Viewing

- Announcements.
- A Note About Transformations.
- Orthographic and Perspective Projection
- Implementation
- Vanishing Points

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Announcements

- Reading for Thursday: Shirley Ch: 6, & 7

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Rotation About An Arbitrary Vector

Rigid Body Transformations

- A transformation matrix of the form

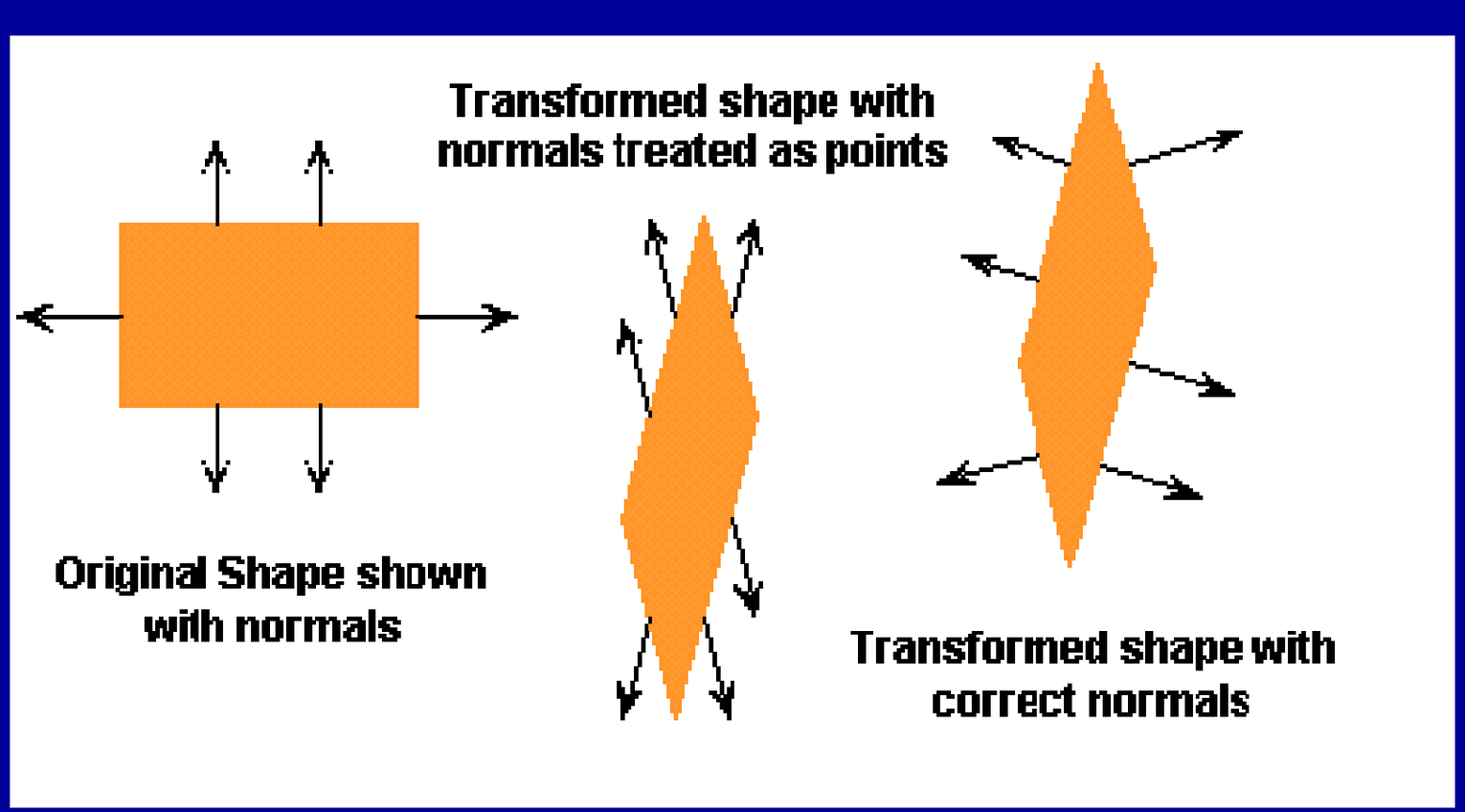
$$\begin{bmatrix} x_x & x_y & t_x \\ y_x & y_y & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

where the upper 2x2 submatrix is a rotation matrix and column 3 is a translation vector, is a *rigid body transformation.*

- Any series of rotations and translations results in a rotation and translation of this form (and no change in the distance between vertices)

Transforming Normals

- It's tempting to think of normal vectors as being like porcupine quills, so they would transform like points
- Alas, it's not so.
- We need a different rule to transform normals.



chalkboard

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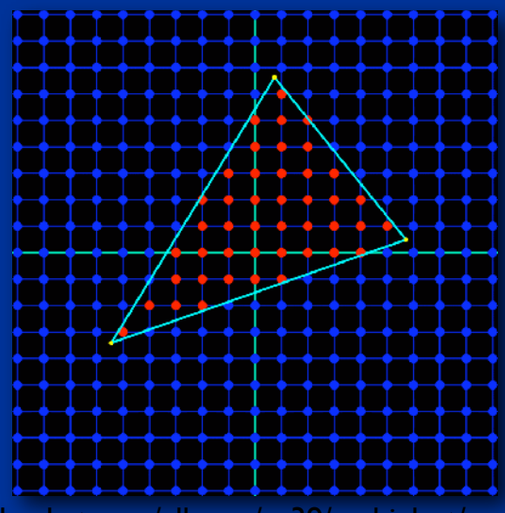
Viewing and Projection

- Our eyes collapse 3-D world to 2-D retinal image (brain then has to reconstruct 3D)
- In CG, this process occurs by *projection*
- Projection has two parts:
  - *Viewing transformations:* camera position and direction
  - *Perspective/orthographic transformation:* reduces 3-D to 2-D
- Use homogeneous transformations (of course…)

Getting Geometry on the Screen

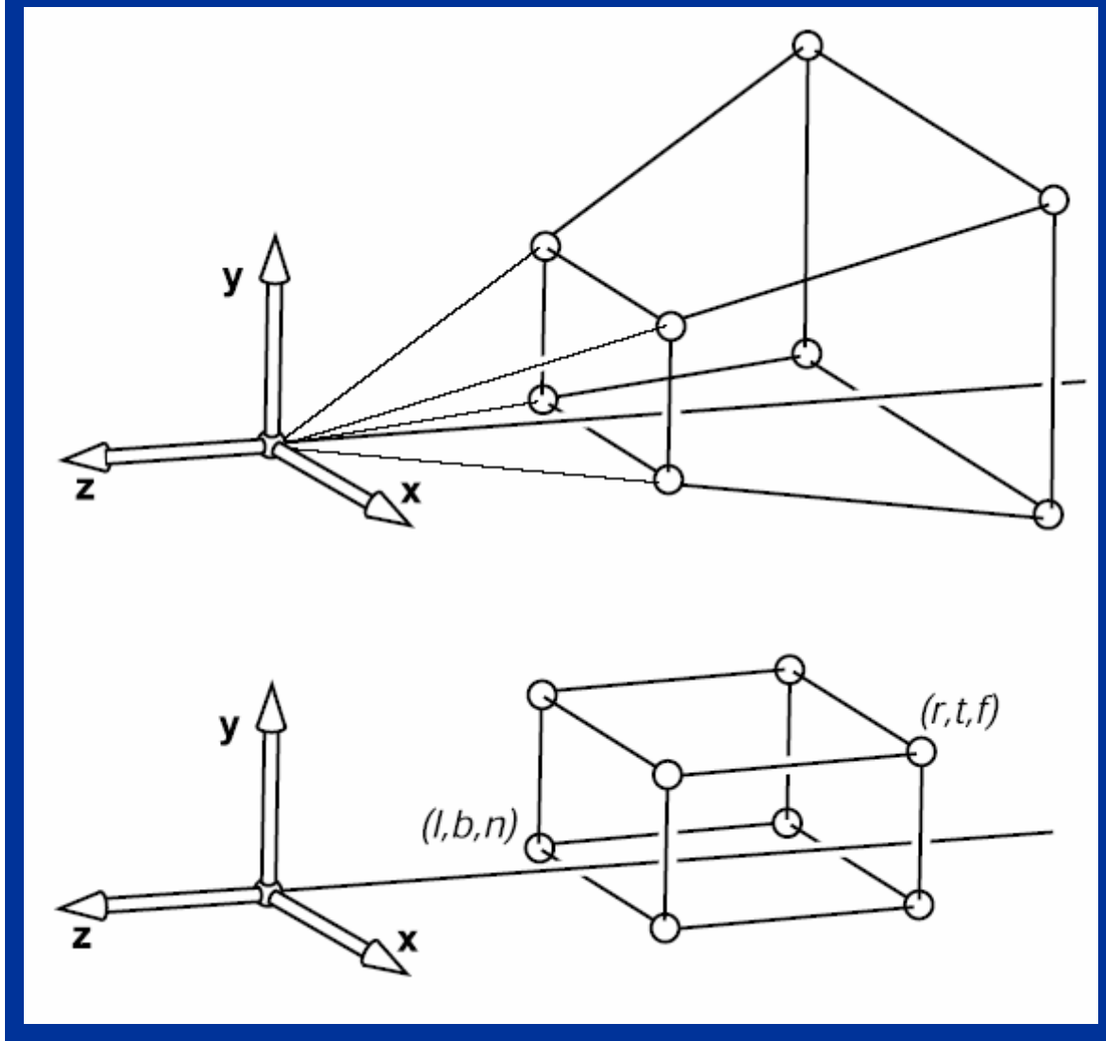
Given geometry positioned in the world coordinate system, how do we get it onto the display?

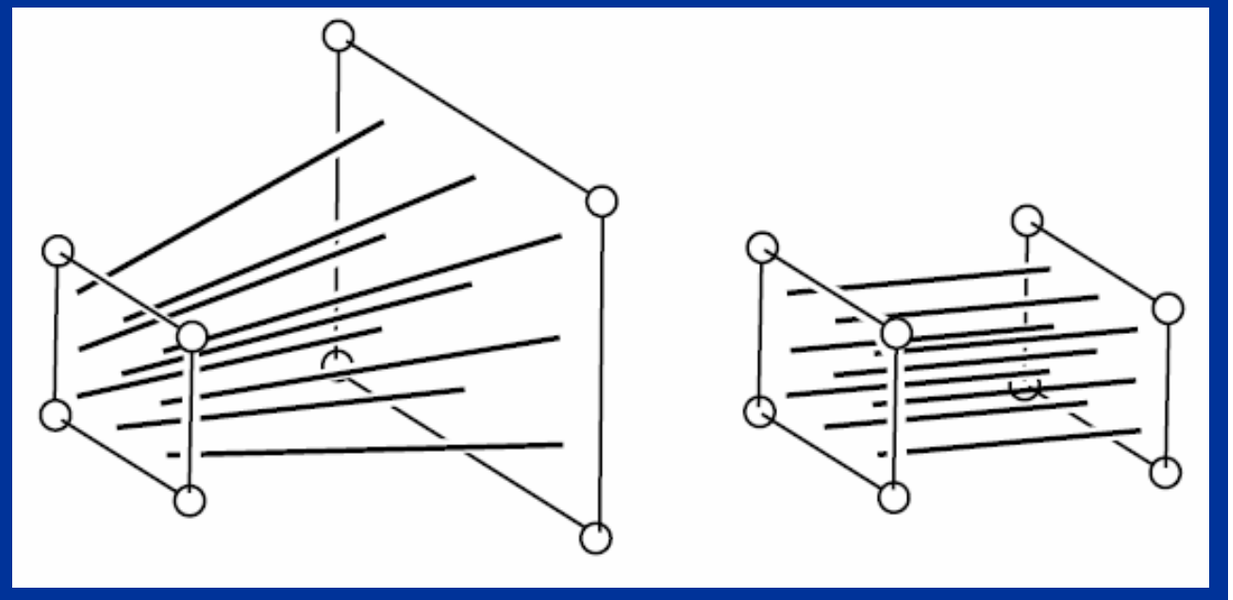
- Transform to camera coordinate system
- Transform (warp) into canonical view volume
- Clip
- Project to display coordinates
- Rasterize



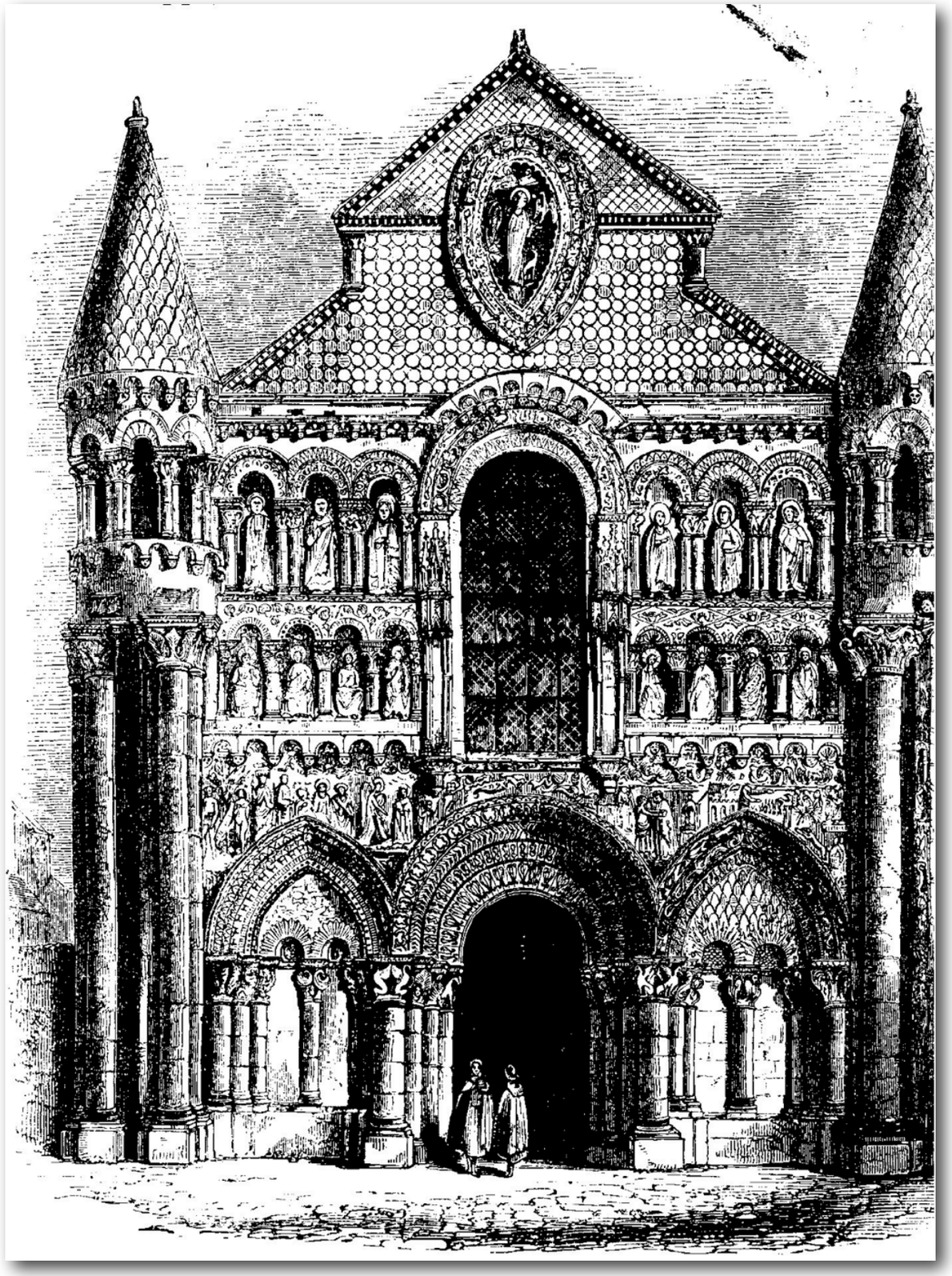
http://i200.photobucket.com/albums/aa39/archiebot/rasterization.png

Perspective and Orthographic Projection





Orthographic Projection



Viewing and Projection

Build this up in stages

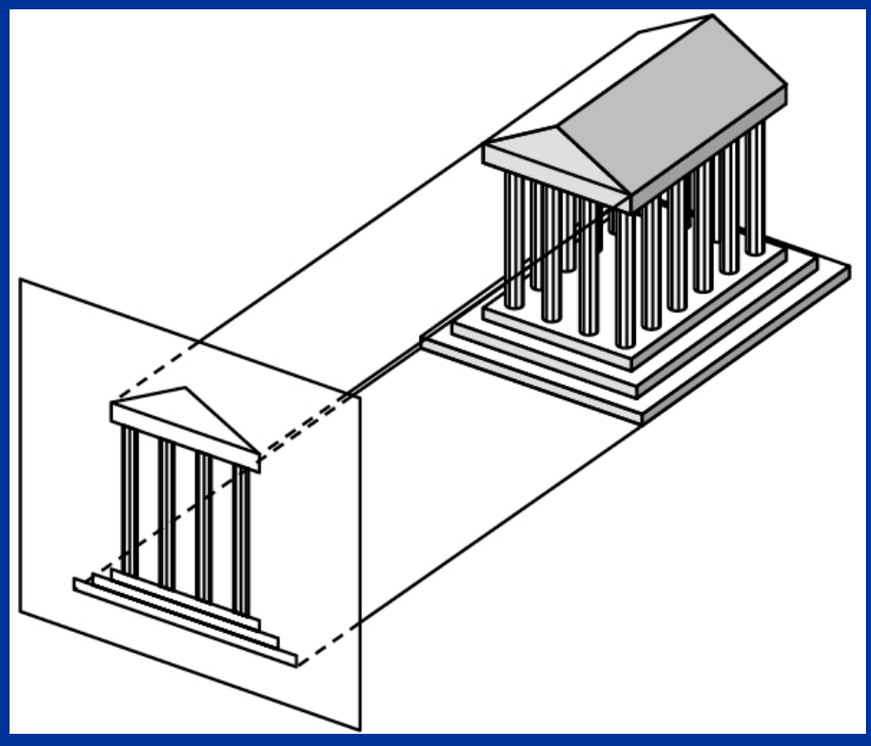
- Canonical view volume to screen
- Orthographic projection to canonical view volume
- Perspective projection to orthographic space

Orthographic Projection

the focal point is at infinity, the rays are parallel, and orthogonal to the image plane

good model for telephoto lens. No perspective effects.

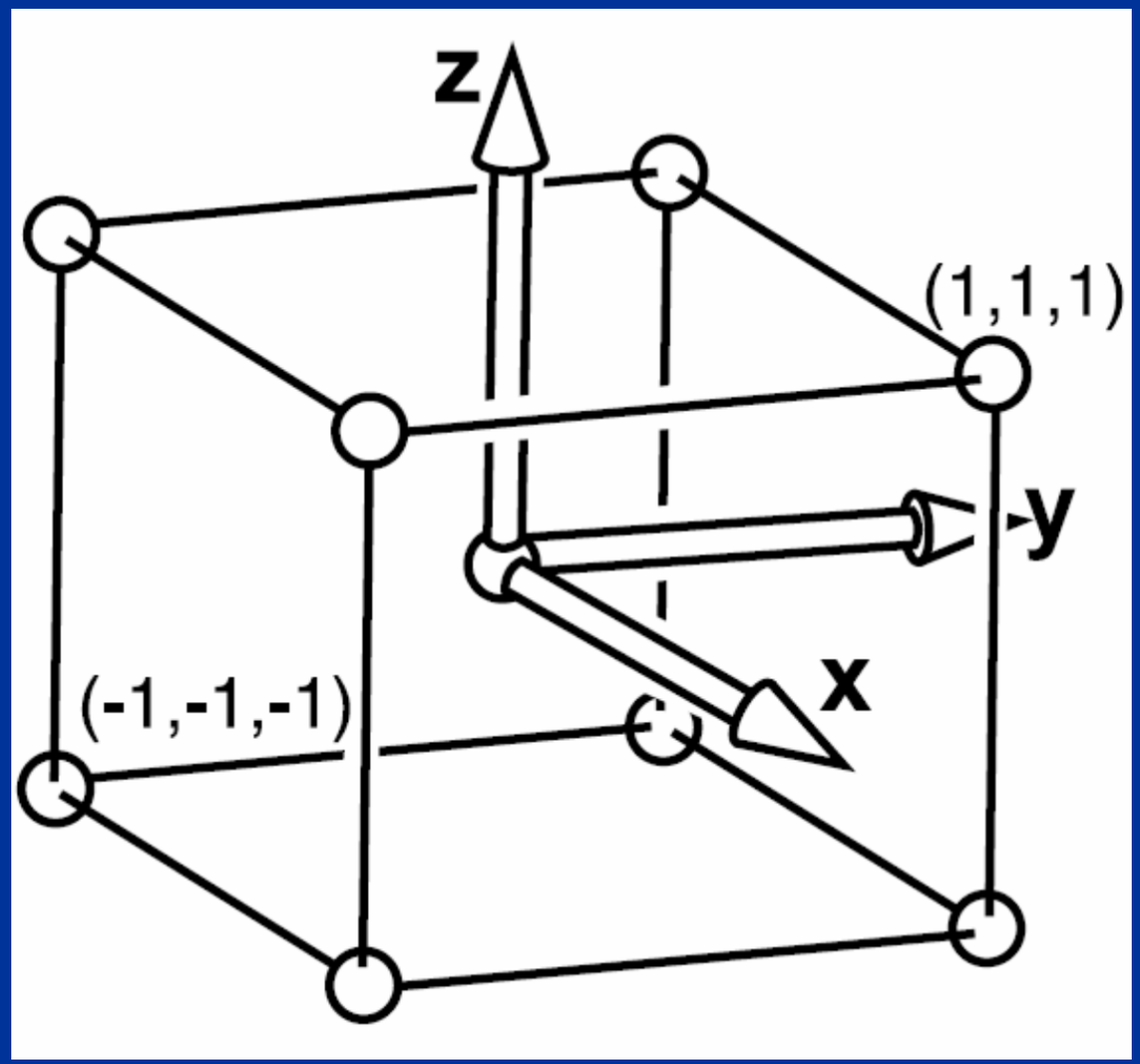
when *xy*-plane is the image plane (x,y,z) -> (x,y,0) front orthographic view



Telephoto Lenses and Fashion Photography

http://farm4.static.flickr.com/3057/2555706112_20a3015ddb.jpg

Canonical View Volume



Why this shape?

- Easy to clip to
- Trivial to project from 3D to 2D image plane

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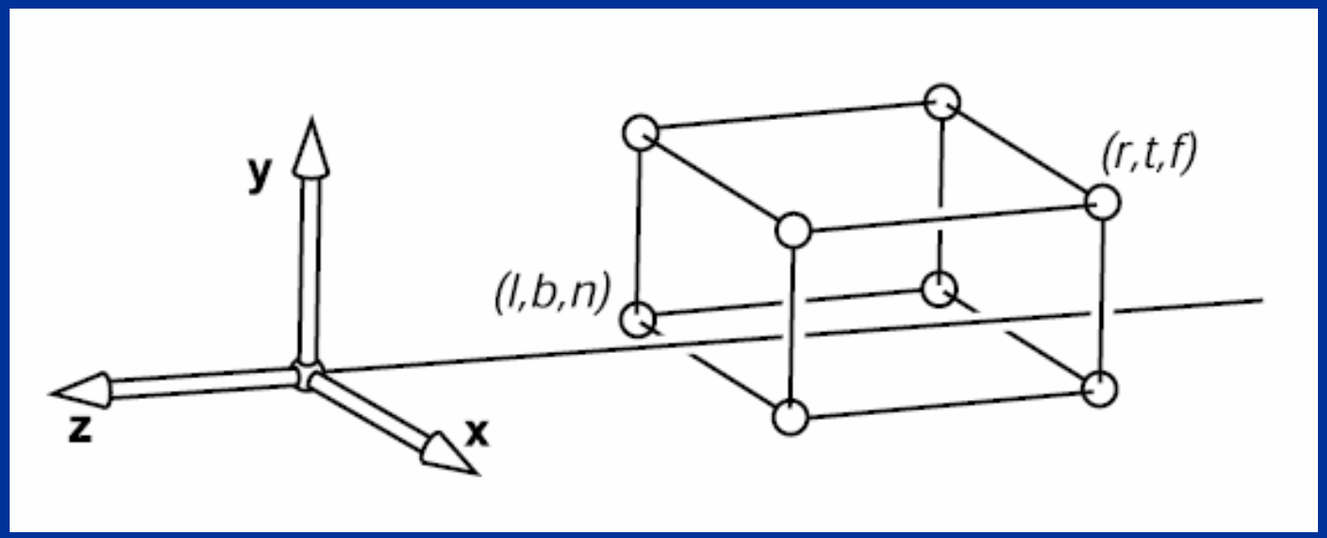
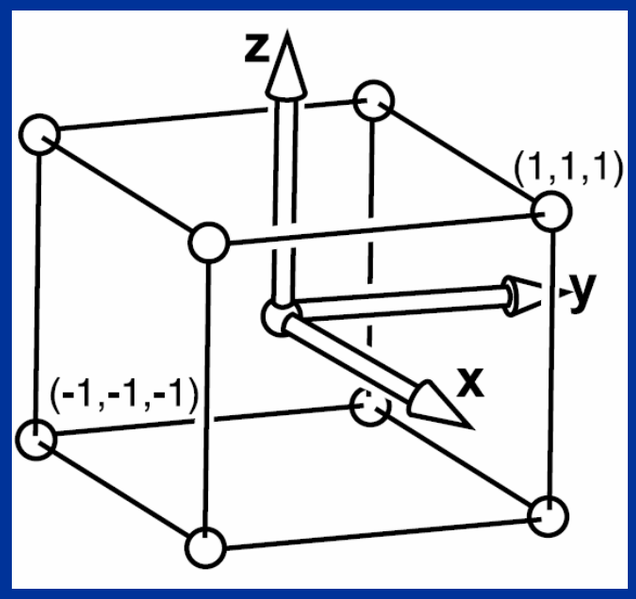
Orthographic Projection



X=l left plane
X=r right plane
Y=b bottom plane
Y=t top plane
Z=n near plane
Z=f far plane



Why near plane? Prevent points behind the camera being seen
Why far plane? Allows *z* to be scaled to a limited fixed-point value (*z*-buffering)

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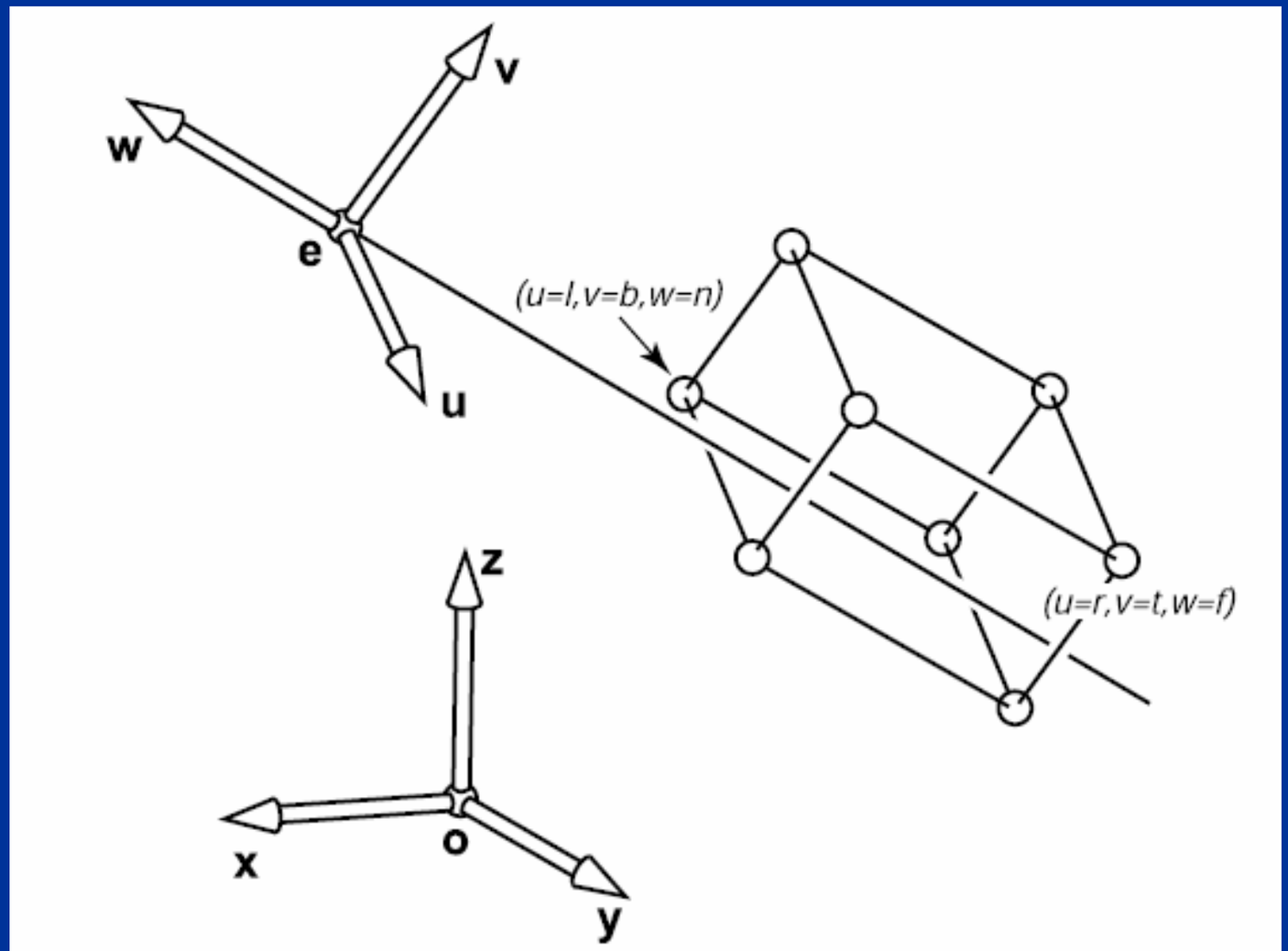
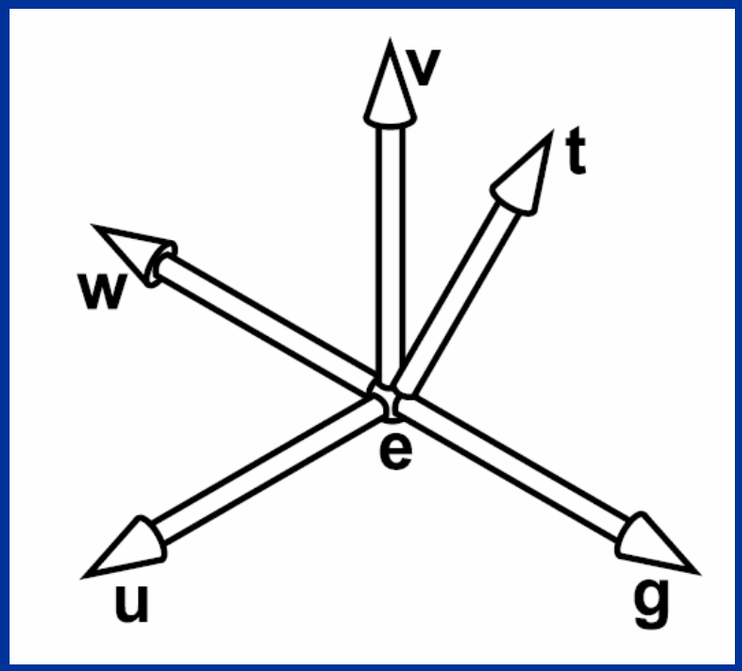
Arbitrary View Positions





Eye position: e
Gaze direction: g
view-up vector: t

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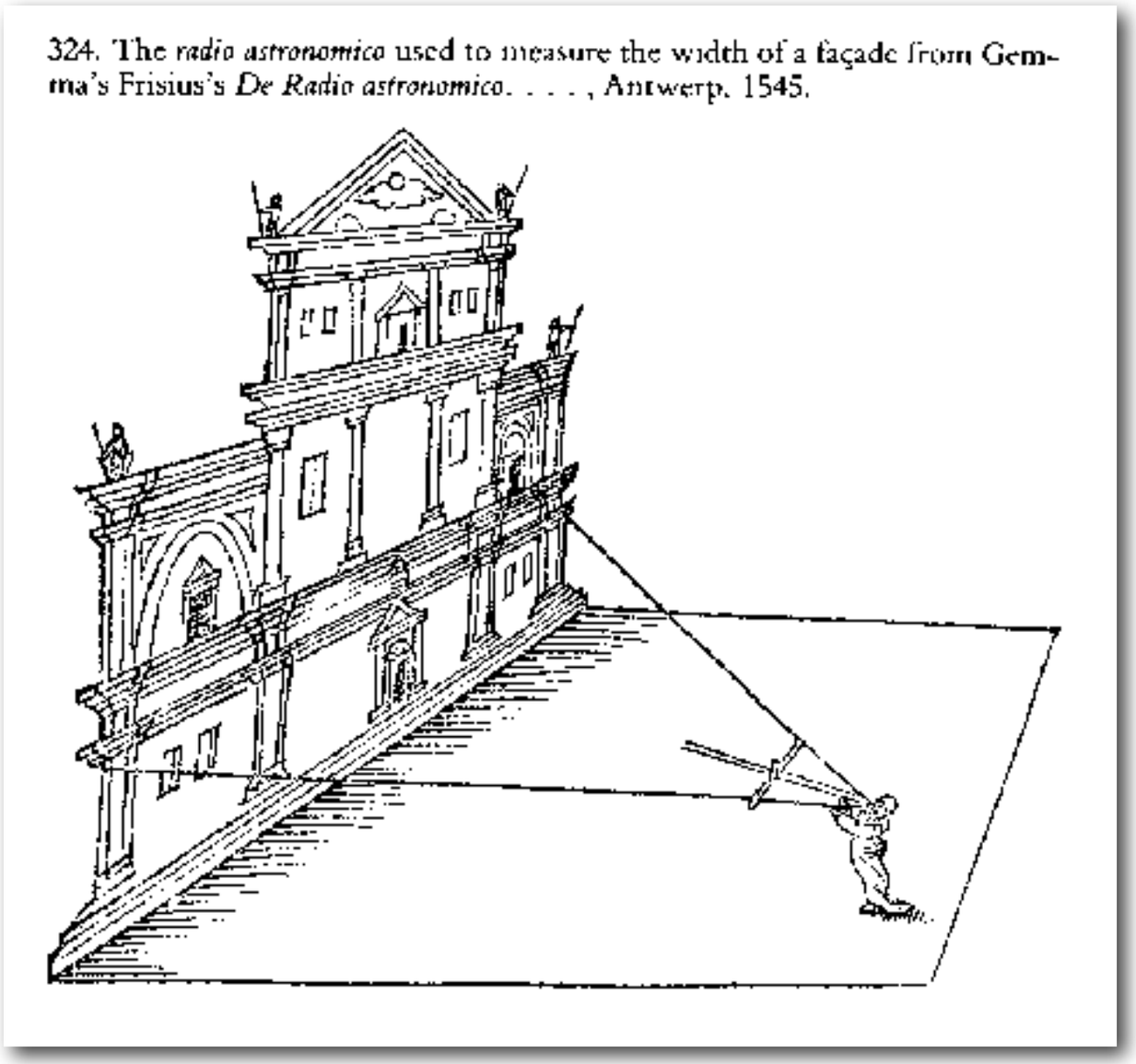
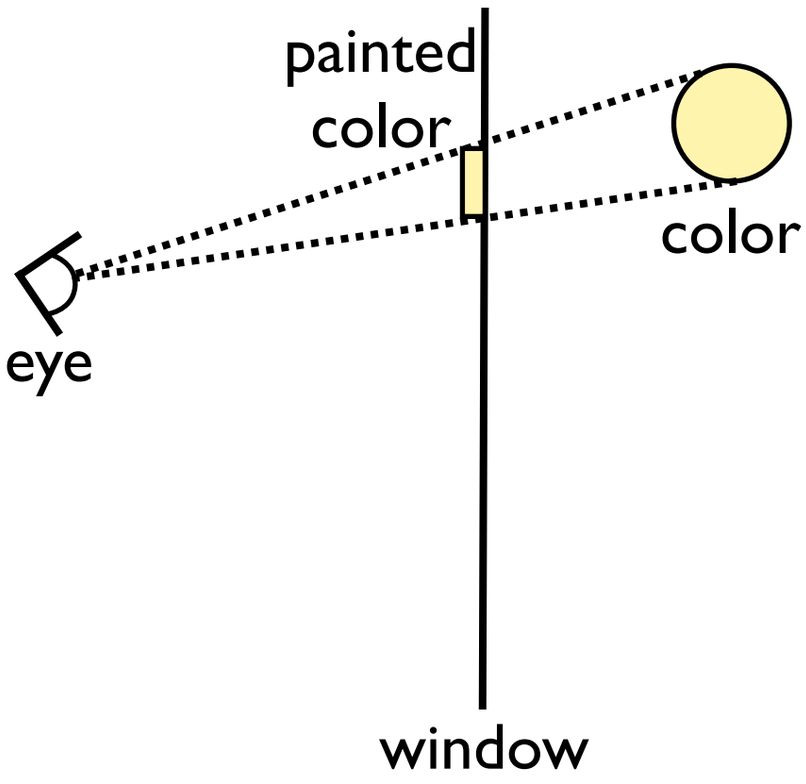
Perspective Projection



source: http://www.dartmouth.edu/~matc/math5.geometry/unit15/Frisius.gif

The simplest way to look at perspective projection is as painting on a window....



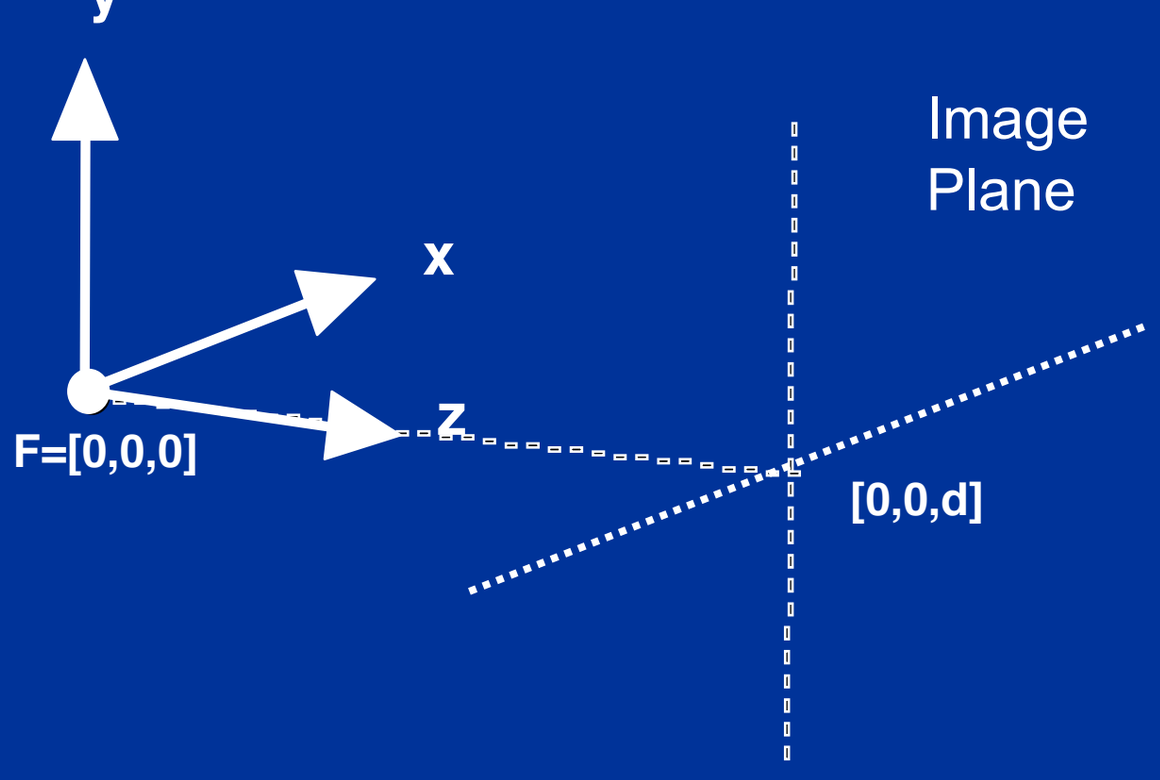
Paint on the window whatever color you see there.

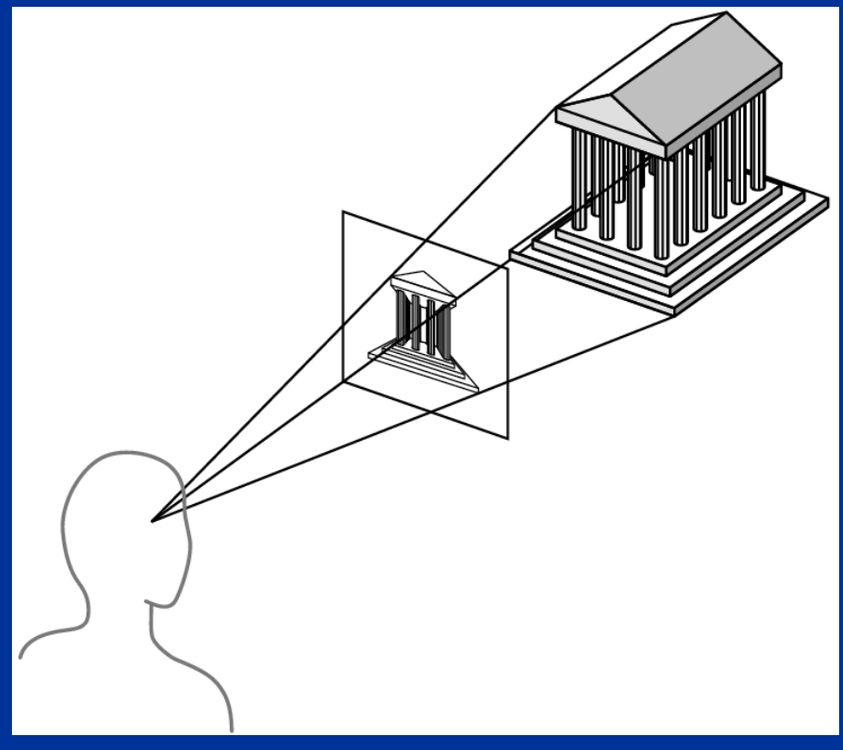
source: http://blog.mlive.com/flintjournal/newsnow/2007/11/WINDOW_PAINTING_02.jpg

Simple Perspective Camera

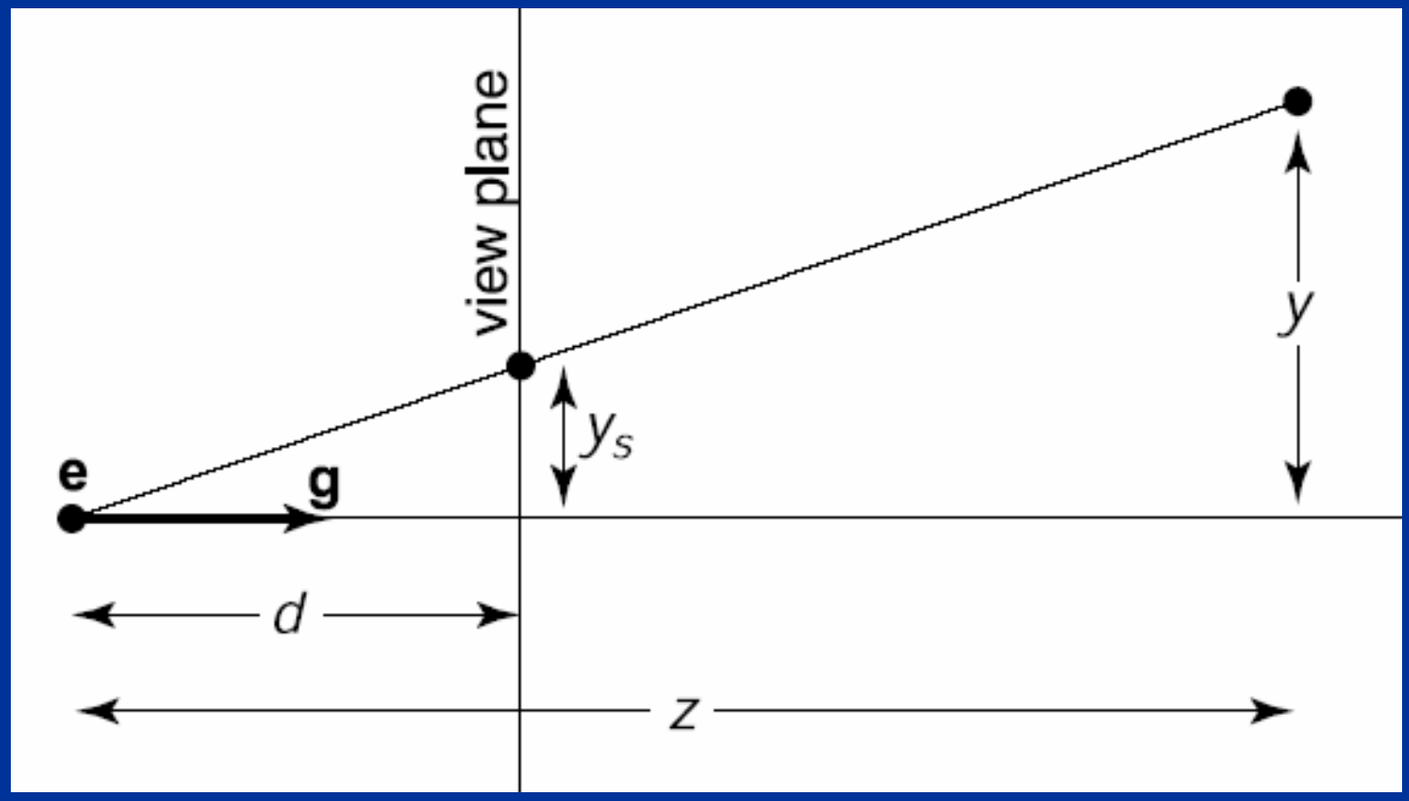
Canonical case:

- camera looks along the *z*-axis
- focal point is the origin
- image plane is parallel to the *xy*-plane at distance *d*
- (We call d the focal length, mainly for historical reasons)





Perspective Projection of a Point



$$y_s = d\frac{y}{z}$$

History of Perspective Projection

source: http://en.wikipedia.org/wiki/File:Reconstruction_of_the_temple_of_Jerusalem.jpg

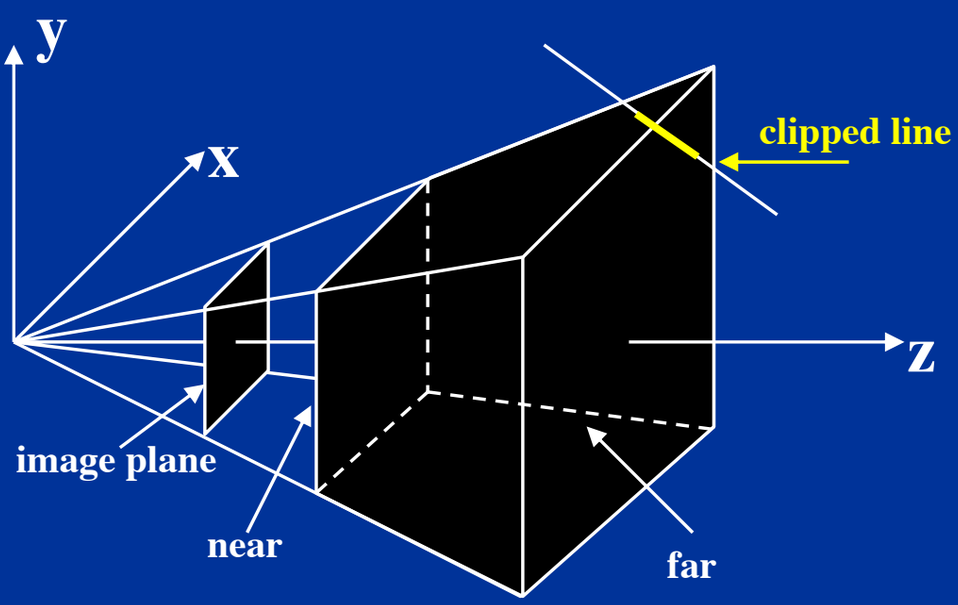
source: http://en.wikipedia.org/wiki/File:Giotto_-_Legend_of_St_Francis_-_-07-_-_Confirmation_of_the_Rule.jpg

source: http://en.wikipedia.org/wiki/File:Perugino_Keys.jpg

Clipping

Something is missing between projection and viewing...

Before projecting, we need to eliminate the portion of scene that is outside the viewing frustum

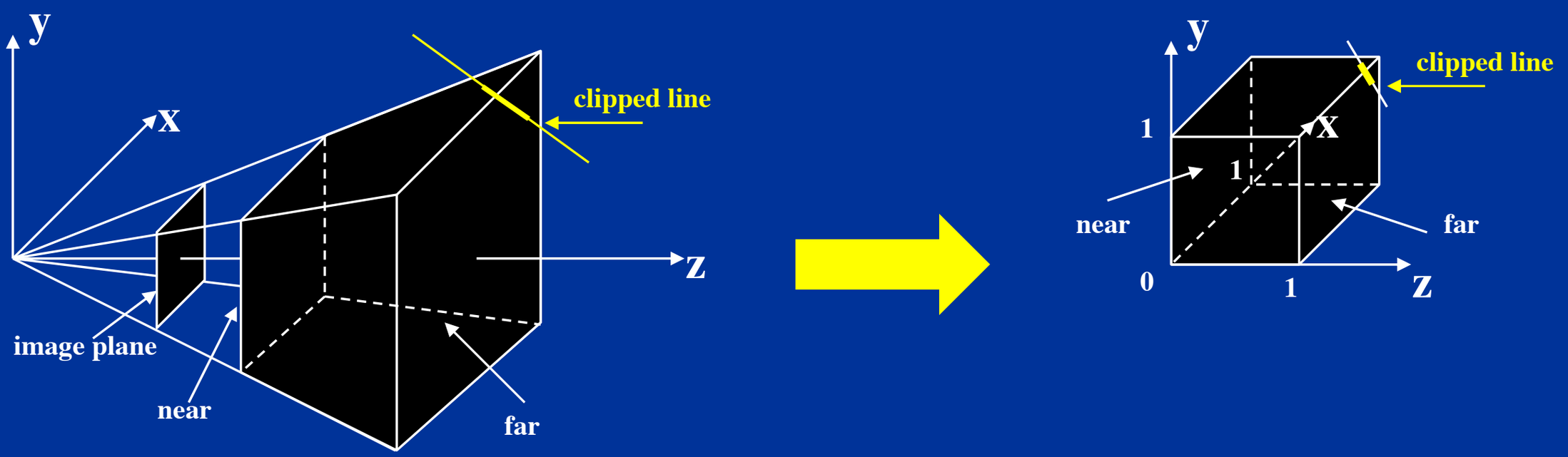


Need to clip objects to the frustum (truncated pyramid)

Now in a canonical position but it still seems kind of tricky...

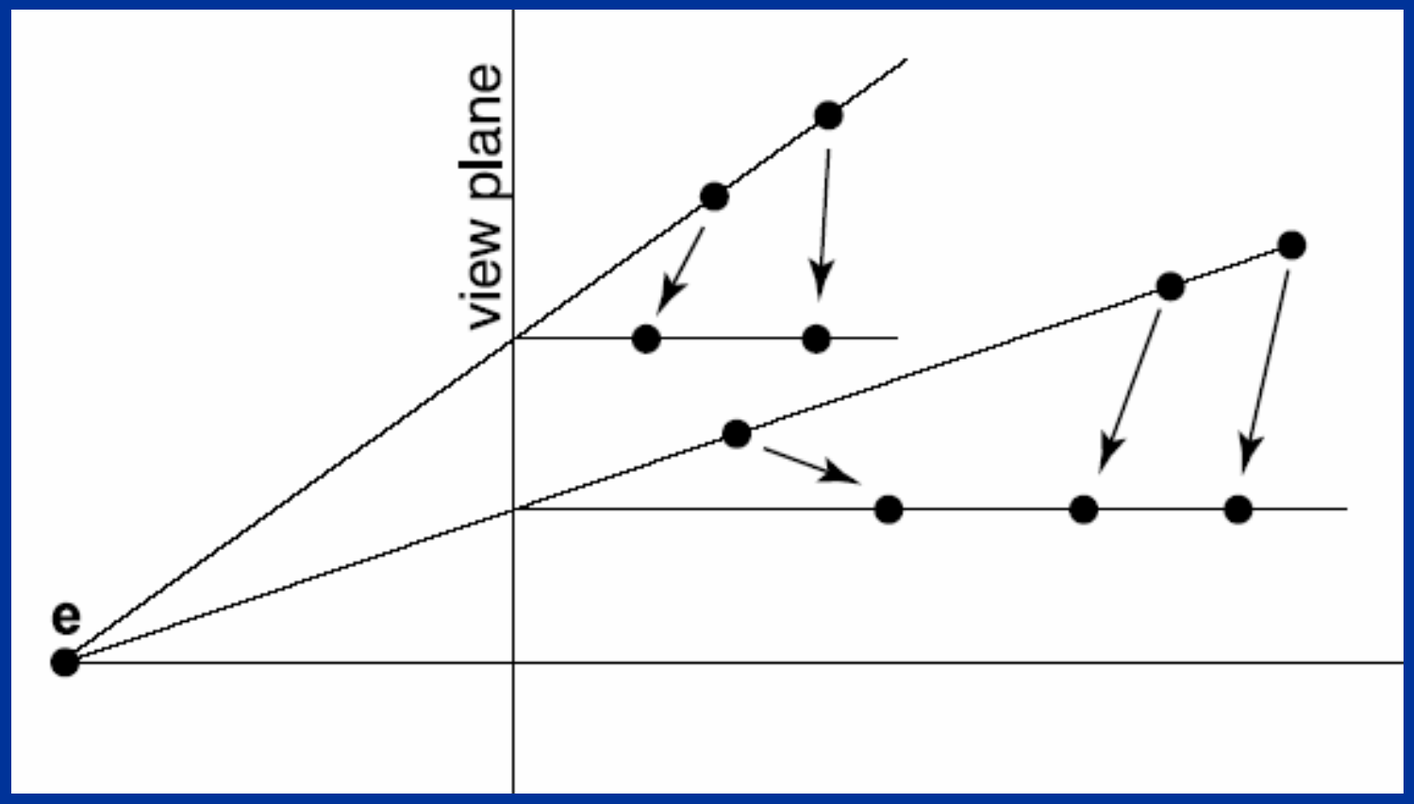
Normalizing the Viewing Frustum

Solution: transform frustum to a cube before clipping



Converts perspective frustum to orthographic frustum
Yet another homogeneous transform!

Perspective Projection



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Warping a perspective projection into and orthographic one

Lines for the two projections intersect at the view plane

How can we put this in matrix form?

Need to divide by z—haven't seen a divide in our matrices so far…

Requires our w from last time (or h in the book)

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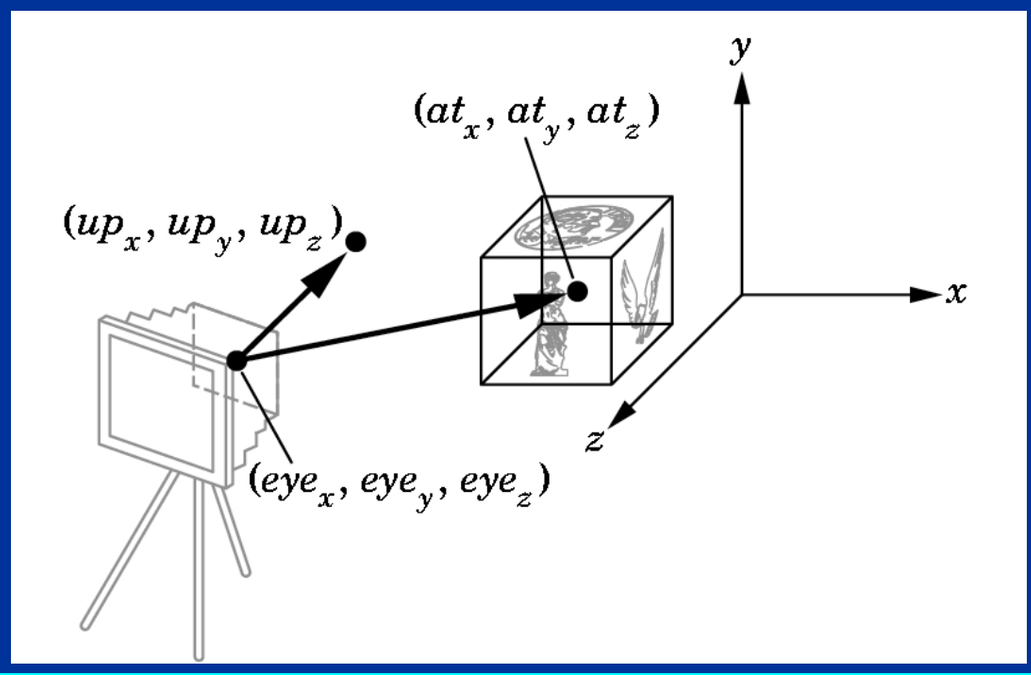
Camera Control Values

- All we need is a single translation and angle-axis rotation (orientation), but...
- Good animation requires good camera control--we need better control knobs
- Translation knob - move to the *lookfrom* point
- Orientation can be specified in several ways:
  - specify camera rotations
  - specify a *lookat* point (solve for camera rotations)

A Popular View Specification Approach

- Focal length, image size/shape and clipping planes are in the perspective transformation
- In addition:
  - *lookfrom:* where the focal point (camera) is
  - *lookat:* the world point to be centered in the image
- Also specify camera orientation about the *lookat-lookfrom* axis



Implementation

Implementing the *lookat/lookfrom/vup* viewing scheme

(1) Translate by *-lookfrom*, bring focal point to origin

(2) Rotate *lookat-lookfrom* to the *z*-axis with matrix R:

» v = (*lookat-lookfrom*) (normalized) and z = [0,0,1]

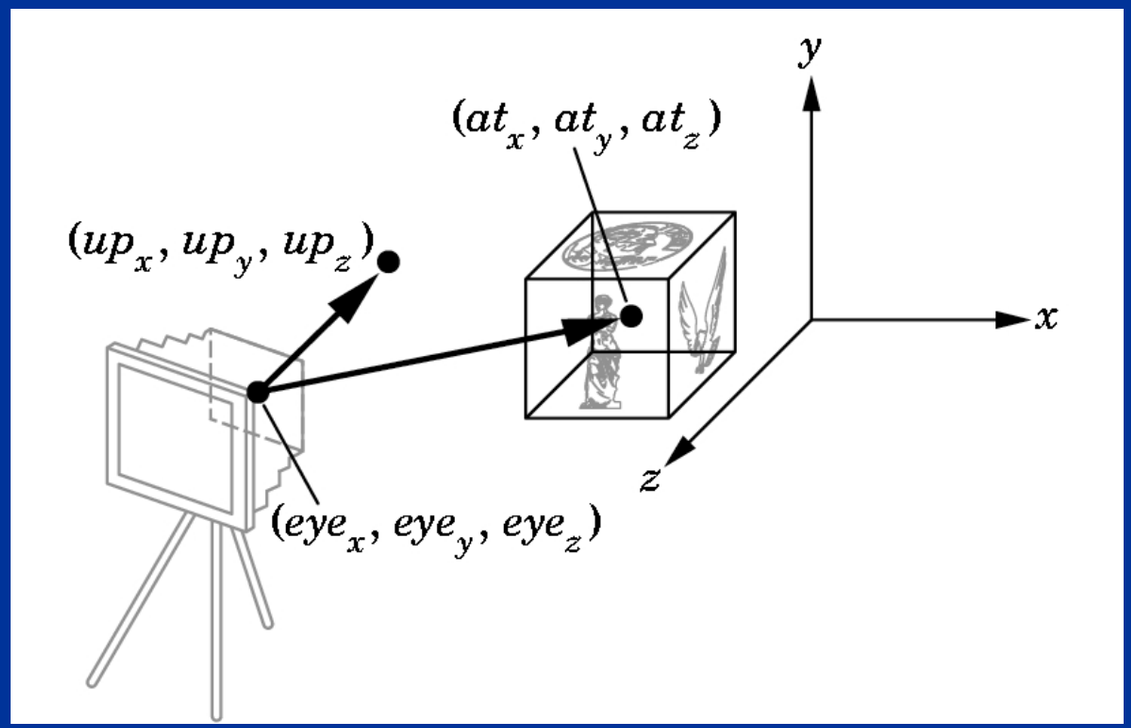
» rotation axis: $a = (v \times z)/|v \times z|$

» rotation angle: $\cos\theta = v \bullet z$ and $\sin\theta = |v \times z|$

glRotate(θ, a_x, a_y, a_z)

(3) Rotate about *z*-axis to get *vup* parallel to the y-axis

The Whole Picture



LOOKFROM: Where the camera is

LOOKAT: A point that should be centered in the image

VUP: A vector that will be pointing straight up in the image

FOV: Field-of-view angle.

d: focal length

WORLD COORDINATES

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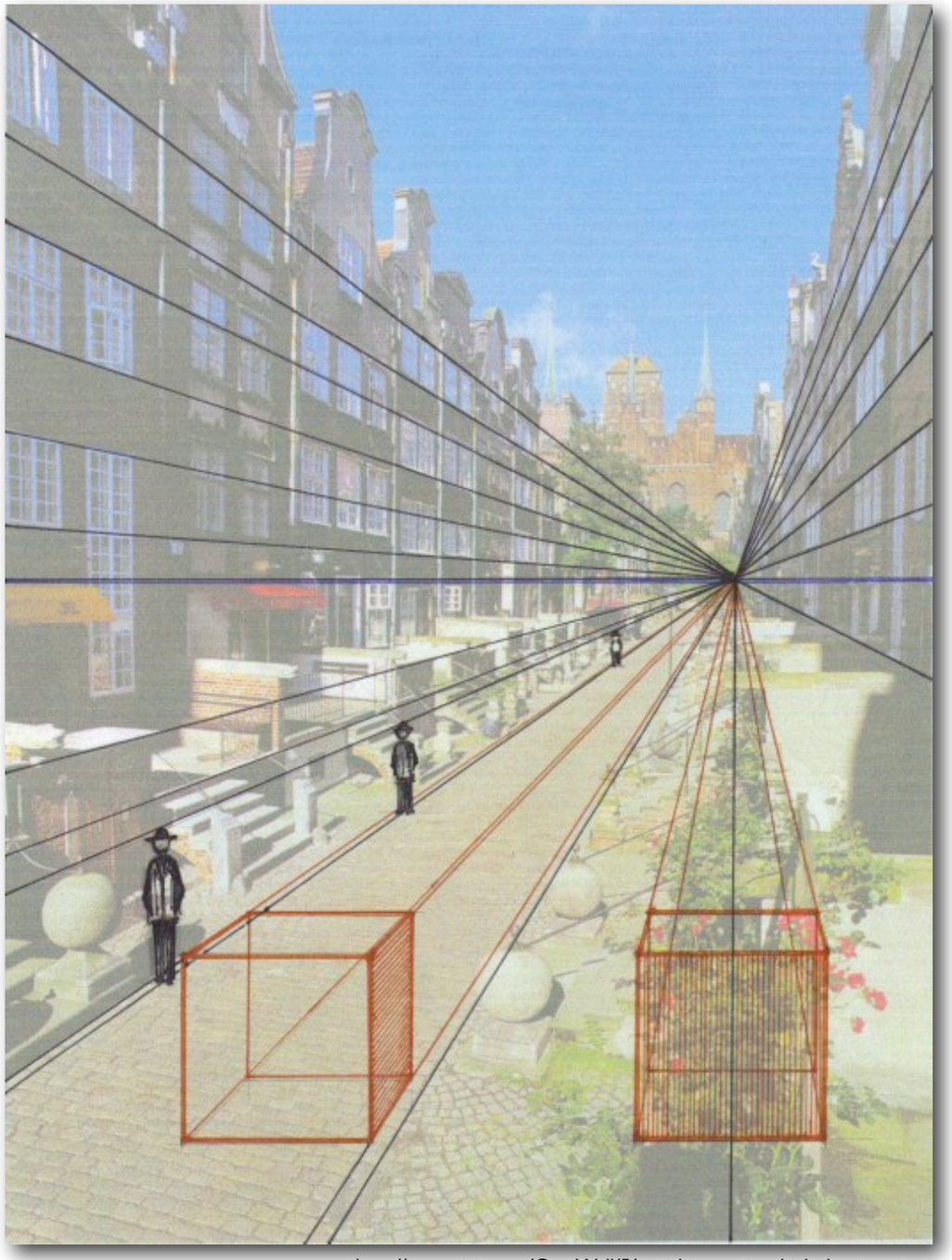
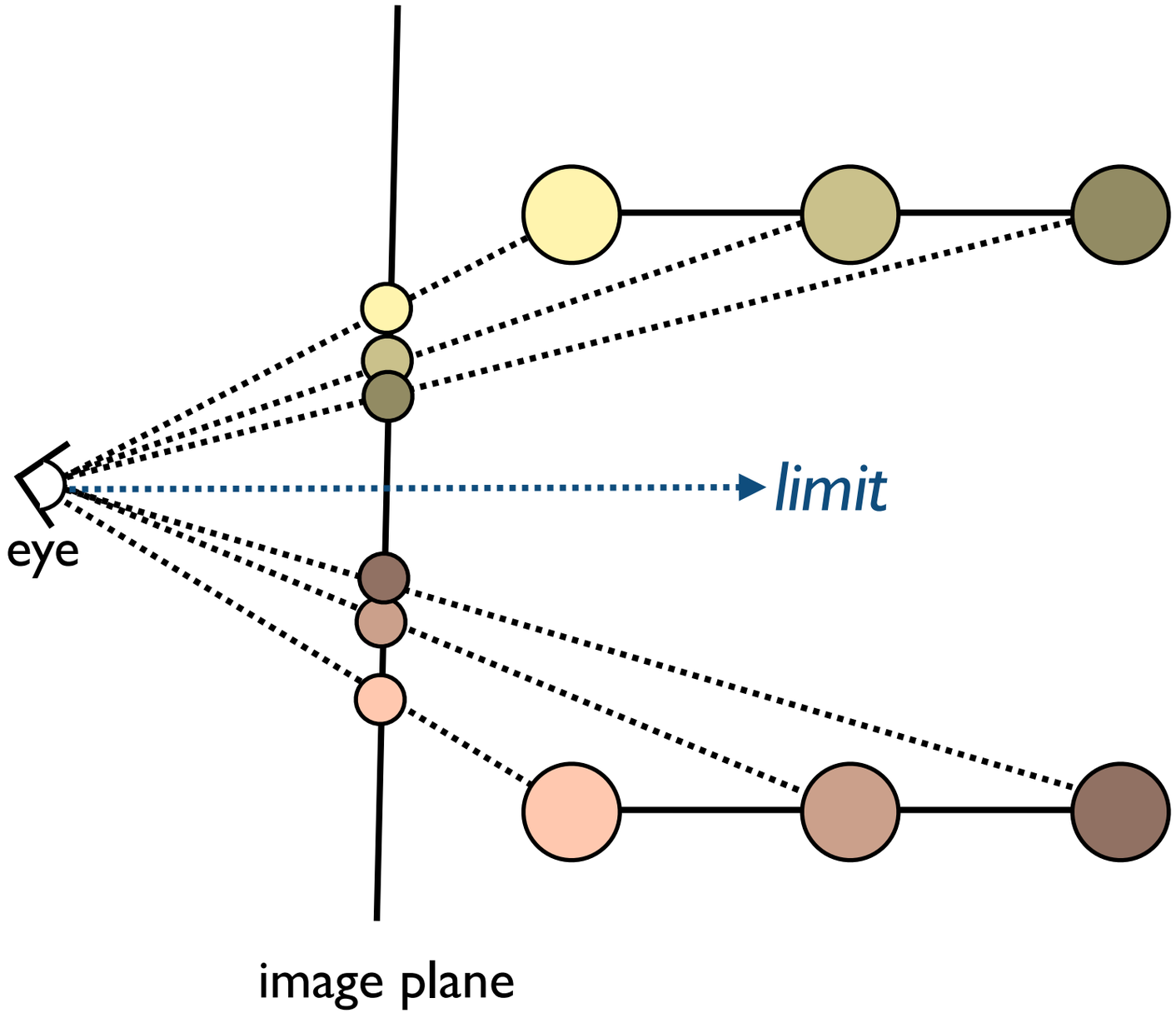
Vanishing Points

source: http://stevewebel.com/photographer/wp-content/uploads/2008/04/vanishing-point.jpg

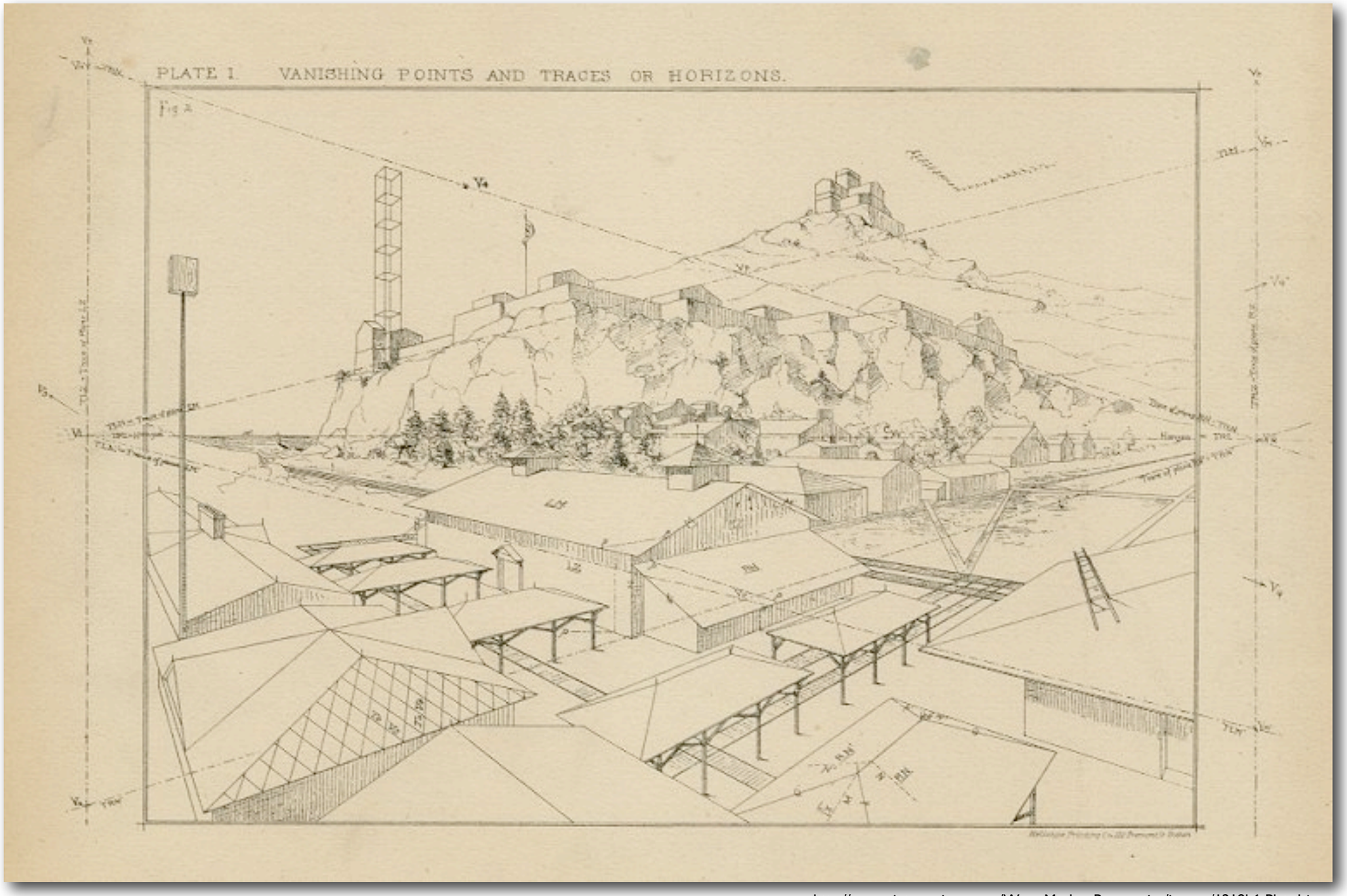


source: http://cavespirit.com/CaveWall/5/vanishing_point_high_horizon.jpg

What Causes Vanishing Points?


limit
eye
image plane

2 Vanishing Points



source: http://www.vintage-views.com/WaresModernPerspective/images/1219k6-Plate1.jpg

How many vanishing points can an image have?

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