

11-695: Competitive Engineering

Convolution I

Spring 2018

Outline

① Recap and motivation

② Convolution

③ Convolution in Neural Network

④ Pooling

⑤ Case Studies

Recap: Tensorflow

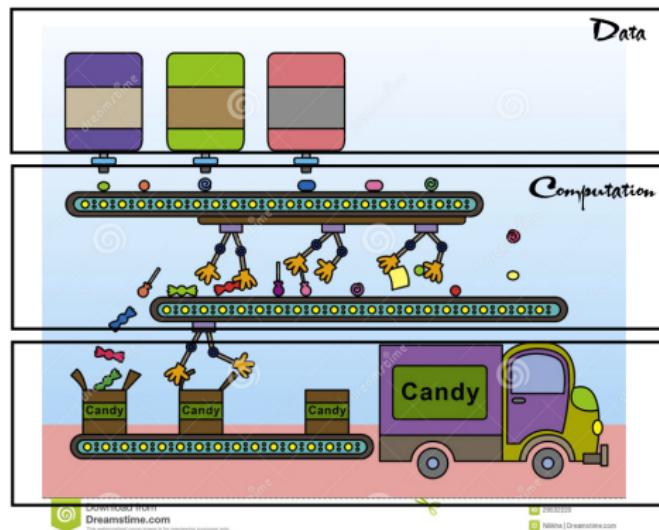
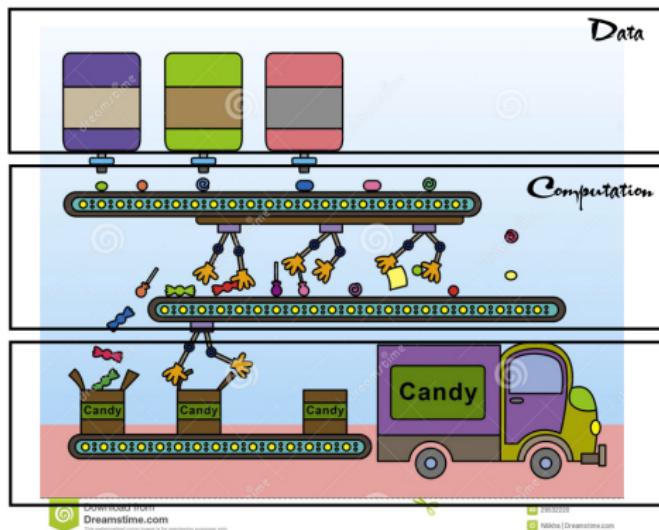


Image credit: Dreamstime.com

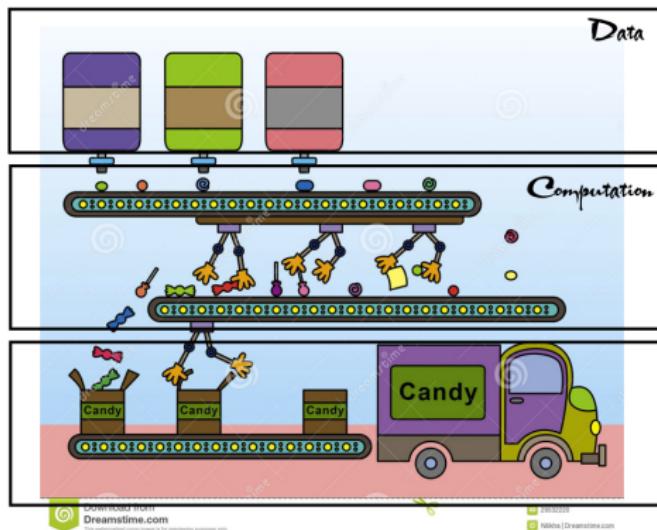
Recap: Tensorflow



- Distinguish between computational graph and data

Image credit: Dreamstime.com

Recap: Tensorflow



- Distinguish between computational graph and data
- Understand the role of a Session

Image credit: Dreamstime.com

Recap: Feed-forward NN - A Motivation

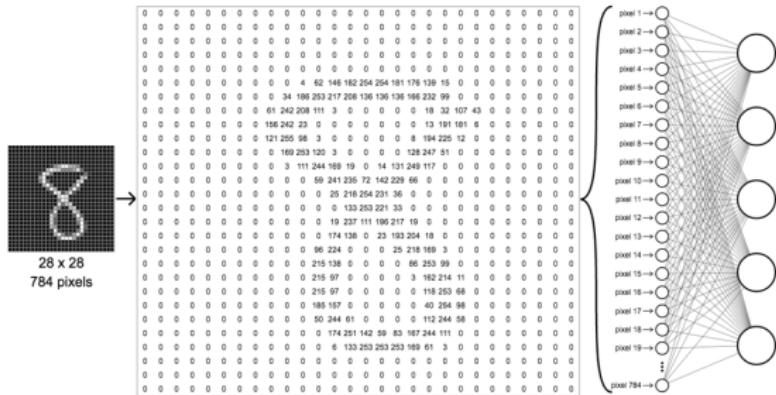
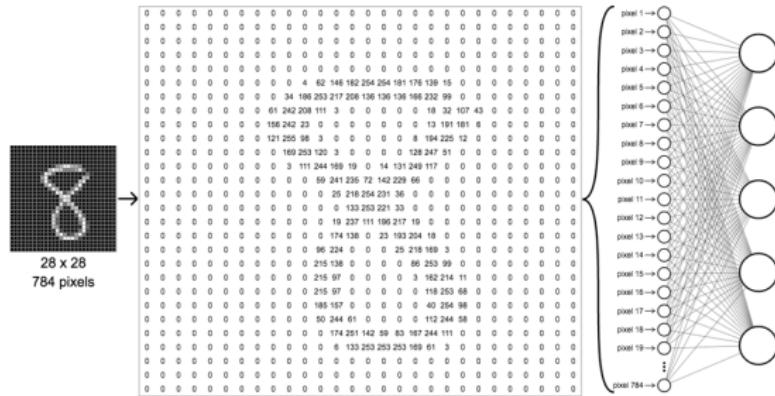


Image credit: https://ml4a.github.io/ml4a/neural_networks/

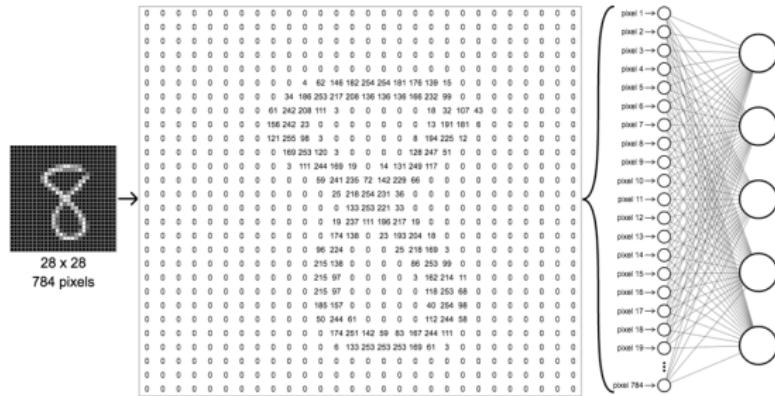
Recap: Feed-forward NN - A Motivation



- The first layer of a NN
 - Number of params?

Image credit: https://ml4a.github.io/ml4a/neural_networks/

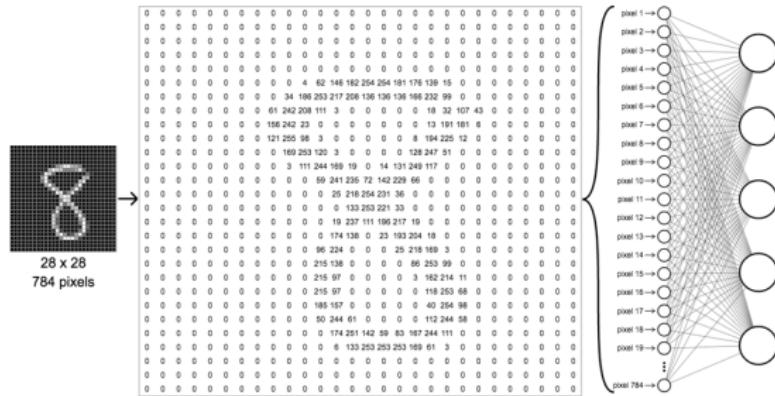
Recap: Feed-forward NN - A Motivation



- The first layer of a NN
 - Number of params? $28 * 28 * n$

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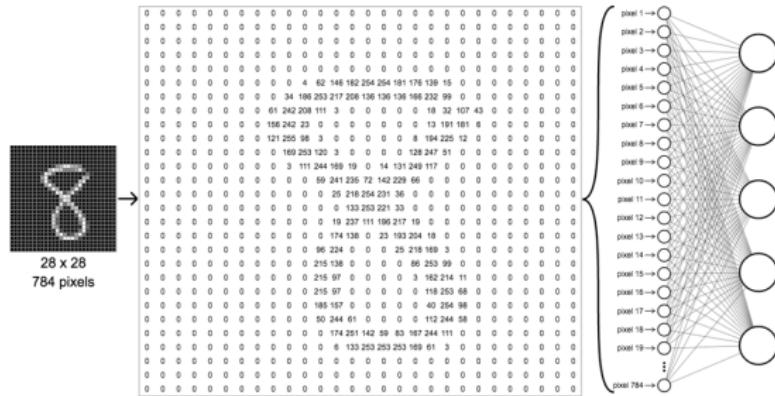
Recap: Feed-forward NN - A Motivation



- The first layer of a NN
 - Number of params? $28 * 28 * n$
 - Real world: $200 * 200 * 3 * 1000 \approx 1e8$ for the first layer

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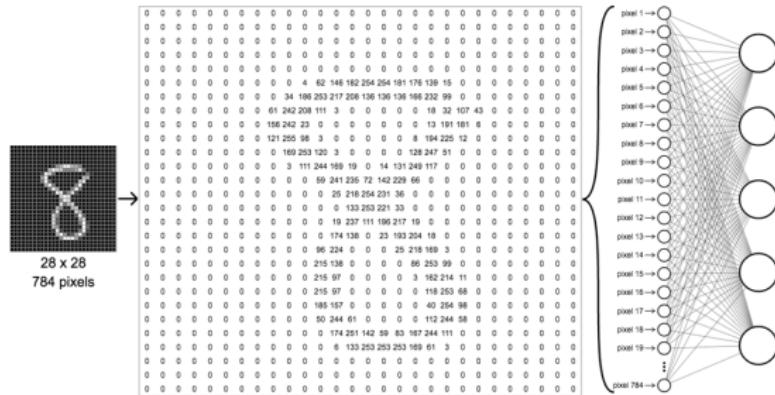
Recap: Feed-forward NN - A Motivation



- The first layer of a NN
 - Number of params? $28 * 28 * n$
 - Real world: $200 * 200 * 3 * 1000 \approx 1e8$ for the first layer
 - What's more?

Image credit: https://ml4a.github.io/ml4a/neural_networks/

Recap: Feed-forward NN - A Motivation



- The first layer of a NN
 - Number of params? $28 * 28 * n$
 - Real world: $200 * 200 * 3 * 1000 \approx 1e8$ for the first layer
 - What's more? How about spatial correlations?

Image credit: https://ml4a.github.io/ml4a/neural_networks/

Another Motivation



- Local spatial features at different locations are the similar

Image credit: Dreamstime.com

Another Motivation



- Local spatial features at different locations are the similar
- Model parts of the image instead of the whole

Image credit: Dreamstime.com

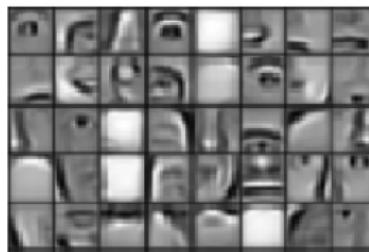
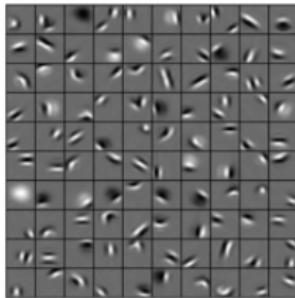
Another Motivation



- Local spatial features at different locations are the similar
- Model parts of the image instead of the whole
- Exploit image's redundancy: e.g. edges

Image credit: Dreamstime.com

Even More Motivation

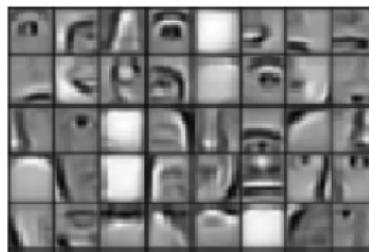
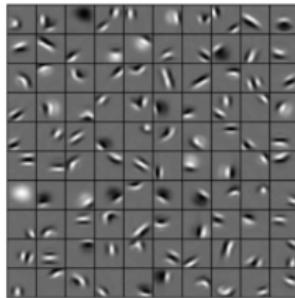


- Human cognition works similarly
 - Eyes detect edges
 - Visual cortex uses **Gabor**-like filter to recognize objects

¹ Bengio J. et al. [Representation Learning: A Review and New Perspectives](#)

Image credit: Nvidia Developer Blog

Even More Motivation

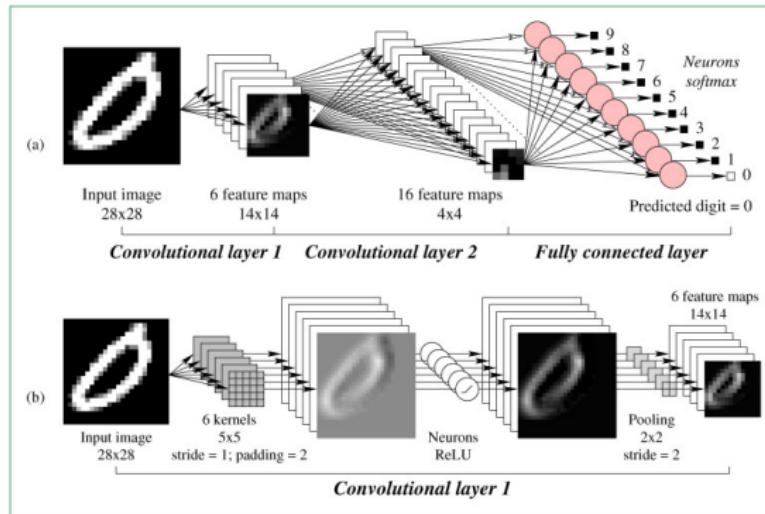


- Human cognition works similarly
 - Eyes detect edges
 - Visual cortex uses **Gabor**-like filter to recognize objects
- Intention to build hierarchical abstract representation¹

¹ Bengio J. et al. [Representation Learning: A Review and New Perspectives](#)

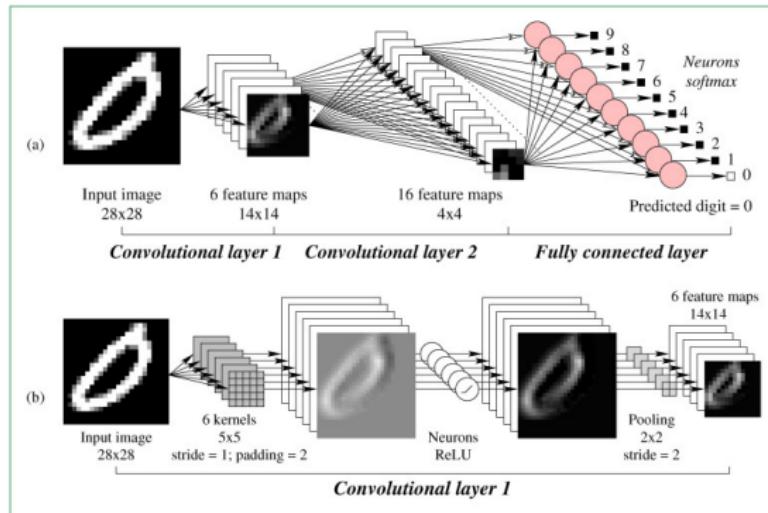
Image credit: Nvidia Developer Blog

Convolutional Neural Network



- Yet another type of feed-forward NN

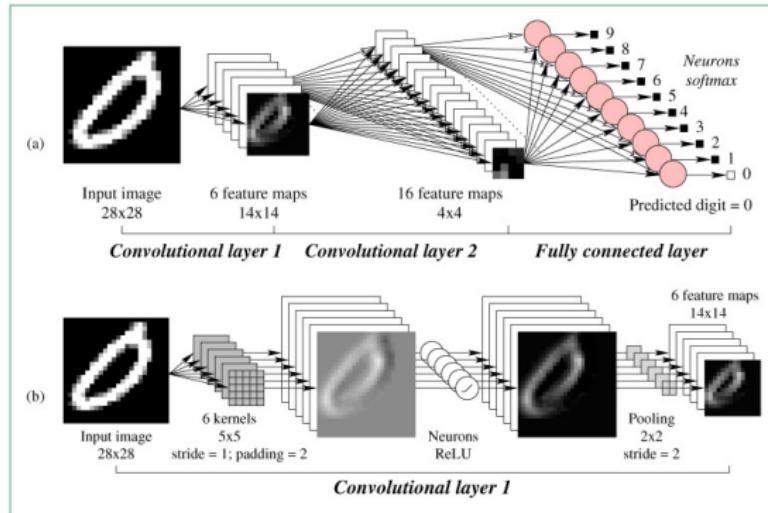
Convolutional Neural Network



- Yet another type of feed-forward NN
- With additions of:
 - Convolutional Layers
 - Pooling Layers

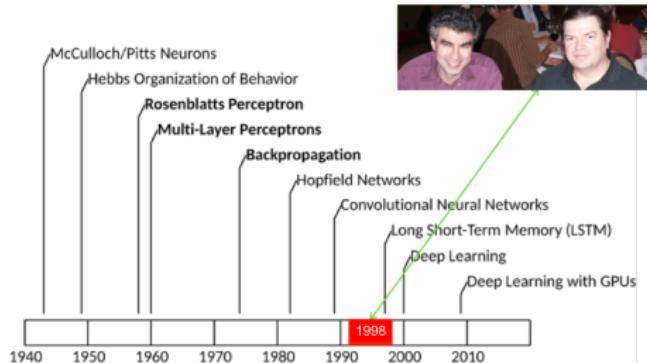
Image credit: ScienceDirect.com

Convolutional Neural Network



- Yet another type of feed-forward NN
- With additions of:
 - Convolutional Layers
 - Pooling Layers
- Renaming MLPs into the so-call Fully Connected

Recap: History of (C)NN

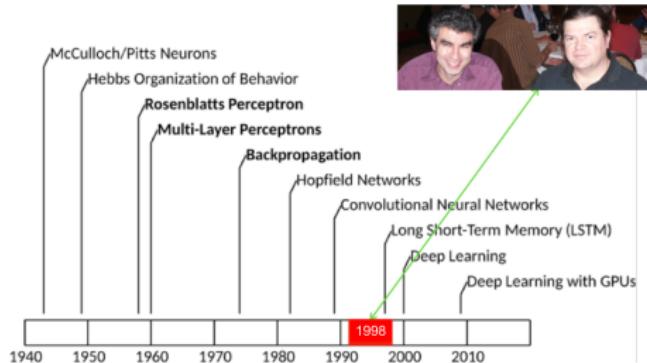


- Be a go-to feature extraction solution for images/videos

²Yin W. et al Comparative Study of CNN and RNN for NLP

Image credit: IBM and Recode.net

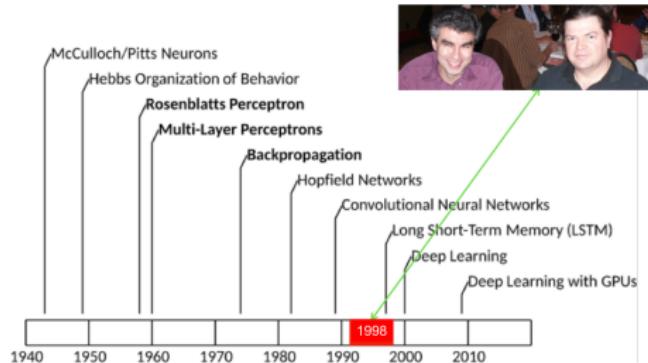
Recap: History of (C)NN



- Be a go-to feature extraction solution for images/videos
- Even outperform over the advantages of RNN in some language tasks ?!! ²

²Yin W. et al [Comparative Study of CNN and RNN for NLP](#)

Recap: History of (C)NN



- Be a go-to feature extraction solution for images/videos
- Even outperform over the advantages of RNN in some language tasks ?!! ²
- Be an essential part in many SoTA solutions for classifications, detections, recognition, segmentation, OCR, motion, pose, etc.

²Yin W. et al [Comparative Study of CNN and RNN for NLP](#)

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5 Case Studies

Convolution

- Yet another mathematics operation [▶ demo](#)

$$(f * g)(t) = \int_{-\infty}^{\infty} f(u)g(t-u)du = \int_{-\infty}^{\infty} f(t-u)g(u)du$$

Convolution

- Yet another mathematics operation [▶ demo](#)

$$(f * g)(t) = \int_{-\infty}^{\infty} f(u)g(t-u)du = \int_{-\infty}^{\infty} f(t-u)g(u)du$$

- A linear time invariant (LTI) operation, means that no new frequency components are created, and so output is the pointwise product of input and a transfer function (Wikipedia)

Convolution

- Yet another mathematics operation [▶ demo](#)

$$(f * g)(t) = \int_{-\infty}^{\infty} f(u)g(t-u)du = \int_{-\infty}^{\infty} f(t-u)g(u)du$$

- A linear time invariant (LTI) operation, means that no new frequency components are created, and so output is the pointwise product of input and a transfer function (Wikipedia)
- Relation to Fourier Transformation [▶ demo](#)

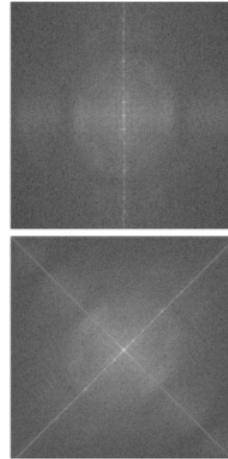
$$(f * g)(t) = \mathcal{F}^{-1}(\sqrt{2\pi} \cdot \mathcal{F}|f| \cdot \mathcal{F}|g|)$$

Convolution (cont'd)

Sonnet for Lens

O dear Lens, your beauty is so vast,
It is hard sometimes to describe it best.
I have tried to paint your picture, but I cannot,
If only your portrait I could compose.
Alas! I have no skill to do such a task,
I fear that your checks belong to only you
Your only hair is light and thin,
Held in place with some of delicate coquetry
And for your eyes, a mirror and a mirror fractal.
These are your beauties not my painter's fault.
And while these wrinkles are all grace across
Lips and cheeks, they are not all grace at all.
But when stars look sparkle from your eyes
I note, Once all this I'll just digitize.

Thomas Cooksey



- Convolution is an operation in Fourier domain

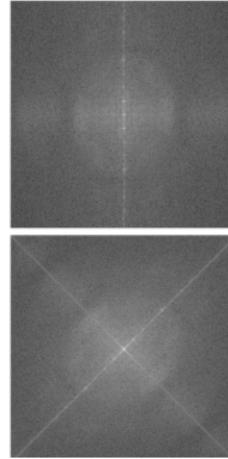
Image credit: Timdettmers.com

Convolution (cont'd)

Sonnet for Lens

O dear Lens, your beauty is no secret.
It is hard sometimes to describe it best.
I have tried to paint your picture, but I can't,
If only your portrait I could compose.
All I can do is to draw a few lines,
I know that your checks belong to only you
Your eyes like stars look sparkle from your eyes
Your hair like a crown of diamonds, and your smile
Held by your fingers with some of delicate caresses
And for your nose seems not longer floral,
Than a rose flower not longer floral.
And while these words are all optics across
Landscape, I can't paint your portrait at all.
But when stars look sparkle from your eyes
I wait, Until all this I'll just digitize.

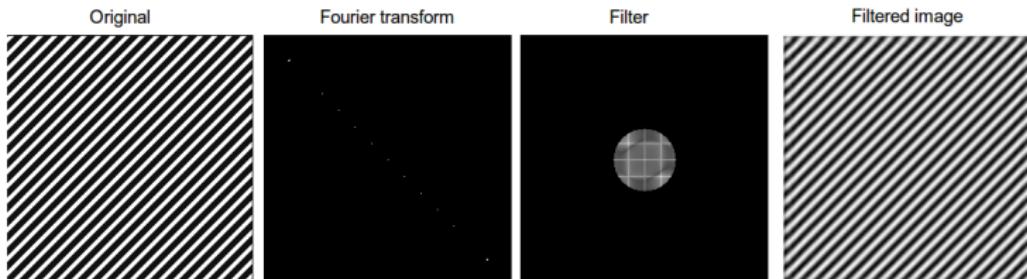
Thomas Cookhart



- Convolution is an operation in Fourier domain
- It can capture orientation change

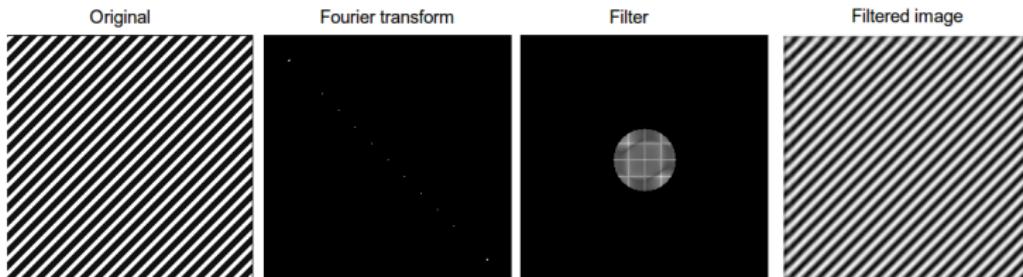
Image credit: Timdettmers.com

Convolution (cont'd)



- Convolution is often referred to as filtering

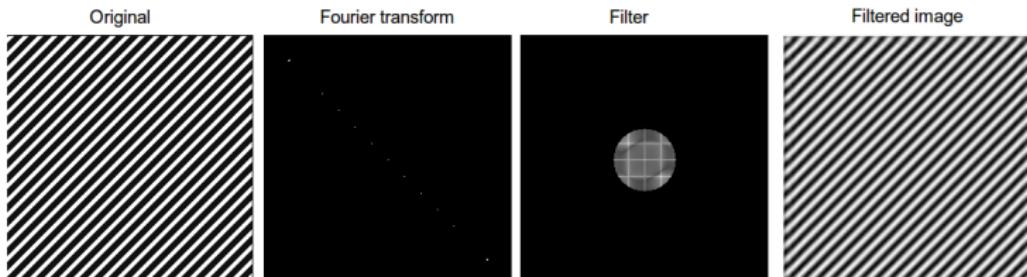
Convolution (cont'd)



- Convolution is often referred to as filtering
- Other names: kernel, receptive field

Image credit: Timdettmers.com

Convolution (cont'd)



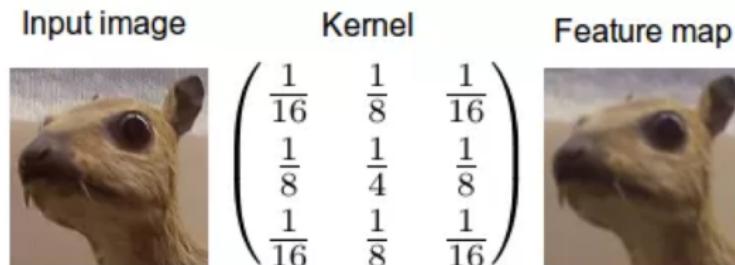
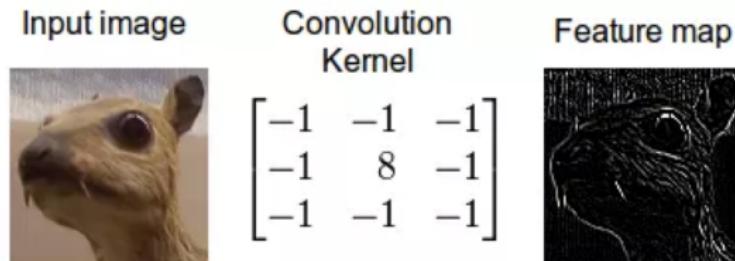
- Convolution is often referred to as filtering
- Other names: kernel, receptive field
- And now:

$$\text{feature_map} = \text{filter} * \text{input}$$

$$\begin{aligned}
 &= \sum_{y=1}^{n_rows} \left(\sum_{x=1}^{n_columns} \text{input}(x-a, y-b) \text{filter}(x, y) \right) \\
 &= \mathcal{F}^{-1}(\sqrt{2\pi} \cdot \mathcal{F}|\text{input}| \cdot \mathcal{F}|\text{filter}|)
 \end{aligned}$$

Image credit: Timdettmers.com

Convolution (cont'd)



- Similarity: Kernel SVM, PCA?

Image credit: Timdettmers.com

Break?

Recap: Fun with Python

fun_break.py

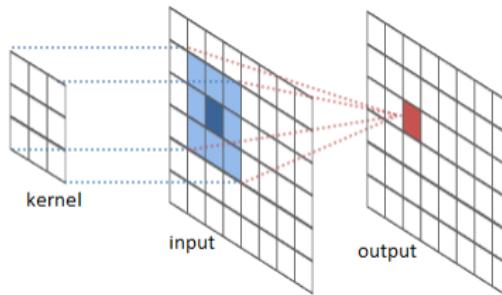
```
1 # what is the difference?
2 x = [10 * i for i in range(100)]
3 type(x)
4
5 y = (10 * i for i in range(100))
6 type(y)
7
8 # does this work?
9 for i in range(10): yield i**2
10
11 # does this work?
12 def f():
13     for i in xrange(10):
14         yield i**2
15 type(f)
16 for j in f():
17     print(j)
18
19 # does this work?
20 f = lambda: [(yield i**2) for i in range(10)]
21 type(f)
22 for j in f():
23     print(j)
```

End of Break!

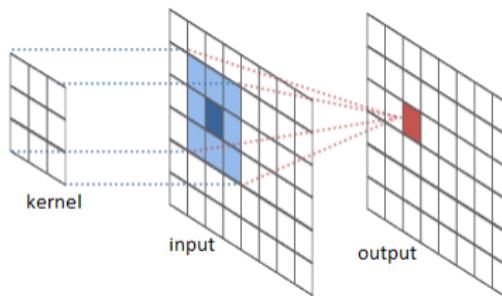
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Convolution In Action

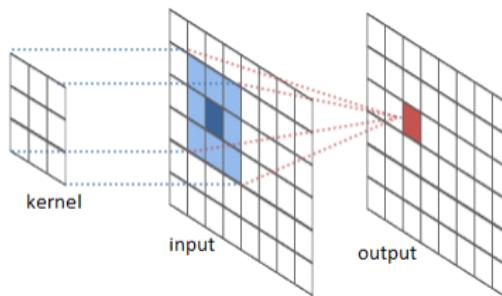


- Given a 200x200 image
- A fully-connected layer with n hidden neurons: $200 * 200 * n$ params



- Given a 200x200 image
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- With convolution with filter size 3x3, then how many params?

Convolution In Action



- Given a 200x200 image
- A fully-connected layer with n hidden neurons: $200 * 200 * n$ params
- With convolution with filter size 3x3, then how many params?
 $3 * 3 * n$

Convolution In Action (cont'd)

$$\begin{array}{c} \text{I} \\ \begin{array}{|c|c|c|c|c|c|c|} \hline 0 & 1 & 1 & 1 & 0 & 0 & 0 \\ \hline 0 & 0 & 1 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 0 & 1 & 1 & 1 & 0 \\ \hline 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ \hline 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ \hline 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ \hline \end{array} \end{array} * \begin{array}{|c|c|c|} \hline 1 & 0 & 1 \\ \hline 0 & 1 & 0 \\ \hline 1 & 0 & 1 \\ \hline \end{array} = \begin{array}{|c|c|c|c|c|} \hline 1 & 4 & 3 & 4 & 1 \\ \hline 1 & 2 & 4 & 3 & 3 \\ \hline 1 & 2 & 3 & 4 & 1 \\ \hline 1 & 3 & 3 & 1 & 1 \\ \hline 3 & 3 & 1 & 1 & 0 \\ \hline \end{array} \text{K} \quad \text{I} * \text{K}$$

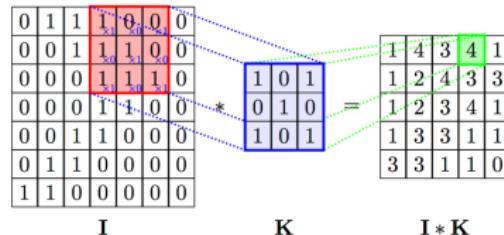
- How it works?

Convolution In Action (cont'd)

$$\begin{array}{c} \text{I} \\ \begin{array}{|c|c|c|c|c|c|c|} \hline 0 & 1 & 1 & 1 & 0 & 0 & 0 \\ \hline 0 & 0 & 1 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 0 & 1 & 1 & 1 & 0 \\ \hline 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ \hline 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ \hline 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ \hline \end{array} \end{array} * \begin{array}{c} \text{K} \\ \begin{array}{|c|c|c|} \hline 1 & 0 & 1 \\ \hline 0 & 1 & 0 \\ \hline 1 & 0 & 1 \\ \hline \end{array} \end{array} = \begin{array}{c} \text{I} * \text{K} \\ \begin{array}{|c|c|c|c|c|} \hline 1 & 4 & 3 & 4 & 1 \\ \hline 1 & 2 & 4 & 3 & 3 \\ \hline 1 & 2 & 3 & 4 & 1 \\ \hline 1 & 3 & 3 & 1 & 1 \\ \hline 3 & 3 & 1 & 1 & 0 \\ \hline \end{array} \end{array}$$

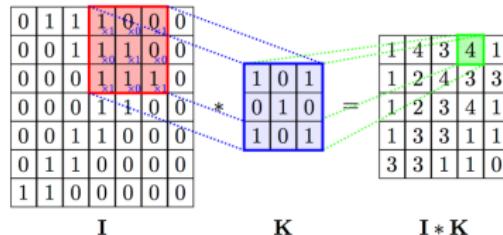
- How it works? Simply, it's a dot product

Convolution In Action (cont'd)



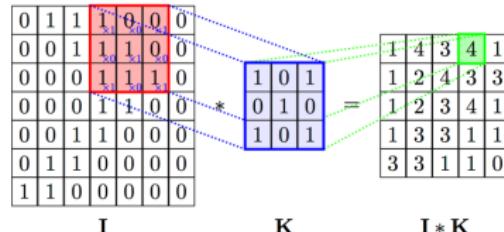
- How it works? Simply, it's a dot product
- A filter scan through the whole image which is convolved by it
- *Important:* a filter has a fixed weight → output is similar if the region is similar

Convolution In Action (cont'd)



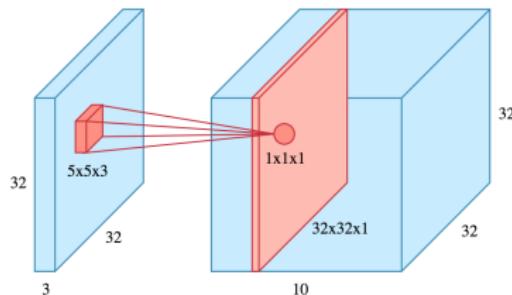
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- Practice: $n * n$ image, $k * k$ filter, output?

Convolution In Action (cont'd)



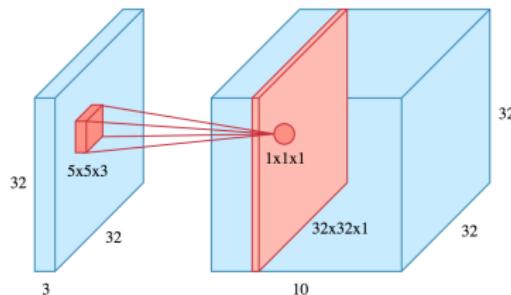
- How it works? Simply, it's a dot product
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- *Important:* a filter has a fixed weight → output is similar if the region is similar
- Practice: $n * n$ image, $k * k$ filter, output? $(n - k + 1) * (n - k + 1)$

Depth of Convolution



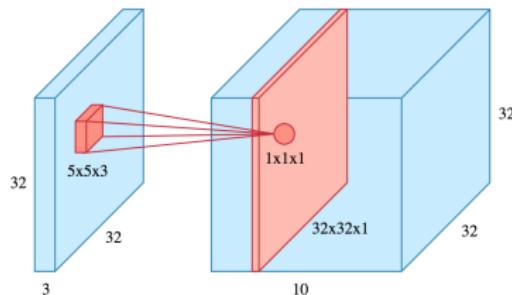
- Filter shares the *same depth* with input
- If input image has 3 channels: $200 * 200 * 3 \rightarrow$ the filter should be $n * n * 3$

Depth of Convolution



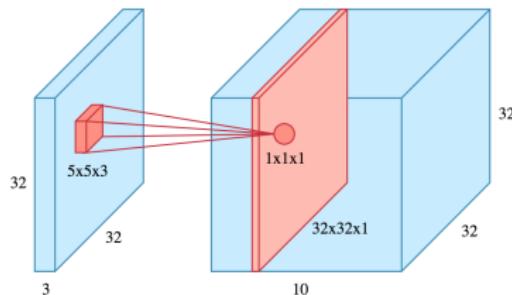
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Depth of Convolution



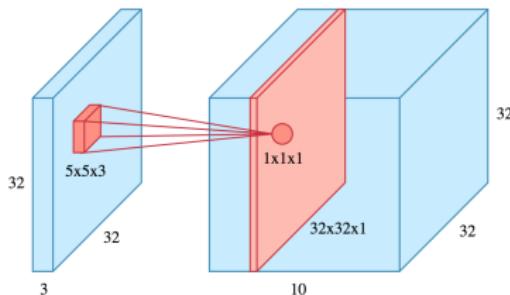
- Filter shares the *same depth* with input
- If input image has 3 channels: $200 * 200 * 3 \rightarrow$ the filter should be $n * n * 3$
- Dimension of each convolution operation? Simply, a scalar.

Depth of Convolution



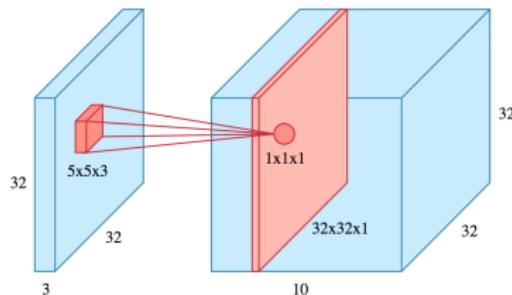
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- Dimension of each convolution operation? Simply, a scalar.
- Recall, what if we want many feature maps?

Depth of Convolution



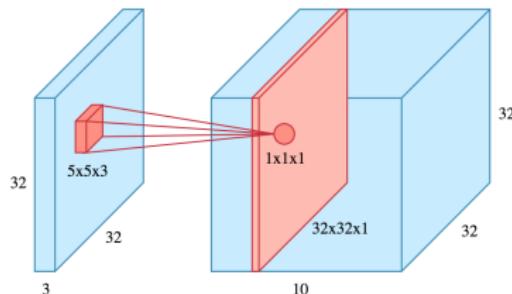
- Filter shares the *same depth* with input
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- Dimension of each convolution operation? Simply, a scalar.
- Recall, what if we want many feature maps? Use many filters.
- Practice: $n * n * 3$ image, $k * k * 3$ filter, output?

Depth of Convolution



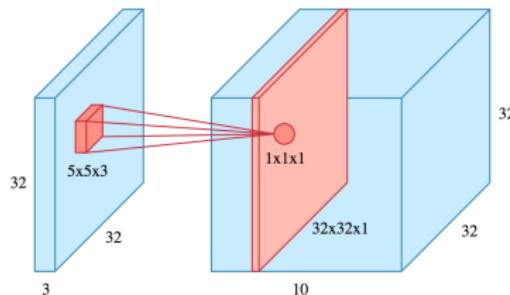
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- Recall, what if we want many feature maps? Use many filters.
- Practice: $n * n * 3$ image, $k * k * 3$ filter, output?
 $(n - k + 1) * (n - k + 1) *$

Depth of Convolution



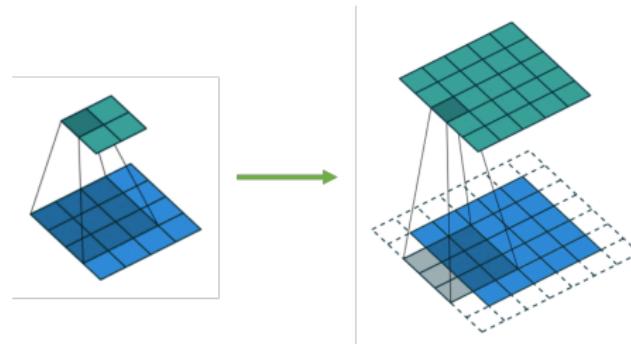
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- Practice: $n * n * 3$ image, $k * k * 3$ filter, output?
 $(n - k + 1) * (n - k + 1) * 1$

Depth of Convolution



- Filter shares the *same depth* with input
- If input image has 3 channels: $200 * 200 * 3 \rightarrow$ the filter should be $n * n * 3$
- Dimension of each convolution operation? Simply, a scalar.
- Recall, what if we want many feature maps? Use many filters.
- Practice: $n * n * 3$ image, $k * k * 3$ filter, output?
 $(n - k + 1) * (n - k + 1) * 1$
- Practice: If there are 10 filters?

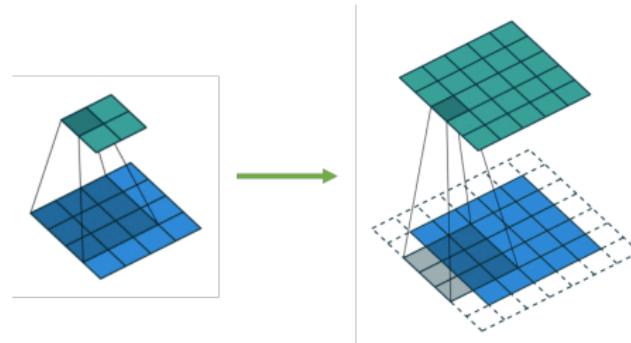
Padding



- Change the size of output, normally with zero [▶ Demo](#)

Image credit: deeplearning.net

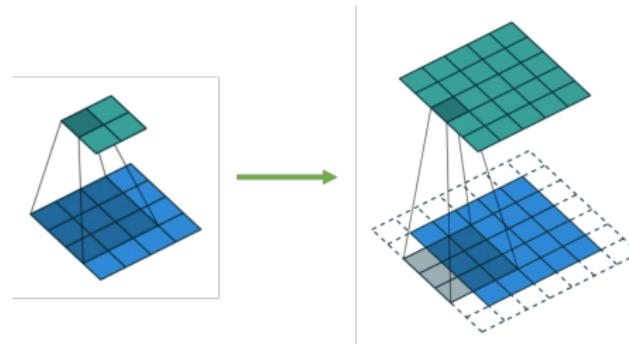
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- Change the size of output, normally with zero [▶ Demo](#)
- There are 2 types of padding
 - *Valid*: no padding

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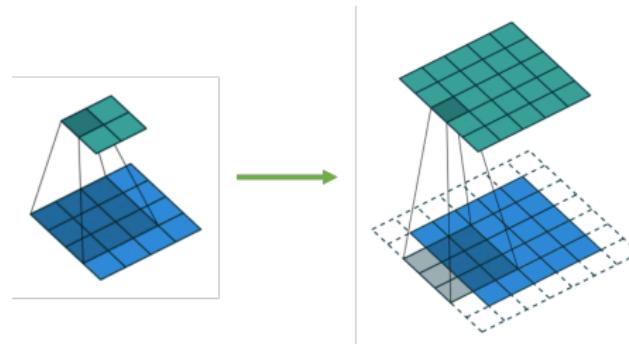
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- There are 2 types of padding
 - *Valid*: no padding
 - *Same*: pad so that output size is the same as input's

Image credit: deeplearning.net

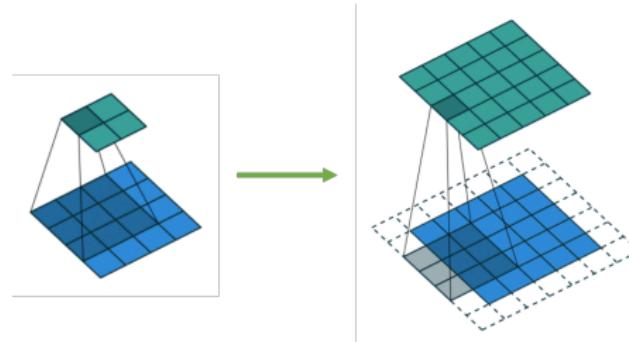
Padding



- Change the size of output, normally with zero [▶ Demo](#)
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- Practice: $n * n$ convolves $k * k$, padding p , output?

Image credit: deeplearning.net

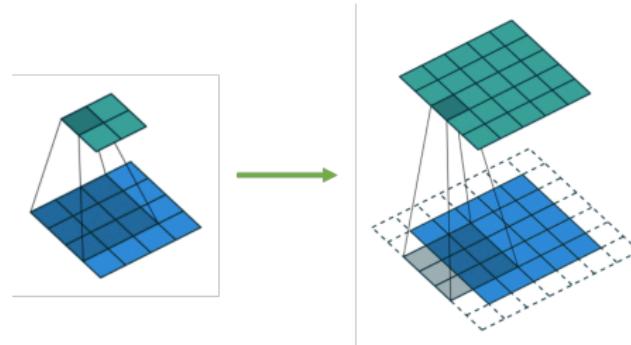
Padding



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 $(n - k + 1 + 2p) * (n - k + 1 + 2p)$

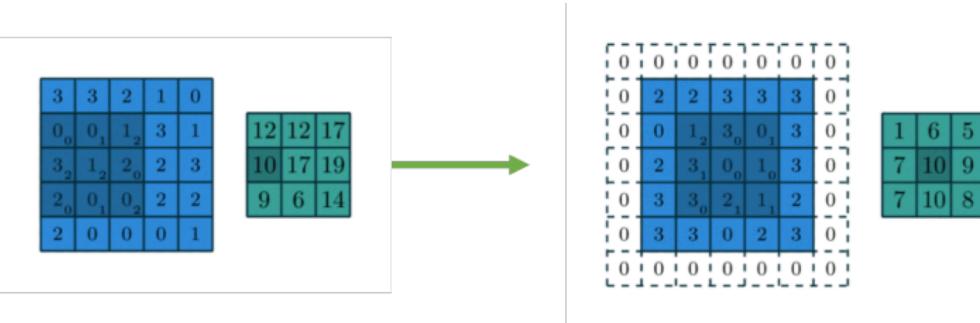
Image credit: deeplearning.net

Padding



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 $(n - k + 1 + 2p) * (n - k + 1 + 2p)$
- Assumption of this formula (and the ones above)?

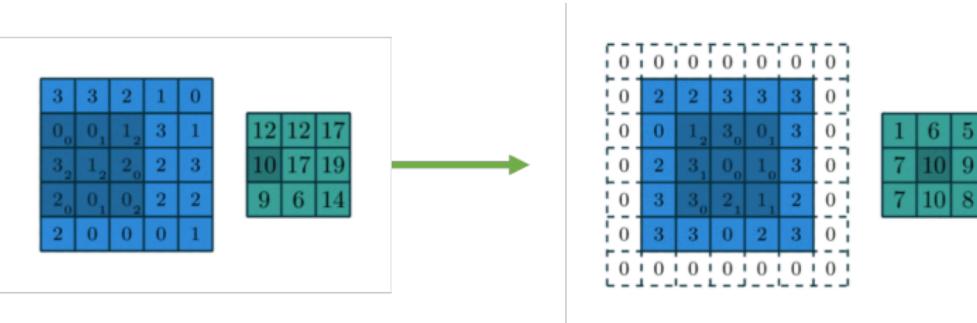
Image credit: deeplearning.net



- Velocity of convolution [▶ Demo](#)
- Practice: 5x5 convolves 3x3
 - Valid padding, stride 1, output?

Image credit: deeplearning.net

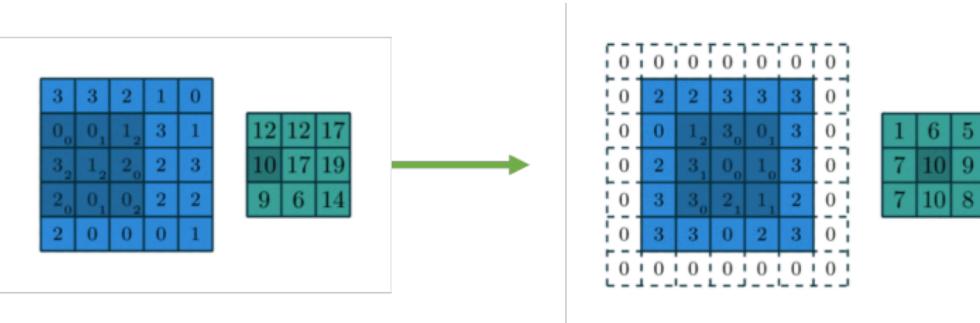
Stride



- Velocity of convolution [▶ Demo](#)
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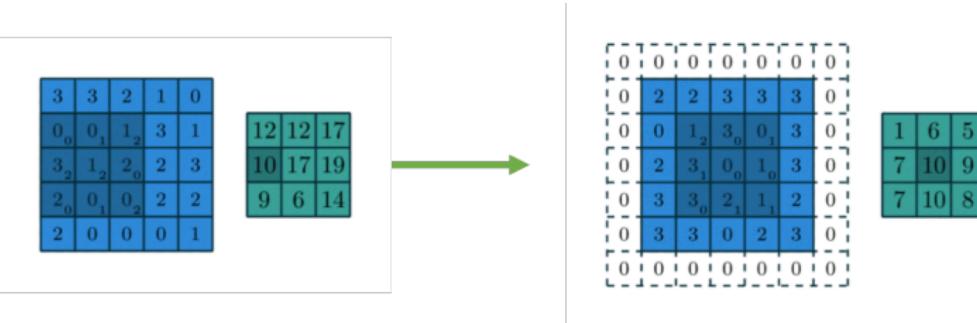
Image credit: deeplearning.net

Stride



- Velocity of convolution [▶ Demo](#)
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 - Valid padding, stride 1, output? $(5 - 3 + 1)(5 - 3 + 1)$
 - Pad 1, stride 1, output? $(5 - 3 + 1 + 2)(5 - 3 + 1 + 2)$
 - Pad 1, stride 2, output?

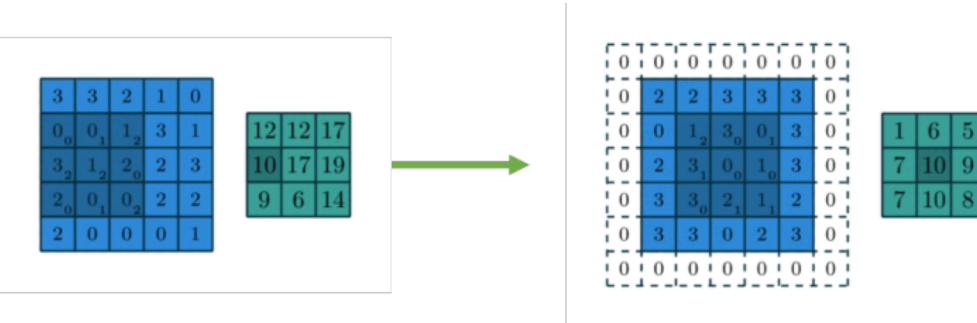
Stride



- Velocity of convolution [▶ Demo](#)
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Image credit: deeplearning.net

Stride



- Velocity of convolution [▶ Demo](#)
- Practice: 5x5 convolves 3x3
 - Valid padding, stride 1, output? $(5 - 3 + 1)(5 - 3 + 1)$
 - Pad 1, stride 1, output? $(5 - 3 + 1 + 2)(5 - 3 + 1 + 2)$
 - Pad 1, stride 2, output? $((5 - 3 + 2)/2 + 1)((((5 - 3 + 2)/2 + 1))$
 - Which one is Same padding?
- So the formula is: $(\frac{n-k+2p}{2} + 1)$, Note: n can vary by dimensions
- Practice: *Same* convolution, how p relates to k ?

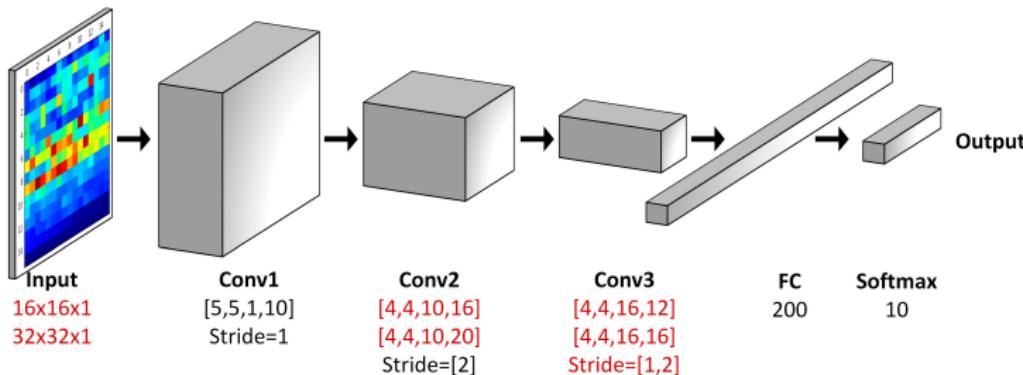
Image credit: deeplearning.net

Break?

Outline

- 1 Recap and motivation
- 2 Convolution
- 3 Convolution in Neural Network
- 4 Pooling
- 5 Case Studies

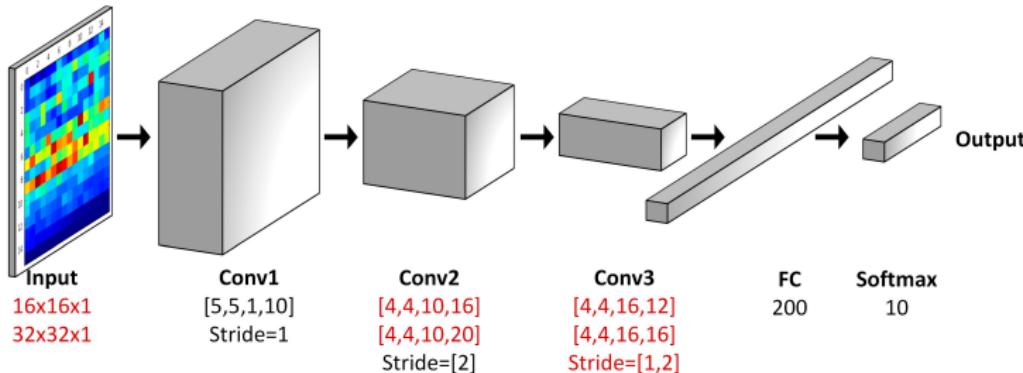
Motivation of Pooling



- Practice: given valid conv and zero padding, identify filter size at each step? Then calculate number of parameters at each step?

Image credit: mdpi.com

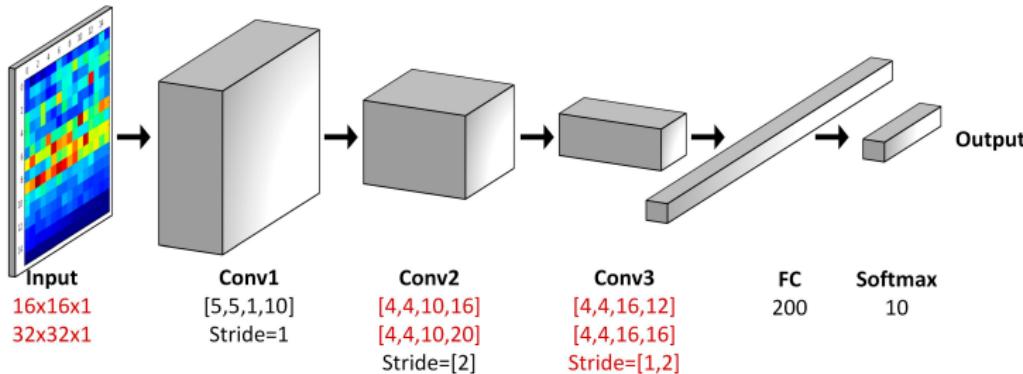
Motivation of Pooling



- Practice: given valid conv and zero padding, identify filter size at each step? Then calculate number of parameters at each step?
- Can we go deeper with this? Imagine the real world cases of 200x200, or even 1024x1024.

Image credit: mdpi.com

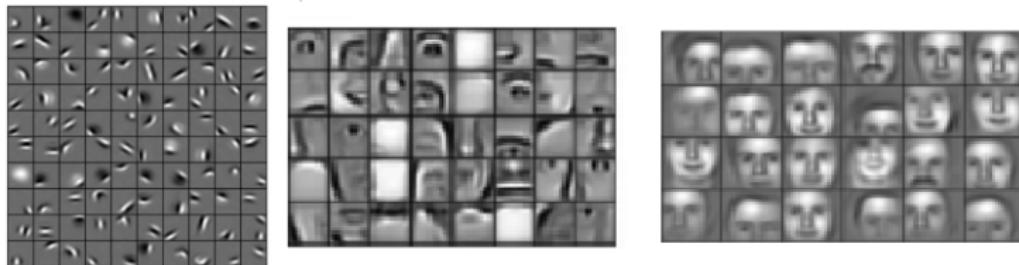
Motivation of Pooling



- Practice: given valid conv and zero padding, identify filter size at each step? Then calculate number of parameters at each step?
- Can we go deeper with this? Imagine the real world cases of 200x200, or even 1024x1024.
- Too many params → overfitting → reduce number of params

Image credit: mdpi.com

More Motivation of Pooling



- We want to reduce size of feature maps to easily control

Image credit: mdpi.com

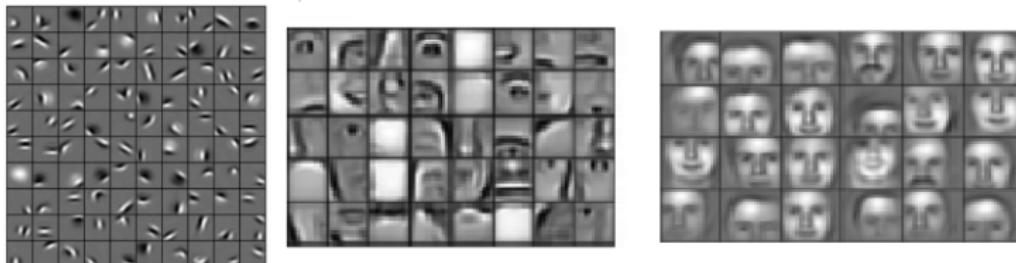
More Motivation of Pooling



- We want to reduce size of feature maps to easily control
- To prevent loss, we summarize features:
 - Each node (scalar) in a feature map represents features of a kernel-size region

Image credit: mdpi.com

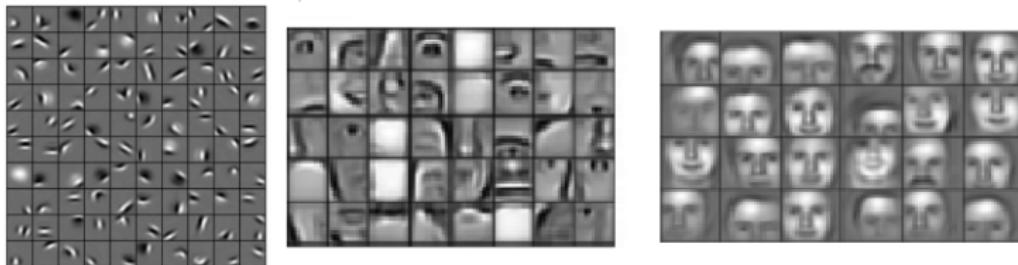
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Image credit: mdpi.com

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Image credit: mdpi.com

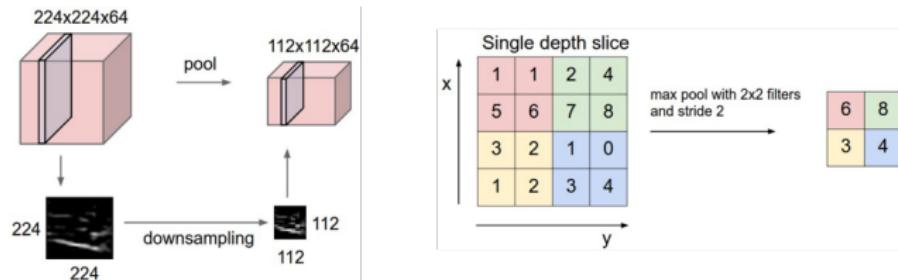
More Motivation of Pooling



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→ *hierarchy*
- To get *translation invariance* for higher object levels

Image credit: mdpi.com

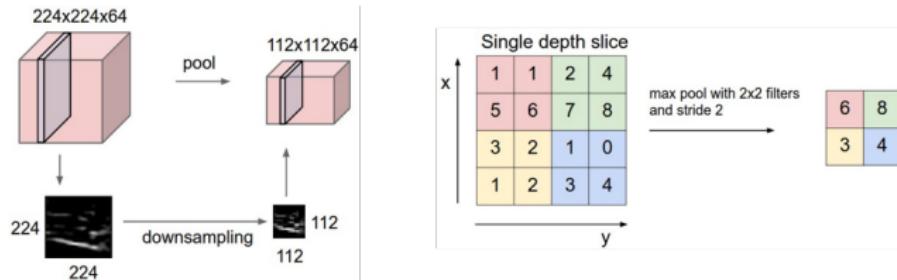
How Pooling Works?



- Process each feature map *independently*
- *a.k.a* subsampling or downsampling process.

Image credit: <http://cs231n.github.io/convolutional-networks>

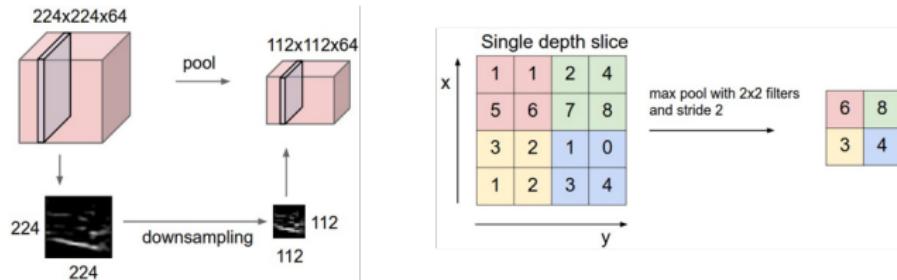
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- Process each feature map *independently*
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- The window is also called a kernel/filter
- Popular types: MAX, AVG
- Practice: 5×5 with filter 3×3 , stride 1, output?

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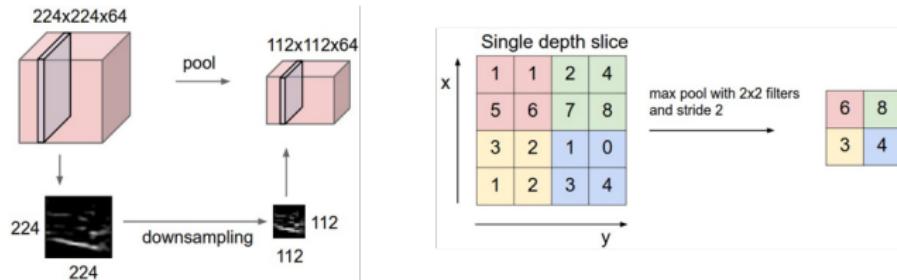
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- Practice: And how many params?

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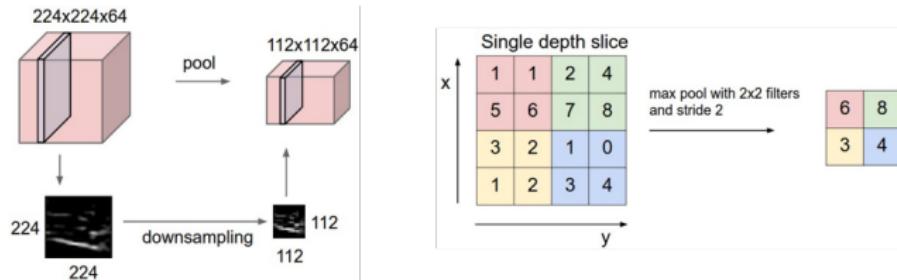
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- Popular types: MAX, AVG
- Practice: 5×5 with filter 3×3 , stride 1, output? 2×2
- Practice: And how many params? Zero

Image credit: <http://cs231n.github.io/convolutional-networks>

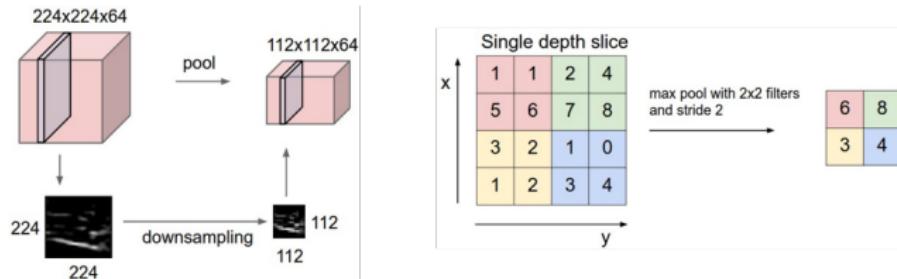
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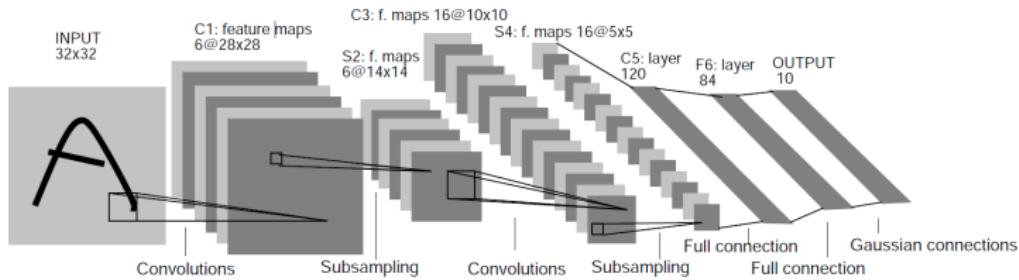


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- The window is also called a kernel/filter
- Popular types: MAX, AVG
- Practice: 5×5 with filter 3×3 , stride 1, output? 2×2
- Practice: And how many params? Zero, and None padding.
- Output formula? $(n - k)/s + 1$

Image credit: <http://cs231n.github.io/convolutional-networks>

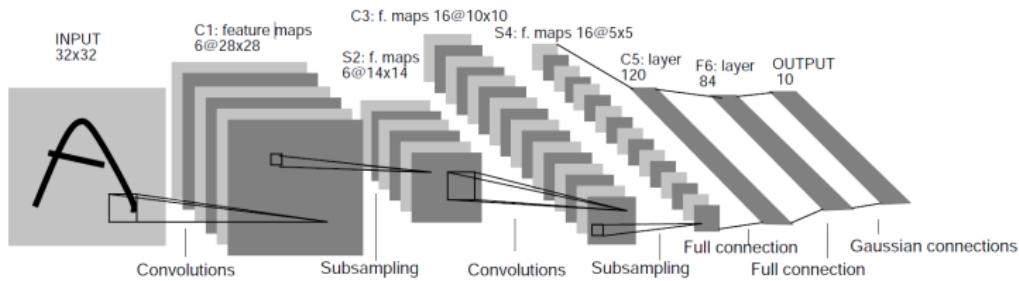
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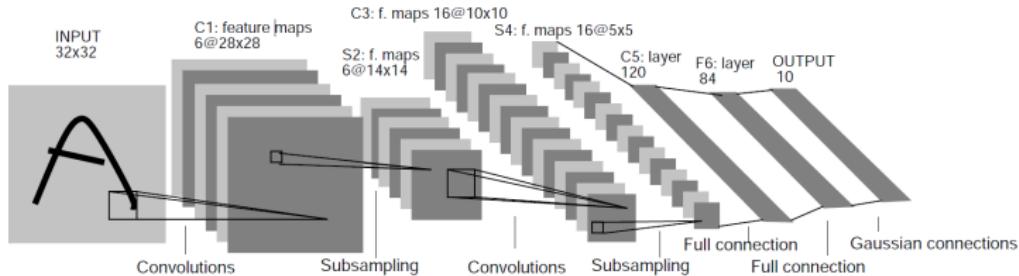
- Practice: what are the sizes of kernels and strides for Conv, and for Pooling?

Image credit: pythonmachinelearning.pro



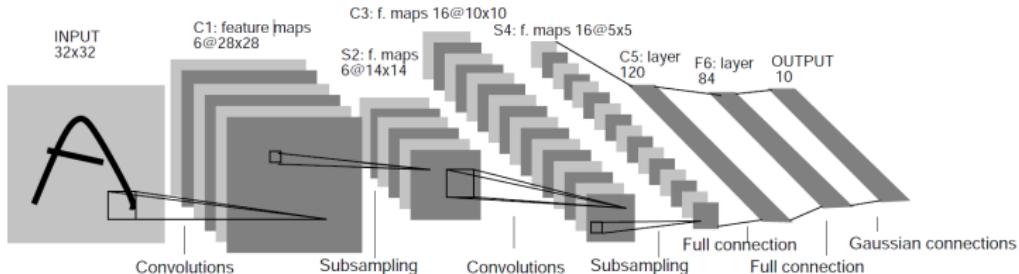
- Practice: what are the sizes of kernels and strides for Conv, and for Pooling? conv: 5x5 and 1, pool: 2x2 and 2
- Practice: how many params at each step?

Image credit: pythonmachinelearning.pro



- Arguably the first CNN that *really* works [▶ Demo](#)
- Practice: what are the sizes of kernels and strides for Conv, and for Pooling?

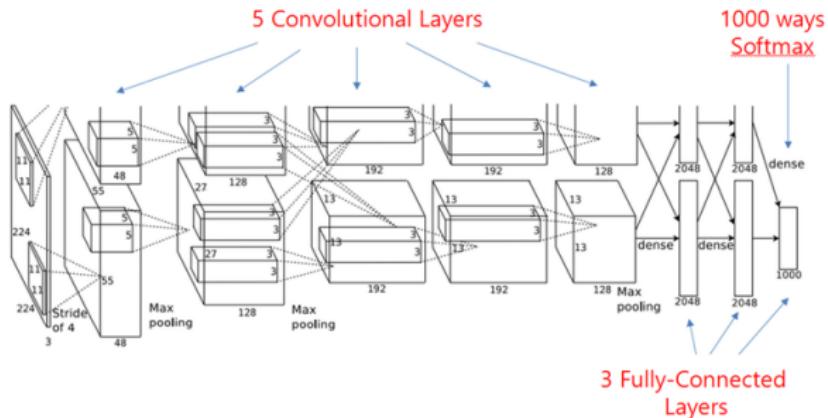
Image credit: Yann Lecun et. al 1998



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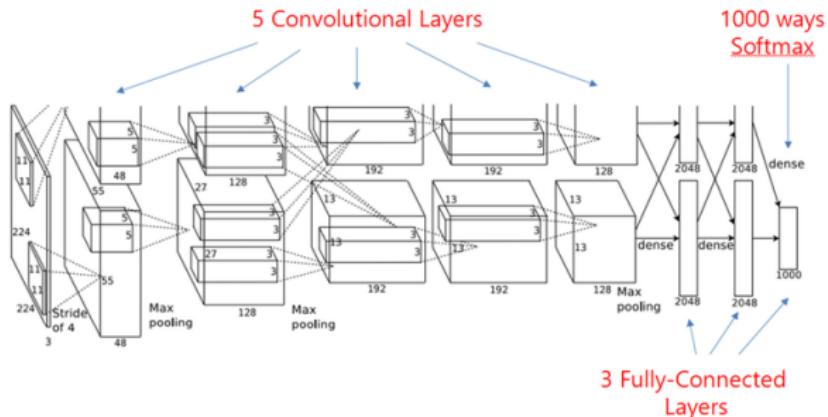
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AlexNet: A Revolution



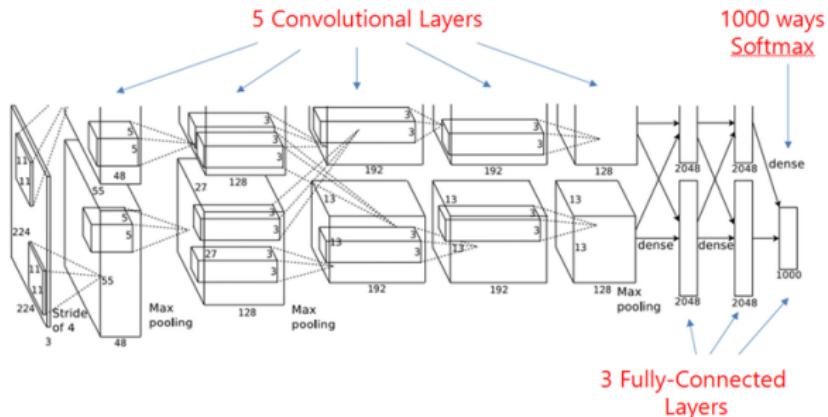
- First use of ReLU, Norm layers, heavy augmentation, dropout, momentum
- Input: 227x227x3
- Conv1: 96 of 11×11 filters, stride 4, output?

AlexNet: A Revolution



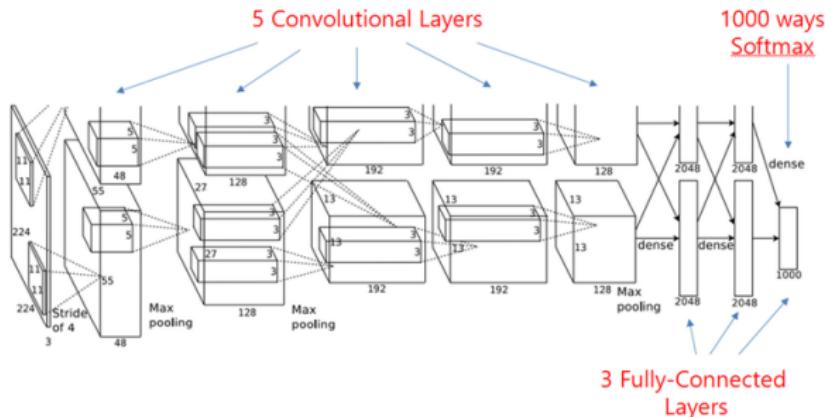
- First use of ReLU, Norm layers, heavy augmentation, dropout, momentum
- Input: 227x227x3
- Conv1: 96 of 11 * 11 filters, stride 4, output? 55 * 55 * 96,

AlexNet: A Revolution



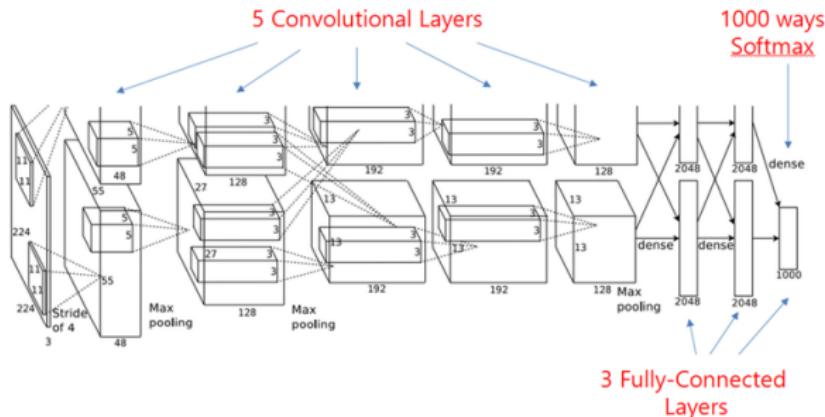
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AlexNet: A Revolution



- First use of ReLU, Norm layers, heavy augmentation, dropout, momentum
- Input: 227x227x3
- Conv1: 96 of 11×11 filters, stride 4, output? $55 \times 55 \times 96$, params? $(11 \times 11 \times 3) \times 96$
- Pool1: 3×3 filter, stride 2, output?

AlexNet: A Revolution



- First use of ReLU, Norm layers, heavy augmentation, dropout, momentum
- Input: 227x227x3
- Conv1: 96 of $11 * 11$ filters, stride 4, output? $55 * 55 * 96$, params? $(11 * 11 * 3) * 96$
- Pool1: $3 * 3$ filter, stride 2, output? $27 * 27 * 96$

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
 $27 \times 27 \times 256$ (same padding),

AlexNet (cont'd)

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 $27 \times 27 \times 256$ (same padding), params?

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
 $27 \times 27 \times 256$ (same padding), params? $(5 \times 5 \times 96) \times 256$
- Pool2: 3×3 filter, stride 2, output?

AlexNet (cont'd)

- Conv2: 256 of $5 * 5$ filters, stride 1, padding 2, output?
 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
- Pool2: $3 * 3$ filter, stride 2, output? $13 * 13 * 256$
- Conv3: 384 of $3 * 3$ filters, stride 1, padding 1, output?

AlexNet (cont'd)

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AlexNet (cont'd)

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 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
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- Conv3: 384 of $3 * 3$ filters, stride 1, padding 1, output?
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- Conv4: 384 of $3 * 3$ filters, stride 1, padding 1, output?

AlexNet (cont'd)

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AlexNet (cont'd)

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- Conv5: 256 of $3 * 3$ filters, stride 1, padding 1, output?

AlexNet (cont'd)

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- Conv3: 384 of $3 * 3$ filters, stride 1, padding 1, output?
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- Conv5: 256 of $3 * 3$ filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding),

AlexNet (cont'd)

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- Conv5: 256 of $3 * 3$ filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
- Pool3: $3 * 3$ filter, stride 2, output?

AlexNet (cont'd)

- Conv2: 256 of $5 * 5$ filters, stride 1, padding 2, output?
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- Conv5: 256 of $3 * 3$ filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
- Pool3: $3 * 3$ filter, stride 2, output? $6 * 6 * 256$
- FC6: 4096 neurons, output?

AlexNet (cont'd)

- Conv2: 256 of $5 * 5$ filters, stride 1, padding 2, output?
 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
- Pool2: $3 * 3$ filter, stride 2, output? $13 * 13 * 256$
- Conv3: 384 of $3 * 3$ filters, stride 1, padding 1, output?
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- Conv2: 256 of $5 * 5$ filters, stride 1, padding 2, output?
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- Conv5: 256 of $3 * 3$ filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
- Pool3: $3 * 3$ filter, stride 2, output? $6 * 6 * 256$
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AlexNet (cont'd)

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- Conv3: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 256) * 384$
- Conv4: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 384) * 384$
- Conv5: 256 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
- Pool3: 3×3 filter, stride 2, output? $6 * 6 * 256$
- FC6: 4096 neurons, output? 4096, params? $6 * 6 * 256 * 4096$
- FC7: 4096 neurons, output?

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
- Pool2: 3×3 filter, stride 2, output? $13 * 13 * 256$
- Conv3: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 256) * 384$
- Conv4: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 384) * 384$
- Conv5: 256 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
- Pool3: 3×3 filter, stride 2, output? $6 * 6 * 256$
- FC6: 4096 neurons, output? 4096, params? $6 * 6 * 256 * 4096$
- FC7: 4096 neurons, output? 4096,

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
- Pool2: 3×3 filter, stride 2, output? $13 * 13 * 256$
- Conv3: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 256) * 384$
- Conv4: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 384) * 384$
- Conv5: 256 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
- Pool3: 3×3 filter, stride 2, output? $6 * 6 * 256$
- FC6: 4096 neurons, output? 4096, params? $6 * 6 * 256 * 4096$
- FC7: 4096 neurons, output? 4096, params?

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
- Pool2: 3×3 filter, stride 2, output? $13 * 13 * 256$
- Conv3: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 256) * 384$
- Conv4: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 384) * 384$
- Conv5: 256 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
- Pool3: 3×3 filter, stride 2, output? $6 * 6 * 256$
- FC6: 4096 neurons, output? 4096, params? $6 * 6 * 256 * 4096$
- FC7: 4096 neurons, output? 4096, params? $4096 * 4096$
- FC8: 1000 neurons, output?

AlexNet (cont'd)

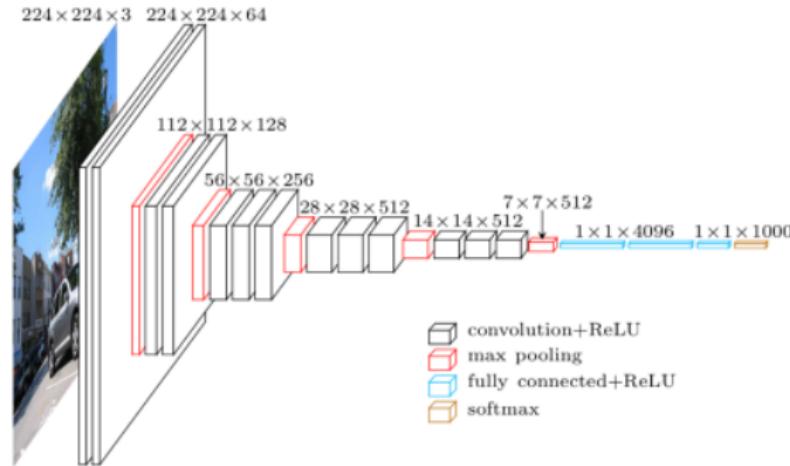
- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
- Pool2: 3×3 filter, stride 2, output? $13 * 13 * 256$
- Conv3: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 256) * 384$
- Conv4: 384 of 3×3 filters, stride 1, padding 1, output?
 $13 * 13 * 384$ (same padding), params? $(3 * 3 * 384) * 384$
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- FC7: 4096 neurons, output? 4096, params? $4096 * 4096$
- FC8: 1000 neurons, output? 1000,

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
 $27 * 27 * 256$ (same padding), params? $(5 * 5 * 96) * 256$
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- FC8: 1000 neurons, output? 1000, params?

AlexNet (cont'd)

- Conv2: 256 of 5×5 filters, stride 1, padding 2, output?
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 $13 * 13 * 256$ (same padding), params? $(3 * 3 * 384) * 256$
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- FC6: 4096 neurons, output? 4096, params? $6 * 6 * 256 * 4096$
- FC7: 4096 neurons, output? 4096, params? $4096 * 4096$
- FC8: 1000 neurons, output? 1000, params? $4096 * 1000$



- Got 11.2% top 5 error at ILSVRC 2013

Image credit: David Frossard

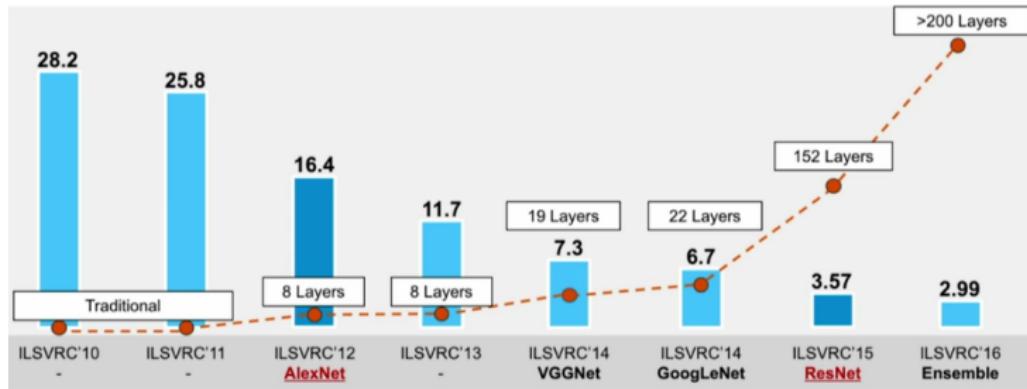


Image credit: SQLML