



A Brief History of Early Mechanical Computation

15-110 supplemental slides, 11/25/24



Taking a step back...

- Most “History of Computing” lectures begin around the time of Babbage, Lovelace, and the Analytical Engine in the early 1800s
- If we broaden our perspective on computation, its history stretches *much* farther back

**What is computing? What is a
computer?**

Let's use a loose definition

- Loosely, something that generates an output given a particular set of inputs or initial configuration
- We'll restrict ourselves to inputs and outputs that (mathematically) represent concepts or parts of problems
- Generally they solve (or allow us to solve) a set of problems faster
- A simple example: multiplication tables

Multiplication Square

x	1	2	3	4	5	6	7	8	9	10
1	1	2	3	4	5	6	7	8	9	10
2	2	4	6	8	10	12	14	16	18	20
3	3	6	9	12	15	18	21	24	27	30
4	4	8	12	16	20	24	28	32	36	40
5	5	10	15	20	25	30	35	40	45	50
6	6	12	18	24	30	36	42	48	54	60
7	7	14	21	28	35	42	49	56	63	70
8	8	16	24	32	40	48	56	64	72	80
9	9	18	27	36	45	54	63	72	81	90
10	10	20	30	40	50	60	70	80	90	100

Function tables: How do they “work?”

It stores precomputed knowledge that we can systematically access to perform calculations faster.

To the right is an image of a rather intimidating logarithm table ---->

Multiplication Square

x	1	2	3	4	5	6	7	8	9	10
1	1	2	3	4	5	6	7	8	9	10
2	2	4	6	8	10	12	14	16	18	20
3	3	6	9	12	15	18	21	24	27	30
4	4	8	12	16	20	24	28	32	36	40
5	5	10	15	20	25	30	35	40	45	50
6	6	12	18	24	30	36	42	48	54	60
7	7	14	21	28	35	42	49	56	63	70
8	8	16	24	32	40	48	56	64	72	80
9	9	18	27	36	45	54	63	72	81	90
10	10	20	30	40	50	60	70	80	90	100

TABLE I
Logarithms of Numbers

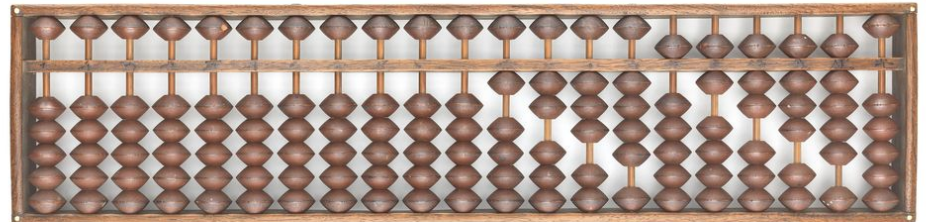
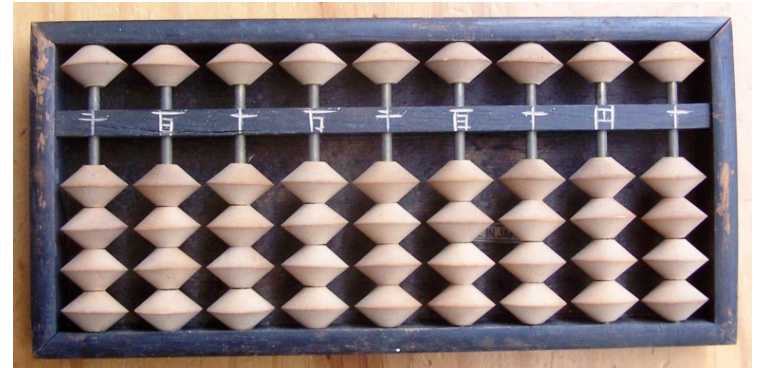
1000-1500

No.	0	d	1	d	2	d	3	d	4	d	5	d	6	d	7	d	8	d	9	d	Prop. parts
100	00003	00083	00087	00130	00133	00173	00217	00260	00303	00346	00389	00431	00473	00515	00557	00600	00642	00684	00726	00768	41 43
101	00432	00475	00518	00561	00604	00647	00689	00732	00775	00817	00860	00902	00945	00987	01030	01072	01115	01157	01200	01242	44 46
102	00866	00903	00945	00988	01030	01072	01115	01157	01200	01242	01284	01326	01368	01410	01452	01494	01536	01578	01620	01662	47 49
103	01286	01329	01381	01440	01500	01560	01620	01680	01740	01800	01860	01920	01980	02040	02100	02160	02220	02280	02340	02400	51 53
104	01703	01745	01787	01828	01870	01912	01953	01995	02036	02078	02120	02162	02204	02246	02288	02330	02372	02414	02456	02498	55 57
105	02119	02160	02202	02243	02284	02325	02366	02407	02449	02490	02532	02574	02616	02658	02700	02742	02784	02826	02868	02910	59 61
106	02531	02572	02613	02653	02694	02735	02776	02816	02857	02898	02939	02980	03021	03062	03103	03144	03185	03226	03267	03308	63 65
107	02938	02979	03019	03060	03100	03141	03181	03222	03262	03302	03343	03383	03424	03464	03505	03545	03586	03626	03667	03707	67 69
108	03342	03383	03423	03463	03503	03544	03584	03624	03664	03704	03745	03785	03825	03865	03906	03946	03986	04027	04067	04107	71 73
109	03743	03783	03823	03863	03903	03943	03983	04023	04063	04103	04143	04183	04223	04263	04303	04343	04383	04423	04463	04503	75 77
110	04139	04179	04218	04258	04297	04336	04376	04415	04454	04493	04533	04572	04612	04651	04691	04730	04770	04809	04848	04888	79 81
111	04532	04571	04610	04649	04689	04727	04766	04805	04844	04883	04922	04961	04999	05039	05078	05117	05156	05195	05234	05273	83 85
112	04922	04961	05000	05039	05078	05117	05156	05195	05234	05273	05312	05351	05390	05429	05468	05507	05546	05585	05624	05663	87 89
113	05308	05346	05385	05423	05461	05500	05538	05576	05614	05652	05691	05729	05767	05806	05844	05883	05921	05959	06000	06038	91 93
114	05600	05637	05675	05712	05750	05788	05825	05863	05900	05938	05975	06013	06051	06088	06126	06164	06202	06240	06278	06316	95 97
115	06070	06107	06145	06183	06221	06258	06296	06333	06371	06408	06446	06483	06521	06558	06596	06634	06671	06709	06746	06784	99 101
116	06446	06483	06521	06558	06596	06633	06671	06709	06746	06784	06821	06858	06896	06933	06971	07008	07045	07083	07120	07157	103 105
117	06819	06856	06893	06930	06967	07004	07041	07078	07115	07151	07188	07225	07262	07299	07336	07373	07410	07447	07484	07521	107 109
118	07188	07225	07262	07299	07336	07373	07410	07447	07484	07521	07558	07595	07632	07669	07706	07743	07780	07817	07854	07891	111 113
119	07555	07591	07628	07664	07700	07737	07773	07809	07846	07882	07918	07955	07991	08028	08064	08101	08137	08174	08210	08247	115 117
120	07918	07954	07990	08027	08063	08099	08135	08171	08207	08243	08279	08315	08351	08387	08423	08459	08495	08531	08567	08603	119 121
121	08279	08314	08350	08386	08422	08458	08493	08529	08565	08600	08636	08672	08708	08744	08780	08816	08852	08888	08924	08960	123 125
122	08636	08672	08707	08743	08778	08814	08849	08884	08920	08955	08991	09026	09062	09097	09133	09168	09204	09239	09275	09310	127 129
123	08891	08926	08961	08996	09032	09067	09102	09137	09173	09208	09243	09279	09314	09349	09384	09419	09455	09490	09525	09560	131 133
124	09343	09377	09412	09447	09482	09517	09552	09587	09621	09656	09691	09726	09761	09796	09831	09866	09901	09936	09971	10006	135 137
125	09691	09726	09761	09796	09831	09866	09901	09936	09971	10006	10041	10076	10111	10146	10181	10216	10251	10286	10321	10356	139 141
126	10037	10072	10106	10140	10175	10209	10243	10278	10312	10347	10381	10416	10450	10485	10519	10554	10588	10623	10657	10692	143 145
127	10180	10214	10249	10283	10317	10351	10385	10419	10453	10487	10521	10555	10589	10623	10657	10691	10725	10759	10793	10827	147 149
128	10721	10755	10789	10823	10857	10891	10925	10959	10993	11027	11061	11095	11129	11163	11197	11231	11265	11299	11333	11367	151 153
129	11059	11093	11126	11160	11193	11227	11261	11294	11327	11361	11395	11429	11462	11496	11530	11564	11598	11632	11666	11700	155 157
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131	11727	11760	11793	11826	11860	11893	11926	11959	11992	12024	12058	12091	12125	12158	12192	12225	12259	12292	12326	12359	163 165
132	12057	12090	12123	12156	12189	12222	12255	12288	12321	12354	12387	12420	12453	12486	12519	12552	12585	12618	12651	12684	167 169
133	12385	12418	12450	12483	12516	12549	12581	12614	12647	12680	12713	12746	12779	12811	12844	12877	12910	12943	12976	13009	171 173
134	12710	12743	12775	12808	12840	12872	12905	12937	12969	13001	13033	13065	13097	13129	13161	13193	13225	13257	13289	13321	175 177
135	13033	13066	13098	13130	13162	13194	13226	13258	13290	13322	13354	13386	13418	13450	13482	13514	13546	13578	13610	13642	179 181
136	13354	13386	13418	13450	13481	13513	13545	13577	13609	13640	13672	13704	13736	13767	13800	13831	13863	13895	13926	13958	183 185
137	13672	13704	13735	13767	13799	13830	13862	13893	13925	13956	13987	14019	14050	14082	14113	14145	14176	14208	14239	14270	187 189
138	13988	14019	14051	14082	14114	14145	14176	14208	14239	14270	14301	14332	14363	14394	14425	14456	14487	14518	14549	14580	191 193
139	14301	14333	14364	14395	14426	14457	14489	14520	14551	14582	14613	14644	14675	14706	14737	14768	14799	14829	14860	14891	195 197
140	14613	14644	14675	14706	14737	14768	14799	14829	14860	14891	14921	14952	14983	15013	15044	15074	15105	15135	15166	15196	199 201
141	14922	14953	14983	15014	15045	15076	15106	15137	15168	15198	15229	15259	15289	15319	15349	15379	15409	15439	15469	15499	203 205
142	15229	15259	15290	15320	15351	15381	15412	15442	15472	15503	15533	15563	15594	15624	15654	15684	15714	15744	15774	15804	207 209
143	15534	15564	15594	15625	15655	15685	15715	15746	15776	15806	15836	15866	15896	15926	15956	15986	16016	16046	16076	16106	211 213
144	15836	15866	15897	15927	15957	15987	16017	16047	16077	16107	16137	16167	16197	16227	16257	16287	16317	16347	16377	16407	215 217
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146	16436	16466	16496	16526	16556	16586	16616	16646	16676	16706	16736	16766	16796	16826	16856	16886	16916	16946	16976	17006	223 225
147	16732	16761	16791	16820	16850	16879	16909	16938	16967	16997	17026	17056	17085	17114	17144	17173	17202	17231	17260	17289	227 229
148	17026	17056	17085	17114	17143	17173	17202	17231	17260	17289	17318	17347	17376	17405	17434	17463	17492	17521	17550	17579	231 233
149	17319	17348	17377	1																	

Simple computers

The abacus: 2500BC to present

- Originally lines drawn in sand, pebbles
- Oldest known “computer,” excluding simple counting aids like tally sticks
- Procedural interaction allows user to perform four-function math on large numbers by storing an intermediate state
- Still in widespread use until recent decades
 - Japanese soroban was taught nationally and used in business until recently
- <http://www.mathematik.uni-marburg.de/~thormae/lectures/ti1/code/abacus/soroban.html>



Napier's Bones (1617)

Physical aid for multiplying large numbers

Represented with pen and paper or with inscribed rods: <http://mathworld.wolfram.com/NapiersBones.html>

John Napier also invented logarithms!



Slide rules: 1620 - 1950

Basic principle:

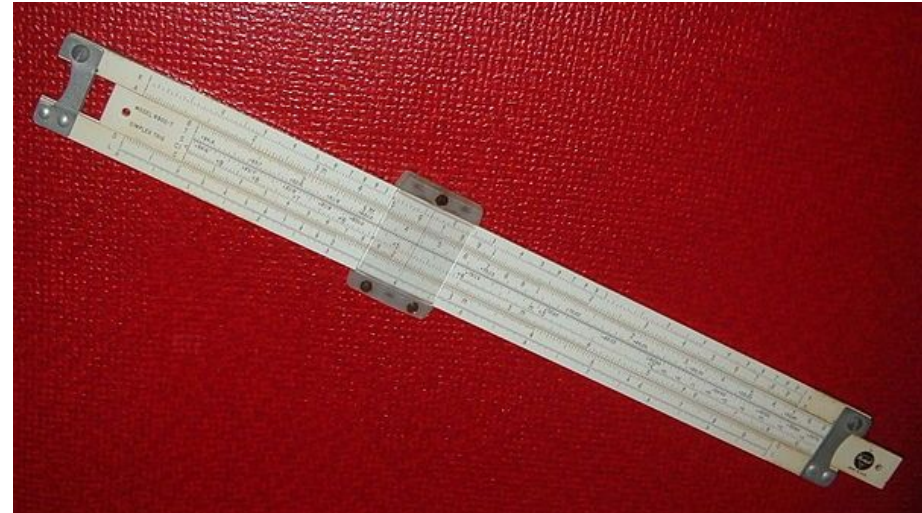
$$\log(xy) = \log(x) + \log(y)$$

$$\log(x/y) = \log(x) - \log(y)$$

Multiplication and division can be quickly performed using the sum of logarithms!

https://en.wikipedia.org/wiki/Slide_rule

<http://www.antiquark.com/sliderule/sim/virtual-slide-rule.html>



Mechanical calculators (1623 - 1970)

Similar function to previous tools, but meant to be more convenient or automatic



Antikythera mechanism

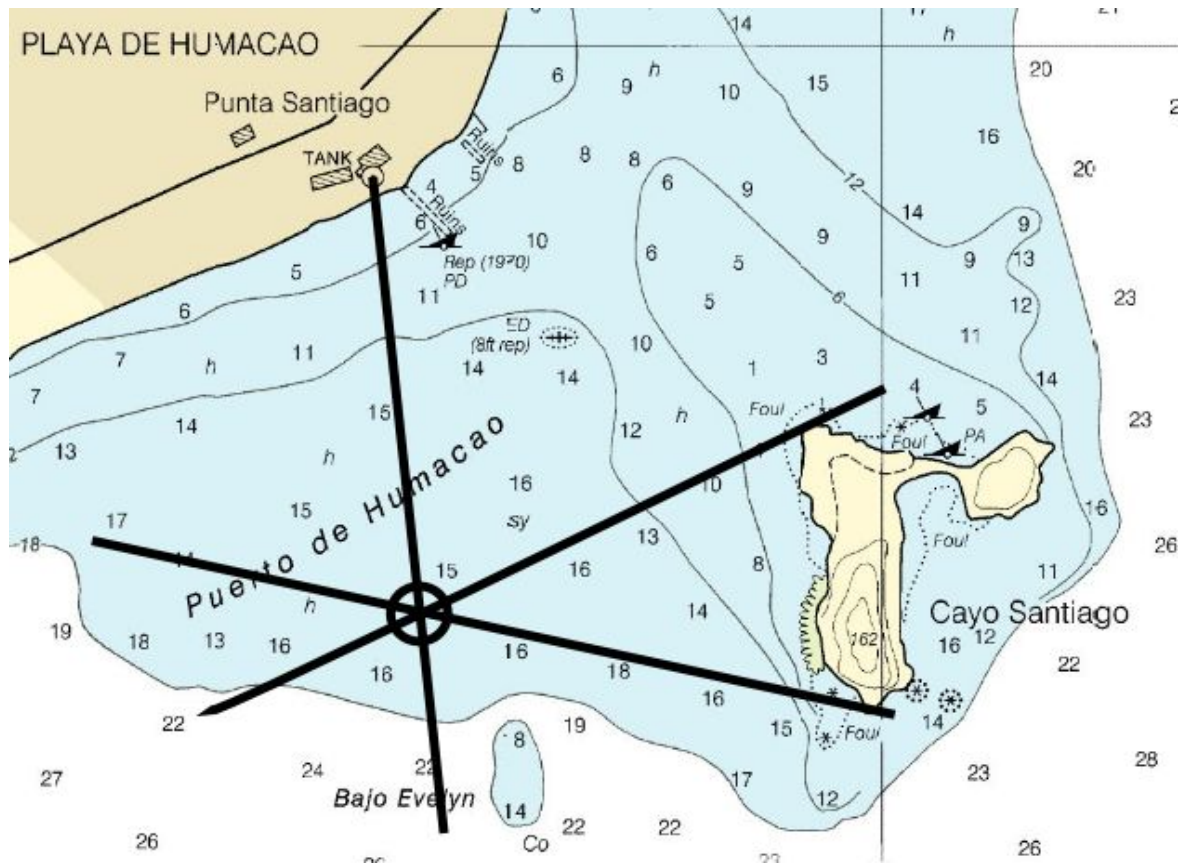
Mechanical complexity is *ancient*

- Antikythera mechanism: 2100 years old
- Accurately calculates celestial positions, eclipses, etc
- <https://www.youtube.com/watch?v=UpLcnAlpVRA&feature=youtu.be&t=164>
- Discuss: Why might this have been built?



Navigation!

A major incentive for innovation



Positional navigation using landmarks



Sextants, astrolabes, etc for measuring angles



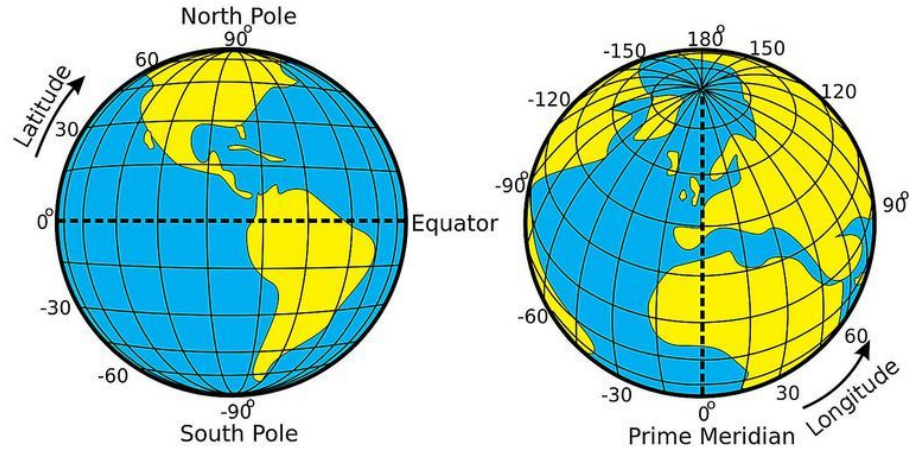
Time!

**Can't navigate across an ocean
without knowing the time.**

Why is time important for navigational calculations?

- When we travel long distances, the sky changes
- Small errors are a big deal over large voyages

- So let's build a clock! Why is this hard?
 - Mechanical
 - No way to correct fast/slow if clock if you're alone in the ocean (don't know where)
 - Clock must be *extremely* accurate and precise, even through rough weather





Quick aside: How long have battery-powered watches been widespread?



Quick aside: How long have battery-powered watches been widespread?

Before the 1980s, most watches were entirely mechanical.

The first “electric” watches from 1969 were absurdly expensive and still relied on mechanical regulation of time.

The first all-digital watch cost more than \$2k when it first came out in 1970.



What functional parts do we need for a mechanical timekeeper?

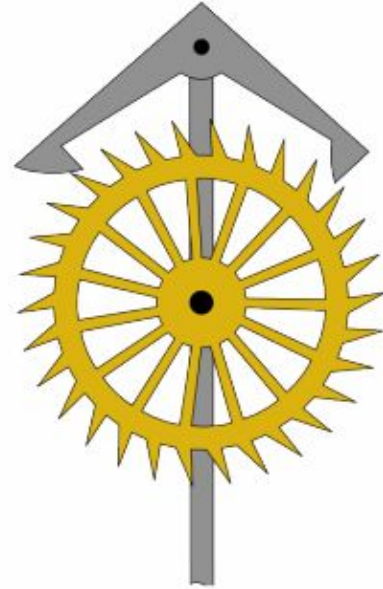
1. A way to store energy (a spring)
2. A way to convert between seconds, minutes, and hours (gears)
3. Most importantly: A way to move the hands at a very constant rate. **Ideate: How would you do that?**

The Escapement

- Why watches and clocks “tick”
- <https://en.wikipedia.org/wiki/Escapement>
- The escapement keeps the spring from rapidly unwinding
- A pendulum (or escape wheel, i.e. a rotary pendulum) allows the gears to advance a fixed amount at every oscillation
- The escapement also injects energy to keep the pendulum moving

Explanatory video:

https://youtu.be/rL0_vOw6eCc?t=370



Back to navigation

- Early timepieces were still inaccurate
- Isochronism: The ability to keep time at a constant rate over long periods of time
- 1714: British government offers the Longitude Prize, \$4 million in 2019 currency for the first clock accurate enough for navigation
 - John Harrison wins the prize in 1761 after 31 years of dedicated work to improve the escapement
 - Chronometer escapement:
 - <https://www.youtube.com/watch?v=cQvopnjDI6E>

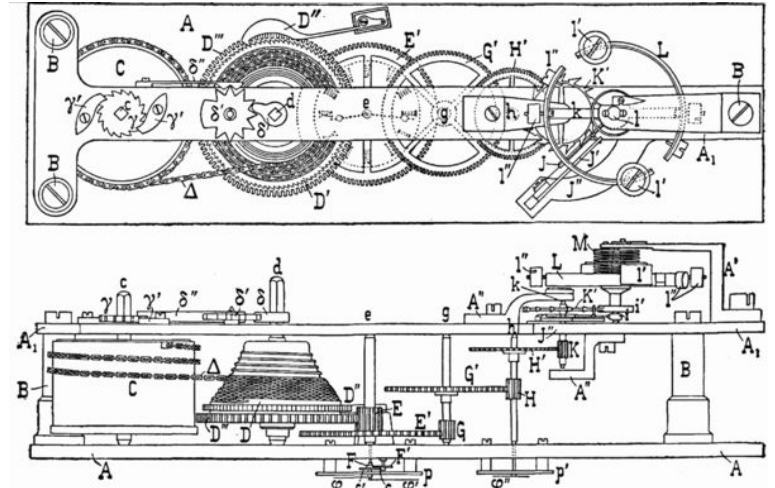


Fig. 1. *A* obere Platine. *A*₁ untere Platine. *A'* Brücke der Unruhe. *A''* Brücke der Hemmung. *B* Pfeiler der Platine. *C* Federhaus. *c* Federwelle. *γ* Sperrad für die Feder. *γ'* Sperrkegel. *D* Schnecke. *D'* Gegenperrad. *D''* Sperrfeder für das Gegenperrad. *D'''* Schneckenrad. *d* Schneckenwelle. *Δ* Kette. *δ* Zahn der Stellung. *δ'* Stellungrad. *δ''* Stellungsfeder. *E* Trieb des Großbodenrads. *E'* Großbodenrad. *e* Achse des Großbodenrads. *F* Minutenrohr. *F'* Wechleirad. *f* Trieb des Wechleirads. *f'* Stundenrad. *φ* Stundenzeiger. *φ'* Minutenzeiger. *G* Trieb des Kleinbodenrads. *G'* Kleinbodenrad. *g* Achse des Kleinbodenrads. *H* Trieb des Sekundenrads. *H'* Sekundenrad. *h* Achse des Sekundenrads. *J* Hemmungsfeder. *J'* Anschlagkloben für die Hemmungsfeder. *J''* Brücke der Hemmungsfeder. *i* Kleine Rolle. *i'* Große Rolle. *K* Trieb des Hemmungsrads. *K'* Hemmungsrad. *k* Steg der Unruhe. *L* Unruhe. *l* Achse der Unruhe. *l'* Kompensationsgewichte. *l''* Regulierchrauben. *M* Spirale.

From watches to automata: Machines with programs



Other (more impressive) automata

Birdcage automata

Brittany Nicole Cox and Antiquarian Horology: <https://www.youtube.com/watch?v=irdTng8MbIE>

Late 1700s Creepy music robot: <https://www.youtube.com/watch?v=nITEU4fsgCU>

Late 1700s Writing robot: <https://www.youtube.com/watch?v=C7oSFNKllaM>

And now we're back to Babbage