Mobile Robotics, Mathematics, Models, and Methods

Errata in Initial Revision

Prepared by Professor Alonzo Kelly Rev 1.0, June 20, 2015

Locations in the first column are given in several formats:

- 1. x,y,z means page x, para y, line z
- 2. x, Fig y.z means figure y.z on page x.
- 3. x, Eq y.z means Equation y.z on page x.
- 4. etc.

Generally, errors in cross references will make it more difficult to follow derivations. With a few exceptions, errors in math (both in-line and otherwise) are typically notational.

A few severe issues are noted in the comments. Look for the word severe. If your time is limited, I suggest that you use a pencil in your text to fix the severe issues and the cross reference errors. Everything else is minor.

| Location | Present | Revised | Comment |
|----------|--|--|--|
| 28, 8,5 | is \mathfrak{R}^n . $\mathcal{R}(A)$ | is \mathfrak{R}^n . $\mathcal{R}(A)$ | Add space |
| 113,6,2 | we have: | we have the matrix: | clarify quantity is a matrix |
| 118,8,3 | Let the set of solutions to the above constraint be parameter- ized locally by a parameter <i>s</i> to produce the surface $\underline{x}(s)$. Each element of the vector $\underline{x}(s)$ is a <i>level curve</i> . | Let the set of solutions to the above constraint be parameter- ized locally in one direction by a parameter s to produce the curve $\underline{x}(s) \cdot \underline{x}(s)$ is called a <i>level curve</i> . | This discussion is con- fusing when applied to n dimensions. |
| 119,1,1 | We can conclude that the gradient $\partial \underline{g} / \partial \underline{x}$ | We can conclude that the gradient $\partial g / \partial x$ | remove underline |
| 1467,1,2 | composite vector of unknowns $\left[\Delta \underline{x}^T \ \underline{\lambda} \Delta^T\right]^T.$ | composite vector of unknowns $\left[\Delta \underline{x}^T \ \Delta \underline{\lambda}^T\right]^T.$ | move delta symbol |

| Location | Present | Revised | Comment |
|----------|--|--|---|
| 151 | Form the matrix (math font) V whose rows are two arbitrary vectors (math font, underlined) \underline{v}_1 and (math font, underlined) \underline{v}_2 in the plane.Use constrained optimization to show that the unit vector that maximizes the sum of its squared projections onto both vectors is an eigen- vector of (math font) V^{TV} . | Form the matrix V whose rows are two arbitrary vectors \underline{v}_1 and \underline{v}_2 in the plane. Use constrained optimization to show that the unit vector that maximizes the sum of its squared projections onto both vectors is an eigenvec- tor of $V^T V$. | remove format spec, take V down fromfinal superscript |
| 176, 7,1 | Consider next two frames of ref- erence that are rotating with respect to each one another | Consider next two frames of ref- erence that are rotating with respect to one another | remove word each |
| 192,4,1 | 4.2.2.1.1 Wheel Wheel Steering Control | 4.2.2.1.1 Wheel Steering Con- trol | delete extra word |
| 195,2,1 | Box 4.2 WMR Forward Kine- matics: Offset Wheels | Box 4.2 WMR Forward and Inverse Kinematics: Offset Wheels | add words |
| 213,8,3 | projection that occurs at line 11 | projection that occurs at line 12 | |
| 217,3,8 | the eigenvectors associated with the $n-1$ largest eigenvalues of C^{TC} | the eigenvectors associated with the $n - 1$ largest eigenvalues of $C^{T}C$ | move second C down from superscript |
| 217,4,2 | However, later content | However, earlier content | |
| 242,6,1 | The state vector is $\underline{x}(t) = \begin{bmatrix} x(t) & y(t) & \theta(t) \end{bmatrix}^T$ and | The state vector is $\underline{x}(t) = [x(t) \ y(t) \ \psi(t)]^T$ and | change theta to psi |
| 251,3,3 | counteract the increasing ten- dency increasing tendency to roll over | counteract the increasing ten- dency to roll over | delete double phrase |
| 261,3,1 | using the above Jacobian | using the Jacobian | delete word |
| 262,3,1 | the parameters \underline{p} may only be obtainable | the parameters ρ may only be obtainable | change letter p to rho |
| 268, 7 | 4.5.7.2 Papers | see comment | move Raol and Wong up to Books |

| Location | Present | Revised | Comment |
|----------------|--|---|--|
| 268, 7 | Proceedings of International symposium on Reading Review, 2011 | Proceedings of International Symposium on Robotics Research, 2011. | |
| 274,3 Spot 5.1 | The exponent $[\underline{x} - \underline{\mu}]^T C^{-1} [\underline{x} - \underline{\mu}]$ is called the <i>Mahalanobis dis-</i> <i>tance</i> (MHD) | The exponent $[\underline{x} - \underline{\mu}]^T C^{-1} [\underline{x} - \underline{\mu}]$ is called the (squared) <i>Mahala-</i> <i>nobis distance</i> (MHD) | add word "squared" |
| 278,1,2 | when the exponent (the squared <i>Mahalanobis distance</i>) is a constant | when the exponent (the squared <i>Mahalanobis distance</i>) is a constant | add word "squared" |
| 290,4,2 | in terms of it evolution over time; | in terms of its evolution over time; | change it to its |
| 308, 7 | It is not possible to invert this relationship to determine R from Σ_{xx} . | It is not possible to invert this relationship to determine R from Σ_{xx} . Also note that: $\hat{\underline{x}}^* = \Sigma_{xx} H^T R^{-1} \underline{z}$ In other words, the solution covariance appears in the for- mula for the solution itself. | Add sentence to clarify. |
| 309 | The weighted least squares solu- tion from Equation 5.79 for $H = \begin{bmatrix} 1 & 1 \end{bmatrix}^T$ and $R = \text{diag} \begin{bmatrix} \sigma_z^2 & \sigma_x^2 \end{bmatrix}$ is | The weighted least squares solu- tion from Equation 5.79 for $H' = \begin{bmatrix} 1 & 1 \end{bmatrix}^T$ and $R' = \text{diag} \begin{bmatrix} \sigma_z^2 & \sigma_x^2 \end{bmatrix}$ is | add primes to H and R |
| 310,2,2 | Now, suppose that another measurement $z_2 = 6$ was pro- duced at the same time as the first with variance $\sigma_{z1}^2 = (1.5)^2$. | Now, suppose that another measurement $z_2 = 6$ was produced at the same time as the first with variance $\sigma_{z2}^2 = (1.5)^2$. | Change variance sub- script to z2 |
| 312,11,5 | By substituting Equation 5.85 into Equation 5.80, we immedi- ately get: | We already know that the covari- ance of the MLE estimate is the first matrix in the solution. Therefore, from Equation 5.85 and Equation 5.84, we can immediately write: | Add sentence and reuse earlier result. |

| Location | Present | Revised | Comment |
|-----------|--|--|----------------------|
| 313, 11,1 | Subsequent measurements have covariances of $R_3 = diag \begin{bmatrix} 1 & 0.1 \\ 0.1 & 0.1 \end{bmatrix}$ and $R_4 = diag \begin{bmatrix} 0.1 & 0.1 \\ 0.1 & 0.1 \end{bmatrix}$. | Subsequent measurements have covariances of $R_3 = diag \begin{bmatrix} 1 & 0.1 \end{bmatrix}$ and $R_4 = diag \begin{bmatrix} 0.1 & 1 \end{bmatrix}$. | Change 0.1 to 1 |
| 325,4,3 | The "complement" of the linear- ized filter is an system dynamics model | The "complement" of the linear- ized filter is a system dynamics model | Change an to a |
| 331,1,1 | Let $\overrightarrow{\rho}$ be the position vector of the wheel relative to the body frame and let $\overrightarrow{\omega}$ denote the angular velocity which, is assumed | Let $\overrightarrow{\rho}$ be the position vector of the wheel relative to the body frame and let $\overrightarrow{\omega}$ denote the angular velocity, which is assumed | move comma |
| 346,3,5 | We will denote by \overline{A} the proposition that event that A did not occur. | We will denote by \overline{A} the proposition that event A did not occur. | delete second "that" |
| 353, 5,2 | Bayes', filter [17]. | Bayes' filter [17]. | remove comma |
| 361,2,3 | (Figure 5.48) | Figure 5.48 | remove brackets |
| 375, 3,3 | However, there may no solution | However, there may be no solu- tion | add word be |
| 276,2,2 | imagine placing the vehicle at the origin | imagine placing the vehicle on the hyperbola at y=0 | |
| 401,2 | measure the angle | measures the angle | add s |
| 401,3,1 | Inexpensive devices have band- widths on the order or 2 Hz | Inexpensive devices have bandwidths on the order of 2 Hz | or -> of |
| 401,3,2 | a <i>rebalance loop</i> that prevent the sensor | a <i>rebalance loop</i> that prevents the sensor | add s |
| 403,4,1 | neither constant nor entirely a real force. | neither constant nor entirely associated with a real force. | add two words |
| 407,5,2 | is fixed with a lasing medium | is filled with a lasing medium | fixed->filled |
| 414,6,2 | but the above assumes a zyx sequence. | but the above assumes a <i>zxy</i> sequence. | |
| 419,3,3 | Note that R_v^n and R_v^n are very different matrices | Note that \mathfrak{R}_{v}^{n} and R_{v}^{n} are very different matrices | different fonts |

| Location | Present | Revised | Comment |
|----------|---|---|----------------------|
| 432,5,6 | three to five meter accuracy | Three to five meter accuracy | capitalize T |
| 438,3,1 | The trajectory control level con- siders and entire trajectory | The trajectory control level con- siders an entire trajectory | and->an |
| 453,1 | Provide the details of the trans- fer function derivation for the cascade controller shown in Figure 7.14. | Provide the details of the transfer function $T(s)$ (before assuming $K_{vi} = 0$) derivation for the cascade controller shown in Figure 7.14. Its tricky. | |
| 469,4,6 | and an entire terminal state $\underline{x}s_f = \begin{bmatrix} x_f \ y_f \ \psi_f \ \kappa_f \end{bmatrix}.$ | and an entire terminal state $\underline{x}(s_f) = \begin{bmatrix} x_f \ y_f \ \psi_f \ \kappa_f \end{bmatrix}.$ | add brackets |
| 484,5,1 | Much of the forth coming dis- cussion | Much of the forthcoming discus- sion | join words |
| 491,3,1 | Of course, there are situations, such as operation in cluttered environments where | Of course, there are situations, such as operation in cluttered environments, where | add comma |
| 503,2,3 | Most sensors measure anyway. | Most sensors measure surfaces anyway. | add word "surfaces" |
| 503,4,1 | 7.4.3.3.4 Sampled versus Con- tinuum . | 7.4.3.3.4 Sampled versus Con- tinuum . | remove space |
| 503,4,6 | In such a representation compu- tational complexity | In such a representation, compu- tational complexity | add comma |
| 515,1,1 | Although states estimation | Although state estimation | states->state |
| 530,7,2 | similarity measures 9. | similarity measures [9]. | add [] |
| 536,5,3 | same color it is not possible | same color, it is not possible | add comma |
| 539,4,4 | defined by the Bessel function Figure 8.26 | defined by the Bessel function (Figure 8.26) | add () |
| 544,5,2 | In the latter case the corners can be very small | In the latter case, the corners can be very small | add comma |
| 560,5,5 | Hence, a camara that is sensitive | Hence, a camera that is sensitive | camara->camera |
| 562,4,1 | identical basic principles to those or sonar | identical basic principles to those of sonar | or->of |
| 569,3,2 | Section 1.3.10 of Chapter 5. | Section 5.1.3.10 of Chapter 5 | |
| 570,4,4 | optics are also relative inexpen- sive | optics are also relatively inex- pensive | relative->relatively |

| Location | Present | Revised | Comment |
|----------|--|---|-----------------------------------|
| 629,7,1 | Conversely, the residual $z(\underline{x}) = \underline{b} - \underline{c}(\underline{x})$ can be added | Conversely, the residual $z(\underline{x}) = \underline{b} - \underline{g}(\underline{x})$ can be added | c -> g |
| 635,4,1 | Let the measurement project onto a a few states | Let the measurement project onto a few states | delete redundant word |
| 637, 3 | to locate the landmark Figure 9.48. | to locate the landmark (Figure 9.48). | add () |
| 643,5 | Soundness Feasible Admissible Completeness If any If not Optimality | Soundness Feasible Admissible Completeness If any If not Optimality | Indent 2nd,3rd,4th,5th bullets |
| 651, 3,2 | set of roads and vehicles | set of roads, and vehicles | |
| 655,5,1 | to encode arbitrary gradient. | to encode arbitrary strategies. | gradient->strategies |
| 659,1,2 | described in terms of a traversal of a tree that restrict traversal is discovered during the search process | described in terms of a traversal of a tree that is discovered dur- ing the search process | delete "restrict tra- versal" |
| 662,2,1 | the g values nodes | the g values | |
| 664, 2,1 | The cost estimate $f(\underline{x})$ is computed | The cost estimate $f(\underline{x})$ is computed | add space |
| 666,3,6 | total costs any new nodes added to OPEN | total costs of any new nodes added to OPEN | insert "of" |
| 668,6,6 | order to process child nodes is unknown means this | order to process child nodes is unknown, means this | add comma |
| 669, 8,4 | In difficult terrain the details | In difficult terrain, the details | add comma |
| 671,4,3 | (only when headed) | (only when needed) | headed->needed |
| 679,5,5 | Node costs refer to the esti- mated total cost | Node costs refer to the estimated total cost | estimate->estimated |

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|---------------|---|---|---|
| 40 | $\frac{\partial}{\partial \underline{p}} f(\underline{x}, \underline{p}) = f_{\underline{x}} \cdot \frac{\partial \underline{x}}{\partial \underline{p}} + f_{\underline{x}}$ | $\frac{\partial}{\partial \underline{p}} f(\underline{x}, \underline{p}) = f_{\underline{x}} \cdot \frac{\partial \underline{x}}{\partial \underline{p}} + f_{\underline{p}}$ | Add <u>p</u> subscript |
| 77,Eq 2.72 | $\begin{bmatrix} 1 & -\delta\psi & \delta\theta & 0 \\ \delta\psi & 1 & -\delta\phi & 0 \\ -\delta\theta & \delta\phi & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$ | $\begin{bmatrix} 0 & -\delta\psi & \delta\theta & 0 \\ \delta\psi & 0 & -\delta\phi & 0 \\ -\delta\theta & \delta\phi & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$ | severe error, replace diagonal with zeros |
| 95, Eq 2.96 | $T_{R2}^{R1} = T_B^R T_P^B (T_T^B)^{-1} (T_B^R)^{-1}$ | $T_{R2}^{R1} = T_B^R T_P^{B1} (T_T^B)^{-1} (T_B^R)^{-1}$ | replace superscript B with B1 |
| 97,Eq 2.97 | $\begin{bmatrix} c\psi_{k_{1}}^{i} - s\psi_{k}^{i} \ c\psi_{j}^{i}a_{k}^{j} - s\psi_{j}^{i}b_{k}^{j} + a_{j}^{i} \\ s\psi_{k_{1}}^{i} \ c\psi_{k}^{i} \ s\psi_{j}^{i}a_{k}^{j} + c\psi_{j}^{i}b_{k}^{j} + b_{j}^{i} \\ 0 & 0 & 1 \end{bmatrix}$ | $\begin{bmatrix} c\psi_k^i - s\psi_k^i c\psi_j^i a_k^j - s\psi_j^i b_k^j + a_j^i \\ s\psi_k^i - c\psi_k^i - s\psi_j^i a_k^j + c\psi_j^i b_k^j + b_j^i \\ 0 & 0 & 1 \end{bmatrix}$ | move column separa- tors right |
| 124, Eq 3.7 | subject to: $\underline{c}' \operatorname{mp}(\underline{x}) = \underline{0}$ | subject to: $\underline{c}(\underline{x}) = \underline{0}$ | remove letters mp |
| 127, Eq 3.12 | $f(\underline{x}) = \frac{1}{2} \underline{x}^T Q_{xx} \underline{x} + \underline{b}^T \underline{x} + \underline{c}$ | $f(\underline{x}) = \frac{1}{2} \underline{x}^T Q_{xx} \underline{x} + \underline{b}^T \underline{x} + c$ | no underline on c |
| 163, Eq 3.119 | $k_p = \frac{\tau}{\Delta t}$ | $k_p = \frac{\Delta t}{\tau}$ | reciprocal |
| 199, Eq 4.62 | $r_{c1}^{s1} = d \begin{bmatrix} -s\gamma_1 & -c\gamma_1 \end{bmatrix}^T$ $r_{c3}^{s3} = d \begin{bmatrix} -s\gamma_3 & -c\gamma_3 \end{bmatrix}^T$ $r_{c2}^{s2} = d \begin{bmatrix} s\gamma_2 & c\gamma_2 \end{bmatrix}^T$ $r_{c4}^{s4} = d \begin{bmatrix} s\gamma_4 & c\gamma_4 \end{bmatrix}^T$ | $r_{c1}^{s1} = d \begin{bmatrix} -s\gamma_1 & c\gamma_1 \end{bmatrix}^T$ $r_{c3}^{s3} = d \begin{bmatrix} -s\gamma_3 & c\gamma_3 \end{bmatrix}^T$ $r_{c2}^{s2} = d \begin{bmatrix} s\gamma_2 & -c\gamma_2 \end{bmatrix}^T$ $r_{c4}^{s4} = d \begin{bmatrix} s\gamma_4 & -c\gamma_4 \end{bmatrix}^T$ | severe error, change sign of all y coordinates |
| 208,1 | $\underline{\rho}_i^T = \dots = \begin{bmatrix} 0 & 0 & (c\gamma x_i^v + s\gamma y_i^v) \end{bmatrix}$ | $\underline{\rho}_i^T = \dots = -\left[0 \ 0 \ (c\gamma x_i^{\nu} + s\gamma y_i^{\nu})\right]$ | severe error, add minus sign to 3rd expression only |
| 210, Eq 4.94 | $\underline{c}_{\underline{x}} = \begin{bmatrix} -s\psi & c\psi & -L \\ -s\psi\gamma & c\psi\gamma & Lc\gamma \end{bmatrix}$ | $\underline{c}_{\underline{x}} = \begin{bmatrix} -s\psi & c\psi & -L \\ -s\psi\gamma & c\psi\gamma & Lc\gamma \end{bmatrix}$ | change subscript to \dot{x} |

Table 2: Math and Algorithm Edits

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| Location | Present | Revised | Comment |
|---------------|--|---|---|
| 224, Eq 4.111 | $\underline{c}(\underline{x}) = \begin{bmatrix} v \\ v_z \\ \omega_x \\ \omega_y \end{bmatrix}_{W}^{V} = \underline{0}$ | $\underline{c}(\underline{x}) = \begin{bmatrix} v \begin{bmatrix} v_z \\ \omega_x \\ \omega_y \end{bmatrix}_v^w = \underline{0}$ | switch right super and subscript, leave left alone |
| 227,7 | $\frac{\tau}{\Delta t}(y_{k+1}-y_k)+y_{k+1} = \dots$ | $\frac{\tau}{\Delta t}(y_{k+1}-y_k)+y_k = \dots$ | change k+1 to k |
| 227,8 | $\dots = y_k + \frac{\Delta t}{\tau} (u_{k+1} - y_{k+1})$ | $y_{k+1} = y_k + \frac{\Delta t}{\tau} (u_{k+1} - y_k)$ | change k+1 to k |
| 242, Eq 4.152 | $\begin{bmatrix} c\theta(t) - s\theta(t) & 0 \\ s\theta(t) & c\theta(t) & 0 \\ 0 & 0 & 1 \end{bmatrix}$ | $\begin{bmatrix} c\psi(t) & -s\psi(t) & 0 \\ s\psi(t) & c\psi(t) & 0 \\ 0 & 0 & 1 \end{bmatrix}$ | change theta to psi everywhere |
| 242, 7,1 | $\begin{bmatrix} 0 & 0 & -[s\theta(t)V_x(t) + c\theta(t)V_y(t)] \\ 0 & 0 & [c\theta(t)V_x(t) - s\theta(t)V_y(t)] \\ 0 & 0 & 0 \end{bmatrix}$ | $\begin{bmatrix} 0 & 0 & -[s\psi(t)V_x(t) + c\psi(t)V_y(t)] \\ 0 & 0 & [c\psi(t)V_x(t) - s\psi(t)V_y(t)] \\ 0 & 0 & 0 \end{bmatrix}$ | change theta to psi everywhere (including inline 2 lines above) |
| 242, 8,1 | $\begin{bmatrix} c\theta(t) - s\theta(t) & 0\\ s\theta(t) & c\theta(t) & 0\\ 0 & 0 & 1 \end{bmatrix}$ | $\begin{bmatrix} c\psi(t) & -s\psi(t) & 0 \\ s\psi(t) & c\psi(t) & 0 \\ 0 & 0 & 1 \end{bmatrix}$ | change theta to psi everywhere |
| 243, Eq 4.154 | $\begin{bmatrix} c\theta(t) - s\theta(t) - \Delta y(t, \tau) \\ s\theta(t) \ c\theta(t) \ \Delta x(t, \tau) \\ 0 \ 0 \ 1 \end{bmatrix}$ | $\begin{bmatrix} c\psi(t) - s\psi(t) - \Delta y(t, \tau) \\ s\psi(t) \ c\psi(t) \ \Delta x(t, \tau) \\ 0 \ 0 \ 1 \end{bmatrix}$ | change theta to psi everywhere |
| 243, Eq 4.155 | $\begin{bmatrix} c\theta(t) - s\theta(t) - \Delta y(t, \tau) \\ s\theta(t) \ c\theta(t) \ \Delta x(t, \tau) \\ 0 \ 0 \ 1 \end{bmatrix}$ | $\begin{bmatrix} c\psi(t) - s\psi(t) - \Delta y(t, \tau) \\ s\psi(t) \ c\psi(t) \ \Delta x(t, \tau) \\ 0 \ 0 \ 1 \end{bmatrix}$ | change theta to psi everywhere (just like line above) |
| 263,7 | $\begin{bmatrix} V(t)\cos\theta(t) \\ V(t)\sin\theta(t) \\ \omega(t) \end{bmatrix}, \begin{bmatrix} c\theta & 0 \\ s\theta & 0 \\ 0 & 1 \end{bmatrix}$ | $\begin{bmatrix} V(t)\cos\psi(t)\\V(t)\sin\psi(t)\\\omega(t)\end{bmatrix}, \begin{bmatrix} c\psi & 0\\s\psi & 0\\0 & 1 \end{bmatrix}$ | change theta to psi everywhere |

| Location | Present | Revised | Comment |
|---------------|--|--|--|
| 264,1 | $\begin{bmatrix} c\theta & c\theta \\ s\theta & s\theta \\ 1/W - 1/W \end{bmatrix}$ | $\begin{bmatrix} c\psi & c\psi \\ s\psi & s\psi \\ 1/W - 1/W \end{bmatrix}$ | change theta to psi everywhere |
| 264,2 | $\begin{bmatrix} (v_r + v_l)c\theta \\ (v_r + v_l)s\theta \\ (v_r - v_l)/W \end{bmatrix}$ | $\begin{bmatrix} (v_r + v_l)c\psi \\ (v_r + v_l)s\psi \\ (v_r - v_l)/W \end{bmatrix}$ | change theta to psi everywhere |
| 265, Eq 4.221 | $\delta \underline{x}(t) = F \delta \underline{x}(t) + G \delta \underline{u}(t)$ | $\delta \dot{\underline{x}}(t) = F \delta \underline{x}(t) + G \delta \underline{u}(t)$ | missing dot (time deriv- ative) |
| 274, 1 | $p(x) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$ | $p(x) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$ | sigma is not inside square root |
| 298,10 | $\sigma_k^2 = \left(\frac{k-1}{k}\right)\sigma_k^2 = \left(1 - \frac{1}{k}\right)\sigma_k^2$ | $\sigma_k^2 = \left(\frac{k-1}{k}\right)\sigma_{k-1}^2 = \left(1 - \frac{1}{k}\right)\sigma_{k-1}^2$ | change k subscript to k- 1 |
| 302,3,3 | $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \begin{bmatrix} c_i & -l_i s_i \\ s_i & l_i c_i \end{bmatrix}$ | $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \begin{bmatrix} -l_i s_i \\ l_i c_i \end{bmatrix}$ | delete first col of 2nd matrix |
| 304,7 | $Exp[\Phi(t, t_0)\delta \underline{x}(t_0)\delta \underline{x}(t_0)\Phi(t, t_0)^T]$ | $Exp[\Phi(t, t_0)\delta \underline{x}(t_0)\delta \underline{x}(t_0)^T \Phi(t, t_0)^T]$ | add transpose |
| 311,1,2 | The measurements relationship is: $\begin{bmatrix} \underline{z} \\ \underline{x} \end{bmatrix} = \begin{bmatrix} H \\ I \end{bmatrix} \underline{x}'$ | The measurement relationship is: $\begin{bmatrix} z \\ \underline{x} \end{bmatrix} = \begin{bmatrix} H \\ I \end{bmatrix} \underline{x}'$ | Remove s at end of word "measurements". Add second equality. |
| 311, Eq 5.84 | $\underline{\mathbf{x}}' = (\boldsymbol{H}^T \boldsymbol{R}^{-1} \boldsymbol{H})^{-1} \boldsymbol{H}^T \boldsymbol{R}^{-1} \underline{\boldsymbol{z}}$ | $x' = (H'^{T}R'^{-1}H')^{-1}H'^{T}R'^{-1}z$ | Add primes to H and R |
| 328, Eq 5.111 | $\begin{bmatrix} \dots & \dots & \partial \dot{x} / \partial \theta & \dots & \dots \\ \dots & \dots & \partial \dot{y} / \partial \theta & \dots & \dots \\ \dots & \dots & \partial \dot{\theta} / \partial \theta & \dots & \dots \\ \dots & \dots & \partial \dot{v} / \partial \theta & \dots & \dots \\ \dots & \dots & \partial \dot{\omega} / \partial \theta & \dots & \dots \end{bmatrix}$ | ∂x/∂ψ | Change theta to psi everywhere (3rd col) and thetadot to psidot everywhere (3rd row). |

Table 2: Math and Algorithm Edits

| Location | Present | Revised | Comment |
|---------------|--|--|--|
| 328, Eq 5.112 | $\begin{bmatrix} \dots \\ \dots \\ \psi_{k+1} \\ v_k \\ \omega_k \end{bmatrix}$ | $\begin{bmatrix} \dots \\ \dots \\ \Psi_{k+1} \\ \nu_{k+1} \\ \omega_{k+1} \end{bmatrix}$ | Change subscripts of last two elements to k+1. |
| 376, Eq 6.8 | $\begin{bmatrix} \delta x \\ \delta y \\ \delta \theta \end{bmatrix}$ | $\begin{bmatrix} \delta x \\ \delta y \\ \delta \psi \end{bmatrix}$ | change theta to psi |
| 380, 2 | Writing total differentials: + + $F_{\theta_1} \delta \psi_1 + F_{\theta_2} \delta \psi_2 = 0$ + + $G_{\theta_1} \delta \psi_1 + G_{\theta_2} \delta \psi_2 = 0$ | Writing total differentials: $\dots + \dots + F_{\psi_1} \delta \psi_1 + F_{\psi_2} \delta \psi_2 = 0$ $\dots + \dots + G_{\psi_1} \delta \psi_1 + G_{\psi_2} \delta \psi_2 = 0$ | change theta to psi |
| 391,6 | $\begin{bmatrix} \sigma_{xx}(0) & \sigma_{xy}(0) & \sigma_{x\theta}(0) \\ \sigma_{xy}(0) & \sigma_{yy}(0) & \sigma_{y\theta}(0) \\ \sigma_{x\theta}(0) & \sigma_{y\theta}(0) & \sigma_{\theta\theta}(0) \end{bmatrix}$ | $\begin{bmatrix} \sigma_{xx}(0) & \sigma_{xy}(0) & \sigma_{x\psi}(0) \\ \sigma_{xy}(0) & \sigma_{yy}(0) & \sigma_{y\psi}(0) \\ \sigma_{x\psi}(0) & \sigma_{y\psi}(0) & \sigma_{\psi\psi}(0) \end{bmatrix}$ | change theta to psi |
| 594,4 | $\underline{\rho}_{S}^{W} = \underline{\rho}_{O}^{W} * \underline{\rho}_{S}^{W}$ | $\underline{\rho}_{S}^{W} = \underline{\rho}_{O}^{W} * \underline{\rho}_{S}^{O}$ | severe, superscript W - > O |
| 601,4 | $\underline{\rho} = argmin$ $\left[f(\underline{\rho}) = \frac{1}{2}r^{T}(\underline{\rho}, \underline{Z})r(\underline{\rho}, \underline{Z})\right]$ | $\underline{\rho}^* = \operatorname{argmin} \\ \left[f(\underline{\rho}) = \frac{1}{2} t^T (\underline{\rho}, \underline{Z}) t(\underline{\rho}, \underline{Z}) \right]$ | change $\underline{\rho}$ to $\underline{\rho}^*$ |
| 601,5 | $\underline{\rho} = argmax$ $[f(\underline{\rho}) = \underline{z}_{obs}^{T} \underline{z}_{pred}(\underline{\rho}, \underline{Z})]$ | $\underline{\rho}^* = argmax$ $[f(\underline{\rho}) = \underline{z}_{obs}^T \underline{z}_{pred}(\underline{\rho}, \underline{Z})]$ | change $\underline{\rho}$ to $\underline{\rho}^*$ |
| 608,2 | $\underline{\rho} = argmin$ $\left[f(\underline{\rho}) = \frac{1}{2}r^{T}(\underline{\rho}, \underline{Z})r(\underline{\rho}, \underline{Z})\right]$ | $\underline{\rho}^* = \operatorname{argmin} \\ \left[f(\underline{\rho}) = \frac{1}{2} \boldsymbol{r}^T (\underline{\rho}, \underline{X}) \boldsymbol{r}(\underline{\rho}, \underline{X}) \right]$ | change $\underline{\rho}$ to $\underline{\rho}^*$ and \underline{Z} to \underline{X} |
| 629, Eq 9.43 | $c(\underline{x}) = \underline{b}$ | $\underline{g}(\underline{x}) = \underline{b}$ | c -> g |

Table 2: Math and Algorithm Edits

| Location | Present | Revised | Comment |
|---|---|--|------------------------|
| 662, algo- rithm expand- NodeDijkstra, line 05 | else if $(gnew < x \cdot g)$ | else if $(gnew < x_{next} \cdot g)$ | x -> xnext, severe bug |
| 665, algo- rithm expand- NodeAstar, line 05 | $\mathbf{if}(x_{next} \in O \&\& fnew < x . f)$ | $\mathbf{if}(x_{next} \in O \&\& fnew < x_{next} \cdot f)$ | x -> xnext, severe bug |
| 665, algo- rithm expand- NodeAstar, line 08 | else if $(x_{next} \in C \&\& fnew < x.f)$ | else if $(x_{next} \in C \&\& fnew < x_{next}.f)$ | x -> xnext, severe bug |

Table 3: Cross Reference Edits

| Location | Present | Revised | Comment |
|----------------------|--|--|---------------------------------------|
| 41,1,2 | Figure 2.7 | Figure 2.8 | |
| 139,4,2 | section Figure 3.2.1.4 | section 3.2.1.5 | Figure -> Section 3.2.1.4->3.2.1.5 |
| 167,1 | Solve Equation 3.104 | Solve Equation 3.105 | 4 -> 5 |
| 170,6,1 | Substituting this into Equation 3.139 above | Substituting this into Equation 3.140 above | |
| 180, 1, (Box 4.1) | Equation 4.11, Equation 4.12, and Equation 4.13. | Equation 4.12, Equation 4.13, and Equation 4.14. | |
| 201,4 | Rewrite Equation 4.40 | Rewrite Equation 4.39 | |
| 209, 6,1 | Equation 4.91 | Equation 3.91 | |
| 210,10,1 | Algorithm 4.2 | Algorithm 4.1 | |
| 224,3 | Based on Equation 4.74 | Based on Equation 2.74 | 4 -> 2 |
| 225, 3 | constraint from Figure 4.6 | constraint from Figure 4.17 | 6 -> 17 |
| 228,12,1 | Equation 4.114 | Equation 4.116 | |
| 230,2,2 | The transform of our first-order system (Equation 4.113) | The transform of our first-order system (Equation 4.114) | |
| 258,1 | Section 2.2.3 of Chapter 3 | Section 3.2.2.3 of Chapter 3 | clarify reference |
| 258, 5 | the functional in Equation 3.122 in Chapter 3 | the functional in Equation 3.133 in Chapter 3 | |
| 264, 2, 1 | Equation 4.214 | Equation 4.216 | |

| Location | Present | Revised | Comment |
|----------|---|--|-----------------------|
| 265,6,2 | Jacobian of the left-hand side of Equation 4.221 | Jacobian of the left-hand side of Equation 4.222 | |
| 296,8,3 | Equation 5.58 | Equation 5.57 | |
| 297,4,3 | Equation 5.61 | Equation 5.60 | |
| 305,3,2 | Equation 5.71 | Equation 5.69 | |
| 305,5,1 | Equation 5.69 | Equation 5.68 | |
| 306,2,2 | Equation 4.138 | Equation 4.150 | |
| 309,3,2 | Equation 5.80 | Equation 5.79 | |
| 311,7,1 | The result of Equation 5.87 | The result of Equation 5.86 | |
| 342,10,2 | It can be derived by returning to Equation 5.83 and including the above | It can be derived by returning to Equation 5.84 and including the above | |
| 350,6,4 | the computation of the denomi- nator in Equation 5.142 requires that | the computation of the denomi- nator in Equation 5.143 requires that | |
| 361,5,1 | Recall Equation 5.151 and Equation 5.152 | Recall Equation 5.150 and Equa- tion 5.151 | |
| 389 | Section 4.5.6 of Chapter 4 | Section 4.5.6.6 of Chapter 4 | more precise xref |
| 415,2,3 | based on Equation 2.76 in Chapter 2 | based on Equation 2.81 in Chap- ter 2 | |
| 415,3,1 | Equivalently, based on Equation 2.132 in Chapter 2 | Equivalently, based on Equation 2.133 in Chapter 2 | |
| 424,7 | first two lines of Equation 6.57 | first two lines of Equation 6.58 | |
| 427,3,5 | Figure 6.28 illustrates the equivalent | Figure 6.32 illustrates the equivalent | |
| 596,1,1 | then we can use Equation 2.55 | then we can use Equation 2.56 | |
| 596,3,1 | For the camera, we can use Equation 2.81 | For the camera, we can use Equation 2.82 | |
| 615,6,3 | Figure 5.38 | Figure 5.36 | |
| 629,4,1 | This is of the form of equation Equation 9.37. | This is of the form of Equation 9.37. | delete redundant word |
| 638,1,3 | varies along the line of the laser (Figure 9.48). | varies along the line of the laser (Figure 9.49). | |

Table 3: Cross Reference Edits

| Location | Present | Revised | Comment |
|--------------------------|---|---|---|
| 65, Fig 2.22 | as drawn | see comment | x,y axes should not be partially erased |
| 416, Fig 6.30 | $\stackrel{i}{\underline{\Omega}}_{n}^{i} = \underline{\Omega} \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}^{T}$ | $\stackrel{i}{\underline{\Omega}}_{e}^{i} = \underline{\Omega} \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}^{T}$ | change n sub/sup script to e |
| | ${}^{n}\Omega_{-n}^{i} = \Omega \Big[c\lambda \ 0 \ -s\lambda \Big]^{T}$ | $\stackrel{e}{\underline{\Omega}}_{\underline{-e}}^{i} = \Omega \begin{bmatrix} c\lambda & 0 & -s\lambda \end{bmatrix}^{T}$ | |
| 428, Fig 6.33 caption | two antenna | two antennae | |
| 503,Fig 7.44 | as drawn | see comment | increase contrast in left image |
| 598, Fig 9.16 | as drawn | see comment | increase contrast in right figure to see high- lighted fork holes |
| 618, Fig 9.35 caption | Line are approximately 1 pixel wide | Lines are approximately 1 pixel wide | line -> lines |
| 621, Fig 9.39 | as drawn | see comment | increase contrast to see feature traces |
| 663, Fig 10.19 | as drawn | see comment | increase contrast to see left image |

Table 4: Figure Edits