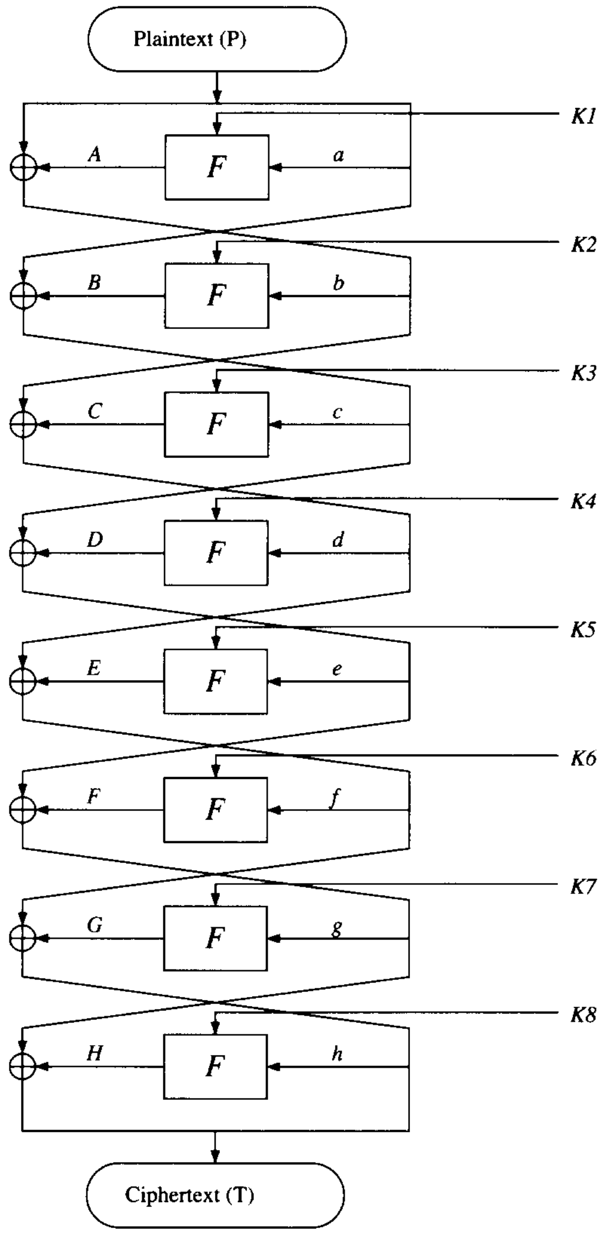
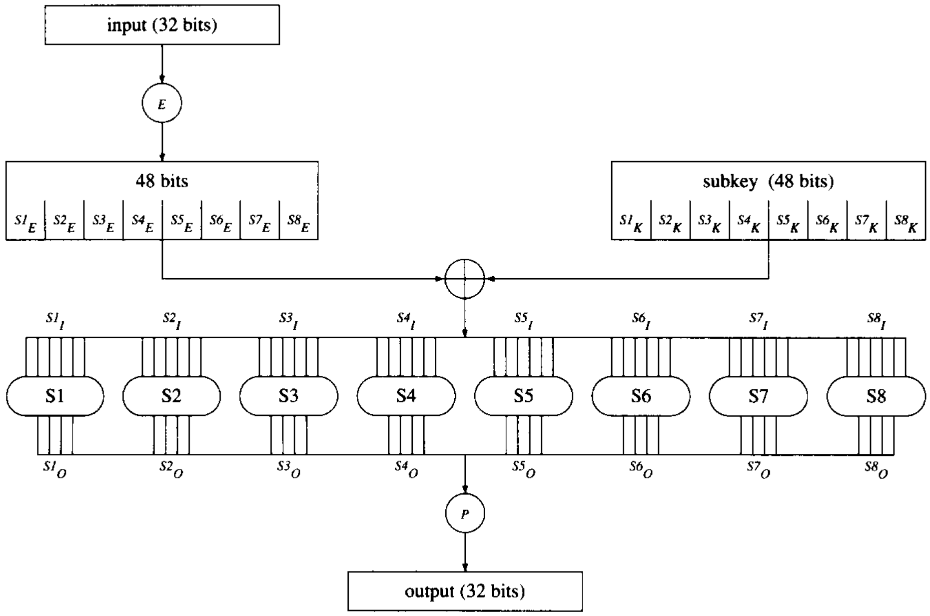
DES reduced to eight rounds



F function of DES



S1 Table

14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
0	14	7	4	14	2	13	1	10	6	12	11	9	5	3	8
4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13

The Difference Distribution Table (S1)

Input	Output XOR															
XOR	0_x	1_x	2_x	3_x	4_x	5_x	6_x	7_x	8_x	9_x	A_x	B_x	C_x	D_x	E_x	F_x
0_x	64	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1_x	0	0	0	6	0	2	4	4	0	10	12	4	10	6	2	4
2_x	0	0	0	8	0	4	4	4	0	6	8	6	12	6	4	2
3_x	14	4	2	2	10	6	4	2	6	4	4	0	2	2	2	0
4_x	0	0	0	6	0	10	10	6	0	4	6	4	2	8	6	2
5_x	4	8	6	2	2	4	4	2	0	4	4	0	12	2	4	6
6_x	0	4	2	4	8	2	6	2	8	4	4	2	4	2	0	12
7_x	2	4	10	4	0	4	8	4	2	4	8	2	2	2	4	4
8_x	0	0	0	12	0	8	8	4	0	6	2	8	8	2	2	4
9_x	10	2	4	0	2	4	6	0	2	2	8	0	10	0	2	12
A_x	0	8	6	2	2	8	6	0	6	4	6	0	4	0	2	10
B_x	2	4	0	10	2	2	4	0	2	6	2	6	6	4	2	12
C_x	0	0	0	8	0	6	6	0	0	6	6	4	6	6	14	2
D_x	6	6	4	8	4	8	2	6	0	6	4	6	0	2	0	2
E_x	0	4	8	8	6	6	4	0	6	6	4	0	0	4	0	8
F_x	2	0	2	4	4	6	4	2	4	8	2	2	2	6	8	8
10_x	0	0	0	0	0	0	2	14	0	6	6	12	4	6	8	6
11_x	6	8	2	4	6	4	8	6	4	0	6	6	0	4	0	0
12_x	0	8	4	2	6	6	4	6	6	4	2	6	6	0	4	0
13_x	2	4	4	6	2	0	4	6	2	0	6	8	4	6	4	6
14_x	0	8	8	0	10	0	4	2	8	2	2	4	4	8	4	0
15_x	0	4	6	4	2	2	4	10	6	2	0	10	0	4	6	4
16_x	0	8	10	8	0	2	2	6	10	2	0	2	0	6	2	6
17_x	4	4	6	0	10	6	0	2	4	4	4	6	6	6	2	0
18_x	0	6	6	0	8	4	2	2	2	4	6	8	6	6	2	2
19_x	2	6	2	4	0	8	4	6	10	4	0	4	2	8	4	0
$1A_x$	0	6	4	0	4	6	6	6	6	2	2	0	4	4	6	8
$1B_x$	4	4	2	4	10	6	6	4	6	2	2	4	2	2	4	2
$1C_x$	0	10	10	6	6	0	0	12	6	4	0	0	2	4	4	0
$1D_x$	4	2	4	0	8	0	0	2	10	0	2	6	6	6	14	0
$1E_x$	0	2	6	0	14	2	0	0	6	4	10	8	2	2	6	2
$1F_x$	2	4	10	6	2	2	2	8	6	8	0	0	0	4	6	4
20_x	0	0	0	10	0	12	8	2	0	6	4	4	4	2	0	12
21_x	0	4	2	4	4	8	10	0	4	4	10	0	4	0	2	8
22_x	10	4	6	2	2	8	2	2	2	2	6	0	4	0	4	10
23_x	0	4	4	8	0	2	6	0	6	6	2	10	2	4	0	10
24_x	12	0	0	2	2	2	2	0	14	14	2	0	2	6	2	4
25_x	6	4	4	12	4	4	4	10	2	2	2	0	4	2	2	2
26_x	0	0	4	10	10	10	2	4	0	4	6	4	4	4	2	0
27_x	10	4	2	0	2	4	2	0	4	8	0	4	8	8	4	4
28_x	12	2	2	8	2	6	12	0	0	2	6	0	4	0	6	2
29_x	4	2	2	10	0	2	4	0	0	14	10	2	4	6	0	4
$2A_x$	4	2	4	6	0	2	8	2	2	14	2	6	2	6	2	2
$2B_x$	12	2	2	2	4	6	6	2	0	2	6	2	6	0	8	4
$2C_x$	4	2	2	4	0	2	10	4	2	2	4	8	8	4	2	6
$2D_x$	6	2	6	2	8	4	4	4	2	4	6	0	8	2	0	6
$2E_x$	6	6	2	2	0	2	4	6	4	0	6	2	12	2	6	4
$2F_x$	2	2	2	2	2	6	8	8	2	4	4	6	8	2	4	2
30_x	0	4	6	0	12	6	2	2	8	2	4	4	6	2	2	4
31_x	4	8	2	10	2	2	2	2	6	0	0	2	2	4	10	8
32_x	4	2	6	4	4	2	2	4	6	6	4	8	2	2	8	0
33_x	4	4	6	2	10	8	4	2	4	0	2	2	4	6	2	4
34_x	0	8	16	6	2	0	0	12	6	0	0	0	0	8	0	6
35_x	2	2	4	0	8	0	0	0	14	4	6	8	0	2	14	0
36_x	2	6	2	2	8	0	2	2	4	2	6	8	6	4	10	0
37_x	2	2	12	4	2	4	4	10	4	4	2	6	0	2	2	4
38_x	0	6	2	2	2	0	2	2	4	6	4	4	4	6	10	10
39_x	6	2	2	4	12	6	4	8	4	0	2	4	2	4	4	0
$3A_x$	6	4	6	4	6	8	0	6	2	2	6	2	2	6	4	0
$3B_x$	2	6	4	0	0	2	4	6	4	6	8	6	4	4	6	2
$3C_x$	0	10	4	0	12	0	4	2	6	0	4	12	4	4	2	0
$3D_x$	0	8	6	2	2	6	0	8	4	4	0	4	0	12	4	4
$3E_x$	4	8	2	2	2	4	4	14	4	2	0	2	0	8	4	4
$3F_x$	4	8	4	2	4	0	2	4	4	2	4	8	8	6	2	2

Example Consider entry $34_x \rightarrow 4_x$ in the difference distribution table S1. These inputs must be 13_x and 27_x, whose corresponding outputs are 6_x and 2_x respectively.

Possible input value for $S1'_I = 34_x$ by the output XOR

Output XOR ($S1'_O$)	Possible input in hex ($S1_I$)
1	03, 0F, 1E, 1F, 2A, 2B, 37, 3B
2	04, 05, 0E, 11, 12, 14, 1A, 1B, 20, 25, 26, 2E, 2F, 30, 31, 3A
3	01, 02, 15, 21, 35, 36
4	13, 27
7	00, 08, 0D, 17, 18, 1D, 23, 29, 2C, 34, 39, 3C
8	09, 0C, 19, 2D, 38, 3D
D	06, 10, 16, 1C, 22, 24, 28, 32
F	07, 0A, 0B, 33, 3E, 3F

Assume we know that $S1_E = 1_x$, $S1^*_E = 35_x$, and $S1'_O = D_x$ and we want to find the key value $S1_K$. The input to the S box has eight possibilities, making eight possibilites for the key (since $S_K = S_E \oplus S_I$).

Possible keys for $34_x \rightarrow D_x$ by S1 with input 1_x, 35_x (in hexadecimal)

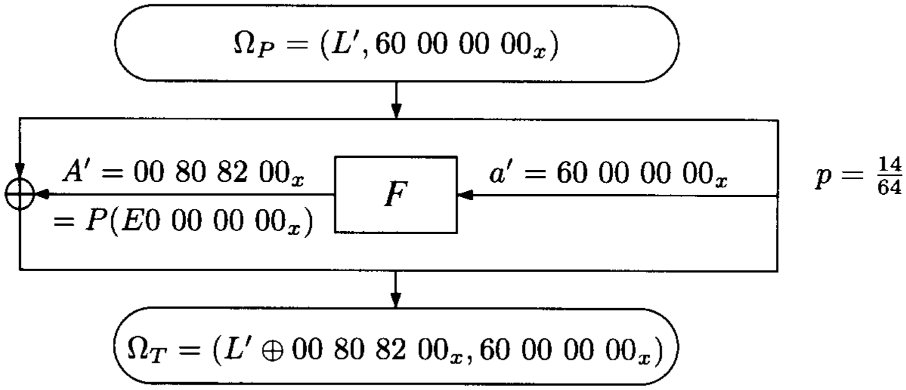
S box input	Possible keys
06, 32	07, 33
10, 24	11, 25
16, 22	17, 23
1C, 28	1D, 29

Assume further pair $S1_E = 21_x$, $S1^*_E = 15_x$ ($S1'_O = 3_x$). Right key must occur in both tables (17_x and 23_x).

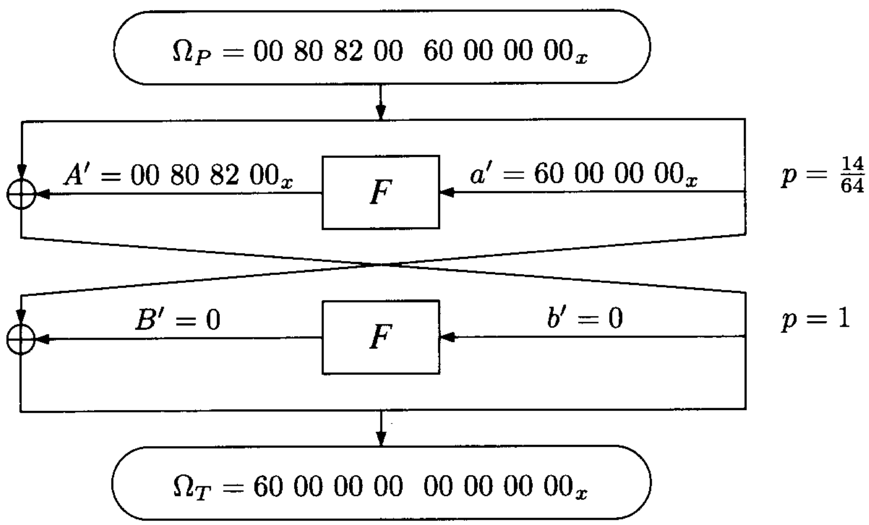
Possible keys for $34_x \rightarrow 3_x$ by S1 with input 21_x, 15_x

S box input	Possible keys
01, 35	20, 14
02, 36	23, 17
15, 21	34, 00

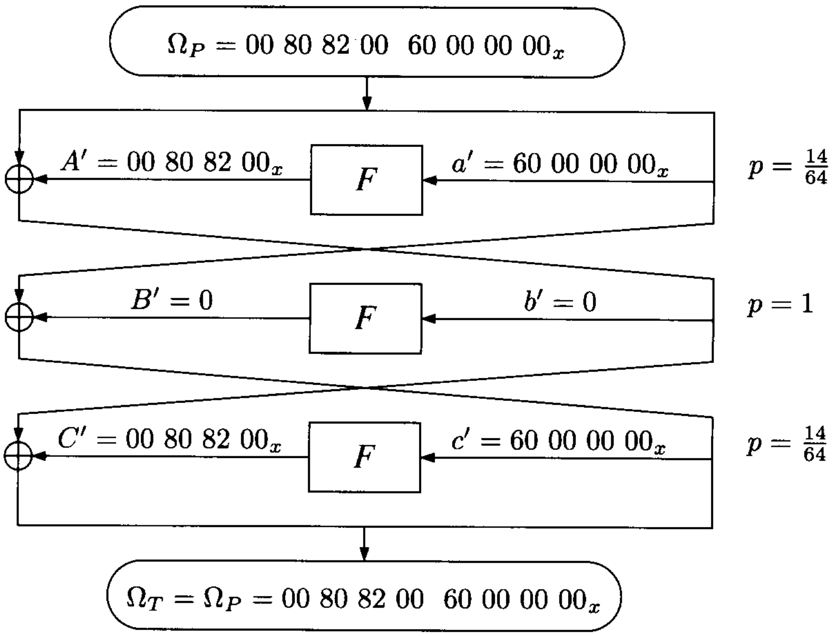
Simple characteristic example



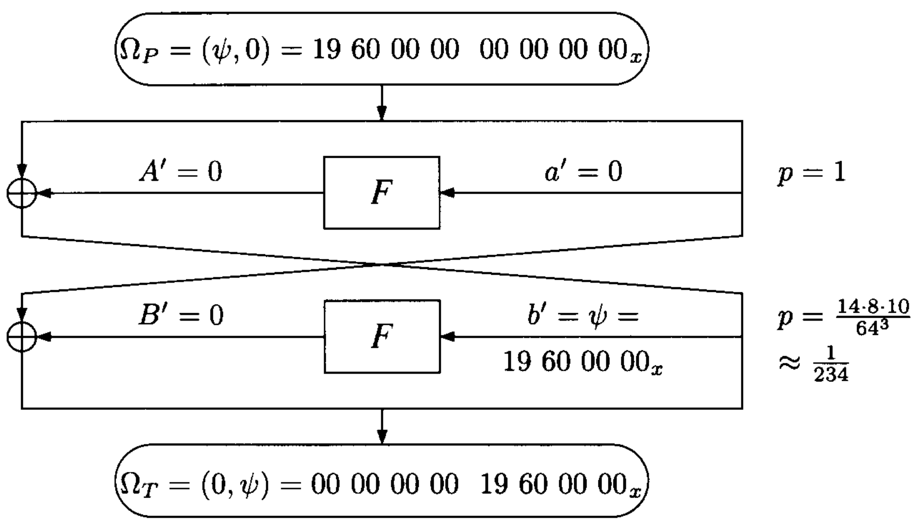
Characteristic concatenation



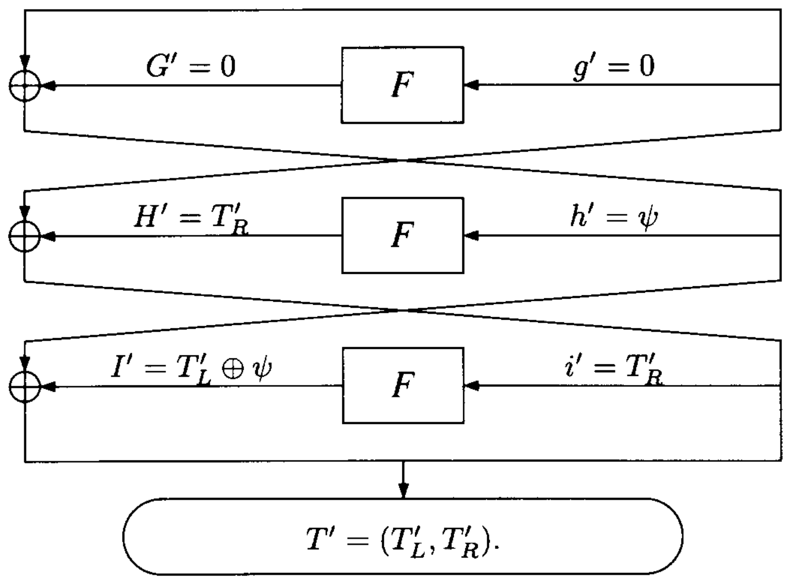
Three round characteristic



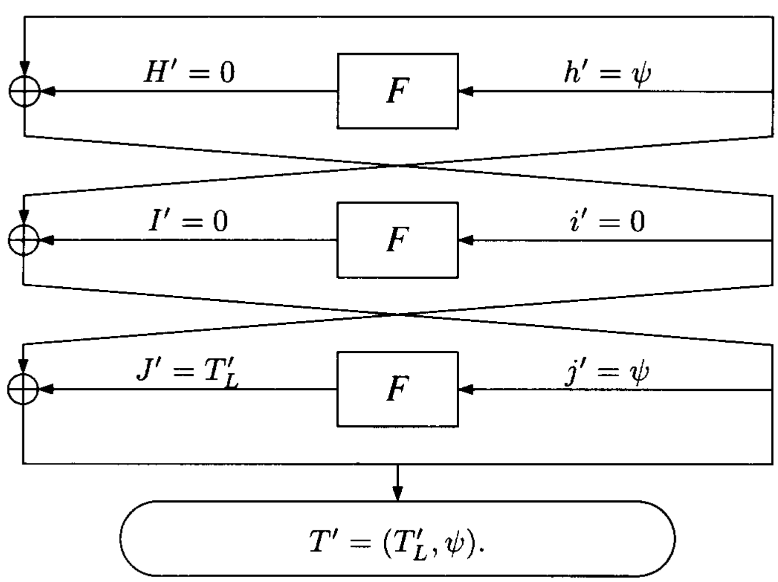
Iterative Characteristic



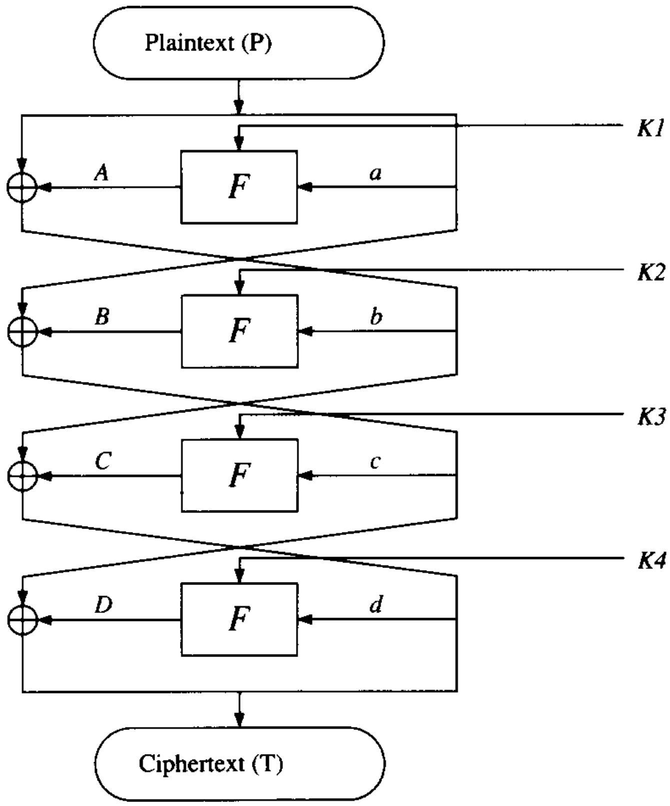
2R-Attack



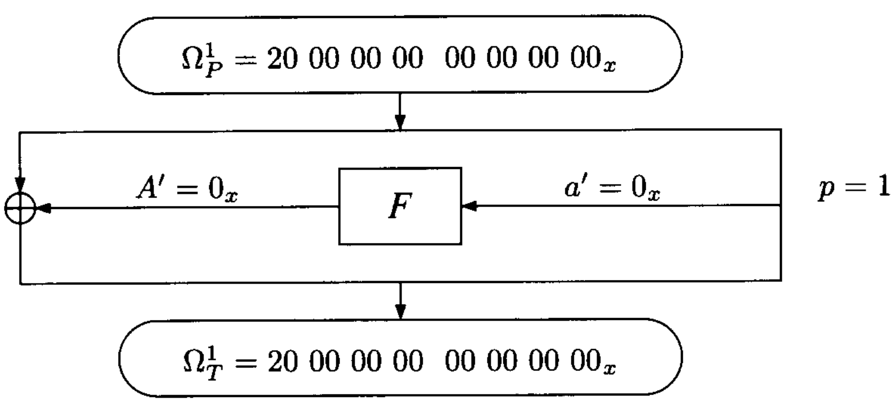
1R-Attack



DES reduced to four round



Characteristic used in four-round-DES



D' = a' ⊕ B' ⊕ T'L

S_{1Ed}, S_{2Ed} and S'_{Od} for seven S boxes is known

Try 64 possible SKd and check :

$S(S_{1Ed} \oplus S_{Kd}) \oplus S(S_{2Ed} \oplus S_{Kd}) = S'_{Od}$