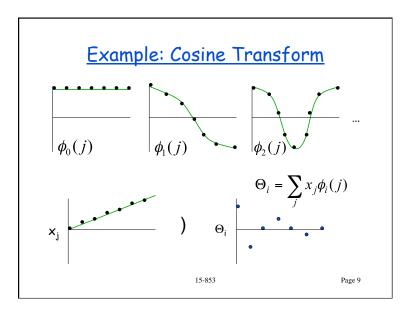
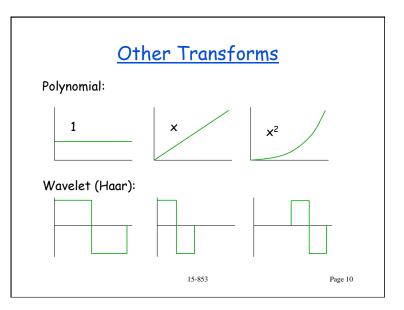


| Linear Transform Coding | |
|--|--------|
| Coefficients: $\Theta_i = \sum_i x_j \phi_i(j) = \sum_i x_j a_{ij}$ | |
| $\Theta_i = i^{th}$ resulting coefficient | |
| $x_j = j^{th}$ input value | |
| $a_{ij} = ij^{th}$ transform coefficient $= \phi_i(j)$ | |
| In matrix notation: $\begin{split} \Theta &= Ax \\ x &= A^{-1}\Theta \end{split}$ | |
| Where A is an n × n matrix, and each row defines a basis function | |
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<u>How to Pick a Transform</u> <u>Goals:</u>

- Decorrelate

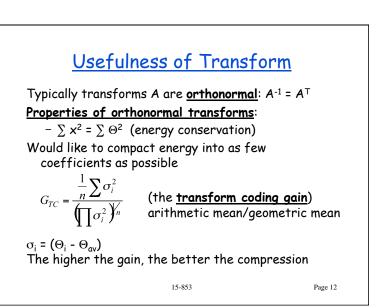
- Low coefficients for many terms

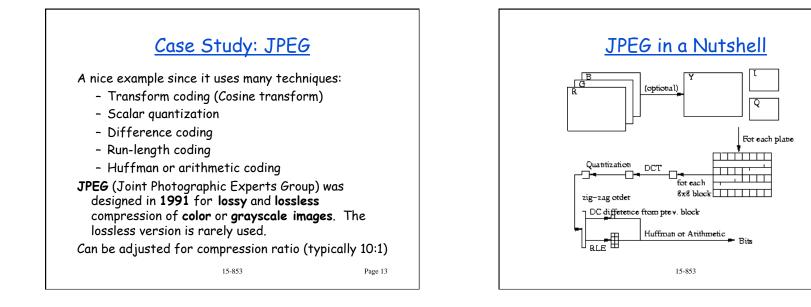
- Basis functions that can be ignored by perception

Why is using a Cosine of Fourier transform across a whole image bad?

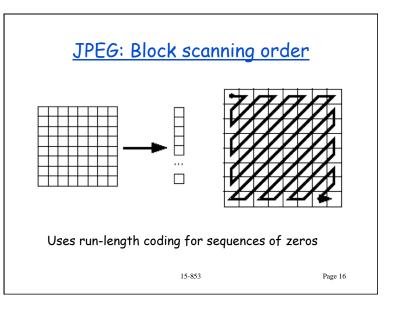
How might we fix this?

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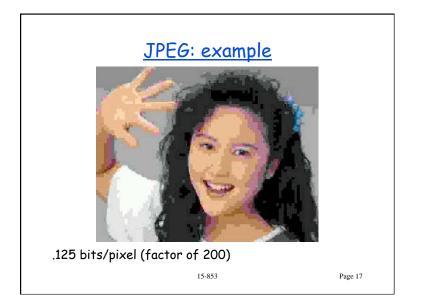


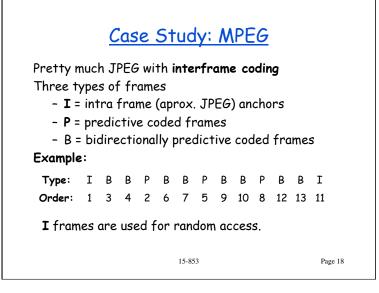


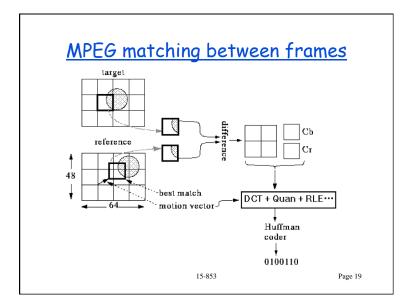
| 12 12 14 19 26 58 60 |
|--|
| |
| 14 13 16 24 40 57 69 |
| 14 17 22 29 51 87 80 |
| 18 22 37 56 68 109 103 |
| 24 35 55 64 81 104 113 |
| 49 64 78 87 103 121 120 1 |
| 72 92 95 98 112 100 103 |

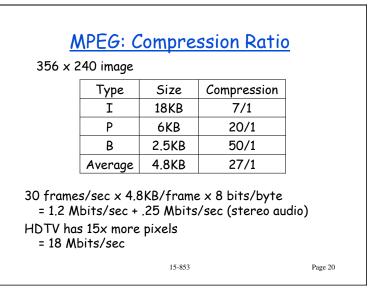


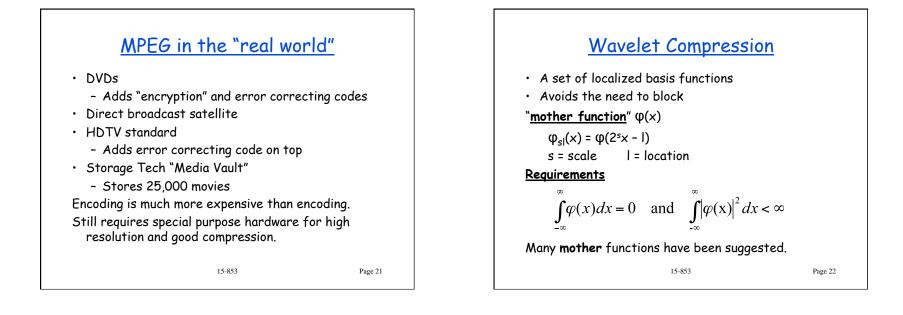
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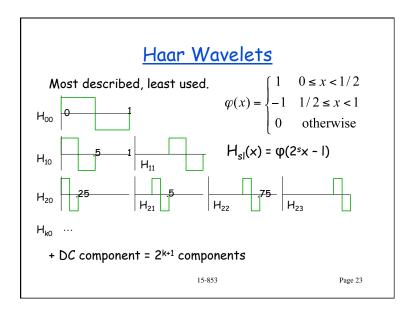


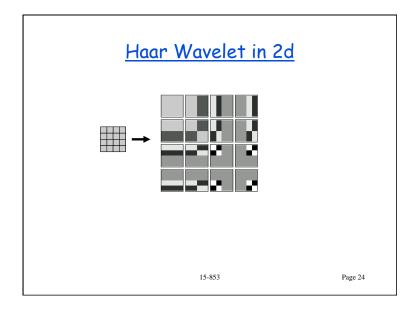


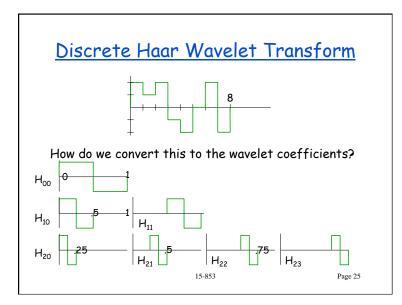


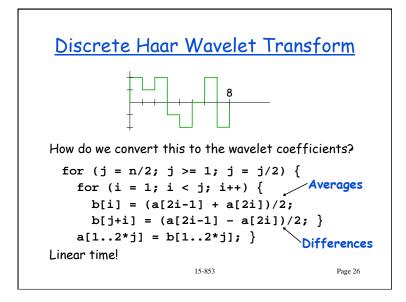


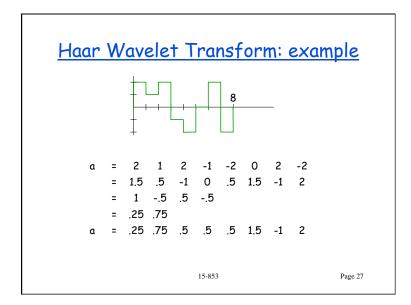


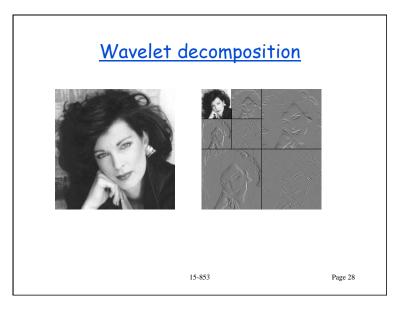


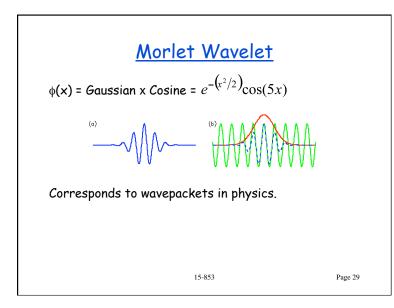


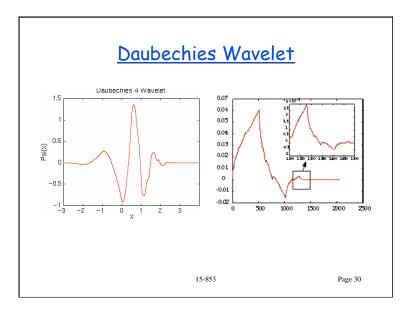


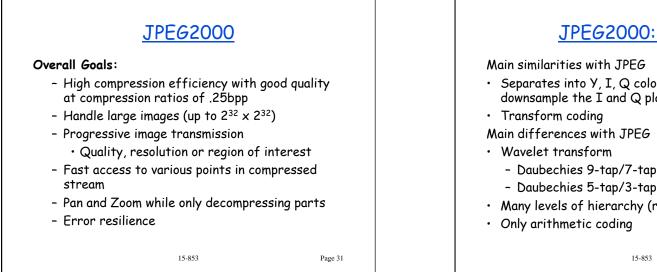






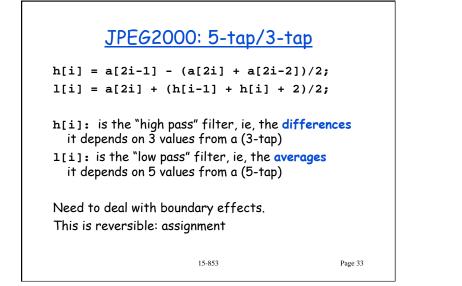


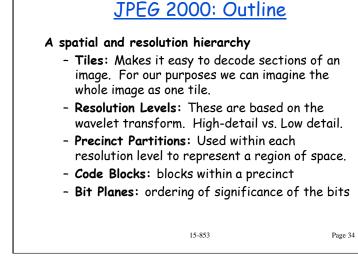


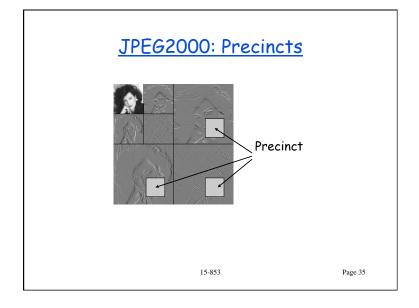


JPEG2000: Outline

- Separates into Y, I, Q color planes, and can downsample the I and Q planes
 - Daubechies 9-tap/7-tap (irreversible)
 - Daubechies 5-tap/3-tap (reversible)
- Many levels of hierarchy (resolution and spatial)









Compression Outline

Introduction: Lossy vs. Lossless, Benchmarks, ... Information Theory: Entropy, etc. Probability Coding: Huffman + Arithmetic Coding Applications of Probability Coding: PPM + others Lempel-Ziv Algorithms: LZ77, gzip, compress, ... Other Lossless Algorithms: Burrows-Wheeler Lossy algorithms for images: JPEG, MPEG, ... Compressing graphs and meshes: BBK

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<u>Compressing Structured Data</u>

So far we have concentrated on Text and Images, compressing sound is also well understood.

What about various forms of "structured" data?

- Web indexes
- Triangulated meshes used in graphics
- Maps (mapquest on a palm)
- XML
- Databases



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How to start? Lower bound for n vertices and m edges? 1. If there are N possible graphs then we will need og N bits to distinguish them. 2. in a directed graph there are n² possible edges (alowing self edges). 3. we can choose any m of them so h (n² choose m) = O(m log (n²/m)) bits in general. 3. For sparse graphs (m = kn) this is hardly any better than adjacency lists (perhaps factor of 2 or 3).

What now?

Are all graphs equally likely?

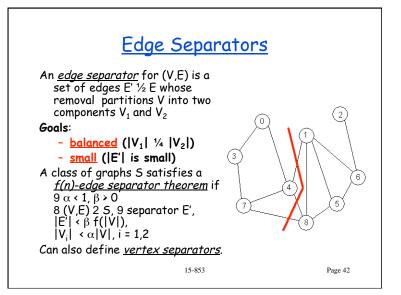
Are there properties that are common across "real world" graphs?

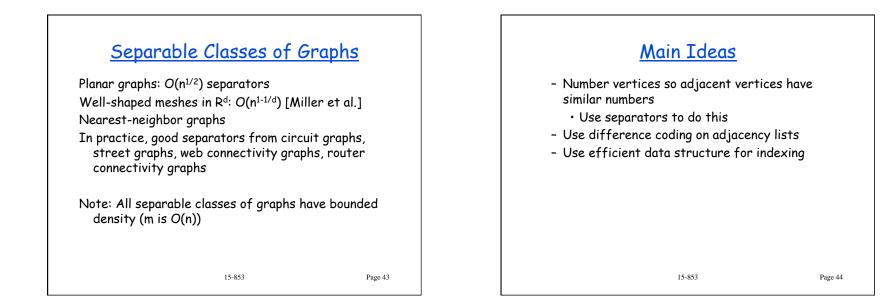
Consider

- link graphs of the web pages
- map graphs
- router graphs of the internet
- meshes used in simulations
- circuit graphs

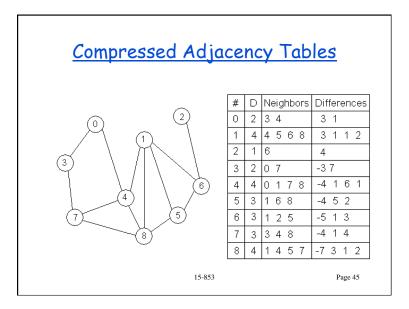
LOCAL CONNECTIONS / SMALL SEPARATORS

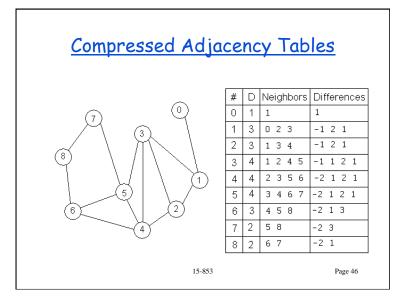
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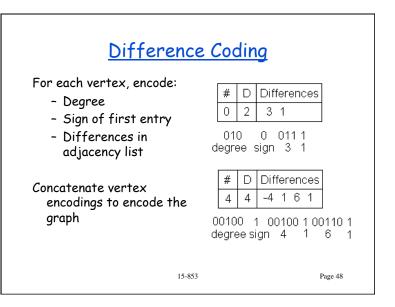


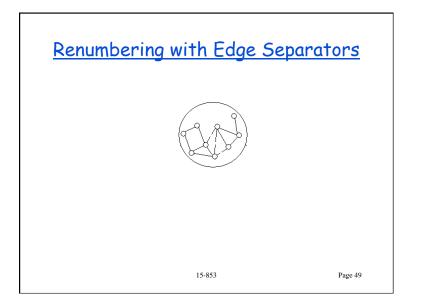
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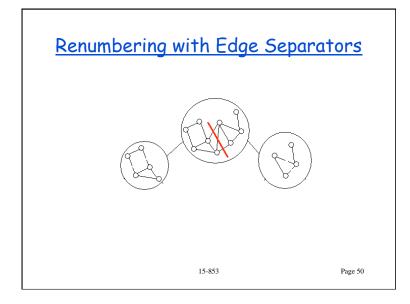


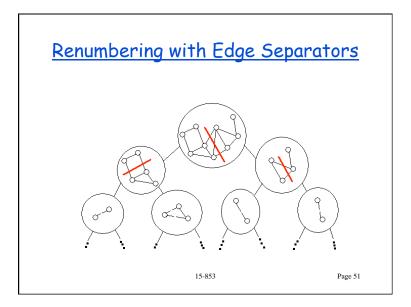


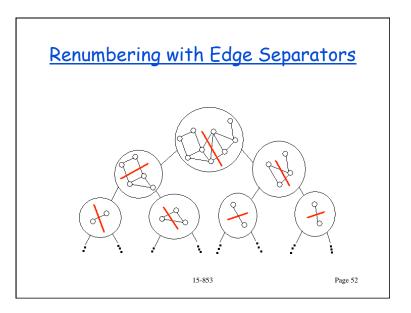
| Example: Gamma code Decimal Gamma Prefix: unary code for [log d] 1 1 2 010 | |
|--|--|
| Suffix: binary code for d-2llog dl 3 01 1 (binary code for d, except leading 4 001 100 1 is implied) 5 001 10 7 001 10 10 8 0001 100 | |

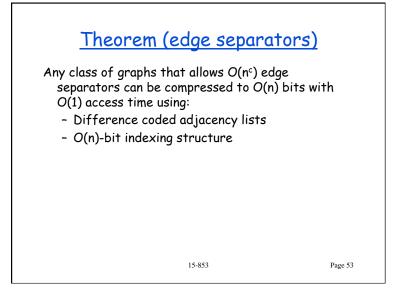












Performance: Adjacency Table

| | | dfs | metis-cf | | bu-bpq | | bu-cf | |
|---------|-------|-------|----------|-------|---------|-------|---------|-------|
| | T_d | Space | T/T_d | Space | T/T_d | Space | T/T_d | Space |
| auto | 0.79 | 9.88 | 153.11 | 5.17 | 7.54 | 5.90 | 14.59 | 5.52 |
| feocean | 0.06 | 13.88 | 388.83 | 7.66 | 17.16 | 8.45 | 34.83 | 7.79 |
| m14b | 0.31 | 10.65 | 181.41 | 4.81 | 8.16 | 5.45 | 15.32 | 5.13 |
| ibm17 | 0.44 | 13.01 | 136.43 | 6.18 | 11.0 | 6.79 | 20.25 | 6.64 |
| ibm18 | 0.48 | 11.88 | 129.22 | 5.72 | 9.5 | 6.24 | 17.29 | 6.13 |
| CA | 0.76 | 8.41 | 382.67 | 4.38 | 14.61 | 4.90 | 35.21 | 4.29 |
| PA | 0.43 | 8.47 | 364.06 | 4.45 | 13.95 | 4.98 | 33.02 | 4.37 |
| googleI | 1.4 | 7.44 | 186.91 | 4.08 | 12.71 | 4.18 | 40.96 | 4.14 |
| googleO | 1.4 | 11.03 | 186.91 | 6.78 | 12.71 | 6.21 | 40.96 | 6.05 |
| lucent | 0.04 | 7.56 | 390.75 | 5.52 | 19.5 | 5.54 | 45.75 | 5.44 |
| scan | 0.12 | 8.00 | 280.25 | 5.94 | 23.33 | 5.76 | 81.75 | 5.66 |
| Avg | | 10.02 | 252.78 | 5.52 | 13.65 | 5.86 | 34.54 | 5.56 |

Time is to create the structure, normalized to time for $DFS_{Page 54}$

| <u> Performance: Overall</u> | | | | | | |
|------------------------------|-------|-------|------|-------|------------|-------|
| | Array | | List | | bu-cf/semi | |
| Graph | time | space | time | space | time | space |
| auto | 0.24 | 34.2 | 0.61 | 66.2 | 0.51 | 7.17 |
| feocean | 0.04 | 37.6 | 0.08 | 69.6 | 0.09 | 11.75 |
| m14b | 0.11 | 34.1 | 0.29 | 66.1 | 0.24 | 6.70 |
| ibm17 | 0.15 | 33.3 | 0.40 | 65.3 | 0.34 | 7.72 |
| ibm18 | 0.14 | 33.5 | 0.38 | 65.5 | 0.32 | 7.33 |
| \mathbf{CA} | 0.34 | 43.4 | 0.56 | 75.4 | 0.58 | 11.66 |
| PA | 0.19 | 43.3 | 0.31 | 75.3 | 0.32 | 11.68 |
| googleI | 0.24 | 37.7 | 0.49 | 69.7 | 0.45 | 7.86 |
| googleO | 0.24 | 37.7 | 0.50 | 69.7 | 0.51 | 9.90 |
| lucent | 0.02 | 42.0 | 0.04 | 74.0 | 0.05 | 11.87 |
| scan | 0.04 | 43.4 | 0.06 | 75.4 | 0.08 | 12.85 |

