# 15-745 Instruction Scheduling Software Pipelining Copyright © Seth Copen Goldstein 2000-5 © Tim Callahan 2007 (some slides borrowed from M. Voss)

# Instruction-level Parallelism Most modern processors have the ability to execute several adjacent instructions simultaneously. Pipelined machines. Very-long-instruction-word machines (VLIW). Superscalar machines. Dynamic scheduling/out-of-order machines. ILP is limited by several kinds of *execution constraints*. Data dependence constraints. Resource constraints ("hazards") Control hazards

### **Execution** Constraints • Data-dependence constraints: - If instruction A computes a value that is read by instruction B, then B cannot execute before A is completed. • Resource hazards: For example: ld [%fp-28], %o1 - Limited # of function • If there are *n* functional u add %01, %12, %13 multipliers), then only *n* in: of unit can execute at once. Limited instruction issue. • If the instruction-issue unit can issue only *n* instructions at a time, then this limits ILP. - Limited register set. · Any schedule of instructions must have a valid register allocation. 15-745 @ Seth Copen Goldstein 2000-5

### Instruction Scheduling

• The purpose of instruction scheduling (IS) is to order the instructions for maximum ILP.

- Keep all resources busy every cycle.
- If necessary, eliminate data dependences and resource hazards to accomplish this.
- The IS problem is NP-complete (and bad in practice).
  - So heuristic methods are necessary.

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### Instruction Scheduling

- There are *many* different techniques for IS.
  Still an open area of research.
- Most optimizing compilers perform good local IS, and only simple global IS.
- The biggest opportunities are in scheduling the code for loops.....

### What we will cover

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- Scheduling basic blocks
  - List scheduling
  - Long-latency operations
  - Delay slots
- Software Pipelining
- What we need to know
  - pipeline structure
  - data dependencies
  - register renaming
  - scalar replacement



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• And can't be optimal since IS is NP-complete.



| Ex                                   | ample [              | )epende                   | ncies |
|--------------------------------------|----------------------|---------------------------|-------|
| S1) a=0;<br>S2) b=a;<br>S3) c=a+d+e; |                      |                           |       |
| S4) d=b;                             |                      |                           | (2    |
| S5) b=5+e;                           | S1 δ <sup>f</sup> S2 | due to a                  |       |
|                                      | S1 δ <sup>f</sup> S3 | due to a                  |       |
|                                      | S2 δ <sup>f</sup> S4 | due to b                  |       |
|                                      | S3 δ <sup>a</sup> S4 | due to d                  |       |
|                                      | S4 δ <sup>a</sup> S5 | due to b                  | 4     |
|                                      | S2 δ⁰ S5             | due to b                  |       |
|                                      | S3 δ <sup>i</sup> S5 | due to a                  | 5     |
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Register Renaming Example  $\leftarrow$  r2 + 1 || r7 r1  $\leftarrow$  r2 + 1 r7  $\leftarrow$  r2 + 1 [fp+8]  $\leftarrow$  r7 r1  $\leftarrow$  r3 + 2 [fp+8]  $\leftarrow$  r1 $\rightarrow$  $\leftarrow$  r3 + 2 || [fp+8]  $\leftarrow$  r7 r1  $\leftarrow$  r3 + 2 r1 [fp+12] ← r1 [fp+12] ← r1  $[fp+12] \leftarrow r1$ Phase ordering problem · Can perform register renaming atter register allocation • Constrained by available registers · Constrained by live on entry/exit • Instead, do scheduling before register allocation 15-745 © Seth Copen Goldstein 2000-5

### The Scheduler

- Given:
  - Code to schedule
  - Resources available (FU and # of Reg)
  - Latencies of instructions
- Goal:
  - Correct code
  - Better code [fewer cycles, less power, fewer registers, ...]

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- Do it quickly













































| for (i=0; i <n< th=""><th>ealing with exit</th><th>conditions</th></n<> | ealing with exit                    | conditions              |
|---|-------------------------------------|-------------------------|
| A <sub>i</sub>  | i=0                                 | loop:                   |
| B <sub>i</sub>  | if (i >= N) goto done               | ,<br>A,                 |
| C <sub>i</sub>  | A <sub>0</sub>                      | B <sub>i-1</sub>        |
| ,   | Bo                                  | C <sub>i-2</sub>        |
|   | if (i+1 == N) goto last             | i++                     |
|   | i=1                                 | if (i < N) goto loop    |
|   | <b>A</b> <sub>1</sub>               | epilog:                 |
|   | if (i+2 == N) goto epilog           | Bi                      |
|   | i=2                                 | <i>C</i> <sub>i-1</sub> |
|   |                                     | last:                   |
|   |                                     | c <sub>i</sub>          |
|   |                                     | done:                   |
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### Aiken/Nicolau Scheduling Step 1

Perform *scalar replacement* to eliminate memory references where possible.

| <pre>for i:=1 to N do     a := j ⊕ V[i-1]     b := a ⊕ f     c := e ⊕ j     d := f ⊕ c     e := b ⊕ d     f := U[i]     g: V[i] := b     h: W[i] := d     j := X[i]</pre> | <pre>for i:=1 to N do     a := j ⊕ b     b := a ⊕ f     c := e ⊕ j     d := f ⊕ c     e := b ⊕ d     f := U[i]     g: V[i] := b     h: W[i] := d     j := X[i]</pre> |
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| Aiken/N   | Nicolau Scheduling<br>Step 7  |
|---|---|
| <b>Generate code</b> .<br>(Assume VLIW-like mo<br>each line should be iss   | achine for this example. The instructions on<br>ued in parallel.)                                     |
| a1 := j0 ⊕ b0 c1 := e0  |   |
| b1 := a1 ⊕ f0 d1 := f0  | $\Theta$ c1 f2 := U[2] j2 := X[2]   |
| e1 := b1 ⊕ d1 V[1] := b   | ol W[1] := d1 a2 := j1⊕ b1  |
| c2 := e1 ⊕ j1 b2 := a2  | ⊕ f1 f3 := U[3] j3 := X[3]  |
| d2 := f1 ⊕ c2 V[2] := b   | a3 := j2 ⊕ b2   |
| e2 := b2 ⊕ d2 W[2] := d   | l2 b3 := a3 ⊕ f2 f4 := U[4] j4 := X[4]  |
| c3 := e2 ⊕ j2 V[3] := b   | o3 a4 := j3 ⊕ b3 i := 3   |
| L:  |   |
| $d_i := f_{i-1} \bigoplus c_i \qquad b_{i+1} := a_i$  | ⊕ f <sub>i</sub>  |
| e <sub>i</sub> := b <sub>i</sub> ⊕ d <sub>i</sub> W[i] := d   | $V[i+1] := b_{i+1} f_{i+2} := V[I+2] j_{i+2} := X[i+2]$   |
| $\mathbf{c}_{i+1} := \mathbf{e}_i \oplus \mathbf{j}_i  \mathbf{a}_{i+2} := \mathbf{j}_i$                                | $\mathbf{\Phi} \mathbf{b}_{i+1} \mathbf{i} := \mathbf{i} + 1$ if $\mathbf{i} < \mathbf{N} - 2$ goto L |
| $\mathbf{d}_{N-1} := \mathbf{f}_{N-2} \oplus \mathbf{c}_{N-1} \mathbf{b}_{N} := \mathbf{a}_{N} \oplus \mathbf{c}_{N-1}$ | 9 f <sub>N-1</sub>  |
| $e_{N-1} := b_{N-1} \bigoplus d_{N-1}  W[N-1] :=$   | $d_{N-1}$ $v[N] := b_N$   |
| $\mathbf{c}_{\mathbf{N}} := \mathbf{e}_{\mathbf{N}-1} \oplus \mathbf{j}_{\mathbf{N}-1}$                                 |   |
| $\mathbf{d}_{\mathbf{N}} := \mathbf{f}_{\mathbf{N}-1} + \mathbf{c}_{\mathbf{N}}$  |   |
| $\mathbf{e}_{N} := \mathbf{b}_{N} \bigoplus \mathbf{d}_{N} \qquad \mathbf{w}[N] := \mathbf{d}$                          | n   |
|   |   |
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### Aiken/Nicolau Scheduling Step 8

• Since several versions of a variable (e.g.,  $j_i$  and  $j_{i+1}$ ) might be live simultaneously, we need to add new temps and moves

|    | al := j0 ⊕ b0<br>bl := al ⊕ f0<br>el := bl ⊕ d1   | c1 := e0 ⊕ j0<br>d1 := f0 ⊕ c1<br>V[1] := b1                                  | f1 := U[1]<br>f2 := U[2]<br>W[1] := d1   | j1 := X[1]<br>j2 := X[2]<br>a2 := j1                 |
|----|---|---|--|--|
|    | $c2 := e1 \oplus j1$<br>$d2 := f1 \oplus c2$<br>$e2 := b2 \oplus d2$<br>$c3 := e2 \oplus j2$  | b2 := a2 🕀 f1<br>V[2] := b2<br>W[2] := d2<br>V[3] := b3                       | <b>f3</b> := U[3]<br>a3 := j2 ⊕ b2<br>b3 := a3 ⊕ <b>f2</b><br>a4 := <b>j3</b> ⊕ b3 | <pre>j3 := X[3] f4 := U[4] j4 := X[4] i := 3</pre>   |
| L: |   | $b_{i+1} := a_i \oplus f_i$ $W[i] := d_i$ $a_{i+2} := j_{i+1} \oplus b_{i+1}$ | V[i+1] := b <sub>i+1</sub><br>i := i+1   | $\begin{array}{llllllllllllllllllllllllllllllllllll$ |
|    | $\begin{array}{l} \mathbf{d}_{N-1} & := \ \mathbf{f}_{N-2} \ \textcircled{\textbf{G}} \ \mathbf{c}_{N-1} \\ \mathbf{e}_{N-1} & := \ \mathbf{b}_{N-1} \ \textcircled{\textbf{G}} \ \emph{\textbf{G}}_{N-1} \\ \mathbf{c}_{N} & := \ \mathbf{e}_{N-1} \ \textcircled{\textbf{G}} \ \emph{\textbf{J}}_{N-1} \\ \mathbf{d}_{N} & := \ \emph{\textbf{f}}_{N-1} + \ \mathbf{c}_{N} \\ \mathbf{e}_{N} & := \ \mathbf{b}_{N} \ \textcircled{\textbf{G}} \ \mathbf{d}_{N} \end{array}$ | $\begin{array}{llllllllllllllllllllllllllllllllllll$                          | r[N] := b <sub>N</sub>   |  |
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### Aiken/Nicolau Scheduling Step 8

• Since several versions of a variable (e.g.,  $j_i$  and  $j_{i+1}$ ) might be live simultaneously, we need to add new temps and moves

|    | al := j0 🕀 b0                           | c1 := e0 🕀 j0                              | f1 := U[1]                 | j1 := X[1]                                |                            |
|----|---|--|----------------------------|---|----------------------------|
|    | b1 := a1 🕀 f0                           | d1 := f0 🕀 c1                              | f'' := U[2]                | j2 := X[2]                                |                            |
|    | el := b1 ⊕ d1                           | V[1] := b1                                 | W[1] := d1                 | a2 := j1 ⊕ b1                             |                            |
|    | c2 := e1 ⊕ j1                           | b2 := a2 ⊕ f1                              | f' := U[3]                 | j' := X[3]                                |                            |
|    | d2 := f1 ⊕ c2                           | V[2] := b2                                 | a3 := j2 ⊕ b2              |   |                            |
|    | e2 := b2 ⊕ d2                           | W[2] := d2                                 | b3 := a3 🕀 f''             | f4 := U[4]                                | j4 := X[4]                 |
|    | c3 := e2 ⊕ j2                           | V[3] := b3                                 | a4 := j′ ⊕ b3              | i := 3                                    |                            |
| L: |   |  |                            |   |                            |
|    | d, := <b>f'' ⊕</b> c,                   | b <sub>i+1</sub> := <b>a' ⊕ f'</b>         | b' := b; a'=a;             | f''=f'; f'=f;                             | j′′=j′; j′=j               |
|    | e, := b′ ⊕ d,                           | W[i] := d,                                 | V[i+1] := b <sub>i+1</sub> | $f_{i+2} := U[I+2]$                       | j <sub>i+2</sub> := X[i+2] |
|    | c <sub>i+1</sub> := e <sub>i</sub> ⊕ j' | a <sub>i+2</sub> := j'' ⊕ b <sub>i+1</sub> | i := i+1                   | if i <n-2 goto<="" th=""><th>L</th></n-2> | L                          |
|    | d:= <b>f</b> ⊕ c                        | b. := a. ⊕ f                               |                            |   |                            |
|    | $e_{n-1} := b_{n-2} \oplus d_{n-1}$     | $W[N-1] := d_{}$                           | z[N] := b.                 |   |                            |
|    | $c := e \oplus i$                       |  |                            |   |                            |
|    | $d_{i} := f_{i} + c_{i}$                |  |                            |   |                            |
|    | $e := b \oplus d$                       | w[N] := d                                  |                            |   |                            |
|    | N N N                                   | -N   |                            |   |                            |
|    |   |  |                            |   |                            |
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## Next Step in SP

- AN88 did not deal with resource constraints.
- Modulo Scheduling is a SP algorithm that does.
- It schedules the loop based on
  - resource constraints
  - precedence constraints
- Basically, it's list scheduling that takes into account resource conflicts from overlapping iterations

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### **Resource** Constraints

- Minimally indivisible sequences, *i* and *j*, can execute together if combined resources in a step do not exceed available resources.
- R(i) is a resource configuration vector
   R(i) is the number of units of resource i
- r(i) is a resource usage vector s.t.
   0 ≤ r(i) ≤ R(i)
- Each node in G has an associated r(i)



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### Software Pipelining Goal

- Find the same schedule for each iteration.
- Stagger by iteration initiation interval, s
- Goal: minimize *s.*



# <text><list-item><list-item>





### Precedence Constraints

- Review: for acyclic scheduling, constraint is just the required delay between two ops u, v: <d(u,v)>
- For an edge,  $u \rightarrow v$ , we must have  $\sigma(v) \sigma(u) \ge d(u, v)$

### **Iterative Approach**

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- Finding minimum S that satisfies the constraints is NP-Complete.
- Heuristic:
  - Find lower and upper bounds for S
  - foreach s from lower to upper bound?
    - Schedule graph.
    - If succeed, done
    - $\cdot\,$  Otherwise try again (with next higher s)
- Thus: "Iterative Modulo Scheduling" Rau, et.al.

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### **Iterative Approach**

- Heuristic:
  - Find lower and upper bounds for S
  - foreach s from lower to upper bound
    - Schedule graph.
    - If succeed, done
    - $\cdot\,$  Otherwise try again (with next higher s)
- · So the key difference:
  - AN88 does not assume S when scheduling
  - IMS must assume an S for each scheduling attempt to understand resource conflicts

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### Lower Bounds

- Resource Constraints: S<sub>R</sub> (also called II<sub>res</sub>) maximum over all resources of # of uses divided by # available... rounded up or down?
- Precedence Constraints: S<sub>E</sub> (also called II<sub>rec</sub>) max over all cycles: d(c)/p(c)

 $\label{eq:sector} \frac{\text{In practice}}{\text{Signal}}, \text{ one is easy, other is hard.} \\ \text{Tim's secret approach: just use } S_{\text{R}} \text{ as lower bound,} \\ \text{ then do binary search for best } S \\ \end{array}$ 

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![](_page_16_Figure_6.jpeg)

![](_page_16_Figure_7.jpeg)

### Scheduling data structures

To schedule for initiation interval s:

- Create a resource table with s rows and R columns
- Create a vector, *o*, of length N for n instructions in the loop
  - o[n] = the time at which n is scheduled, or NONE

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- Prioritize instructions by some heuristic
  - critical path (or cycle)
  - resource critical

![](_page_17_Figure_2.jpeg)

### Scheduling algorithm - cont.

- We now schedule n at earliest, I.e.,  $\sigma(n)$  = earliest
- Fix up schedule
  - Successors, x, of n must be scheduled s.t. σ(x) >= σ(n)+d(n,x)-s·p(n,x), otherwise they are removed (descheduled) and put back on worklist.
- · repeat this some number of times until either

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- succeed, then register allocate
- fail, then increase s

![](_page_17_Figure_10.jpeg)

![](_page_17_Figure_11.jpeg)

![](_page_18_Figure_2.jpeg)

![](_page_18_Figure_3.jpeg)

![](_page_18_Figure_4.jpeg)

![](_page_18_Figure_5.jpeg)

![](_page_19_Figure_2.jpeg)

![](_page_19_Figure_3.jpeg)

![](_page_19_Figure_4.jpeg)

![](_page_19_Figure_5.jpeg)

![](_page_20_Figure_2.jpeg)

![](_page_20_Figure_3.jpeg)

![](_page_20_Figure_4.jpeg)

![](_page_20_Figure_5.jpeg)

![](_page_21_Figure_2.jpeg)

![](_page_21_Figure_3.jpeg)

![](_page_21_Figure_4.jpeg)

![](_page_21_Figure_5.jpeg)

![](_page_22_Figure_2.jpeg)

| f0 = U[0];  |              |  |
|---|--------------|--|
| j0 = X[0];  |              |  |
| FOR i = 0 to N<br>f1 := U[i+1]<br>j1 := X[i+1]<br>nop<br>a := j0 ? b<br>b := a ? f0<br>c := e ? j0<br>d := f0 ? c |              |  |
| e := b ? d<br>h: W[i] := d<br>f0 = f1<br>j0 = j1  | g: V[i] := b |  |
|   |              |  |

### Conditionals

- What about internal control structure, I.e., conditionals
- Three approaches
  - Schedule both sides and use conditional moves
  - Schedule each side, then make the body of the conditional a macro op with appropriate resource vector

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- Trace schedule the loop

### What to take away

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- Dependence analysis is very important
- Software pipelining is cool
- Registers are a key resource