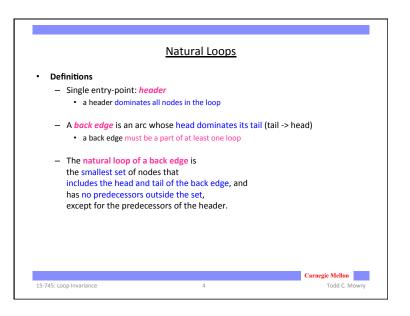
## Lecture 8 Loop Invariant Computation and Code Motion I. Finding loops II. Loop-invariant computation III. Algorithm for code motion

15-745: Loop Invariance

Todd C. Mowry

## Formal Definitions • Dominators - Node d dominates node n in a graph (d dom n) if every path from the start node to n goes through d - Dominators can be organized as a tree • a ->b in the dominator tree iff a immediately dominates b Carregie Mellon 15-745: Loop Invariance 3 Todd C. Mowry

## What is a Loop? • Goals: Define a loop in graph-theoretic terms (control flow graph) Not sensitive to input syntax A uniform treatment for all loops: DO, while, goto's Not every cycle is a "loop" from an optimization perspective start a b Intuitive properties of a loop single entry point edges must form at least a cycle



### Algorithm to Find Natural Loops

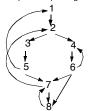
- 1. Find the dominator relations in a flow graph
- 2. Identify the back edges
- 3. Find the natural loop associated with the back edge

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### 2. Finding Back Edges

- · Depth-first spanning tree
  - Edges traversed in a depth-first search of the flow graph form a depth-first spanning tree



- · Categorizing edges in graph
  - · Advancing edges: from ancestor to proper descendant
  - · Cross edges: from right to left
  - Retreating edges: from descendant to ancestor (not necessarily proper)

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## 1. Finding Dominators

- Definition
  - Node *d* dominates node *n* in a graph (*d* dom *n*) if every path from the start node to *n* goes through *d*
- · Formulated as MOP problem:
  - node d lies on all possible paths reaching node  $n \Rightarrow d \operatorname{dom} n$ 
    - Direction:
    - Values:
    - Meet operator:
    - Top:
    - Bottom:
    - Boundary condition: start/entry node =
    - Initialization for internal nodes
    - Finite descending chain?
    - Transfer function:
- Speed:
- With reverse postorder, most flow graphs (reducible flow graphs) converge in 1 pass

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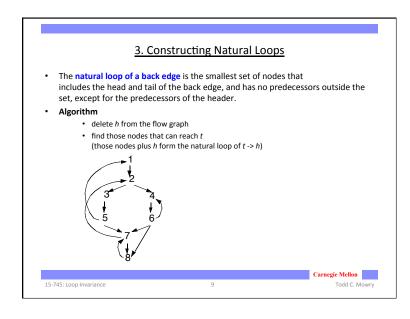
### **Back Edges**

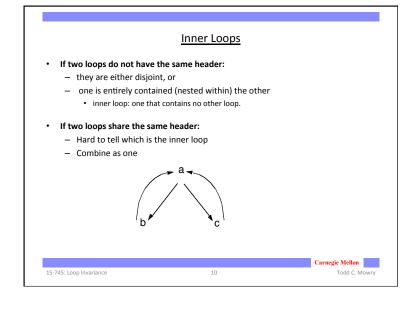
- Definition
  - Back edge: t->h, h dominates t
- · Relationships between graph edges and back edges
- Algorithm
  - Perform a depth first search
  - For each retreating edge t->h, check if h is in t's dominator list
- Most programs (all structured code, and most GOTO programs) have reducible flow graphs
  - retreating edges = back edges

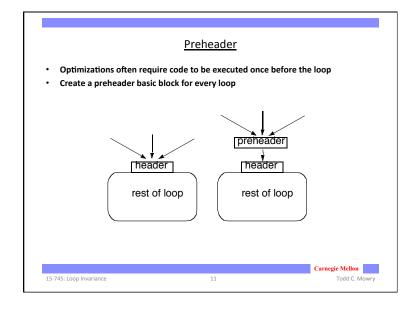
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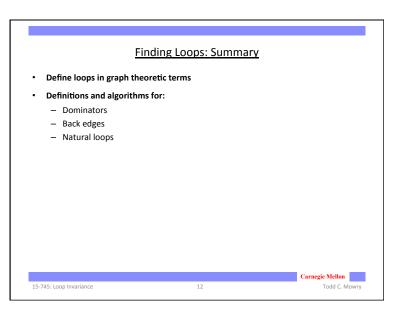
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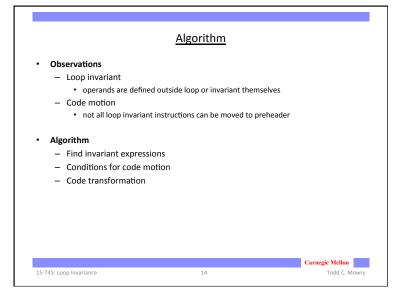




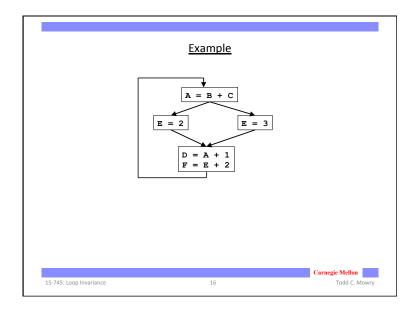




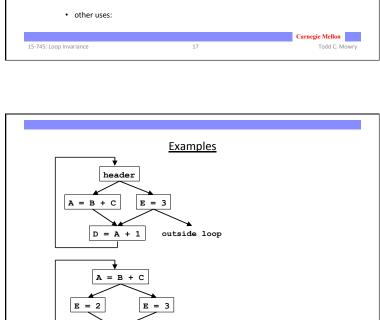
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# Detecting Loop Invariant Computation Compute reaching definitions Mark INVARIANT if all the definitions of B and C that reach a statement A=B+C are outside the loop constant B, C? Repeat: Mark INVARIANT if all reaching definitions of B are outside the loop, or there is exactly one reaching definition for B, and it is from a loop-invariant statement inside the loop similarly for C until no changes to set of loop-invariant statements occur.



# III. Conditions for Code Motion • Correctness: Movement does not change semantics of program • Performance: Code is not slowed down • Basic idea: defines once and for all • control flow: • other definitions: • other uses: Carnegie Mellon 15-745: Loop Invariance 17 Code Motion Carnegie Mellon

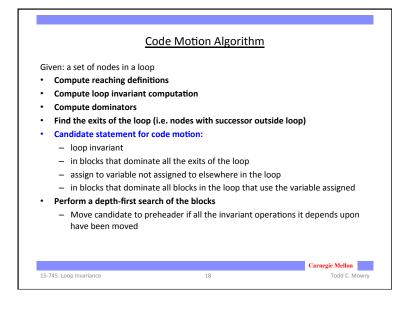


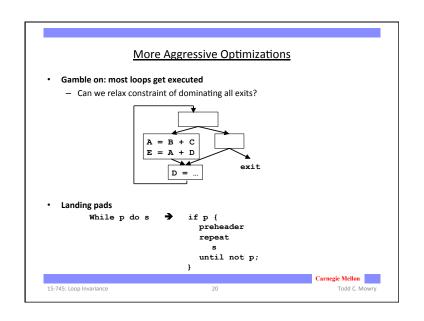
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D = A + 1F = E + 2

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### Summary

- Precise definition and algorithm for loop invariant computation
- Precise algorithm for code motion
- Use of reaching definitions and dominators in optimizations

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