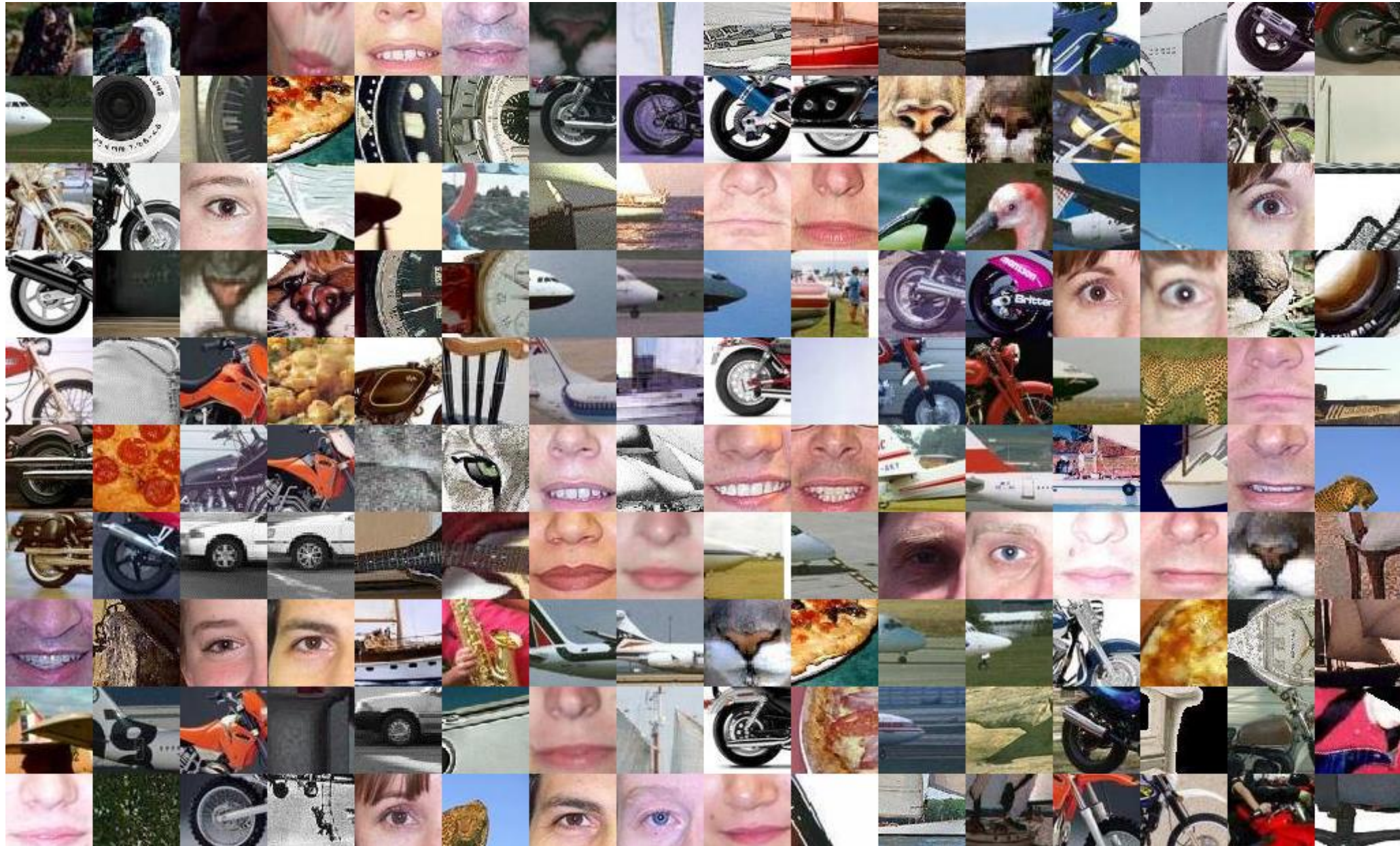


# Feature detectors and descriptors



# Course announcements

- Homework 1 is due tonight at 23:59!
- Homework 2 will be posted tonight and will be due on Monday, February 25<sup>th</sup>.
- There are additional office hours today: 3-5pm, covered by **Abhay**, at the graphics lounge in Smith Hall.

# Overview of today's lecture

Leftover from lecture 5:

- Finish Harris corner detector.
- Multi-scale detection.

New in lecture 6:

- Why do we need feature descriptors?
- Designing feature descriptors.
- MOPS descriptor.
- GIST descriptor.
- Histogram of Textons descriptor.
- HOG descriptor.
- SIFT.

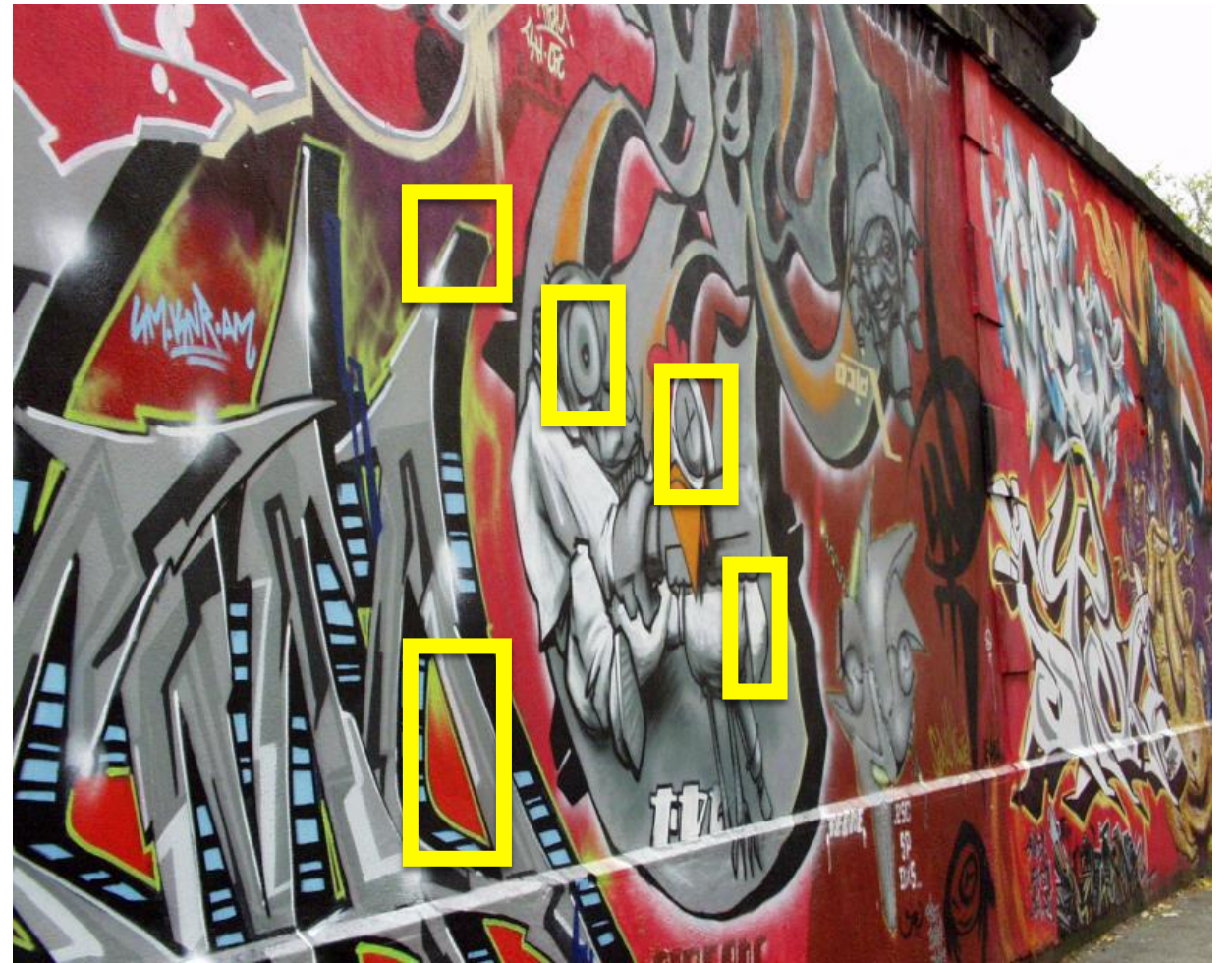
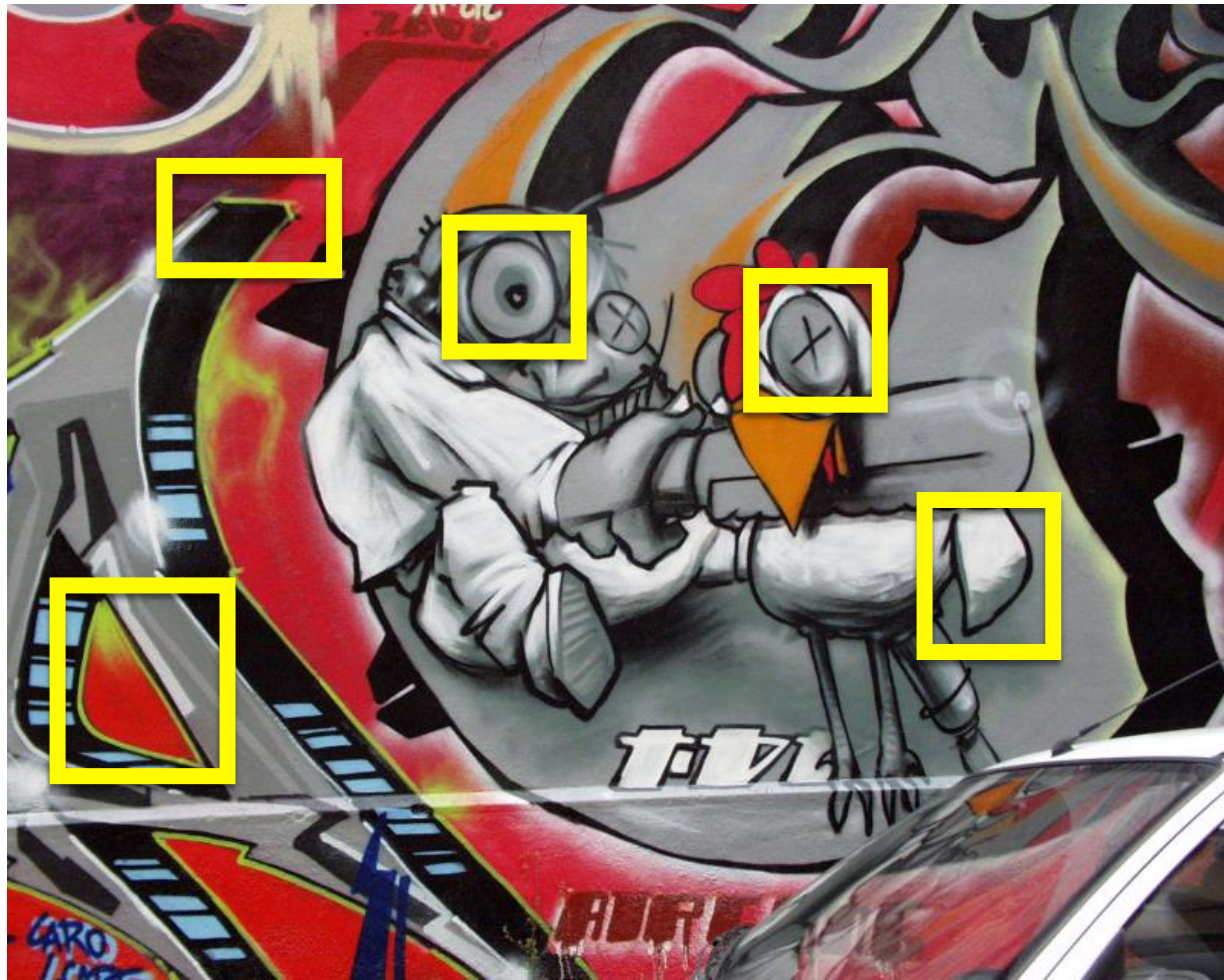
# Slide credits

Most of these slides were adapted from:

- Kris Kitani (16-385, Spring 2017).

Why do we need feature  
descriptors?





*If we know where the good features are,  
how do we match them?*



# Object instance recognition



Schmid and Mohr 1997



Sivic and Zisserman, 2003



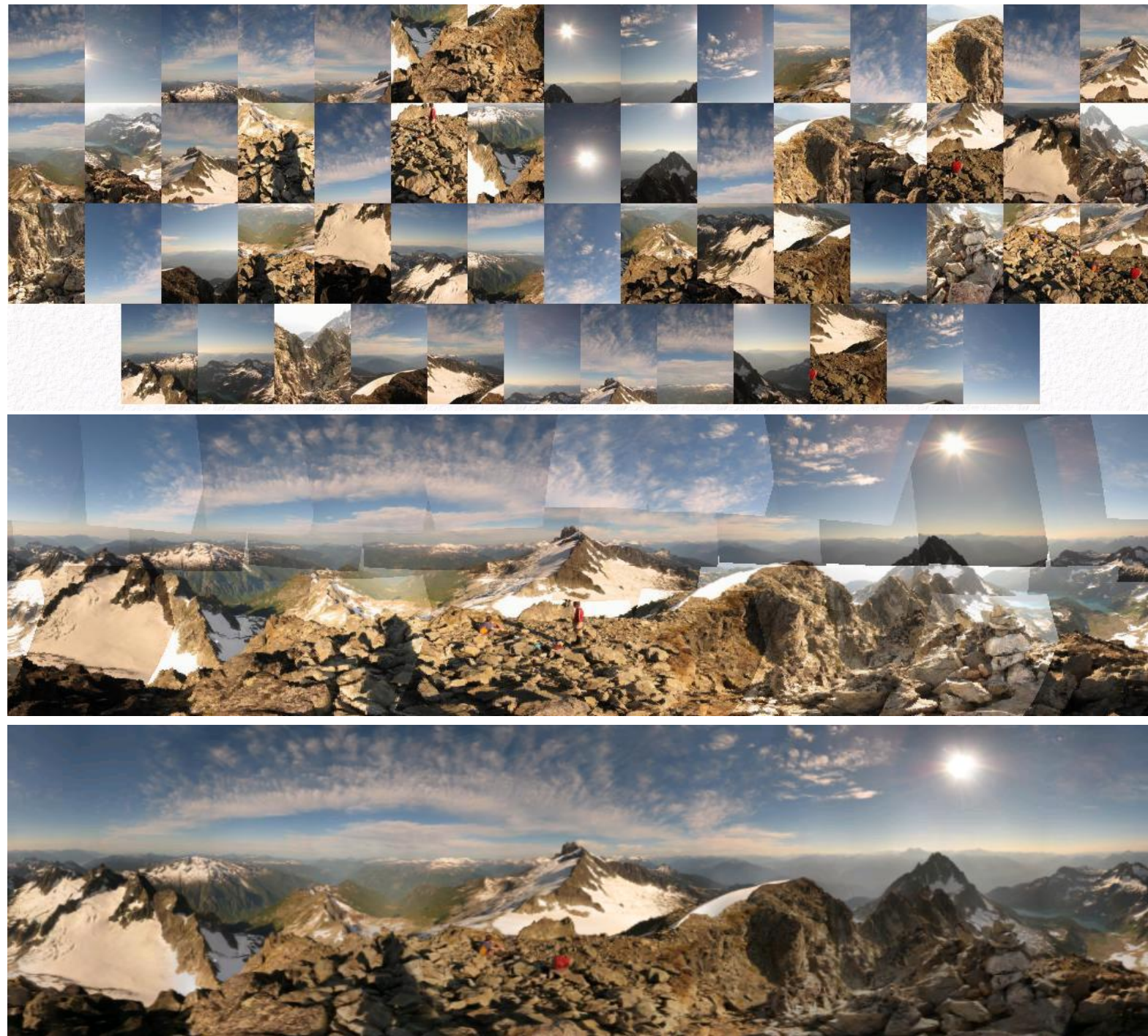
Rothganger et al. 2003



Lowe 2002



# Image mosaicing







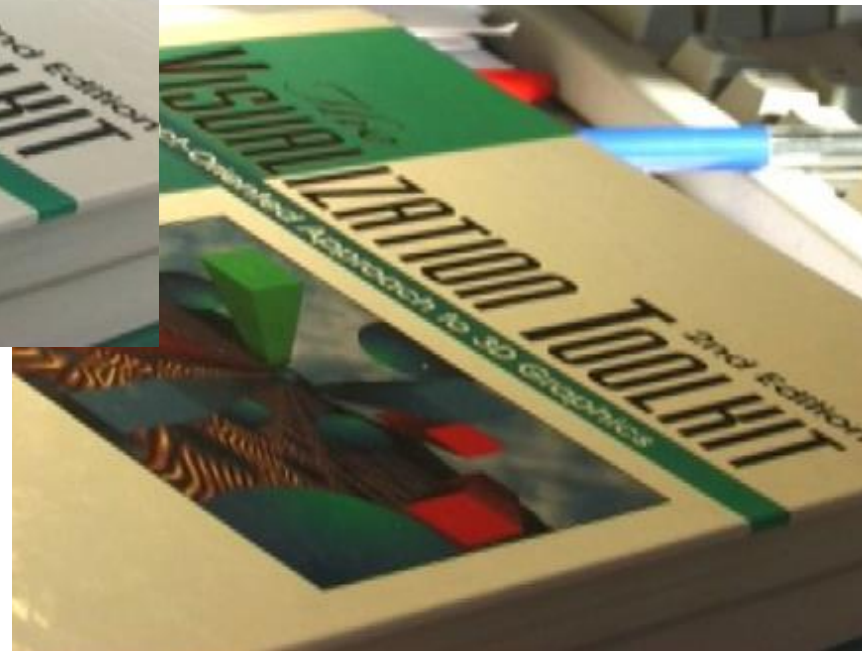
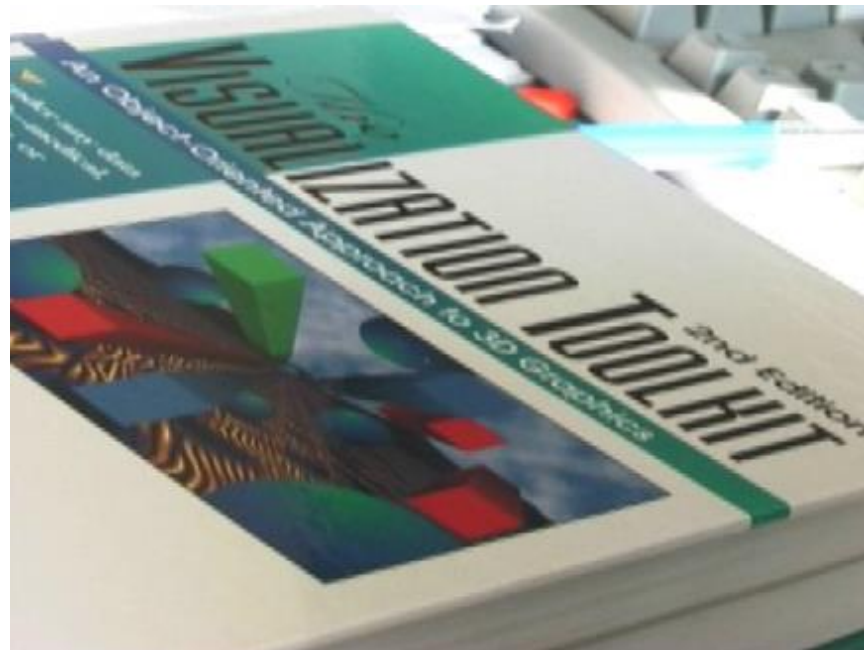
# How do we describe an image patch?

Patches with similar content should have similar descriptors.

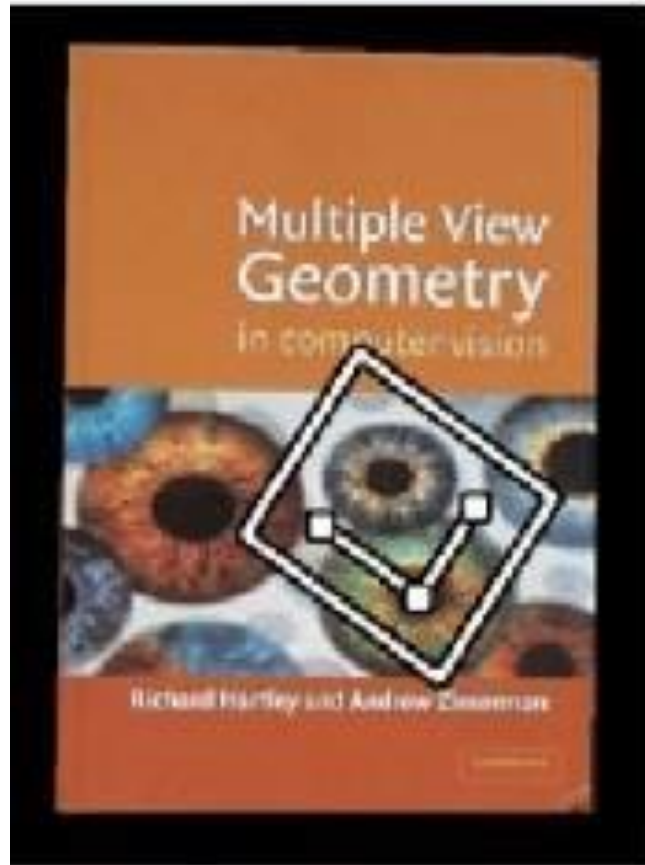
# Designing feature descriptors



# Photometric transformations



# Geometric transformations

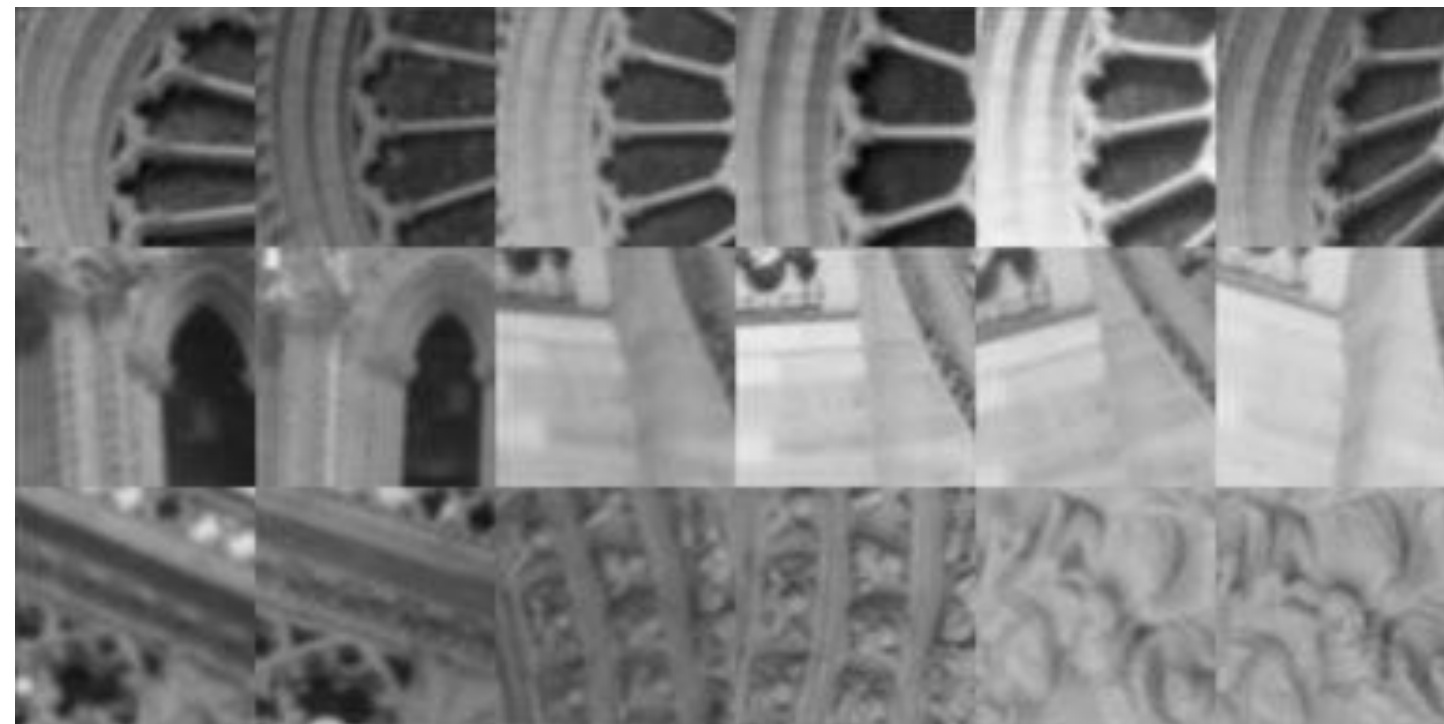


objects will appear at different scales,  
translation and rotation





*What is the best descriptor for an image feature?*



# Image patch

Just use the pixel values of the patch



Perfectly fine if geometry and appearance is unchanged  
(a.k.a. template matching)



# Tiny Images



Just down-sample it!  
Simple, fast, robust to small affine transforms.





# Image patch

Just use the pixel values of the patch



Perfectly fine if geometry and appearance is unchanged  
(a.k.a. template matching)

*What are the problems?*

# Image patch

Just use the pixel values of the patch



Perfectly fine if geometry and appearance is unchanged  
(a.k.a. template matching)

*What are the problems?*

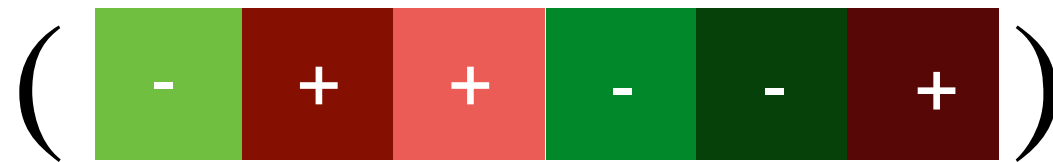
*How can you be less sensitive to absolute intensity values?*



# Image gradients

Use pixel differences

1	2	3
4	5	6
7	8	9



vector of x derivatives

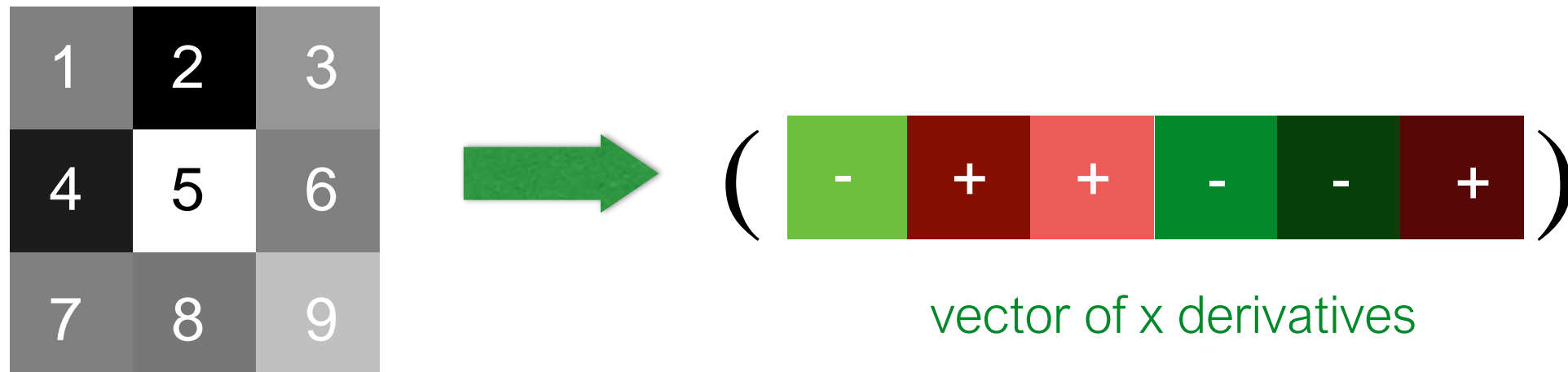
'binary descriptor'

Feature is invariant to absolute intensity values

*What are the problems?*

# Image gradients

Use pixel differences



Feature is invariant to absolute intensity values

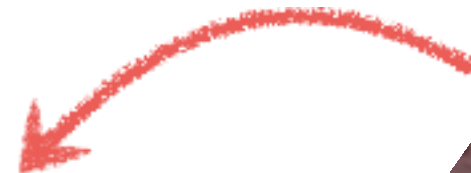
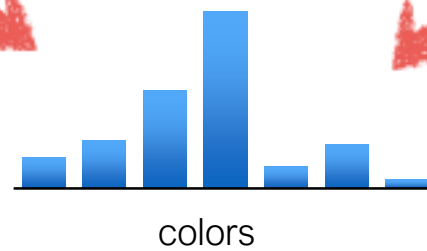
*What are the problems?*

*How can you be less sensitive to deformations?*



# Color histogram

Count the colors in the image using a histogram

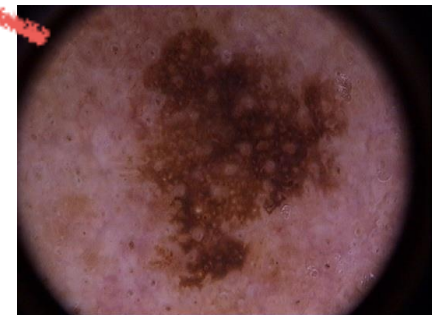
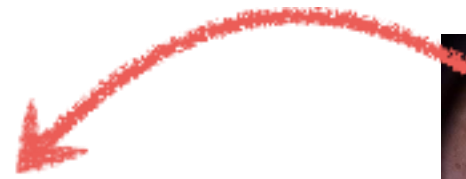
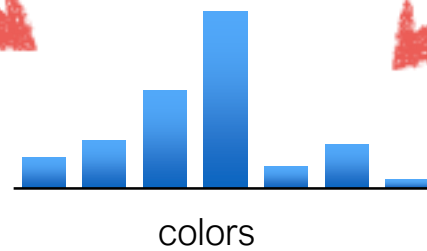


Invariant to changes in scale and rotation

*What are the problems?*

# Color histogram

Count the colors in the image using a histogram

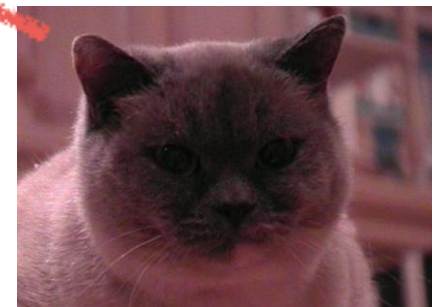
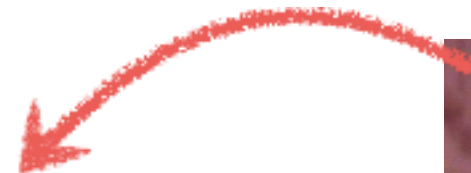
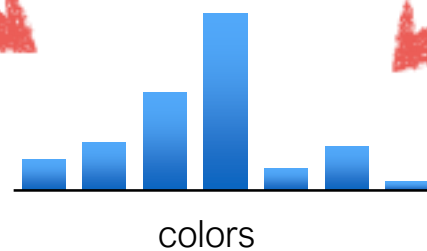
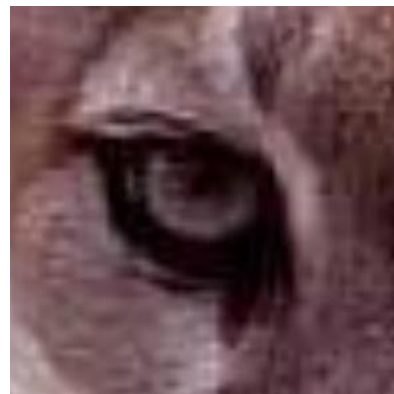


Invariant to changes in scale and rotation

*What are the problems?*

# Color histogram

Count the colors in the image using a histogram



Invariant to changes in scale and rotation

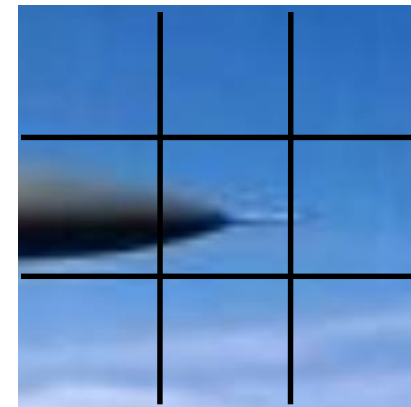
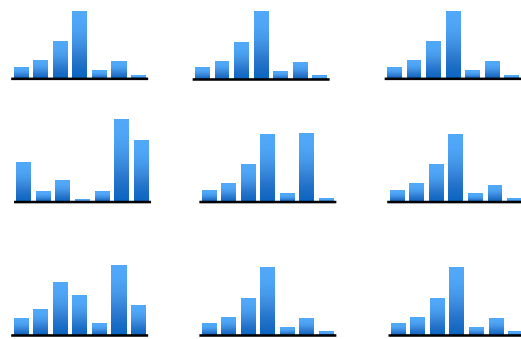
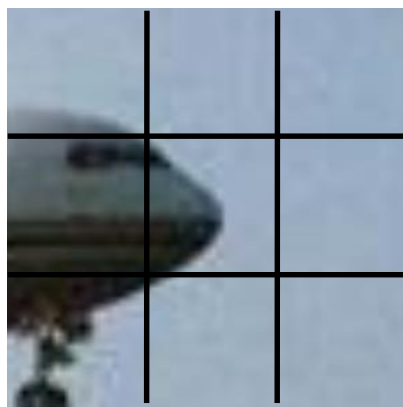
*What are the problems?*

*How can you be more sensitive to spatial layout?*



# Spatial histograms

Compute histograms over spatial 'cells'

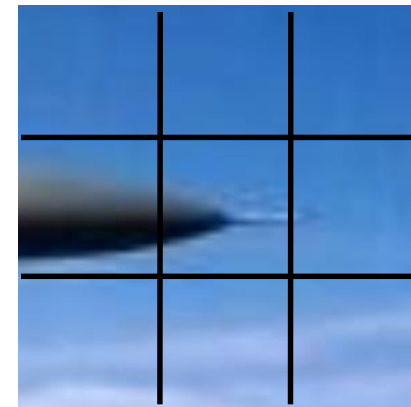
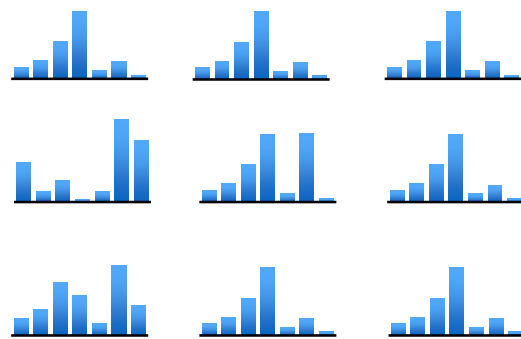
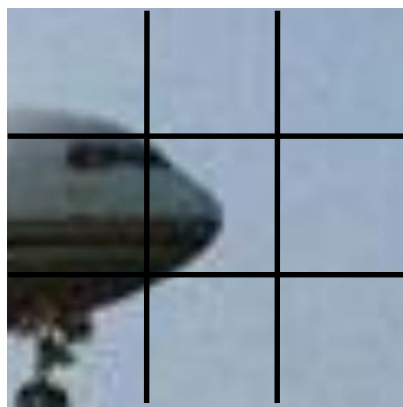


Retains rough spatial layout  
Some invariance to deformations

*What are the problems?*

# Spatial histograms

Compute histograms over spatial 'cells'



Retains rough spatial layout  
Some invariance to deformations

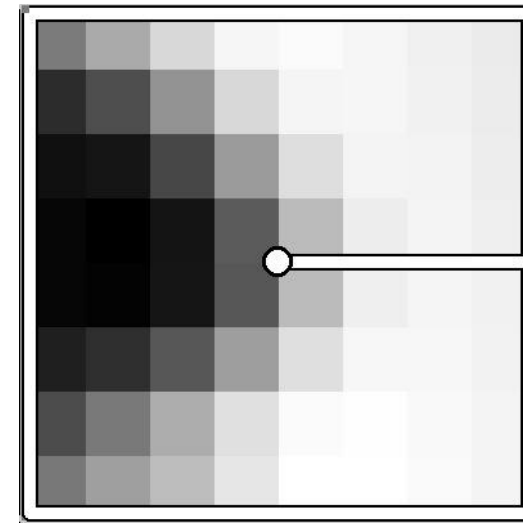
*What are the problems?*

*How can you be completely invariant to rotation?*



# Orientation normalization

Use the dominant image gradient direction to normalize the orientation of the patch



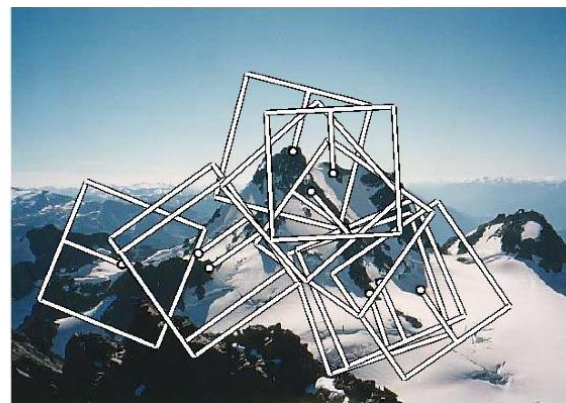
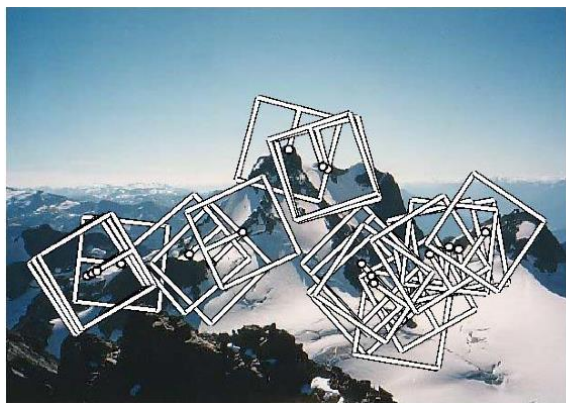
save the orientation angle  $\theta$  along with  $(x, y, s)$

*What are the problems?*

MOPS descriptor

# Multi-Scale Oriented Patches (MOPS)

Multi-Image Matching using Multi-Scale Oriented Patches. M. Brown, R. Szeliski and S. Winder.  
International Conference on Computer Vision and Pattern Recognition (CVPR2005). pages 510-517





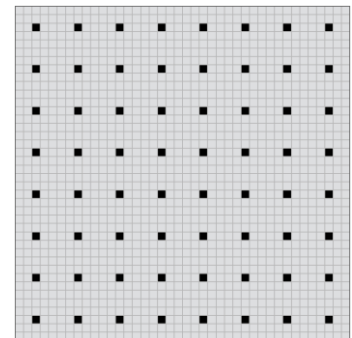
# Multi-Scale Oriented Patches (MOPS)

Multi-Image Matching using Multi-Scale Oriented Patches. M. Brown, R. Szeliski and S. Winder.  
International Conference on Computer Vision and Pattern Recognition (CVPR2005). pages 510-517

Given a feature  $(x, y, s, \theta)$

Get 40 x 40 image patch, subsample every 5th pixel

*(what's the purpose of this step?)*



Subtract the mean, divide by standard deviation

*(what's the purpose of this step?)*

Haar Wavelet Transform

*(what's the purpose of this step?)*

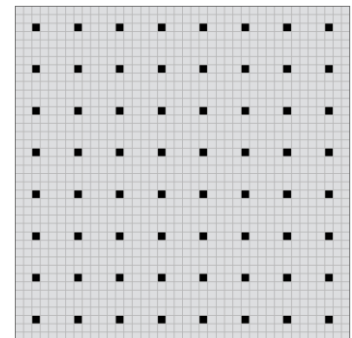
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Given a feature  $(x, y, s, \theta)$

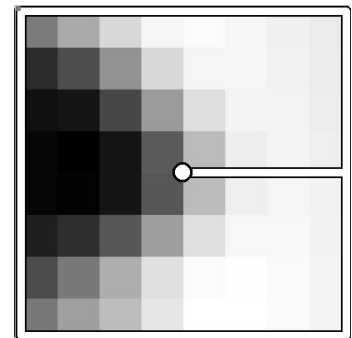
Get 40 x 40 image patch, subsample every 5th pixel

(low frequency filtering, absorbs localization errors)



Subtract the mean, divide by standard deviation

*(what's the purpose of this step?)*



Haar Wavelet Transform

*(what's the purpose of this step?)*

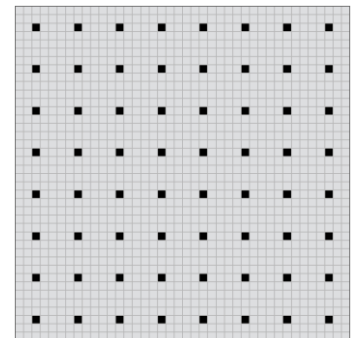
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Given a feature  $(x, y, s, \theta)$

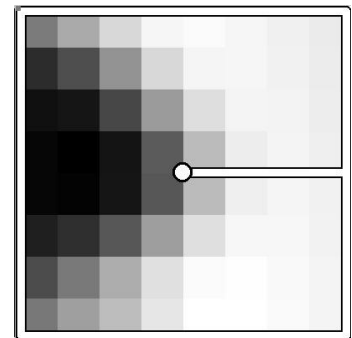
Get 40 x 40 image patch, subsample every 5th pixel

(low frequency filtering, absorbs localization errors)



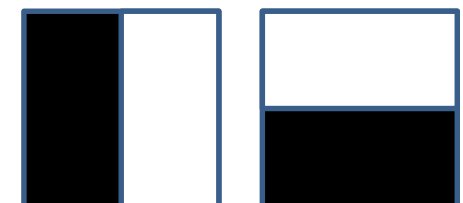
Subtract the mean, divide by standard deviation

(removes bias and gain)



Haar Wavelet Transform

(*what's the purpose of this step?*)





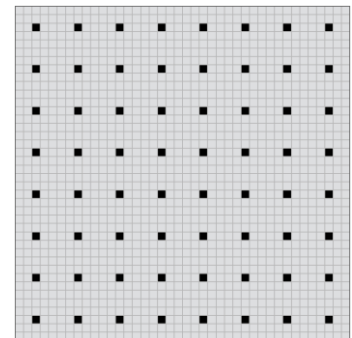
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International Conference on Computer Vision and Pattern Recognition (CVPR2005). pages 510-517

Given a feature  $(x, y, s, \theta)$

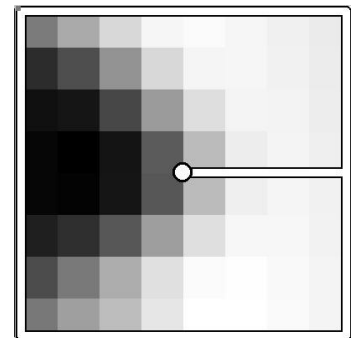
Get 40 x 40 image patch, subsample  
every 5th pixel

(low frequency filtering, absorbs localization errors)



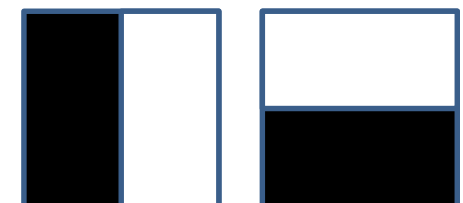
Subtract the mean, divide by standard  
deviation

(removes bias and gain)



Haar Wavelet Transform

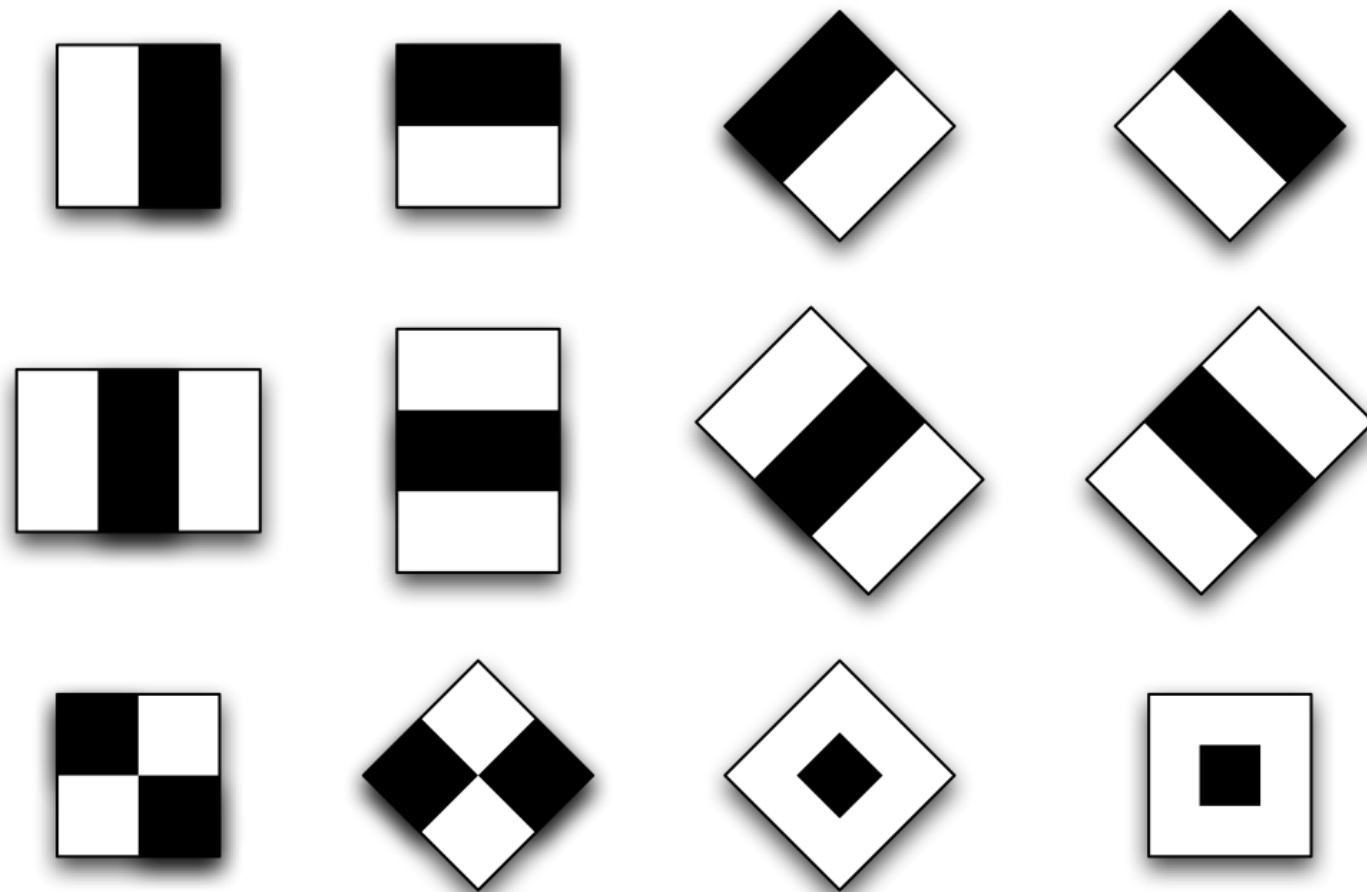
(low frequency projection)



# Haar Wavelets

(actually, Haar-like features)

Use responses of a bank of filters as a descriptor



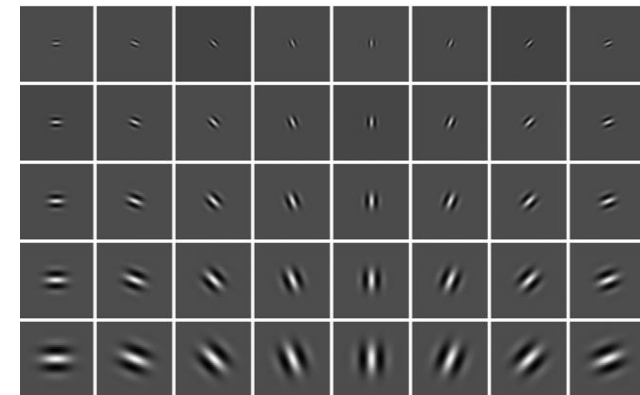
We will see later in class how to compute Haar wavelet responses **efficiently** (in constant time) with integral images

GIST descriptor

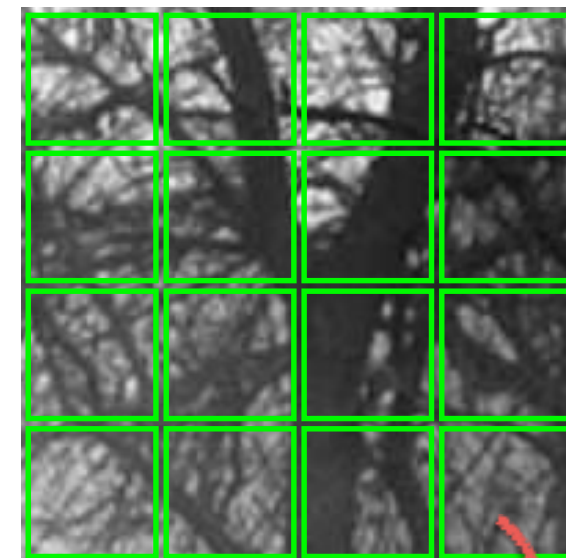
# GIST

1. Compute filter responses (filter bank of Gabor filters)
2. Divide image patch into 4 x 4 cells
3. Compute filter response averages for each cell
4. Size of descriptor is 4 x 4 x N, where N is the size of the filter bank

Filter bank



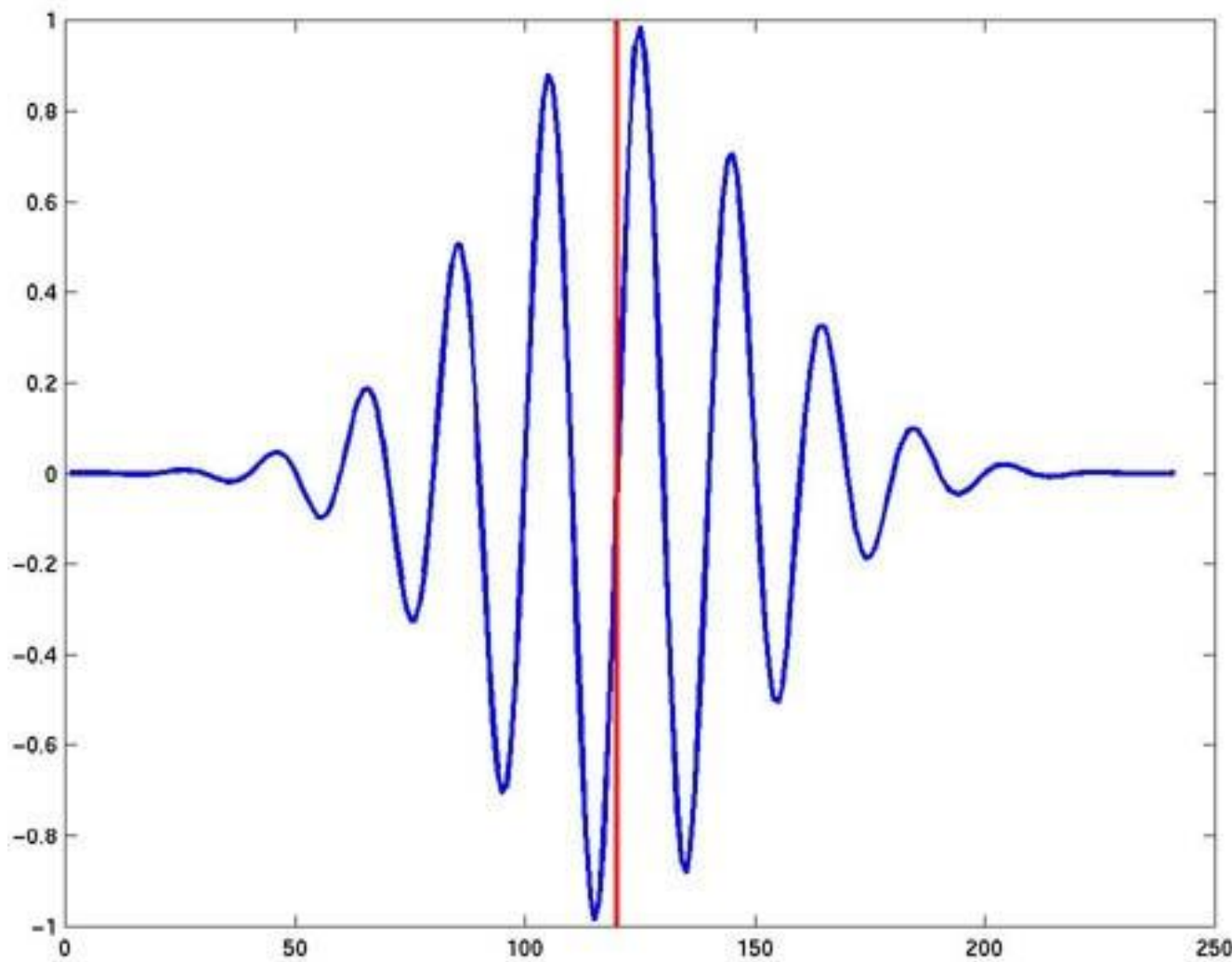
4 x 4 cell



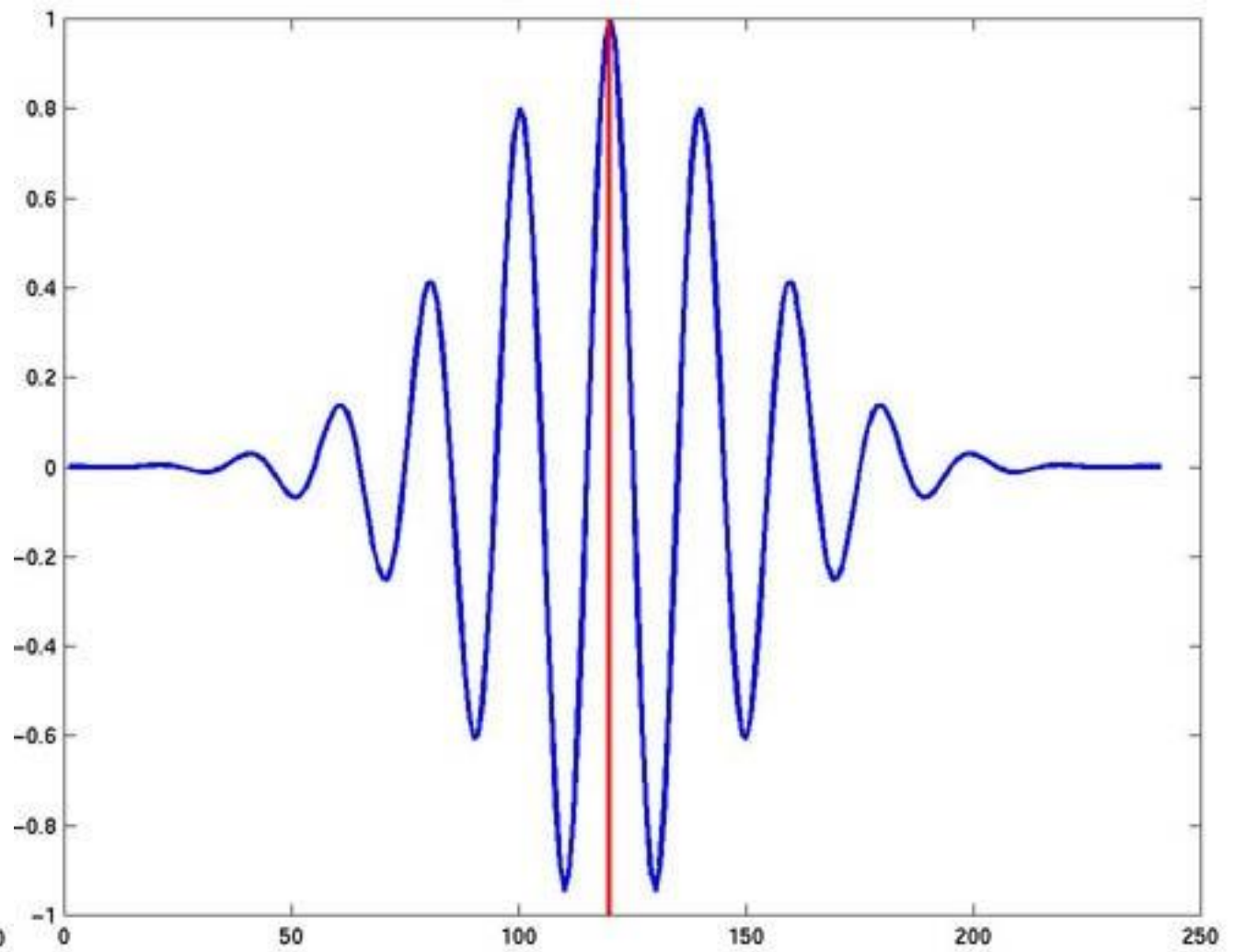


# Gabor Filters

(1D examples)



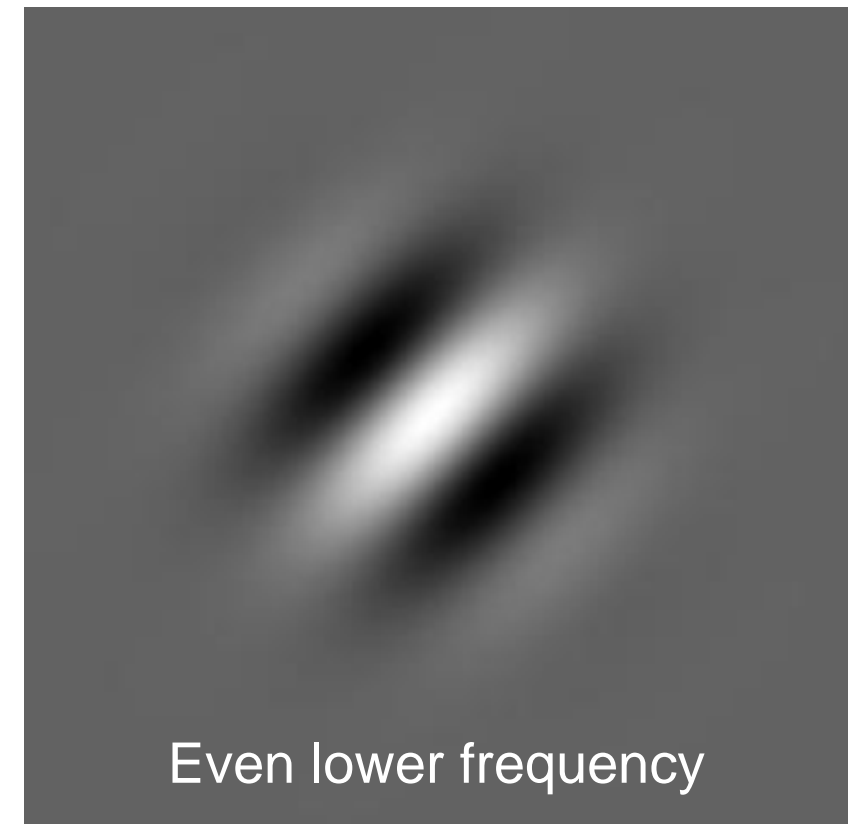
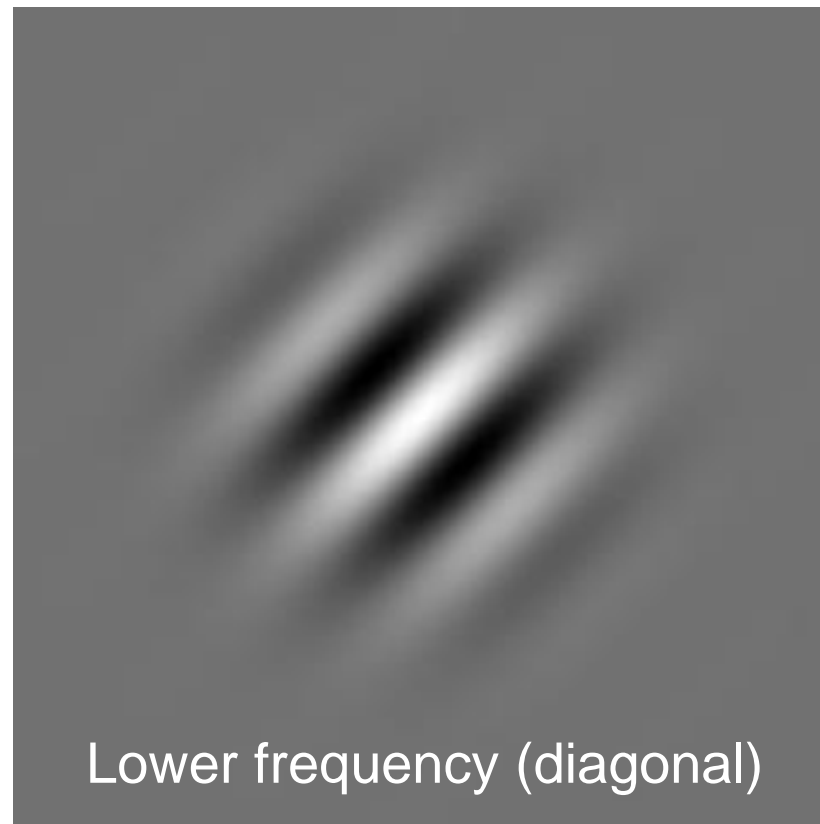
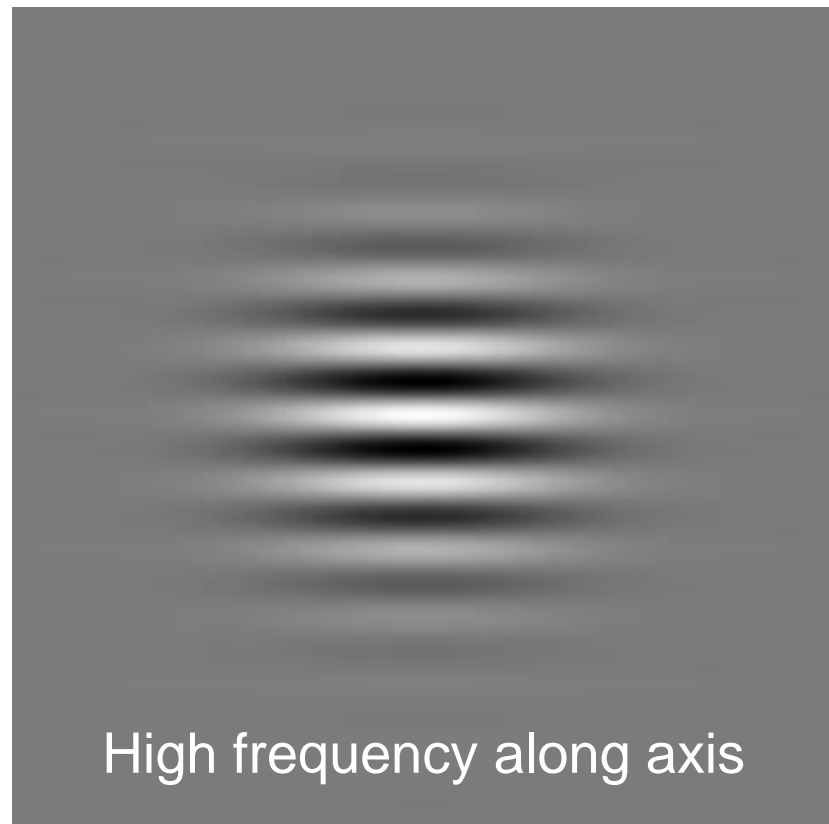
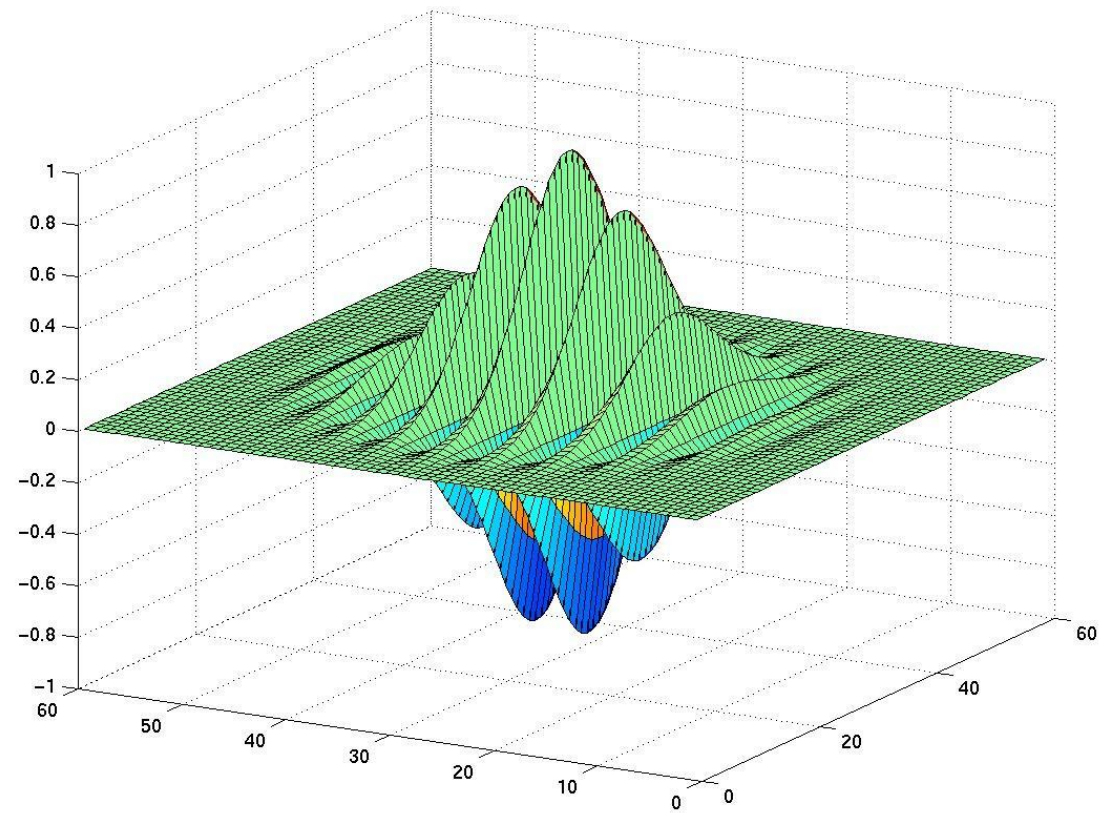
$$e^{-\frac{x^2}{2\sigma^2}} \sin(2\pi\omega x)$$

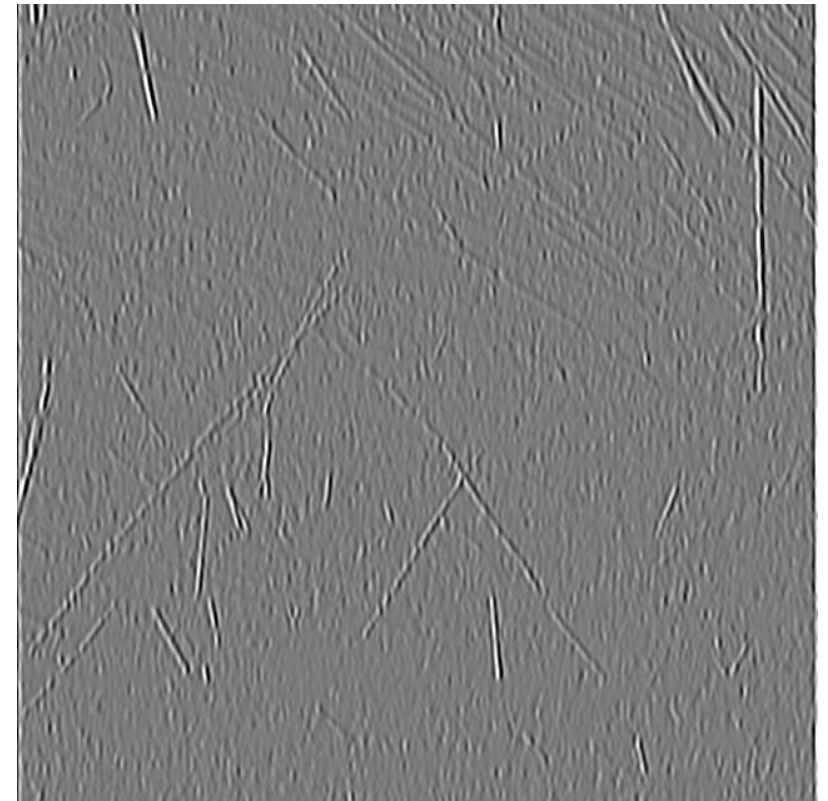
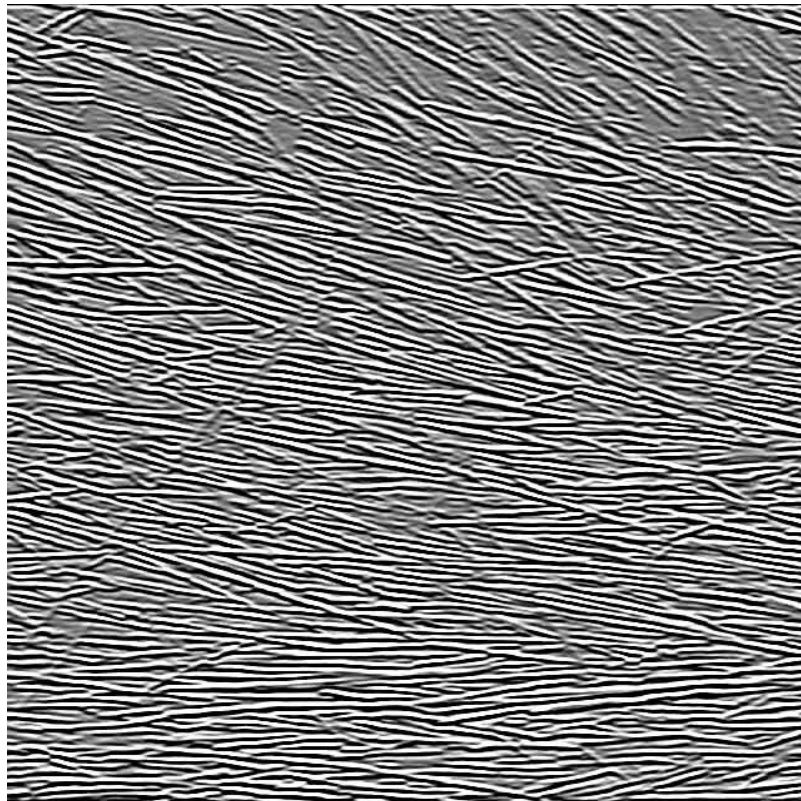
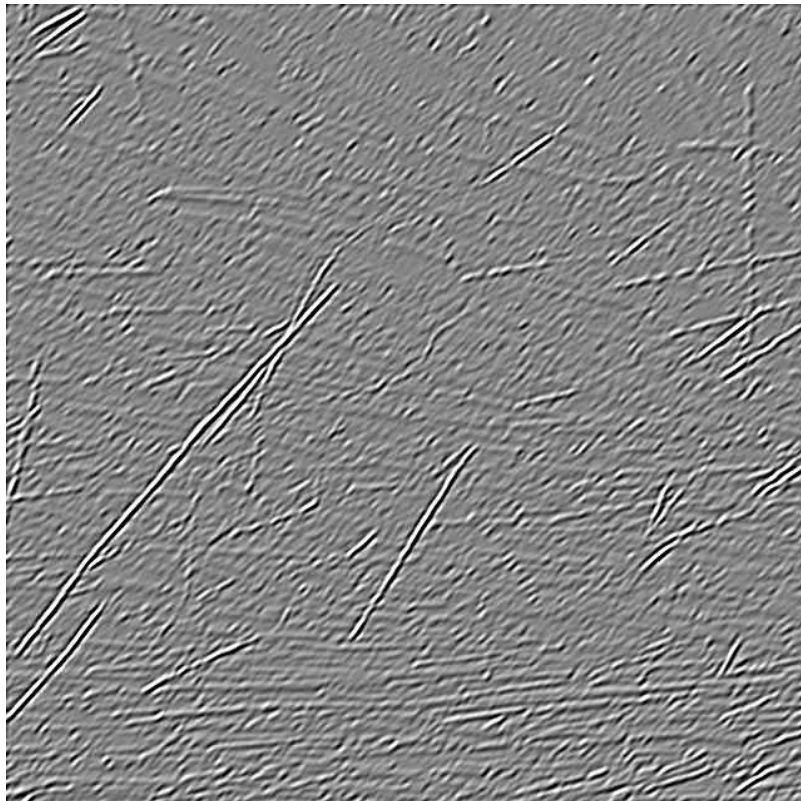
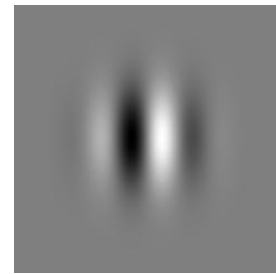
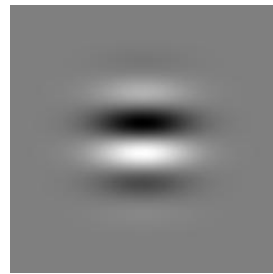
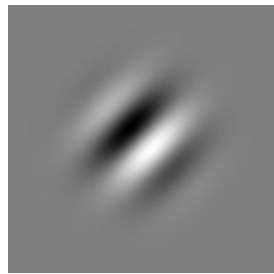
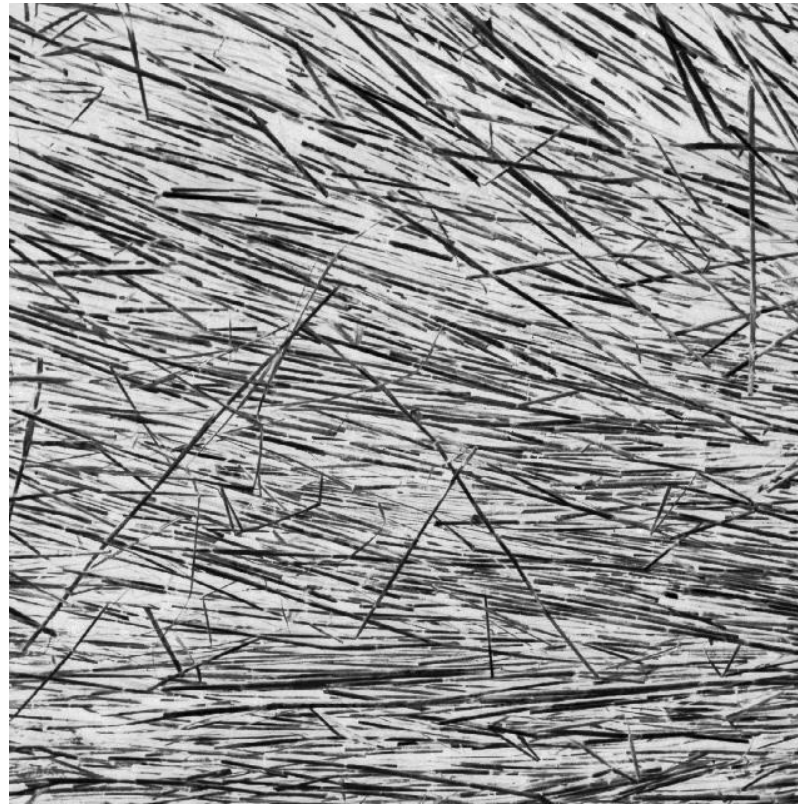


$$e^{-\frac{x^2}{2\sigma^2}} \cos(2\pi\omega x)$$

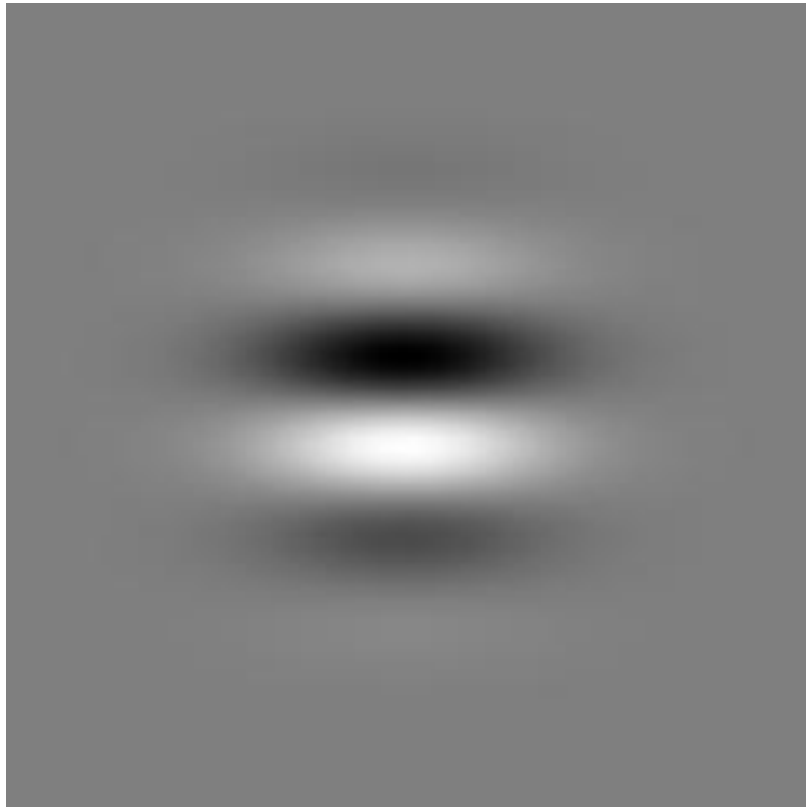
# 2D Gabor Filters

$$e^{-\frac{x^2+y^2}{2\sigma^2}} \cos(2\pi(k_x x + k_y y))$$

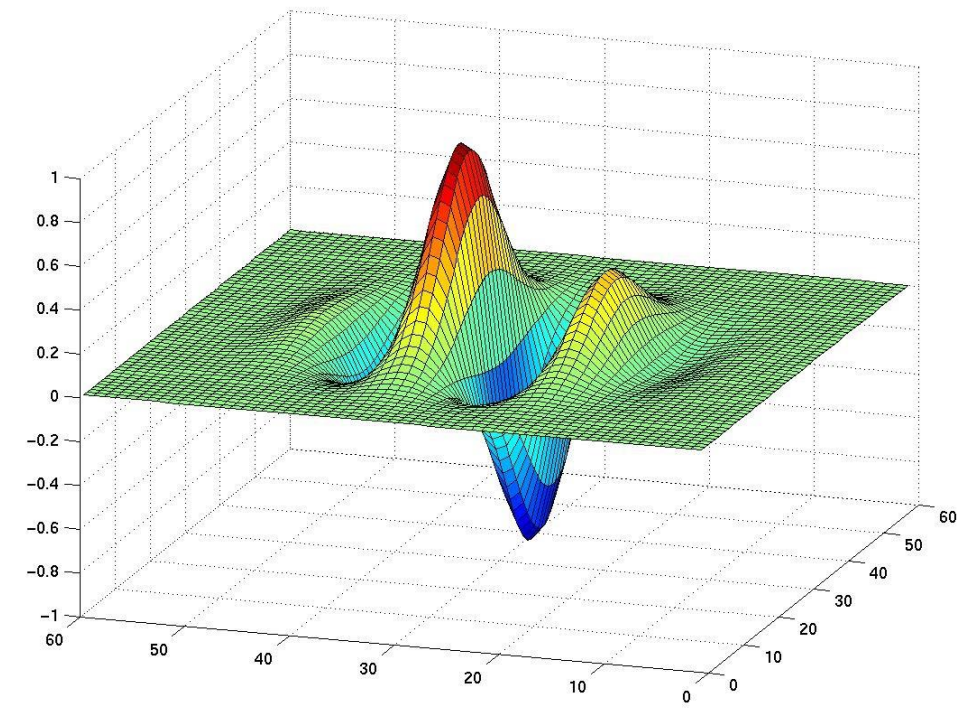




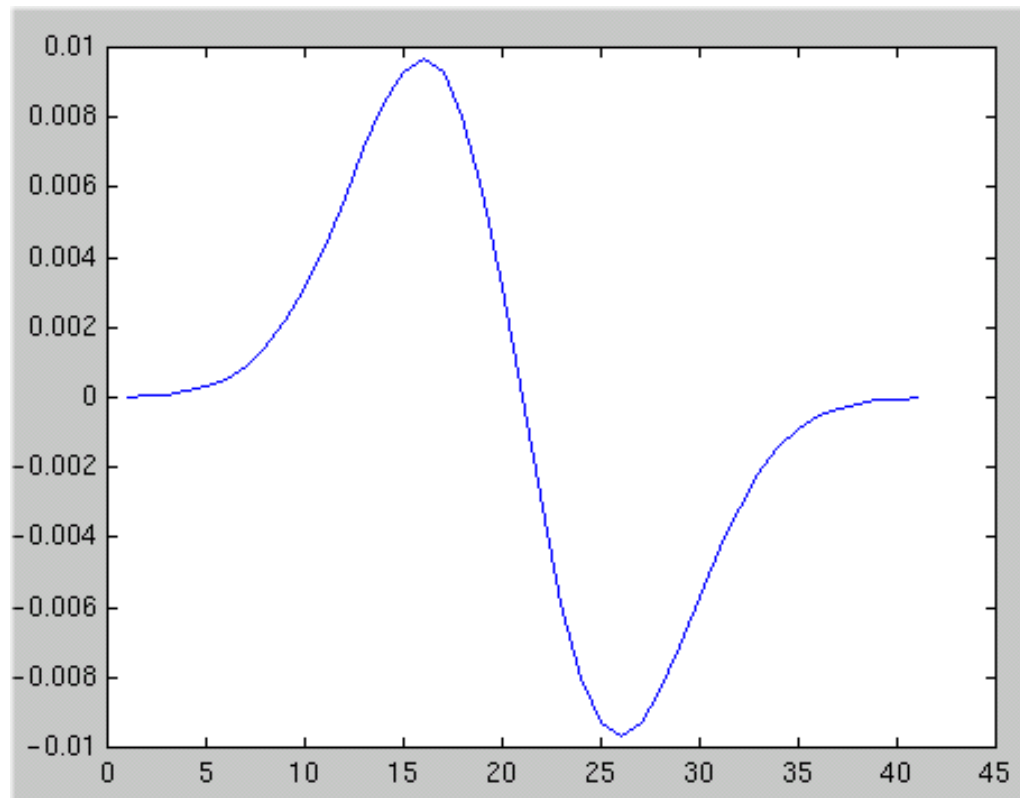




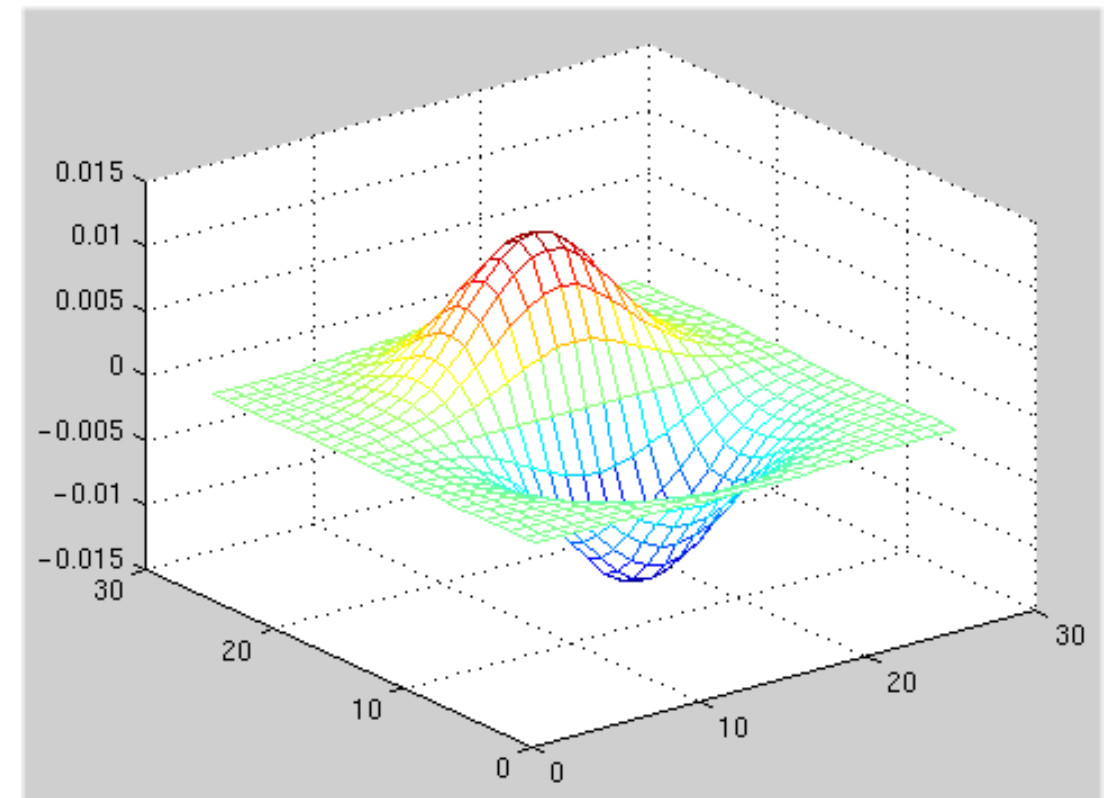
Odd  
Gabor  
filter



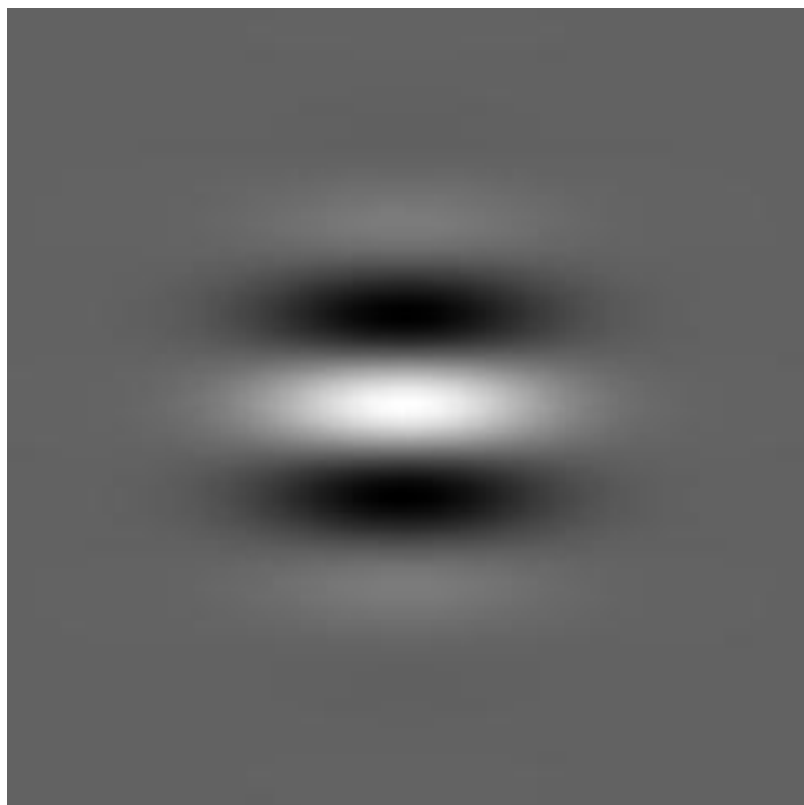
... looks a lot like...



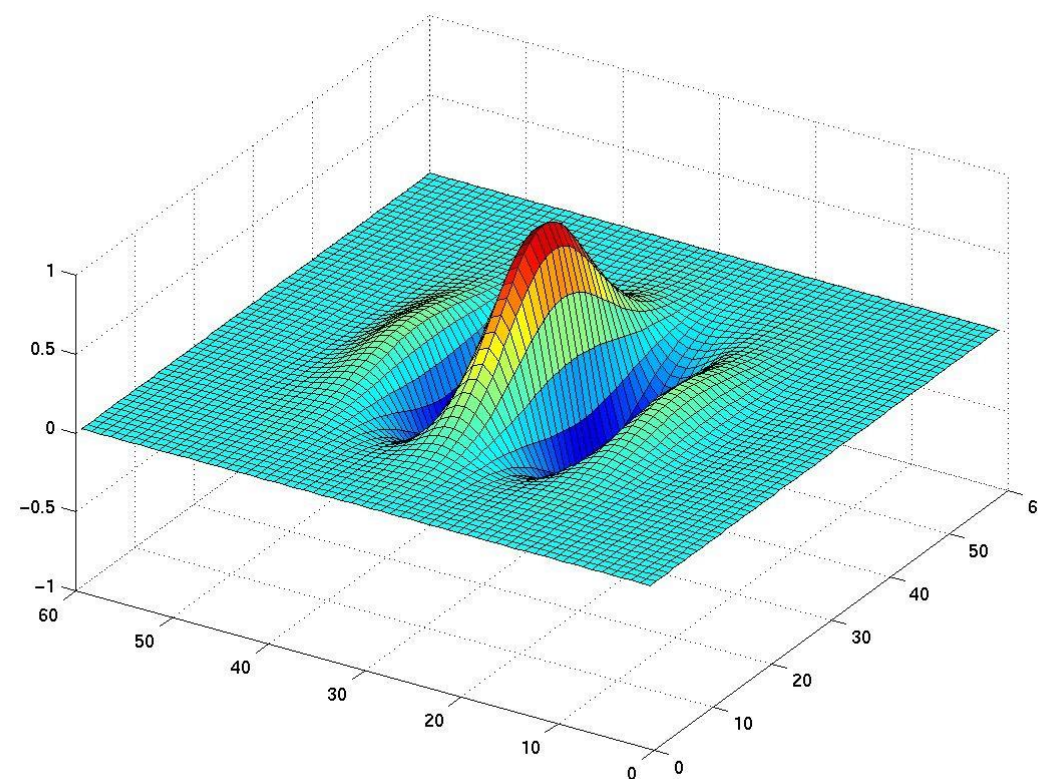
Gaussian  
Derivative



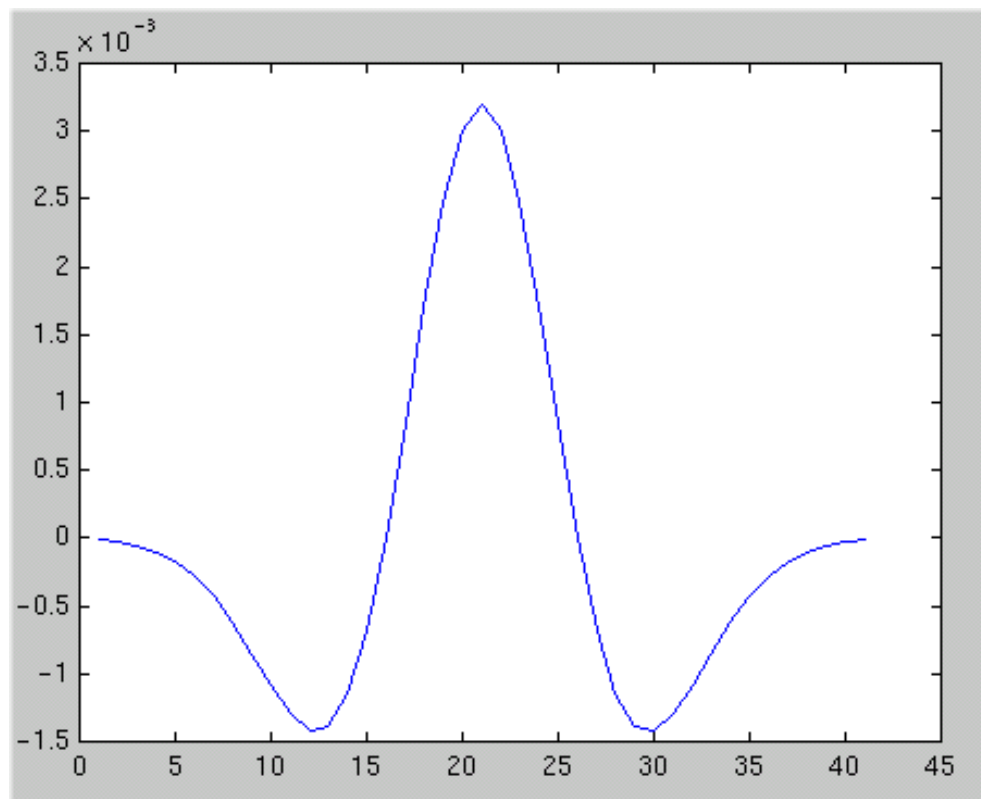




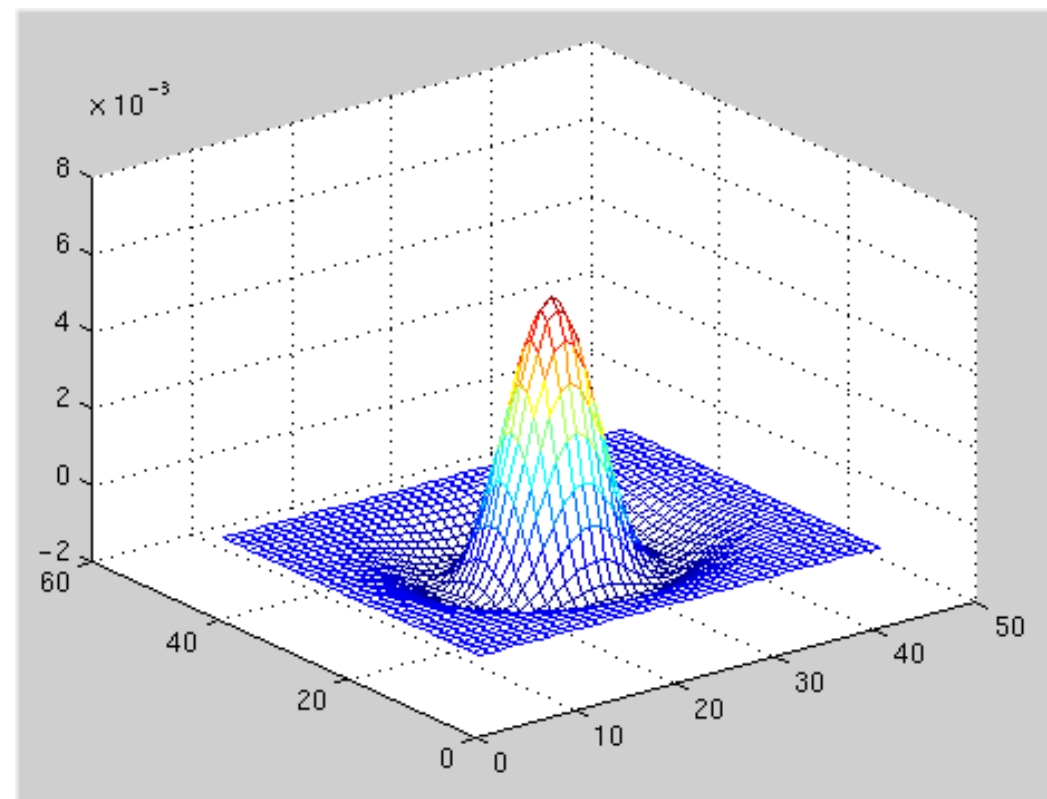
Even  
Gabor  
filter



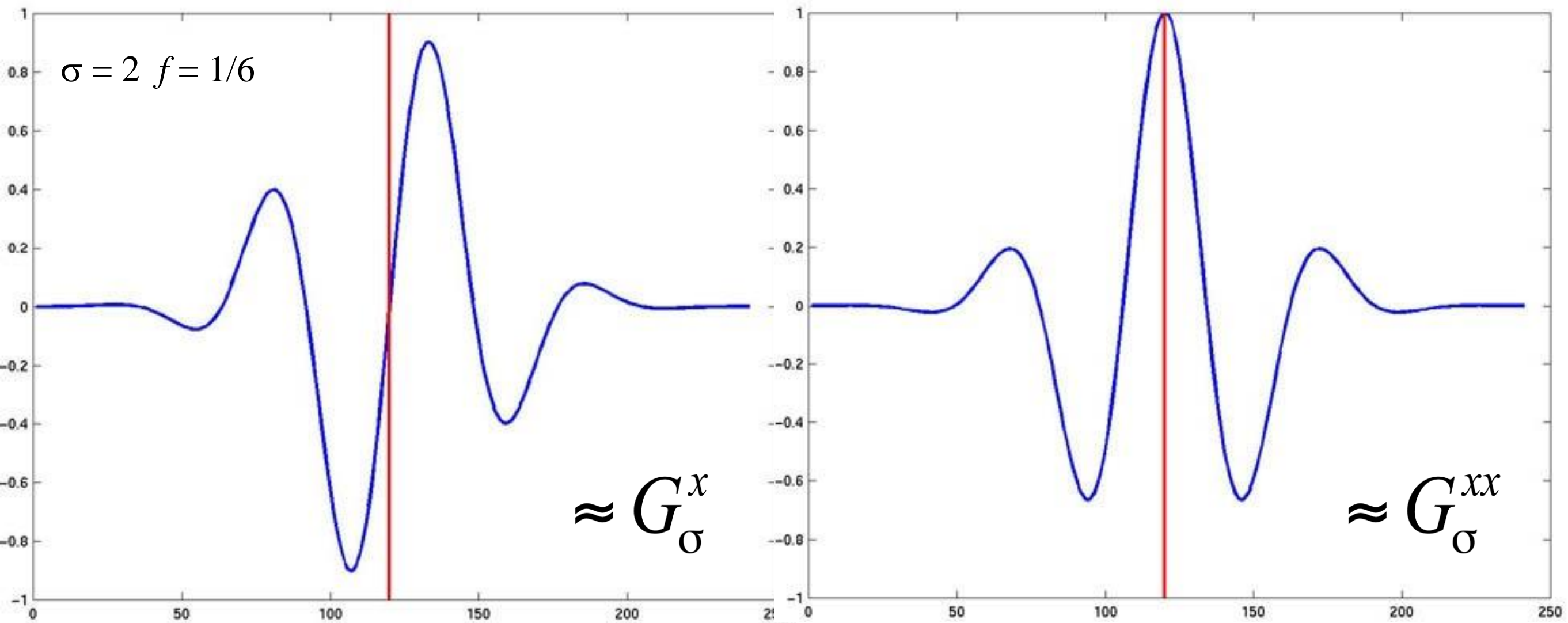
... looks a lot like...



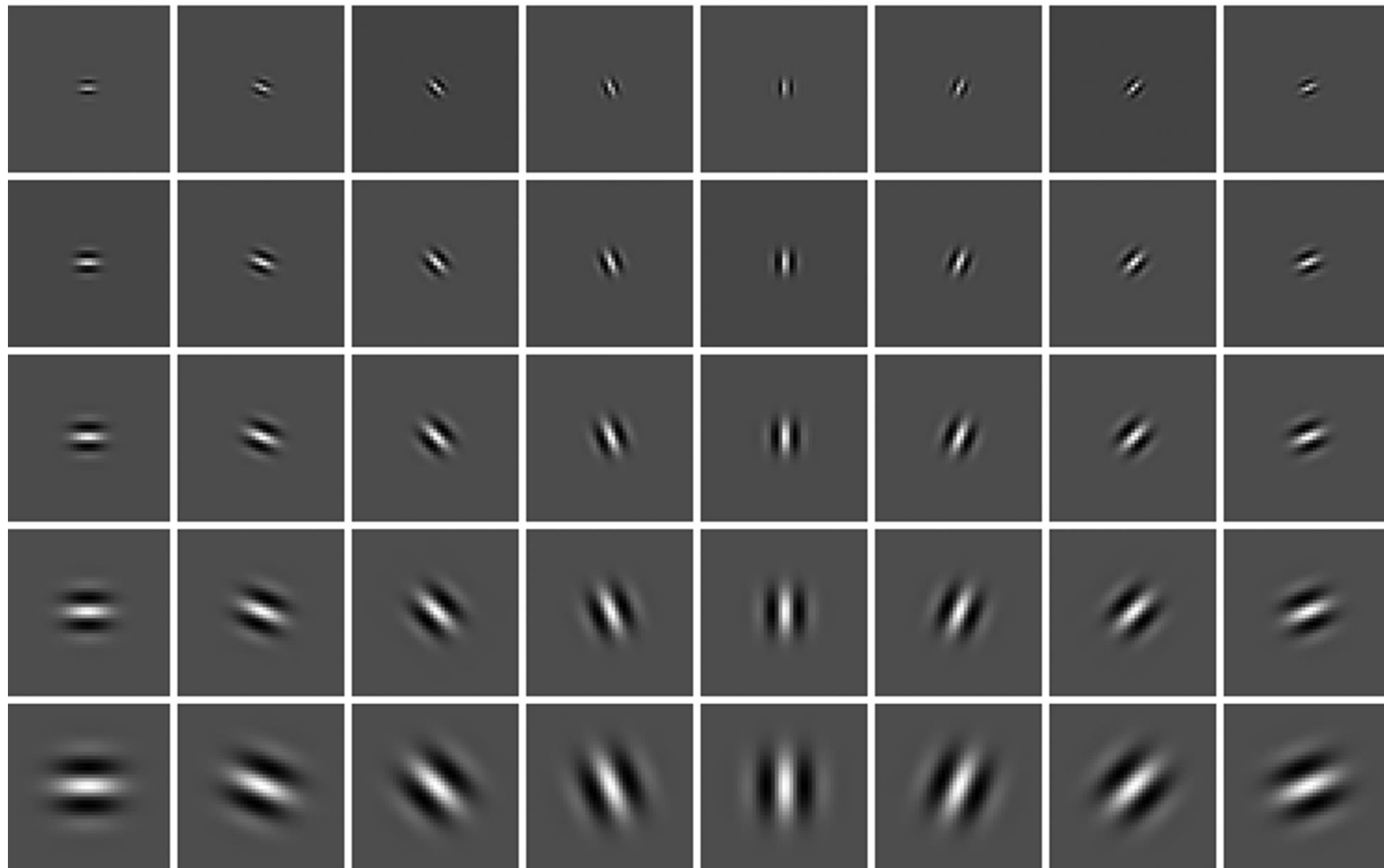
Laplacian



If scale small compared to inverse frequency, the Gabor filters become derivative operators



# Directional edge detectors

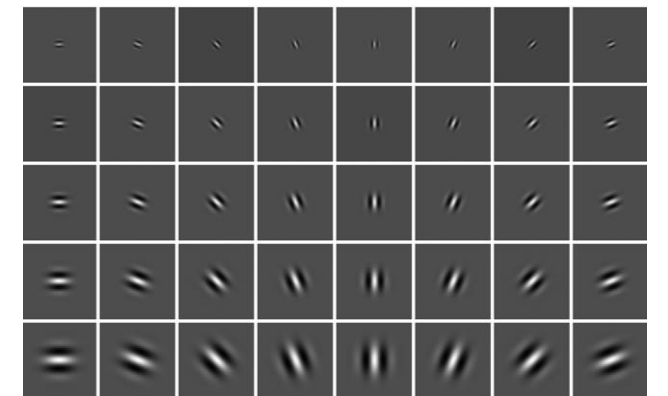


# GIST

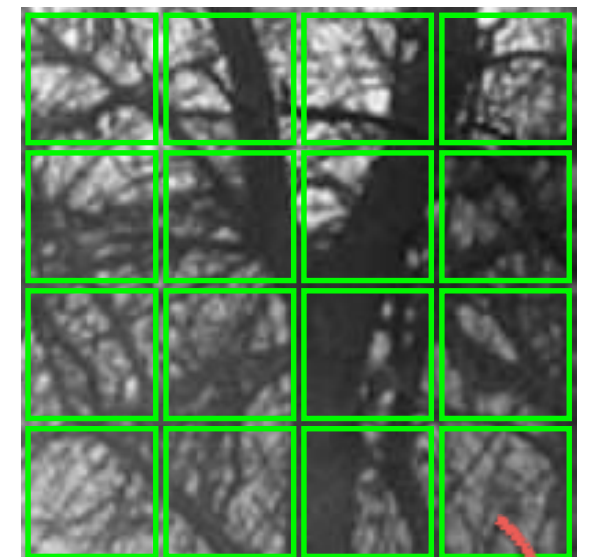
1. Compute filter responses (filter bank of Gabor filters)
2. Divide image patch into 4 x 4 cells
3. Compute filter response averages for each cell
4. Size of descriptor is 4 x 4 x N, where N is the size of the filter bank

*What is the GIST descriptor encoding?*

Filter bank



4 x 4 cell





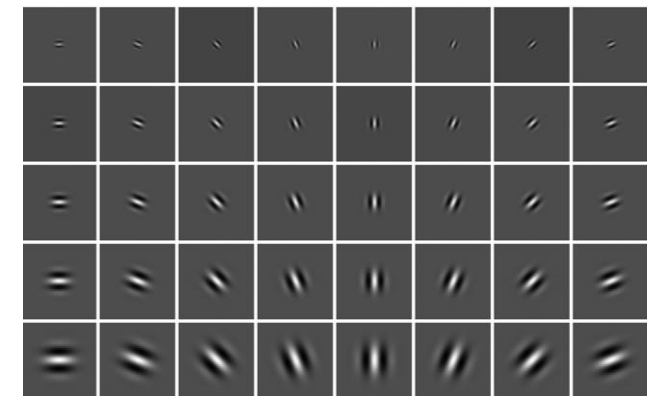
# GIST

1. Compute filter responses (filter bank of Gabor filters)
2. Divide image patch into 4 x 4 cells
3. Compute filter response averages for each cell
4. Size of descriptor is 4 x 4 x N, where N is the size of the filter bank

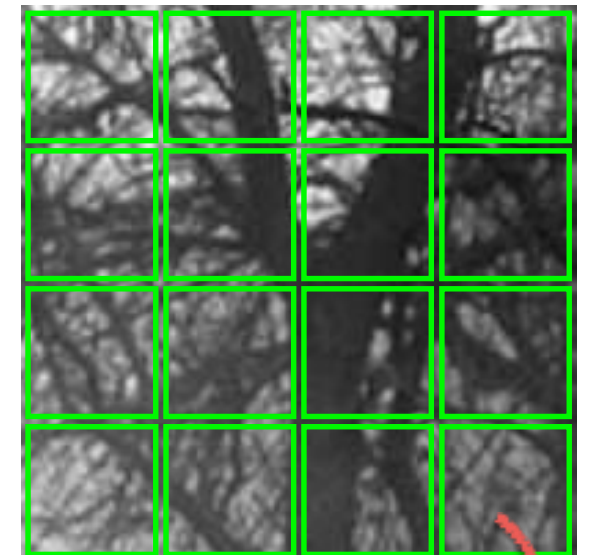
*What is the GIST descriptor encoding?*

Rough spatial distribution of image gradients

Filter bank



4 x 4 cell

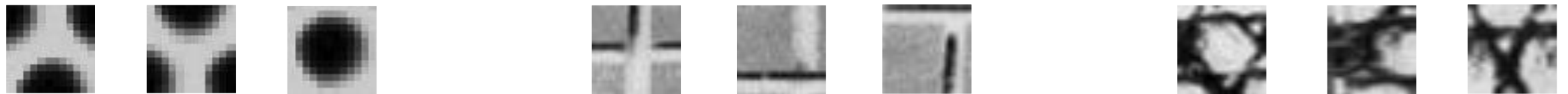


# Histogram of Textons descriptor

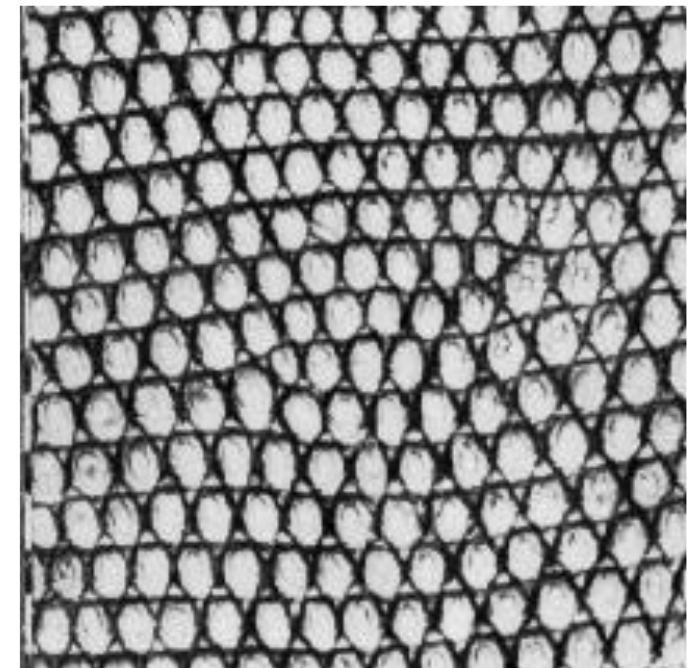
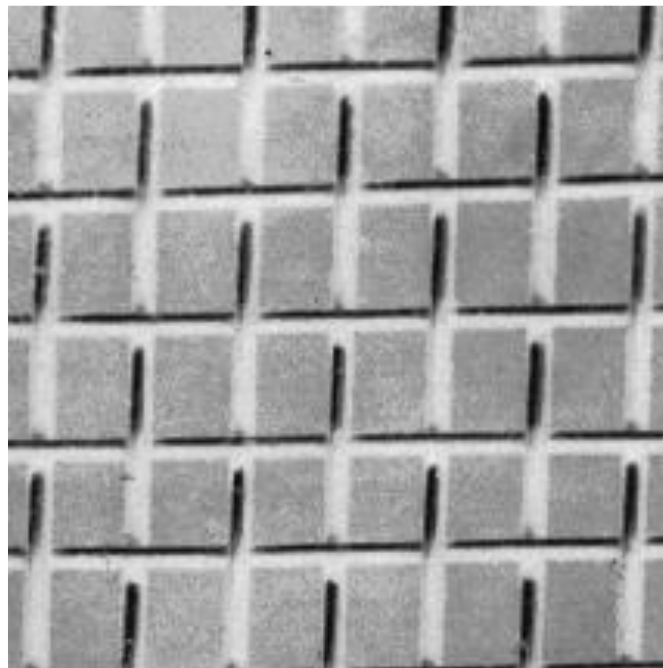
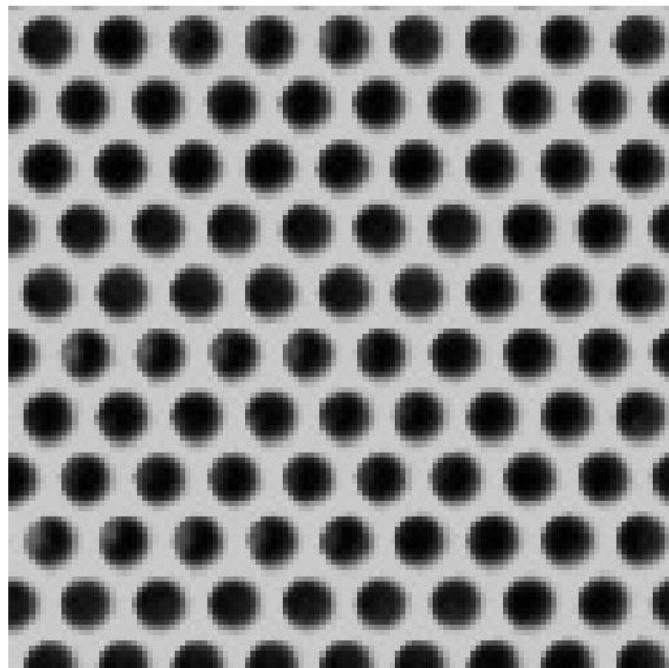
# Textons

Julesz. Textons, the elements of texture perception, and their interactions. Nature 1981

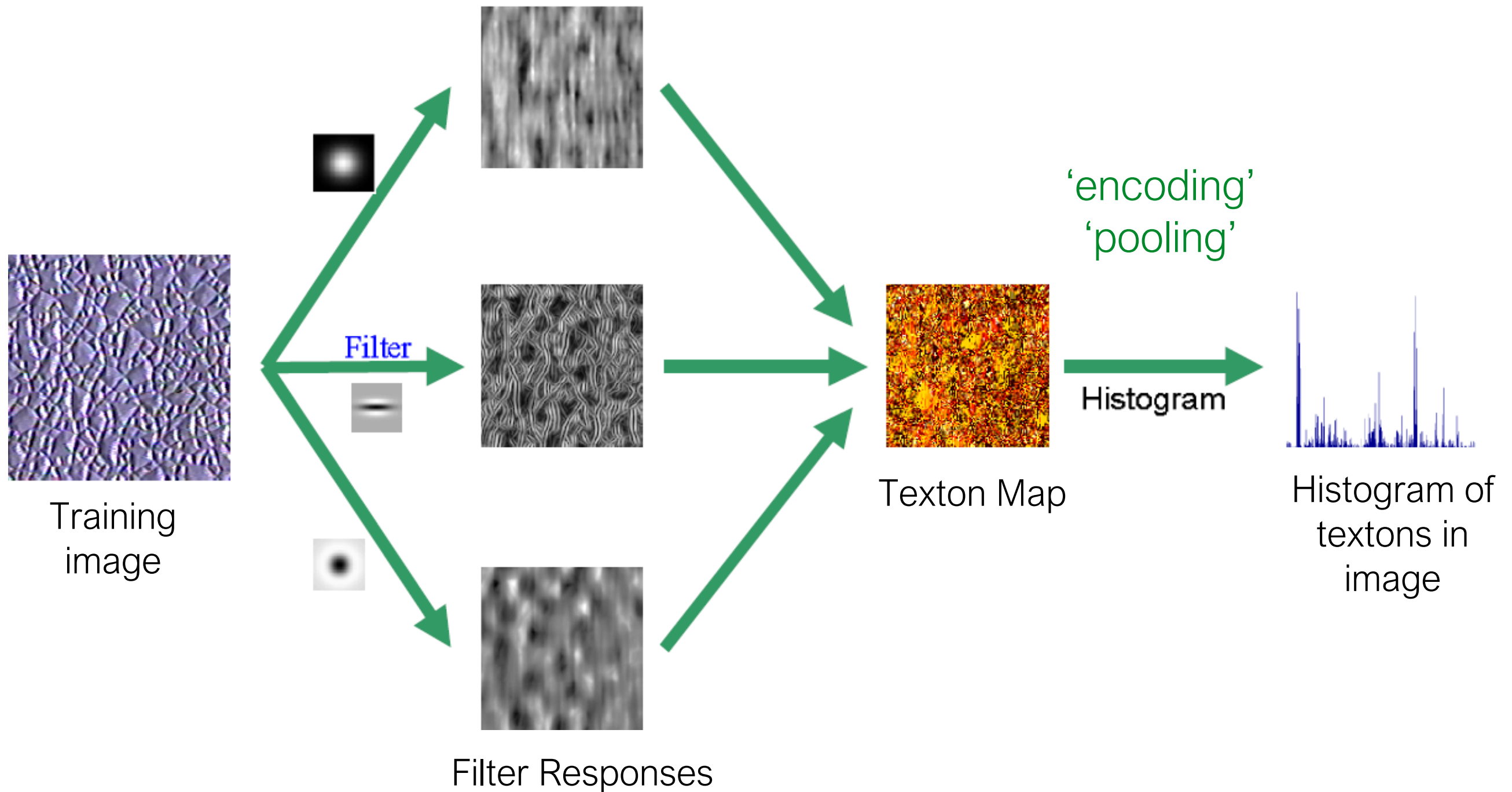
**Texture** is characterized by the repetition of basic elements or ***textons***



For stochastic textures, it is the identity of the ***textons***, not their spatial arrangement, that matters

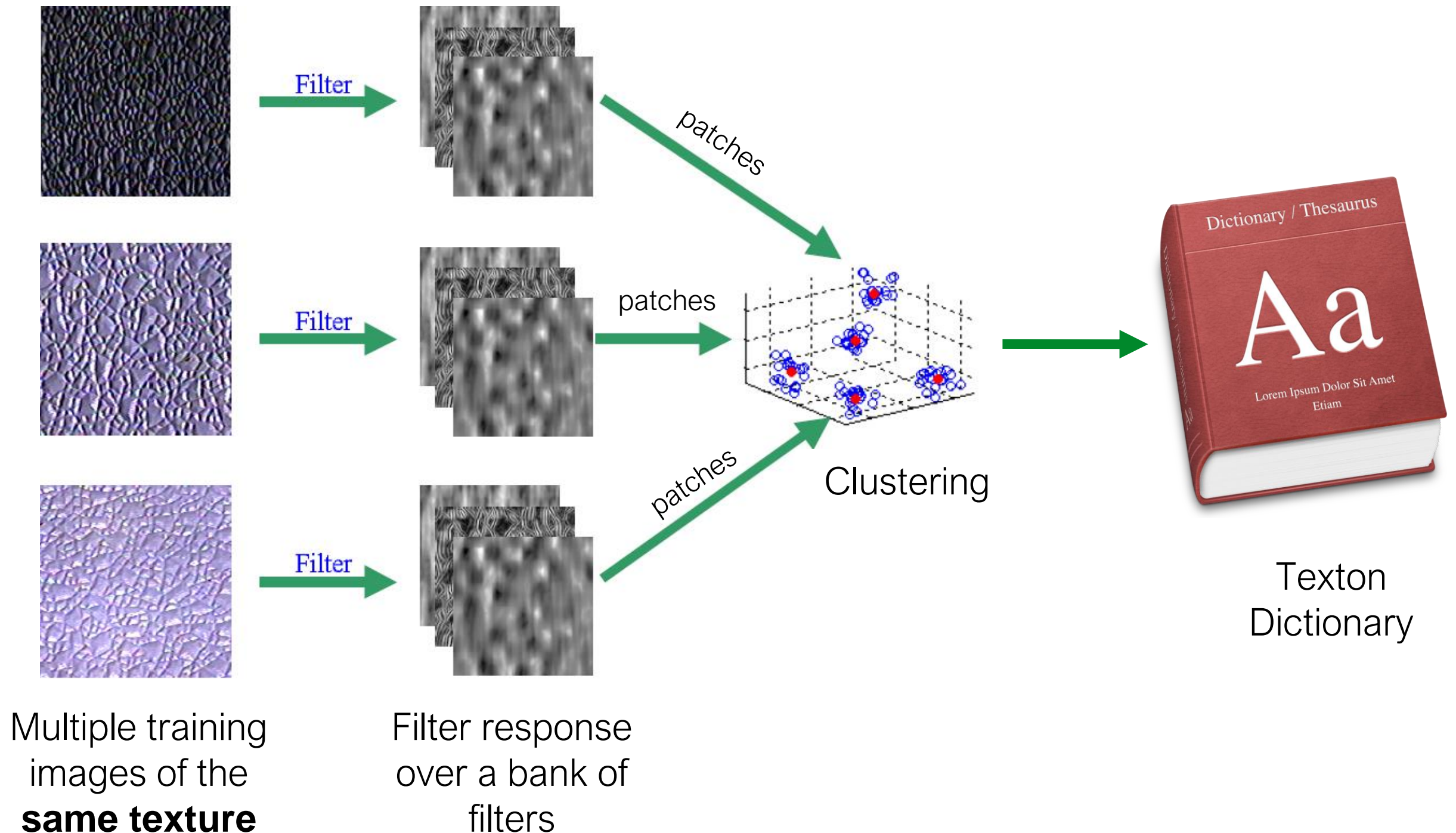


# Histogram of Textons descriptor

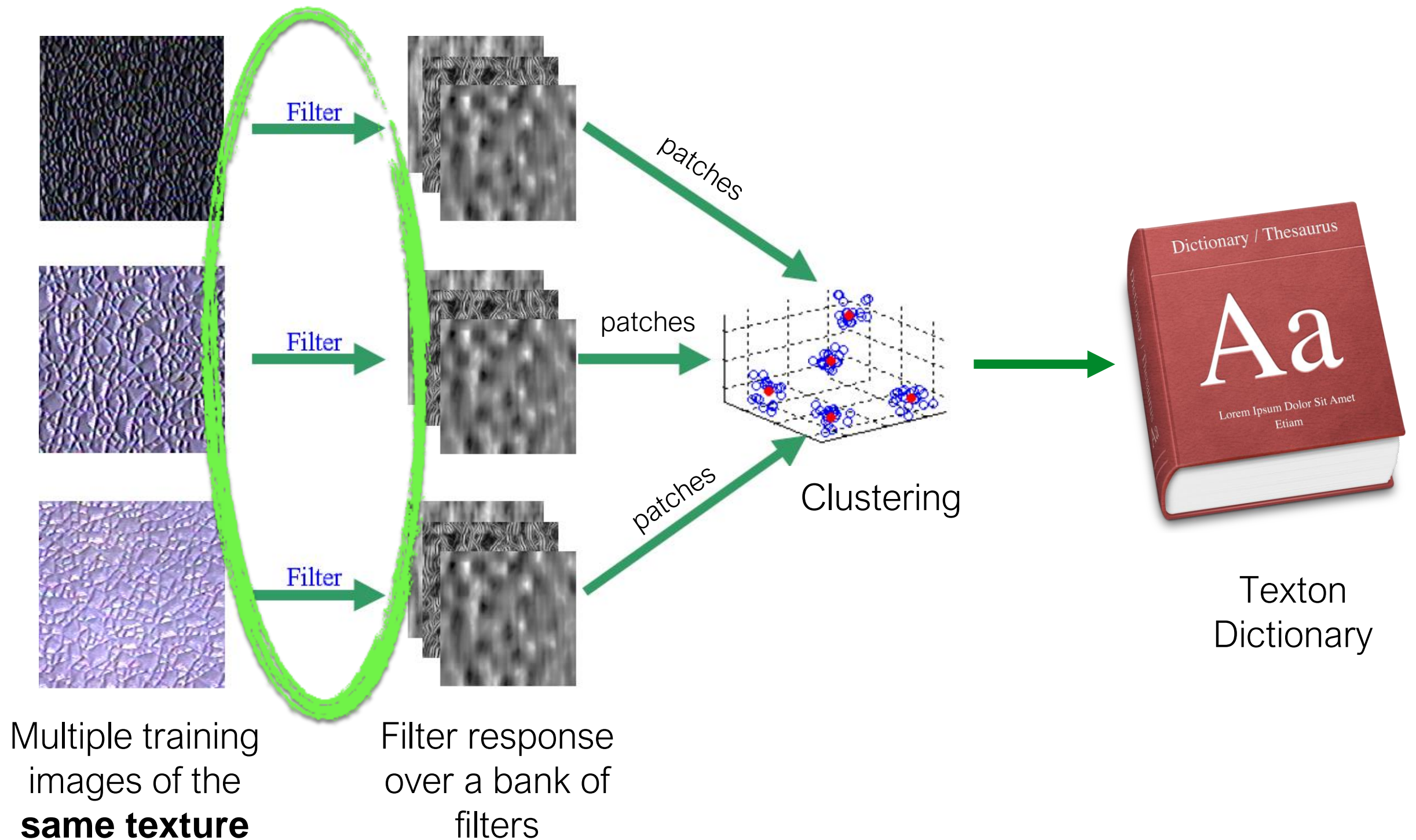




# Learning Textons from data

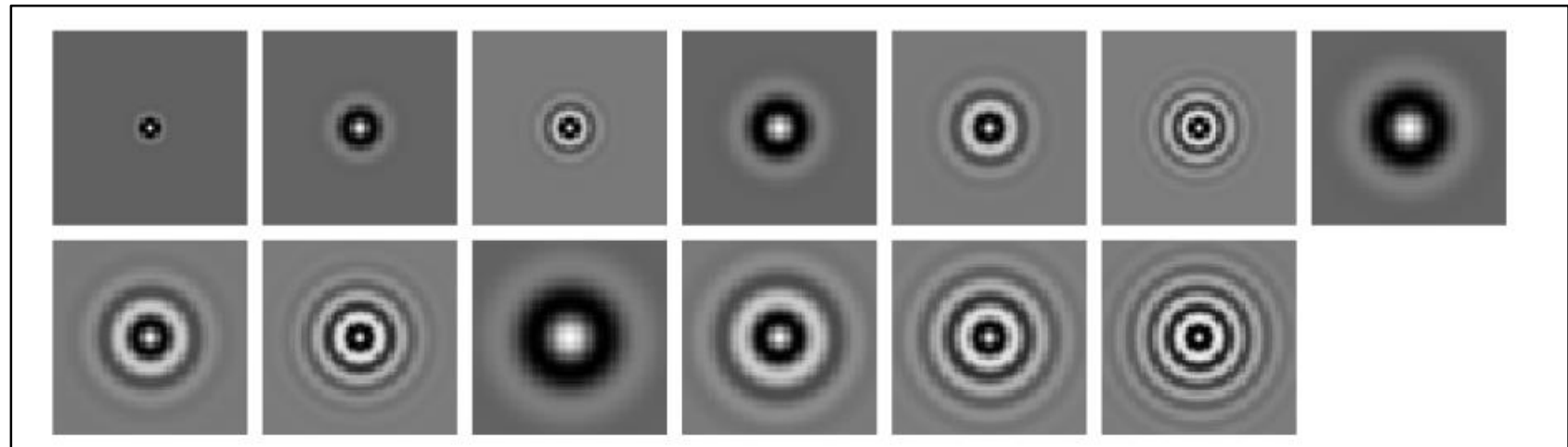


# Learning Textons from data



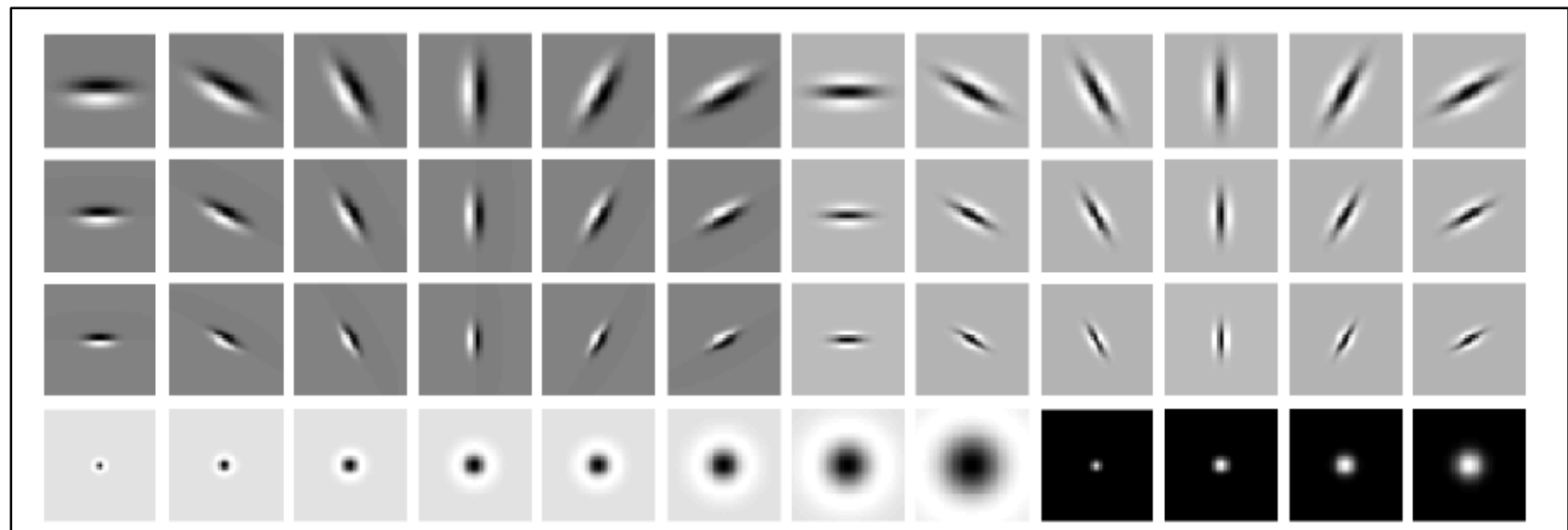
# Example of Filter Banks

Isotropic Gabor

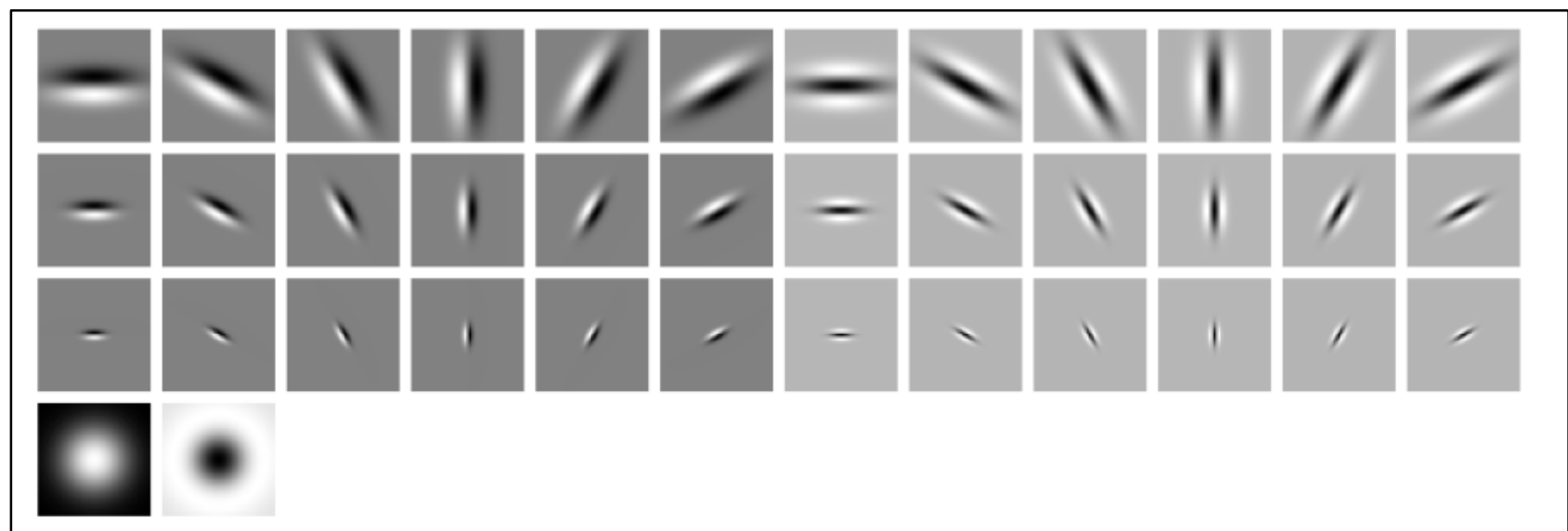


'S'

Gaussian derivatives at different scales and orientations



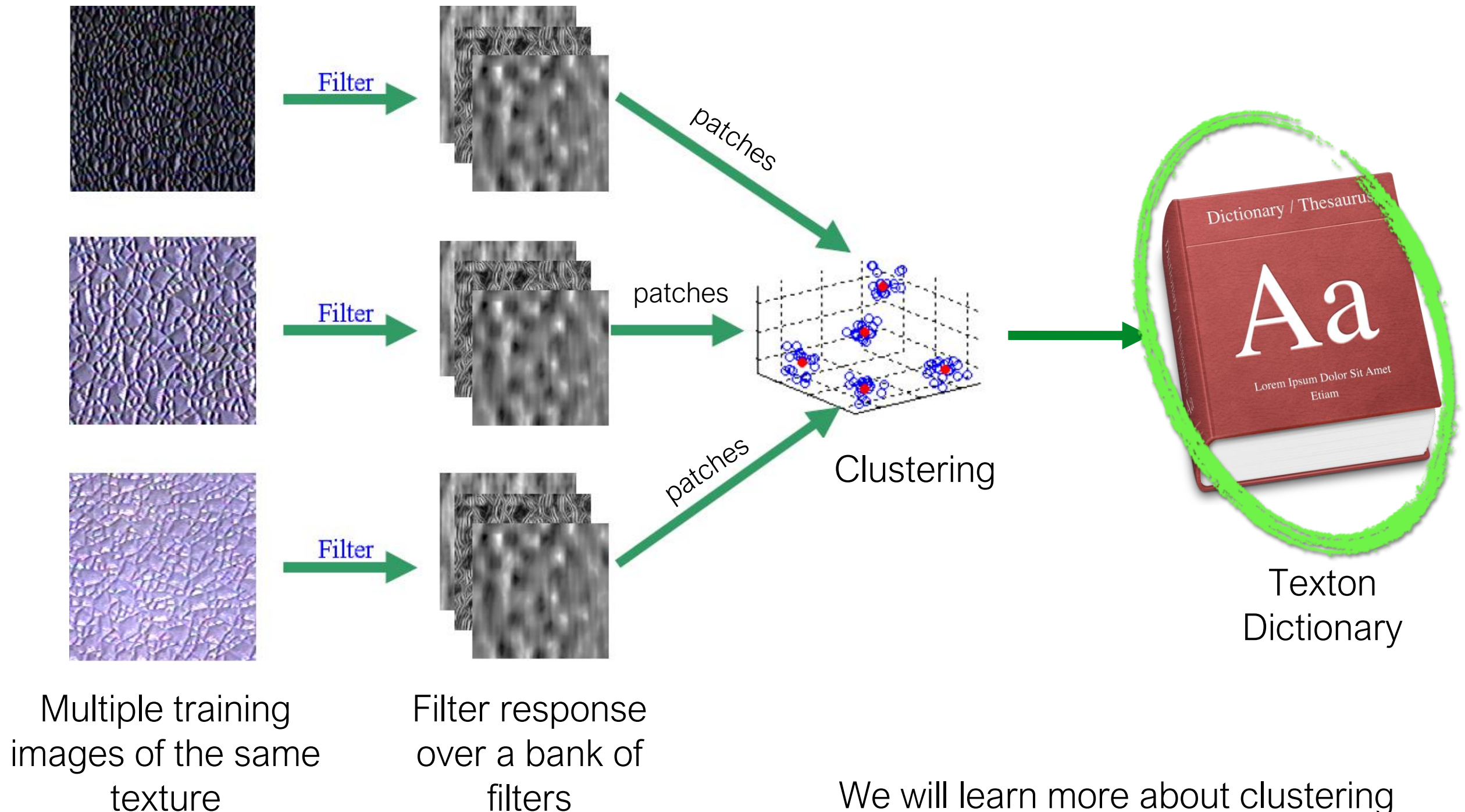
'LM'



'MR8'



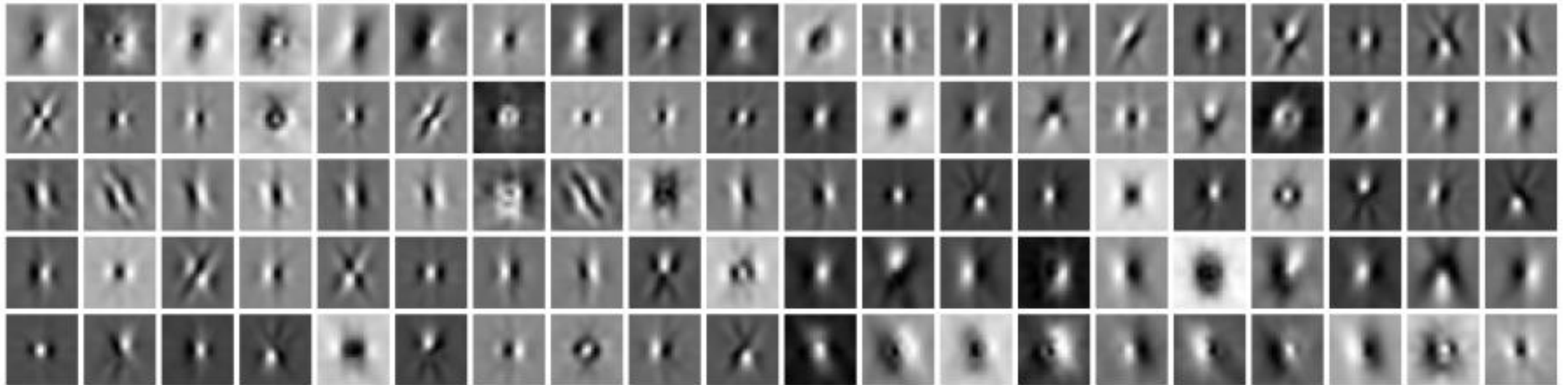
# Learning Textons from data



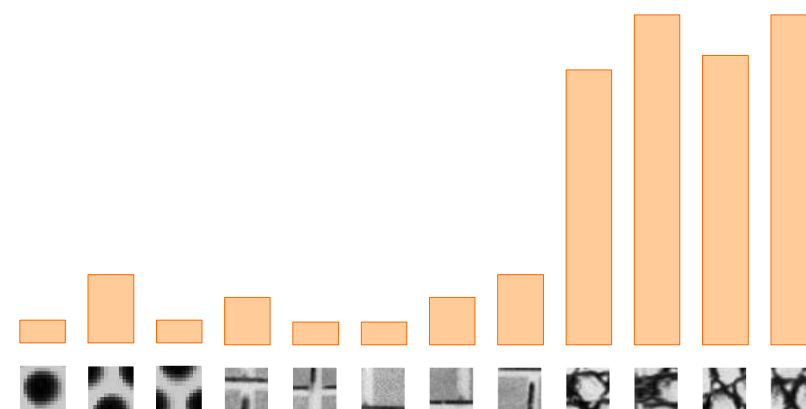
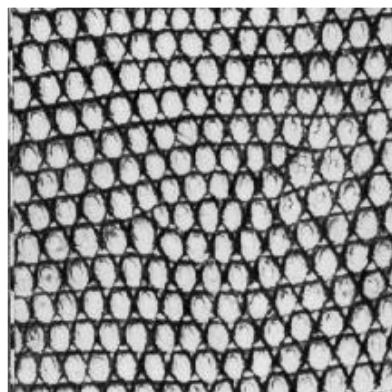
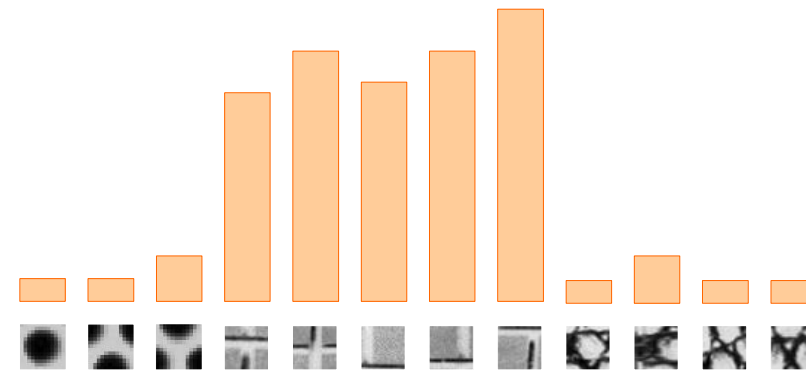
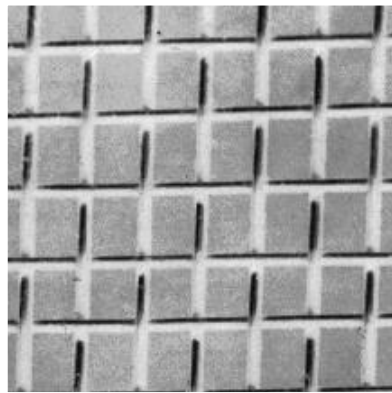
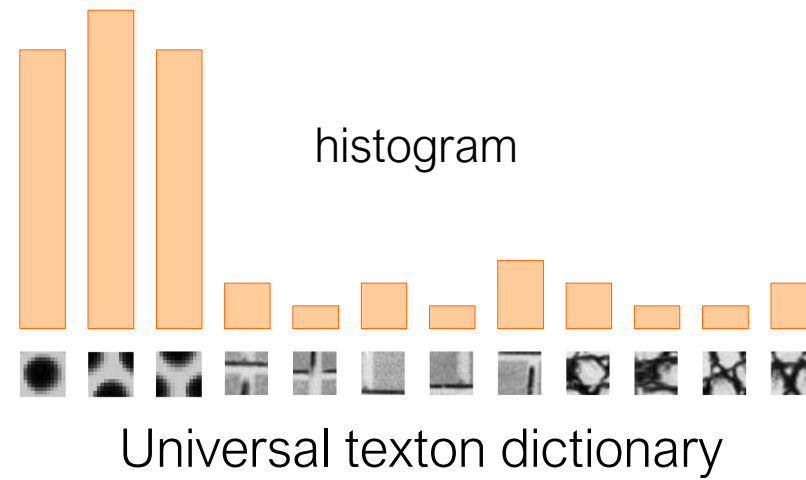
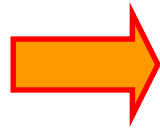
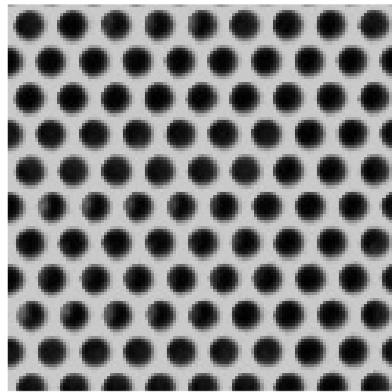
We will learn more about clustering later in class (Bag of Words lecture).



# Texton Dictionary



Malik, Belongie, Shi, Leung. Textons, Contours and Regions: Cue Integration in Image Segmentation. ICCV 1999.



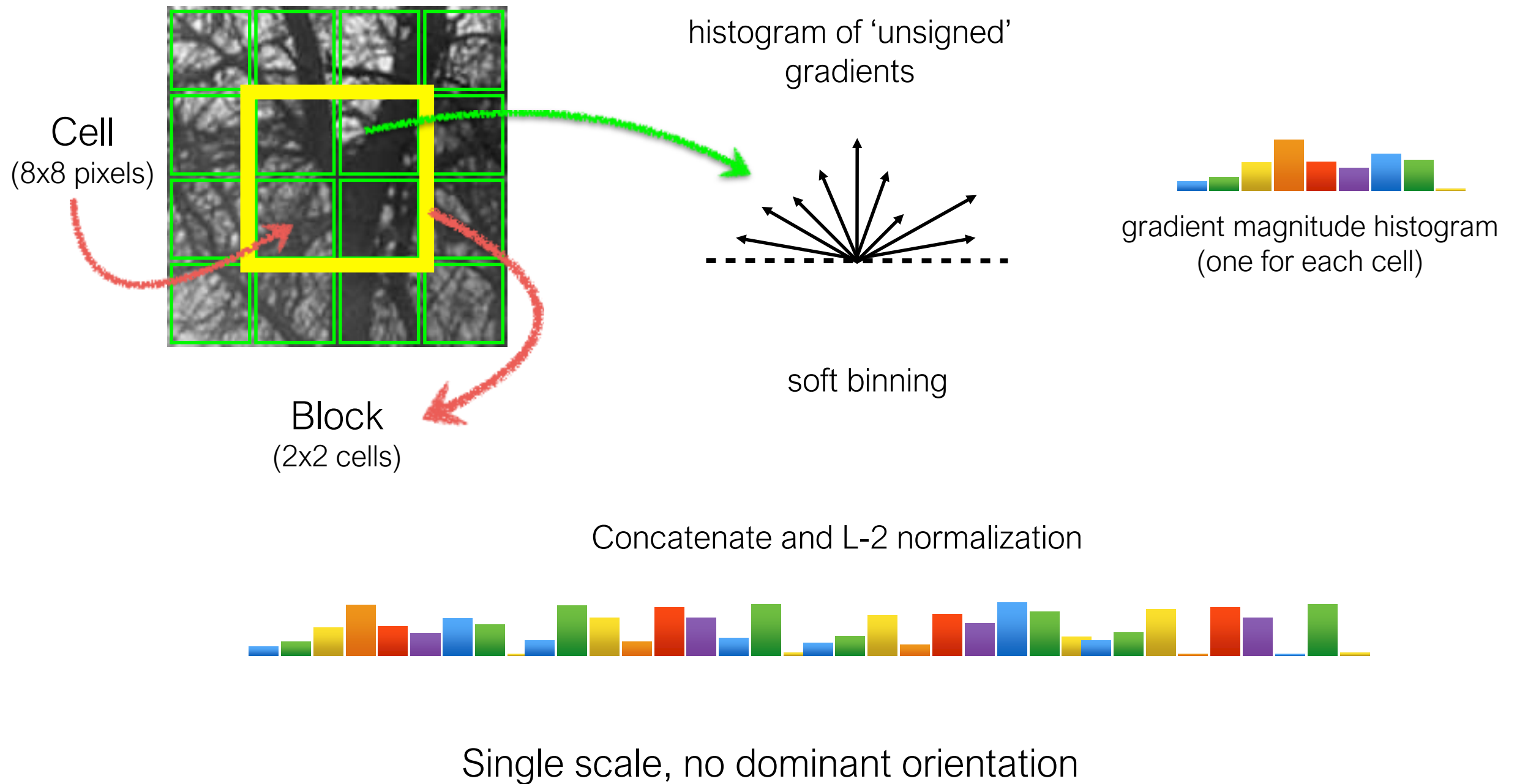
Julesz, 1981; Cula & Dana, 2001; Leung & Malik 2001; Mori, Belongie & Malik, 2001; Schmid 2001; Varma & Zisserman, 2002, 2003; Lazebnik, Schmid & Ponce, 2003

HOG descriptor

# HOG



Dalal, Triggs. **Histograms of Oriented Gradients** for Human Detection. CVPR, 2005





# Pedestrian detection

1 cell step size

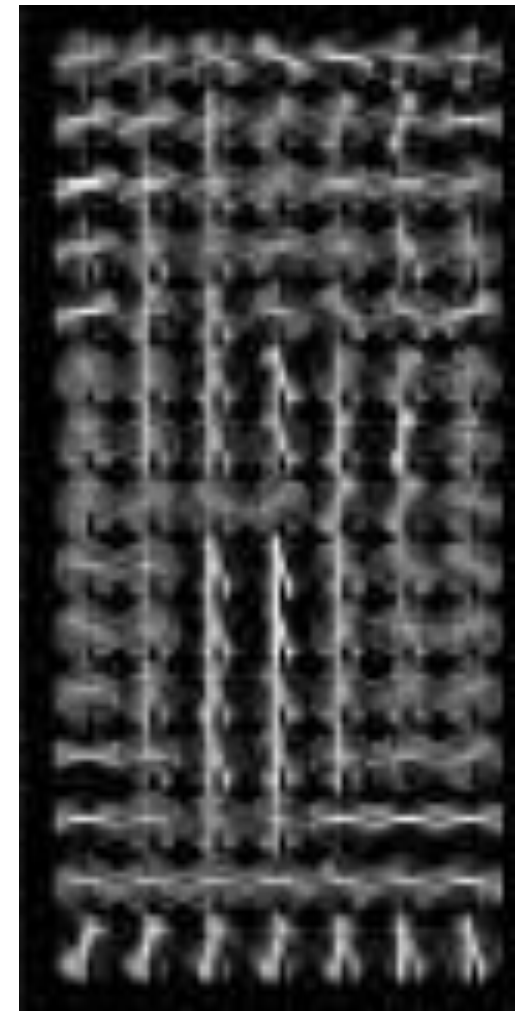


128 pixels  
16 cells  
15 blocks



$$15 \times 7 \times 4 \times 36 = 3780$$

visualization



64 pixels  
8 cells  
7 blocks

Redundant representation due to overlapping blocks

*How many times is each inner cell encoded?*



SIFT



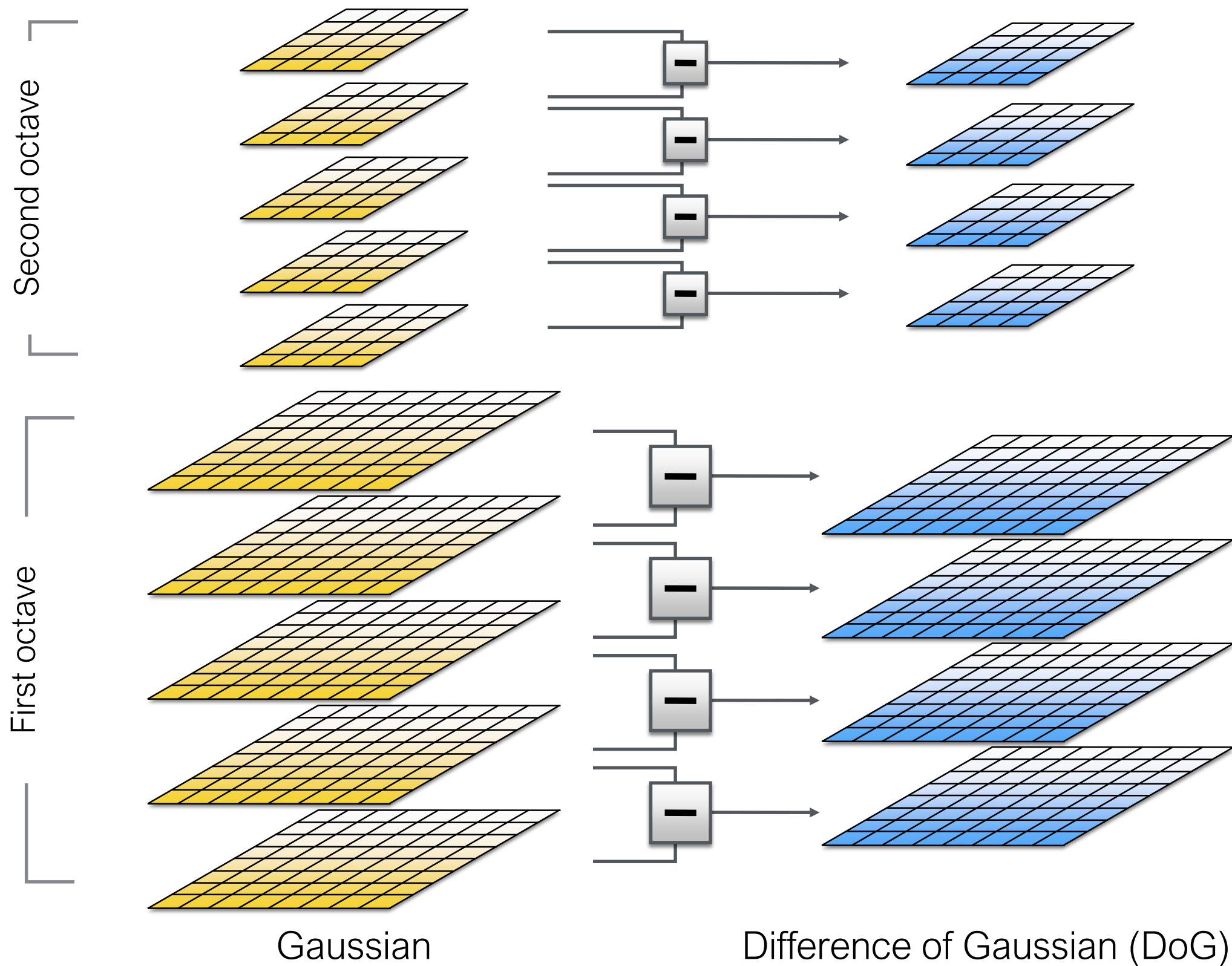
# SIFT

(Scale Invariant Feature Transform)

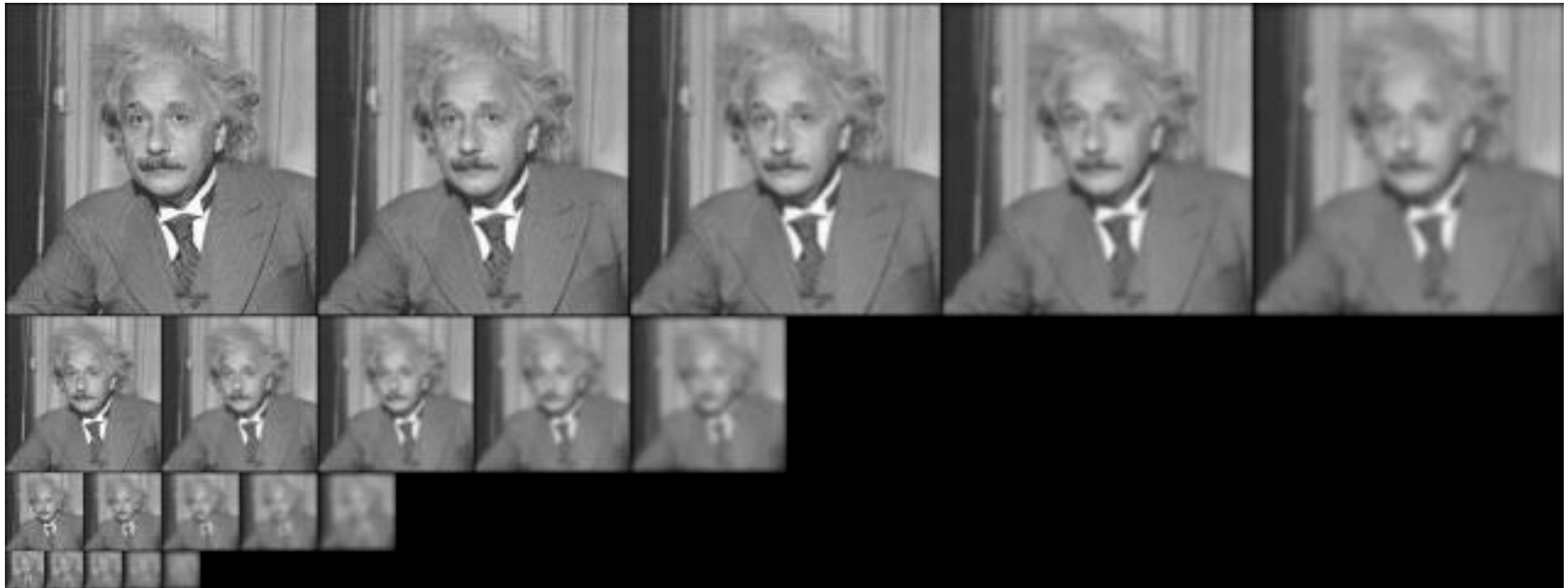
SIFT describes both a **detector** and **descriptor**

1. Multi-scale extrema detection
2. Keypoint localization
3. Orientation assignment
4. Keypoint descriptor

# 1. Multi-scale extrema detection





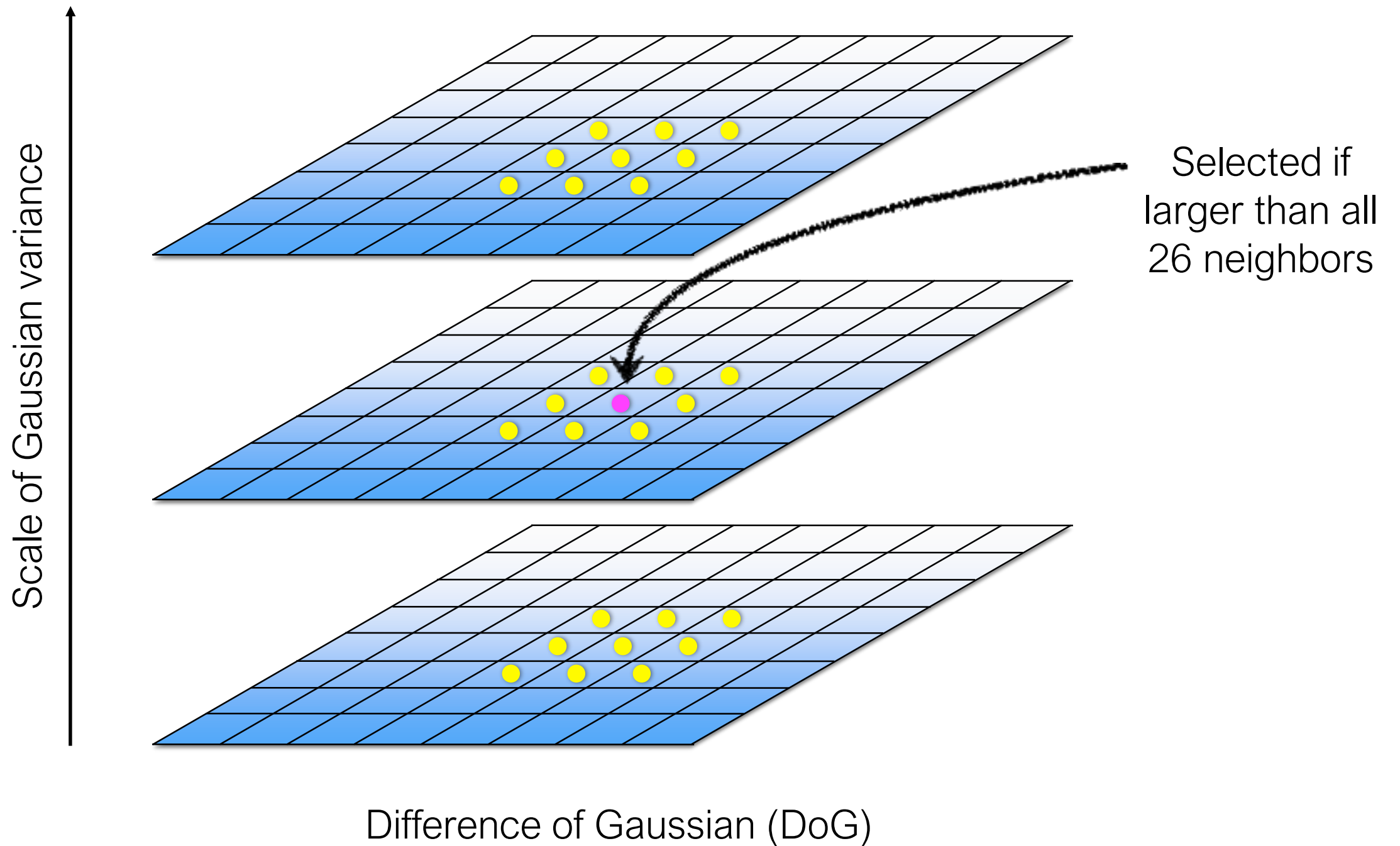


Gaussian



Laplacian

# Scale-space extrema



# 2. Keypoint localization

2nd order Taylor series approximation of DoG scale-space

$$f(\mathbf{x}) = f + \frac{\partial f^T}{\partial \mathbf{x}} \mathbf{x} + \frac{1}{2} \mathbf{x}^T \frac{\partial^2 f}{\partial \mathbf{x}^2} \mathbf{x}$$

$$\mathbf{x} = \{x, y, \sigma\}$$

Take the derivative and solve for extrema

$$\mathbf{x}_m = - \frac{\partial^2 f^{-1}}{\partial \mathbf{x}^2} \frac{\partial f}{\partial \mathbf{x}}$$

Additional tests to retain only strong features

# 3. Orientation assignment

For a keypoint, **L** is the **Gaussian-smoothed** image with the closest scale,

$$m(x, y) = \sqrt{\underbrace{(L(x+1, y) - L(x-1, y))^2}_{\text{x-derivative}} + \underbrace{(L(x, y+1) - L(x, y-1))^2}_{\text{y-derivative}}}$$

$$\theta(x, y) = \tan^{-1}((L(x, y+1) - L(x, y-1)) / (L(x+1, y) - L(x-1, y)))$$

Detection process returns

$$\{x, y, \sigma, \theta\}$$

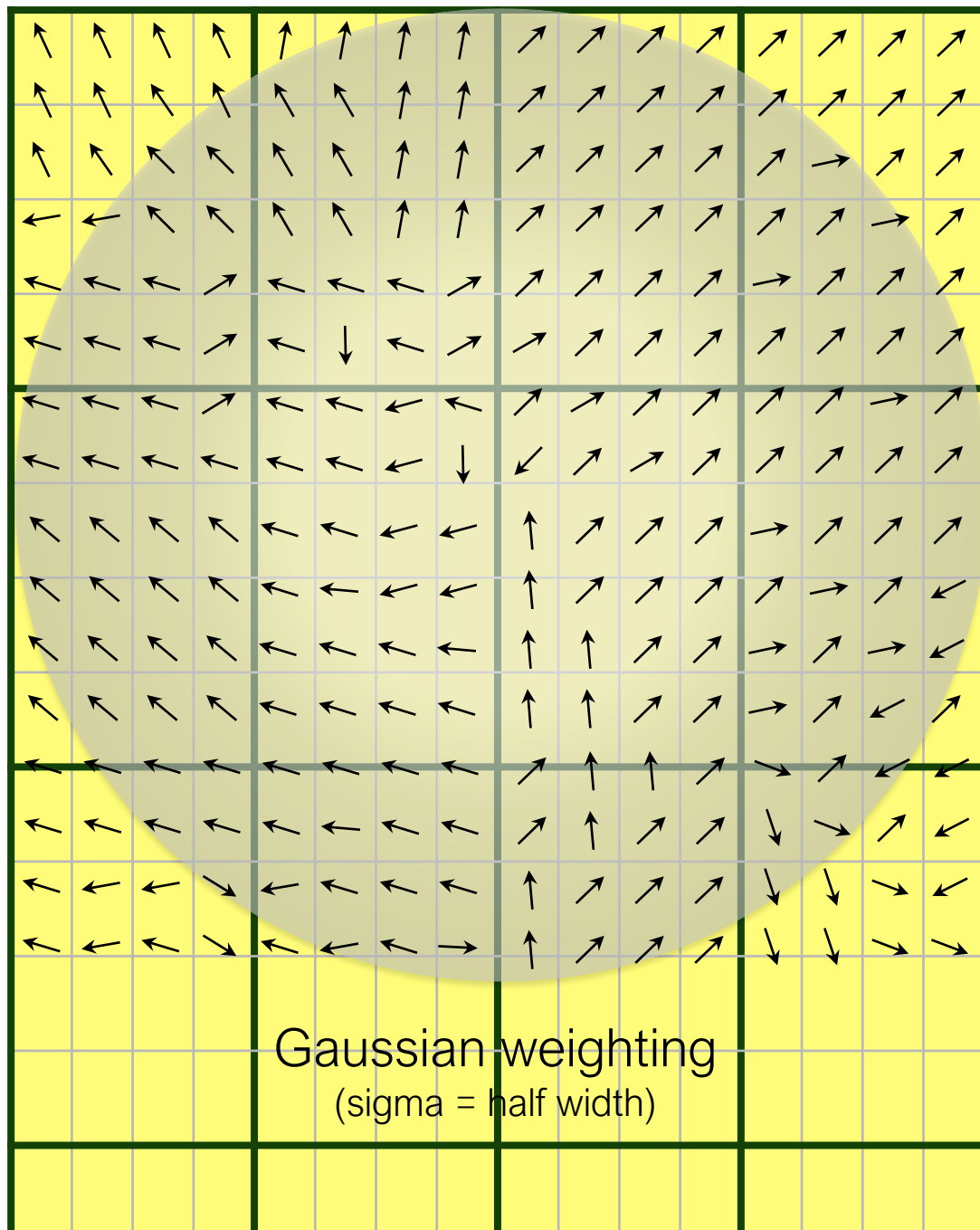
location    scale    orientation



# 4. Keypoint descriptor

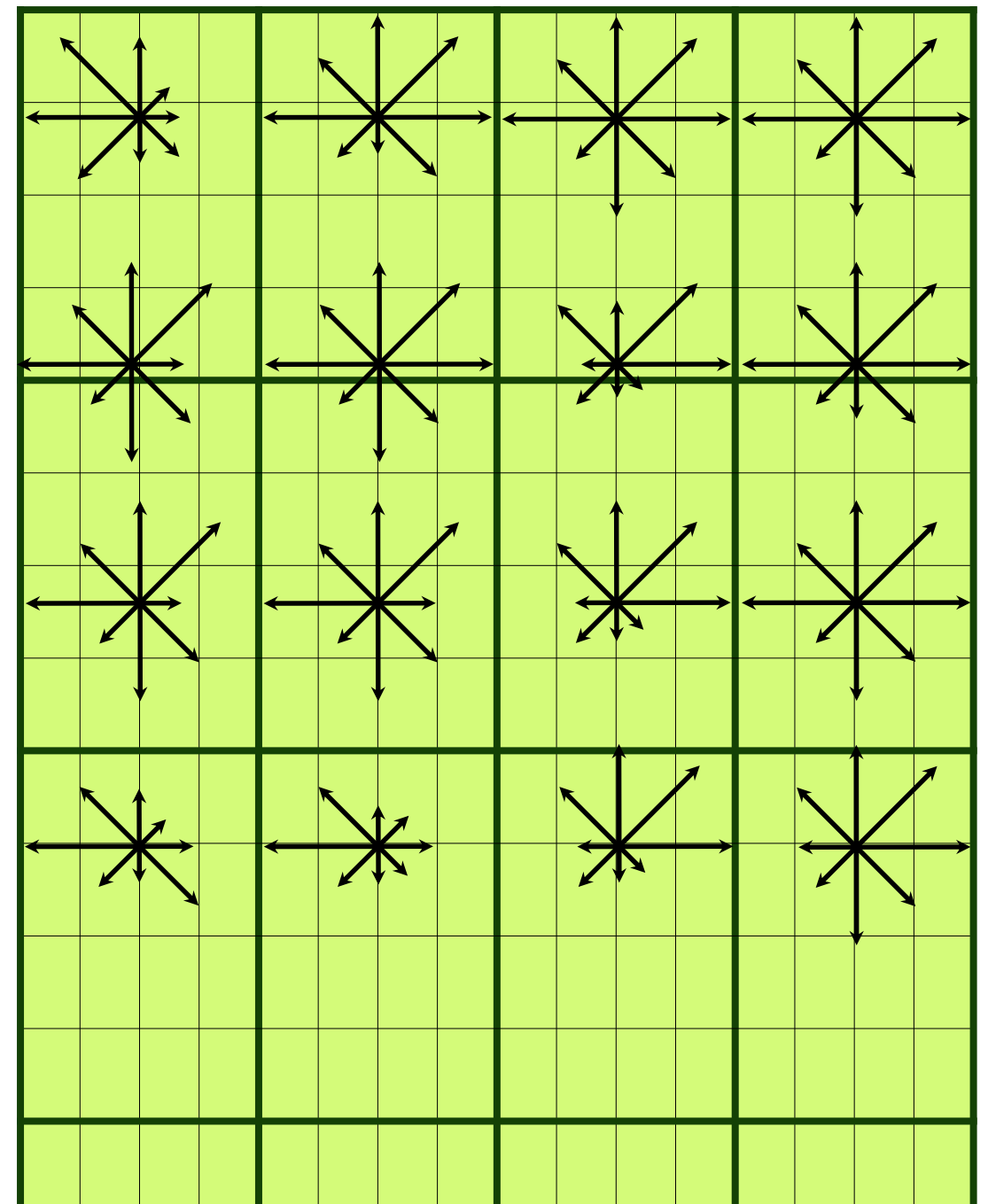
## Image Gradients

(4 x 4 pixel per cell, 4 x 4 cells)

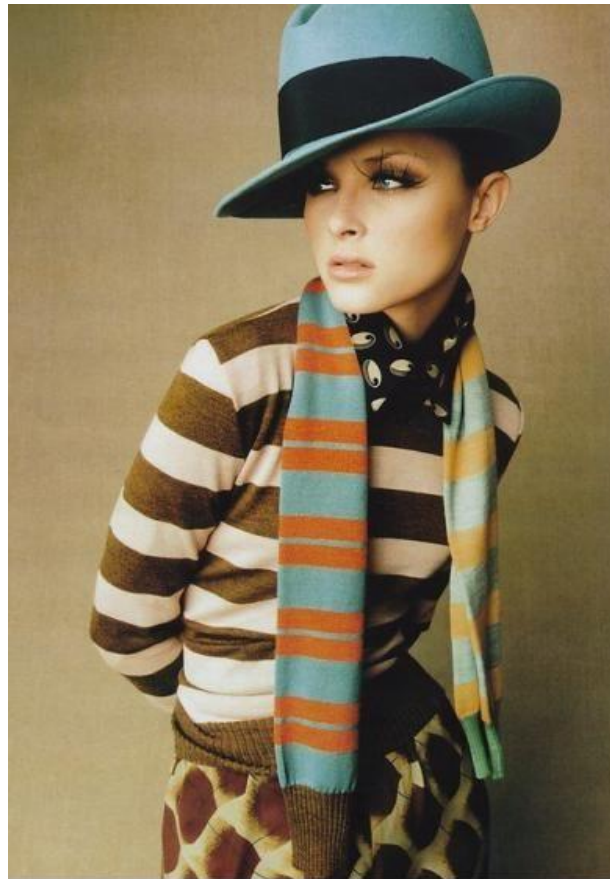


## SIFT descriptor

(16 cells x 8 directions = 128 dims)



# Discriminative power



Raw pixels



Sampled



Locally orderless



Global histogram

# Generalization power



# References

Basic reading:

- Szeliski textbook, Sections 4.1.2, 14.1.2.