

15-150

Fall 2024

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LECTURE 1

Introduction, Philosophy, Some Basics

About 15-150

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19 TAs

<http://www.cs.cmu.edu/~15150/>

We are on Canvas!

Today

- Organization of the course
- Philosophy of the course
- Basics of types, values, expressions in SML

Course tasks

- **Assignments** 40%
- **Labs** 10%
- **Midterm 1** 15% (Sep 26)
- **Midterm 2** 15% (Nov 7)
- **Final** 20%

Collaboration policy

- Make sure to read and understand the policy for this semester

Extra help

- Office Hours by TAs
- Instructors available by appointment
- Student Academic Success Center
 - Drop-in Tutoring
 - Wednesdays POS 280
 - 1-on-1 tutoring by appointment

Course philosophy

- **Computation** is functional.
- **Programming** is an explanatory linguistic process.

Functional programming

LISP • APL • FP • Scheme • KRC • Hope
Miranda™ • Erlang • Curry • Gofer • Mercury
Charity • Cayenne • Mondrian • Epigram
SML • Clean • Caml • Haskell



Everything else is just
*dys*functional
programming!

Computation is functional

- **values** classified with respect to **types**
- **expressions**
- **functions** map values to values

Imperative vs. Functional

command



executed

has an effect

$x := 5$

(new state)

expression




evaluated

no effect

$3 + 5$

(new value)

Programming as explanation

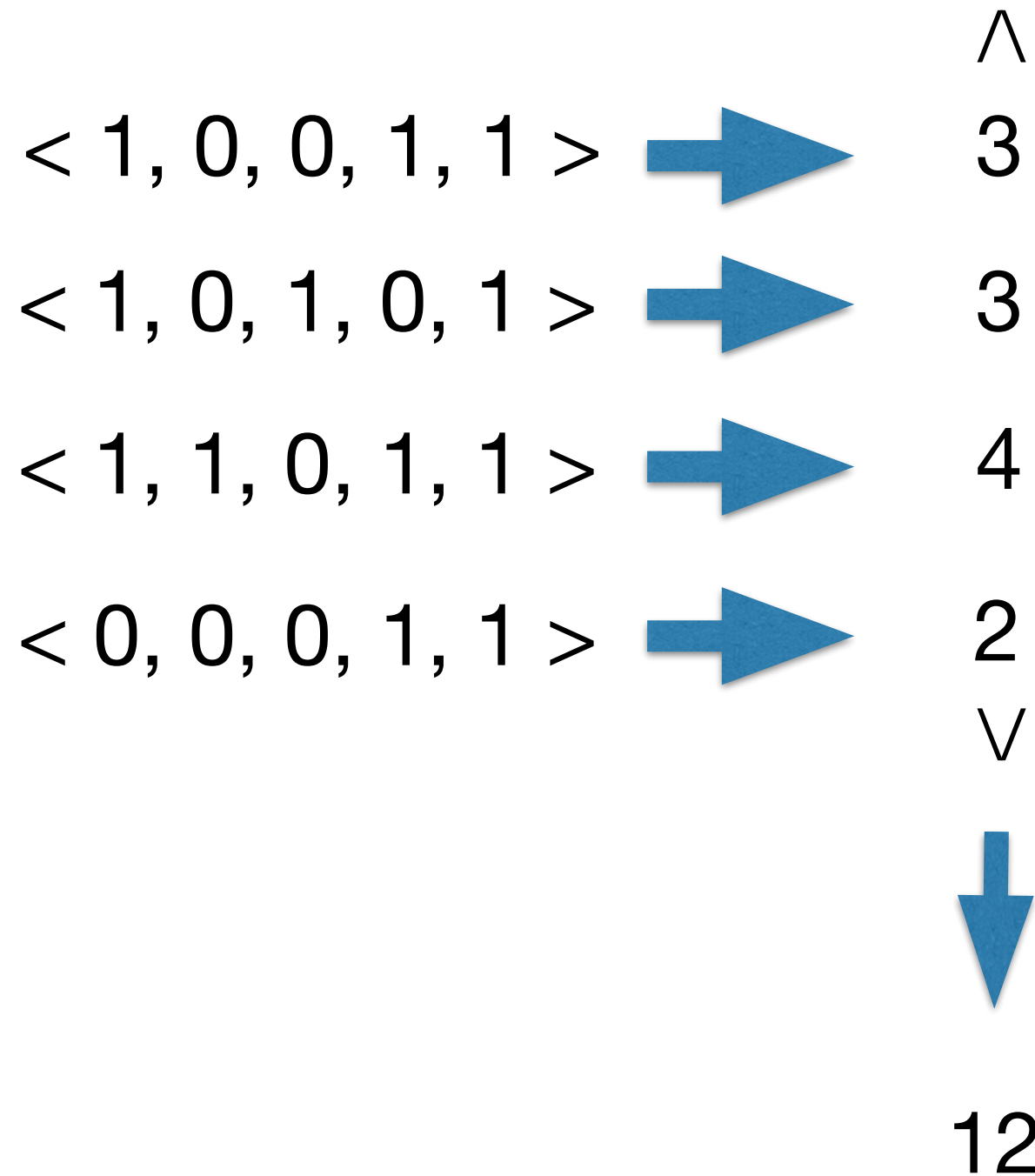
- Problem statement
 - Invariants
 - Specifications
 - Proofs of correctness
- 
- High expectation to explain precisely and concisely
- Analyze, decompose and fit, prove

Parallelism

How many people have taken 15-122?

Let's count it using parallelism.

Parallelism



```
sum: int sequence → int
```

```
type row = int sequence
```

```
type room = row sequence
```

```
fun count (class: room): int = sum (map sum class)
```

Analysis

- How could you improve the running time of `count`?

Divide and conquer

Parallelism

- Expression evaluation has ***no side-effects***
 - can evaluate *independent* code *in parallel*
 - evaluation order has *no effect* on *value*
- Parallel evaluation may be *faster* than sequential

Learn to *exploit* parallelism!

Cost Analysis

Work

- Sequential computation
- Total sequential time; number of operations

Span

- Parallel computation
- How long would it take if one could have as many processors as one wants; length of longest critical path

Introducing ML

- Types t
- Expressions e
- Values v (subset of expressions)

Examples

$$(3 + 4) * 2$$

$$\stackrel{1}{\Rightarrow} 7 * 2$$

$$\stackrel{1}{\Rightarrow} 14$$

$$(3 + 4) * (2 + 1)$$

$$\stackrel{3}{\Rightarrow} 21$$

How many steps would the second take if we used parallelism?

"the " + "walrus"
==> "the walrus"

"the walrus" + 1 ill-typed

SML never evaluates an ill-typed expression!

Types, Expressions, Values

- A type is a “prediction” about the kind of value that an expression will have if it winds up having a value
- An expression is **well-typed** if it has at least one type, and **ill-typed** otherwise.
- A well-typed expression has a type, may have a value, and may have an effect (not for our effect-free fragment)

Every well-formed ML expression e

- has type t , written as $e : t$
- may have a value, written as $e \hookrightarrow v$
(or $e \implies v$)
- may have an effect (not our effect-free fragment)

Example:

$(3 + 4) * 2 : \text{int}$

$(3 + 4) * 2 \hookrightarrow 14$

Types in ML

- Basic types
 - `int`, `real`, `bool`, `char`, `string`
- Constructed types
 - Product types
 - Function types
 - User-defined types

Integers, Expressions

- Type `int`
- Values `...`, `~1`, `0`, `1`, `...`
- Expressions `e1 + e2`, `e1 - e2`, `e1 * e2`,
`e1 div e2`, `e1 mod e2`, `...`
- Example `~4 * 3`

Integers, Typing

- Typing rules
 - $n : \text{int}$
 - $e_1 + e_2 : \text{int}$ if $e_1 : \text{int}$ and $e_2 : \text{int}$
 - similar for other operations

$(3 + 4) * 2 : \text{int}$ because

$(3 + 4) : \text{int}$ $2 : \text{int}$

$(3 + 4) : \text{int}$ because $3 : \text{int}$ and $4 : \text{int}$

Integers, Evaluation

- $e_1 + e_2 \xRightarrow{1} e_1' + e_2$ if $e_1 \xRightarrow{1} e_1'$
- $n_1 + e_2 \xRightarrow{1} n_1 + e_2'$ if $e_2 \xRightarrow{1} e_2'$
- $n_1 + n_2 \xRightarrow{1} n$

where n is the sum of n_1 and n_2

Example

Well-typed expression with no value

`5 div 0 : int`

Notation Recap

$e: t$

e has type t

$e \implies e'$

e reduces to e'

$e \hookrightarrow v$

e evaluates to v

Extensional equivalence

\approx

An equivalence relation on expressions of the same type

Extensional Equivalence

- Expressions of type **int** are *extensionally equivalent* whenever one of the following is true
 - if they **evaluate to the same integer**
 - if they **both loop forever**
 - if they **both raise the same exception**

Equivalence is a form of semantic equality

Equivalence

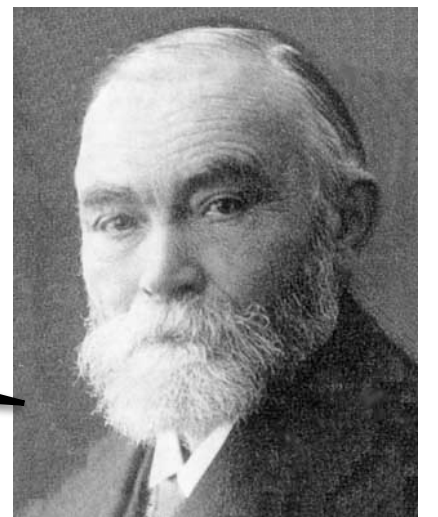
- Functions of type **int -> int** are *extensionally equivalent* if they map *extensionally equivalent arguments* to *extensionally equivalent results*

Referential transparency

for types and values

- The *type* of an expression depends only on the *types* of its sub-expressions
- The *value* of an expression depends only on the *values* of its sub-expressions

safe substitution,
compositional reasoning



Extensional Equivalence

- Expressions of type **int** are *extensionally equivalent* whenever one of the following is true
 - if they **evaluate to the same integer**
 - if they both loop forever
 - if they both raise the same exception

For now, we will mostly focus on the first condition by making appropriate assumptions.

Equivalence

$$21 + 21 \cong 42 \cong 7 * 6$$

$$[2, 4, 6] \cong [1+1, 2+2, 3+3]$$

$$(\mathbf{fn} \ x \Rightarrow x + x) \cong (\mathbf{fn} \ x \Rightarrow 2 * x)$$

Types in ML

- Basic types
 - `int`, `real`, `bool`, `char`, `string`
- Constructed types
 - Product types
 - Function types
 - User-defined types

Products, Expressions

- Types $t_1 * t_2$ for any type t_1 and t_2
- Values (v_1, v_2) for values v_1 and v_2
- Expressions (e_1, e_2) , $\# e_1, \# e_2$
- Example $(\sim 4 * 3, \text{true})$



usually bad
style

$(3, 5, \text{"another example"})$

Products, Typing

- $(e_1, e_2) : t_1 * t_2$ if $e_1 : t_1$ and $e_2 : t_2$
- Example
 $(\sim 4 * 3, \text{true}) : \text{int} * \text{bool}$
 $(3, 5, \text{"another example"}) :$
 $\text{int} * \text{int} * \text{string}$

Products, Evaluation

- $(e_1, e_2) \xRightarrow{1} (e_1', e_2)$ if $e_1 \xRightarrow{1} e_1'$
- $(v_1, e_2) \xRightarrow{1} (v_1, e_2')$ if $e_2 \xRightarrow{1} e_2'$
- $(v_1, v_2) \xRightarrow{1} (v_1, v_2)$

Evaluation:

$(3*4, 1.1+7.2, \text{true})$

$\implies (12, 1.1+7.2, \text{true})$

$\implies (12, 8.3, \text{true})$

We could also write:

$(3*4, 1.1+7.2, \text{true}) \hookrightarrow (12, 8.3, \text{true})$

Exercises

What are the type and values of the following expressions?

	Type	Value
<code>(3*4, 1.1+7.2, true)</code>	<code>int * real * bool</code>	<code>(12, 8.3, true)</code>
<code>(5 div 0, 2+1)</code>	<code>int * int</code>	<i>No value</i>
<code>(5 + "8 miles", false)</code>	<code>ill-typed</code>	<i>No value</i>
<code>(2, (true, "a"), 3.1)</code>	<code>int * (bool * string) * real</code>	<code>(2, (true, "a"), 3.1)</code>

Functions

In math, one talks about a function f being a mapping between spaces X and Y .

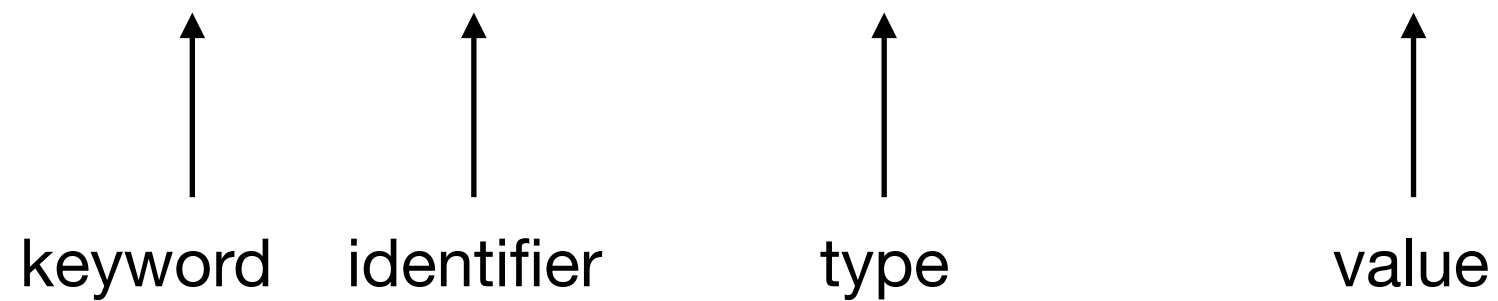
$$f : X \rightarrow Y$$

In SML, we do the same with X and Y being types.

Declarations, Environments, Scope

Declaration

`val pi : real = 3.14`



Introduces binding of `3.14` to `pi`, sometimes written as `[3.14/x]`

Lexically statically scoped

Environment

```
val x : int = 8 - 5      [3/x]  
val y : int = x + 1     [4/y]
```

Environment

```
val x : int = 8 - 5      [3/x]  
val y : int = x + 1     [4/y]  
val x : int = 10        [10/x]  
val z : int = x + 1     [11/z]
```

Second binding of x **shadows** first binding. First binding has been *shadowed*.

Local declarations

```
let
  val m : int = 3
  val n : int = m * m
in
  m + n
end
```

This is an expression with type `int` and value 12.

Local declarations

```
val k : int = 4
```

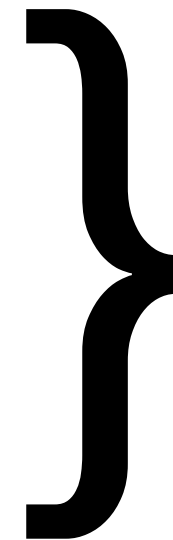
```
let
```

```
    val k : real = 3.0
```

```
in
```

```
    k * k
```

```
end
```



Type?
Value?

Local declarations

```
val k : int = 4
```

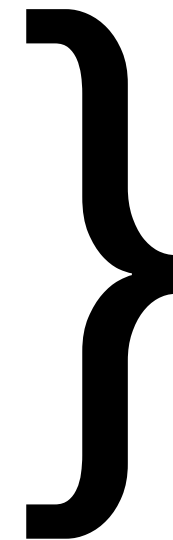
```
let
```

```
    val k : real = 3.0
```

```
in
```

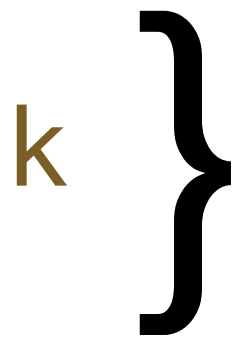
```
    k * k
```

```
end
```



Type?
Value?

9.0 : real



Type?
Value?

4 : int

Concrete Type Definitions

```
type float = real  
type point = float * float  
val p : point = (1.0, 2.6)
```

Functions

Function declaration

```
(* square : int -> int
   REQUIRES: true
   ENSURES: square(x) evaluates to x * x
*)
```

```
fun square (x : int) : int = x * x
```

function name



function body



Closures

Function declarations also create bindings:

```
fun square (x : int) : int = x * x
```

binds the identifier square to a closure:

[ / square]



Lambda expression `fn x:int => x * x`

Environment (all prior bindings when square was declared)

5-step methodology

- Function name and type
- REQUIRES,
- ENSURES
- Function body
- Tests

Step 6: Proof

How does ML evaluate a function application e_2

- Evaluate e_2 to a function value f
- Reduce e_1 to a value v
- Locally extend the environment that existed at the time of the definition of f with a binding of value v to the variable x
- Evaluate the body in the resulting environment

To Do Tonight

- Canvas
 - Assignments
 - Set up lab