Model Checking Cell Decision Processes



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Goals for Mechanistic Modeling

- Understand
- Control
- Treat

Molecular mechanisms of cellular decisions



Mast cell degranulation

IL-17 signaling

T cell differentiation

Challenges for Modeling (both mental and computational)

- Large number of components and interactions
- Rapidly evolving list of important components and interactions
- Feedback and feedforward loops
- Involvement of multiple processes
 - Signaling
 - Gene regulation / protein expression
 - Metabolism
 - Cell processes
 - Growth
 - Proliferation
 - Death
 - ...
- Cell populations
 - Heterogeneity
 - Multi-scale integration



Rule-Based Modeling: An Intermediate Level Abstraction for Systems Biology



Gln 61

Ras

Combinatorial Complexity

a simple model can produce many species and reactions



Hlavacek, Faeder, et al., Biotechnol. Bioeng. (2003)

Combinatorial complexity in a more realistic model of EGFR signaling

ErbB3:ErbB1 has > 3.8x10⁹ states

ErbB1:ErbB1 has > 5.5x10¹⁰ states



Creamer et al. (2012) BMC Syst. Biol. [TGen group]

Statistical Model Checking in *BioLab* : Applications to the automated analysis of T-Cell Receptor Signaling Pathway *

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Property 2 In our second experiment, we were interested in the truth of the hypothesis that the system can go from the inactive state to the active state. We verified the following property with various values of the probability p.

$$Pr_{>p}(\mathbf{F^{300}}(ppERK/totalERK < 0.1 \land \mathbf{F^{300}} (ppERK/totalERK > 0.5))$$

Our first model started with 100 molecules of agonist pMHC (with dissociation constant 1/20 per second) while antagonist pMHC was assumed to be absent in the initial state. The results are presented in Table 5.

Sl.	p_1	p_0	Result	Total	Number of	Time
				Number o		
				Samples	Samples	
1	0.90	0.95	Yes	160	160	412.25
2	0.70	0.75	Yes	120	120	309.58
3	0.50	0.55	Yes	80	80	214.74
4	0.20	0.25	Yes	40	40	88.32
5	0.10	0.15	Yes	40	40	98.84

Table 5. N_1 : 100, N_2 : 0, Type-I and Type II error : 0.001

Large Scale TCR Signaling Model



Subway Map of Cell Signaling



Logical model of peripheral T cell differentiation

www.SCIENCESIGNALING.org 5 November 2013 Vol 6 Issue 300 ra97

RESEARCH ARTICLE

IMMUNOLOGY

The Duration of T Cell Stimulation Is a Critical Determinant of Cell Fate and Plasticity

Natasa Miskov-Zivanov,¹ Michael S. Turner,²* Lawrence P. Kane,² Penelope A. Morel,^{2†} James R. Faeder^{1†}

Logical model of peripheral T cell differentiation

Model predicts timing of Ag stimulation key to the outcome

Model

Experiment

High antigen dose scenario

Simulation: average element trajectories **High Ag dose** Foxp3 IL-2 **PTEN CD25** PI3K mTORC1 mTORC2 10 15 20 25 30 0 5 Update round

Magnitude of transient is 0.1-0.15, which means that a maximum of 15% trajectories have Foxp3=1 in the same round.

How often Foxp3 increases to 1? How often it remains 0? Probability of Foxp3 becoming 1 is higher than the peak

value in simulations -> Foxp3 transiently increases on a larger number of trajectories.

#	Property	Probability estimate	Success count	Sample size	Elapsed time [s]
P1	F^{29} (FOXP3 == 1); F^{10} (FOXP3 == 1 & F^{19} (FOXP3 == 0))	0.237494	2857	12032	120
P2	F ¹⁰ G ² (FOXP3 == 1)	0.0415313	10970	264160	2704
Р3	F ¹⁰ G ¹ (FOXP3 == 1)	0.119089	830	6976	73
Ρ4	F ²⁰ G ⁹ (FOXP3 == 0 & IL2 == 1 & PTEN == 0 & CD25 == 1 & PI3K == 1 & MTORC1 == 1 & MTORC2 == 1)	0.996124	256	256	2

