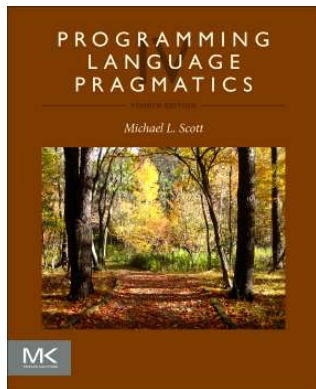


Bottom-Up LR Parsing

17-363/17-663: Programming Language Pragmatics



Reading: PLP section 2.3

Top-Down vs. Bottom-Up Parsing

- Top-Down/LL Parsing Intuition

program

Start trying to parse a program

stmt_list \$\$\$

Based on lookahead, refine to *stmt_list*
then to *stmt stmt_list*

stmt stmt_list \$\$\$

Stack tracks predicted future parsing

...

- Bottom-Up/LR Parsing Intuition

read A

Start by shifting a few tokens

stmt

Reduce tokens to a *stmt*, then to a *stmt_list*

stmt_list

Continue to shift and reduce tokens
tokens to recognize another *stmt*

stmt_list read B

stmt_list stmt

Stack shows what constructs
have been recognized so far

Example Program and SLR(1) Grammar

```
read A
read B
sum := A + B
write sum
write sum / 2
```

1. $program \rightarrow stmt_list \ \$\$$
2. $stmt_list \rightarrow stmt_list \ stmt$
3. $stmt_list \rightarrow stmt$
4. $stmt \rightarrow id \ := \ expr$
5. $stmt \rightarrow read \ id$
6. $stmt \rightarrow write \ expr$
7. $expr \rightarrow term$
8. $expr \rightarrow expr \ add_op \ term$
9. $term \rightarrow factor$
10. $term \rightarrow term \ mult_op \ factor$
11. $factor \rightarrow (\ expr \)$
12. $factor \rightarrow id$
13. $factor \rightarrow number$
14. $add_op \rightarrow +$
15. $add_op \rightarrow -$
16. $mult_op \rightarrow *$
17. $mult_op \rightarrow /$

Modeling a Parse with LR Items

- Initial parse state captured by an *item*

$program \longrightarrow \bullet \text{ stmt_list } \$\$$

- includes start symbol, production, and current location

- What we see next might be inside *stmt_list*

- So we expand *stmt_list* and add more items to the set:

$program \longrightarrow \bullet \text{ stmt_list } \$\$$

$\text{stmt_list} \longrightarrow \bullet \text{ stmt_list } \text{stmt}$

$\text{stmt_list} \longrightarrow \bullet \text{ stmt}$

Modeling a Parse with LR Items

- We can likewise expand *stmt* to get the item set:

program \longrightarrow \bullet *stmt_list* $\$ \$$

stmt_list \longrightarrow \bullet *stmt_list* *stmt*

stmt_list \longrightarrow \bullet *stmt*

stmt \longrightarrow \bullet *id* *:=* *expr*

stmt \longrightarrow \bullet *read* *id*

stmt \longrightarrow \bullet *write* *expr*

- This is an SLR parser *state*
 - We'll call it state 0

Modeling a Parse with LR Items

- Our starting stack has state 0 on it:

0

- Input: read A read B ...

```
program → • stmt_list $$  
stmt_list → • stmt_list stmt  
stmt_list → • stmt  
stmt → • id := expr  
stmt → • read id  
stmt → • write expr
```

- From state 0, we *shift* read onto the stack and move to state 1:

0 read 1

- State 1 represents the following item:

```
stmt → read • id
```

Modeling a Parse with LR Items

- stack / item: 0 read 1 *stmt* \longrightarrow read • id
- input: A read B ...

- From state 1, we shift *id* onto the stack
- stack / item: 0 read 1 id 1' *stmt* \longrightarrow read id •
- input: read B ...

- Now we reduce to *stmt*, and put *stmt* into the input
- stack / item: 0 *program* \longrightarrow • *stmt_list* \$\$
- input: *stmt* read B ... *stmt_list* \longrightarrow • *stmt_list* *stmt*
- *stmt_list* \longrightarrow • *stmt*
- *stmt* \longrightarrow • id := *expr*
- *stmt* \longrightarrow • read id

Modeling a Parse with LR Items

- stack / item: 0
- input: *stmt* read B ...

- We now shift *stmt*
- stack / item: 0 *stmt* 0'
- input: read B ...

- Next we reduce to *stmt_list*
- stack / item: 0
- input: *stmt_list* read B ...

program \longrightarrow • *stmt_list* \$\$
stmt_list \longrightarrow • *stmt_list* *stmt*
stmt_list \longrightarrow • *stmt*
stmt \longrightarrow • *id* := *expr*
stmt \longrightarrow • read *id*
stmt \longrightarrow • write *expr*

stmt_list \longrightarrow *stmt* •

program \longrightarrow • *stmt_list* \$\$
stmt_list \longrightarrow • *stmt_list* *stmt*
stmt_list \longrightarrow • *stmt*
stmt \longrightarrow • *id* := *expr*
stmt \longrightarrow • read *id*
stmt \longrightarrow • write *expr*

Modeling a Parse with LR Items

- stack / item: 0
- input: *stmt_list* read B ...

```
program → • stmt_list $$
stmt_list → • stmt_list stmt
stmt_list → • stmt
stmt → • id := expr
stmt → • read id
stmt → • write expr
```

- Now we shift *stmt_list*
- stack / item: 0 *stmt_list* 2
- input: read B ...

```
program → stmt_list • $$
stmt_list → stmt_list • stmt
stmt → • id := expr
stmt → • read id
stmt → • write expr
```

The Characteristic Finite State Machine (CFSM)

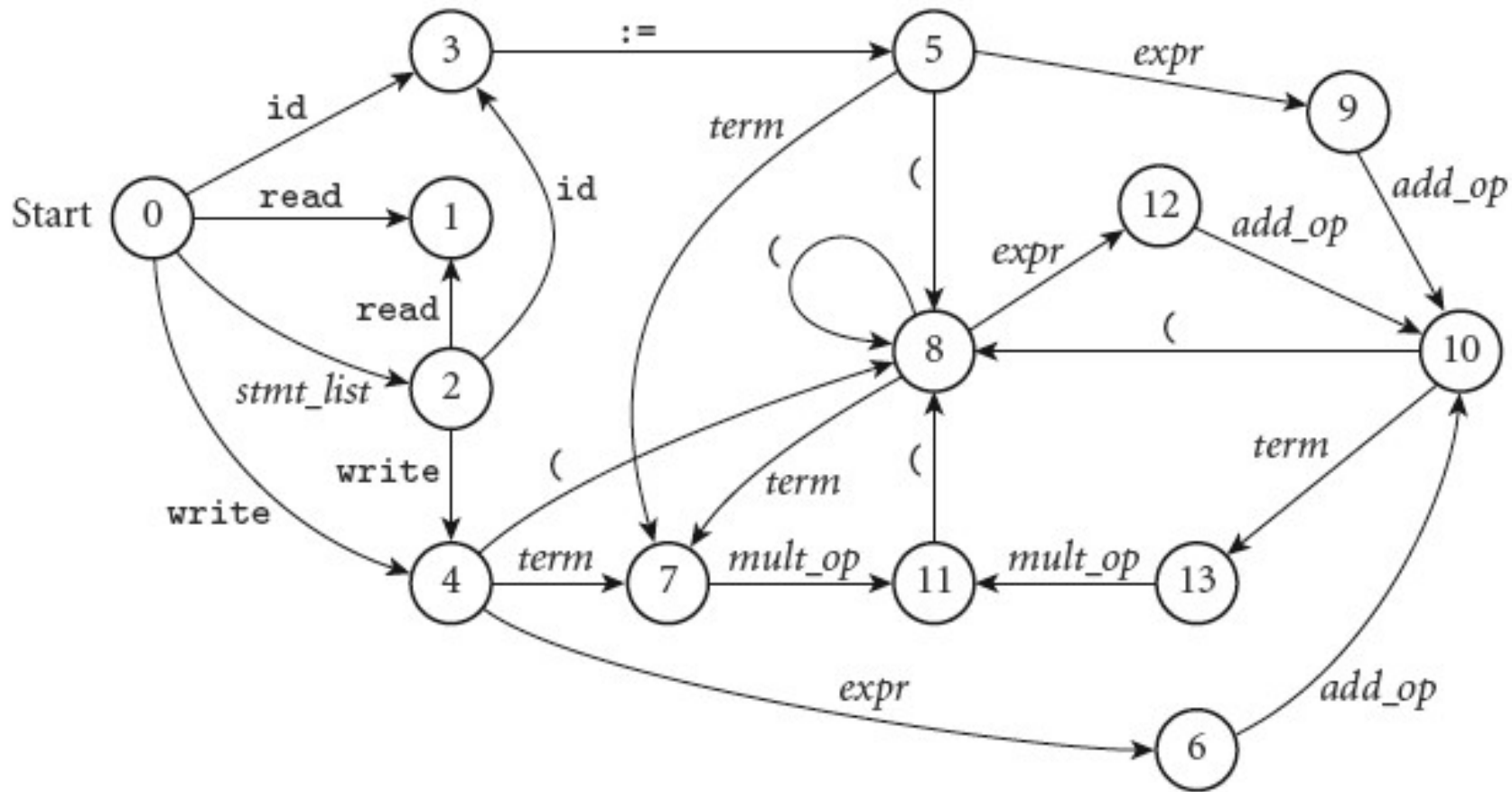


Figure 2.27 Pictorial representation of the CFSM of Figure 2.26. Reduce actions are not shown.

There are also shift-reduce actions. So our states 0', 1' aren't shown here: they are "in between" states within a shift-reduce action

The CFSM as a Table

Top-of-stack state	Current input symbol																			
	<i>sl</i>	<i>s</i>	<i>e</i>	<i>t</i>	<i>f</i>	<i>ao</i>	<i>mo</i>	<i>id</i>	<i>lit</i>	<i>r</i>	<i>w</i>	<i>:=</i>	<i>(</i>	<i>)</i>	<i>+</i>	<i>-</i>	<i>*</i>	<i>/</i>	<i>\$\$</i>	
0	s2	b3	-	-	-	-	-	s3	-	s1	s4	-	-	-	-	-	-	-	-	-
1	-	-	-	-	-	-	-	b5	-	-	-	-	-	-	-	-	-	-	-	-
2	-	b2	-	-	-	-	-	s3	-	s1	s4	-	-	-	-	-	-	-	-	b1
3	-	-	-	-	-	-	-	-	-	-	-	s5	-	-	-	-	-	-	-	-
4	-	-	s6	s7	b9	-	-	b12	b13	-	-	-	s8	-	-	-	-	-	-	-
5	-	-	s9	s7	b9	-	-	b12	b13	-	-	-	s8	-	-	-	-	-	-	-
6	-	-	-	-	-	s10	-	r6	-	r6	r6	-	-	-	b14	b15	-	-	-	r6
7	-	-	-	-	-	-	s11	r7	-	r7	r7	-	-	r7	r7	r7	b16	b17	r7	-
8	-	-	s12	s7	b9	-	-	b12	b13	-	-	-	s8	-	-	-	-	-	-	-
9	-	-	-	-	-	s10	-	r4	-	r4	r4	-	-	-	b14	b15	-	-	-	r4
10	-	-	-	s13	b9	-	-	b12	b13	-	-	-	s8	-	-	-	-	-	-	-
11	-	-	-	-	b10	-	-	b12	b13	-	-	-	s8	-	-	-	-	-	-	-
12	-	-	-	-	-	s10	-	-	-	-	-	-	-	b11	b14	b15	-	-	-	-
13	-	-	-	-	-	-	s11	r8	-	r8	r8	-	-	r8	r8	r8	b16	b17	r8	-

Figure 2.28 SLR(1) parse table for the calculator language. Table entries indicate whether to shift (*s*), reduce (*r*), or shift and then reduce (*b*). The accompanying number is the new state when shifting, or the production that has been recognized when (shifting and) reducing. Production numbers are given in Figure 2.25. Symbol names have been abbreviated for the sake of formatting. A dash indicates an error. An auxiliary table, not shown here, gives the left-hand-side symbol and right-hand-side length for each production.

A Detailed Explanation of the CFMSM

State	Transitions
0. <u>$program \rightarrow \cdot stmt_list \ \#\#$</u> $stmt_list \rightarrow \cdot stmt_list \ stmt$ $stmt_list \rightarrow \cdot stmt$ $stmt \rightarrow \cdot id \ := \ expr$ $stmt \rightarrow \cdot read \ id$ $stmt \rightarrow \cdot write \ expr$	on $stmt_list$ shift and goto 2 on $stmt$ shift and reduce (pop 1 state, push $stmt_list$ on input) on id shift and goto 3 on $read$ shift and goto 1 on $write$ shift and goto 4
1. $stmt \rightarrow read \ \cdot id$	on id shift and reduce (pop 2 states, push $stmt$ on input)
2. <u>$program \rightarrow stmt_list \ \cdot \#\#$</u> <u>$stmt_list \rightarrow stmt_list \ \cdot \ stmt$</u> $stmt \rightarrow \cdot id \ := \ expr$ $stmt \rightarrow \cdot read \ id$ $stmt \rightarrow \cdot write \ expr$	on $\#\#$ shift and reduce (pop 2 states, push $program$ on input) on $stmt$ shift and reduce (pop 2 states, push $stmt_list$ on input) on id shift and goto 3 on $read$ shift and goto 1 on $write$ shift and goto 4
3. $stmt \rightarrow id \ \cdot \ := \ expr$	on $:=$ shift and goto 5
4. <u>$stmt \rightarrow write \ \cdot \ expr$</u> $expr \rightarrow \cdot term$ $expr \rightarrow \cdot expr \ add_op \ term$ $term \rightarrow \cdot factor$	on $expr$ shift and goto 6 on $term$ shift and goto 7 on $factor$ shift and reduce (pop 1 state, push $term$ on input)

A Detailed Explanation of the CFMSM

State	Transitions
0. $\text{program} \rightarrow \cdot \text{stmt_list} \ \#\#$ <hr/> $\text{stmt_list} \rightarrow \cdot \text{stmt_list} \ \text{stmt}$ $\text{stmt_list} \rightarrow \cdot \text{stmt}$ $\text{stmt} \rightarrow \cdot \text{id} \text{ :- expr}$ $\text{stmt} \rightarrow \cdot \text{read} \ \text{id}$ $\text{stmt} \rightarrow \cdot \text{write} \ \text{expr}$	on <i>stmt_list</i> shift and goto 2 on <i>stmt</i> shift and reduce (pop 1 state, push <i>stmt_list</i> on input) on <i>id</i> shift and goto 3 on <i>read</i> shift and goto 1 on <i>write</i> shift and goto 4
1. $\text{stmt} \rightarrow \text{read} \cdot \ \text{id}$	on <i>id</i> shift and reduce (pop 2 states, push <i>stmt</i> on input)
2. $\text{program} \rightarrow \text{stmt_list} \cdot \ \#\#$ <hr/> $\text{stmt_list} \rightarrow \text{stmt_list} \cdot \ \text{stmt}$ <hr/> $\text{stmt} \rightarrow \cdot \text{id} \text{ :- expr}$ $\text{stmt} \rightarrow \cdot \text{read} \ \text{id}$ $\text{stmt} \rightarrow \cdot \text{write} \ \text{expr}$	on <i>##</i> shift and reduce (pop 2 states, push <i>program</i> on input) on <i>stmt</i> shift and reduce (pop 2 states, push <i>stmt_list</i> on input) on <i>id</i> shift and goto 3 on <i>read</i> shift and goto 1 on <i>write</i> shift and goto 4
3. $\text{stmt} \rightarrow \text{id} \cdot \ \text{ :- expr}$	on <i>:-</i> shift and goto 5
4. $\text{stmt} \rightarrow \text{write} \cdot \ \text{expr}$ <hr/> $\text{expr} \rightarrow \cdot \ \text{term}$ $\text{expr} \rightarrow \cdot \ \text{expr} \ \text{add_op} \ \text{term}$ $\text{term} \rightarrow \cdot \ \text{factor}$ $\text{term} \rightarrow \cdot \ \text{term} \ \text{mult_op} \ \text{factor}$ $\text{factor} \rightarrow \cdot \ (\ \ \text{expr} \)$ $\text{factor} \rightarrow \cdot \ \text{id}$ $\text{factor} \rightarrow \cdot \ \text{number}$	on <i>expr</i> shift and goto 6 on <i>term</i> shift and goto 7 on <i>factor</i> shift and reduce (pop 1 state, push <i>term</i> on input) on (shift and goto 8 on <i>id</i> shift and reduce (pop 1 state, push <i>factor</i> on input) on <i>number</i> shift and reduce (pop 1 state, push <i>factor</i> on input)
5. $\text{stmt} \rightarrow \text{id} \ \text{ :-} \cdot \ \text{expr}$ <hr/> $\text{expr} \rightarrow \cdot \ \text{term}$ $\text{expr} \rightarrow \cdot \ \text{expr} \ \text{add_op} \ \text{term}$ $\text{term} \rightarrow \cdot \ \text{factor}$ $\text{term} \rightarrow \cdot \ \text{term} \ \text{mult_op} \ \text{factor}$ $\text{factor} \rightarrow \cdot \ (\ \ \text{expr} \)$ $\text{factor} \rightarrow \cdot \ \text{id}$ $\text{factor} \rightarrow \cdot \ \text{number}$	on <i>expr</i> shift and goto 9 on <i>term</i> shift and goto 7 on <i>factor</i> shift and reduce (pop 1 state, push <i>term</i> on input) on (shift and goto 8 on <i>id</i> shift and reduce (pop 1 state, push <i>factor</i> on input) on <i>number</i> shift and reduce (pop 1 state, push <i>factor</i> on input)
6. $\text{stmt} \rightarrow \text{write} \ \text{expr} \cdot$ <hr/> $\text{expr} \rightarrow \text{expr} \cdot \ \text{add_op} \ \text{term}$ <hr/> $\text{add_op} \rightarrow \cdot \ +$ $\text{add_op} \rightarrow \cdot \ -$	on FOLLOW(<i>stmt</i>) = { <i>id</i> , <i>read</i> , <i>write</i> , <i>##</i> } reduce (pop 2 states, push <i>stmt</i> on input) on <i>add_op</i> shift and goto 10 on <i>+</i> shift and reduce (pop 1 state, push <i>add_op</i> on input) on <i>-</i> shift and reduce (pop 1 state, push <i>add_op</i> on input)

Figure 2.26 CFMSM for the calculator grammar (Figure 2.25). Basis and closure items in each state are separated by a horizontal rule. Trivial reduce-only states have been eliminated by use of "shift and reduce" transitions. (continued)

A Detailed Explanation of the CFMSM

State	Transitions
7. $expr \rightarrow term \cdot$ $term \rightarrow term \cdot mult_op factor$ <hr/> $mult_op \rightarrow \cdot +$ $mult_op \rightarrow \cdot /$	on FOLLOW($expr$) = {1d, read, write, \$\$, }, +, -} reduce (pop 1 state, push $expr$ on input) on $mult_op$ shift and goto 11 on + shift and reduce (pop 1 state, push $mult_op$ on input) on / shift and reduce (pop 1 state, push $mult_op$ on input)
8. $factor \rightarrow (\cdot expr)$ <hr/> $expr \rightarrow \cdot term$ $expr \rightarrow \cdot expr add_op term$ $term \rightarrow \cdot factor$ $term \rightarrow \cdot term mult_op factor$ $factor \rightarrow \cdot (expr)$ $factor \rightarrow \cdot 1d$ $factor \rightarrow \cdot number$	on $expr$ shift and goto 12 on $term$ shift and goto 7 on $factor$ shift and reduce (pop 1 state, push $term$ on input) on (shift and goto 8 on 1d shift and reduce (pop 1 state, push $factor$ on input) on number shift and reduce (pop 1 state, push $factor$ on input)
9. $stmt \rightarrow 1d := expr \cdot$ $expr \rightarrow expr \cdot add_op term$ <hr/> $add_op \rightarrow \cdot +$ $add_op \rightarrow \cdot -$	on FOLLOW($stmt$) = {1d, read, write, \$\$} reduce (pop 3 states, push $stmt$ on input) on add_op shift and goto 10 on + shift and reduce (pop 1 state, push add_op on input) on - shift and reduce (pop 1 state, push add_op on input)
10. $expr \rightarrow expr add_op \cdot term$ <hr/> $term \rightarrow \cdot factor$ $term \rightarrow \cdot term mult_op factor$ $factor \rightarrow \cdot (expr)$ $factor \rightarrow \cdot 1d$ $factor \rightarrow \cdot number$	on $term$ shift and goto 13 on $factor$ shift and reduce (pop 1 state, push $term$ on input) on (shift and goto 8 on 1d shift and reduce (pop 1 state, push $factor$ on input) on number shift and reduce (pop 1 state, push $factor$ on input)
11. $term \rightarrow term mult_op \cdot factor$ <hr/> $factor \rightarrow \cdot (expr)$ $factor \rightarrow \cdot 1d$ $factor \rightarrow \cdot number$	on $factor$ shift and reduce (pop 3 states, push $term$ on input) on (shift and goto 8 on 1d shift and reduce (pop 1 state, push $factor$ on input) on number shift and reduce (pop 1 state, push $factor$ on input)
12. $factor \rightarrow (expr \cdot)$ $expr \rightarrow expr \cdot add_op term$ <hr/> $add_op \rightarrow \cdot +$ $add_op \rightarrow \cdot -$	on) shift and reduce (pop 3 states, push $factor$ on input) on add_op shift and goto 10 on + shift and reduce (pop 1 state, push add_op on input) on - shift and reduce (pop 1 state, push add_op on input)
13. $expr \rightarrow expr add_op term \cdot$ $term \rightarrow term \cdot mult_op factor$ <hr/> $mult_op \rightarrow \cdot +$ $mult_op \rightarrow \cdot /$	on FOLLOW($expr$) = {1d, read, write, \$\$, }, +, -} reduce (pop 3 states, push $expr$ on input) on $mult_op$ shift and goto 11 on + shift and reduce (pop 1 state, push $mult_op$ on input) on / shift and reduce (pop 1 state, push $mult_op$ on input)

Figure 2.26 (continued)

Exercise: LR Parsing

- Assume you are in parsing state 0 and the token stream is `write sum / 2`
- Show how the parse stack changes as the token stream is consumed
- We'll do the first two actions together

Exercise: LR Parsing

<u>Parse stack</u>	<u>Input stream</u>	<u>Action</u>
0	write sum / 2 \$\$	(starting configuration)

Exercise: LR Parsing

Parse stack	Input stream	Action
0	write sum / 2 \$\$	(starting configuration)
0 write 4	sum / 2 \$\$	shift write
0 write 4	<i>factor</i> / 2 \$\$	shift <i>id</i> (sum) and reduce by <i>factor</i> → <i>id</i>
0 write 4	<i>term</i> / 2 \$\$	shift <i>factor</i> and reduce by <i>term</i> → <i>factor</i>
0 write 4 <i>term</i> 7	/ 2 \$\$	shift <i>term</i> and reduce by <i>term</i> → <i>factor</i>
0 write 4 <i>term</i> 7	<i>mult_op</i> 2 \$\$	shift / and reduce by <i>mult_op</i> → /
... 4 <i>term</i> 7 <i>mult_op</i> 11	2 \$\$	shift <i>mult_op</i>
... 4 <i>term</i> 7 <i>mult_op</i> 11	<i>factor</i> \$\$	shift 2 and reduce by <i>factor</i> → <i>num_lit</i> (2)
0 write 4	<i>term</i> \$\$	shift <i>factor</i> and reduce by <i>term</i> → <i>term mult_op factor</i>
0 write 4 <i>term</i> 7	\$\$	shift <i>term</i>
0 write 4	<i>expr</i> \$\$	reduce by <i>expr</i> → <i>term</i>
0 write 4 <i>expr</i> 6	\$\$	shift <i>expr</i>

Exercise: LR Parsing

<u>Parse stack</u>	<u>Input stream</u>	<u>Action</u>
...		
0 write 4 <i>expr</i> 6	\$\$	shift <i>expr</i>
0	<i>stmt</i> \$\$	reduce by <i>stmt</i> → write <i>expr</i>
0	<i>stmt_list</i> \$\$	shift <i>stmt</i> and reduce by <i>stmt_list</i> → <i>stmt</i>
0 <i>stmt_list</i> 2	\$\$	shift <i>stmt_list</i>
0	program	shift \$\$ and reduce by <i>program</i> → <i>stmt_list</i> \$\$
[done]		

Parsing if-then-else Statements

- A famous parsing challenge (from Algol) involves if-then-else, where else is optional:

$$\begin{aligned} \textit{stmt} ::= & \textit{if exp then stmt} \\ & | \textit{if exp then stmt else stmt} \end{aligned}$$

- Consider the phrase:

$$\textit{if exp then if exp then stmt else stmt}$$

- Which then does the else belong to?

Shift/Reduce Conflicts

- This is a shift-reduce conflict

if exp then if exp then stmt . else stmt

- When the `else` appears
 - we can *shift*, treating it as part of the inner `if` statement, or
 - we can *reduce* the inner `if` statement, treating the `else` as part of the outer `if` statement
- How to solve?
 - Many existing tools prioritize shift over reduce
 - This corresponds to the traditional solution to the `if` problem

Shift/Reduce Conflicts

- This is a shift-reduce conflict

if exp then if exp then stmt . else stmt

- When the `else` appears
 - we can *shift*, treating it as part of the inner `if` statement, or
 - we can *reduce* the inner `if` statement, treating the `else` as part of the outer `if` statement
- How to solve?
 - Many existing tools prioritize shift over reduce
 - **You can declare productions with *precedence***
 - E.g. giving the if-then-else production higher precedence than the if-then production

Shift/Reduce Conflicts

- This is a shift-reduce conflict

if exp then if exp then stmt . else stmt

- When the `else` appears
 - we can *shift*, treating it as part of the inner `if` statement, or
 - we can *reduce* the inner `if` statement, treating the `else` as part of the outer `if` statement
- How to solve?
 - Many existing tools prioritize shift over reduce
 - You can declare productions with *precedence*
 - Rewrite the grammar to make it LR(1)

An LR(0) If-Then-Else Grammar

$stmt \rightarrow balanced_stmt \mid unbalanced_stmt$
 $balanced_stmt \rightarrow if\ cond\ then\ balanced_stmt$
 $\qquad\qquad\qquad else\ balanced_stmt$
 $\qquad\qquad\qquad \mid\ other_stuff$
 $unbalanced_stmt \rightarrow if\ cond\ then\ stmt$
 $\qquad\qquad\qquad \mid\ if\ cond\ then\ balanced_stmt$
 $\qquad\qquad\qquad\qquad\qquad\qquad else\ unbalanced_stmt$

Invariant: *balanced_stmts* may be inside *unbalanced_stmts*

– but not vice versa

Unfortunately, this grammar is LR(0) but not LL(0)

– Have to use precedence in LL parsers
or add custom code to a recursive-descent parser



Advice for Managing Conflicts

- Start with a simple grammar that works
 - Even if it doesn't parse the whole language
- Add constructs incrementally
 - Save and compile the grammar after each change
 - If there was a conflict, adjust the grammar to avoid it before proceeding
 - Error messages are sometimes helpful, but don't actually try to understand/reconstruct the LR parsing table (even experts typically don't go this route)

Connections to Theory

- A scanner is a Deterministic Finite Automaton (DFA)
 - it can be specified with a state diagram
- An LL or LR parser is a Pushdown Automaton (PDA)
 - a PDA can be specified with a state diagram and a stack
 - the state diagram looks just like a DFA state diagram, except the arcs are labeled with <input symbol, top-of-stack symbol> pairs, and in addition to moving to a new state the PDA has the option of pushing or popping a finite number of symbols onto/off the stack
 - For LL(1) parsers the state machine has only two states: processing and accepted
 - All the action is in the input symbol and top of stack
 - LR(1) parsers are richer (and more expressive)

Error Reporting

- Error reporting is relatively simple
- If you get a token for which there's no entry in the current parsing state / top of stack element, signal an error
 - Can tell the user what tokens *would* be OK here

Error Recovery

- Nice to report more than one error to the user
 - Rather than stopping after the first one
- Simple idea: Panic mode
 - In C-like languages, semicolons are good recovery spots
 - So on an error:
 - read tokens until you get to a semicolon
 - discard the parser's stack (predictions in an LL parser, states in an LR parser) until you come to a production that has a semicolon
 - assume you've parsed the semicolon-containing construct, and continue parsing
 - There are ways to do substantially better – see the online supplement to the textbook

Other Parsing Tools

- Generalized LR (GLR) parser generators
 - Accept any grammar – even ambiguous ones!
 - This can be good if you have grammars written by nonexperts, as in SASyLF
 - But for a compiler-writer it is dangerous—you may not even know your grammar is ambiguous, and then your poor users get ambiguity errors when the parser runs
 - Works like an LR parser, but on ambiguity considers all possible parses in parallel
 - Still $O(n)$ if the grammar is LR (or “close”)

Other Parsing Tools

- Parsing Expression Grammar (PEG) parser generators
 - Sidestep ambiguity by always favoring the first production
 - Same danger as GLR parsers – you may not know your grammar is ambiguous
 - Still used some in practice (e.g. in Python)
 - About as efficient as LL or LR in practice
 - Like LR, PEG grammars can be cleaner than LL grammars
 - Requires extreme care to get right – must think algorithmically instead of declaratively
 - Guido van Rossum, the developer of Python, saw this as an advantage