



# Verifying Recursive Programs using Intra-procedural Analyzers

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joint work with

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# First of all

Thanks for the invitation and  
congratulation to Ed!



# Difficulties of Program Verification

- Large/unbounded base types: `int`, `float`, `string`
- User-defined types/classes
- Pointers/aliasing + unbounded #'s of heap-allocated cells
- Procedure calls/recursion/calls through pointers/dynamic method lookup/overloading
- Concurrency + unbounded #'s of threads
- Templates/generics/include files
- Interrupts/exceptions/callbacks
- Use of secondary storage: files, databases
- Absent source code for: libraries, system calls, mobile code
- Size

Source: Turing Lecture of Edmund Clarke



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Almost impossible to attack all features at the same time.

Source: Turing Lecture of Edmund Clarke



# Difficulties of Program Verification

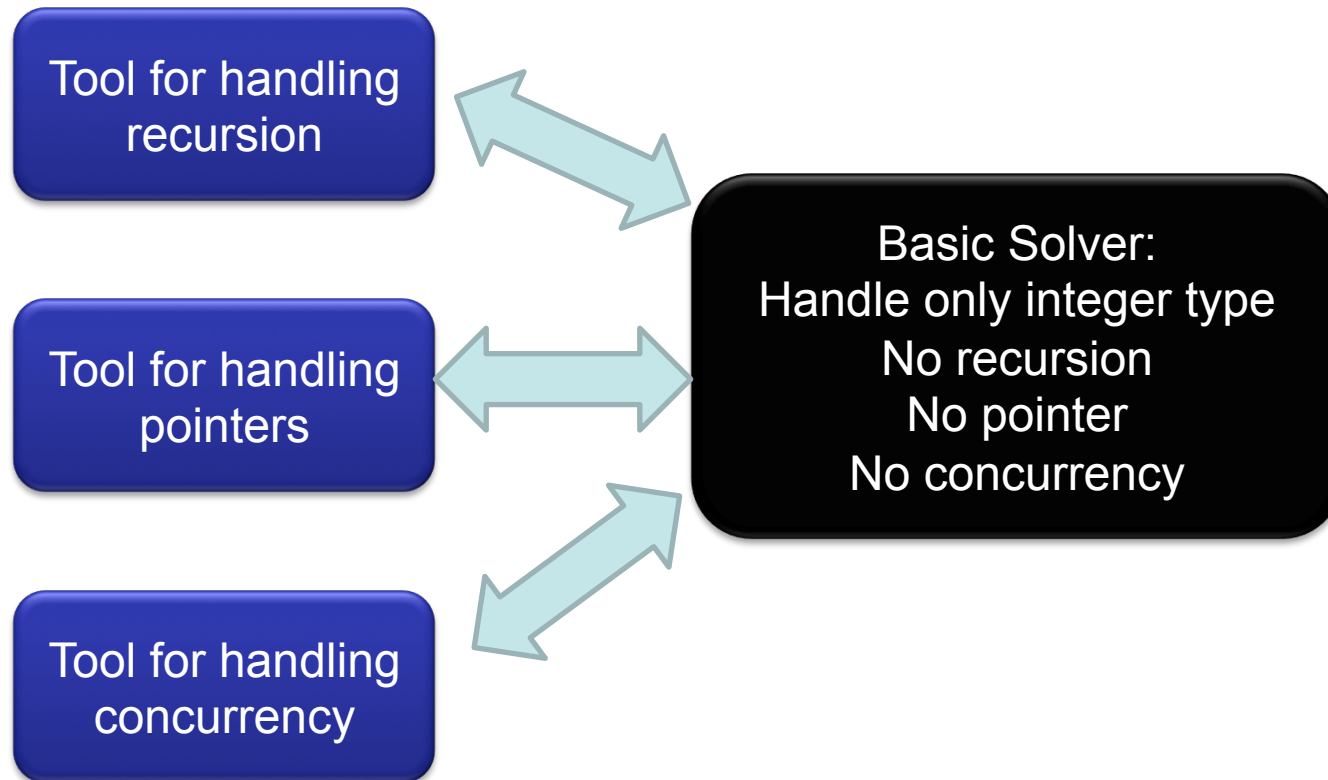
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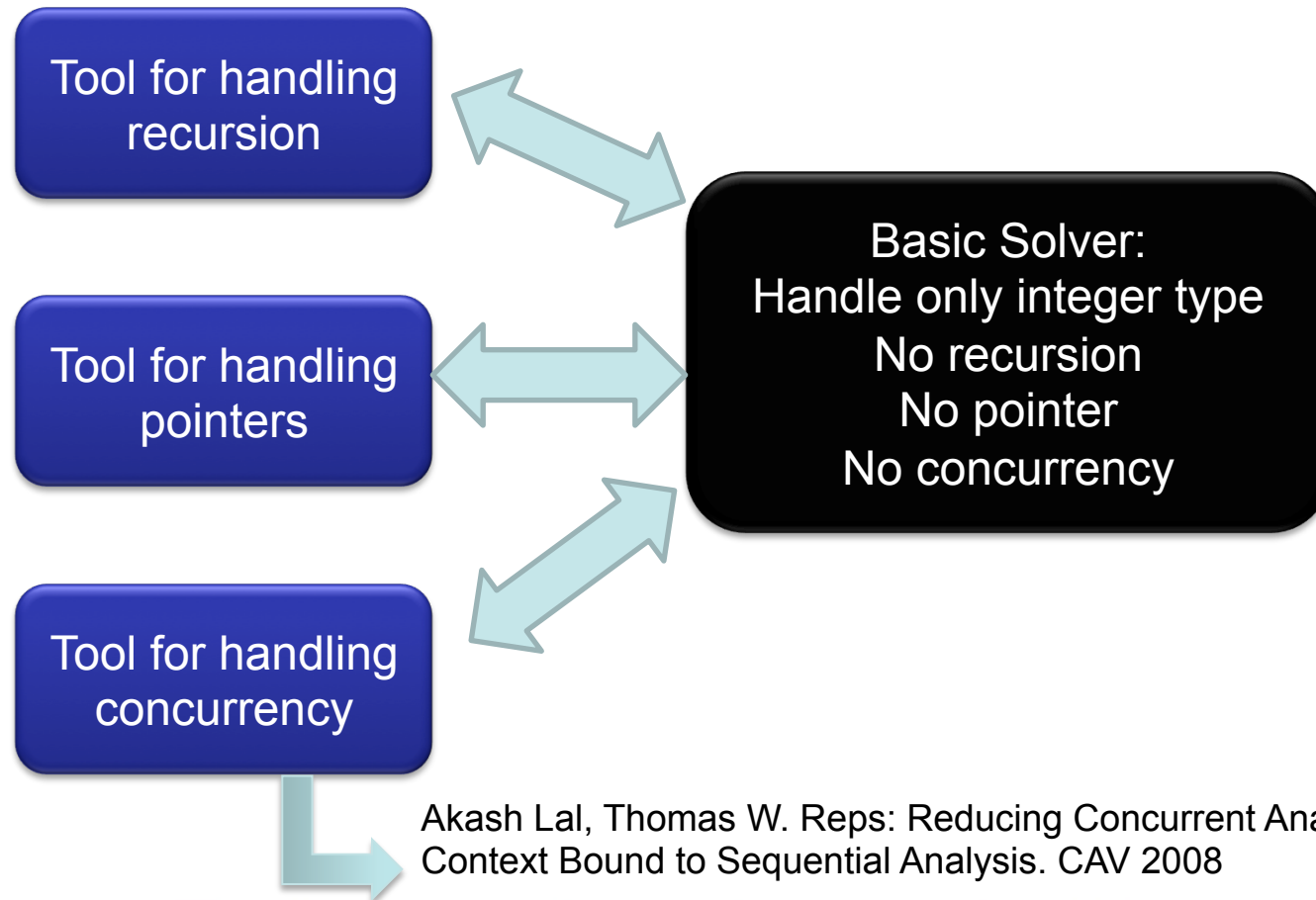
# The Proposal

Basic Solver:  
Handle only integer type  
No recursion  
No pointer  
No concurrency

# The Proposal



# The Proposal



Akash Lal, Thomas W. Reps: Reducing Concurrent Analysis Under a Context Bound to Sequential Analysis. CAV 2008

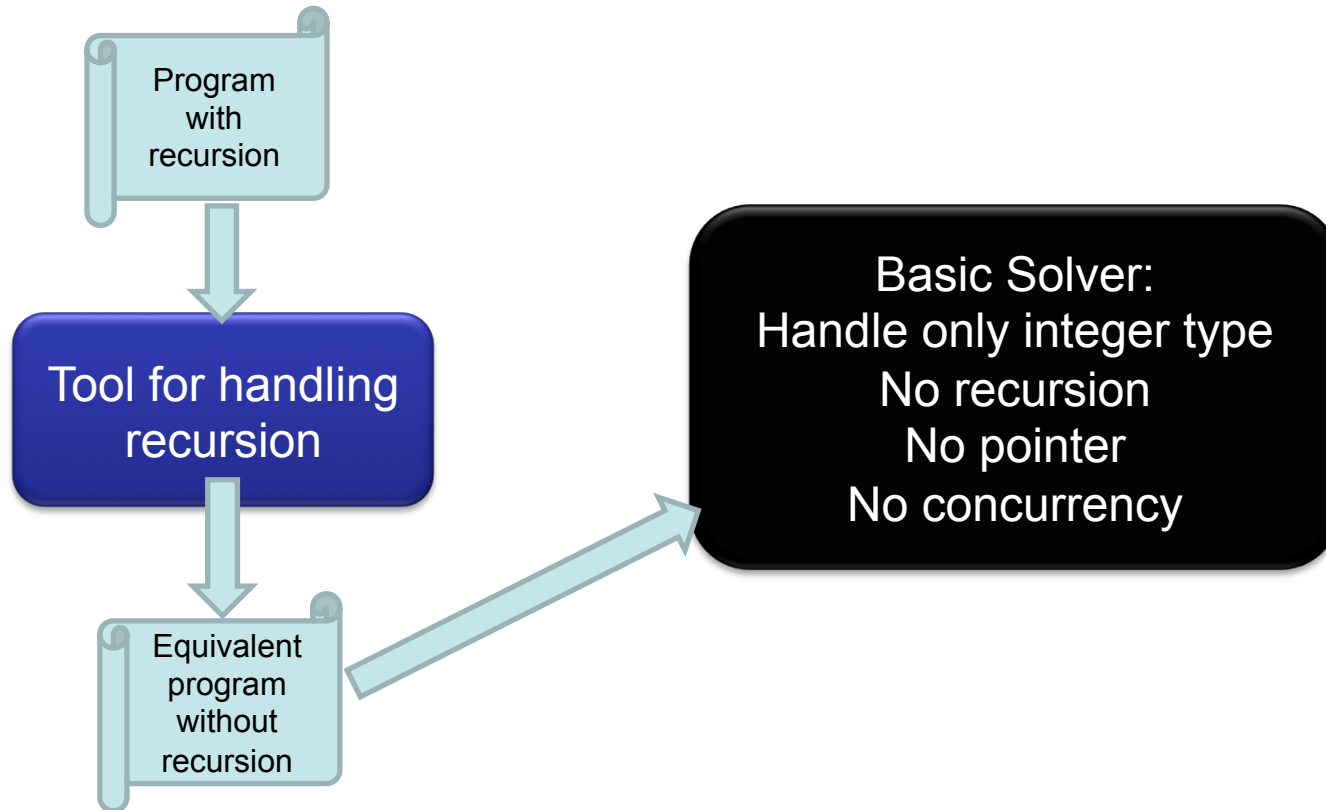


# Handling Recursive Programs

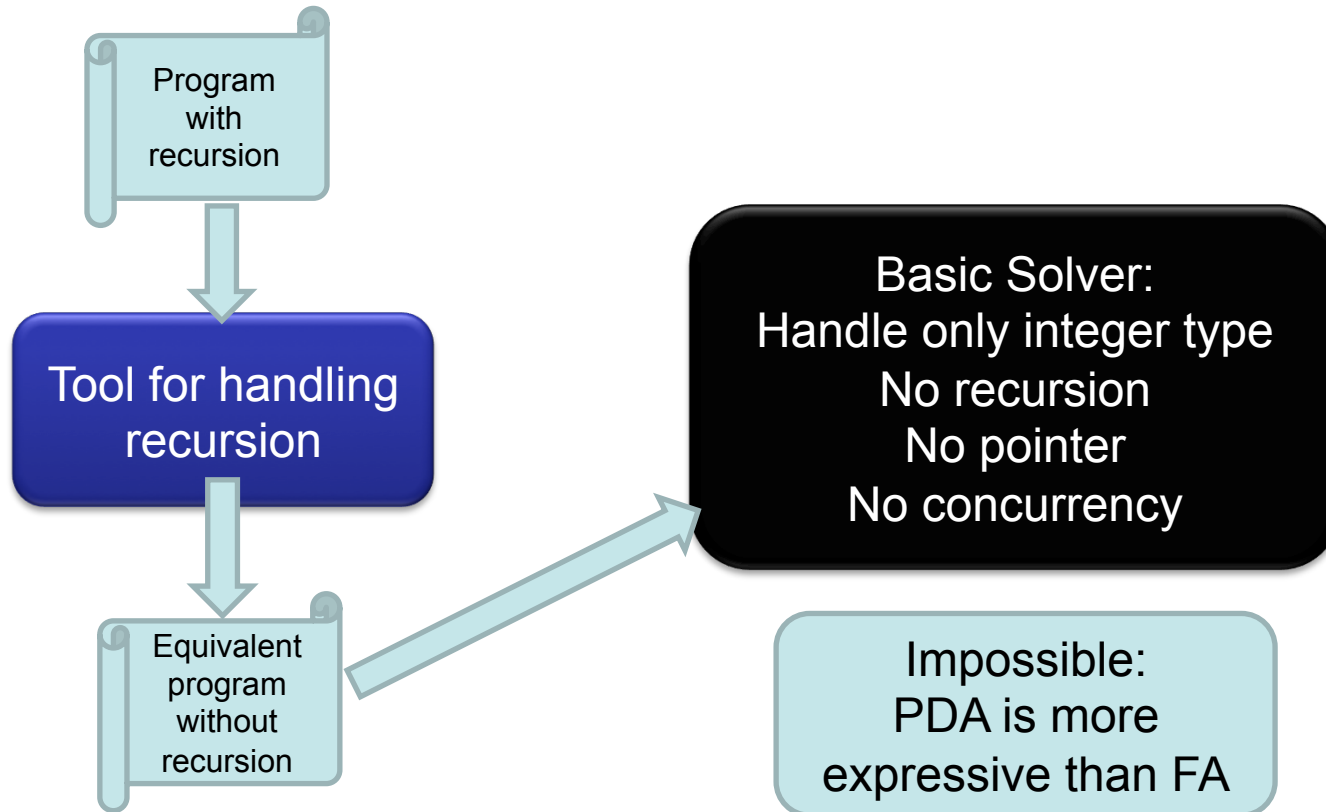
An approach to  
verify recursive program using  
non-recursive verifiers via  
program transformation

**Yu-Fang Chen, Chiao Hsieh, Ming-Hsien Tsai, Bow-Yaw Wang and Farn Wang**, “Verifying Recursive Programs using Intraprocedural Analyzers”, SAS 2014

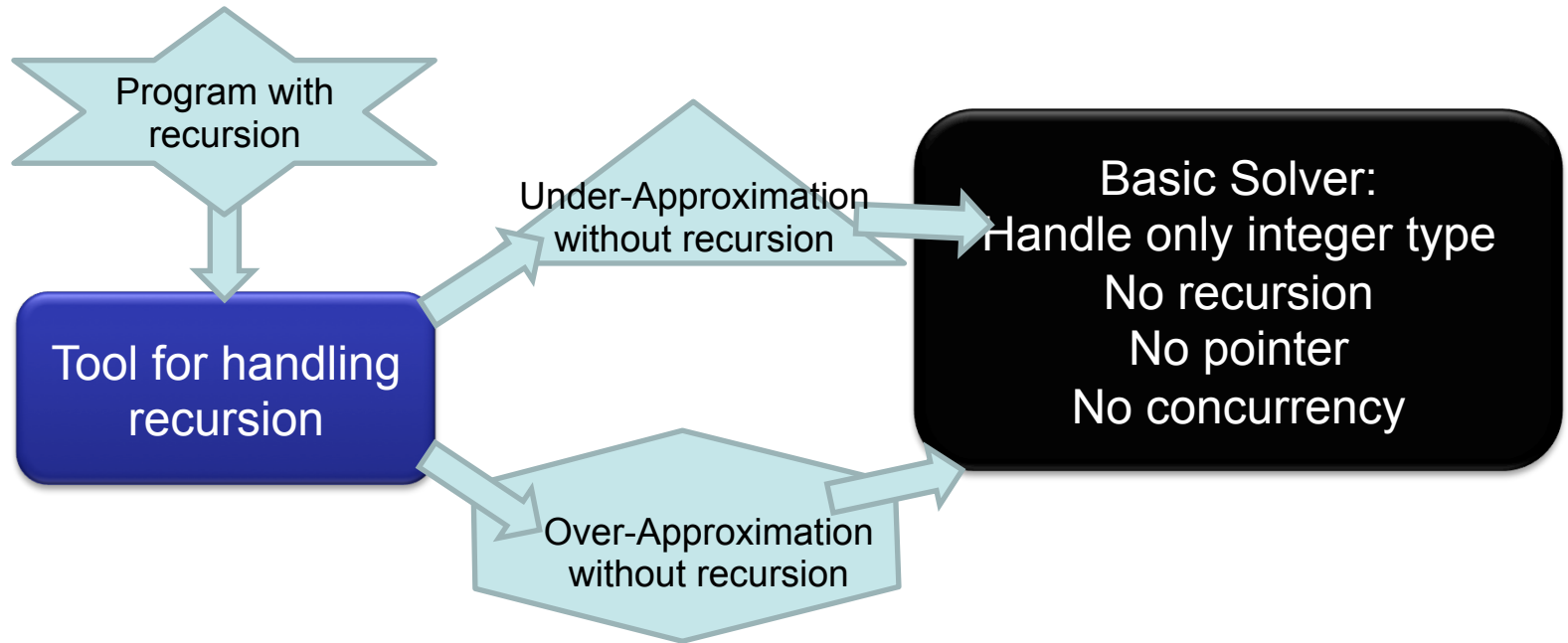
# The Idea



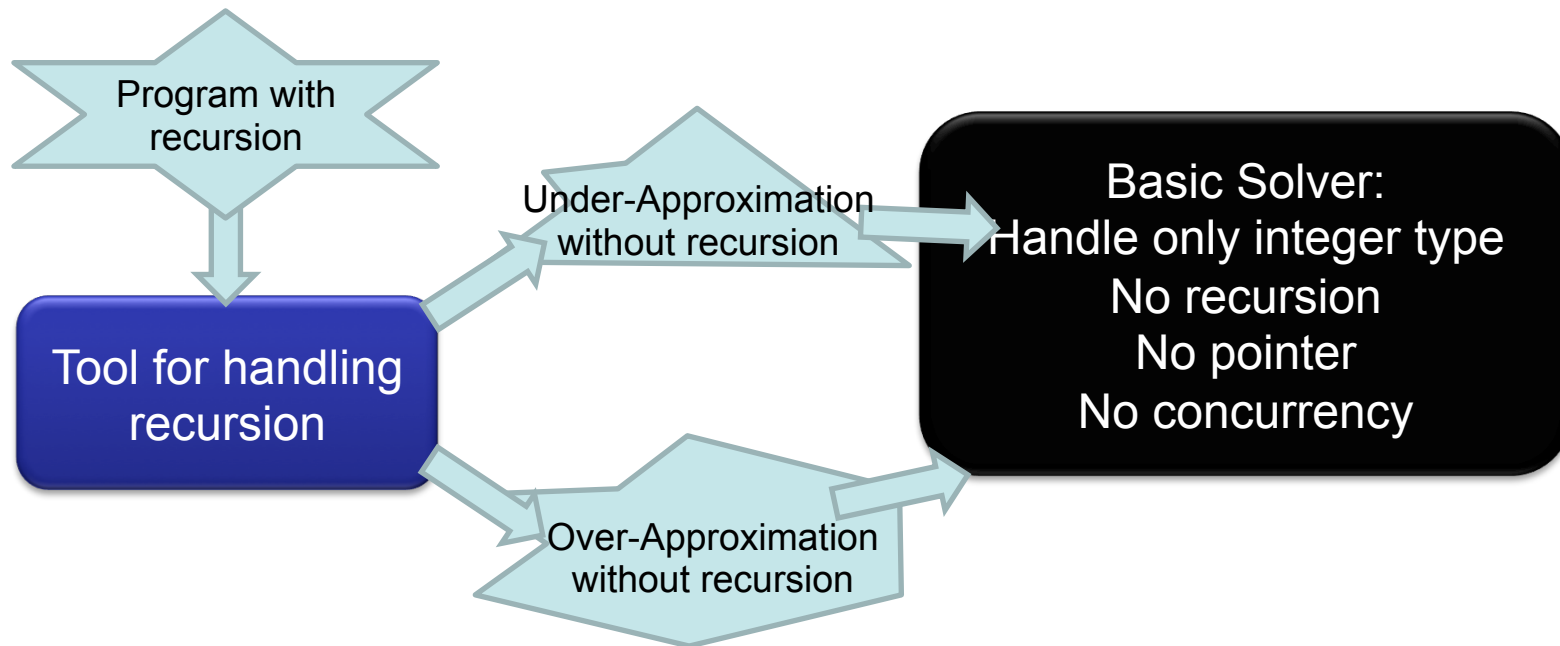
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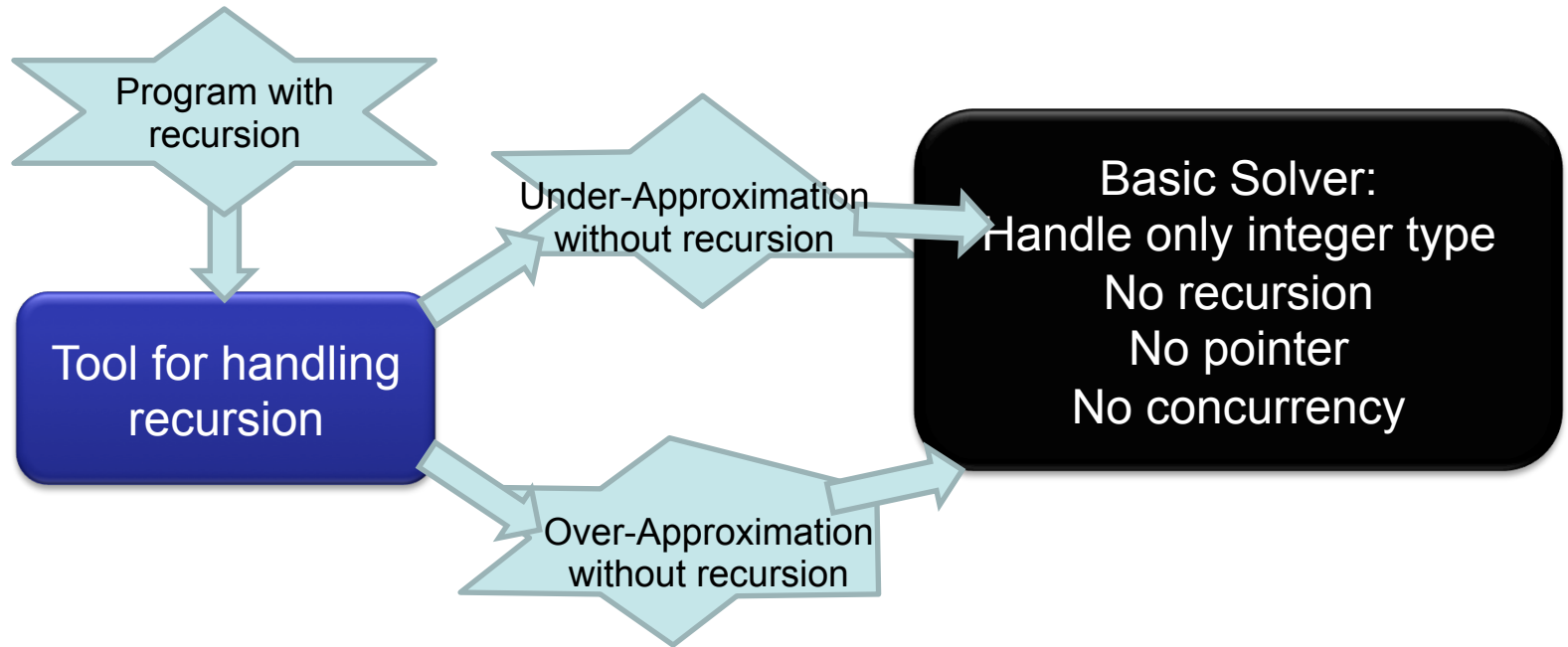
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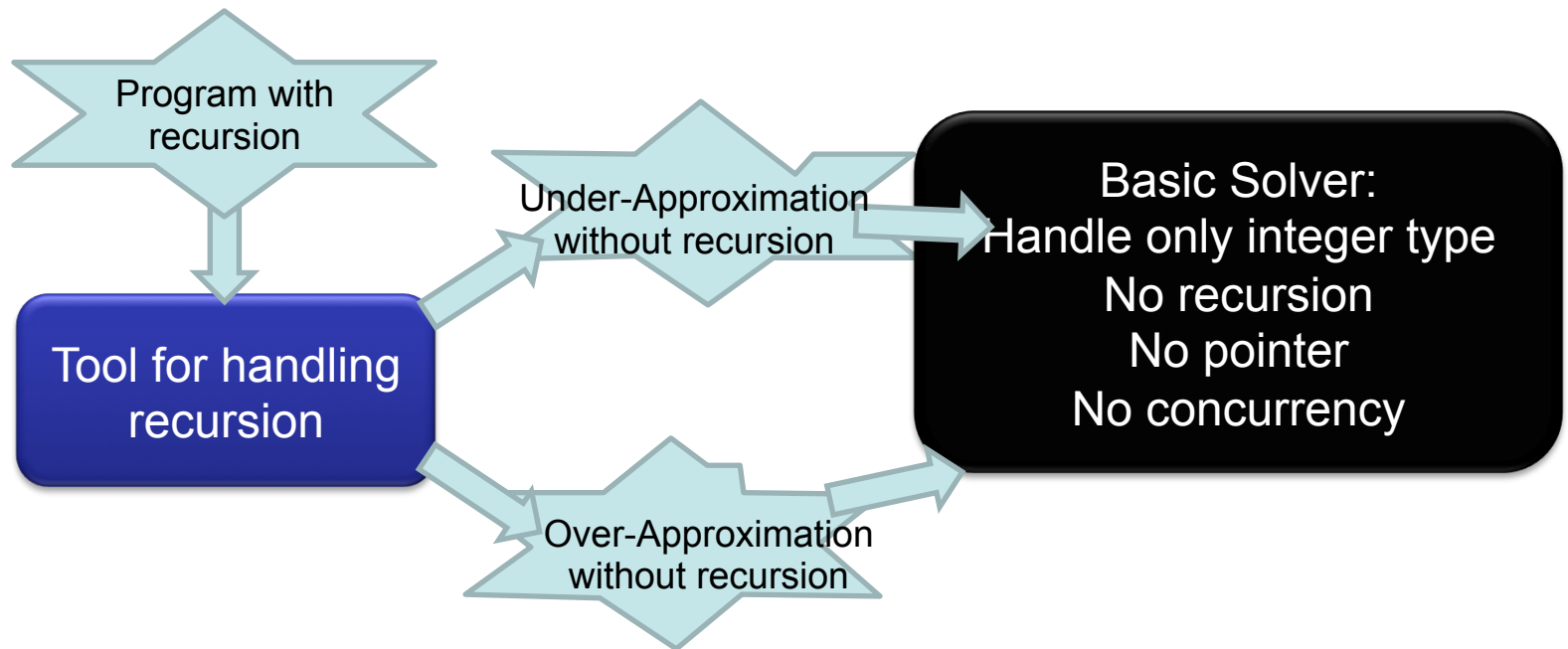
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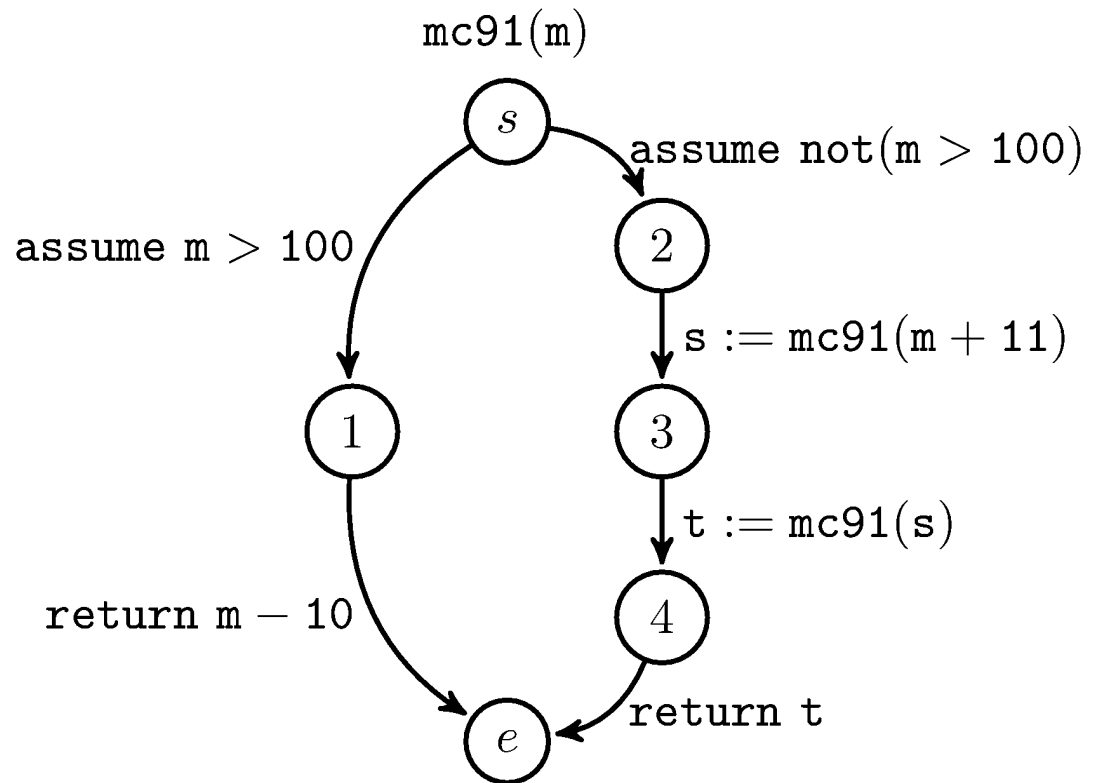
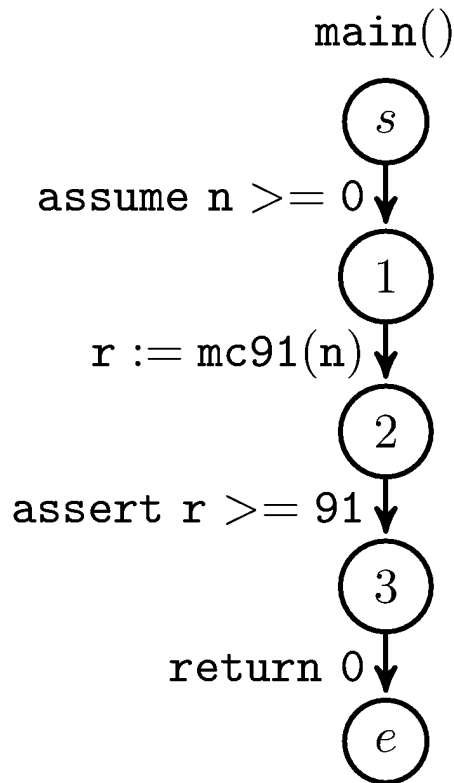
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# The Idea



# An Example: McCarthy 91

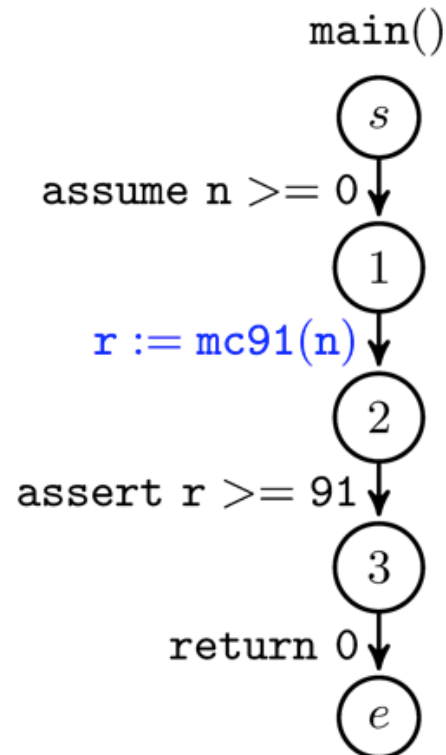


Goal: verify assertion safely

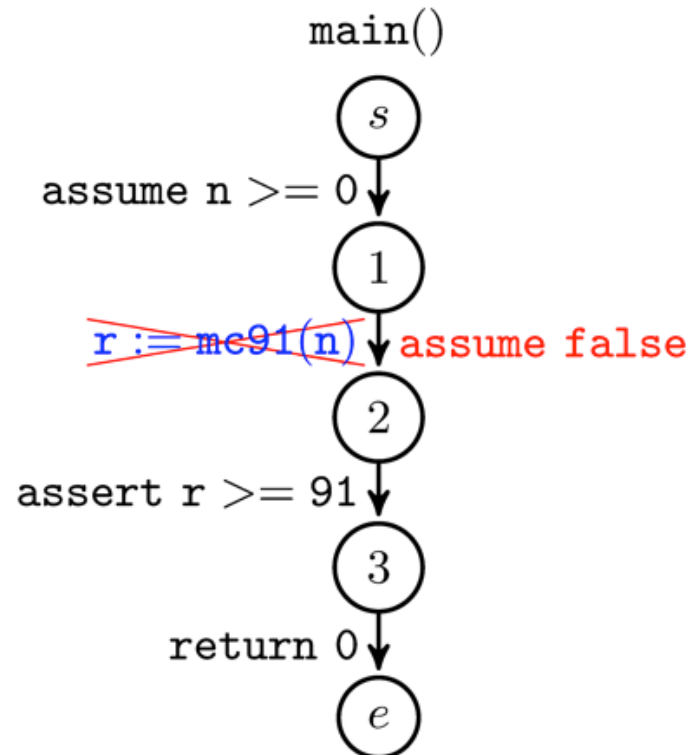
Assumption: Formal parameters are **read-only**



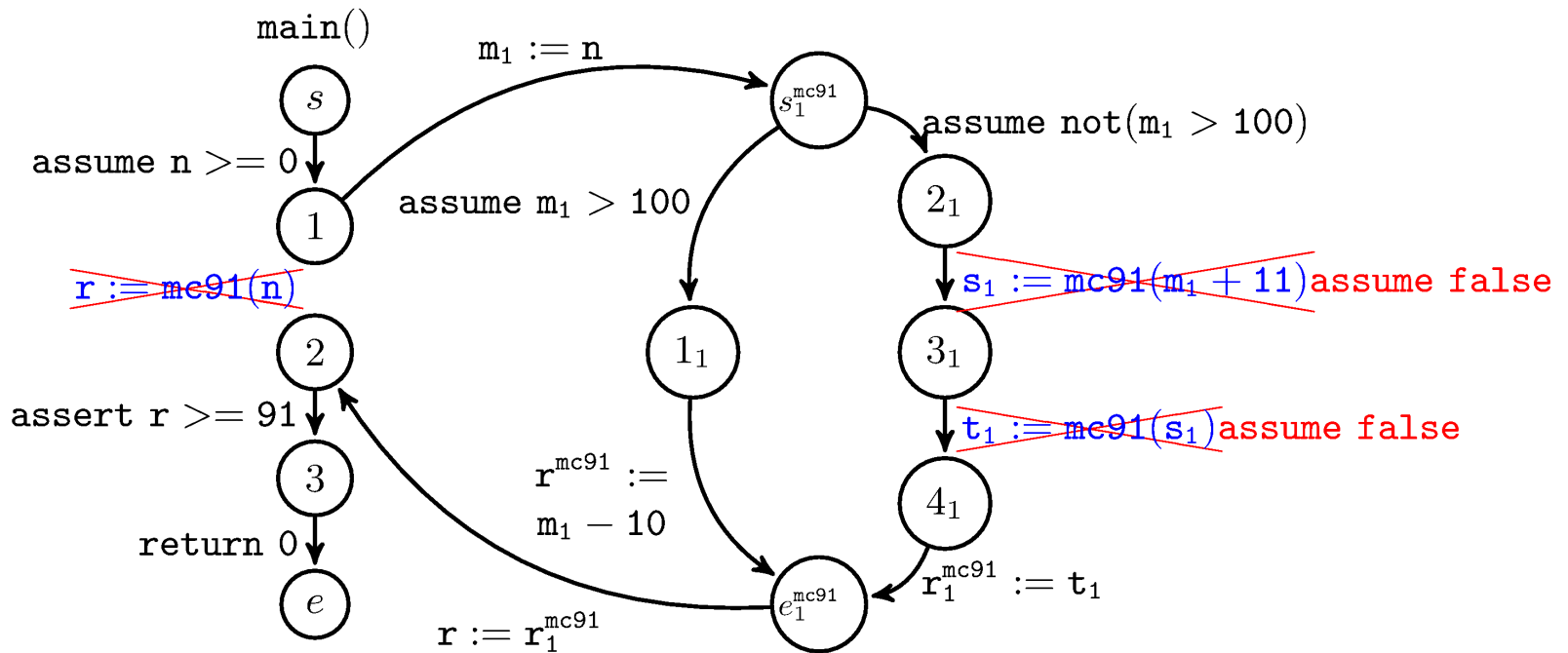
# Construct Under-Approximation



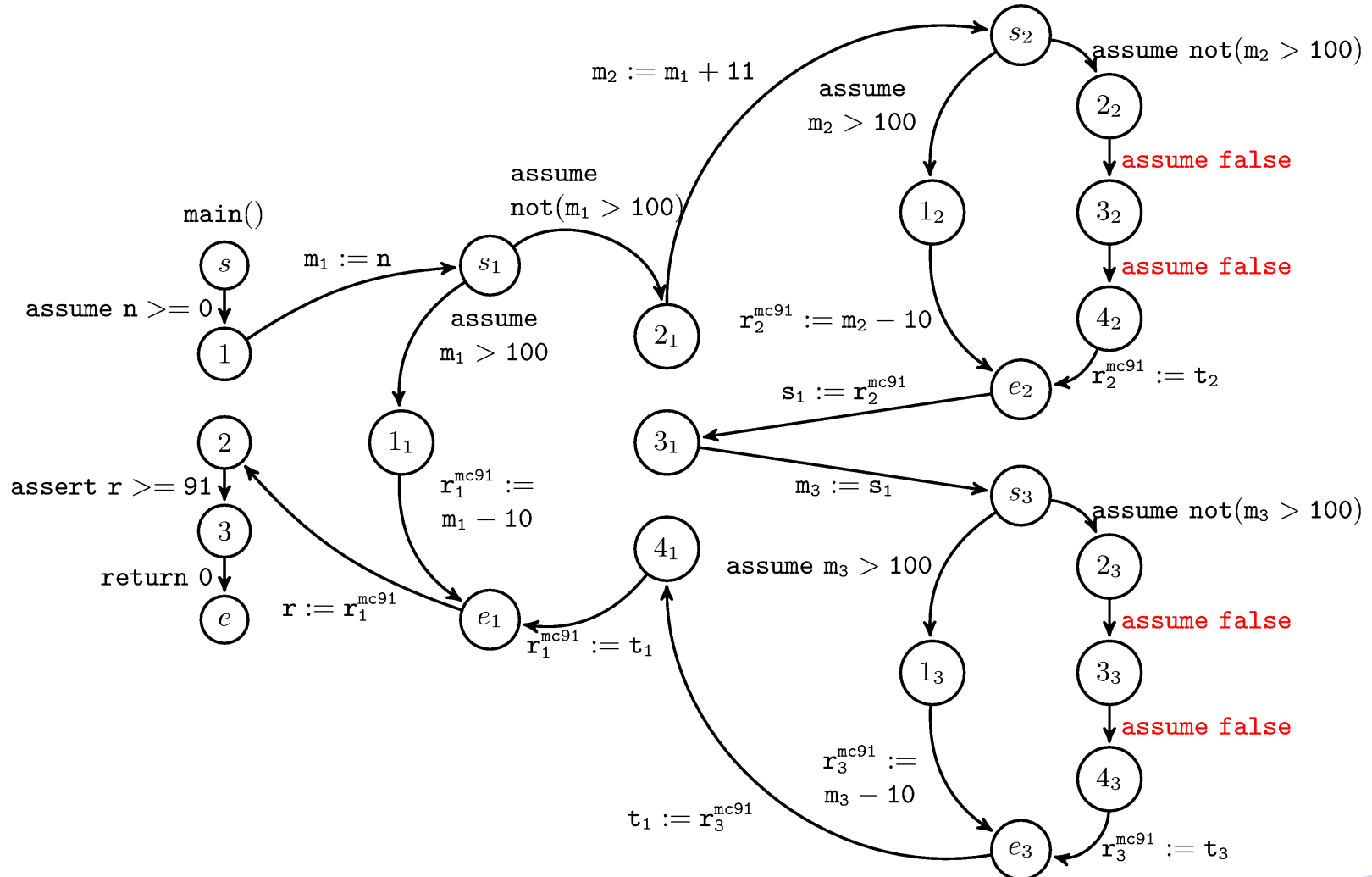
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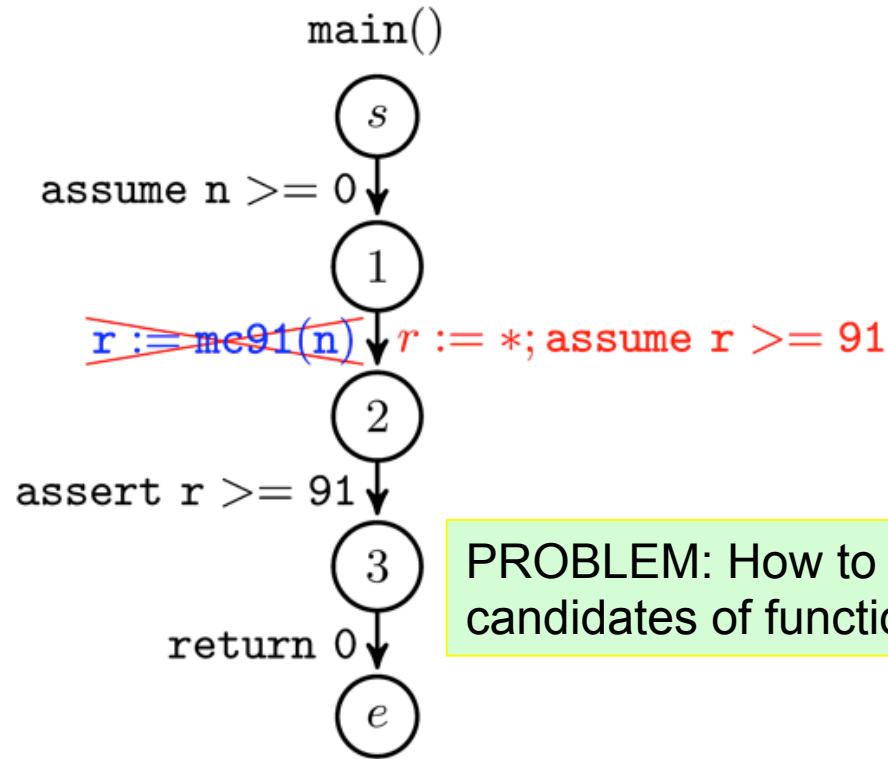
# Refine the Approximation by Unwinding



# More Accurate Refinement



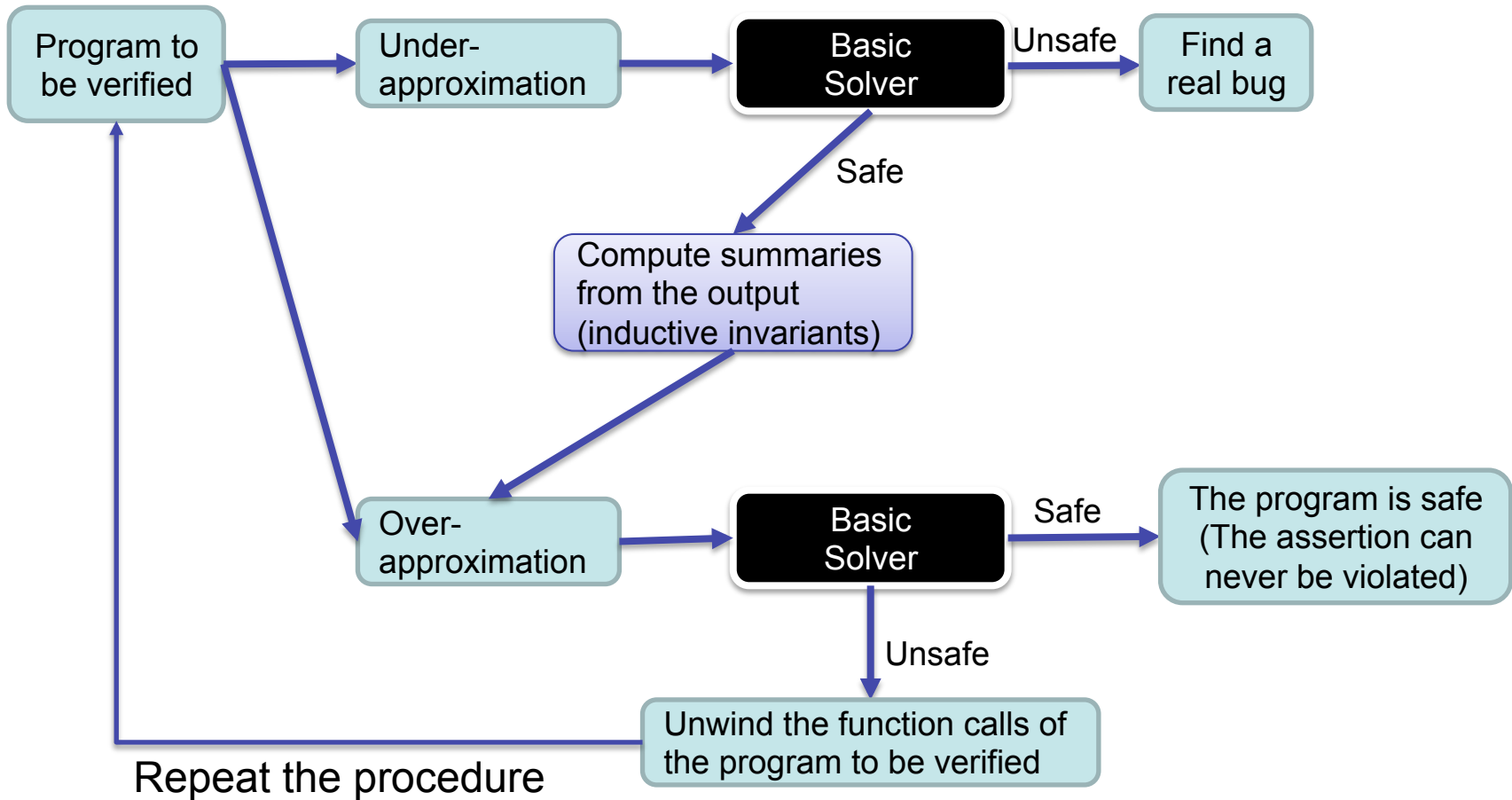
# Construct Over-Approximation



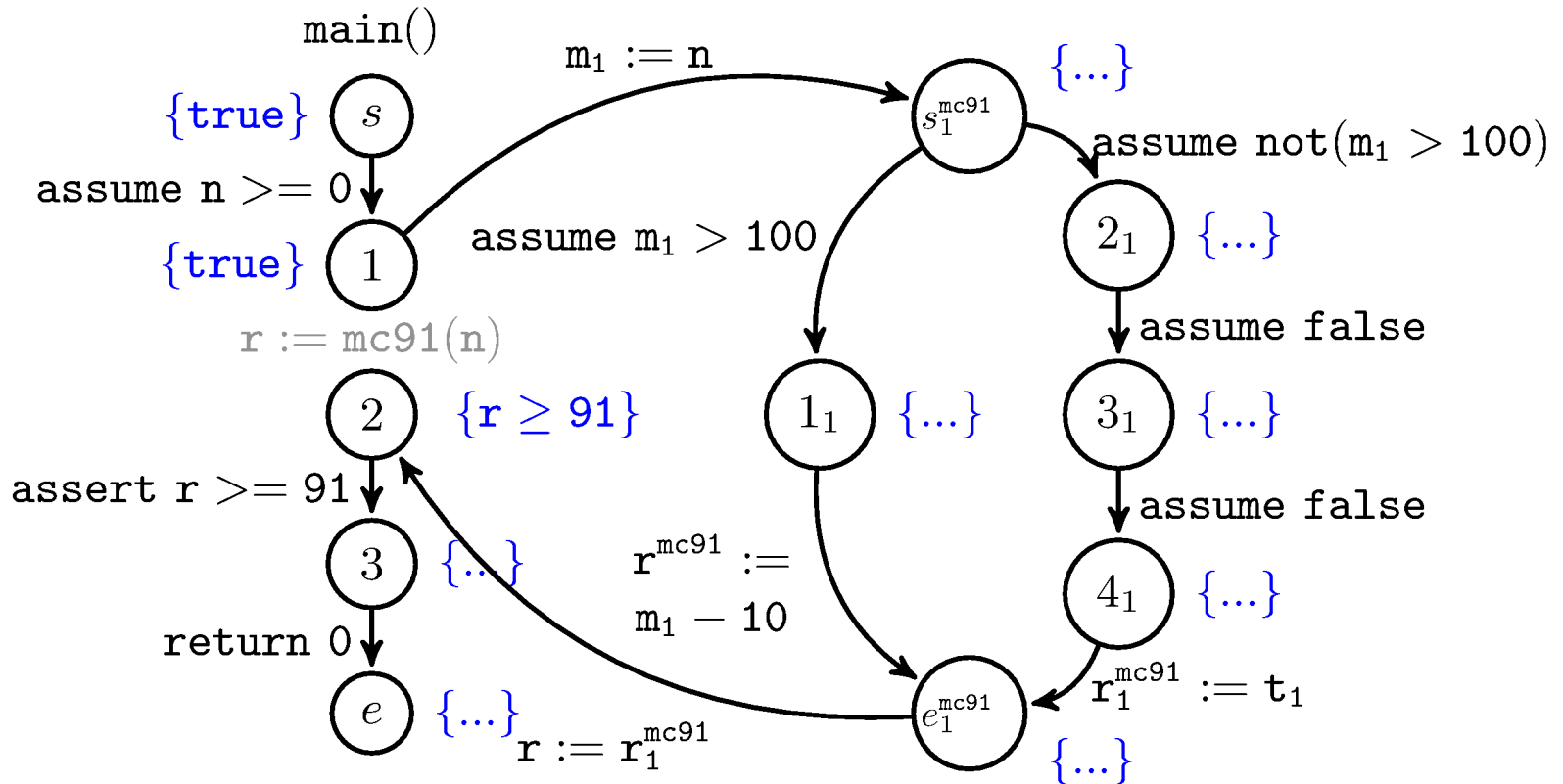
PROBLEM: How to find reasonable candidates of function summaries?

Assume we have a summary  $\{\text{true}\} r := \text{mc91}(n) \{r \geq 91\}$

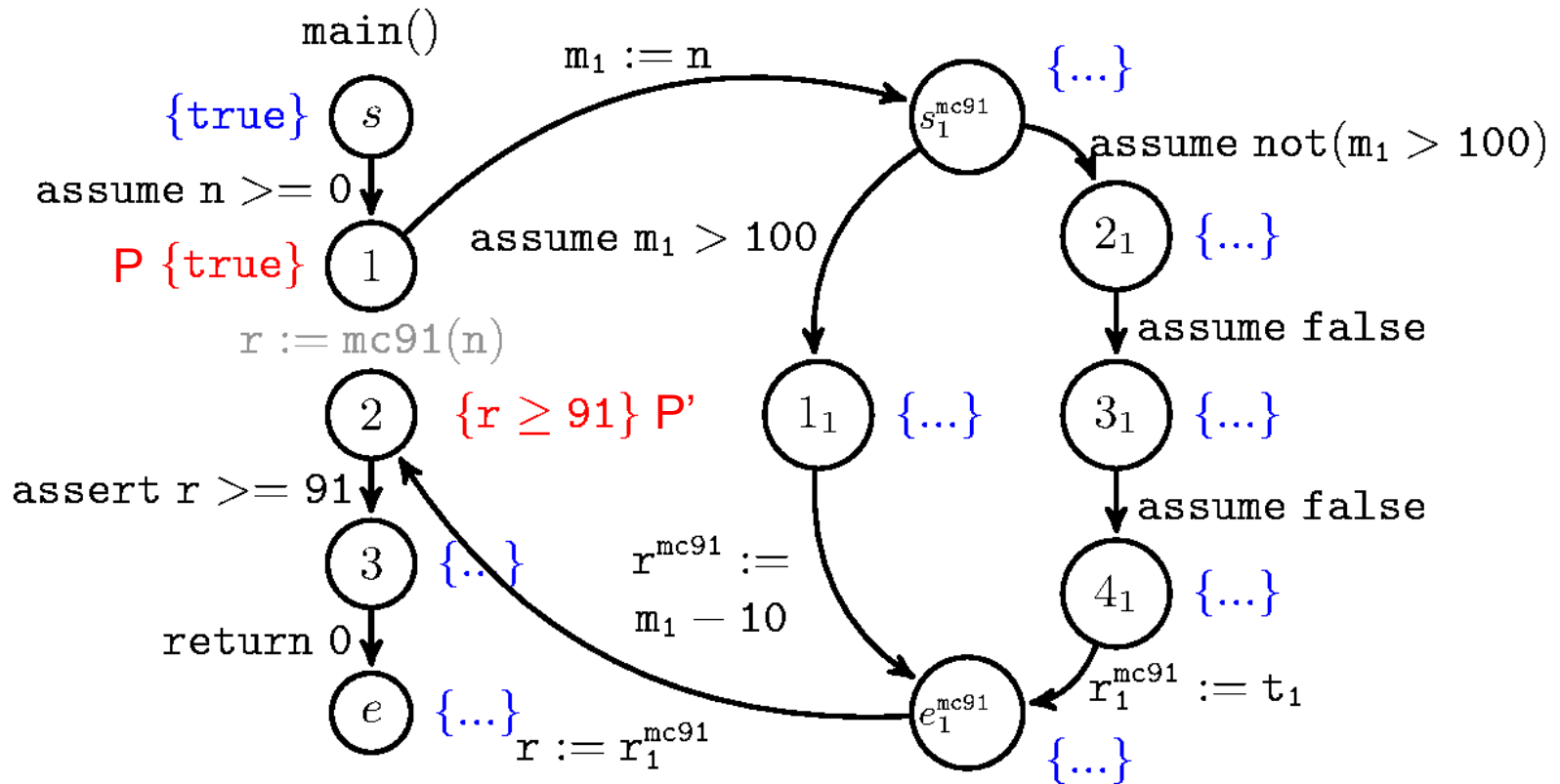
# Basic Flow



# Inductive Invariant from Basic Solver



# Candidate from the Inductive Invariant

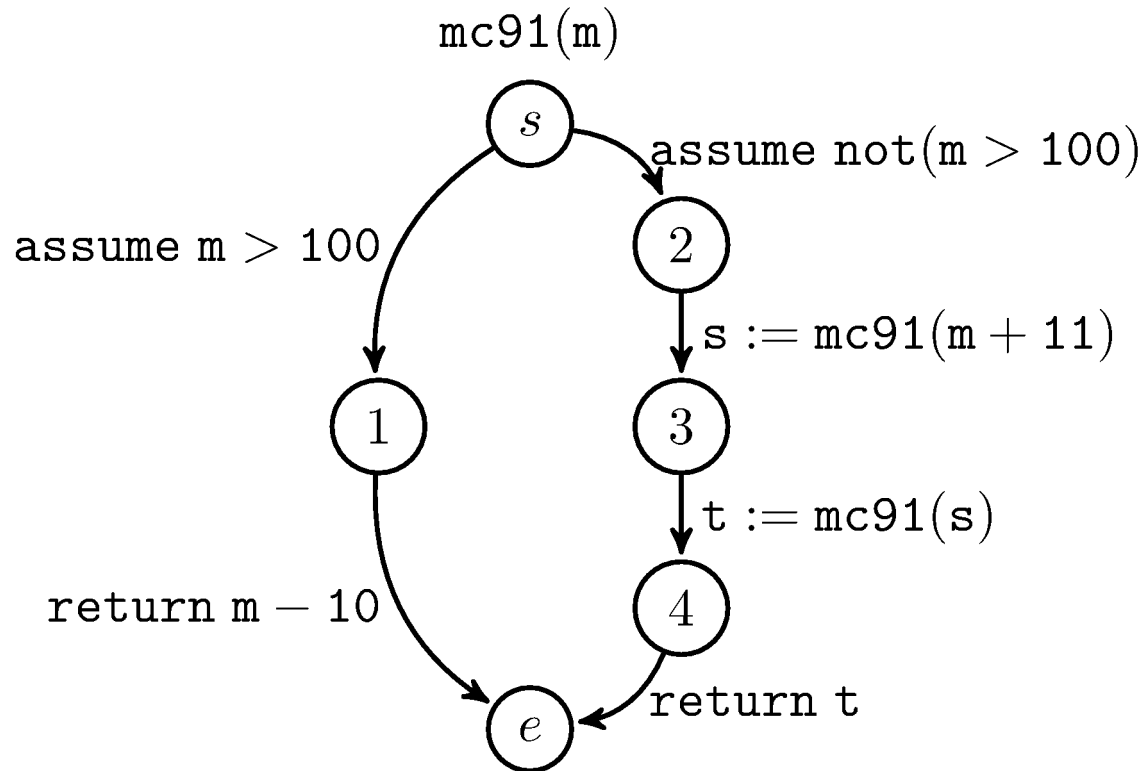


Generate a candidate of summary:  $true \rightarrow r^{mc91} \geq 91$   
 $\forall N_{FR}. P \rightarrow P'$ , where  $N_{FR}$  means all variables other than formal parameters and return variables

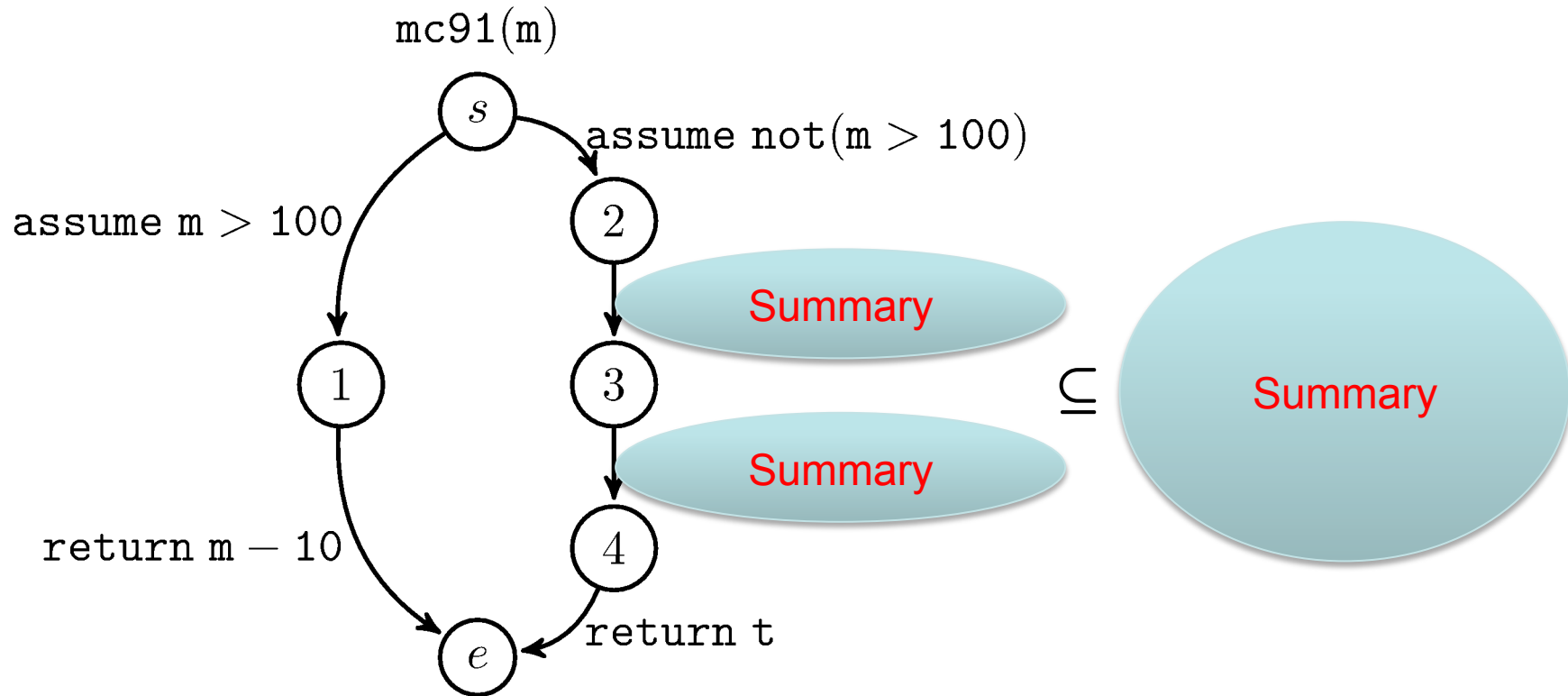
Some renaming is needed.  $r^{mc91}$  is the return variable of the function mc91.



# Check the Summary



# Check the Summary



# Experimental Results

- Benchmarks: the Recursive category of the 2014 Competition on Software Verification

Program	Our Tool	ULTIMATE AUTOMIZER	ULTIMATE KOJAK	CBMC 4.5	BLAST 2.7.2
correct results	11	9	7	22 (10)	3
false negative	0	0	0	1 (0)	0
false positive	1	0	0	0 (0)	4
score	13	12	9	30 (14)	-13

- Blast is the most well-known tool in software verification.
- The rest are the top 3 tools in the competition.

# Our Advantages

- A **light-weight, modular** approach for recursive program verification.
  - Our implementation has 2k lines, CPAChecker has 170k lines
- The performance of the implementation is **comparable** to those specialized for handling recursion