

# Utility theory

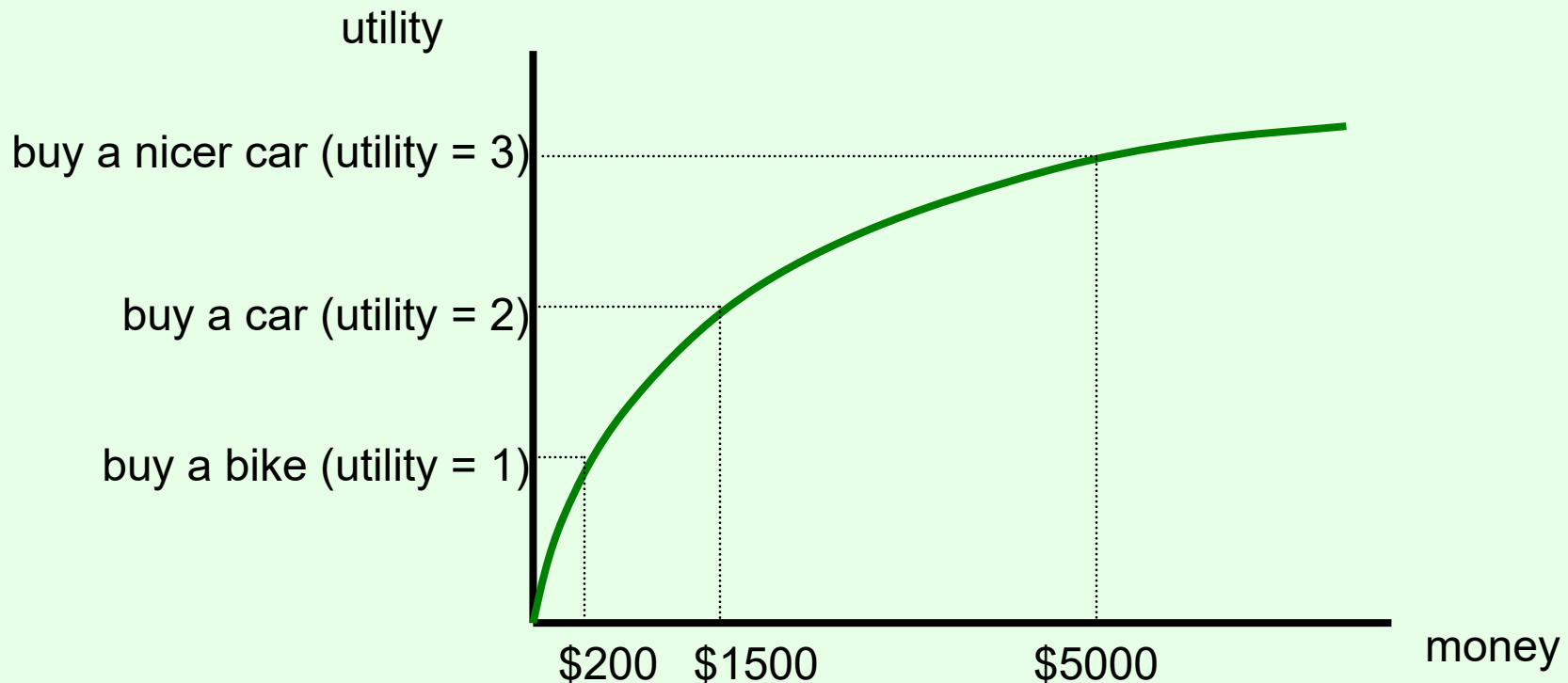
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# Risk attitudes

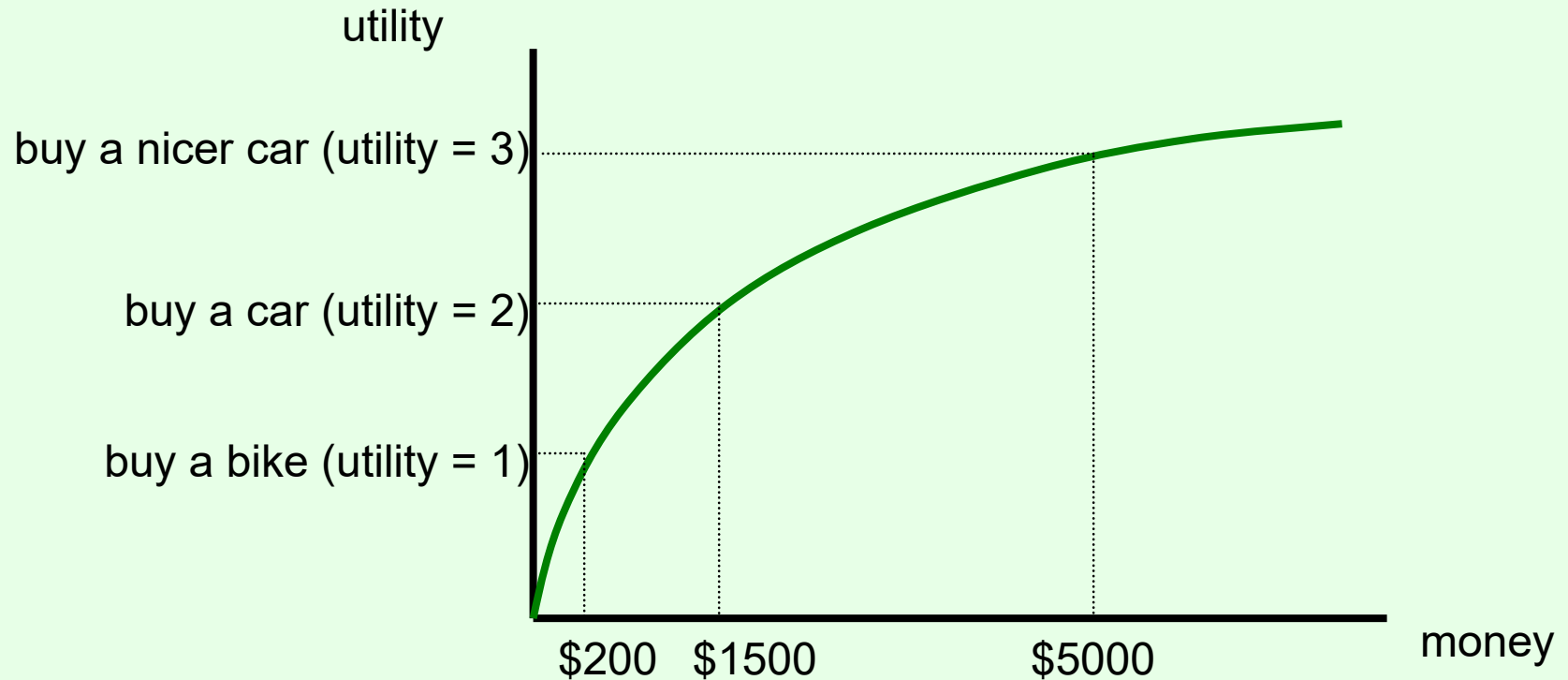
- Which would you prefer?
  - A lottery ticket that pays out \$10 with probability .5 and \$0 otherwise, or
  - A lottery ticket that pays out \$3 with probability 1
- How about:
  - A lottery ticket that pays out \$100,000,000 with probability .5 and \$0 otherwise, or
  - A lottery ticket that pays out \$30,000,000 with probability 1
- Usually, people do not simply go by expected value
- An agent is **risk-neutral** if she only cares about the expected value of the lottery ticket
- An agent is **risk-averse** if she always prefers the expected value of the lottery ticket to the lottery ticket
  - Most people are like this
- An agent is **risk-seeking** if she always prefers the lottery ticket to the expected value of the lottery ticket

# Decreasing marginal utility

- Typically, at some point, having an extra dollar does not make people much happier (**decreasing marginal utility**)

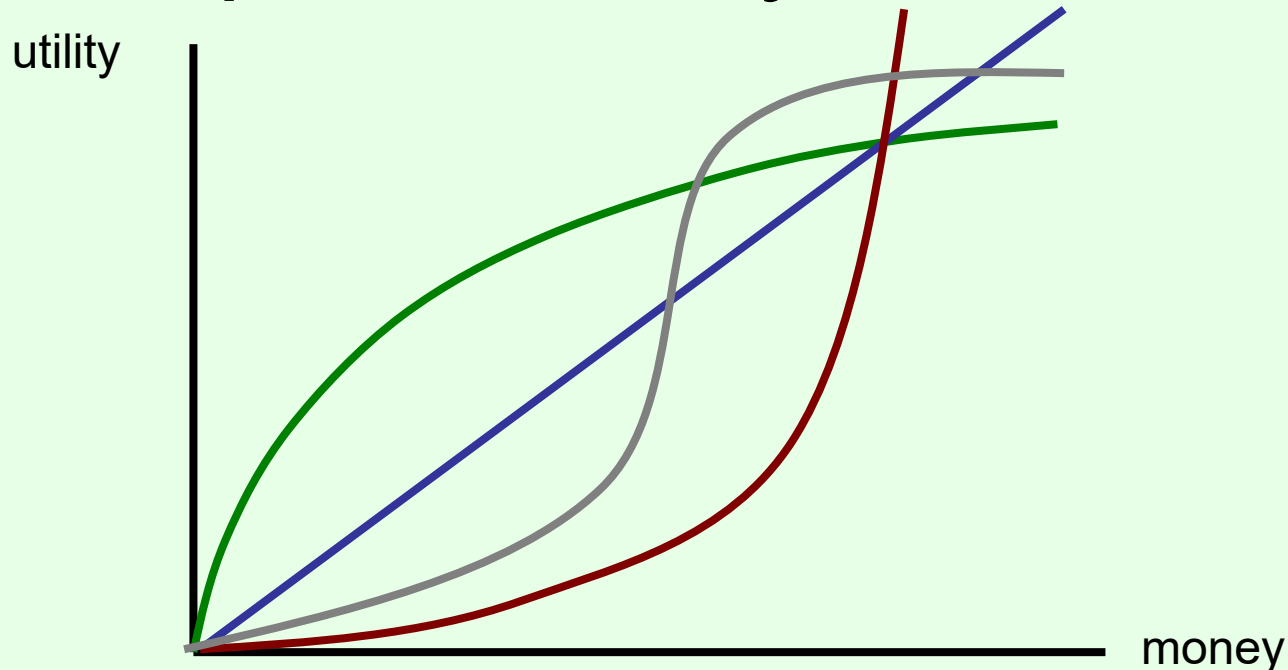


# Maximizing expected utility



- Lottery 1: get \$1500 with probability 1
  - gives expected utility 2
- Lottery 2: get \$5000 with probability .4, \$200 otherwise
  - gives expected utility  $.4*3 + .6*1 = 1.8$
  - (expected amount of money =  $.4*\$5000 + .6*\$200 = \$2120 > \$1500$ )
- So: maximizing expected utility is consistent with risk aversion

# Different possible risk attitudes under expected utility maximization



- **Green** has decreasing marginal utility → risk-averse
- **Blue** has constant marginal utility → risk-neutral
- **Red** has increasing marginal utility → risk-seeking
- **Grey**'s marginal utility is sometimes increasing, sometimes decreasing → neither risk-averse (everywhere) nor risk-seeking (everywhere)

# What is utility, anyway?

- Function  $u: O \rightarrow \mathfrak{R}$  ( $O$  is the set of “outcomes” that lotteries randomize over)
- What are its units?
  - It doesn’t really matter
  - If you replace your utility function by  $u'(o) = a + bu(o)$ , your behavior will be unchanged
- Why would you want to maximize expected utility?
  - This is a question about **preferences over lotteries**