Numbers in C

Balance Sheet ... so far

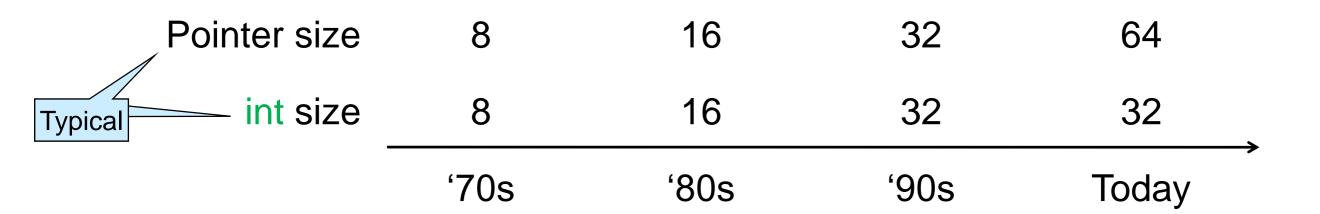
| Lost | Gained |
|--|--|
| Contracts | Preprocessor |
| Safety | Undefined behavior |
| Garbage collection | Explicit memory management |
| Memory initialization | Separate compilation |
| Well-behaved arrays | Pointer arithmetic |
| Fully-defined language | Stack-allocated arrays and structs |
| • Strings | Generalized address-of |

Undefined Behavior

Reading/writing to non-allocated memory Reading uninitialized memory Memory · even if correctly allocated Use after free • Double free Freeing memory not returned by malloc/calloc Writing to read-only memory Numbers **Today**

The type int

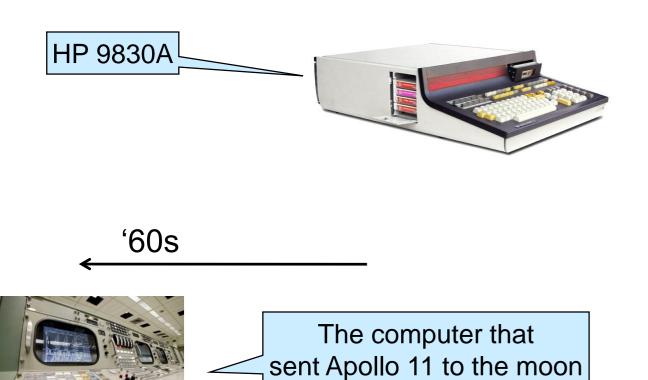
- In C0/C1, the size of values of type int is 32 bits
 and pointers are 64 bits
- In C, the size of an int has evolved over time
 and pointers too



- In C, the size of an int has evolved over time
 and pointers too
 - Pointer size 8 16 32 64

 int size 8 16 32 32

 '70s '80s '90s Today

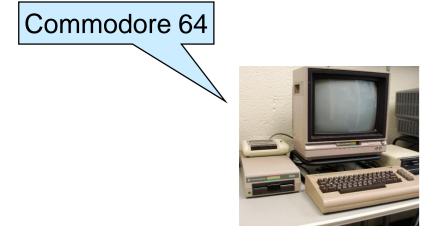


- Early computers had 8-bit addresses
 - 256 *bytes* of memory
 - > RAM was very expensive
- ints ranged from -128 to 127

- In C, the size of an int has evolved over time
 and pointers too
 - Pointer size 8 16 32 64

 int size 8 16 32 32

 '70s '80s '90s Today

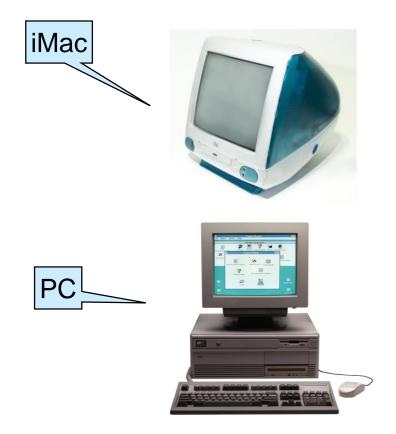




- 16-bit addresses
 - (up to) 64 kilobytes of memory
 - > the Commodore 64
- ints ranged from -32768 to 32767

In C, the size of an int has evolved over time
and pointers too

| | '70s | '80s | '90s | Todav | · |
|--------------|------|------|------|-------|----------|
| int size | 8 | 16 | 32 | 32 | → |
| Pointer size | 8 | 16 | 32 | 64 | |



- 32-bit addresses(up to) 4 gigabytes of memory
- ints ranged in the billions

In C, the size of an int has evolved over time
and pointers too

| | '70s | '80s | '90s | Today |
|--------------|------|------|------|-------|
| int size | 8 | 16 | 32 | 32 |
| Pointer size | 8 | 16 | 32 | 64 |





- 64-bit addresses
 nobody has 2⁶⁴ bytes memory
- billions are still Ok for ints

Implementation-defined Behavior

- The C standard says that it is for the compiler to define the size of an int
 - > with some constraints
- It is implementation-defined
 - The compiler decides, but
 - o it remains fixed
 - o the programmer can find out how big an int is
 - > the file < limits.h > defines the values of INT_MIN and INT_MAX
 - and therefore the size of an int

Undefined behavior ≠ implementation-defined behavior

- undefined behavior does not have to be consistent
- the programmer has no way to find out from inside the program

Implementation-defined Behavior

- Most programmers don't need to know how big an int is
 - just write code normally, possibly using INT_MIN and INT_MAX
 - the compiler will use whatever internal size it has chosen

This is not true of code that uses the bits of an int to encode data: bit patterns (e.g., pixels)

- Same thing for pointers
- Code written in the 1970s still works on today's computers
 - o as long as the code doesn't depend on the size of an int
 - o and the programmer used sizeof inside malloc

int's Undefined Behaviors

Safety violations in C0 are undefined behavior in C

- division/modulus by 0, or INT_MIN divided/mod'ed by -1
- shifting by more than the size of an int

Overflow!

- C programs do not necessarily use two's complement
 - ➤ this makes it essentially impossible to reason about ints in a C program

In 1972, a lot of computers didn't use 2's complement

- > n + n n and n may produce different results
- gcc provides the flag -fwrapv to force the use of two's complement for ints
- And a few more
 - o e.g., left-shifting a negative value

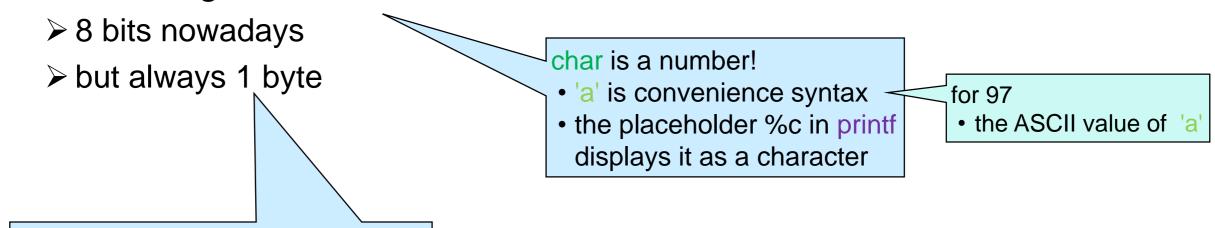
Other Integer Types

Signed Integer Types

- C0 has a single type of integers: int
- C has many more
 - long: integers that are larger than int
 - ➤ 64 bits nowadays
 - short: integers that are smaller than int
 - ➤ 16 bits nowadays

C99 defines a byte as at least 8 bit

char: integers that are smaller than short



o ... and there are more

Unsigned Integer Types

- Lots of code doesn't use negative numbers
- C provides unsigned variants of each integer type
 - > same number of bits but sign bit can be used to represent more numbers
 - □ twice as many numbers

The most significant bit is not special for them

o unsigned long

o unsigned int ______

o unsigned short

- o unsigned char
- Overflow on unsigned numbers is defined to wrap around

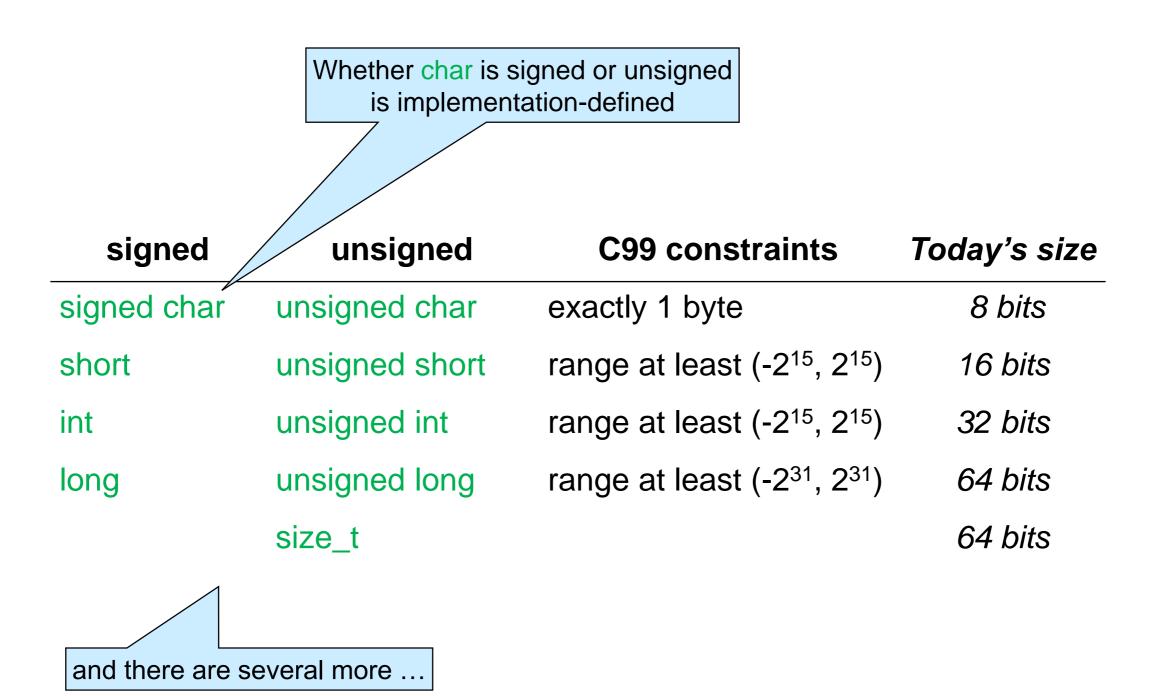
or just unsigned

o unsigned numbers do follow the laws of modular arithmetic

Unsigned Integer Types

- size_t is used to hold pointer and offsets
 - the argument of malloc and calloc
 - array indices
 - return type of sizeof
 - 0 ...
- The size of size_t is the size of a memory address

Implementation-defined Integers



Casting Integers

Integer Casts

 We go back and forth between different number types with casts

int
$$x = 3$$
; $x = 3$; $y = (long)x$;

Literal numbers have always type int

The compiler introduces implicit casts as needed

long
$$x = 3$$
;

> is implicitly turned into

$$long x = (long)3;$$

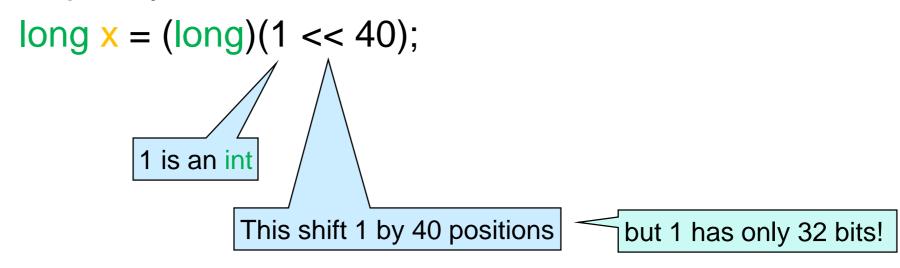
Integer Casts

- Literal numbers have always type int
- The compiler introduces implicit casts as needed
- This can lead to unexpected outcomes

$$long x = 1 << 40;$$

is undefined behavior

This is implicitly turned into



> Fix: long x = ((long)1) << 40;

Casting Rules

If the new type can represent the value, the value is preserved

```
signed char x = 3;  // x = 3 is 3 = 0x03) unsigned char y = (unsigned char)x;  // y = 3 = 0x03)
\circ signed char x = 3;
\circ signed char x = 3;
  unsigned int y = (unsigned int)x;
                                                    // x is (-3) = 0xFD)
// y is (-3) = 0xFFFFFD)
\circ signed char x = -3;
  int y = (int)x;
\circ unsigned char \times = 253;
  unsigned int y = (unsigned int)x;
                                                     // x is -3 (= 0xFFFFFFD)
// y is -3 (= 0xFD)
\circ int x = -3;
  signed char y = (signed char)x;
```

Casting Rules

If the new type *can't* represent the value but is unsigned:

if the new type is smaller or the same,
 the least significant bits are retained

```
o signed char x = -3;  // x is -3 (= 0xFD) unsigned char y = (unsigned char)x; // y is 253 (= 0xFD)
```

• if the new type is bigger, the bits are sign-extended

An unsigned type can't represent

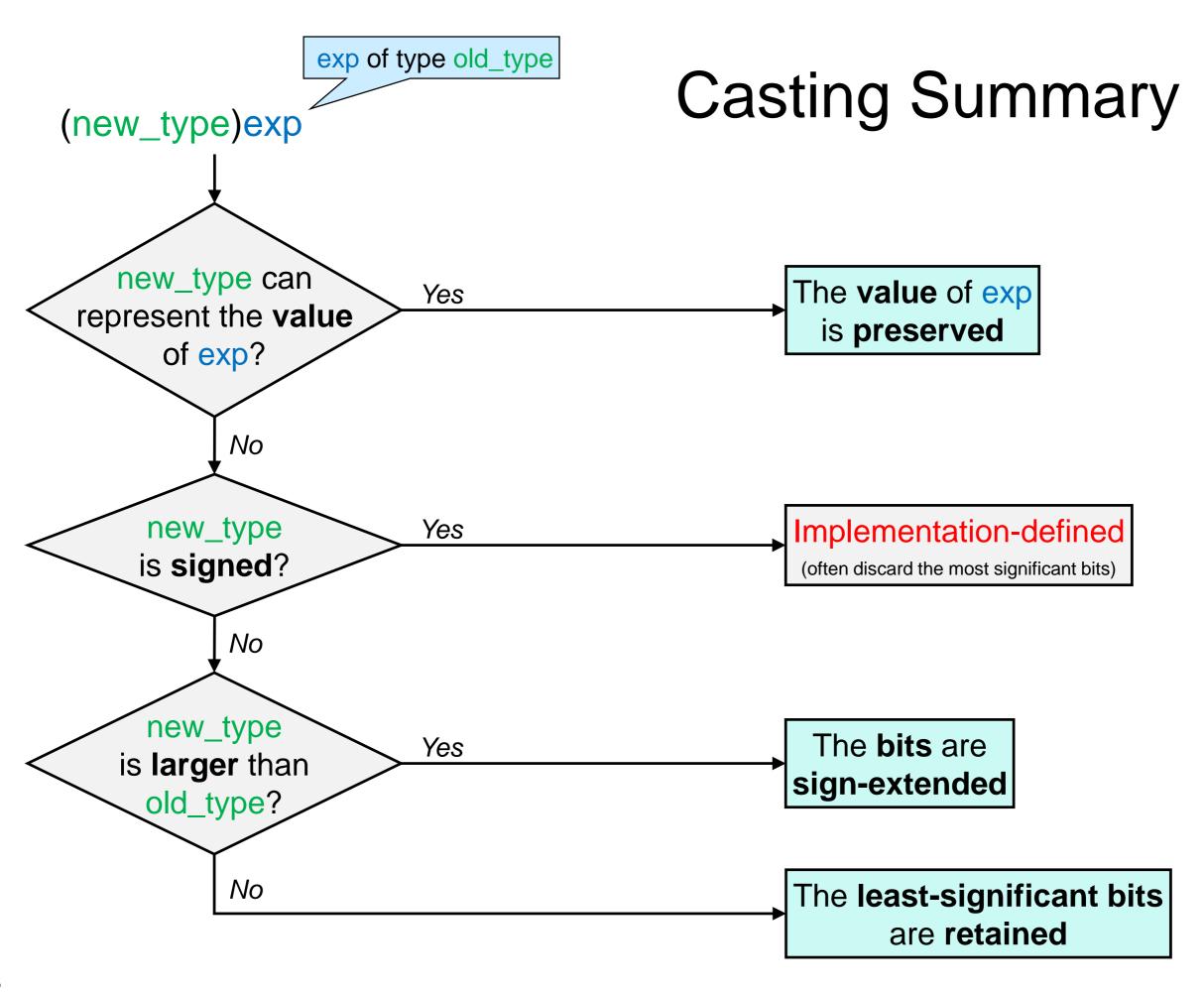
negative numbers

Casting Rules

If the new type *can't represent* the value but is signed, the result is **implementation-defined**

Many compilers discard the most significant bits

```
o int x = -241; // x = -241 // x = -24
```



Fixed-size Numbers

Fixed-size Integers

- For bit patterns, the program needs the number of bits to remain the same as C evolves
- Header file <stdint.h> provides fixed-size integer types
 in signed and unsigned variants

| Fixed-size signed | Today's signed equivalent | Today's unsigned equivalent | Fixed-size unsigned |
|-------------------|---------------------------|-----------------------------|---------------------|
| int8_t | signed char | unsigned char | uint8_t |
| int16_t | short | unsigned short | uint16_t |
| int32_t | int | unsigned int | uint32_t |
| int64_t | long | unsigned long | uint64_t |
| | | | |

That's the number of bits

Floating Point Numbers

The type float represents floating point numbers

```
> nowadays 32 bits

float x = 0.1;

Numbers with a decimal point

float y = 2.0235E-27;

That's 2.0235 * 10^{-27}
```

- float and int use the same number of bits, but float has a much larger range
 - o some numbers with a decimal point are not representable
 - the larger range comes at the cost of precision
 - > operations on floats may cause rounding errors



Operations on floats may cause rounding errors

```
O Example 1

#include <math.h>

#define PI 3.14159265

float x = \sin(PI);

In math, \sin(\pi) is 0 but \sin(PI) is not 0.0

O Example 2

float y = (10E20 / 10E10) * 10E10;

That's (10^{20}/10^{10}) * 10^{10}

Positive sin, cos, log, ...

Any more decimals would be ignored

That's (10^{20}/10^{10}) * 10^{10}

That's (10^{20}/10^{10}) * 10^{10}

Positive sin, cos, log, ...

Any more decimals would be ignored
```

➤ but it isn't always

□ it depends on the compiler



- Operations on floats may cause rounding errors
 - Example 3

```
for (float res = 0.0; res != 5.0; res += 0.1)
printf("res = %f\n", res);
```

- > we expect the loop to terminate after 50 iterations
- > instead it runs for ever
- > That's because 0.1 decimal is a **periodic** number in binary: 0.00011

```
This is how we convert 0.1 to binary

0.1 * 2 = 0.2

0.2 * 2 = 0.4

0.4 * 2 = 0.8

0.8 * 2 = 1.6

0.6 * 2 = 1.2

0.2

At this point, it repeats
```

- Operations on floats may cause rounding errors
- This makes it impossible to reason about programs
 - This is why there are no floats in C0

- Adding more bits does not solve the problem
 - The type double of double-precision floating point numbers has typically 64 bits nowadays
 - > similar issues

Enum and Union Types

Sample Problem

- Print a message based on the season
- How to encode seasons?
 - use strings ...
 - > testing which season we are in is costly
 - use integers
- Drawbacks
 - The encoding is not mnemonic
 - > we will make mistakes
 - A whole int for 4 values seems wasteful

```
// 0 = Winter
// 1 = Spring
// 2 = Summer
// 3 = Fall

int today = 3;
if (today == 0)
  printf("snow!\n");
else if (today == 3)
  printf("leaves!\n");
else
  printf("sun!\n");
```

Enum Types

- The encoding is not mnemonic
- A whole int for 4 values seems wasteful

An enum type lets

- the programmer choose mnemonic values
 - □ no need to remember the encoding just use the names
- the compiler decide how to implement them
 - > what actual type to map them to
 - > what values to use

The compiler maps enum names to some numerical values

the compiler optimizes space usage

```
enum season { WINTER, SPRING, SUMMER, FALL }:

enum season today = FALL:

if (today = WINTER)

printf("snow!\n");

else if (today = FALL)

printf("leaves!\n");

else

printf("sun!\n");
```

By convention, enum

values are written in

all caps

Switch Statements

A switch statement is an alternative to cascaded if-elses

for numerical values

- > including union types
- They make the code more readable
- Each value considered is handled by a case
 - The execution of a case continues till the next break or the end of the switch statement
 - > it exits the switch statement
 - The default case handles any remaining value

```
enum season { WINTER, SPRING, SUMMER, FALL };
enum season today = FALL;
switch (today) {
 case WINTER:
                                a case
  printf("snow!\n");
  break;
 case FALL:
                                another case
  printf("leaves!\n");
  break;
 default:
                                the default case
  printf("sun!\n");
```

Switch Statements



 If a break is missing, the execution continues with the next case

```
This the source of many bugs!
```

```
enum season { WINTER, SPRING, SUMMER, FALL };
enum season today = FALL;
switch (today) {
 case WINTER:
                                a case
  printf("snow!\n");
  break;
 case FALL:
                                another case
  printf("leaves!\n");
  break;
 default:
                                the default case
  printf("sun!\n");
```

Recent versions of gcc issue a warning when this happens

Another Sample Problem

- Define a type for binary trees with int data only in their leaves
 - > and where the empty tree is **not** represented as NULL
 - A leafy tree could be
 an inner node with pointers to two children
 a leaf with int data
 an empty tree

 The empty tree
 An inner node
 A leaf
 - O Then:

```
enum nodekind = { INNER, LEAF, EMPTY };
struct Itree {
    enum nodekind kind;
    int data;
    leafytree *left;
    leafytree *right;
};
typedef struct Itree leafytree;
We now know about
    enum types!
```

Sample Problem

This representation wastes memory

- the compiler will pick a small numerical type for kind
 - ➤ probably a char

```
enum nodekind = { INNER, LEAF, EMPTY };

struct ltree {
   enum nodekind kind;
   int data;
   leafytree *left;
   leafytree *right;
   };

typedef struct ltree leafytree;
```

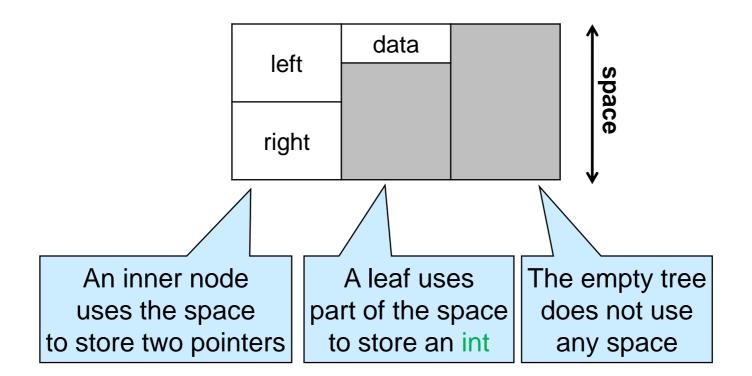
but

- o the remaining 3 fields are never fully utilized for any node type
 - > inner nodes do not make use of the data field
 - ➤ leaves do not use left and right
 - > the empty tree does not need any



Union Types

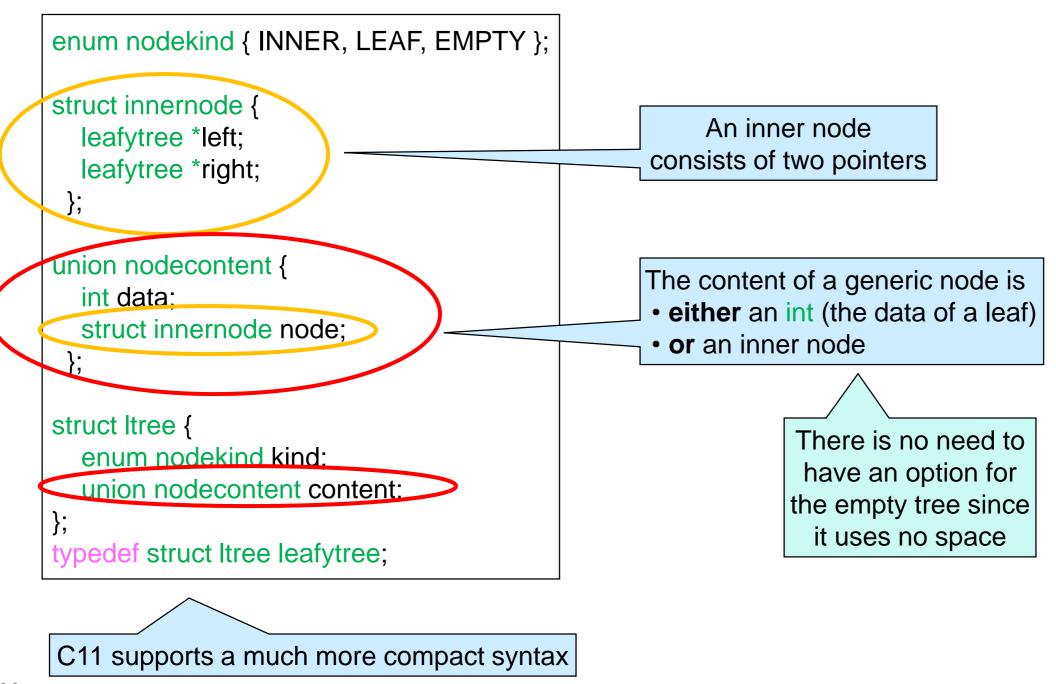
- A union type allows using the same space in different ways
- Consider the space needed for a node, aside from its kind



left data space

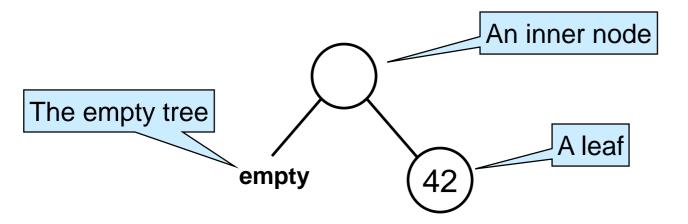
Union Types

A union type allows using the same space in different ways



Building a Tree

Let's write code that creates this tree



```
enum nodekind { INNER, LEAF, EMPTY };

struct innernode {
    leafytree *left;
    leafytree *right;
    };

union nodecontent {
    int data;
    struct innernode node;
    };

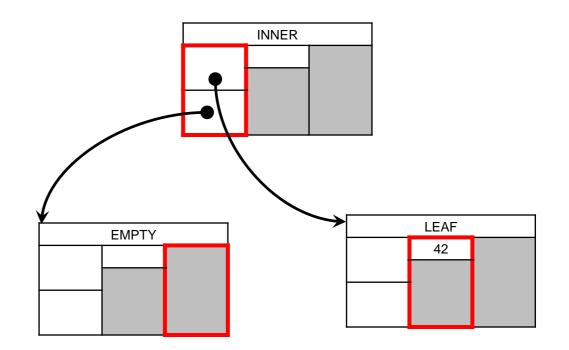
struct ltree {
    enum nodekind kind;
    union nodecontent content;
};

typedef struct ltree leafytree;
```

```
leafytree *T = malloc(sizeof(leafytree));
T->kind = INNER;
T->content.node.left = malloc(sizeof(leafytree));
T->content.node.left->kind = EMPTY;
T->content.node.right = malloc(sizeof(leafytree));
T->content.node.right->kind = LEAF;
T->content.node.right->content.data = 42;

Whenever not following a pointer,
```

we must use the dot notation



Adding up a Leafy Tree

- We use a switch statement to write clear code
 - we discriminate on T->kind
 - it has three possible values
 - ➤ INNER, LEAF and EMPTY

```
int add_tree(leafytree *T) {
 int n = 0;
 switch (T->kind) {
  case INNER:
    n += add_tree(T->content.node.left);
    n += add_tree(T->content.node.right);
    break;
  case LEAF:
    n = T->content.data;
    break;
  default:
    n = 0:
 return n;
```

Summary

Undefined Behavior

Reading/writing to non-allocated memory Reading uninitialized memory Memory even if correctly allocated Use after free Double free Freeing memory not returned by malloc/calloc Writing to read-only memory Division/mod by zero Numbers INT_MIN divided/mod'ed by -1 Shift by more than the number of bits Signed overflow