

Exercise: Counting operations

Given lists of length N ,

Calculate how many multiplications and additions/subtractions are in the following functions. Write your answers in terms of N .

Note: Don't worry about square-root operations.

	Additions+Subtractions	Multiplications
dot(vec1, vec2)	N	N
distance(x1, y1, x2, y2)	3	2
distanceTable	$3N^2$	$2N^2$
distanceTableEfficient	$N + 3(N^2 - N)/2$	$2(N^2 - N)/2$

$$N + 3(1 + 2 + \dots + N - 1)$$

```
def dot(vec1, vec2):
    N = len(vec1)
    result = 0
    for i in range(N):
        val1 = vec1[i]
        val2 = vec2[i]
        result = result + val1*val2

    return result
```

Arithmetic sequence:

$$1 + 2 + 3 + \dots + (N - 2) + (N - 1)$$

$$= \sum_{i=0}^{N-1} i = (N^2 - N)/2$$

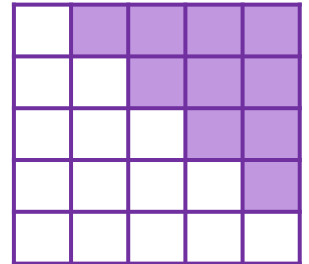
```
def distance(x1, y1, x2, y2):
    dx = x1-x2
    dy = y1-y2
    return math.sqrt(dx*dx + dy*dy)
```

Geometry version:

(Square area – diagonal)

divided by two

$$(N^2 - N)/2$$



```
def distanceTable(pointList):
    # Distance between all pairs of
    # points

    N = len(pointList)

    for i in range(N):
        for j in range(N):
            p1 = pointList[i]
            p2 = pointList[j]
            d = distance(p1[0], p1[1],
                        p2[0], p2[1])
            print(d, end='\t')
        print()
```

```
def distanceTableEfficient(pointList):
    # Distance between all pairs of
    # points (without repeats)

    N = len(pointList)

    for i in range(N):
        start = i+1
        for j in range(start, N):
            p1 = pointList[i]
            p2 = pointList[j]
            d = distance(p1[0], p1[1],
                        p2[0], p2[1])
            print(d, end='\t')
        print()
```