



# 15-110 Exam 2 Review

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# Dictionaries

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# Dictionaries

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- Dictionaries store data in **pairs** by mapping **keys** to **values**.
- We'll be able to access the value by looking up the key, like how we can access a list value using its index.
- Keys must be **immutable** (numbers, strings, booleans)
- Values can be any type of data
- Making empty dictionary: `d = {}` or `d = dict()`
- Looking through a dictionary

```
for <itemVariables> in <iterableValue>:
```

```
    <itemActionBody>
```

# Basic Dictionary Implementation

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```
d = { "apples" : 3, "pears" : 4 }
```

## Getting values:

- d["apples"] => give us the value pair 3
- len(d) => gives us length of dictionary
- d["ice cream"] => key error because ice cream is not a key in d

## Adding/Removing values:

- d["bananas"] = 7  
=> adds new key-value pair
- d["apples"] = d["apples"] + 1  
=> updates key-value pair
- d.pop("pears") => destructively removes

## Searching:

- "apples" in d => returns true
- "kiwis" in d => returns false

# Trees

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- Trees hold hierarchical data => data occurs at different levels and are connected
- Core parts of a tree include: nodes, children, the root, and leaves
- A node has exactly one parent, a parent can have any number of children
- Trees are **recursive!**
  - Each node's children are subtrees which are trees again
  - **Base case** - can be either a leaf or empty tree
  - **Recursive case** - makes problem smaller by repeating on the children
- Binary Trees: have at most 2 children per node

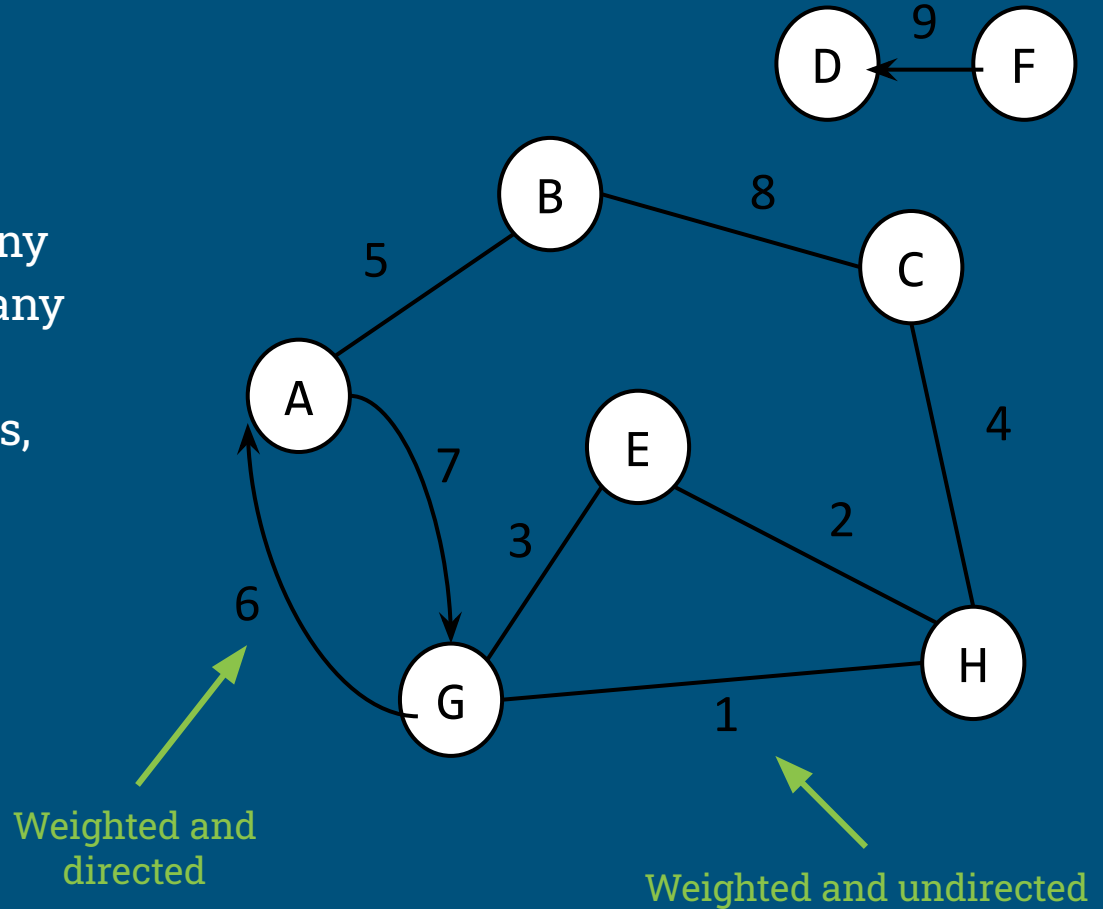
# Coding with Trees

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- Trees are implemented by recursively nested dictionaries
- Each **node** of the tree will be a dictionary that has three keys
  - First key is the string "contents" => value in the node
  - Second key is "left" => either maps to node if node has left child OR None if there is no left child
  - Third key is "right" => either maps to node if node has right child OR None if there is no right child
- Using recursion when coding with trees
  - **Base case:** when current node is a leaf and we need to do something its value
  - **Recursive case:** call function recursively on left child and then call again on right child, if they exist.

# Graphs

- Graphs are like trees, but any node can be connected to any other node
- Core parts of a graph: nodes, edges, neighbors
- Edges can be weighted or unweighted
- Edges can be directed or undirected



# Coding with Graphs

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- The **keys** of the dictionary will be the **values** of the nodes. Each node maps to a **list of its adjacent nodes (neighbors)**, the nodes it has a direct connection with.
- Weighted graphs have values associated with the edges. We need to store these values in the dictionary also
  - We'll do this by changing the list of adjacent nodes to be a **2D list**. Each of the inner lists represents a node/edge pair, so it has two values – the adjacent node's value and the weight of the edge.



Big O



# Best Case & Worst Case

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- Best case:
  - an input of size  $n$  that results in the algorithm taking the least steps possible.
- Worst case:
  - an input of size  $n$  that results in the algorithm taking the most steps possible.

**Consider a function that takes in a list of strings as an input and uses linear search to return the second occurrence of the string, "a" in the list.**

**What's the best case?**

**What's the worst case?**

# Big O

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- When determining which Big O represents the actions taken by an algorithm, we say that **n is the size of the input**
  - For a list, that's the number of elements
  - For a string, that's the number of characters
- To determine an algorithm's Big O, you **ignore constant factors and smaller terms**
  - $3n + 8$  is just  $O(n)$
  - $4n^2$  is just  $O(n^2)$
- Big O is generally the **worst case** runtime of an algorithm

# How to Calculate Big O

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- Calculate the Big-O of each line/action of a function
  - Add sequential and conditional statements
  - Multiply the actions within a loop by the number of iterations performed
  - Get rid of constants and smaller terms!
- Watch out for built-in functions!
  - `L.count(elem)` #  $O(n)$
  - `L.remove(elem)` #  $O(n)$
  - `L.pop(0)` # worst case  $O(n)$

## Practice:

```
def f(L):  
    result = []  
    for i in range(len(L)):  
        for j in range(5):  
            if L[i] * j == 20:  
                x = L.pop(0)  
                result.append(x)  
    return result
```

# Linear Search & Binary Search

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```
def linSearch(lst, target):  
    if len(lst) == 0:  
        return False  
    elif lst[0] == target:  
        return True  
    else:  
        return linSearch(lst[1:], target)
```

**$O(n)$**

```
def binSearch(lst, target):  
    if lst == []:  
        return False  
    else:  
        mid = len(lst) // 2  
        if lst[mid] == target:  
            return True  
        elif target < lst[mid]:  
            return binSearch(lst[:mid], target)  
        else: # lst[mid] < target  
            return binSearch(lst[mid+1:], target)
```

**$O(\log n)$  comparisons, what about runtime?**

# Example Problem

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Come up with runtime of each line and provide overall runtime

```
def f(s): #N == len(s)
    count=0 #O()
    for c in 'aeiou': #O()
        if s.find(c)==True: #O()
            count+=1 #O()
    if count>3: #O()
        for i in range(count**2): #O()
            print(i) #O()
    return count #O()
```

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# Example Problem

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Come up with runtime of each line and provide overall runtime

**OVERALL RUNTIME:  $O(N)$**

```
def f(s): #N == len(s)
    count=0 #O(1)
    for c in 'aeiou': #O(1)
        if s.find(c)==True: #O(N)
            count+=1 #O(1)
    if count>3: #O(1)
        for i in range(count**2): #O(1)
            print(i) #O(1)
    return count #O(1)
```

# Tractability





# Is the problem tractable?

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- A problem is tractable if it has a **reasonably efficient runtime**
- "Reasonably efficient" means the runtime can be expressed as a polynomial equation
  - Tractable:  $O(1)$ ,  $O(\log n)$ ,  $O(n)$ ,  $O(n^2)$ ,  $O(n^k)$
  - Intractable:  $O(2^n)$ ,  $O(k^n)$ ,  $O(n!)$

Why does it matter?

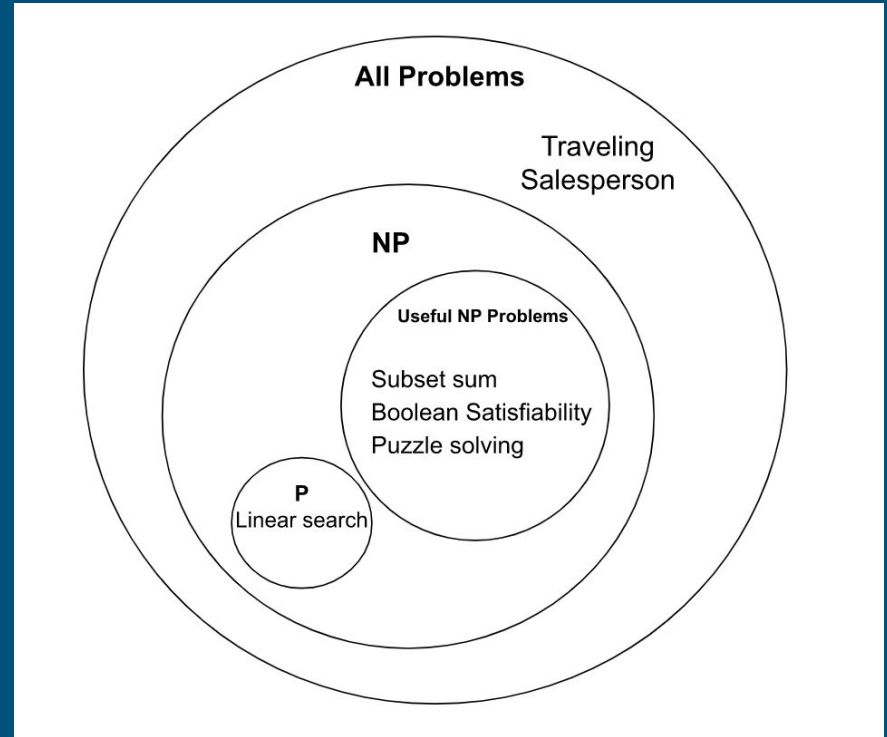
For some problems, we have to use a **brute force approach** (generating every possible solution and checking each of the generated solutions to see if any of them work for the problem's constraints)

If the **size of an input is extremely large**, using an algorithm with a runtime that is not in polynomial time can take far **too long**.

# Complexity Classes

- P is the set of problems that can be
  - Solved in polynomial time (tractable)
  - Checked in polynomial time (tractable)
- NP is the set of problems that can be
  - Checked in polynomial time (tractable)

**Why does it matter?** If  $P = NP$ , we could solve a lot of difficult problems.



# Heuristics

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- A **heuristic** is a technique used to find a solution that is "good enough"
- Typically used for NP problems where finding the solution is intractable
- A heuristic can rank potential next steps to help with each decision

## **Example:**

Consider a weighted graph with nodes consisting of CMU building names and edges having weights representing the distances between the buildings.

**Problem:** Find the best possible path from Gates to Hall of Arts.

**Heuristic:** Always trying to take the shortest path first (edge with the lowest weight)