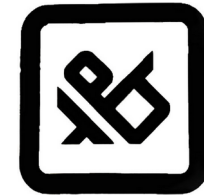
“Anglepoise Lamp”

2:



“Deli Slicer” or
“car seat”

3:



0°

90°

180°

270°

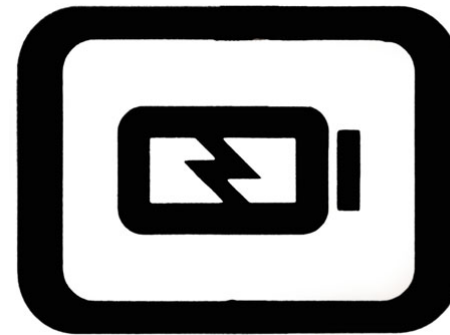
bot

top



The Charger

- Base frame is front lip; marker in back.
- `robot.is_on_charger` is True or False
- Robot won't move while on the charger

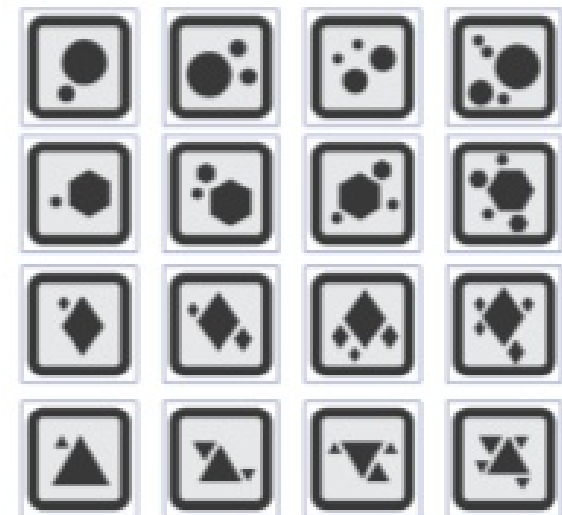


Custom Markers

Markers: Cubes, Charger, & Custom Objects (SDK)



Custom Markers for SDK



Origin ID

- The robot's origin_id starts at 1.
- Every time Cozmo is picked up and put down, he may get a new origin_id value.
- Landmarks can pull him back to an old id.

- Object origin_id's start at -1 (invalid).
- Every time the robot sees an object, that object's origin_id is updated to match the robot's.
- Object poses are only valid if their origin_id matches the robot's.

Cozmo's Localization

- The cubes serve as visual landmarks that contribute to Cozmo's localization.
- The charger also contributes, if Cozmo has seen the marker.
- When Cozmo is on the charger, he knows exactly where he is.
- If a cube changes position, did the cube move, or did Cozmo move?
 - Cozmo knows when he has moved.
 - He also knows when a cube moves.

Object Pose

- The robot, cubes, and charger have a *pose* attribute that is an instance of `cozmo.util.Pose`.
- `robot.pose.position` is (x,y,z) coordinates.
- `robot.pose.rotation` is complicated:
 - a quaternion gives the full 3D pose
 - `angle_z` gives the orientation about the z-axis, which is usually all you care about

Quaternions

- A quaternion q is a four-dimensional complex number (w, x, y, z) or (q_0, q_1, q_2, q_3) .
- w is a point on the real axis, and x, y, z are points on the i, j, k imaginary axes.

$$q = w + x \cdot i + y \cdot j + z \cdot k$$

$$i \cdot i = j \cdot j = k \cdot k = i \cdot j \cdot k = -1$$

$$i \cdot j = k \quad j \cdot k = i \quad k \cdot i = j$$

$$j \cdot i = -k \quad k \cdot j = -i \quad i \cdot k = -j$$

Quaternions and Rotations

The mathematical properties of quaternions mirror those of 3D rotations: multiplication is not commutative!

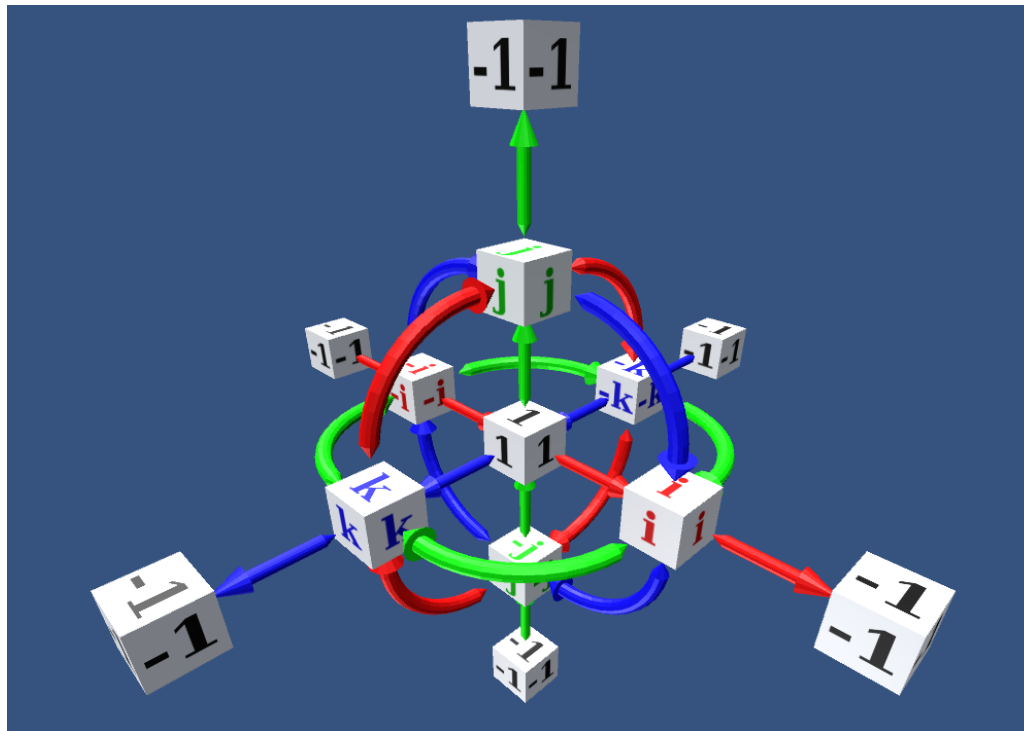


Image source: <https://aha.betterexplained.com>

Magnitude of a Quaternion

$$q = w + x \cdot i + y \cdot j + z \cdot k$$

$$\|q\| = \sqrt{w^2 + x^2 + y^2 + z^2}$$

For pure rotations we want $\|q\|=1$.

Quaternions as Poses

- Quaternions describe *rotations* in terms of an axis of rotation and an angle θ .
- Think of a pose as a rotation from the world reference frame (z up, x forward) to the object's reference frame.
- We can also represent rotations using 4x4 transformation matrices.
- To compose rotations:
 - Multiply the transformation matrices, or
 - Multiply the quaternions

Simple Cases

- “No rotation”:

$$q = (1, 0, 0, 0)$$

- Rotation by θ about the z axis:

$$q = (\cos \theta/2, 0, 0, \sin \theta/2)$$

- General case:

- The magnitude of the rotation is $\sin \theta/2$.
- The direction of rotation is indicated by distributing $\sin \theta/2$ among the i,j,k axes.
- Real $w = \cos \theta/2$ is a normalization term.

Motion Model

- The cozmo-tools particle filter includes a motion model.
- How does it get motion information?
- Look for changes in robot.pose every few milliseconds.
- If origin_id remains the same when pose changes, we have valid motion info.
- If origin_id has changed, cannot subtract poses because their reference frames differ. Wait for next time.

The cozmo-tools World Map

Why make our own world map?

- To support additional object types:
 - ArUco markers
 - Walls
 - Chips
 - Other cameras
 - Other robots (shared world map)
- To allow our own particle filter to maintain the map (SLAM algorithm)

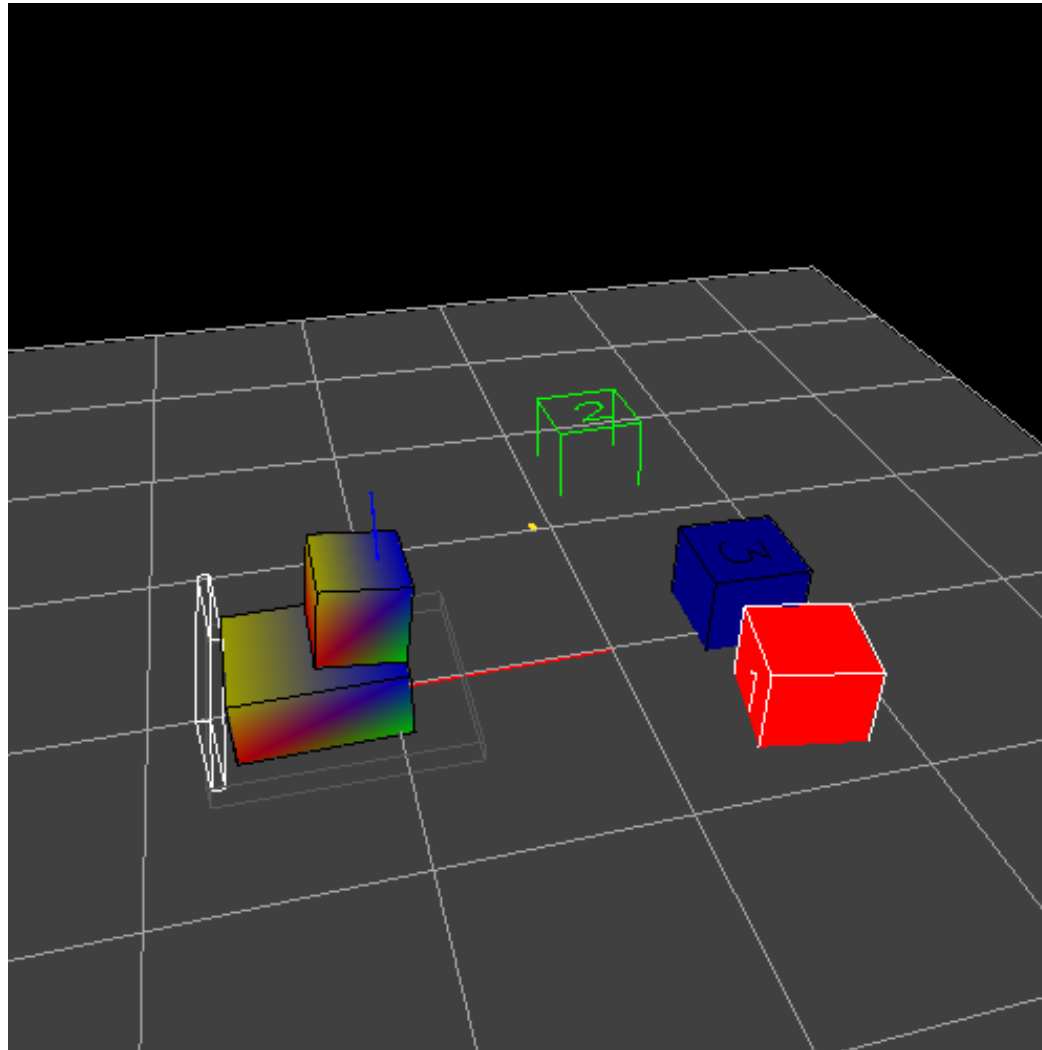
The cozmo-tools World Map

- Stored in `robot.world.world_map`
- Objects are in a dictionary:
`robot.world.world_map.objects`
- Subclasses of `WorldObject`:
 - `LightCubeObj`
 - `ChargerObj`
 - `CustomMarkerObj`
 - etc.
- Type “show objects” to display.

The cozmo-tools World Map

- Robot position maintained by our particle filter, not robot.pose
 - Type “show pose” to see both robot pose estimates
- Cubes and charger imported from their SDK representations as WorldMapObj’s:
 - wcube1, wcube2, wcube3, wcharger
 - wcube1.sdk_obj is cube1

show worldmap_viewer



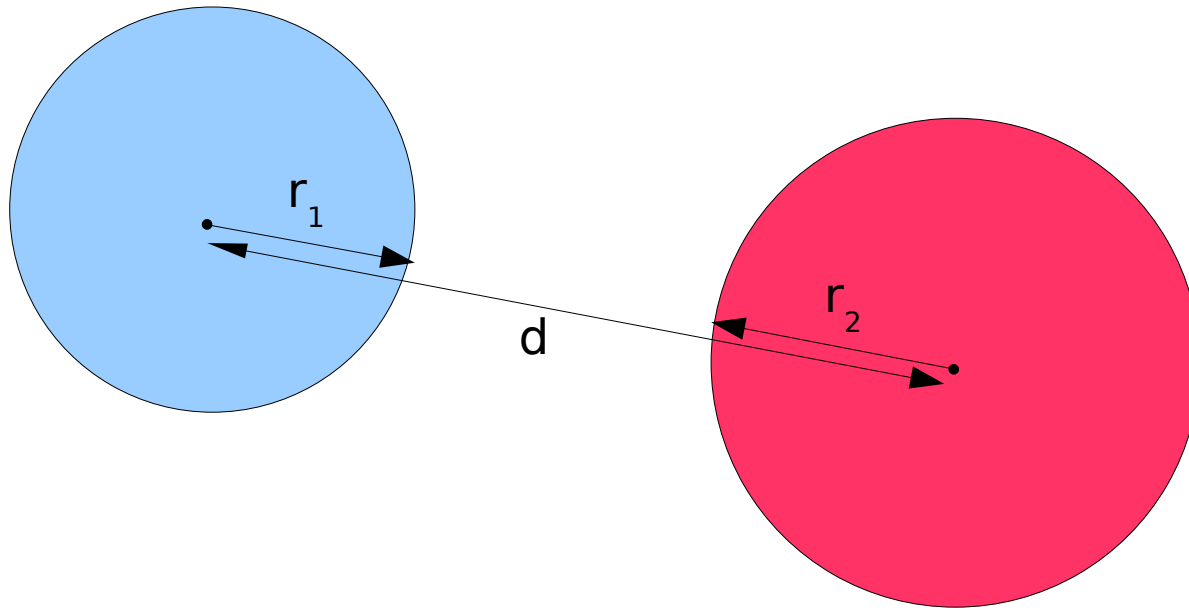
Obstacle Avoidance

- Having a world map allows us to do path planning to avoid obstacles.
- The path planner needs a way to detect when two objects would collide.
- How can we detect collisions?

Collision Detection

- Represent the robot and the obstacles as **convex polygons**.
- In 2D, use the Separating Axis Theorem to check for collisions.
 - Easy to code
 - Fast to compute
- In 3D, things get more complex.
 - The GJK (Gilbert-Johnson-Keerthi) algorithm is used in many physics engines for video games.

Collision Detection: Circles

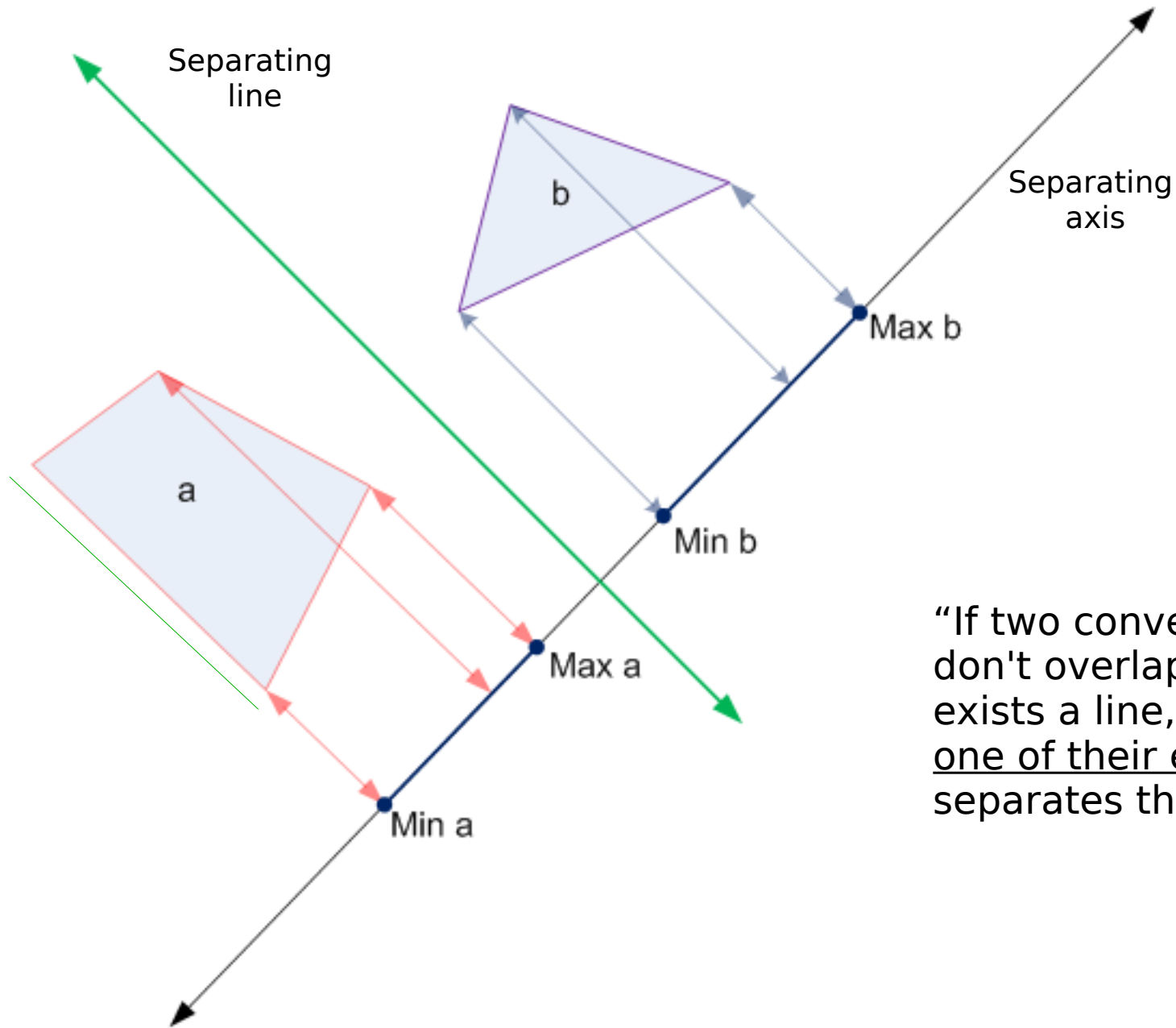


- Let d = distance between centers
- Let r_1, r_2 be the radii
- No collision if $d > r_1 + r_2$

Collision Detection: Two Convex Polygons

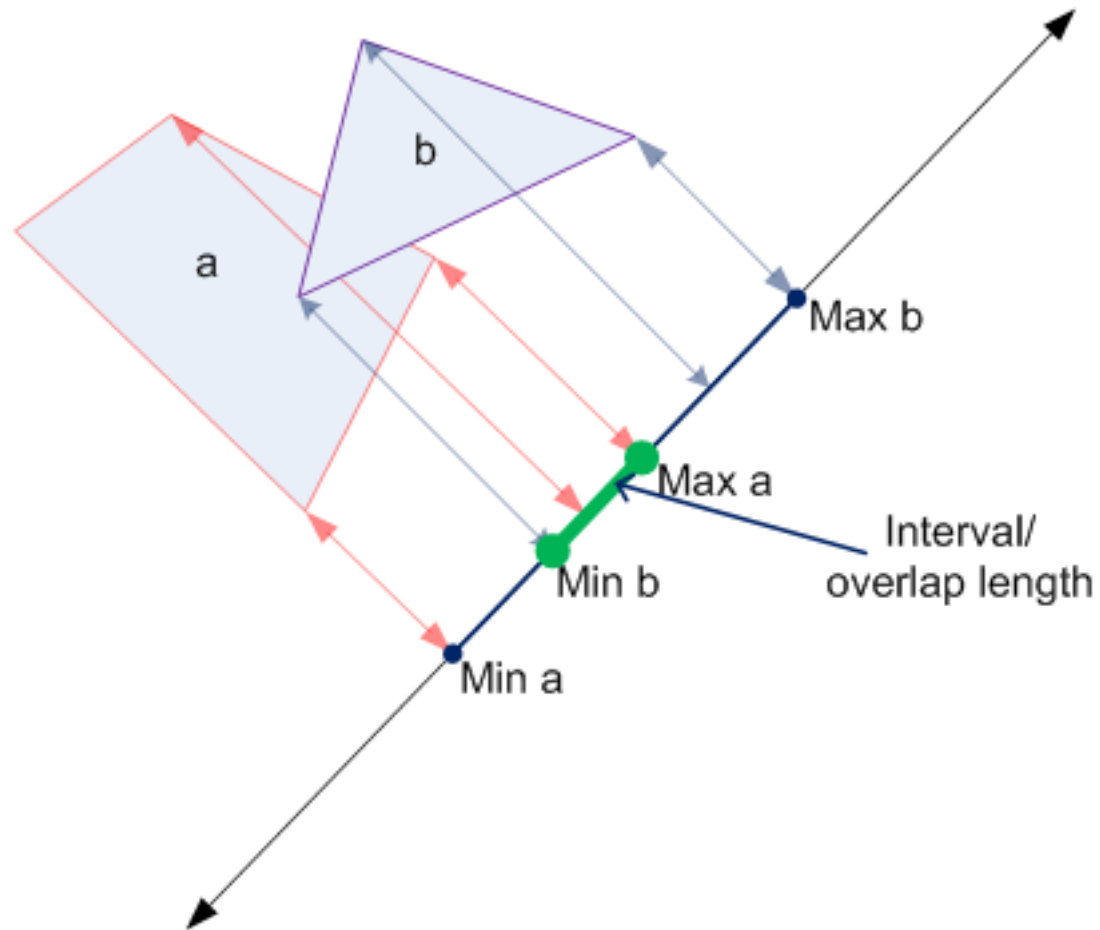
- The Separating Axis Theorem can be used to detect collisions between two convex polygons.
- Time is proportional to the number of vertices.
- To handle non-convex polygons, decompose them into sets of convex polygons and check for collisions between any two components.

Separating Axis Theorem

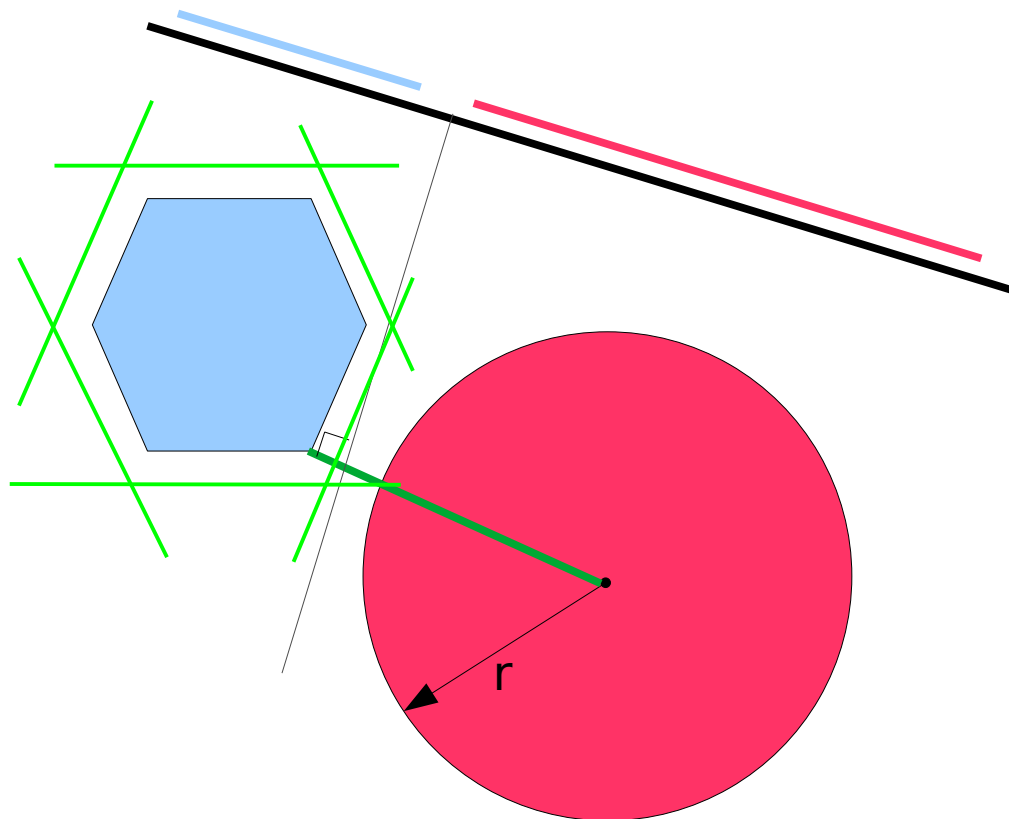


“If two convex polygons don't overlap, then there exists a line, parallel to one of their edges that separates them.”

Separating Axis Theorem



Collision Detection: Circle and Convex Polygon



- Separating axes to check are parallel to the edges of the polygon or the line joining the nearest vertex to the center of the circle.

Collision Detection Algorithm

We only need to find one separating axis to be assured of no collision.

```
def collision_check(poly1, poly2):  
    for axis in Edges(poly1) ∪ Edges(poly2):  
        base = perpendicular_to(axis)  
        proj1 = project_verts(poly1, base)  
        proj2 = project_verts(poly2, base)  
        if not overlap(proj1, proj2):  
            return False  
    return True
```

How To Build A World Map

- SLAM: Simultaneous Localization and Mapping algorithm.
- Each particle stores:
 - a hypothesis about the robot's location (x, y, θ)
 - a hypothesis about the map, e.g., a set of landmark identities and locations: $\{ (i, x_i, y_i, \theta_i) \}$.
- Particles score well if:
 - Landmark locations match the sensor values predicted by the robot's location.