

15-745 Lecture 4

SSA
CCP, ADCE
Dominance & Minimal SSA

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From Before... Def-Use Chains

- ...
- for (i=0; i++; i<10) {
- ... = ... i ...;
- ...
- }
- for (i=j; i++; i<20) {
- ... = i ...
- }

How is this related to RA?

Def-Use chains are expensive

```
foo(int i, int j) {  
  ...  
  switch (i) {  
  case 0: x=3; break;  
  case 1: x=1; break;  
  case 2: x=6; break;  
  case 3: x=7; break;  
  default: x = 11;  
  }  
  switch (j) {  
  case 0: y=x+7; break;  
  case 1: y=x+4; break;  
  case 2: y=x-2; break;  
  case 3: y=x+1; break;  
  default: y=x+9;  
  }  
  ...  
}
```

Def-Use chains are expensive

```
foo(int i, int j) {  
  ...  
  switch (i) {  
  case 0: x=3;  
  case 1: x=1;  
  case 2: x=6;  
  case 3: x=7;  
  default: x = 11;  
  }  
  switch (j) {  
  case 0: y=x+7;  
  case 1: y=x+4;  
  case 2: y=x-2;  
  case 3: y=x+1;  
  default: y=x+9;  
  }  
  ...  
}
```

In general,
N defs
M uses
⇒ O(NM) space and time

A solution is to limit each var to ONE def site

Def-Use chains are expensive

```
foo(int i, int j) {  
  ...  
  switch (i) {  
  case 0: x=3; break;  
  case 1: x=1; break;  
  case 2: x=6;  
  case 3: x=7;  
  default: x = 11;  
  }
```

x1 is one of the above x's

```
  switch (j) {  
  case 0: y=x1+7;  
  case 1: y=x1+4;  
  case 2: y=x1-2;  
  case 3: y=x1+1;  
  default: y=x1+9;  
  }
```

A solution is to limit each
var to ONE def site

SSA

- Static single assignment is an **IR** where every variable is assigned a value at most once in the program text
- Easy for a basic block:
 - assign to a fresh variable at each stmt.
 - Each use uses the most recently defined var.
 - (Similar to Value Numbering)

Advantages of SSA


- Makes du-chains explicit
- Makes dataflow optimizations
 - Easier
 - faster
- Improves register allocation
 - Automatically builds Webs
 - Makes building interference graphs easier
- For most programs reduces space/time requirements

SSA History

- Developed by Wegman, Zadeck, Alpern, and Rosen in 1988
- New to gcc 4.0, used in ORC, LLVM, used in both IBM and Sun Java JIT compilers
 - and others


Straight-line SSA

```
a ← x + y
b ← a + x
a ← b + 2
c ← y + 1
a ← c + a
```



Straight-line SSA

```
a ← x + y
b ← a + x
a ← b + 2
c ← y + 1
a ← c + a
```




```
a1 ← x + y
b1 ← a1 + x
a2 ← b1 + 2
c1 ← y + 1
a3 ← c1 + a2
```

SSA

- Static single assignment is an IR where every variable is assigned a value at most once in the program text
- Easy for a basic block:
 - assign to a fresh variable at each stmt.
 - Each use uses the most recently defined var.
 - (Similar to Value Numbering)
- What about at joins in the CFG?

Merging at Joins

```
c ← 12
if (i) {
  a ← x + y
  b ← a + x
} else {
  a ← b + 2
  c ← y + 1
}
a ← c + a
```

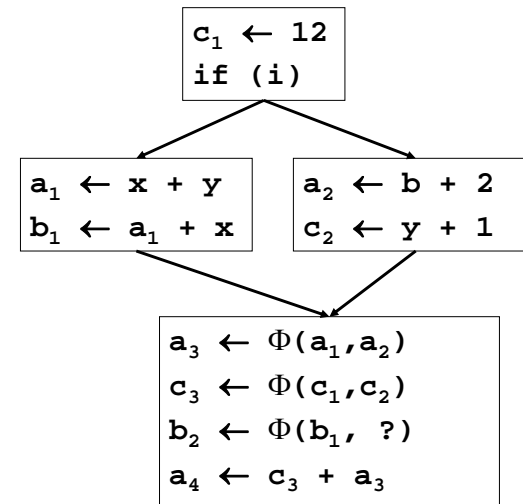


```
graph TD
  A["c1 ← 12  
if (i)"] --> B["a1 ← x + y  
b1 ← a1 + x"]
  A --> C["a ← b + 2  
c ← y + 1"]
  B --> D["a4 ← c2 + a2"]
  C --> D
```

SSA

- Static single assignment is an IR where every variable is assigned a value at most once in the program text
- Easy for a basic block:
 - assign to a fresh variable at each stmt.
 - Each use uses the most recently defined var.
 - (Similar to Value Numbering)
- What about at joins in the CFG?
 - Use a notional fiction: A Φ function

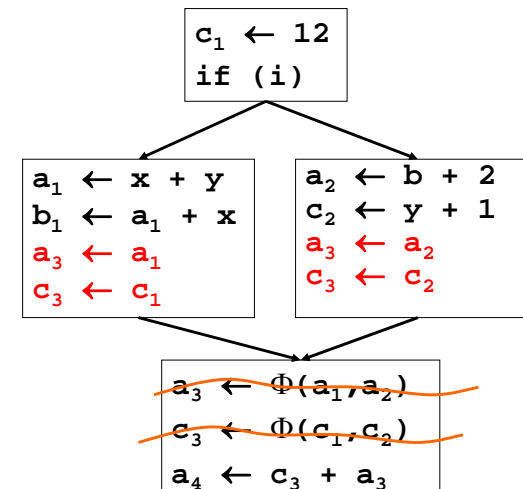
Merging at Joins



The Φ function

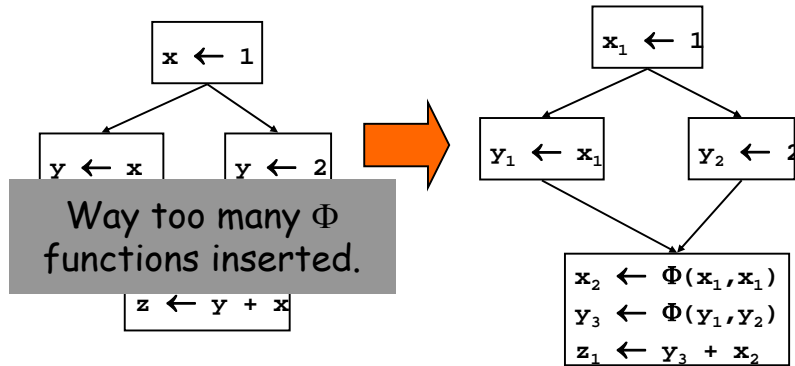
- Φ merges multiple definitions along multiple control paths into a single definition.
- At a BB with p predecessors, there are p arguments to the Φ function.
 $x_{new} \leftarrow \Phi(x_1, x_1, x_1, \dots, x_p)$
- How do we choose which x_i to use?
 - We don't really care!
 - If we care, use moves on each incoming edge

"Implementing" Φ



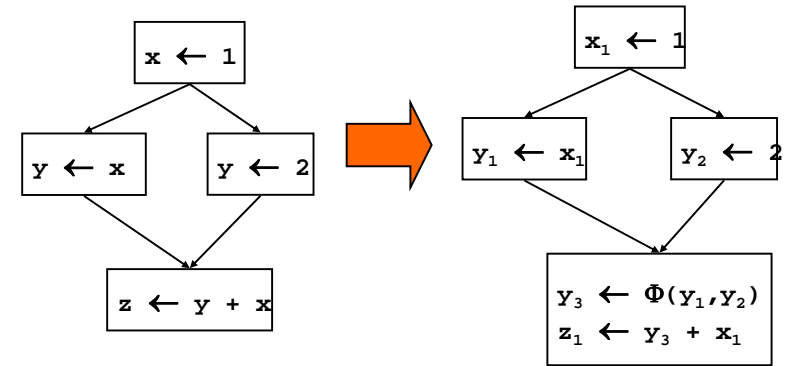
Trivial SSA

- Each assignment generates a fresh variable.
- At each join point insert Φ functions for all live variables.

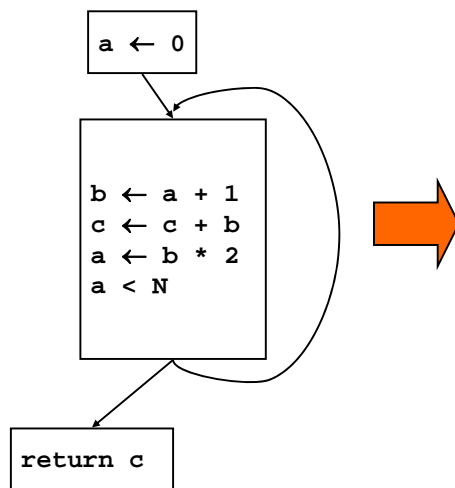


Minimal SSA

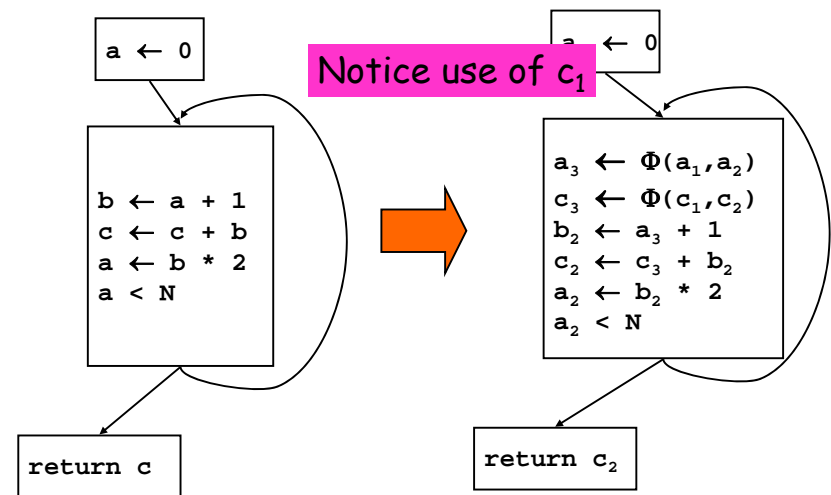
- Each assignment generates a fresh variable.
- At each join point insert Φ functions for all variables with **multiple outstanding defs**.



Another Example



Another Example

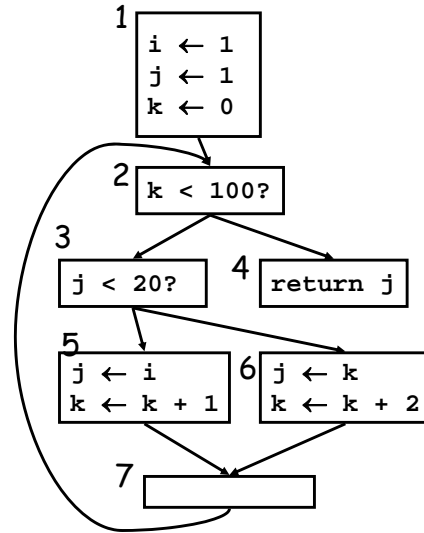


Lets optimize the following:

```

i=1;
j=1;
k=0;
while (k<100) {
  if (j<20) {
    j=i;
    k++;
  } else {
    j=k;
    k+=2;
  }
}
return j;

```

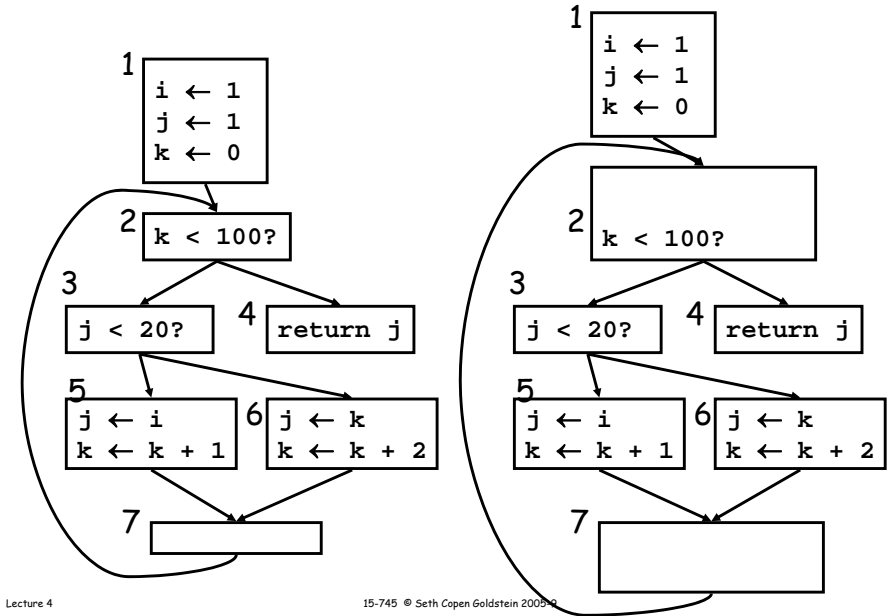


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First, turn into SSA

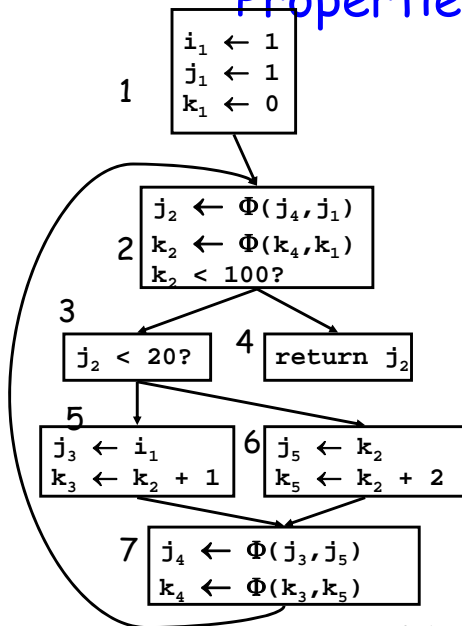


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Properties of SSA



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- Only 1 assignment per variable
- definitions dominate uses
- Can we use this to help with constant propagation?

Constant Propagation

- If " $v \leftarrow c$ ", replace all uses of v with c
- If " $v \leftarrow \Phi(c, c, c)$ " replace all uses of v with c

$W \leftarrow$ list of all defs

while ! W .isEmpty {

$stmt\ S \leftarrow W.removeOne$

 if S has form " $v \leftarrow \Phi(c, \dots, c)$ "

 replace S with $V \leftarrow c$

 if S has form " $v \leftarrow c$ " then

 delete S

 foreach $stmt\ U$ that uses v ,

 replace v with c in U

$W.add(U)$

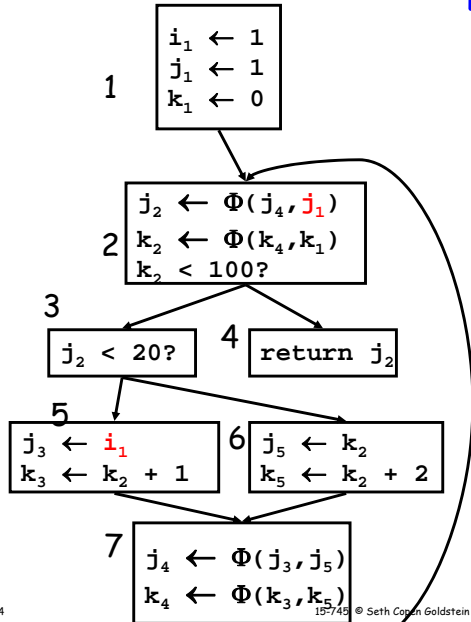
}

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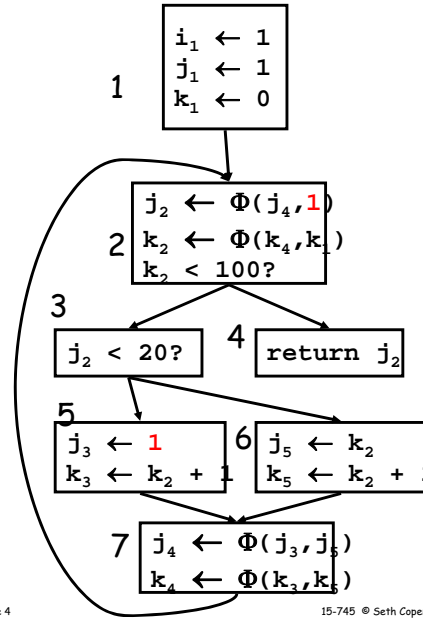
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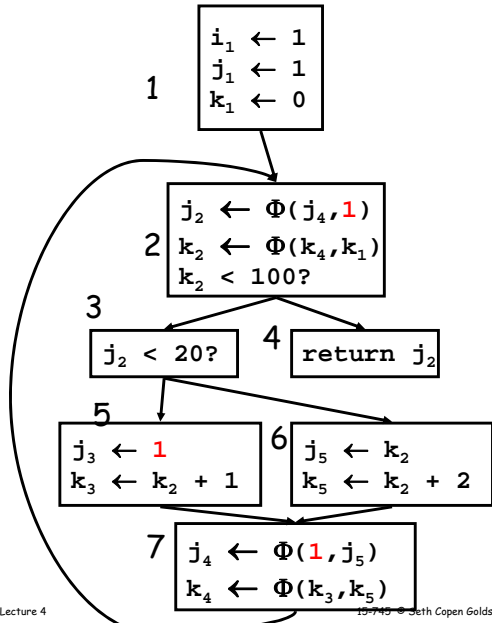
Constant Propagation



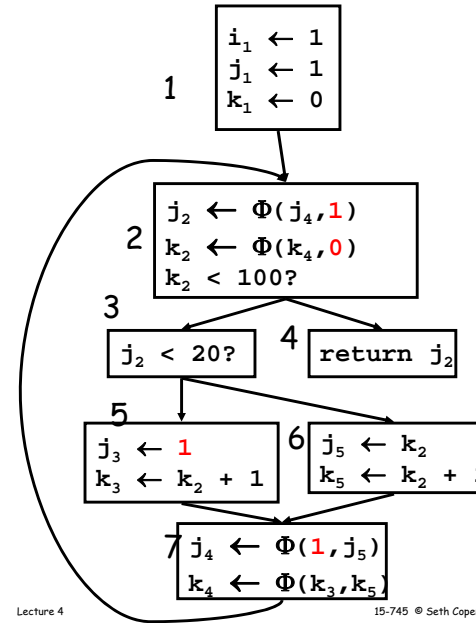
Constant Propagation



Constant Propagation



Constant Propagation

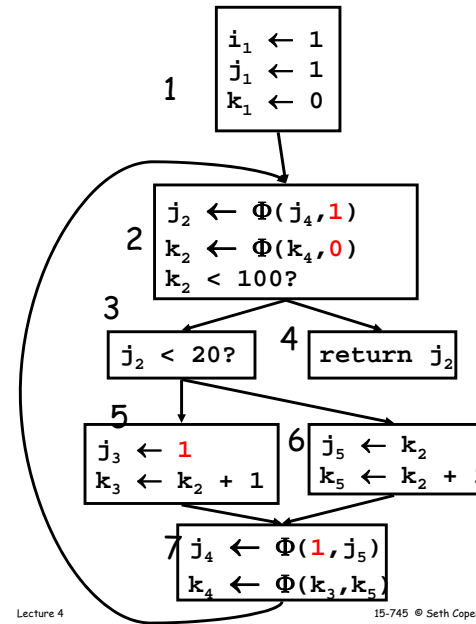


But, so what?

Other stuff we can do?

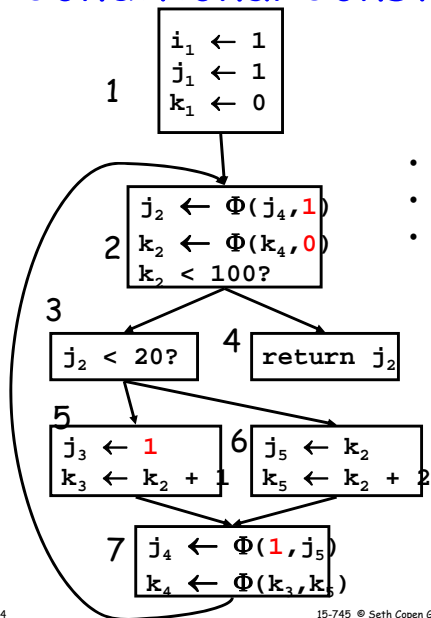
- Copy propagation
delete "x ← Φ(y)" and replace all x with y
delete "x ← y" and replace all x with y
- Constant Folding
(Also, constant conditions too!)
- Unreachable Code
Remember to delete all edges from unreachable block

Constant Propagation



But, so what?

Conditional Constant Propagation



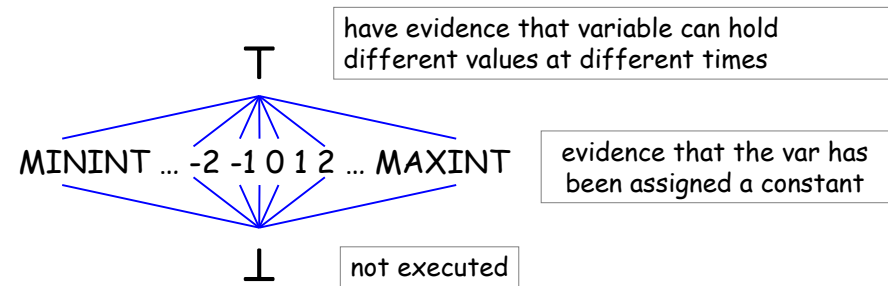
- Does block 6 ever execute?
- Simple CP can't tell
- CCP can tell:
 - Assumes blocks don't execute until proven otherwise
 - Assumes Values are constants until proven otherwise

CCP data structures & lattice

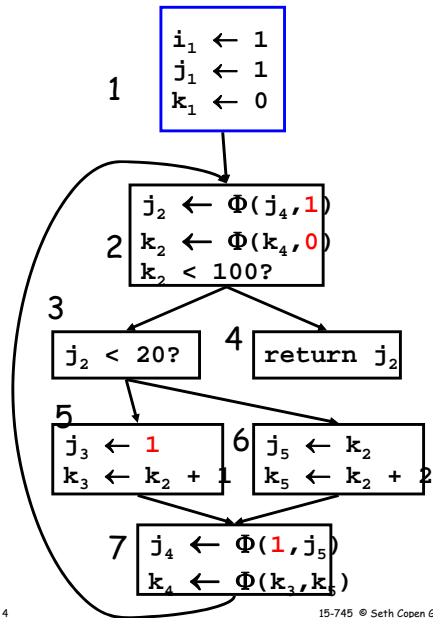
Keep track of:

- Blocks (assume unexecuted until proven otherwise)
- Variables (assume not executed, only with proof of assignments of a non-constant value do we assume not constant)

Use a lattice for variables:



Conditional Constant Propagation

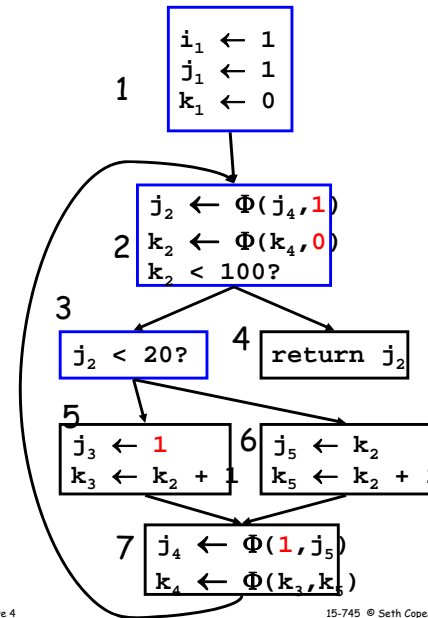


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Conditional Constant Propagation

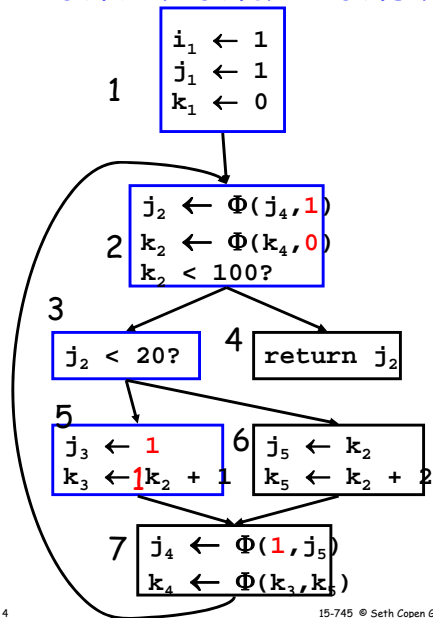


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Conditional Constant Propagation

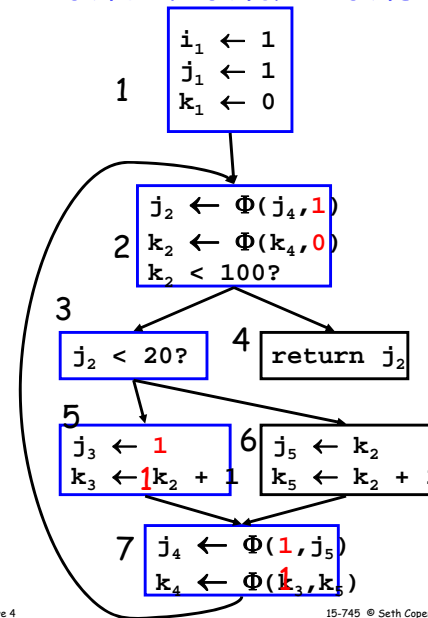


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Conditional Constant Propagation

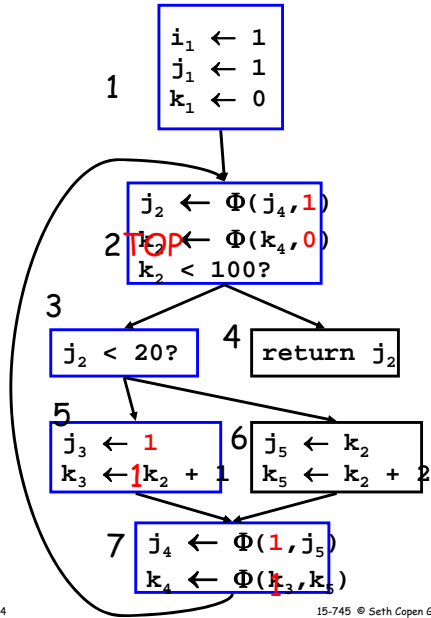


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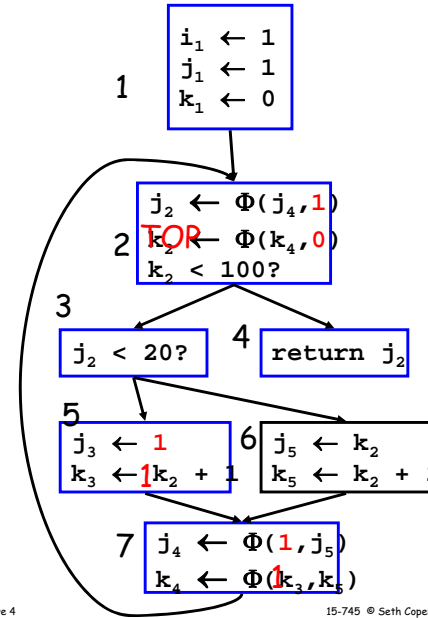
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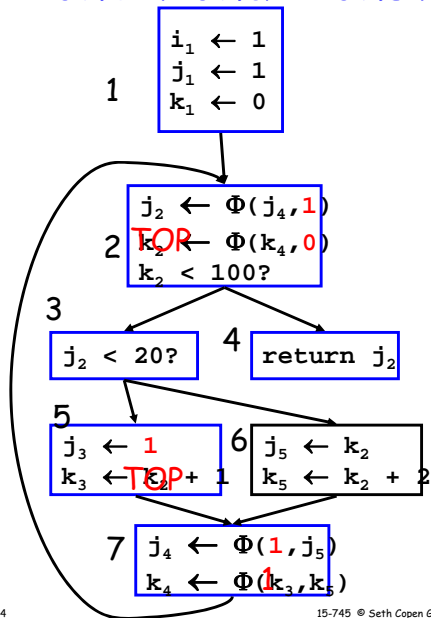
Conditional Constant Propagation



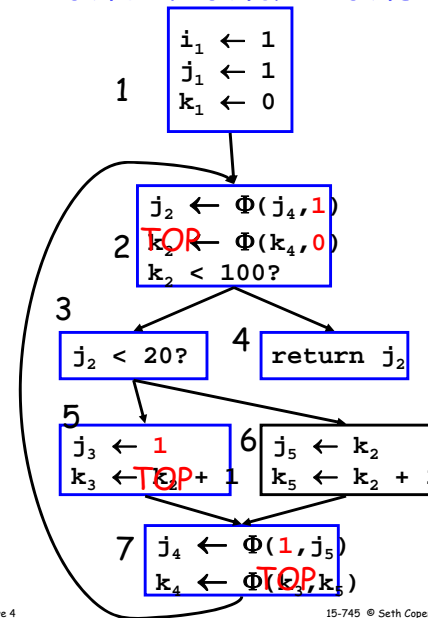
Conditional Constant Propagation



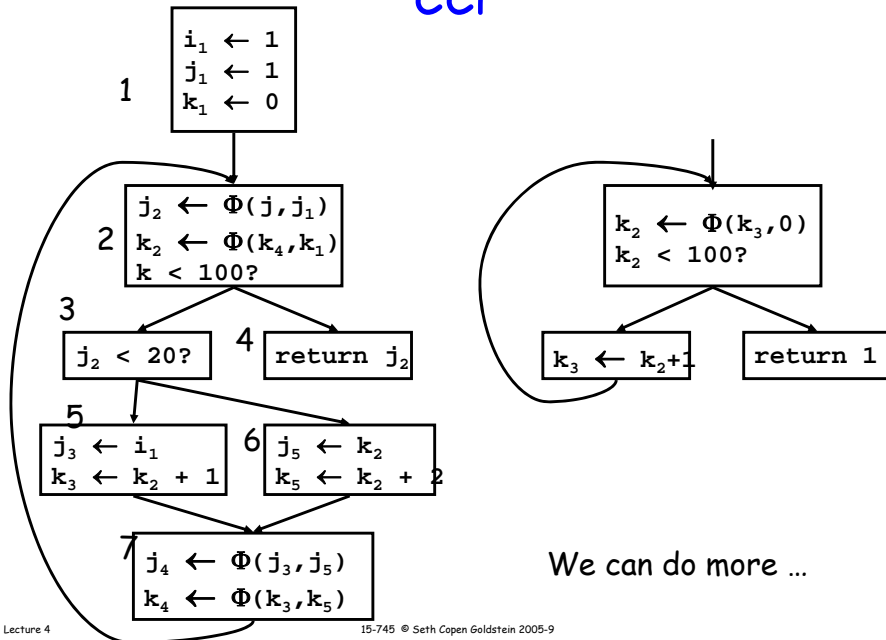
Conditional Constant Propagation



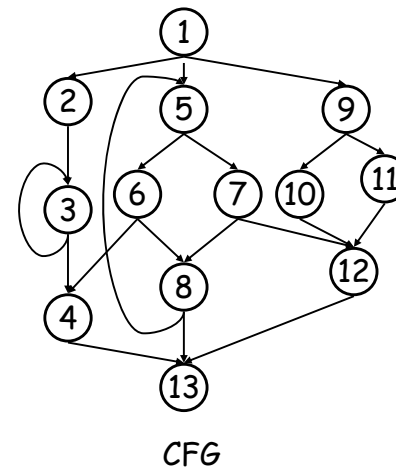
Conditional Constant Propagation



CCP



When do we insert Φ ?



If there is a def of a in block 5, which nodes need a $\Phi()$?

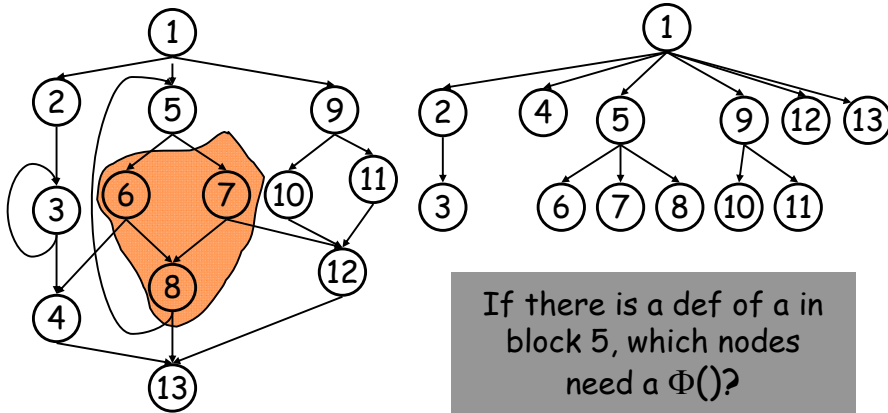
When do we insert Φ ?

- We insert a Φ function for variable A in block Z iff:
 - A was defined more than once before (i.e., A defined in X and Y AND $X \neq Y$)
 - There exists a non-empty path from x to z , P_{xz} , and a non-empty path from y to z , P_{yz} s.t.
 - $P_{xz} \cap P_{yz} = \{z\}$
 - $z \notin P_{xq}$ or $z \notin P_{xr}$ where $P_{xz} = P_{xq} \rightarrow z$ and $P_{yz} = P_{xr} \rightarrow z$
 - Entry block contains an implicit def of all vars
 - Note: $A = \Phi(\dots)$ is a def of A
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Dominance Property of SSA

- In SSA definitions dominate uses.
 - If x_i is used in $x \leftarrow \Phi(\dots, x_i, \dots)$, then $BB(x_i)$ dominates ith pred of $BB(\text{PHI})$
 - If x is used in $y \leftarrow \dots x \dots$, then $BB(x)$ dominates $BB(y)$
 - We can use this for an efficient alg to convert to SSA
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Dominance



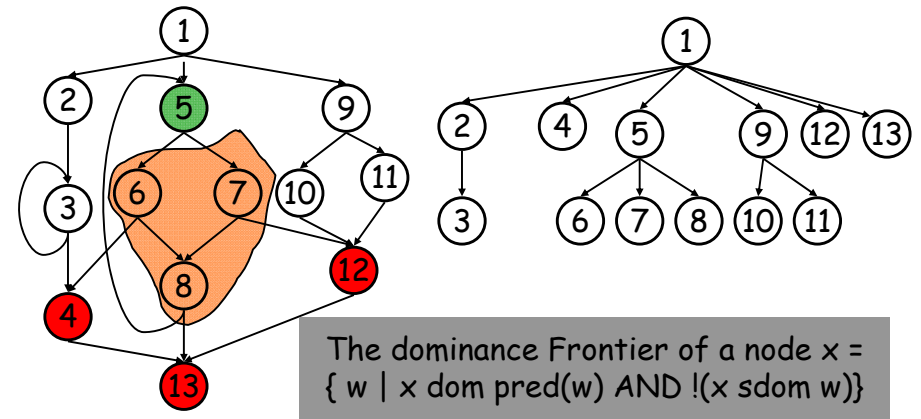
If there is a def of a in block 5, which nodes need a $\Phi()$?

CFG

D-Tree

x strictly dominates w ($s \text{ sdom } w$) iff $x \text{ dom } w$ AND $x \neq w$

Dominance Frontier



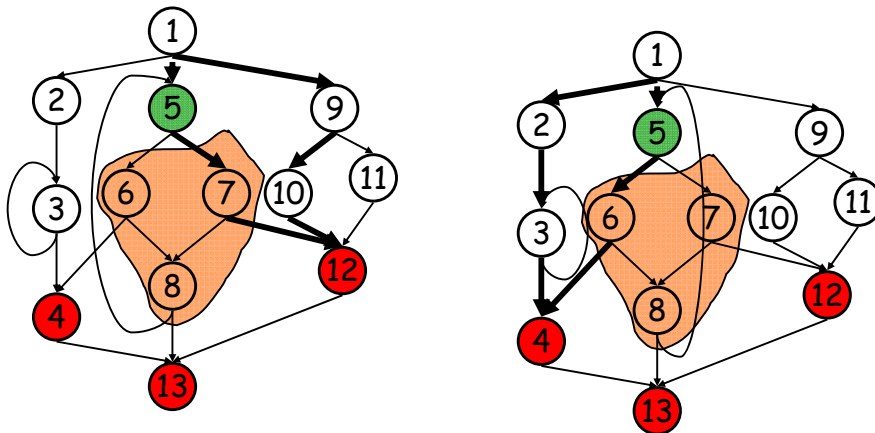
The dominance Frontier of a node $x = \{ w \mid x \text{ dom pred}(w) \text{ AND } !(x \text{ sdom } w) \}$

CFG

D-Tree

x strictly dominates w ($s \text{ sdom } w$) iff $x \text{ dom } w$ AND $x \neq w$

Dominance Frontier & path-convergence



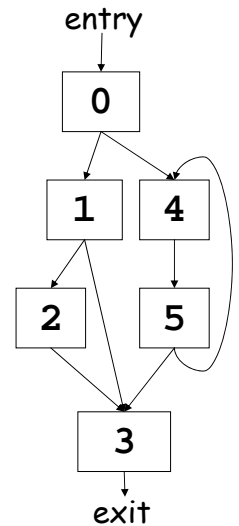
Computing Dominance Frontier

- You've probably already seen a $O(n^3)$ iterative algorithm
- There's also a near linear time algorithm due to Tarjan and Lengauer (Chap 19.2)
 - SSA construction therefore near linear
 - SSA form makes many optimizations linear (no need for iterative data flow)

Side trip: Dominators

Dominators

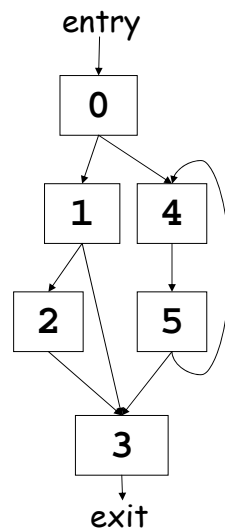
- $a \text{ dom } b$
- block a *dominates* block b if every possible execution path from *entry* to b includes a
 - **entry** dominates everything
 - **0** dominates everything but entry
 - **1** dominates 2 and 5



Dominators are useful in identifying "natural" loops

Definitions

- $a \text{ sdom } b$
- If a and b are different blocks and $a \text{ dom } b$, we say that a *strictly dominates* b
- $a \text{ idom } b$
- If $a \text{ sdom } b$, and there is no c such that $a \text{ sdom } c$ and $c \text{ sdom } b$, we say that a is the *immediate dominator* of b



Properties of Dom

- Dominance is a partial order on the blocks of the flow graph, i.e.,
 1. Reflexivity: $a \text{ dom } a$ for all a
 2. Anti-symmetry: $a \text{ dom } b$ and $b \text{ dom } a$ implies $a = b$
 3. Transitivity: $a \text{ dom } b$ and $b \text{ dom } c$ implies $a \text{ dom } c$
- NOTE: there may be blocks a and b such that neither $a \text{ dom } b$ or $b \text{ dom } a$ holds.
- The dominators of each node n are *linearly ordered* by the *dom* relation. The dominators of n appear in this linear order on any path from the initial node to n .

Computing dominators

- We want to compute $D[n]$, the set of blocks that dominate n

Initialize each $D[n]$ (except $D[\text{entry}]$) to be the set of all blocks, and then iterate until no $D[n]$ changes:

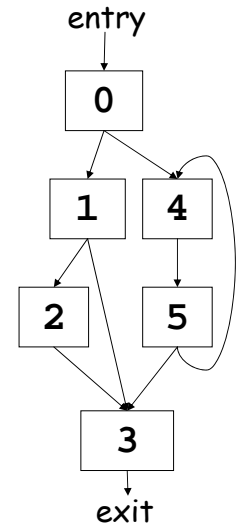
$$D[\text{entry}] = \{\text{entry}\}$$

$$D[n] = \{n\} \cup \left(\bigcap_{p \in \text{pred}(n)} D[p] \right), \text{ for } n \neq \text{entry}$$

Skip example

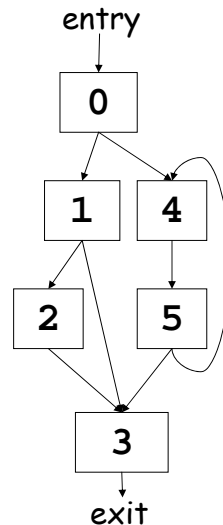
Example

block	Initialization $D[n]$
entry	{entry}
0	{entry,0,1,2,3,4,5,exit}
1	{entry,0,1,2,3,4,5,exit}
2	{entry,0,1,2,3,4,5,exit}
3	{entry,0,1,2,3,4,5,exit}
4	{entry,0,1,2,3,4,5,exit}
5	{entry,0,1,2,3,4,5,exit}
exit	{entry,0,1,2,3,4,5,exit}



Example

block	Initialization $D[n]$	First Pass $D[n]$
entry	{entry}	{entry}
0	{entry,0,1,2,3,4,5,exit}	{0,entry}
1	{entry,0,1,2,3,4,5,exit}	{1,0,entry}
2	{entry,0,1,2,3,4,5,exit}	{2,1,0,entry}
3	{entry,0,1,2,3,4,5,exit}	{3,1,0,entry}
4	{entry,0,1,2,3,4,5,exit}	{4,0,entry}
5	{entry,0,1,2,3,4,5,exit}	{5,4,0,entry}
exit	{entry,0,1,2,3,4,5,exit}	{exit,3,1,0,entry}

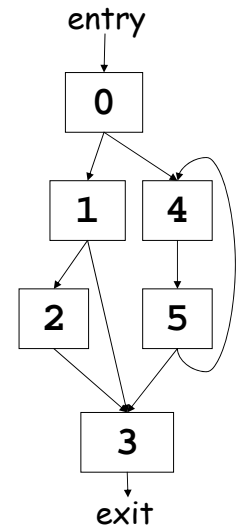


Update rule:

$$D[n] = \{n\} \cup \left(\bigcap_{p \in \text{pred}(n)} D[p] \right)$$

Example

block	First Pass $D[n]$	Second Pass $D[n]$
entry	{entry}	{entry}
0	{0,entry}	{0,entry}
1	{1,0,entry}	{1,0,entry}
2	{2,1,0,entry}	{2,1,0,entry}
3	{3,1,0,entry}	{3,0,entry}
4	{4,0,entry}	{4,0,entry}
5	{5,4,0,entry}	{5,4,0,entry}
exit	{exit,3,1,0,entry}	{exit,3,0,entry}

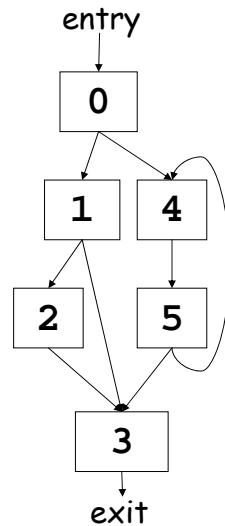


Update rule:

$$D[n] = \{n\} \cup \left(\bigcap_{p \in \text{pred}(n)} D[p] \right)$$

Example

block	Second Pass D[n]	Third Pass D[n]
entry	{entry}	{entry}
0	{0,entry}	{0,entry}
1	{1,0,entry}	{1,0,entry}
2	{2,1,0,entry}	{2,1,0,entry}
3	{3,0,entry}	{3,0,entry}
4	{4,0,entry}	{4,0,entry}
5	{5,4,0,entry}	{5,4,0,entry}
exit	{exit,3,0,entry}	{exit,3,0,entry}



Update rule:

$$D[n] = \{n\} \cup \left(\bigcap_{p \in \text{pred}(n)} D[p] \right)$$

Computing dominators

- Iterative algorithm is $O(n^2e)$
 - assuming bit vector sets
- More efficient algorithm due to Lengauer and Tarjan
 - $O(e \cdot \alpha(e, n))$ *inverse Ackermann*
 - much more complicated
 - your book provides a simple algorithm that is very fast in practice
 - faster than Tarjan algorithm for any realistic CFG

Computing dominators

- Let $sD[n]$ be the set of blocks that strictly dominate n , then

$$sD[n] = D[n] - \{n\}$$

- To compute $iD[n]$, the set of blocks (size ≤ 1) that immediately dominate n

$$iD[n] = sD[n]$$

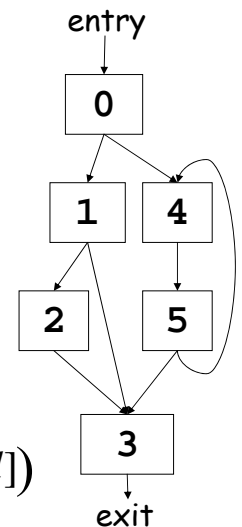
- Set

- Repeat until no $iD[n]$ changes:

$$iD[n] = iD[n] - \bigcup_{d \in iD[n]} sD[d]$$

Example

block	Initialization $iD[n]=sD[n]$	First Pass $iD[n]$
entry	{}	{}
0	{entry}	
1	{0,entry}	
2	{1,0,entry}	
3	{0,entry}	
4	{0,entry}	
5	{4,0,entry}	
exit	{3,0,entry}	



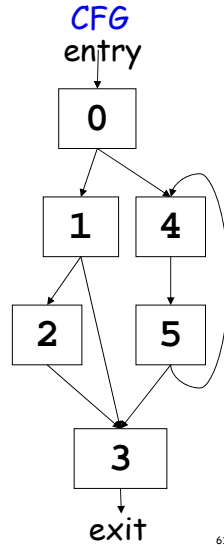
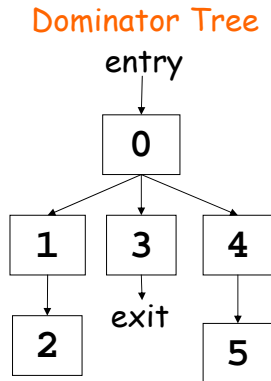
Update rule:

$$iD[n] = iD[n] - \bigcup_{d \in iD[n]} sD[d]$$

Dominator Tree

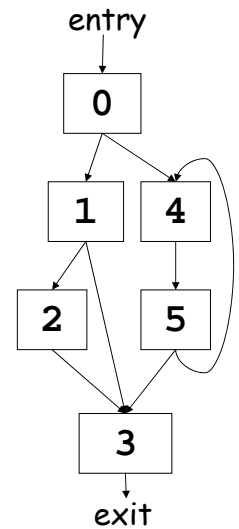
In the **dominator tree** the initial node is the entry block, and the parent of each other node is its **immediate dominator**.

block	iD[n]
entry	{}
0	{entry}
1	{0}
2	{1}
3	{0}
4	{0}
5	{4}
exit	{3}



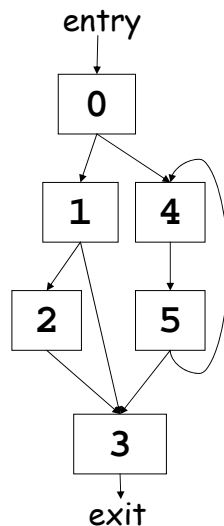
Post-Dominance

- Block **a** post-dominates **b** (**a pdom b**) if every path from **a** to the exit block includes **b**
- pdom** on CFG is the same as **dom** on the reverse (all edges reversed) CFG
- 0** post-dominates ?
- 1** post-dominates ?
- 4** post-dominates ?



Dominance Frontier

- If **z** is the first node we encounter on the path from **x** which **x** does not *strictly* dominate, **z** is in the dominance frontier of **x**
- For some path from node **x** to **z**, $x \rightarrow \dots \rightarrow y \rightarrow z$ where $x \text{ dom } y$ but not $x \text{ sdom } z$.
- Dominance frontier of **1**?
- Dominance frontier of **2**?
- Dominance frontier of **4**?



Calculating the Dominance Frontier

- Let **dominates[n]** be the set of all blocks which block **n** dominates
 - subtree of dominator tree with **n** as the root
- The dominance frontier of **n**, **DF[n]** is

$$DF[n] = \left(\bigcup_{s \in \text{dominates}[n]} \text{Uccs}(s) \right) - (\text{dominates}[n] - \{n\})$$

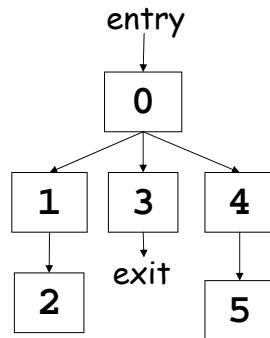
Skip example

Example

First calculate $\text{dominates}[n]$ from the dominator tree

block	$\text{dominates}[n]$
entry	{entry,0,1,2,3,4,5,exit}
0	{0,1,2,3,4,5,exit}
1	{1,2}
2	{2}
3	{3,exit}
4	{4,5}
5	{5}
exit	{exit}

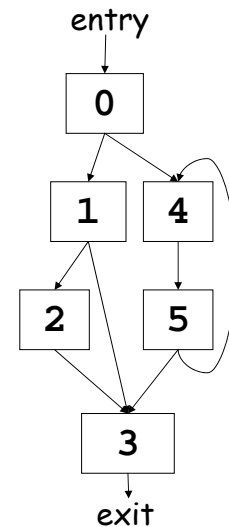
Dominator Tree



Example

Then compute the successor set of $\text{dominates}[n]$

block	$\text{dominates}[n]$	$\text{succ}(\text{dominates}[n])$
entry	{entry,0,1,2,3,4,5,exit}	
0	{0,1,2,3,4,5,exit}	
1	{1,2}	
2	{2}	
3	{3,exit}	
4	{4,5}	
5	{5}	
exit	{exit}	{}



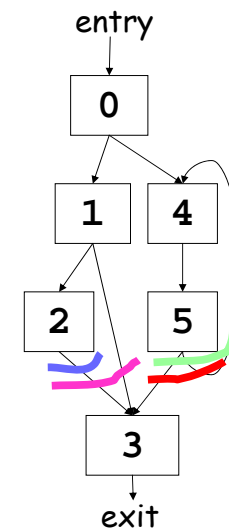
Example

Finally, remove all the blocks from the successor set that are strictly dominated by n to get $\text{DF}[n]$

block	$\text{sdominates}[n]$	$\text{succ}(\text{dominates}[n])$	$\text{DF}[n]$
entry	{entry,0,1,2,3,4,5,exit}	{0,1,2,3,4,5,exit}	
0	{0,1,2,3,4,5,exit}	{1,2,3,4,5,exit}	
1	{1,2}	{2,3}	
2	{2}	{3}	
3	{3,exit}	{exit}	
4	{4,5}	{3,4,5}	
5	{5}	{3,4}	
exit	{exit}	{}	{}

Example

block	$\text{DF}[n]$
entry	{}
0	{}
1	{3}
2	{3}
3	{}
4	{3,4}
5	{3,4}
exit	{}



Recap

- $a \text{ dom } b$
 - every possible execution path from *entry* to b includes a
- $a \text{ sdom } b$
 - $a \text{ dom } b$ and $a \neq b$
- $a \text{ idom } b$
 - a is "closest" dominator of b
- $a \text{ pdom } b$
 - every path from a to the exit block includes b
- Dominator trees
- Dominance frontier

Using DF to compute SSA

- place all $\Phi()$
- Rename all variables

Using DF to Place $\Phi()$

- Gather all the defsites of every variable
- Then, for every variable
 - foreach defsite
 - foreach node in $DF(\text{defsite})$
 - if we haven't put $\Phi()$ in node put one in
 - If this node didn't define the variable before: add this node to the defsites
- This essentially computes the Iterated Dominance Frontier on the fly, inserting the minimal number of $\Phi()$ necessary

Using DF to Place $\Phi()$

```
foreach node n {
  foreach variable v defined in n {
    orig[n]  $\cup$ = {v}
    defsites[v]  $\cup$ = {n}
  }
  foreach variable v {
    W = defsites[v]
    while W not empty {
      foreach y in  $DF[n]$ 
        if  $y \notin PHI[v]$  {
          insert " $v \leftarrow \Phi(v,v,...)$ " at top of y
           $PHI[v] = PHI[v] \cup \{y\}$ 
          if  $v \notin orig[y]$ :  $W = W \cup \{y\}$ 
        }
      }
    }
  }
}
```

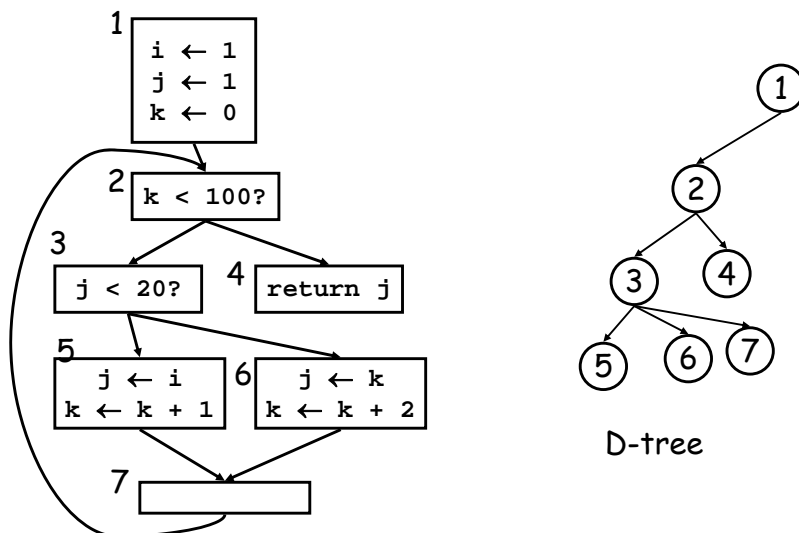
Renaming Variables

- Walk the D-tree, renaming variables as you go
- Replace uses with more recent renamed def
 - For straight-line code this is easy
 - If there are branches and joins?

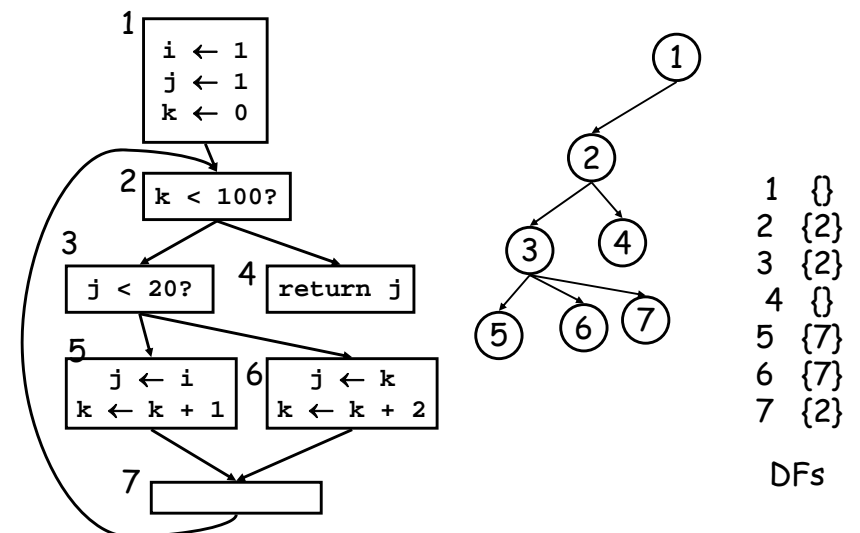
Renaming Variables

- Walk the D-tree, renaming variables as you go
- Replace uses with more recent renamed def
 - For straight-line code this is easy
 - If there are branches and joins use the closest def such that the def is above the use in the D-tree
- Easy implementation:
 - for each var: rename (v)
 - rename(v): replace uses with top of stack at def: push onto stack call rename(v) on all children in D-tree for each def in this block pop from stack

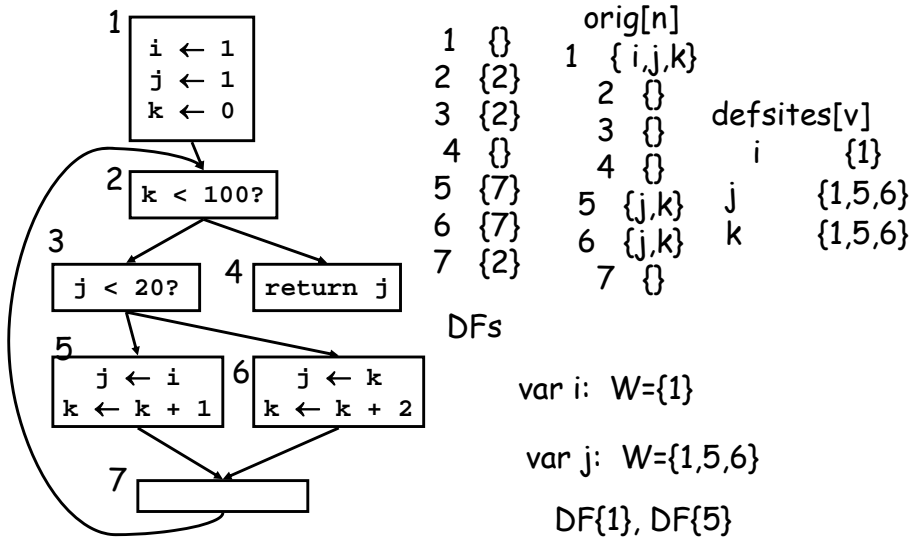
Compute D-tree



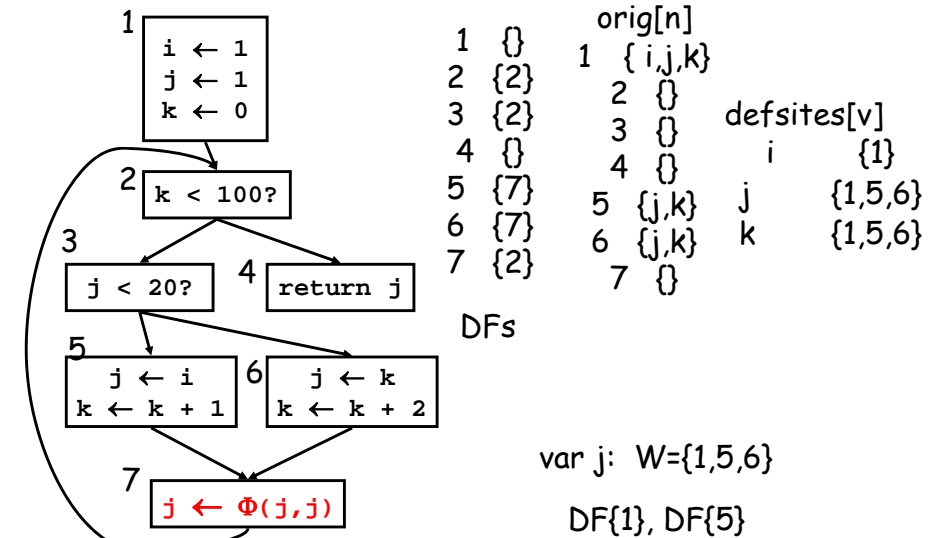
Compute Dominance Frontier



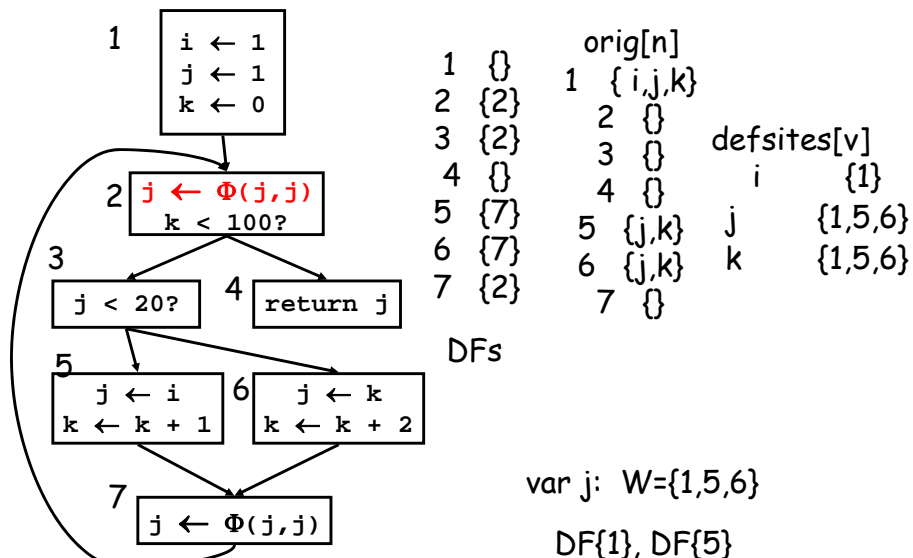
Insert $\Phi()$



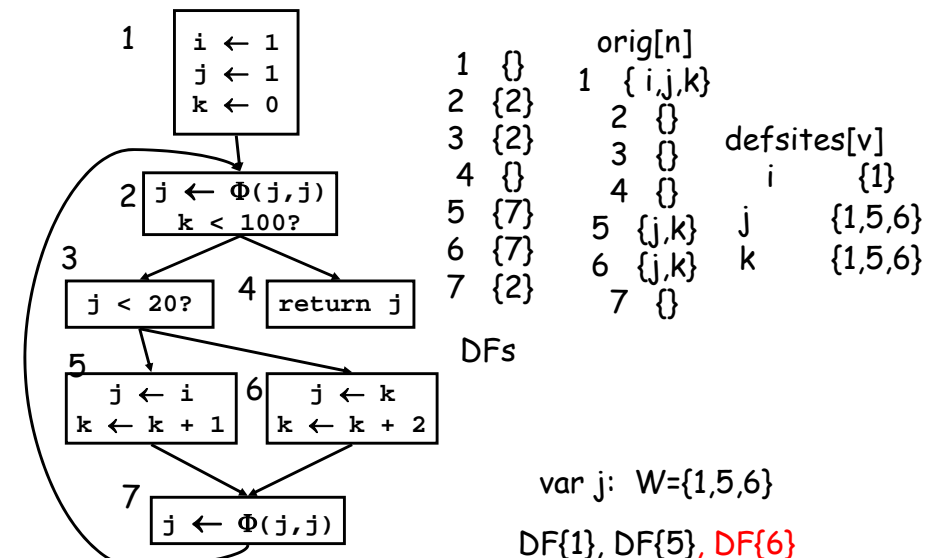
Insert $\Phi()$



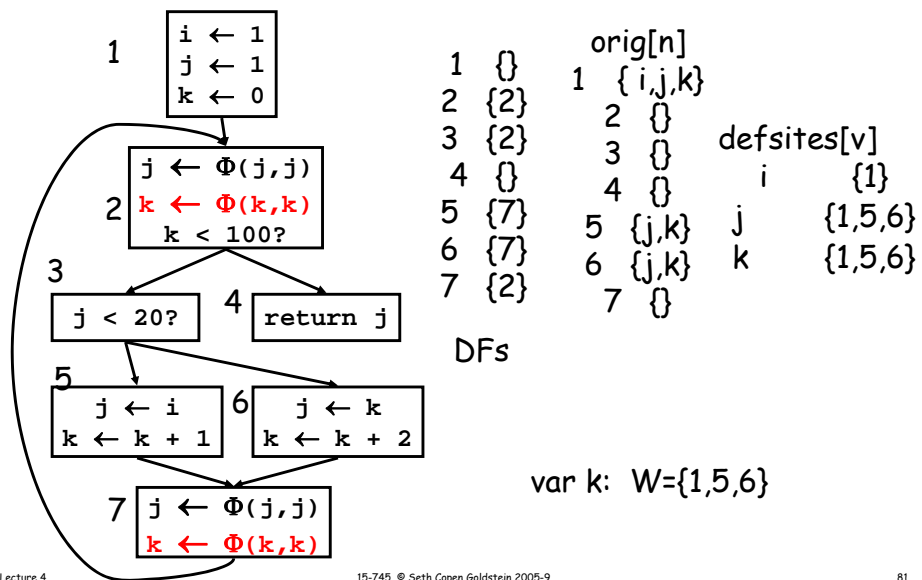
Insert $\Phi()$



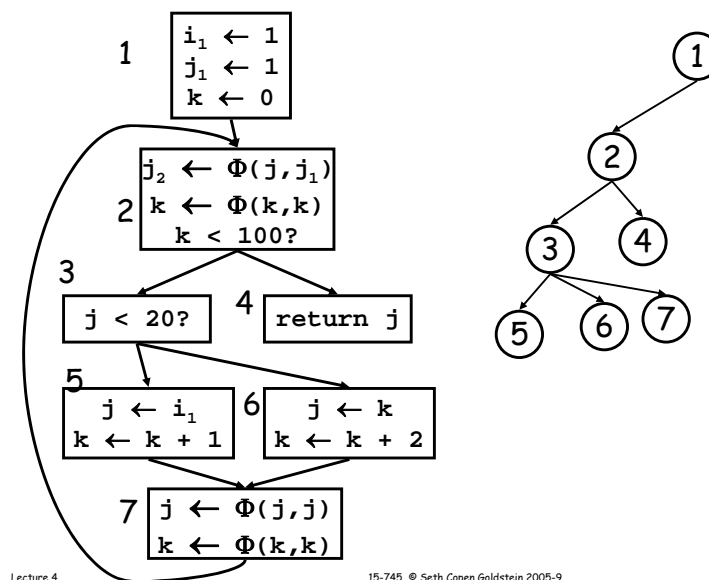
Insert $\Phi()$



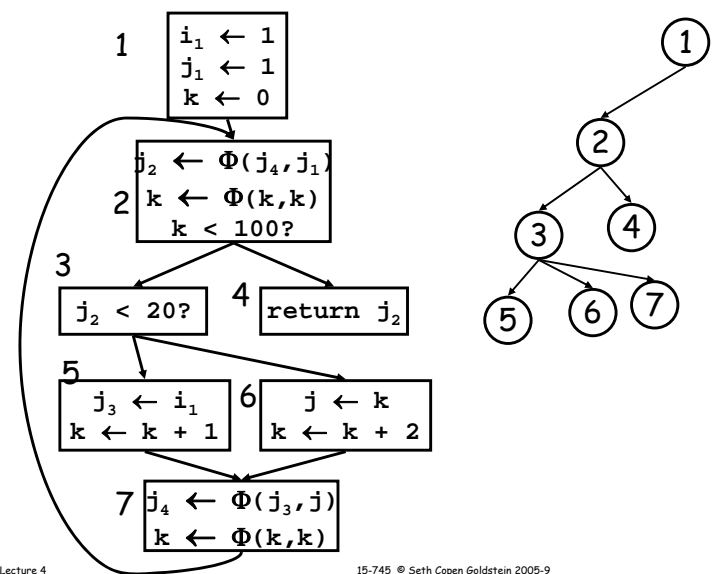
Insert $\Phi()$



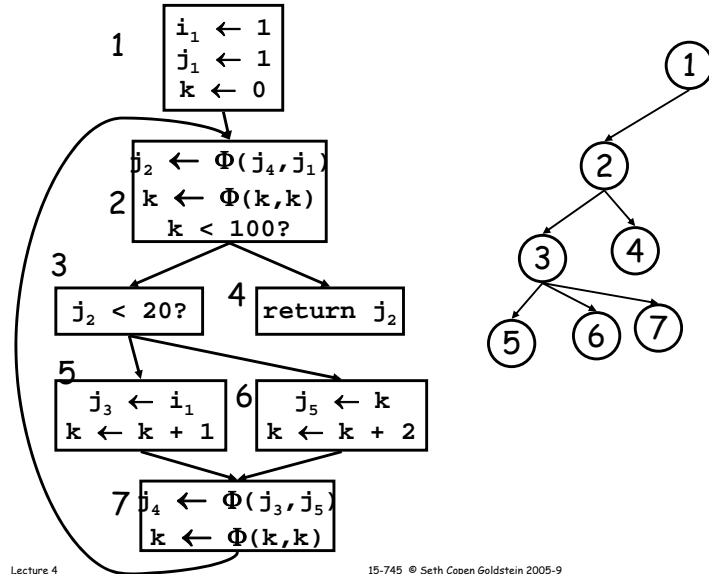
Rename Vars



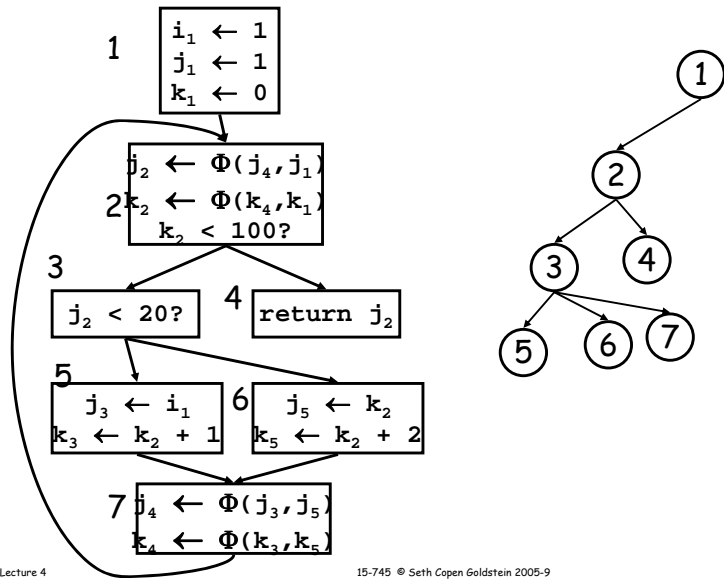
Rename Vars



Rename Vars



Rename Vars



SSA Properties

- Only 1 assignment per variable
- definitions dominate uses

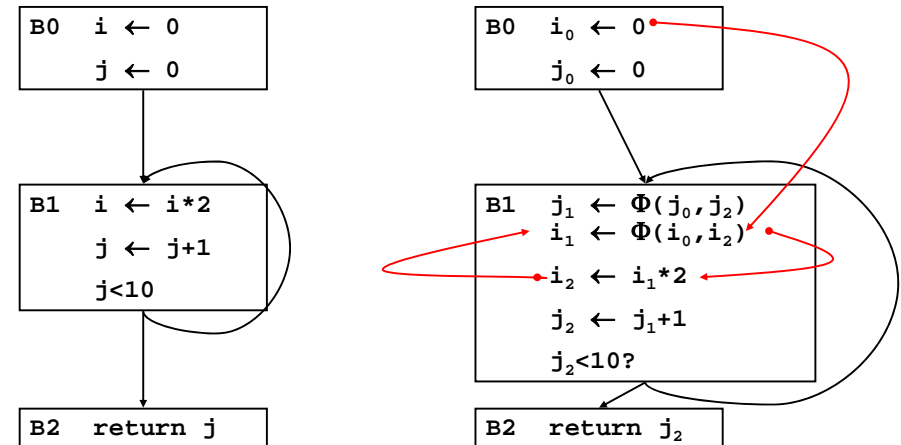
Dead Code Elimination

```

W ← list of all defs
while !W.isEmpty {
  Stmt S ← W.removeOne
  if |S.users| != 0 then continue
  if S.hasSideEffects() then continue
  foreach def in S.definers {
    def.users ← def.users - {S}
    if |def.uses| == 0 then
      W ← W UNION {def}
  }
  delete S
}
    
```

Since we are using SSA, this is just a list of all variable assignments.

Example DCE



Standard DCE leaves Zombies!

Aggressive Dead Code Elimination

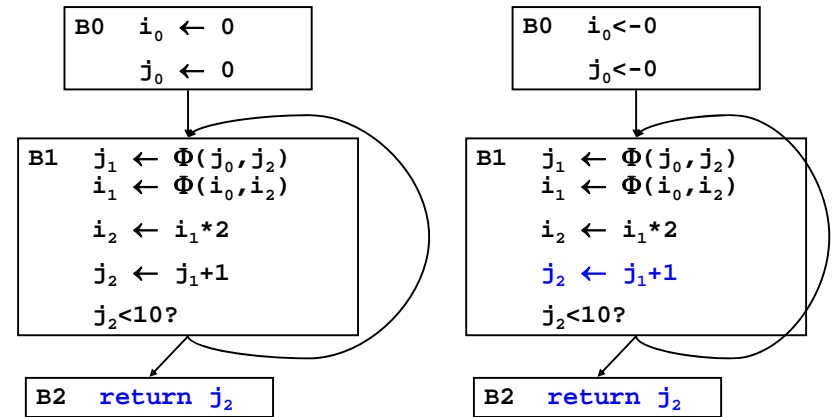
Assume a stmt is dead until proven otherwise.

```

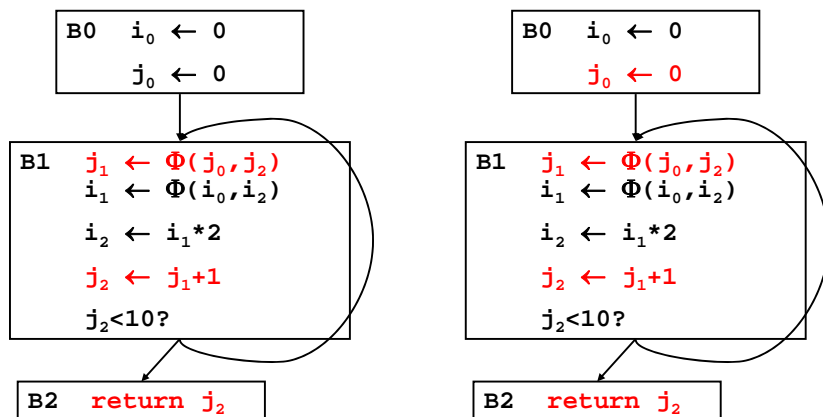
init:
  mark as live all stmts that have side-effects:
  - I/O
  - stores into memory
  - returns
  - calls a function that MIGHT have side-effects
  As we mark S alive, insert S.defs into W

while (|W| > 0) {
  S <- W.removeOne()
  if (S is alive) continue;
  mark S alive, insert S.defs into W
}
    
```

Example DCE



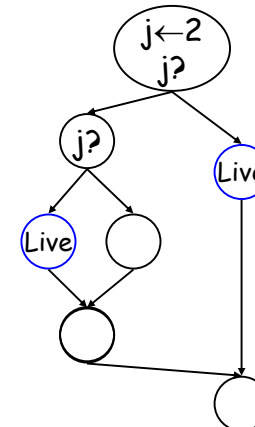
Example DCE



Problem!

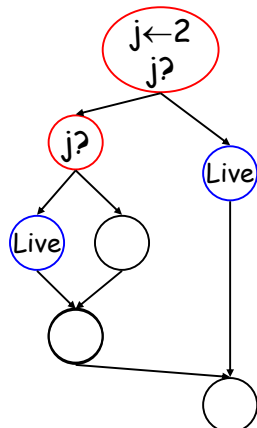
Fixing ADCE

- If S is live, then
If T determines if S can execute, T should be live



Fixing DCE

- If S is live, then
If T determines if S can execute, T should be live



Lecture 4

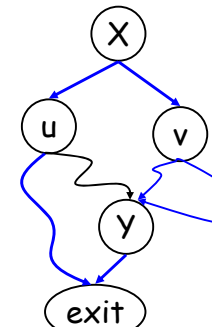
15-745 © Seth Copen Goldstein 2005-9

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Control Dependence

- Y is control-dependent on X if
 - X branches to u and v
 - \exists a path $u \rightarrow \text{exit}$ which does not go through Y
 - \forall paths $v \rightarrow \text{exit}$ go through Y

IOW, X can determine whether or not Y is executed.



Lecture 4

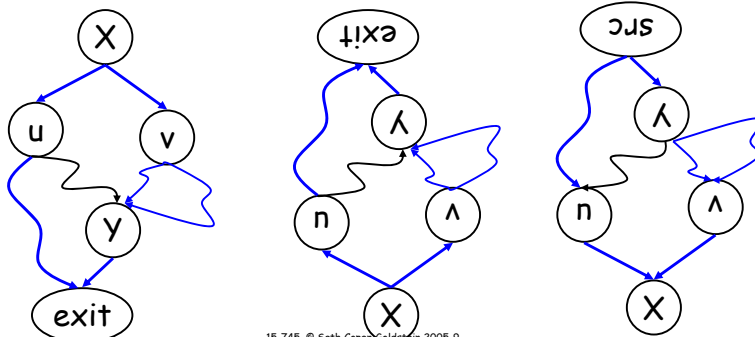
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Finding the CDG

- Y is control-dependent on X if
 - X branches to u and v
 - \exists a path $u \rightarrow \text{exit}$ which does not go through Y
 - \forall paths $v \rightarrow \text{exit}$ go through Y

IOW, X can determine whether or not Y is executed.



Lecture 4

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Finding the CDG

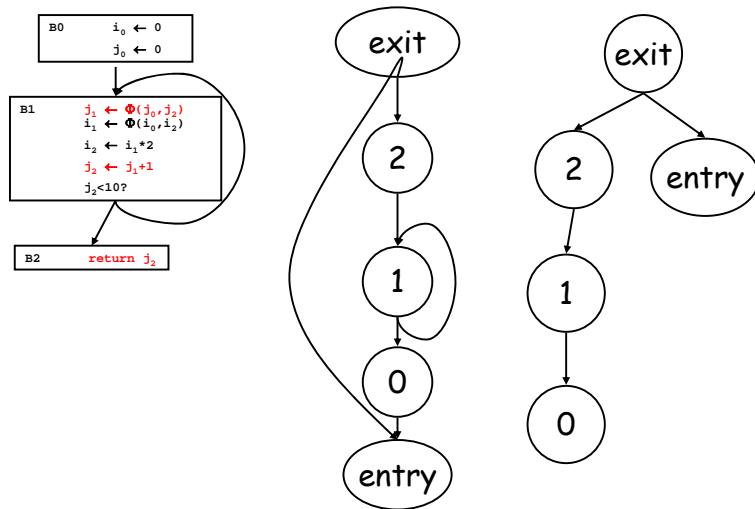
- Construct CFG
- Add entry node and exit node
- Add (entry, exit)
- Create G' , the reverse CFG
- Compute D-tree in G' (post-dominators of G)
- Compute $DF_{G'}(y)$ for all $y \in G'$ (post-DF of G)
- Add $(x, y) \in G$ to CDG if $x \in DF_{G'}(y)$

Lecture 4

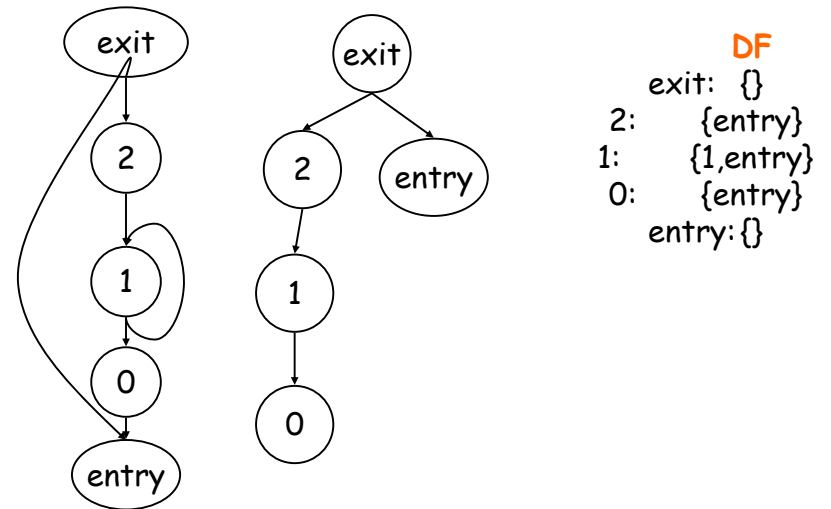
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CDG of example



CDG of example



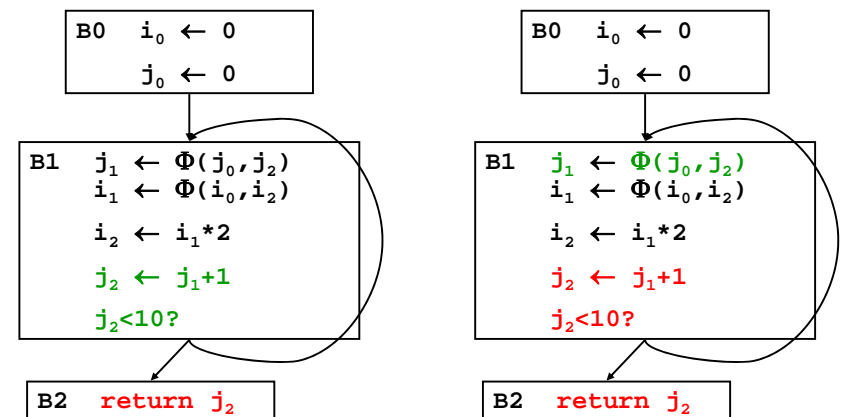
Aggressive Dead Code Elimination

Assume a stmt is dead until proven otherwise.

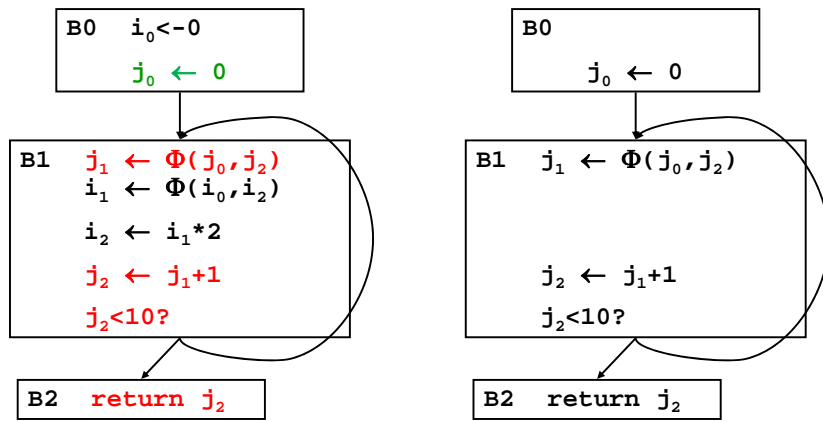
```

while (|W| > 0) {
  S ← W.removeOne()
  if (S is alive) continue;
  mark S alive, insert
  - forall operands, S.operand.definers into W
  - S.CD-1 into W
}
  
```

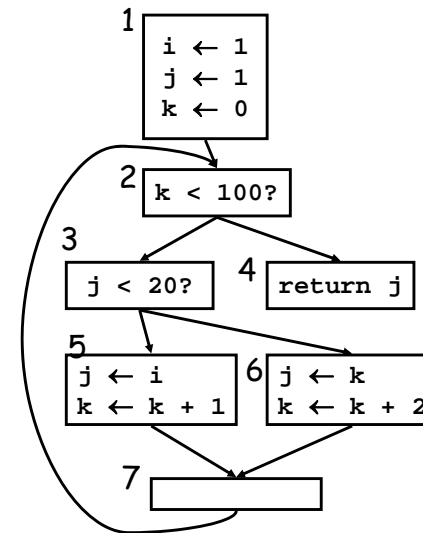
Example DCE



Example DCE

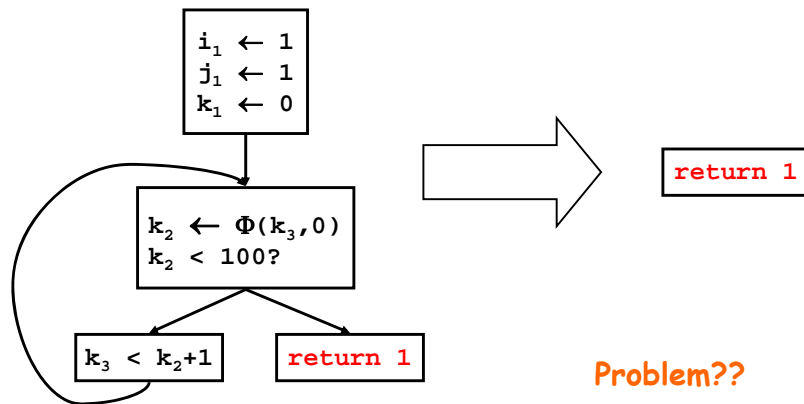


CCP Example



- Does block 6 ever execute?
- Simple CP can't tell
- CCP can tell:
 - Assumes blocks don't execute until proven otherwise
 - Assumes Values are constants until proven otherwise

CCP → DCE



Problem??

Whew!

- SSA: 1 assignment per variable. Defs dom uses
- Minimal SSA, Phi-functions, variable relabeling
- Dominators, dominator trees, dominance frontier
- CCP
- ADCE
- Control dependence