Numbers in C

Balance Sheet ... so far

Lost	Gained
 Contracts 	 Preprocessor
 Safety 	 Undefined behavior
 Garbage collection 	 Explicit memory management
 Memory initialization 	 Separate compilation
 Well-behaved arrays 	 Pointer arithmetic
 Fully-defined language 	 Stack-allocated arrays and structs
 Strings 	 Generalized address-of

Undefined Behavior

mbers	 Freeing memory not returned by malloc/calloc Writing to read-only memory Today
Memory	 Reading/writing to non-allocated memory Reading uninitialized memory even if correctly allocated Use after free Double free Eracing memory not returned by melloc/collect

The type int

- In C0/C1, the size of values of type int is 32 bits
 o and pointers are 64 bits
- In C, the size of an int has evolved over time
 o and pointers too

	'70s	'80s	'90s	Today	-
Typical int size	8	16	32	32	_
Pointer size	8	16	32	64	

In C, the size of an int has evolved over time
 o and pointers too

	'70s	'80s	'90s	Today	
int size	8	16	32	32	•
Pointer size	8	16	32	64	



The computer that

sent Apollo 11 to the moon

'60s



- Early computers had 8-bit addresses
 - \odot 256 *bytes* of memory
 - RAM was very expensive
- ints ranged from -128 to 127

In C, the size of an int has evolved over time
 o and pointers too

Pointer size	8	16	32	64
int size	8	16	32	32
Commodore 64	'70s	'80s	'90s	Today
		 16-bit add ○ (up to) 64 > the Corr 	dresses 4 kilobytes of nmodore 64	memory
Apple II	4	ints range	ed from -327	768 to 32767

In C, the size of an int has evolved over time
 o and pointers too

Pointer size	8	16	32	64
int size	8	16	32	32
	'70s	'80s	'90s	Today



- 32-bit addresses
 - \odot (up to) 4 gigabytes of memory
- ints ranged in the billions

In C, the size of an int has evolved over time
 o and pointers too

Pointer size	8	16	32	64
int size	8	16	32	32
	'70s	'80s	'90s	Today
<image/>		 64-bit add nobody I billions ar 	dresses has 2 ⁶⁴ bytes re still Ok fo	s memory or ints

Implementation-defined Behavior

- The C standard says that it is for the compiler to define the size of an int
 - with some constraints

It is implementation-defined

- The compiler decides, but
- \odot it remains fixed
- \odot the programmer can find out how big an int is
 - the file the file the values of INT_MIN and INT_MAX
 - $\hfill\square$ and therefore the size of an int

Undefined behavior ≠ implementation-defined behavior

- undefined behavior does not have to be consistent
- \odot the programmer has no way to find out from inside the program

Implementation-defined Behavior

Most programmers don't need to know how big an int is

 just write code normally, possibly using INT_MIN and INT_MAX
 the compiler will use whatever internal size it has chosen

This is not true of code that uses the bits of an int to encode data: bit patterns (e.g., pixels)

- Same thing for pointers
- Code written in the 1970s still works on today's computers

 as long as the code doesn't depend on the size of an int
 and the programmer used sizeof inside malloc

int's Undefined Behaviors

• Safety violations in C0 are undefined behavior in C

 \odot division/modulus by 0, or INT_MIN divided/mod'ed by -1

 \odot shifting by more than the size of an int

• Overflow!

C programs do not necessarily use two's complement

 this makes it essentially impossible to reason about ints in a C program

In 1972, a lot of computers didn't use 2's complement

- > *n* + *n n* and *n* may produce different results
- gcc provides the flag -fwrapv to force the use of two's complement for ints
- And a few more

○ e.g., left-shifting a negative value

Other Integer Types

Signed Integer Types

• C0 has a single type of integers: int

• C has many more

- long: integers that are larger than int
 - ≻ 64 bits nowadays
- o short: integers that are smaller than int
 - ➤ 16 bits nowadays

o char: integers that are smaller than short

- 8 bits nowadays
- but always 1 byte

C99 defines a byte as at least 8 bit

char is a number!

- 'a' is convenience syntax
- the placeholder %c in printf displays it as a character

 $\odot \dots$ and there are more

Unsigned Integer Types

- Lots of code doesn't use negative numbers
- C provides unsigned variants of each integer type
 - > same number of bits but sign bit can be used to represent more numbers
 - twice as many numbers
 - o unsigned long
 - O unsigned int ______ or just unsigned
 - o unsigned short
 - o unsigned char

The most significant bit is not special for them

Overflow on unsigned numbers is defined to wrap around
 o unsigned numbers do follow the laws of modular arithmetic

Unsigned Integer Types

size_t is used to hold pointer and offsets

- the argument of malloc and calloc
- o array indices
- return type of sizeof
- 0...
- The size of size_t is the size of a memory address

Implementation-defined Integers



and there are several more ...

Casting Integers

Integer Casts

We go back and forth between different number types with casts

• Literal numbers have always type int

3 —_____this is an int
 O The compiler introduces implicit casts as needed

long x = 3;

➢ is implicitly turned into

long x = (long)3;

Integer Casts

Literal numbers have always type int
 The compiler introduces implicit costs on r

The compiler introduces implicit casts as needed

• This can lead to unexpected outcomes

long x = 1 << 40;

is undefined behavior

 \odot This is implicitly turned into

$$long x = (long)(1 << 40);$$

$$1 is an int$$
This shift 1 by 40 positions but 1 has only 32 bits!

➢ Fix: long x = ((long)1) << 40;</p>

Casting Rules

If the new type can represent the value, the value is preserved

signed char x = 3; // x is 3 = 0x03) unsigned char y = (unsigned char)x; // y is 3 = 0x03) \circ signed char x = 3; // x is 3 (= 0x03) // y is 3 (= 0x00000003) \circ signed char x = 3; unsigned int y = (unsigned int)x; // x is -3 = 0xFD)
// y is -3 = 0xFFFFFFD) \odot signed char x = -3; int y = (int)x; (= 0xFD) (= 0x000000FD) // x is 253 \circ unsigned char x = 253; unsigned int y = (unsigned int)x;// x is -3 = 0xFFFFFD)
// y is -3 = 0xFD) \circ int x = -3; signed char y = (signed char)x;

Casting Rules

If the new type *can't* represent the value but is unsigned:

if the new type is smaller or the same,
 the least significant bits are retained



Casting Rules

If the new type *can't* represent the value but is signed, the result is **implementation-defined**

Many compilers discard the most significant bits







Fixed-size Numbers

Fixed-size Integers

- For bit patterns, the program needs the number of bits to remain the same as C evolves
- Header file <stdint.h> provides fixed-size integer types
 o in signed and unsigned variants

Fixed-size signed	Today's signed equivalent	Today's unsigned equivalent	Fixed-size unsigned
int8_t	signed char	unsigned char	uint8_t
int16_t	short	unsigned short	uint16_t
int32_t	int	unsigned int	uint32_t
int64_t	long	unsigned long	uint64_t

That's the number of bits

Floating Point Numbers

• The type float represents floating point numbers

> nowadays 32 bits float x = 0.1; float y = 2.0235E-27; That's 2.0235 * 10^{-27}

- float and int use the same number of bits, but float has a much larger range
 - o some numbers with a decimal point are not representable
 - \odot the larger range comes at the cost of $\ensuremath{\textit{precision}}$
 - > operations on floats may cause rounding errors



Operations on floats may cause rounding errors





Operations on floats may cause rounding errors

• Example 3

for (float res = 0.0; res != 5.0; res += 0.1)

printf("res = %f\n", res);

- > we expect the loop to terminate after 50 iterations
- instead it runs for ever
- > That's because 0.1 decimal is a **periodic** number in binary: $0.0\overline{0011}$



- Operations on *floats may cause rounding errors*
- This makes it impossible to reason about programs
 This is why there are no floats in C0

- Adding more bits does not solve the problem
 - The type double of double-precision floating point numbers has typically 64 bits nowadays
 - ➤ similar issues

Union and Enum Types

Sample Problem

- Print a message based on the season
- How to encode seasons?

○ use strings …

testing which season we are in is costly

 \circ use integers

Drawbacks

- The encoding is not mnemonic
 - > we will make mistakes
- A whole int for 4 values seems wasteful

// 0 = Winter // 1 = Spring // 2 = Summer // 3 = Fall int today = 3; if (today == 0) printf("snow!\n"); else if (today == 3) printf("leaves!\n"); else printf("sun!\n");

Enum Types

• The encoding is not mnemonic A whole int for 4 values seems wasteful

• An **enum type** lets

• the programmer choose mnemonic values By convention, enum □ no need to remember the encoding – just use the names values are written in o the compiler decide how to implement them \succ what actual type to map them to what values to use enum season { WINTER, SPRING, SUMMER, FALL } enum season today E FALL The compiler maps enum if (today = WINTER) names to some numerical values printf("snow!\n"); else if (today = FALL printf("leaves!\n"); \succ the compiler optimizes else space usage printf("sun!\n");

all caps

Switch Statements

• A switch statement is an alternative to cascaded if-elses for numerical values

- including union types
- They make the code more readable
- Each value considered is handled by a case
 - The execution of a case continues till the next break or the end of the switch statement
 - \succ it exits the switch statement
 - The default case handles any remaining value



Switch Statements



 If a break is missing, the execution continues with the next case





Recent versions of gcc issue a warning when this happens

Another Sample Problem

- Define a type for binary trees with int data only in their leaves
 - > and where the empty tree is **not** represented as NULL



Sample Problem



but

• the remaining 3 fields are never fully utilized for any node type

- > inner nodes do not make use of the data field
- leaves do not use left and right
- the empty tree does not need any



Union Types

- A union type allows using the same space in different ways
- Consider the space needed for a node, aside from its kind



Union Types



• A union type allows using the same space in different ways



enum nodekind { INNER, LEAF, EMPTY };

Building a Tree

• Let's write code that creates this tree



struct innernode {
 leafytree *left;
 leafytree *right;
 };
union nodecontent {
 int data;
 struct innernode node;
 };
struct ltree {
 enum nodekind kind;
 union nodecontent content;
 };
typedef struct ltree leafytree;

leafytree *T = malloc(sizeof(leafytree)); T->kind = INNER; T->content.node.left = malloc(sizeof(leafytree)); T->content.node.left->kind = EMPTY; T->content.node.right = malloc(sizeof(leafytree)); T->content.node.right->kind = LEAF; T->content.node.right->content.data = 42;





Adding up a Leafy Tree

• We use a switch statement to write clear code

- we discriminate on T->kind
- o it has three possible values
 - ➤ INNER, LEAF and EMPTY

```
int add_tree(leafytree *T) {
 int n = 0;
 switch (T->kind) {
  case INNER:
    n += add_tree(T->content.node.left);
    n += add_tree(T->content.node.right);
    break;
  case LEAF:
    n = T->content.data;
    break;
  default:
    n = 0:
 }
 return n;
```

Summary

Undefined Behavior

Memory	 Reading/writing to non-allocated memory Reading uninitialized memory even if correctly allocated Use after free Double free Freeing memory not returned by malloc/calloc Writing to read-only memory
Numbers	 Division/mod by zero INT_MIN divided/mod'ed by -1 Shift by more than the number of bits Signed overflow