

# 15-745

## Introduction

Seth Copen Goldstein  
Seth@cs.cmu.edu  
CMU

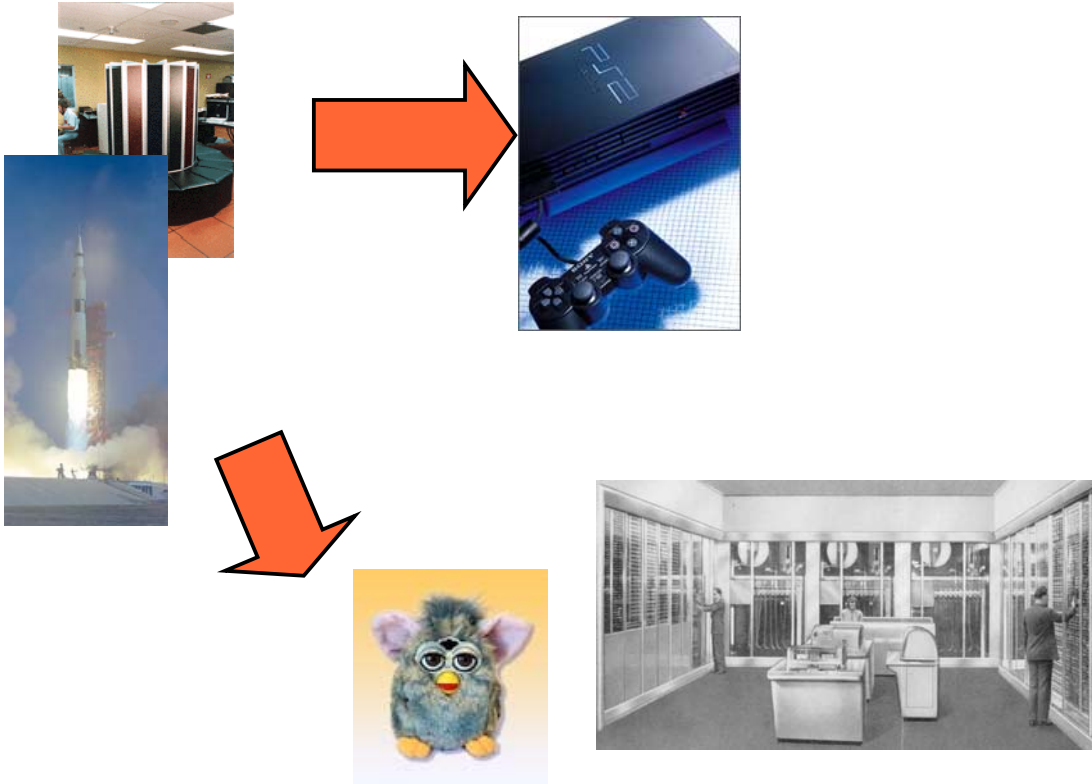
Based in part on slides by  
Todd Mowry and Michael Voss

## Introduction

- Why study compilers?
- Administrivia
- Structure of a Compiler
- Optimization Example

Reference: Muchnick 1.3-1.5

# Moore's Law



lecture 1, 15-745

© 2002-7 Seth Copen Goldstein

3

# Moore's Law

Imagine: Computers that

- 
- 
- 
- 

Imagining it is hard enough,  
achieving it requires a rethink of  
the entire tool chain.

computers from atomic scale components

lecture 1, 15-745

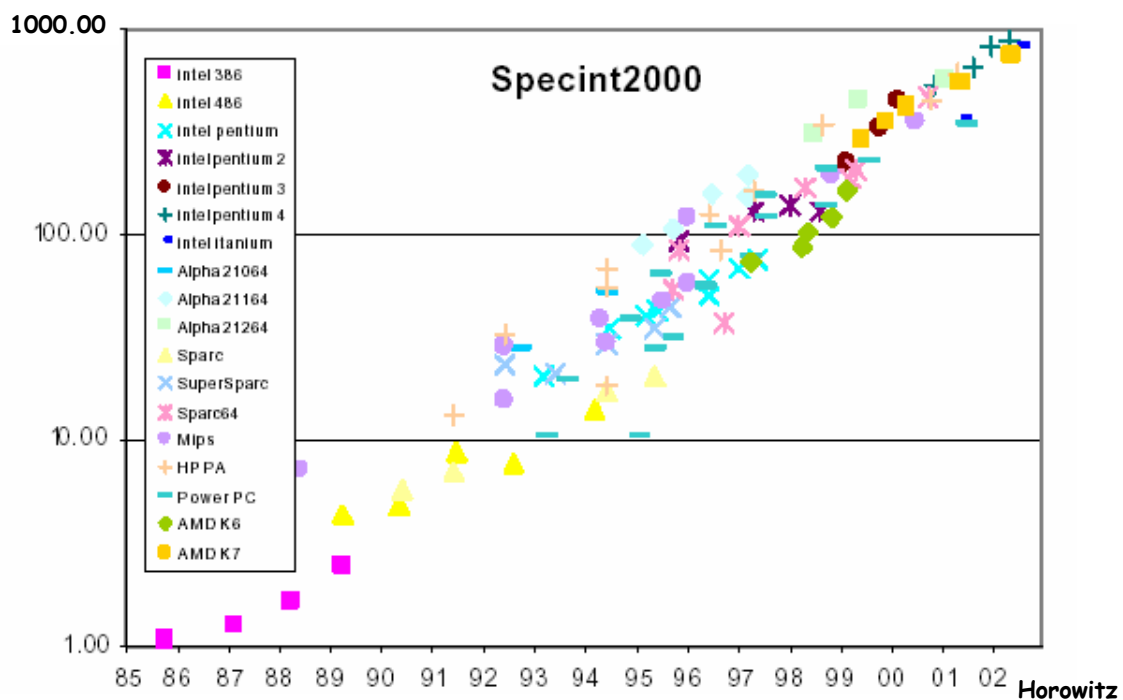
© 2002-7 Seth Copen Goldstein

4

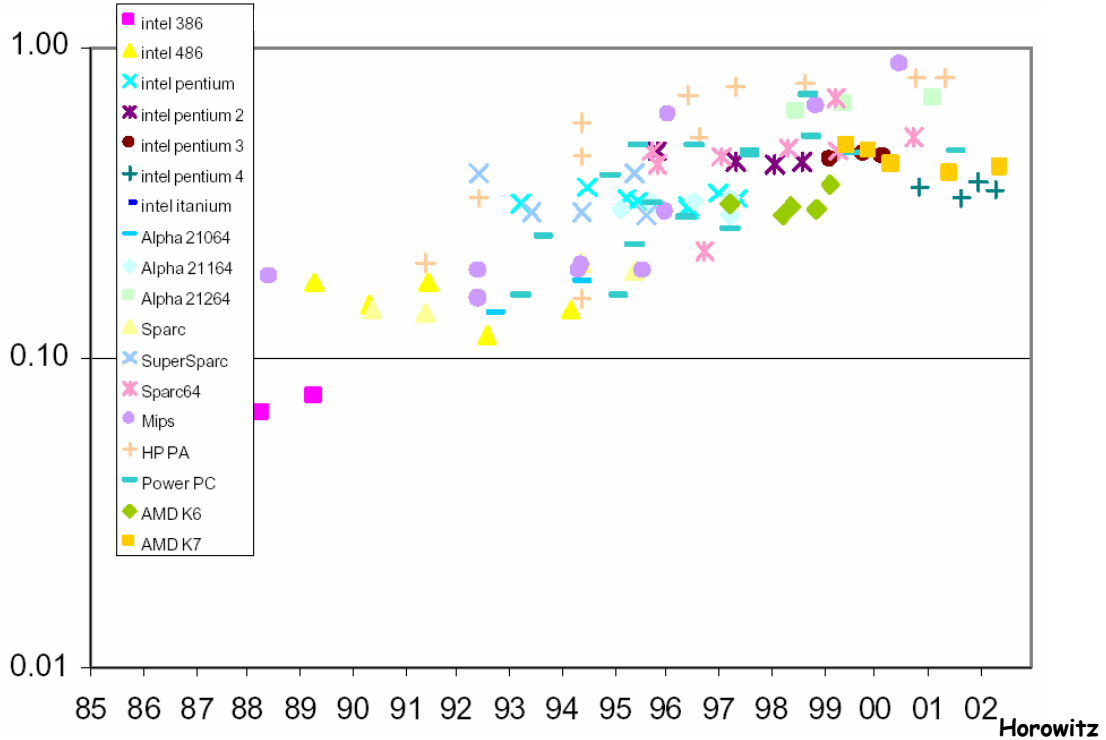
# What is Behind Moore's Law?

- A lot of hard work!
- Two most important tools:
  - Parallelism
    - Bit-level
    - Pipeline
    - Function unit
    - Multi-core
  - Locality

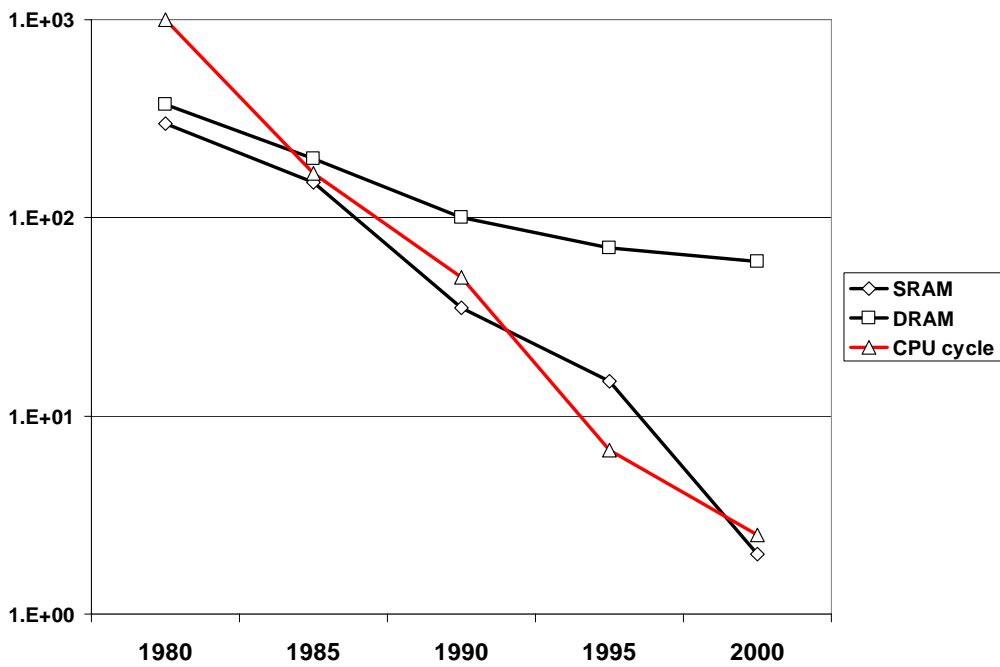
## Performance: Ops/Clk \* Clks/Sec



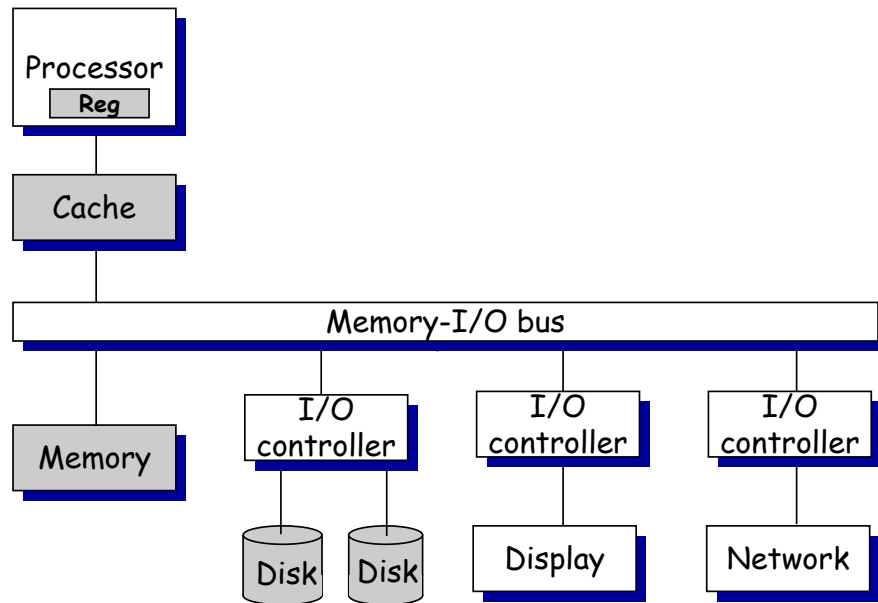
# SpecInt/Mhz



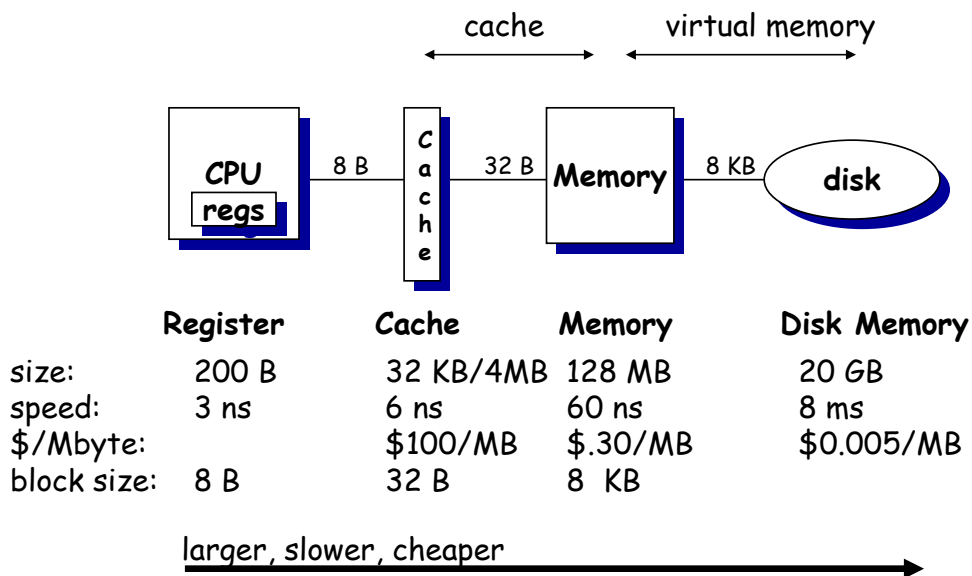
# Another View of Moore's Law



# The Computer System



# The Memory Hierarchy



# Compiler Writer's Job

- Improve locality
- Increase parallelism
- Tolerate latency
- Reduce power

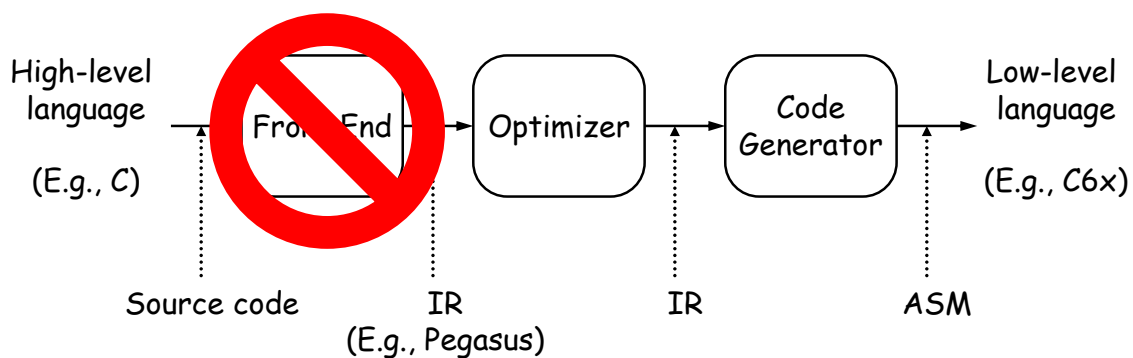
## Why study compilers

- They are really amazing
- Combines theory & practice
  - CS is about abstraction
    - Primary abstraction: programming language
    - Compiler lowers PL to ISA (or further!)
  - Compiler is a big system
- Crucial for performance
  - especially for modern processors
  - practically part of the architecture
- I bet: Everyone will write a compiler

# Why study compilers

- They are really amazing
- Combines theory & practice
  - CS is about abstraction
    - Primary abstraction: programming language
    - Compiler lowers PL to ISA (or further!)
  - Compiler is a big system
- Crucial for performance
  - especially for modern processors
  - practically part of the architecture
- I bet: **Everyone** will write a compiler

## What this course is about



- Theory and practice of modern optimizing compilers
  - No lexing or parsing
  - Focus on IR, back-end, optimizations
- Internals of today's (and tomorrow's) compilers
- Building a real compiler for embedded processor

# Prerequisites

- 211 & 213 or the equivalent
- Parts of 411 or the equivalent
  - Basic compiler data structures
  - Frames, calling conventions, def-use chains, etc.
  - Don't really care about front-end
- Proficient in C/C++ programming
- Basic understanding of architecture

# My Expectations

- You have the prerequisites
  - If not come see tim or me asap
- 4 assignments + a project
- Class participation
  - THIS IS A MUST!
  - Read text/papers before class
  - Attendance is essentially mandatory



# Grading

- Class participation ~20%
  - Throughout the semester
  - During paper presentations
  - Project presentations
- Labs ~20%
- Project ~30%
- Midterm ~15%
- Final ~15%

# Grading

- Class participation ~20%
  - Throughout the semester
  - During paper presentations
  - Project presentations
- Labs ~25%
- Project ~35%
- Midterm ~20%

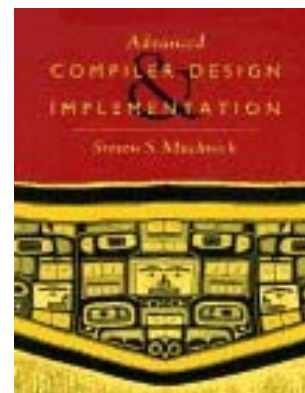
# Labs

- ADCE & CCP in Pegasus
- Global register allocation
- Global Code Scheduling
- Profile-based optimization
  
- All labs and the final project will be done in a state-of-the-art research compiler.



# The Text

- Steven S. Muchnick, *Advanced Compiler Design and Implementation*. Morgan Kaufmann Publishers, 1997
  
- Papers will be assigned



## Before we get too bored

- More admin at the end, but first ...
- What exactly is an optimizing compiler?
  - An optimizing compiler transforms a program into an equivalent, but "better" form.
  - What is equivalent?
  - What is better?

## Full Employment Theorem

- No such thing as "The optimizing compiler"
  - Why not?
- There is **always a better** optimizing compiler, but ...
  - Compiler must preserve correctness
  - On average improve X, where X is:
    - Performance
    - Power
    - ...
  - Finish in your lifetime

# How might performance be improved?

$$\text{execution time} = \frac{\sum \text{cycles per instruction}}{\text{instructions}}$$

- Reduce the number of instructions
- Replace "expensive" instructions with "cheap" ones
- Reduce memory cost
  - Improve locality
  - Reduce # of memory operations
- Increase parallelism

## Ingredients to a compiler opt

- Identify opportunity
  - Avail in many programs
  - Occurs in key areas (what are these?)
  - Amenable to "efficient" algorithm
- Formulate Problem
- Pick a Representation
- Develop an Analysis
  - Detect when legal
  - And desirable
- Implement Code Transformation
- Evaluate (and repeat!)

# Examples of Optimizations

- Machine Independent
  - Algebraic simplification
  - Constant propagation
  - Constant folding
  - Common Sub-expression elimination
  - Dead Code elimination
  - Loop Invariant code motion
  - Induction variable elimination
- Machine Dependent
  - Jump optimization
  - Reg allocation
  - Scheduling
  - Strength reduction

## Really Powerful Opts we won't do

- How to optimize:

```
Sumfrom1toN(int max) {  
    sum = 0;  
    for (i=1; i<=max; i++) sum+=i;  
    return sum;  
}
```

# Really Powerful Opts we won't do

- How to optimize:

```
Sumfrom1toN(int max) {  
    sum = 0;  
    for (i=1; i<=max; i++) sum+=i;  
    return sum;  
}
```

- What we should, but won't do:

```
inline sumfrom1toN(int max) {  
    return max > 0 ?  
        ((max+max*max)>>1) : 0;  
}
```

## Algebraic Simplifications

$$a * 1; \Rightarrow a$$

$$a / 1; \Rightarrow a$$

$$a * 0; \Rightarrow 0$$

$$a + 0; \Rightarrow a$$

$$a - 0; \Rightarrow a$$

$$\begin{array}{l} a = b + 1 \\ c = a - 1 \end{array} \Rightarrow c = b$$

Use algebraic identities to simplify computations

# Jump Optimizations

```
    cmp d0,d1                cmp d0,d1
    beq  L1                    bne  L2
    bra  L2                    L1:      :
                                :      :
L1:      :                    L2:      :
    :                          :
    :
```

Simplify jump and branch instructions.

# Constant Propagation

```
    a = 5;                    a = 5;
    b = 3;                    b = 3;
    :                          :
    :                          :
n = a + b;                    n = 5 + 3;
for (i = 0; i<n; ++i)        for (i = 0; i<n; ++i)
{                               {
    :                             :
}                               }
```

If the compiler can determine that the values of `a` and `b` are constants, then it can replace the variable uses with constant values.

# Constant Folding

```
    :  
    :  
    :  
    :  
n = 8 ;  
for (i = 0 ; i < 8 ; ++i) {  
    :  
}
```

- The compiler evaluates an expression (at compile time) and inserts the result in the code.
- Can lead to further optimization opportunities; esp. constant propagation.

## Common Subexpression Elimination (CSE)

```
    a = c*d;  
    :  
    :  
d = (c*d + t) * u      ⇒      a = c*d;  
                                :  
                                :  
d = (a + t) * u
```

If the compiler can determine that:

- an expression was previously computed
- and that the values of its variables have not changed since the previous computation,

Then, the compiler can use the previously computed value.



## Strength Reduction

- On some processors, the cost of an addition is less than the cost of multiplication.
- The compiler can replace expensive multiplication instructions by less expensive ones.

```
c = b * 2;
```

```
move $2000, d0
muls #2, d0
move d0, $3000
```

```
c = b + b;
```

```
move $2000, d0
add d0, d0
move d0, $3000
```

```
c = lsh(b);
```

```
move $2000, d0
lsl #1, d0
move d0, $3000
```

```
c = -1*b;
```

```
move $2000, d0
muls #-1, d0
move d0, $3000
```

```
c = negative(b);
```

```
move $2000, d0
neg d0
move d0, $3000
```

## Dead Code Elimination

```
debug = False;
:
:
if (debug) {
:
:
}
a = f(b);
```

If the compiler can determine that code will never be executed or that the result of a computation will never be used, then it can eliminate the code or the computation.

# Loop Invariant Code Motion

```
for (i=0; i<100 ; ++i) {
  for (j=0; j<100 ; ++j) {
    for (k=0 ; k<100 ; ++k)
    {
      a[i][j][k] = i*j*k;
    }
  }
}
```

```
for (i=0; i<100 ; ++i) {
  for (j=0; j<100 ; ++j) {
    t1 = a[i][j];
    t2 = i*j;
    for (k=0 ; k<100 ; ++k)
    {
      t1[k] = t2*k;
    }
  }
}
```

- Loop invariant: expression evaluates to the same value each iteration of the loop.
- Code motion: move loop invariant outside loop.
- Very important because inner-most loop executes most frequently.

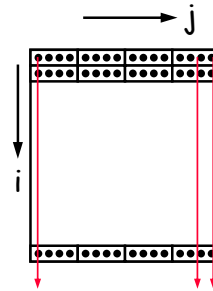
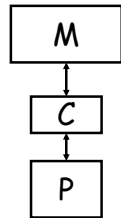
# Loop Invariant Code Motion

```
int *a;
int n;
:
:
scanf("%d", &n);
for (i=0; i<n ; ++i) {
  for (j=0; j<n ; ++j) {
    for (k=0 ; k<n ; ++k)
    {
      f = q/p;
      a[i][j][k] = f*i*j*k;
    }
  }
}
```

```
int *a;
int n;
:
:
scanf("%d", &n);
f = q/p;
for (i=0; i<n ; ++i) {
  for (j=0; j<n ; ++j) {
    t1 = a[i][j];
    t2 = i*j;
    for (k=0 ; k<n ; ++k)
    {
      t1[k] = f*t2*k;
    }
  }
}
Ooops!!!!
```

# Cache Optimizations

```
for (j=0; j<n ; ++j) {  
  for (i=0; i<n ; ++i) {  
    x += a[i][j];  
  }  
}
```

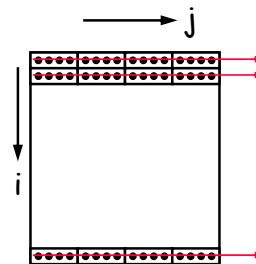
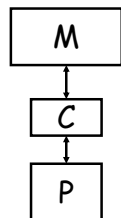


**Loop permutation** changes the order of the loops to improve the spatial locality of a program.

# Cache Optimizations

```
for (j=0; j<n ; ++j) {  
  for (i=0; i<n ; ++i) {  
    x += a[i][j];  
  }  
}
```

```
for (i=0; i<n ; ++i) {  
  for (j=0; j<n ; ++j) {  
    x += a[i][j];  
  }  
}
```



**Loop permutation** changes the order of the loops to improve the spatial locality of a program.

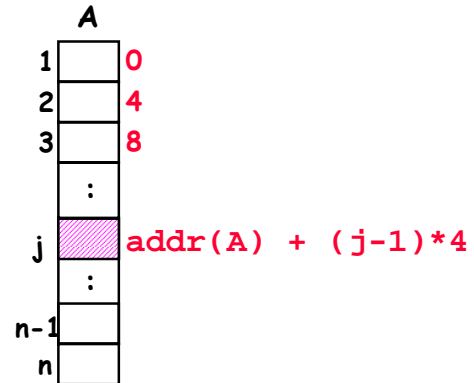
# Example

A program that sorts 4-byte elements in an n-element array of integers  $A[1..n]$  using **bubblesort**.

```

for (i=n-1; i >= 1 ; --i) {
  for (j = 1; j <= i ; ++j) {
    if (A[j] > A[j+1]) {
      temp = A[j];
      A[j] = A[j+1];
      A[j+1] = temp;
    }
  }
}
// i and j are not used later

```



## A Generated IR

```

for i {
  i = n-1
  s5: if i < 1 goto Exit
  for j {
    j = 1
    s4: if j > i goto S2
    A[j] {
      t1 = j-1
      t2 = 4*t1
      t3 = [A+t2]
    }
    A[j+1] {
      t4 = j+1
      t5 = t4-1
      t6 = 4*t5
    }
    if {
      t7 = [A+t6]
      if t3 <= t7 goto S3
    }
    A[j] {
      t8 = j-1
      t9 = 4*t8
      temp = [A+t9]
    }
    s3: j = j+1
    goto S4
  }
  s2: i = i-1
  goto S5
}
Exit:

```

Annotations for the IR code:

- $t10 = j+1$ ,  $t11 = t10-1$ ,  $t12 = 4*t11$ ,  $t13 = [A+t12]$  are grouped as  $A[j+1]$ .
- $t14 = j-1$ ,  $t15 = 4*t14$  are grouped as  $A[j]$ .
- $[A+t15] = t13$  is annotated as  $A[j]=A[j+1]$ .
- $t16 = j+1$ ,  $t17 = t16-1$ ,  $t18 = 4*t17$  are grouped as  $A[j+1]$ .
- $[A+t18] = temp$  is annotated as  $A[j+1]=temp$ .
- $s3: j = j+1$  and  $goto S4$  are grouped as **for j**.
- $s2: i = i-1$  and  $goto S5$  are grouped as **for i**.



# Optimizations II - CSE

```

i = n-1
S5: if i < 1 goto Exit
    j = 1
S4: if j > i goto S2
    t1 = j-1
    t2 = 4*t1
    t3 = [A+t2]
    t6 = 4*j
    t7 = [A+t6]
    if t3 <= t7 goto S3
    t8 = j-1
    t9 = 4*t8
    temp = [A+t9]

    t12 = 4*j
    t13 = [A+t12]
    t14 = j-1
    t15 = 4*t14
    [A+t15] = t13
    t18 = 4*j
    [A+t18] = temp
S3: j = j+1
    goto S4
S2: i = i-1
    goto S5
Exit:

```

Diagram showing Constant Symbolic Equivalence (CSE) boxes:

- `t14 = t1` (points to `t14 = j-1`)
- `t8 = t1` (points to `t8 = j-1`)

# Optimizations II - CSE

```

i = n-1
S5: if i < 1 goto Exit
    j = 1
S4: if j > i goto S2
    t1 = j-1
    t2 = 4*t1
    t3 = [A+t2]
    t6 = 4*j
    t7 = [A+t6]
    if t3 <= t7 goto S3
    t8 = t1
    t9 = 4*t8
    temp = [A+t9]

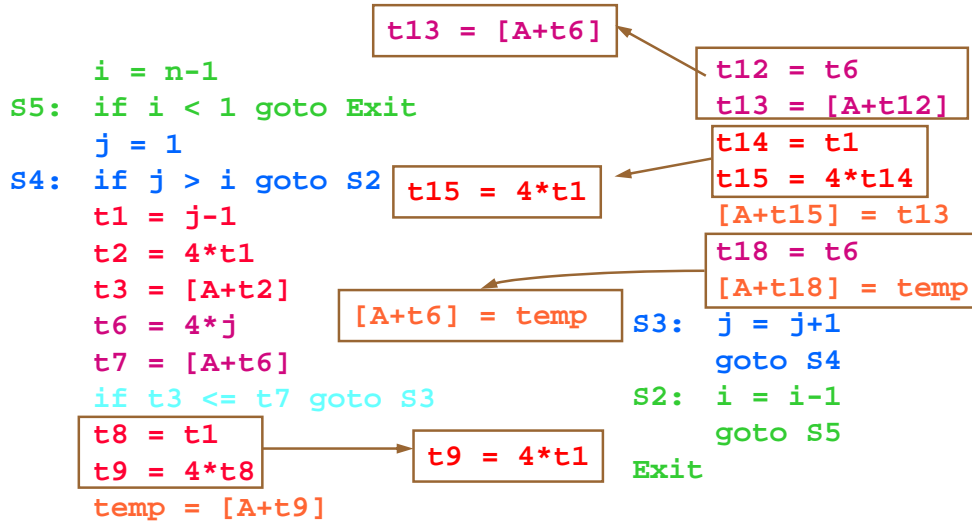
    t12 = 4*j
    t13 = [A+t12]
    t14 = t1
    t15 = 4*t14
    [A+t15] = t13
    t18 = 4*j
    [A+t18] = temp
S3: j = j+1
    goto S4
S2: i = i-1
    goto S5
Exit:

```

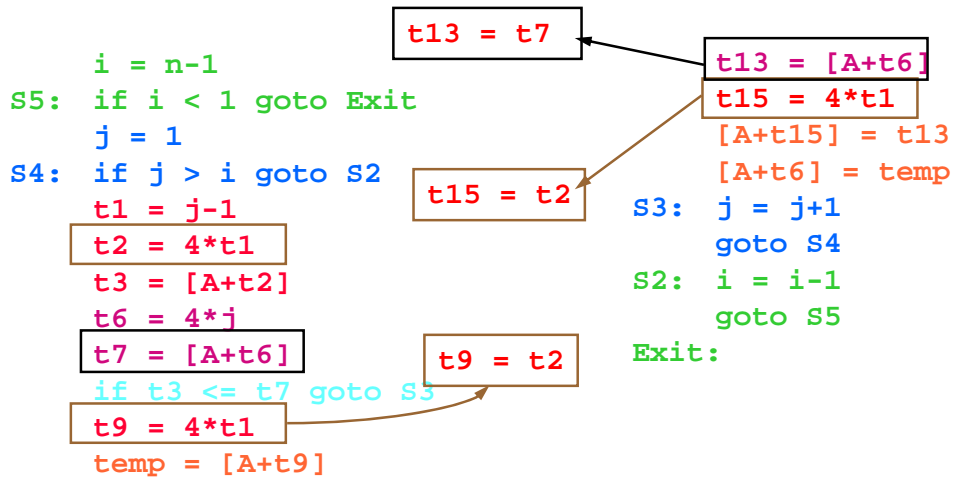
Diagram showing Constant Symbolic Equivalence (CSE) boxes:

- `t12 = t6` (points to `t12 = 4*j`)
- `t18 = t6` (points to `t18 = 4*j`)

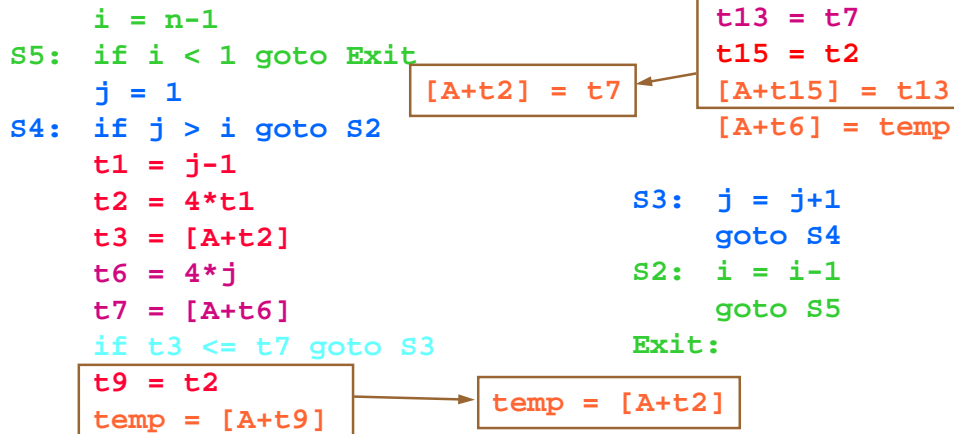
# Optimizations III - Copy Propagation



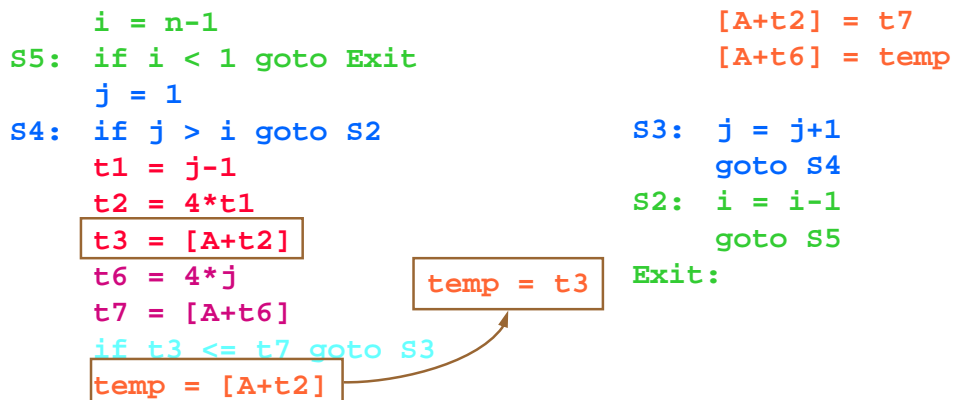
# Optimizations IV - CSE (2)



# Optimizations V - Copy Propagation (2)



# Optimization VI - CSE (3)





## Optimization VII - Copy Propagation (3)

```
    i = n-1
S5:  if i < 1 goto Exit
    j = 1
S4:  if j > i goto S2 [A+t6] = [t3]
    t1 = j-1
    t2 = 4*t1
    t3 = [A+t2]
    t6 = 4*j
    t7 = [A+t6]
    if t3 <= t7 goto S3
    temp = [t3]
S3:  j = j+1
    goto S4
S2:  i = i-1
    goto S5
Exit:
```

[A+t2] = t7  
[A+t6] = temp

## Optimizations VIII - IVE & Strength Reduction

```
    i = n-1
S5:  if i < 1 goto Exit
    j = 1
S4:  if j > i goto S2
    t1 = j-1
    t2 = 4*t1
    t3 = [A+t2]
    t6 = 4*j
    t7 = [A+t6]
    if t3 <= t7 goto S3
    [A+t2] = t7
    [A+t6] = t3
S3:  j = j+1
    goto S4
S2:  i = i-1
    goto S5
Exit:
```

# Optimizations VIII - IVE & Strength Reduction

```

i = n-1
S5: if i < 1 goto Exit
    j = 1
S4: if j > i goto S2
    t1 = j-1
    t2 = 4*t1
    t3 = [A+t2]
    t6 = 4*j
    t7 = [A+t6]
    if t3 <= t7 goto S3
    [A+t2] = t7
    [A+t6] = t3
S3: j = j+1
    goto S4
S2: i = i-1
    goto S5
Exit:
  
```

Loop Invariant  
Code Motion...

```

i = n-1
S5: if i < 1 goto Exit
    t2 = 0
    t6 = 4
S4: t19 = 4*i
    if t6 > t19 goto S2
    t3 = [A+t2]
    t7 = [A+t6]
    if t3 <= t7 goto S3
    [A+t2] = t7
    [A+t6] = t3
S3: t2 = t2+4
    t6 = t6+4
    goto S4
S2: i = i-1
    goto S5
Exit:
  
```

## Done?

```

i = n-1
S5: if i < 1 goto Exit
    t2 = 0
    t6 = 4
S4: t19 = 4*i
    if t6 > t19 goto S2
    t3 = [A+t2]
    t7 = [A+t6]
    if t3 <= t7 goto S3
    [A+t2] = t7
    [A+t6] = t3
S3: t2 = t2+4
    t6 = t6+4
    goto S4
S2: i = i-1
    goto S5
Exit:
  
```

$t19 = i*4$

$t19 < 4$

$[A-4+t6]$

$t19 = t19-4$

## Done?

```
i = n-1
t19 = i*4
S5: if t19 < 4 goto Exit
    t6 = 4
S4: if t6 > t19 goto S2
    t3 = [A+t6-4]
    t7 = [A+t6]
    if t3 <= t7 goto S3
    [A+t6-4] = t7
    [A+t6] = t3
S3: t6 = t6+4
    goto S4
S2: t19 = t19 - 4
    goto S5
Exit:
```

Eliminate mult,  
Use double load (if aligned?)  
Unroll?  
Eliminate jmp

...

## Done For Now.

```
i = n-1
t19 = i<<2
if t19 < 4 goto Exit
S5: t6 = 4
    if t6 > t19 goto S2
S4: t3 = [A+t6-4]
    t7 = [A+t6]
    if t3 <= t7 goto S3
    [A+t6-4] = t7
    [A+t6] = t3
S3: t6 = t6+4
    if t6 <= t19 goto S4
S2: t19 = t19 - 4
    if t19 >= 4 goto S5
Exit:
```

Inner loop: 7 instructions  
4 mem ops  
2 branches  
1 addition

Original inner loop: 25 instructions  
6 mem ops  
3 branches  
10 addition  
6 multiplication

# Course Schedule

- [www.cs.cmu.edu/afs/cs/academic/class/15745-s07h/www/](http://www.cs.cmu.edu/afs/cs/academic/class/15745-s07h/www/)
- The Web site is a vital resource
- Also, class newsgroup
- (And, of course us too)

# Course Staff

- Tim Callahan [www..../~tcal](http://www..../~tcal)
- Seth Goldstein [www..../~seth](http://www..../~seth)
- Mahim Mishra [www..../~mishra](http://www..../~mishra)
- Marilyn Walgora  
[mwalgora@cs.cmu.edu](mailto:mwalgora@cs.cmu.edu)