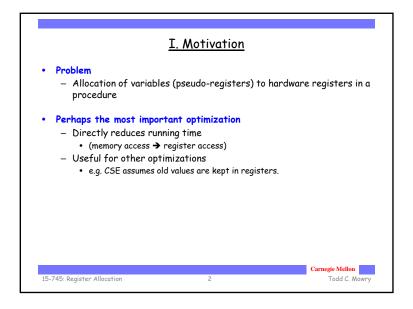
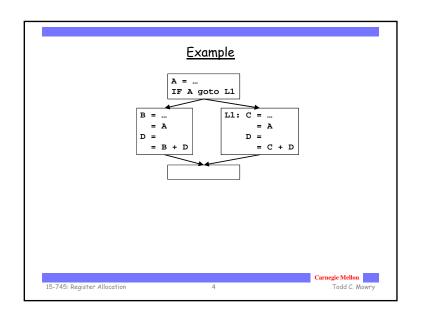
Lecture 15 Register Allocation I. Introduction II. Abstraction and the Problem III. Algorithm Reading: ALSU 8.8.4

Goals • Find an allocation for all pseudo-registers, if possible. • If there are not enough registers in the machine, choose registers to spill to memory Carnegle Mellon 15-745: Register Allocation 3 Todd C. Mowry





II. An Abstraction for Allocation & Assignment

- Intuitively
 - Two pseudo-registers interfere if at some point in the program they cannot both occupy the same register.
- Interference graph: an undirected graph, where
 - nodes = pseudo-registers
 - there is an edge between two nodes if their corresponding pseudo-registers interfere
- · What is not represented
 - Extent of the interference between uses of different variables
 - Where in the program is the interference

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III. Algorithm

Step 1. Build an interference graph

- a. refining notion of a node
- b. finding the edges

Step 2. Coloring

- use heuristics to try to find an n-coloring
 - Success:
 - colorable and we have an assignment
 - Failure:
 - graph not colorable, or
 - graph is colorable, but it is too expensive to color

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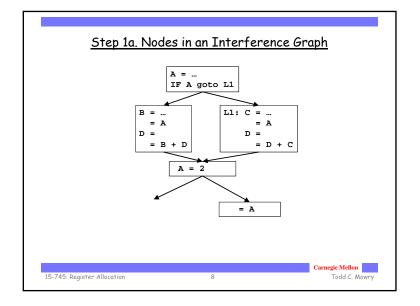
Register Allocation and Coloring

- A graph is n-colorable if:
 - every node in the graph can be colored with one of the n colors such that two adjacent nodes do not have the same color.
- Assigning n register (without spilling) = Coloring with n colors
 - assign a node to a register (color) such that no two adjacent nodes are assigned same registers(colors)
- Is spilling necessary? = Is the graph n-colorable?
- To determine if a graph is n-colorable is NP-complete, for n>2
 - Too expensive
 - Heuristics

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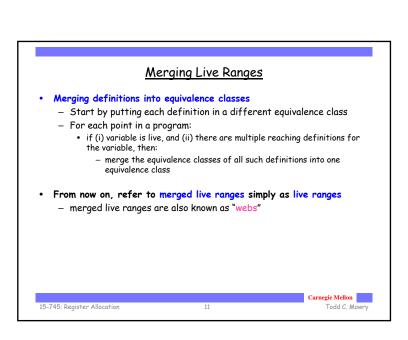
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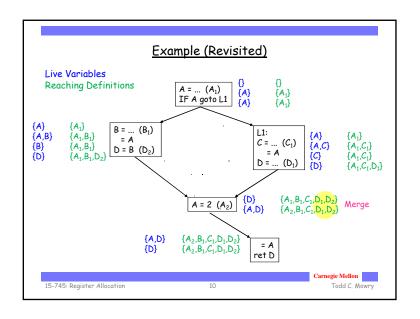


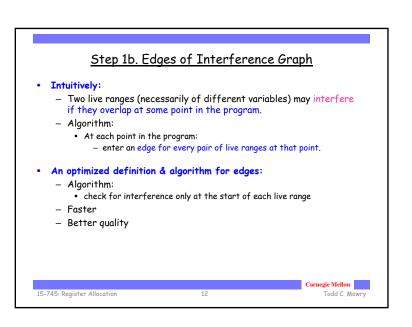
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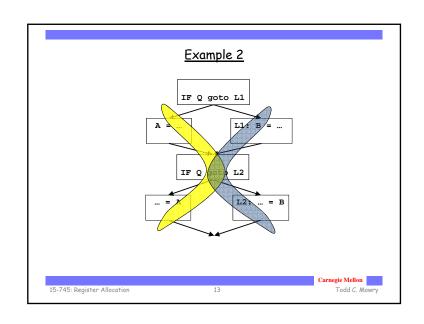
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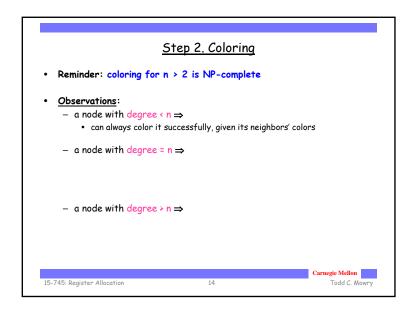


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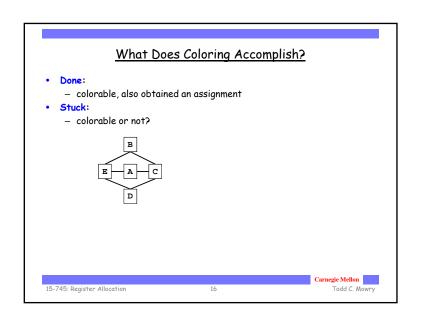








Coloring Algorithm • Algorithm: - Iterate until stuck or done • Pick any node with degree < n • Remove the node and its edges from the graph - If done (no nodes left) • reverse process and add colors • Example (n = 3): • Note: degree of a node may drop in iteration • Avoids making arbitrary decisions that make coloring fail



What if Coloring Fails?

• Use heuristics to improve its chance of success and to spill code

Build interference graph

Iterative until there are no nodes left
If there exists a node v with less than n neighbor
place v on stack to register allocate
else

v = node chosen by heuristics (least frequently executed, has many neighbors) place v on stack to register allocate (mark as spilled) remove v and its edges from graph

While stack is not empty
Remove v from stack
Reinsert v and its edges into the graph
Assign v a color that differs from all its neighbors
(quaranteed to be possible for nodes not marked as spilled)

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Summary

- · Problems:
 - Given n registers in a machine, is spilling avoided?
 - Find an assignment for all pseudo-registers, whenever possible.
- Solution:

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- Abstraction: an interference graph
 - nodes: live ranges
 - edges: presence of live range at time of definition
- Register Allocation and Assignment problems
 - equivalent to n-colorability of interference graph
 - → NP-complete
- Heuristics to find an assignment for n colors
 - successful: colorable, and finds assignment
 - not successful: colorability unknown & no assignment

C

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