Design and Implementation of Speech Recognition Systems

Spring 2012

Class 12: Continuous Speech
29 Feb 2012

Spell Checking

- I retruned and saw unnder thhe sun thet the erace is nott to the svift nor the batle to the sdrong neither yet bread to the weise nor yet riches to men of andurstendin nor yet feyvor to nen of skill but tyme and chance happene to them all

- How to correct spelling?
  - For each word
    - Compare word to all words in dictionary
    - Select closest word

Spell Checking

- I retruned and saw unnder thhe sun thet therace is notto the svift northe batleto the strong neither yet bread tothe weise nor yet riches to men ofandurstendin nor yet feyvor tomen of skill but tyme and chance happeneto them all

- How to correct spelling?
  - Some words have “merged”

Spell Checking

- Iretrunedandsawunnderthhesunthettheraceisnot tothesviftnorthebatletothestrongneitheryetbrea dtotheweisenoryetrichestomenofandurstendinn oryetfeyvortomenofskillbuttymeandchancehap penetothemall

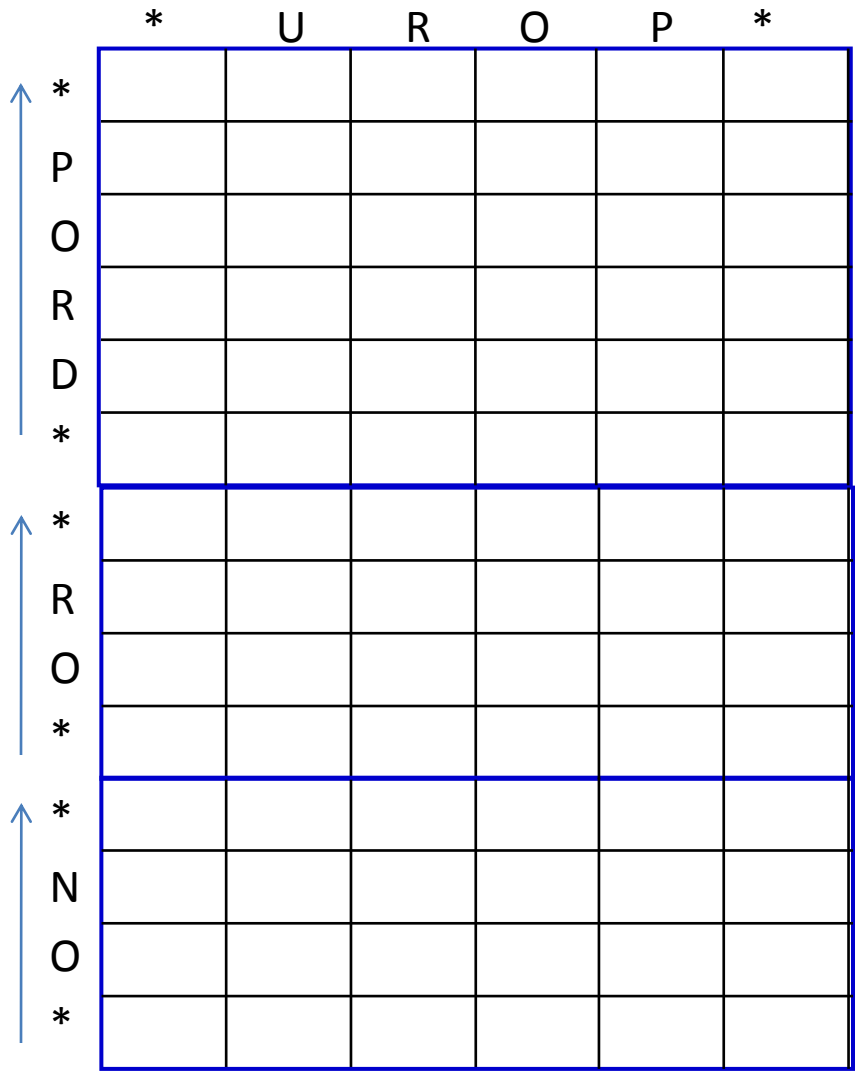
- How to correct spelling now?

A Simpler Problem

- Ireturnedandsawunderthesunthattheraceisnottotheswiftnorthebattletothestrongneitheryetbreadtothewisenoryetrichestomenofunderstandingnoryetfavortomenofskillbuttimeandchancehappentothemall

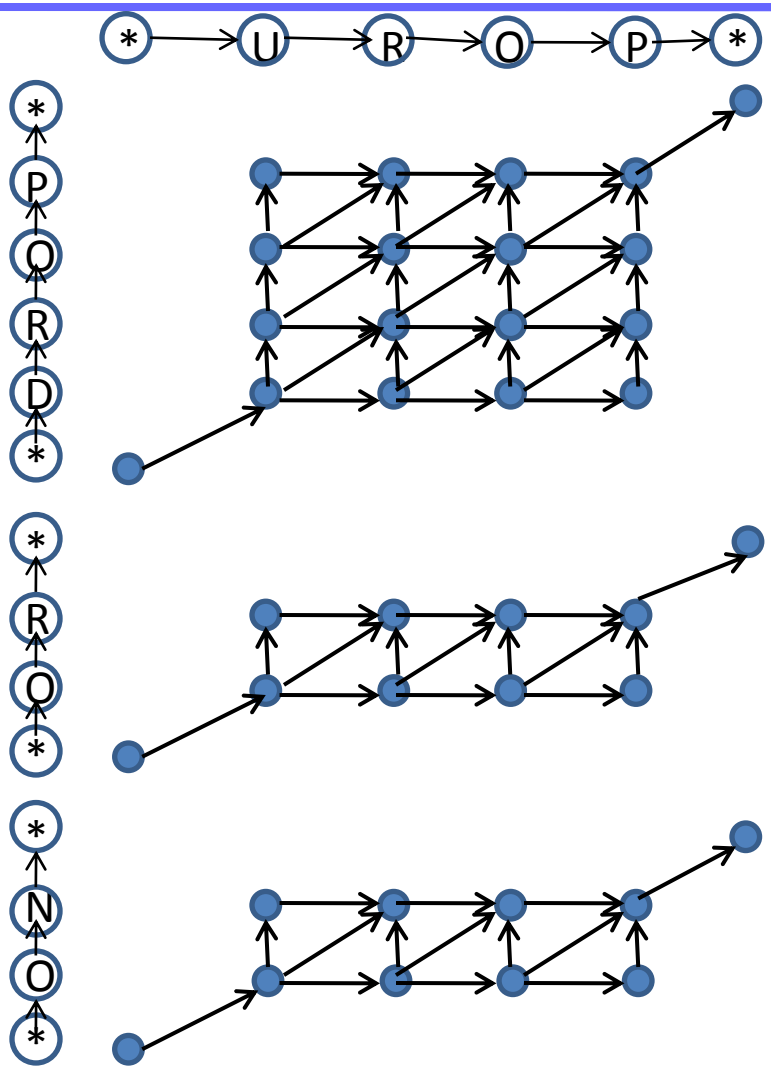
- Automatic introduce spaces

The Basic Spellchecker



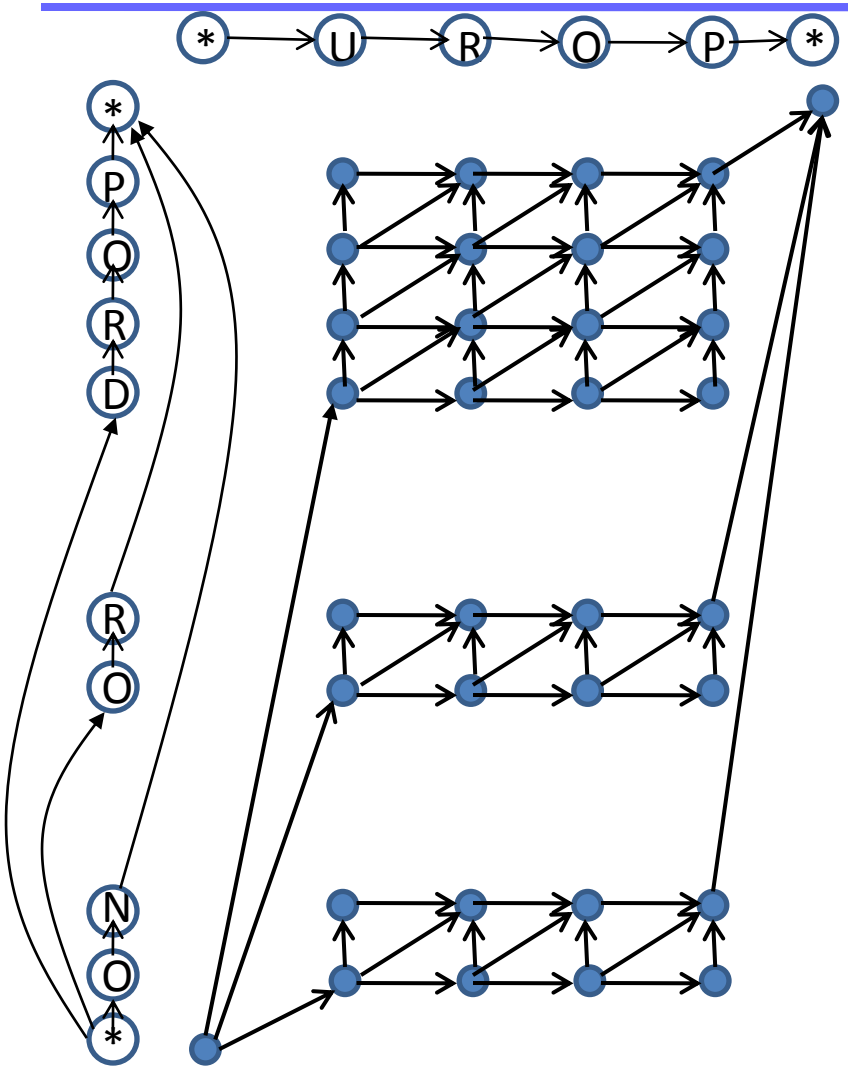
- Compare the string to each of the words in the dictionary

The Basic Spellchecker



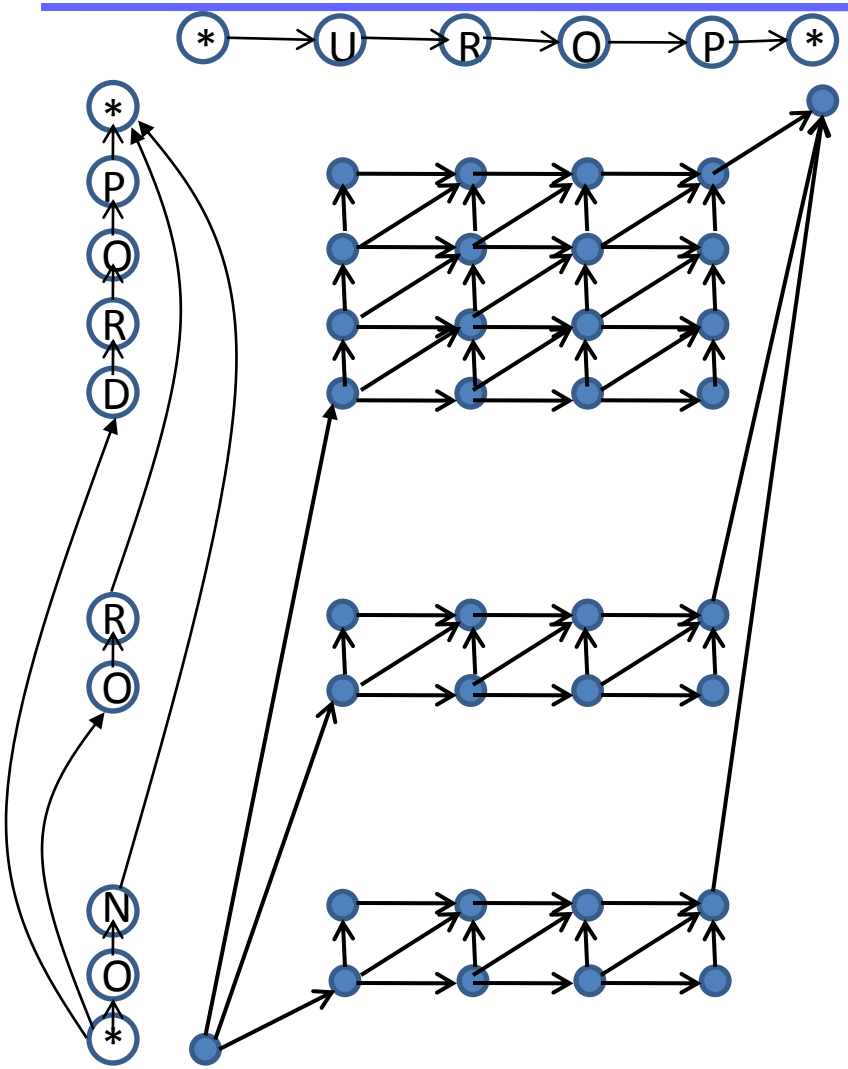
- Compare the string to each of the words in the dictionary
- The corresponding trellis
  - Cross products of the dictionary strings and input string

The Basic Spellchecker



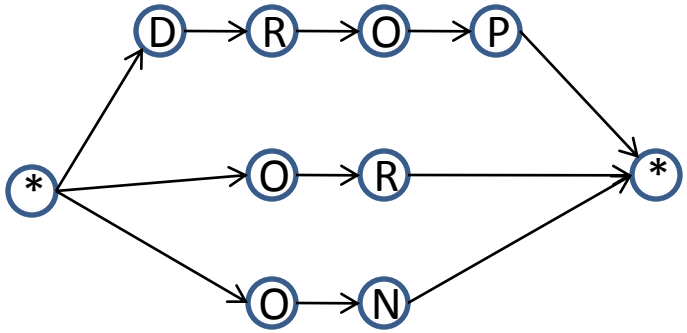
- Compare the string to each of the words in the dictionary
- The corresponding trellis
  - Cross products of the dictionary strings and input string
- An equivalent trellis
  - Note the template model

The Trellis as a Product

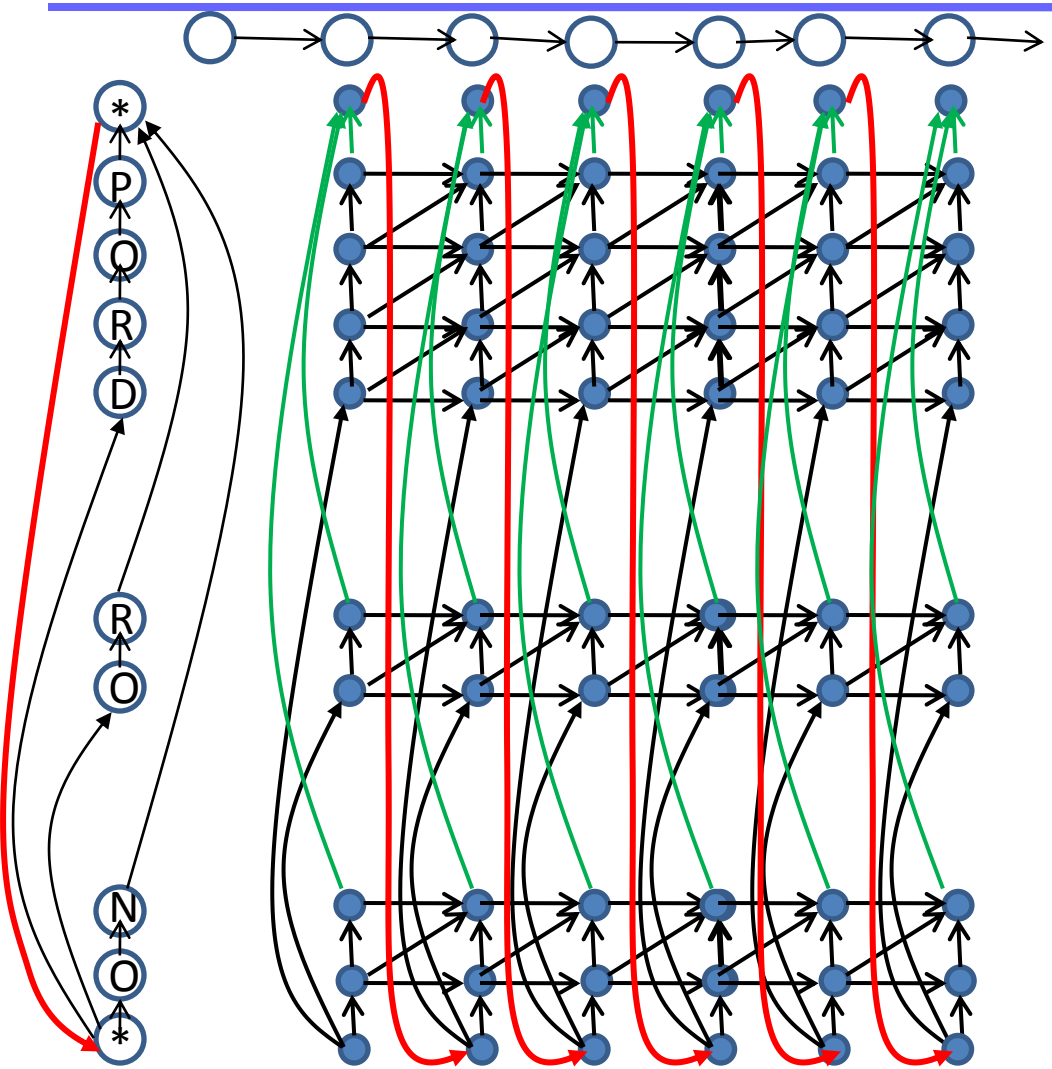


- The Trellis is a “cross product” of the data string..

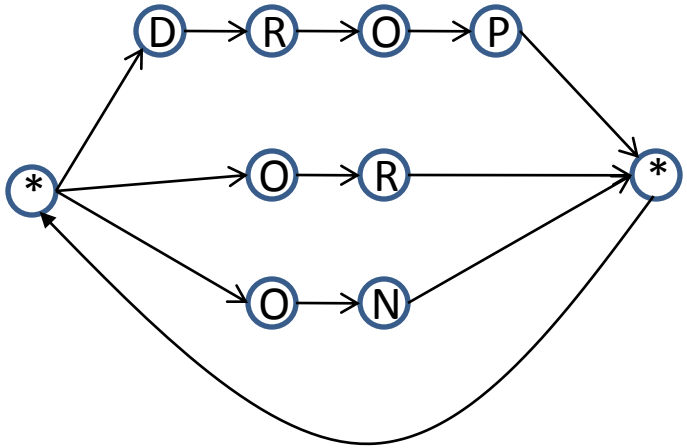
- And a model..



Continuous text: Looping around

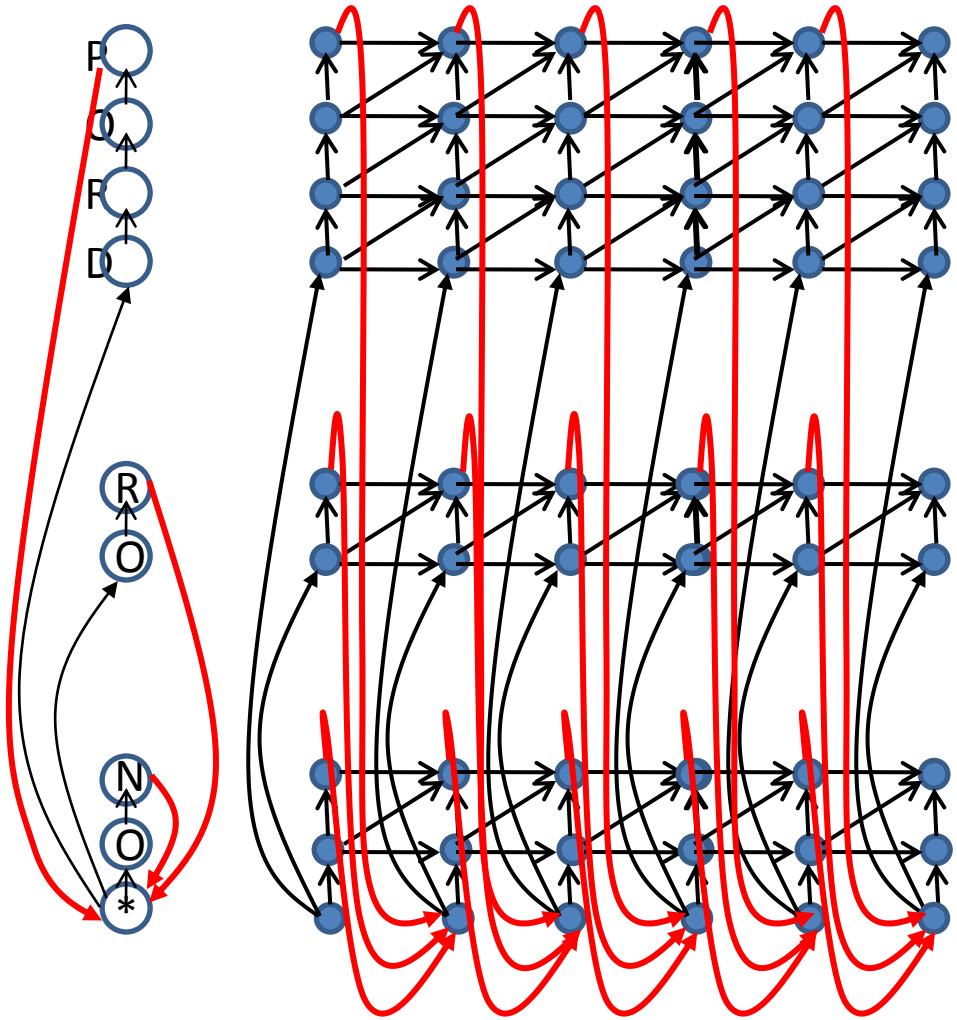


- To model continuous text, include a loopback

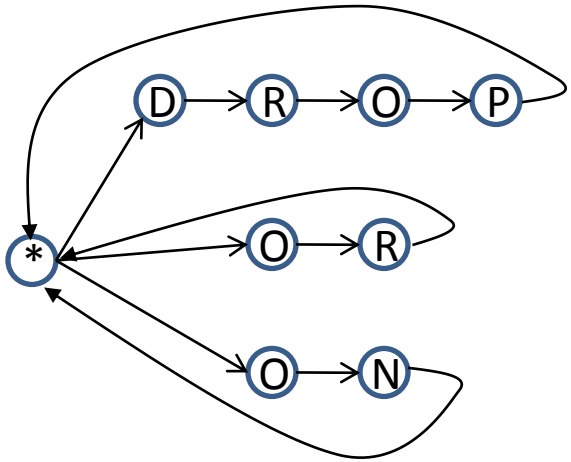


Green arrows to terminating node, red arrows returning to initial node

Continuous text: Looping around

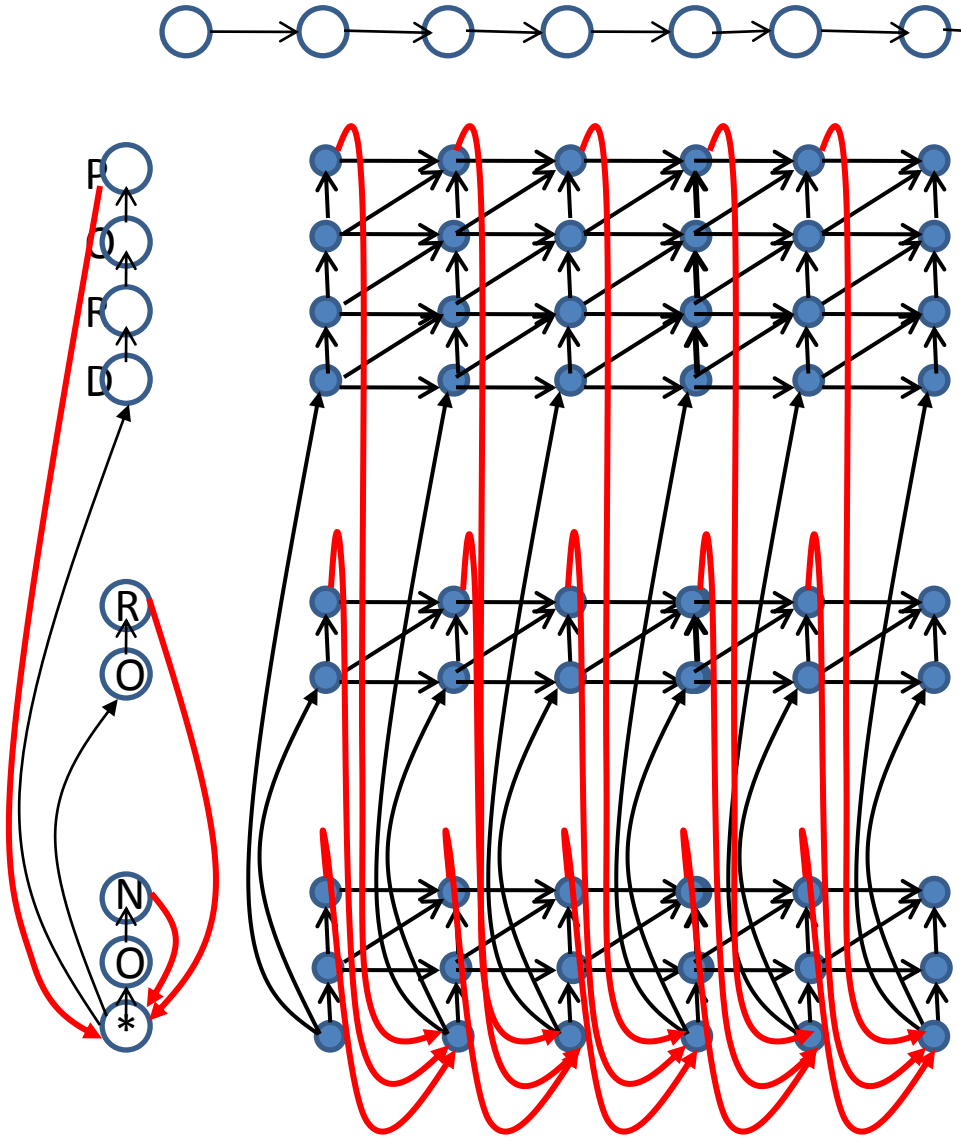


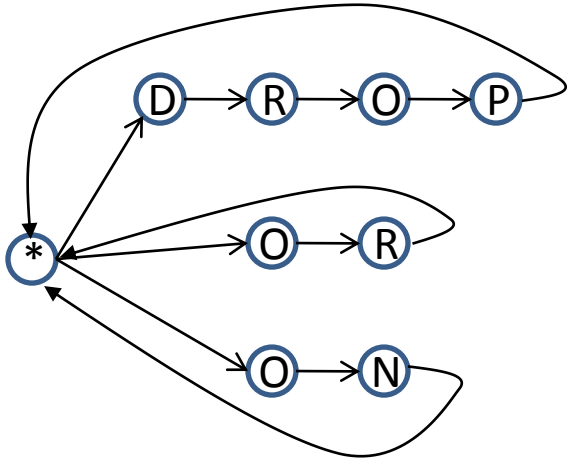
- Loopback from the end of each word



- Alignment finds word boundaries at the dummy node

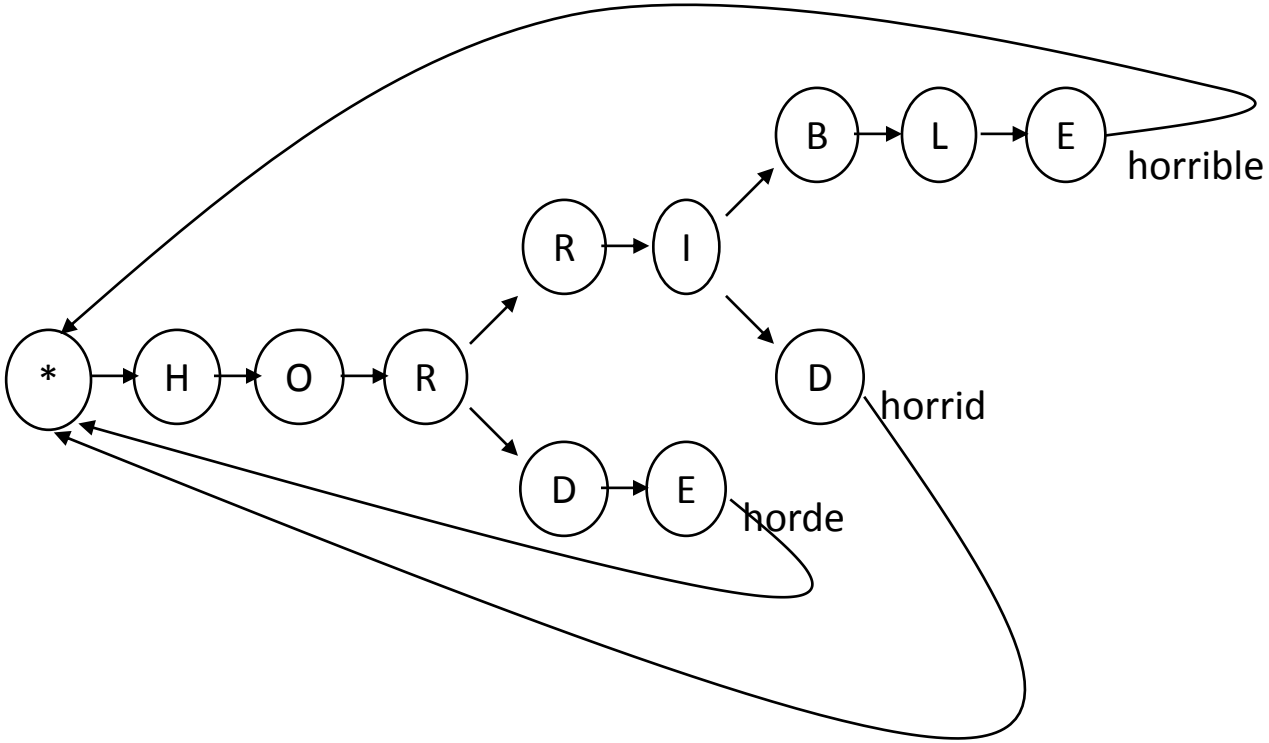
Continuous text: Looping around





- To encourage (or discourage) word boundaries, assign appropriate penalties to loopback edges
  - The red edges
  - By default these are insertion edges
  - Helps decide between "Tothe" == "To The" and "Tothe" == "Tithe"

Continuous Text: Lextree

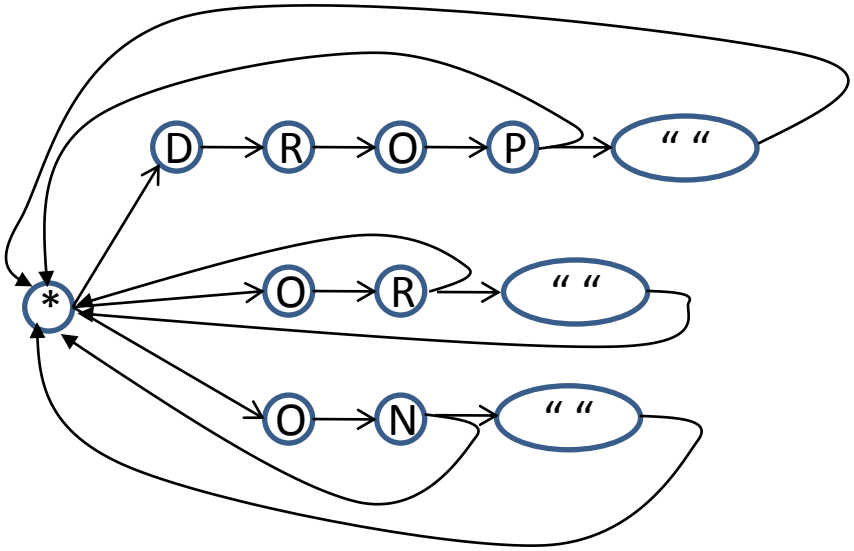


- The trellis can be formed from the loopy lextree
- Loopback arcs always move forward to the next input symbol
  - Cannot represent deletions!

Continuous text with arbitrary spaces

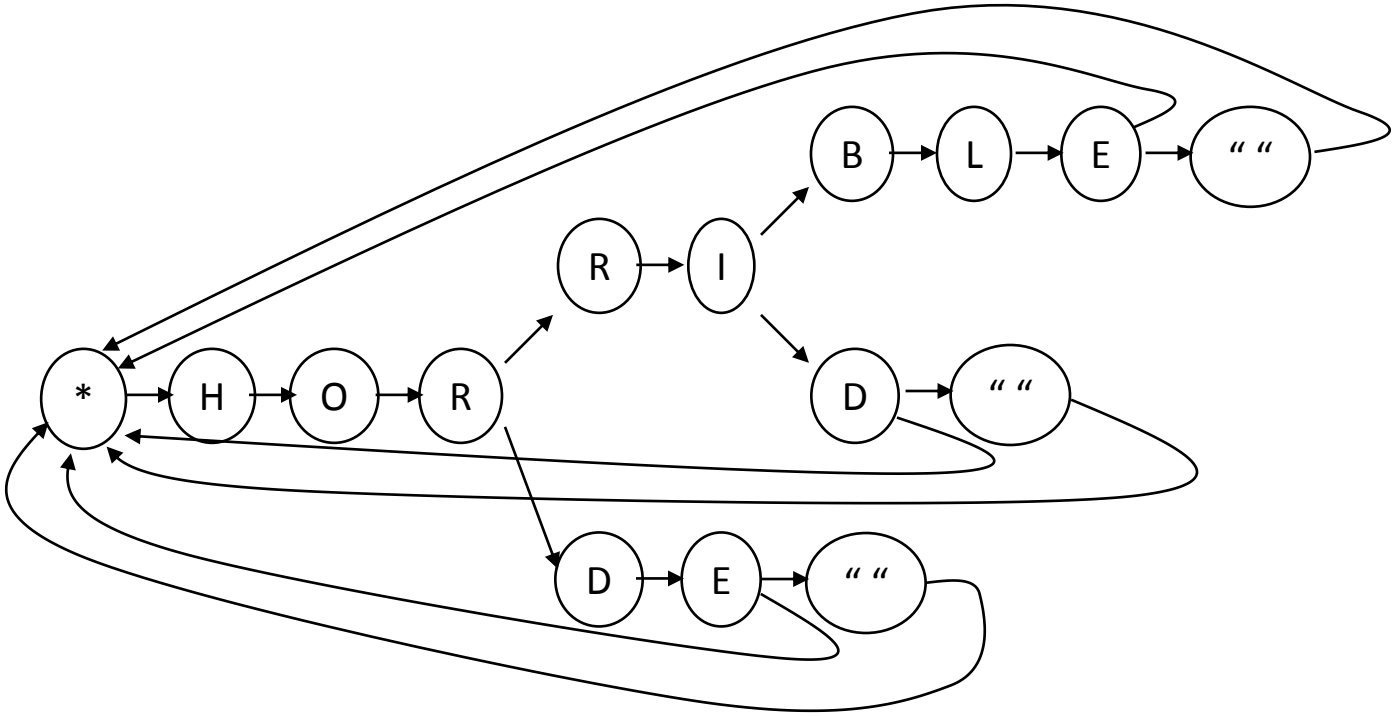
- The methods shown so far permit checking and segmentation (into words) of text without spaces
  - E.g. Iretrunedandsawunnderthhesunthettheraceisnottoth esviftnorthebatletothestrong
- How about text *with* potentially erroneous spaces
  - E.g. I retruned and saw unnder thhe sun thet therace is notto the svift northe batleto the strong

Models with optional spaces



- Flat structure (each chain is a word)
- The spaces are optional

Models with optional spaces



- Lextree (each leaf is a word)
- The spaces are optional

Preview of Topics

- Topics so far: Isolated word recognition

- Today: continuous speech recognition, including:
  - Notion and construction of a *sentence* HMM
  - Review construction of search trellis from sentence HMM (or any graphical model)
  - *Non-emitting* states for simplifying sentence HMM construction
  - Modifying the search trellis for non-emitting states

- To cover later
  - The word-level back-pointer table data structure for efficient retrieval of the best word sequence from the search trellis
  - New pruning considerations: word beams, and absolute pruning
  - Measurement of recognition accuracy or errors
  - The generation of word lattices and N-best lists
    - The A* algorithm and the Viterbi N-best list algorithm

Isolated Word vs Continuous Speech

- A simple way to build a continuous speech recognizer:
  - Learn *Templates* for all possible sentences that may be spoken
  - E.g. record "delete the file" and "save all files" as separate templates
    - For a voice-based UI to an editor
  - Recognize entire sentences (no different from isolated word recognition)

- **Problem:** Extremely large number of sentences possible
  - Even a simple digit recognizer for phone numbers: A billion possible phone numbers!
  - Cannot record every possible phone number as template

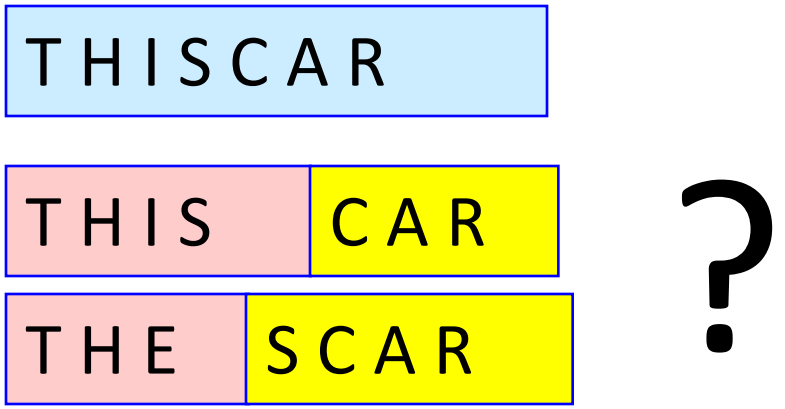
Templates for "Sentences"

- Recording entire sentences as "templates" is a reasonable idea
- But quickly becomes infeasible as the number of sentences increases
- Inflexible: Cannot recognize sentences for which no template has been recorded

Other Issues with Continuous Speech

- Much greater variation in speaking rate
  - Having to speak with pauses forces one to speak more uniformly
  - Greater variation demands better acoustic models for accuracy
- More pronounced contextual effects
  - Pronunciation of words influenced by neighboring words
    - "Did you" -> "Dijjou"
- Spontaneous (unrehearsed) speech may include mispronunciations, false-starts, non-words (*e.g.* umm and ahh)
  - Need templates for all pronunciation and disfluency variants

Treat it as a series of isolated word recognition problems?



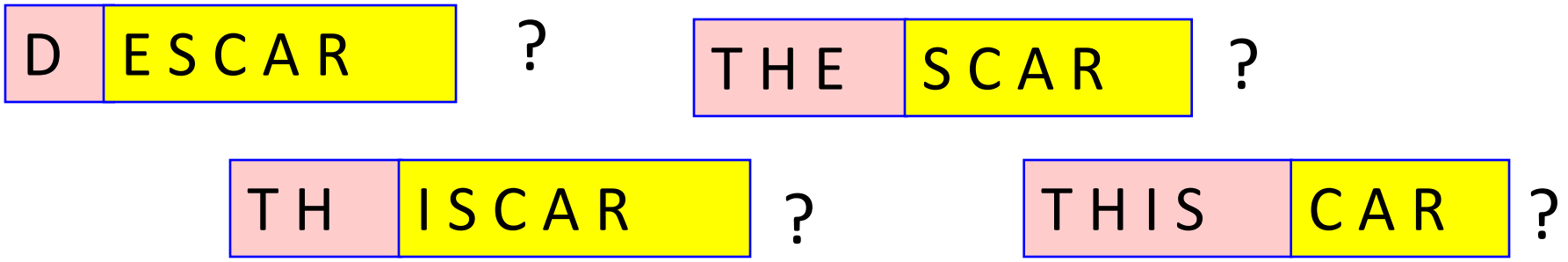
- Record only *word* templates
  - Segment recording into words, recognize individual words

- But how do we choose word boundaries?
  - Choosing different boundaries affects the results
    - *E.g. "This car"* or "*This scar*"? *"The screen"* or "*This green*"?

- Similar to reading text without spaces:

  ireturnedandsawunderthesunthattheraceisnottotheswiftnorthebattletothestrongneitheryetbreadt
  othewisenoryetrichestomenofunderstandingnoryetfavourtomenofskillbuttimeandchancehappe
  nethtothemall

Recording only Word Templates



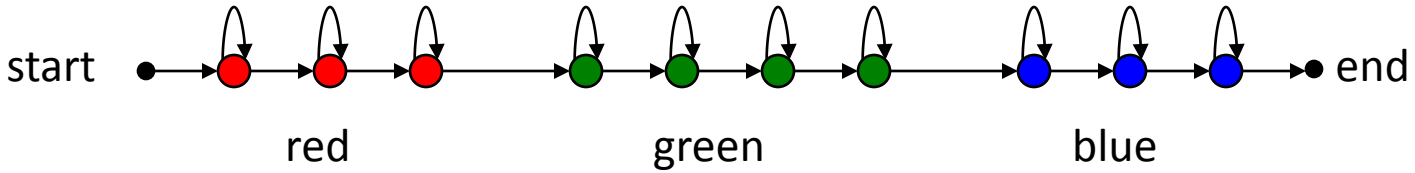
- Brute force: Consider all possibilities
  - Segment recording in every possible way
  - Run isolated word recognition on each segment
  - Select the segmentation (and recognition) with the lowest total cost of match
    - I.e. cost of best match to first segment + cost of best match to second..
- Quickly gets very complex as the number of words increases
  - Combinatorially high number of segmentations
  - Compounded by fact that number of words is unknown

A Simple Solution

- Build/Record word templates
- *Compose* sentence templates from word templates
- Composition can account for all variants, disfluencies etc.
  - We will see how..

Building Sentence Templates

- Build *sentence HMM*s by concatenating the HMMs for the individual words
  - *e.g.* sentence "red green blue"



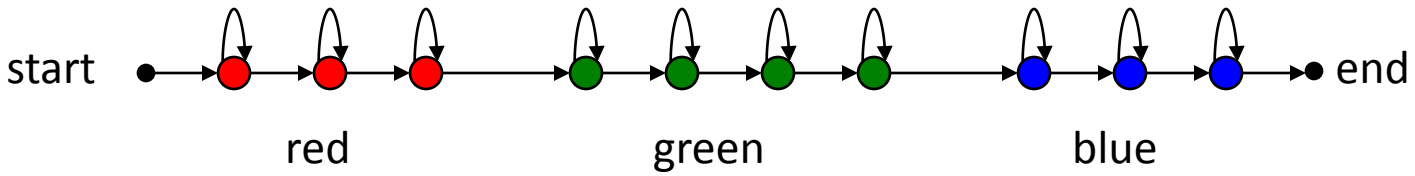
  - The sentence HMM looks no different from a word HMM
  - Can be evaluated just like a word HMM

- Caveat: Must have good models for the individual words
  - Ok for a limited vocabulary application
    - *E.g.* command and control application, such as robot control

Handling Silence

- People often pause between words in continuous speech
  - Often, but not always!
  - Not predictable when there will be a pause

- The composed sentence HMM fails to allow silences in the spoken input

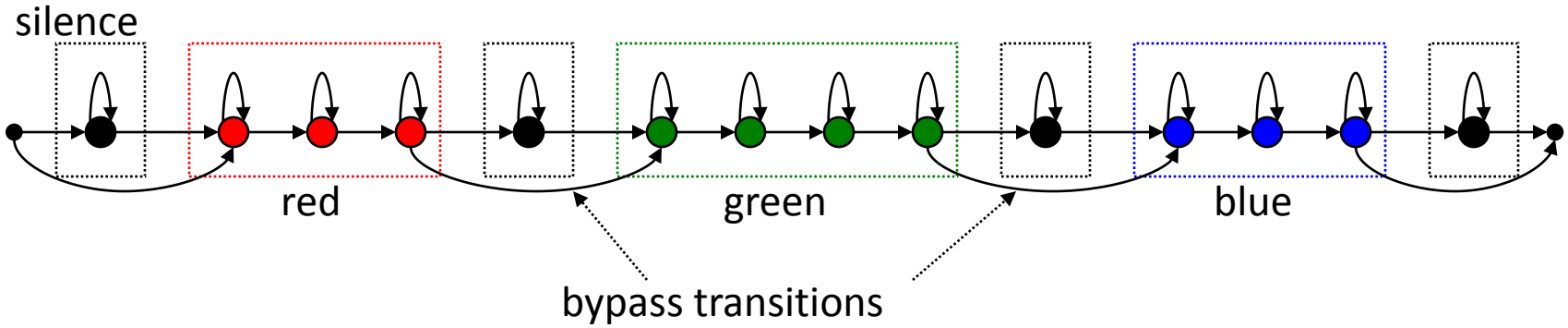


  - If the input contained "[silence] red green [silence] blue [silence]", it would match badly with the sentence HMM

- Need to be able to handle *optional* pauses between words
  - Like spaces between words

Sentence HMM with Optional Silences

- Optional silences can be handled by adding a *silence HMM* between every pair of words, but with a *bypass*:

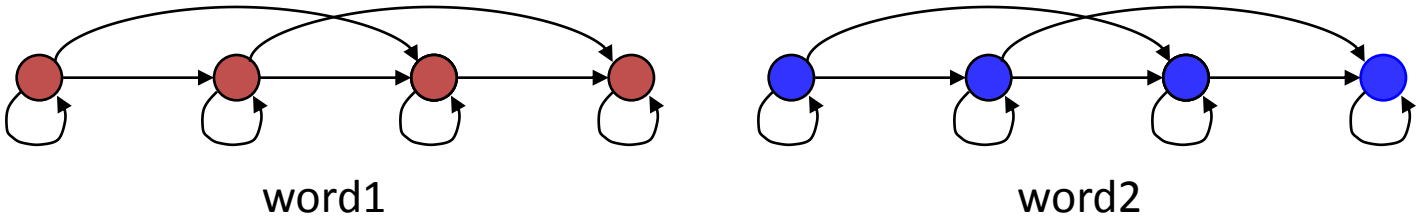


- The "bypass" makes it optional: The person may or may not pause
  - If there is a pause, the best match path will go through the silence HMM
  - Otherwise, it will be bypassed

- The "silence" HMM must be separately trained
  - On examples of recordings with no speech in them (not strictly silence)

Composing HMMs for Word Sequences

- Given HMMs for word1 and word2
  - Which are both Bakis topology

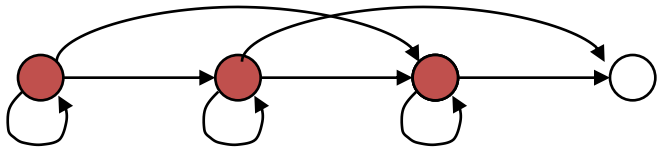


- How do we compose an HMM for the word sequence "word1 word2"
  - Problem: The final state in this model has only a self-transition
  - According the model, once the process arrives at the final state of word1 (for example) it never leaves
  - There is no way to move into the next word

Introducing the Non-emitting state

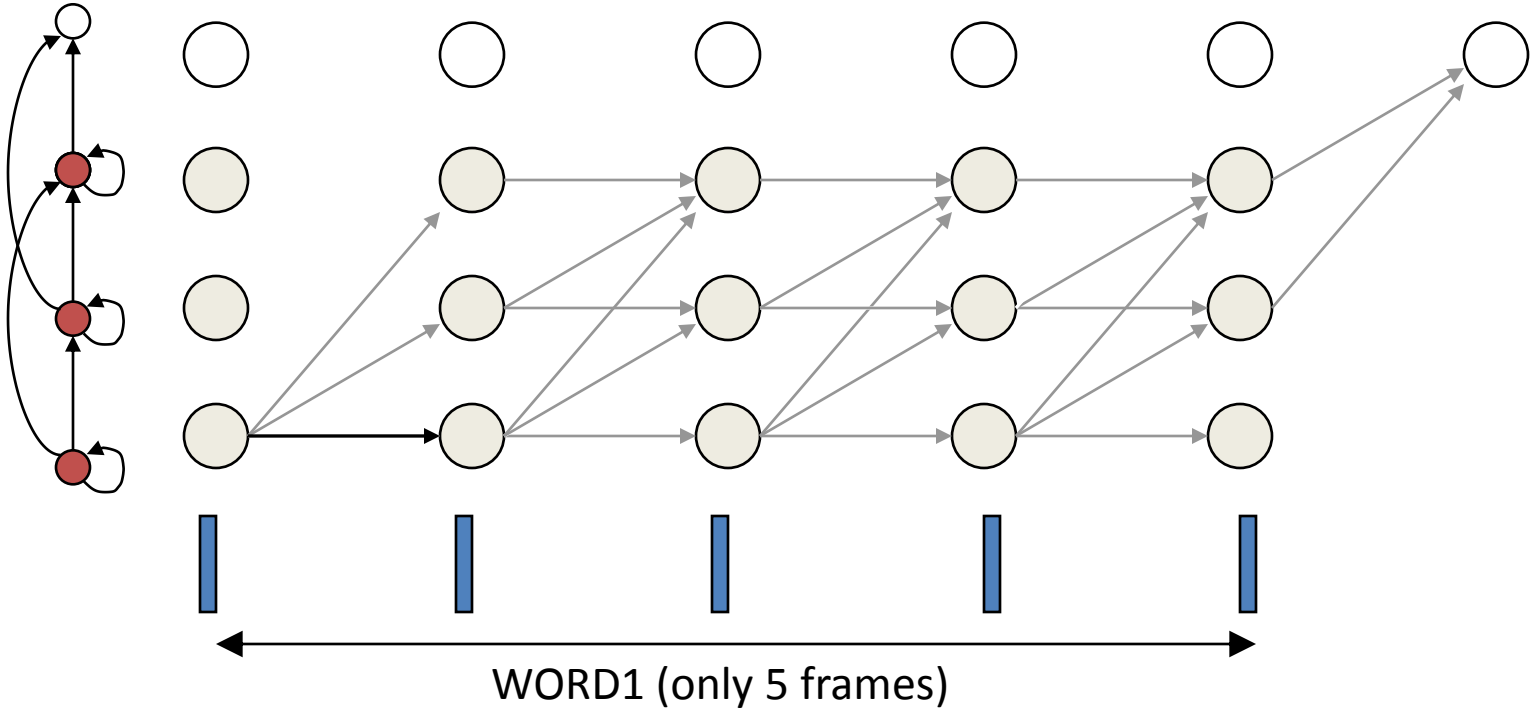
- So far, we have assumed that every HMM state models some output, with some output probability distribution
- Frequently, however, it is useful to include model states that do *not* generate any observation
  - To simplify connectivity

- Such states are called *non-emitting* states or sometimes *null* states
- *NULL STATES CANNOT HAVE SELF TRANSITIONS*
- Example: A word model with a final null state



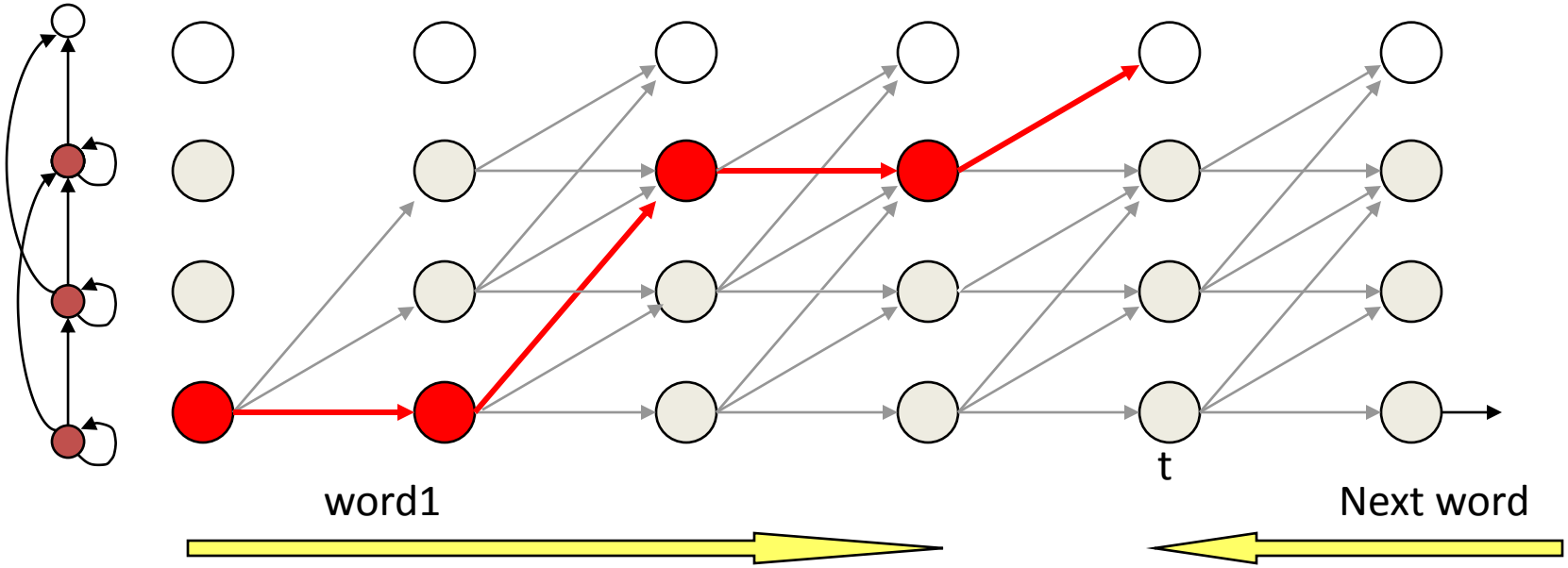
HMMs with NULL Final State

- The final NULL state changes the trellis
  - The NULL state cannot be entered or exited within the word



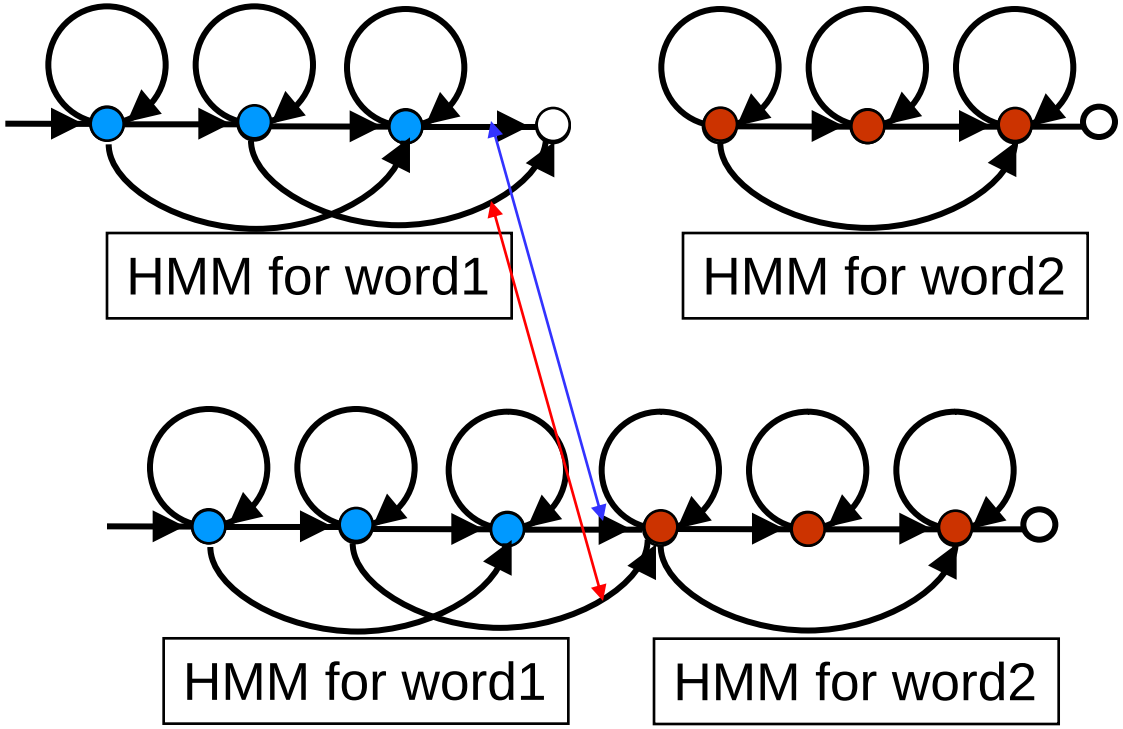
- If there are exactly 5 vectors in word 5, the NULL state may only be visited after all 5 have been scored

The NULL final state



- The probability of transitioning into the NULL final state at any time *t* is the probability that the observation sequence for the word will end at time *t*
- Alternately, it represents the probability that the observation will exit the word at time *t*

Connecting Words with Final NULL States

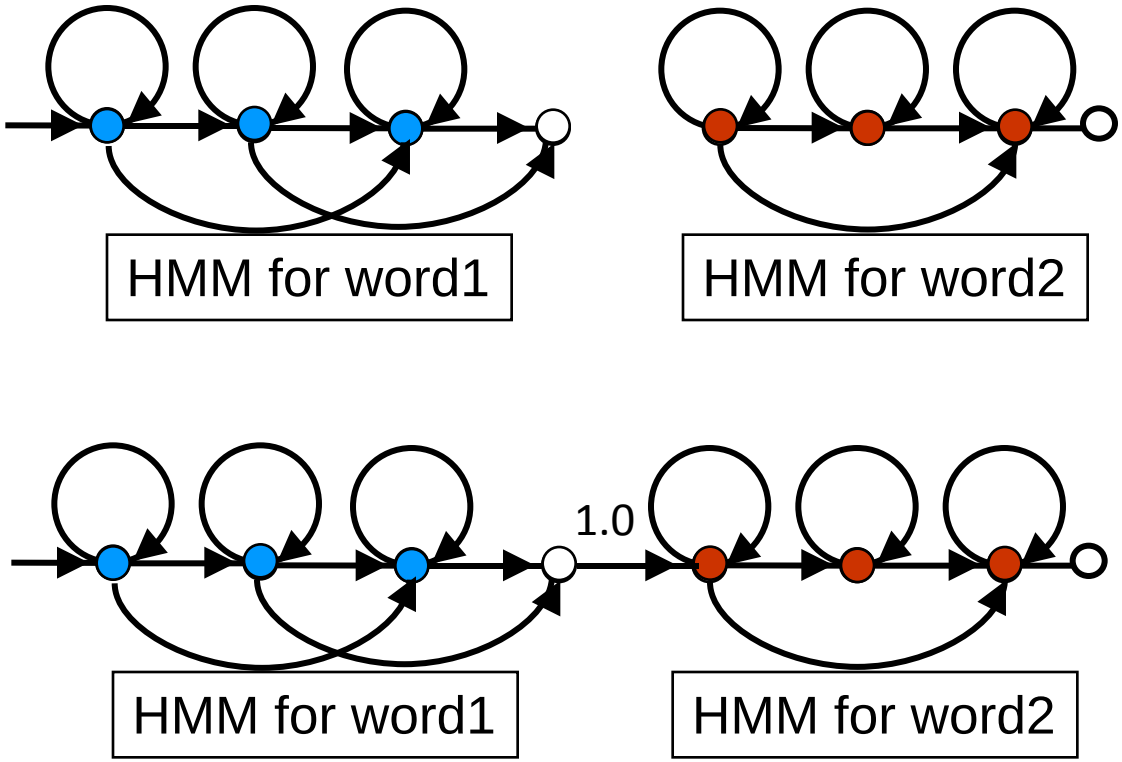


- The probability of leaving word 1 (i.e the probability of going to the NULL state) is the same as the probability of entering word2
  - The transitions pointed to by the two ends of each of the colored arrows are the same

Retaining a non-emitting state between words

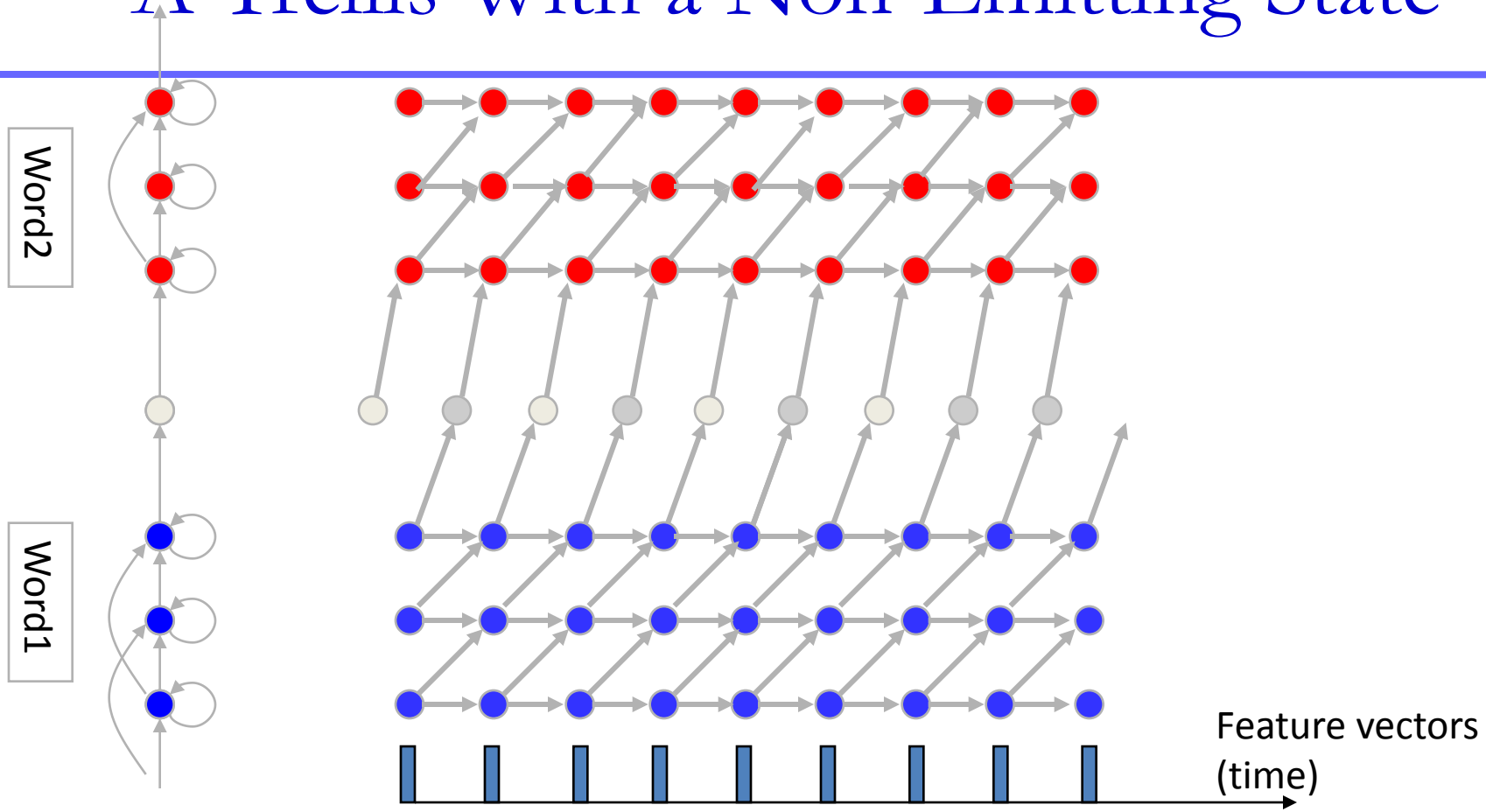
- In some cases it may be useful to retain the non-emitting state as a connecting state
  - The probability of entering word 2 from the non-emitting state is 1.0
  - This is the only transition allowed from the non-emitting state

Retaining the Non-emitting State



HMM for the word sequence “word2 word1”

A Trellis With a Non-Emitting State

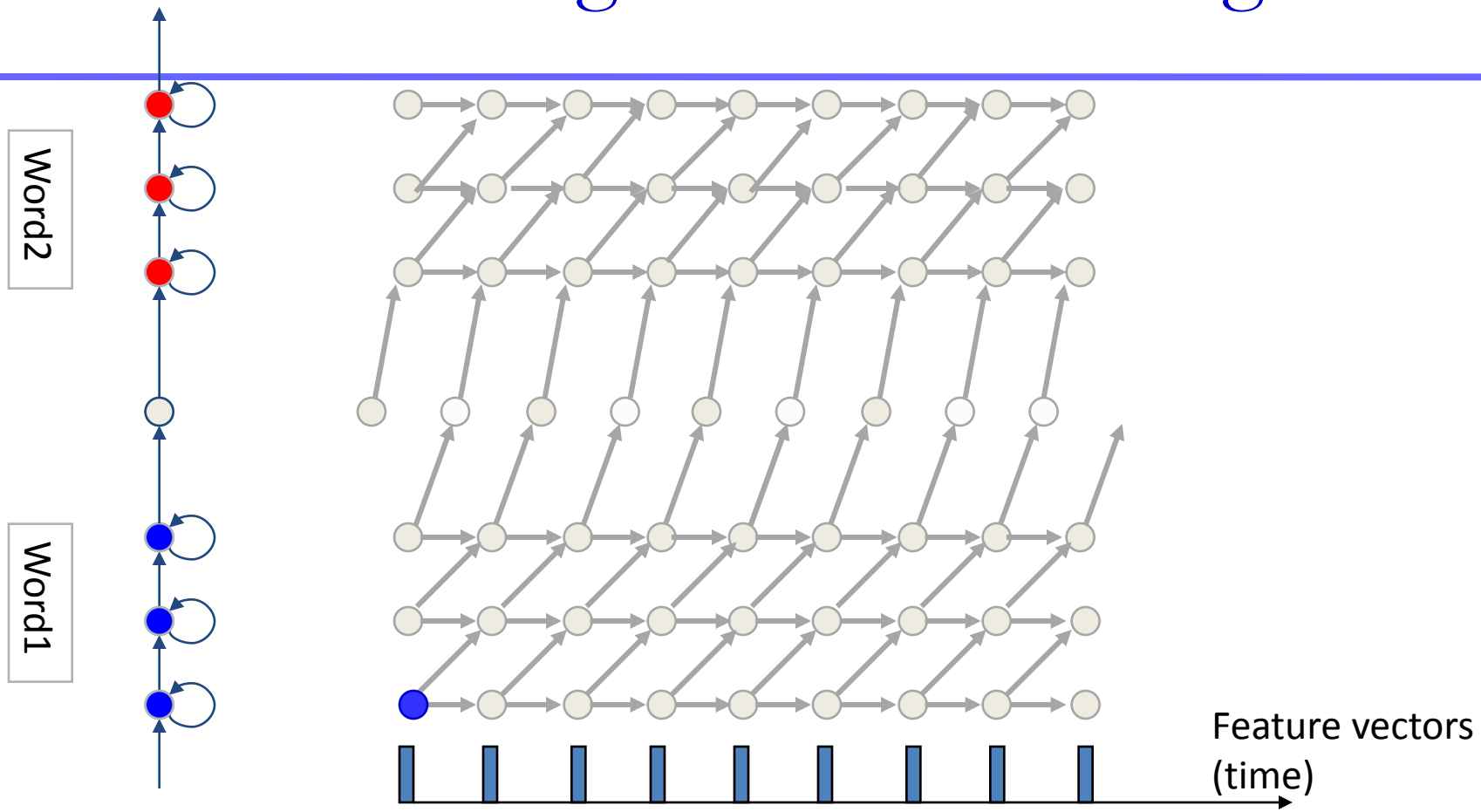


- Since non-emitting states are not associated with observations, they have no "time"
  - In the trellis this is indicated by showing them *between* time marks
  - Non-emitting states have no horizontal edges – they are always exited instantly

Viterbi with Non-emitting States

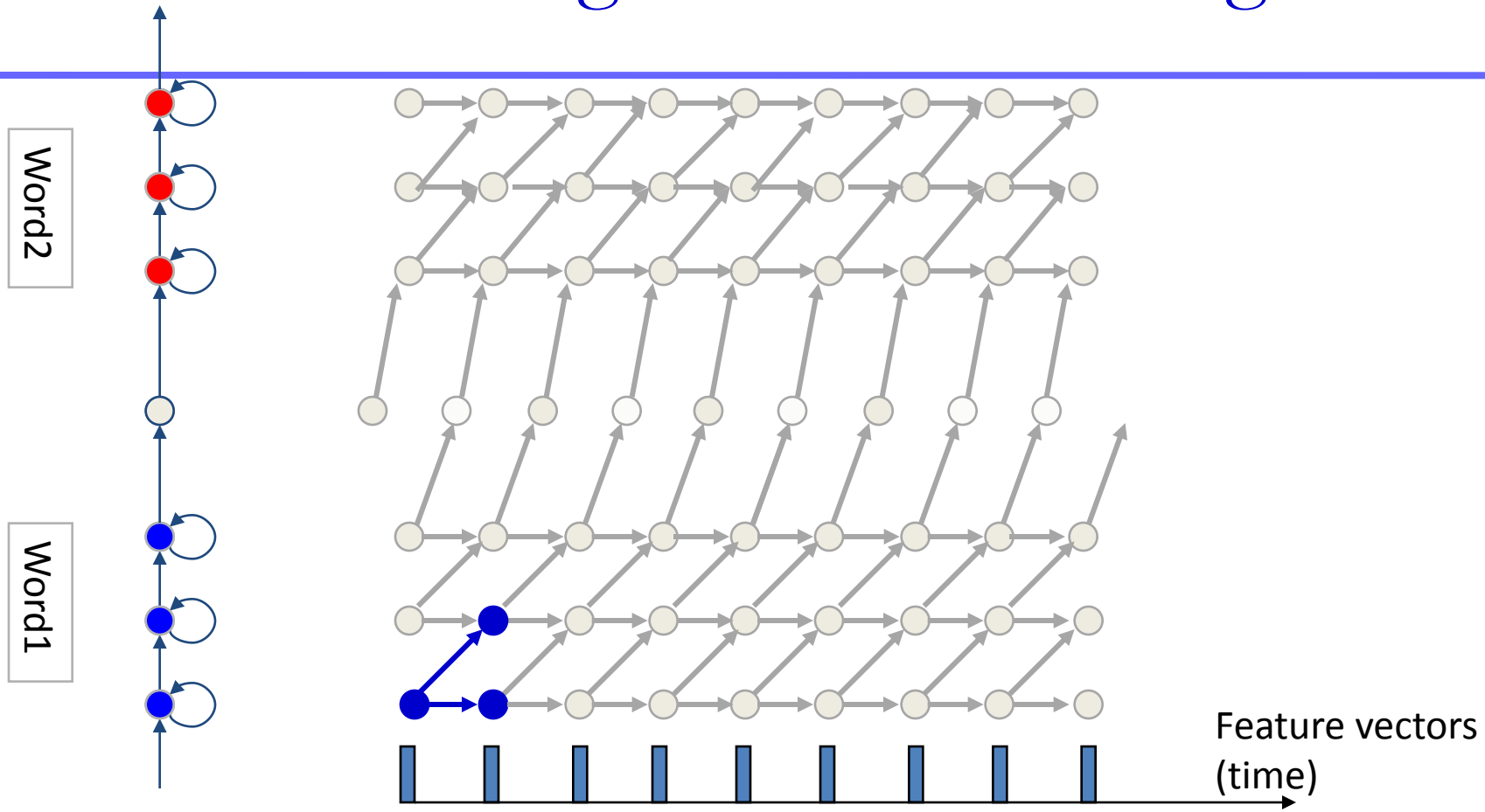
- Non-emitting states affect Viterbi decoding
  - The process of obtaining state segmentations
- This is critical for the actual recognition algorithm for word sequences

Viterbi through a Non-Emitting State



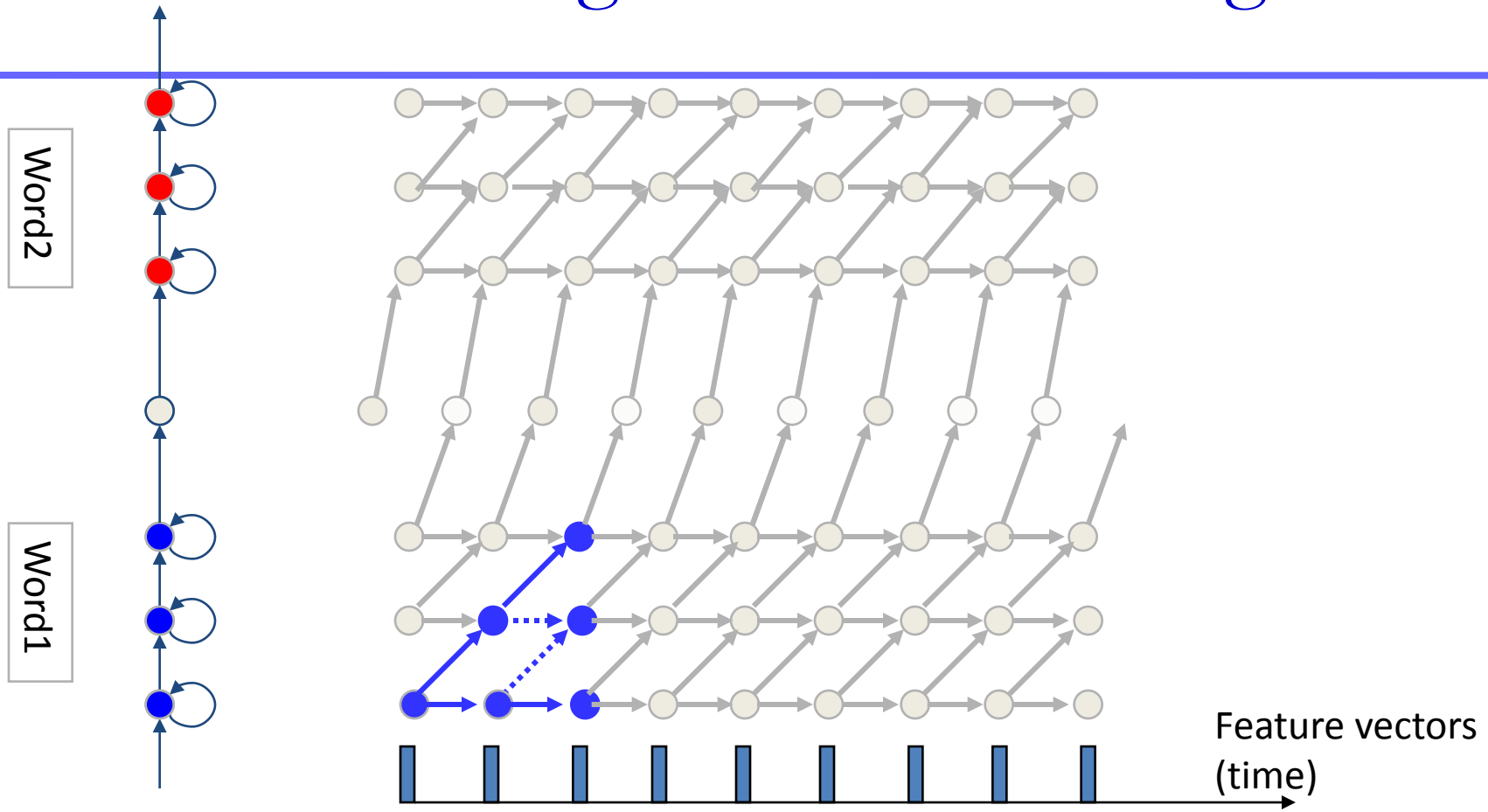
- At the first instant only the first state may be entered

Viterbi through a Non-Emitting State



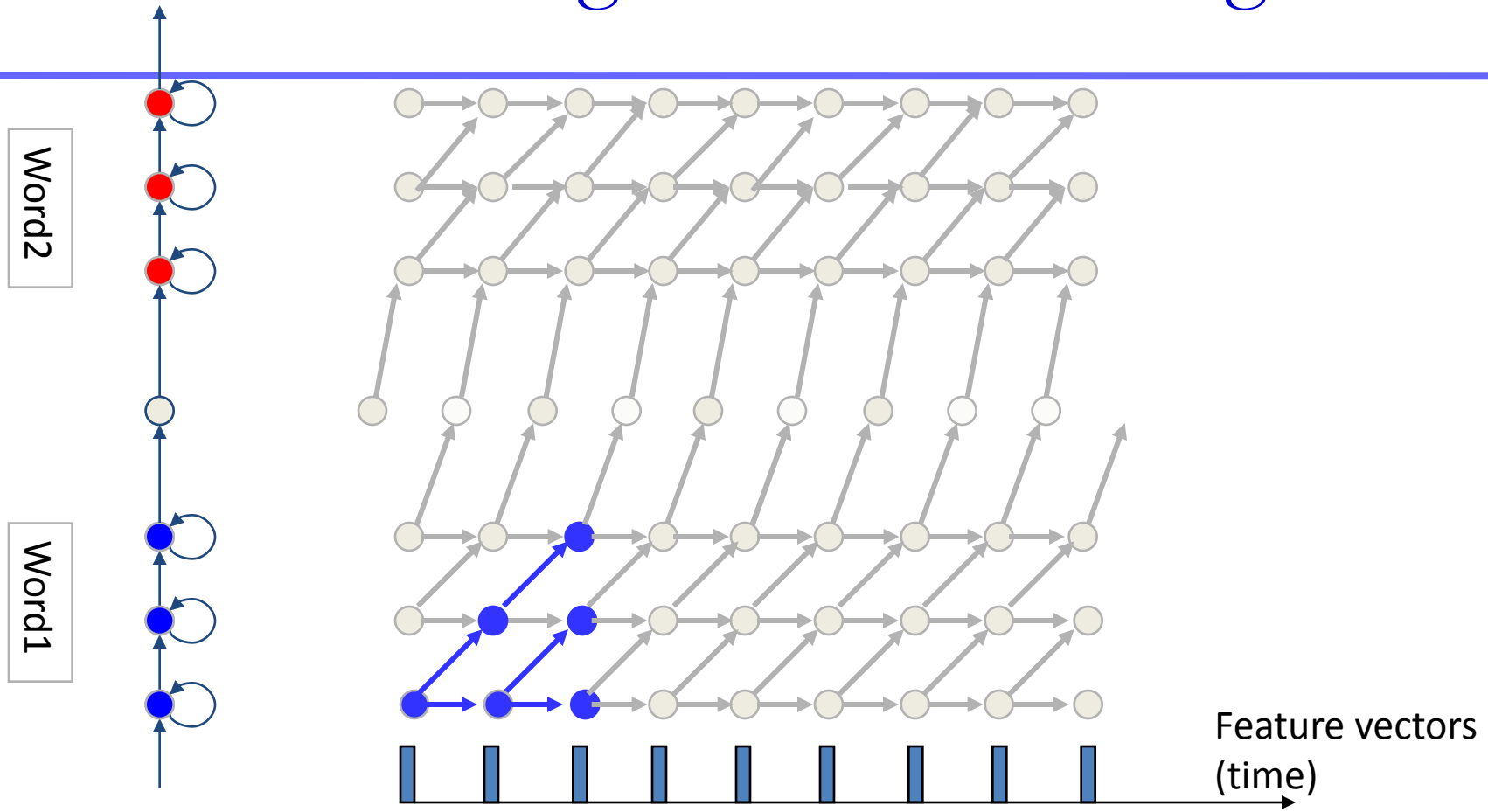
- At t=2 the first two states have only one possible entry path

Viterbi through a Non-Emitting State



- At t=3 state 2 has two possible entries. The best one must be selected

Viterbi through a Non-Emitting State



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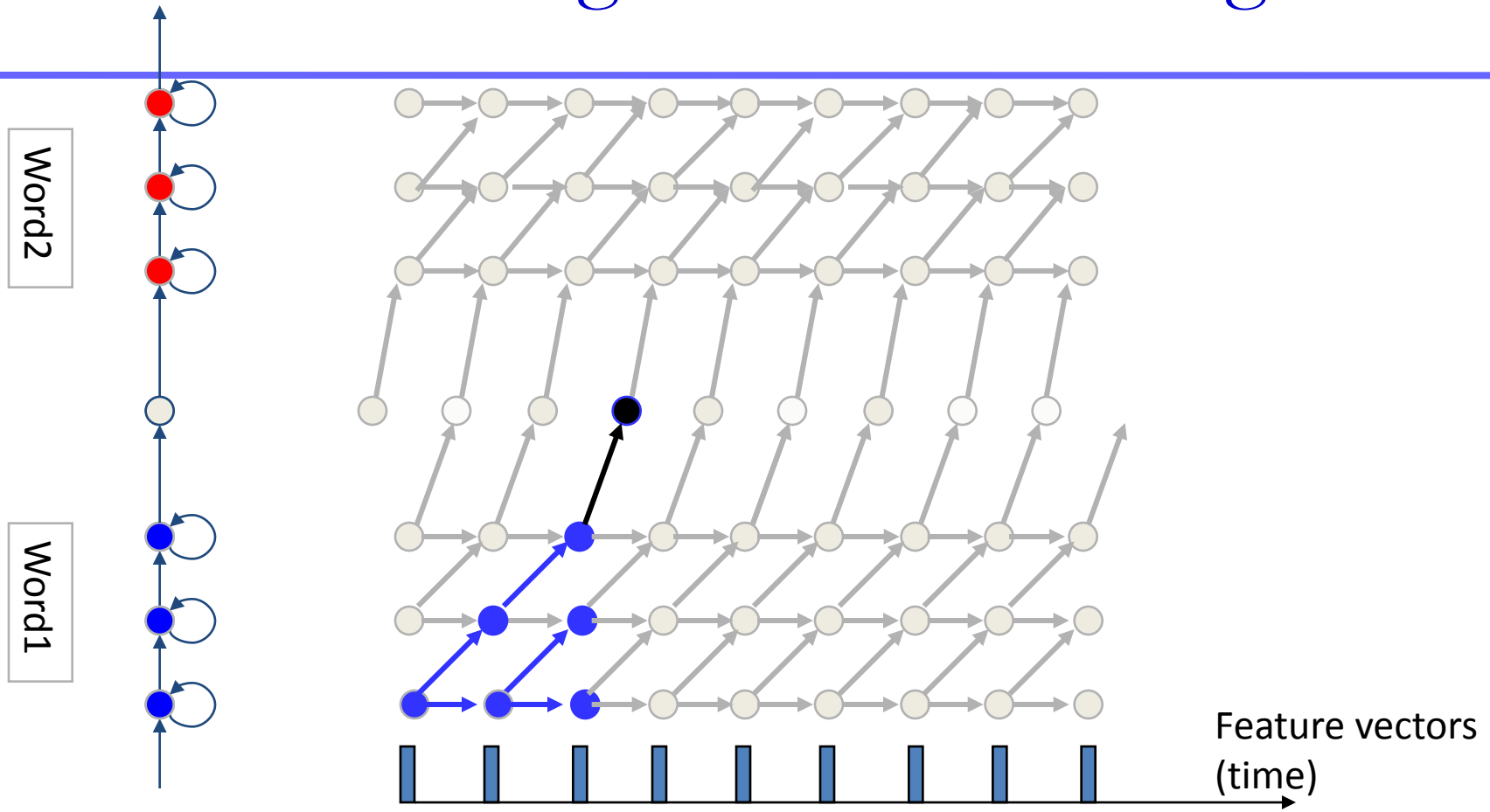
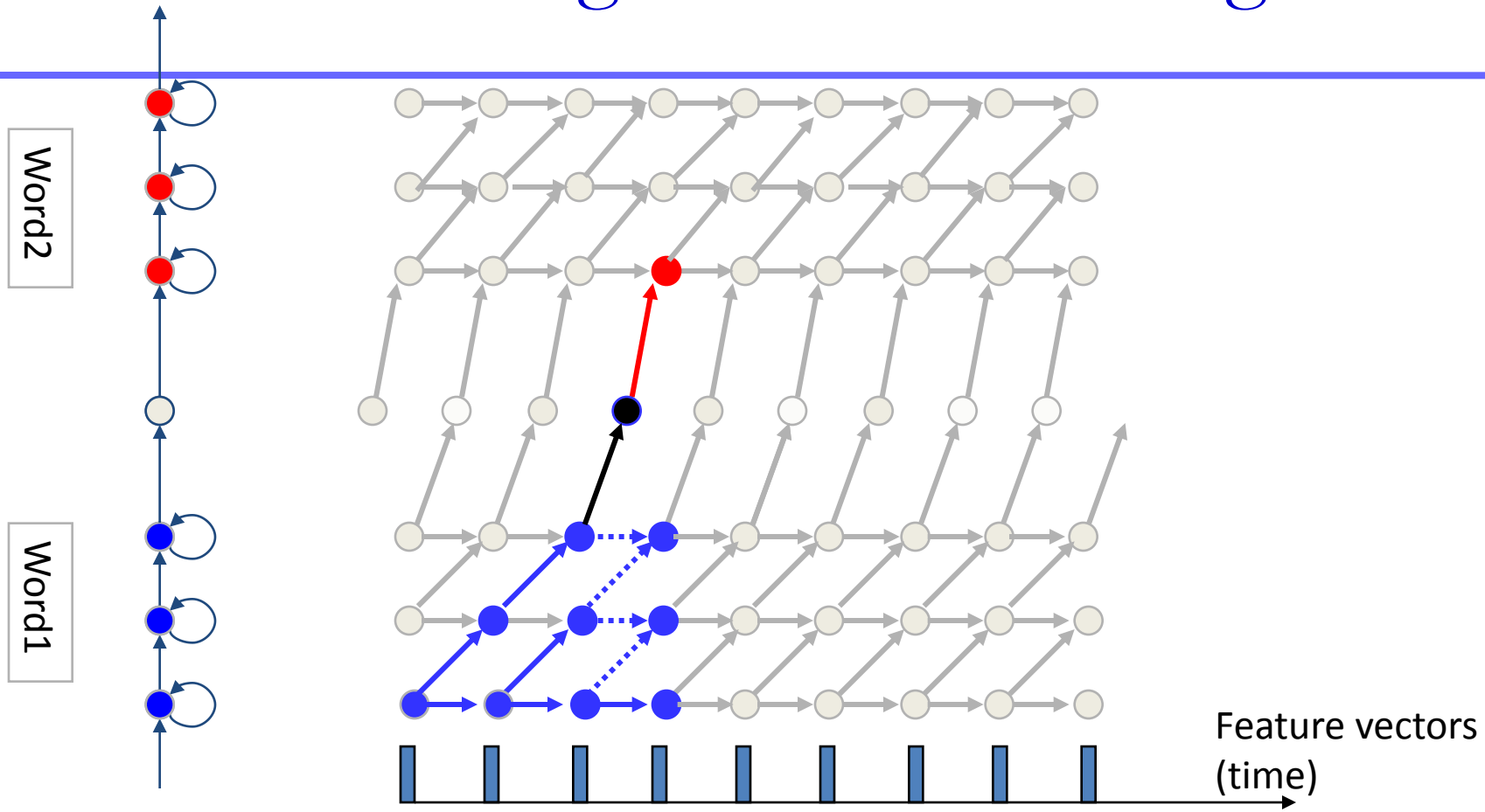


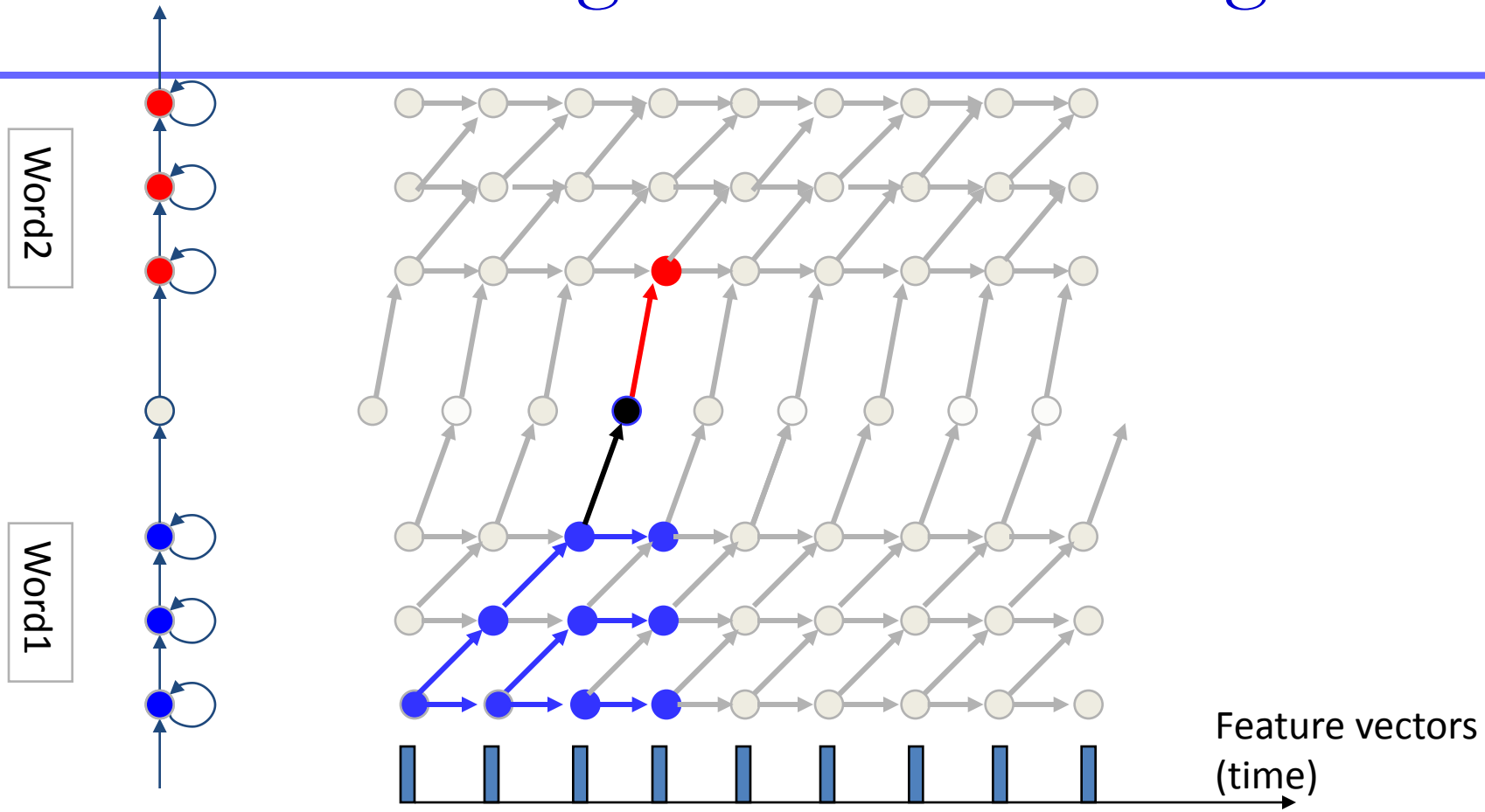
- After the third time instant we an arrive at the non-emitting state. Here there is only one way to get to the non-emitting state

Viterbi through a Non-Emitting State



- Paths exiting the non-emitting state are now in word2
  - States in word1 are still active
  - These represent paths that have not crossed over to word2

Viterbi through a Non-Emitting State



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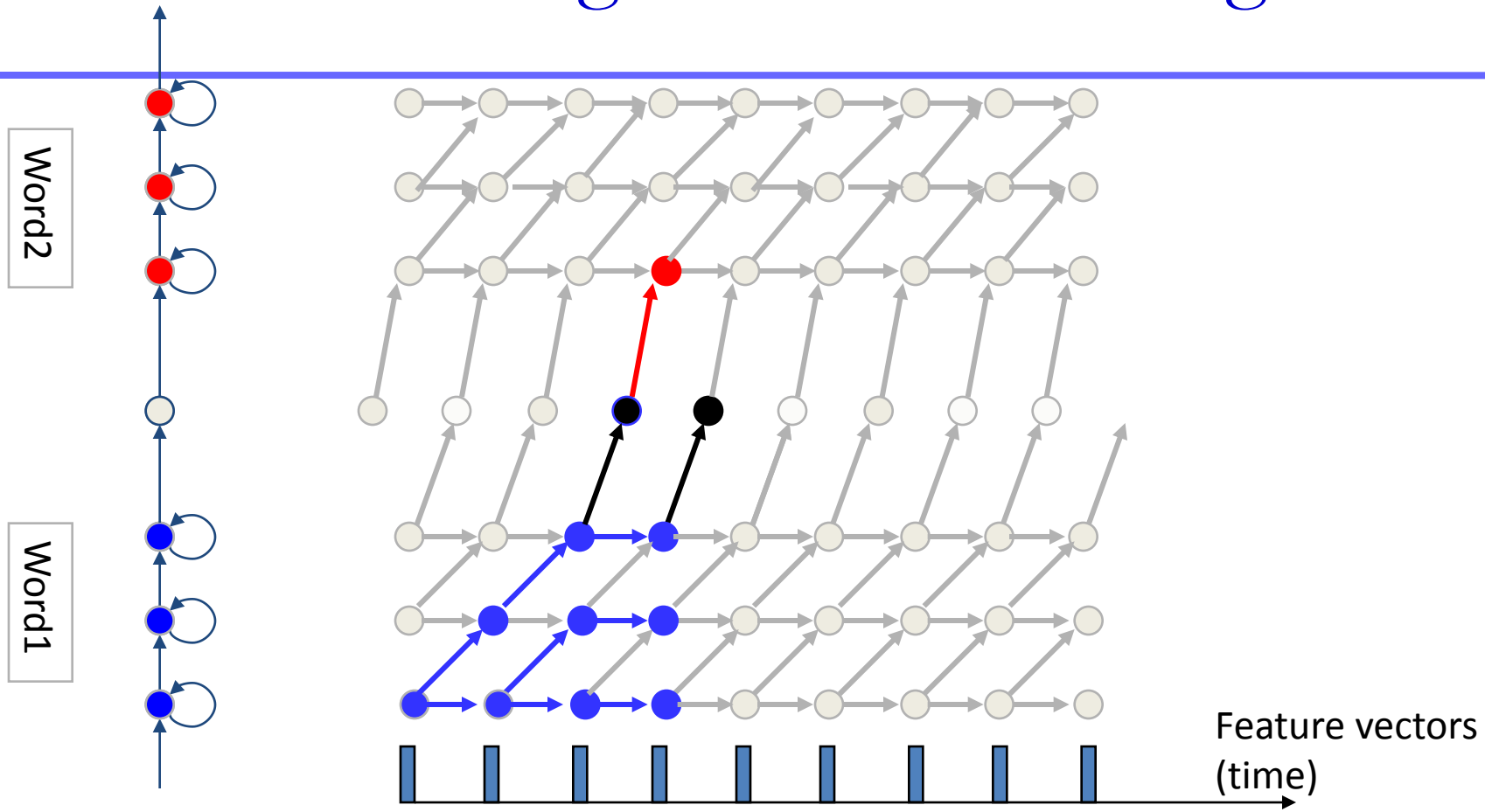
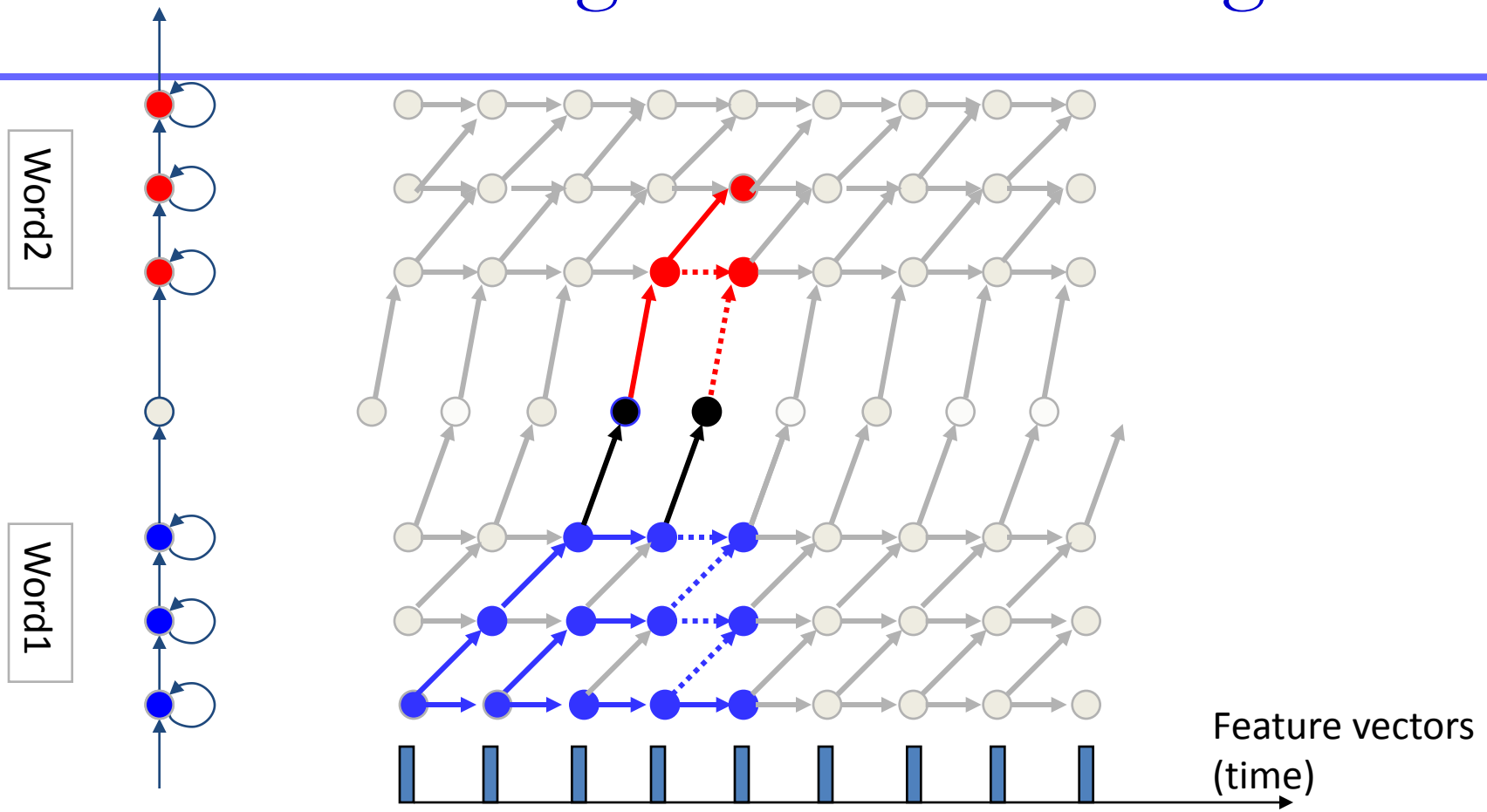
Viterbi through a Non-Emitting State



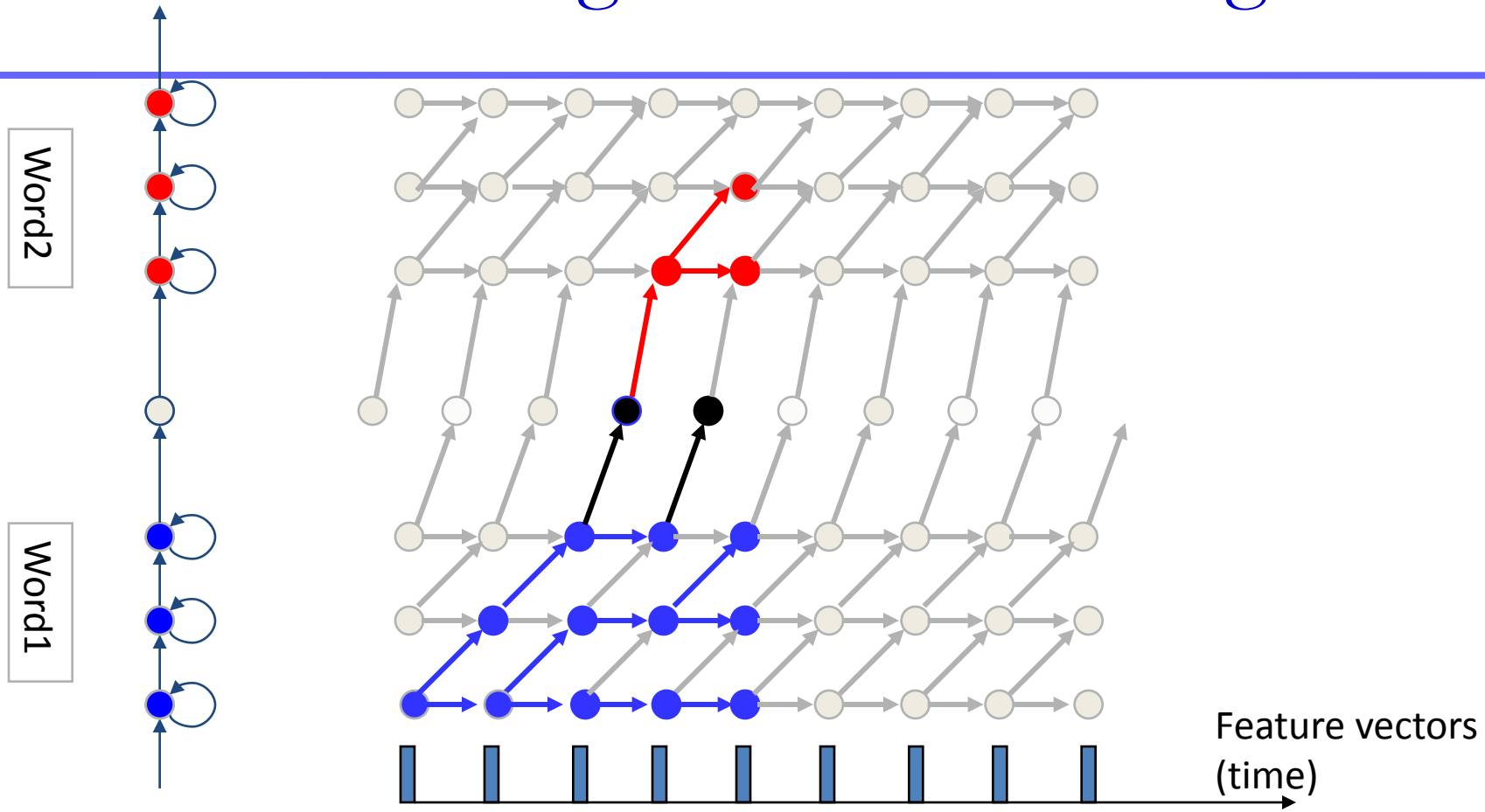
- The non-emitting state will now be arrived at after every observation instant

Viterbi through a Non-Emitting State



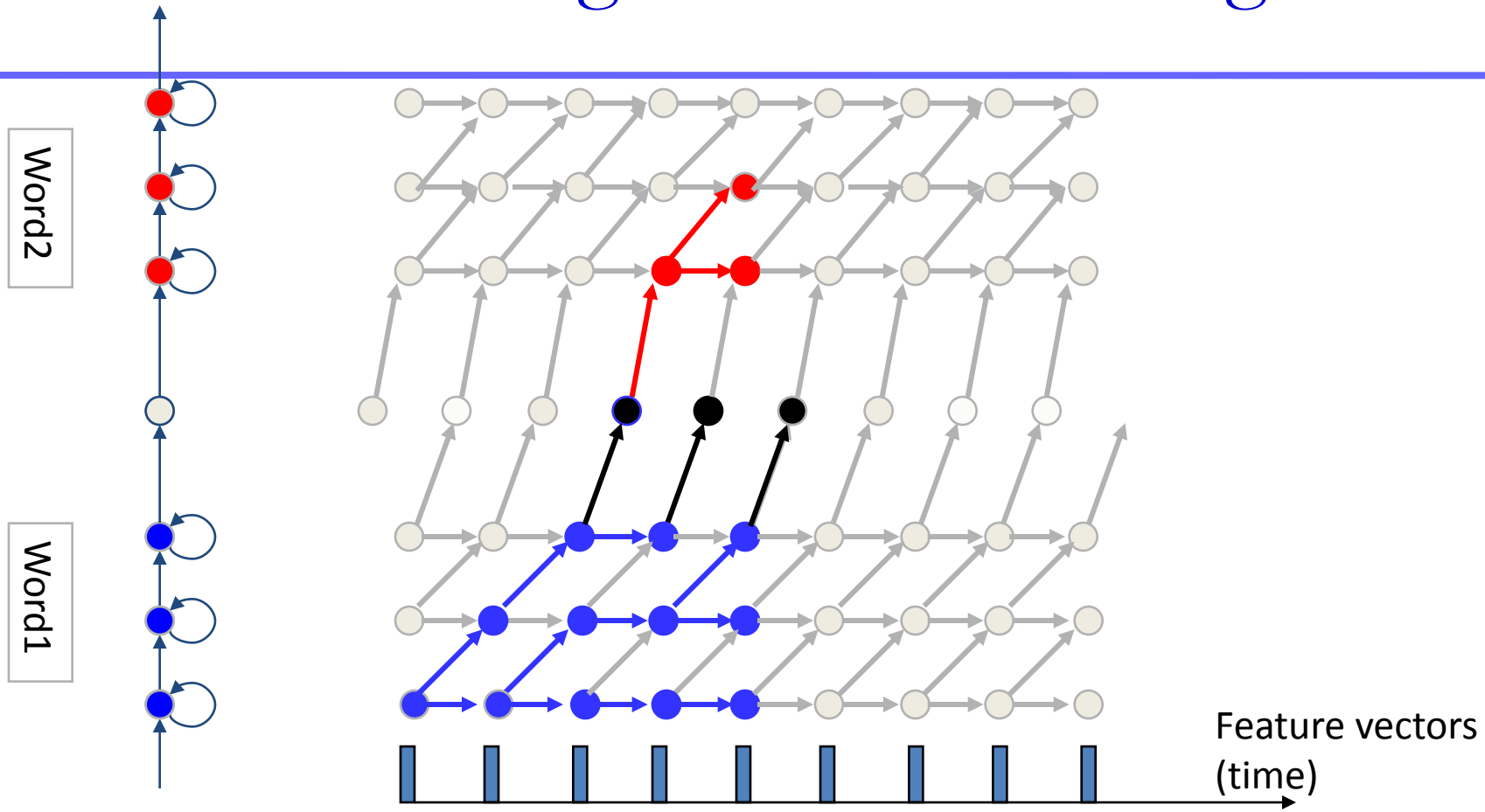
- "Enterable" states in word2 may have incoming paths either from the "cross-over" at the non-emitting state or from within the word
  - Paths from non-emitting states may compete with paths from emitting states

Viterbi through a Non-Emitting State



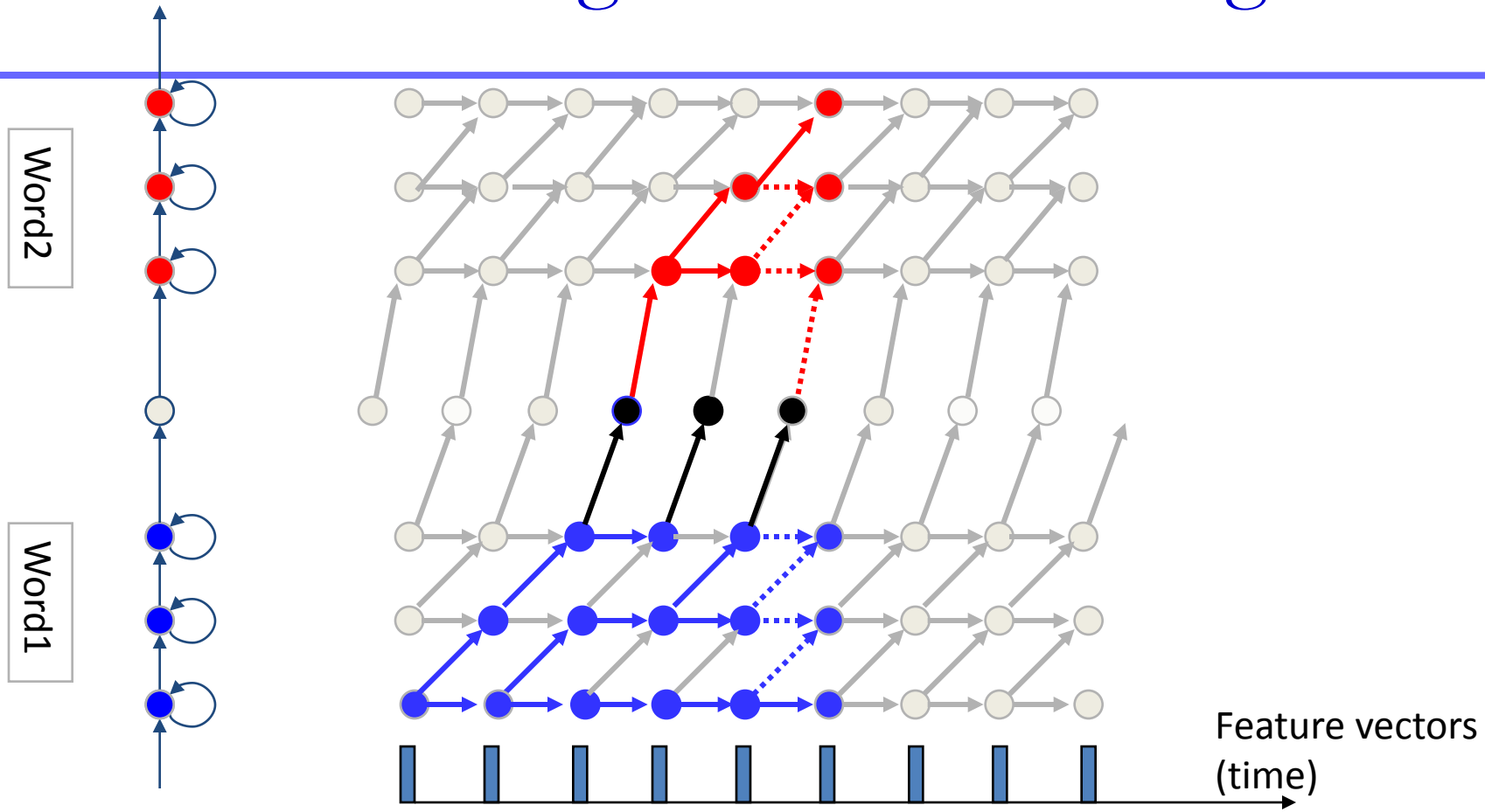
- Regardless of whether the competing incoming paths are from emitting or non-emitting states, the best overall path is selected

Viterbi through a Non-Emitting State



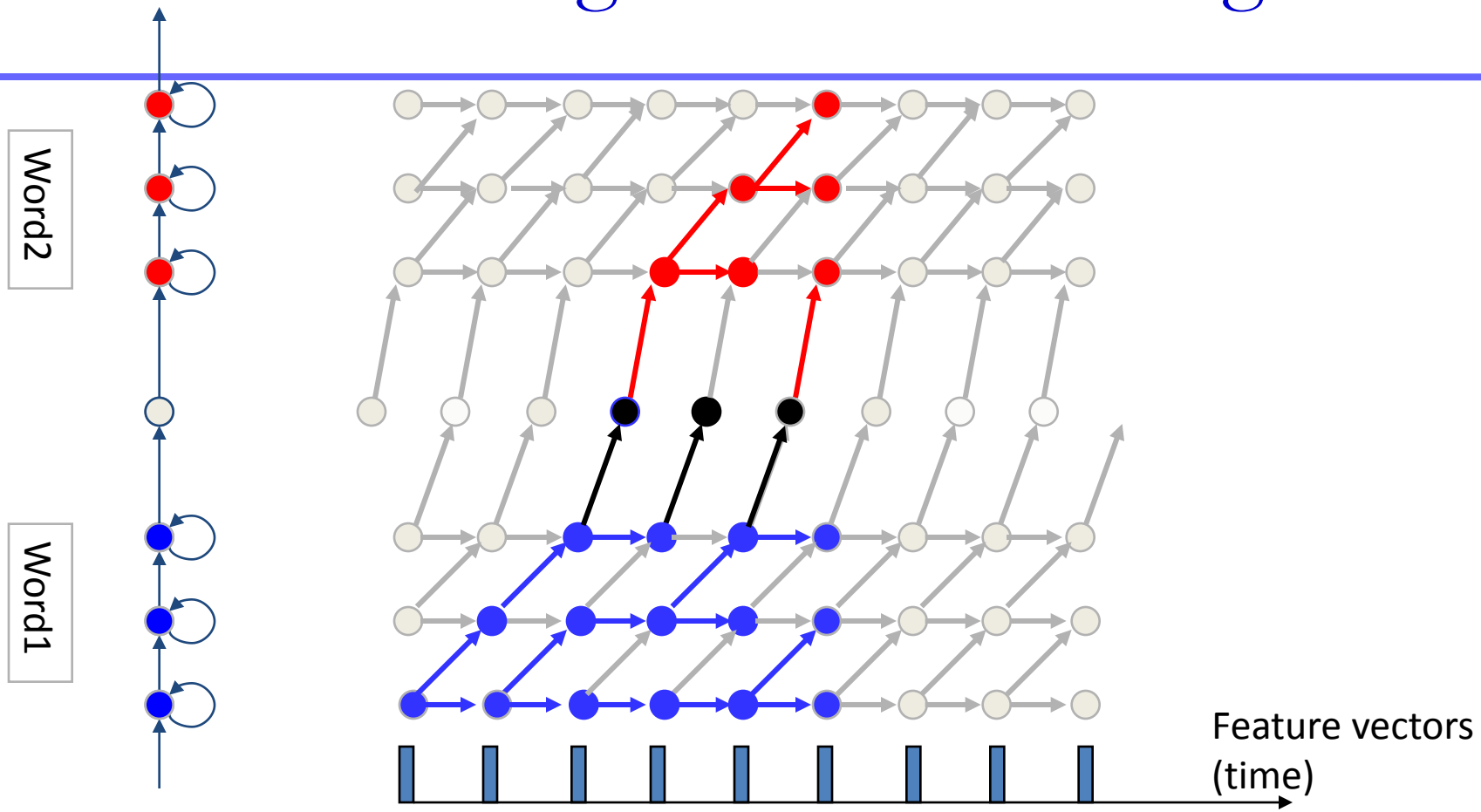
- The non-emitting state can be visited after every observation

Viterbi through a Non-Emitting State



- At all times paths from non-emitting states may compete with paths from emitting states

Viterbi through a Non-Emitting State



- At all times paths from non-emitting states may compete with paths from emitting states
  - The best will be selected
  - This may be from either an emitting or non-emitting state

Viterbi with NULL states

- Competition between incoming paths from emitting and non-emitting states may occur at both emitting and non-emitting states
- The best path logic stays the same. The only difference is that the current observation probability is factored into emitting states
- Score for emitting state (as probabilities)

$$P_u(s,t) = P(x_{u,t} \mid s) \max_{s'} \left(P_u(s',t-1) P(s \mid s') \mid_{s' \in \{emitting\}}, P_u(s',t) P(s \mid s') \mid_{s' \in \{nonemitting\}} \right)$$

- Score for non-emitting state

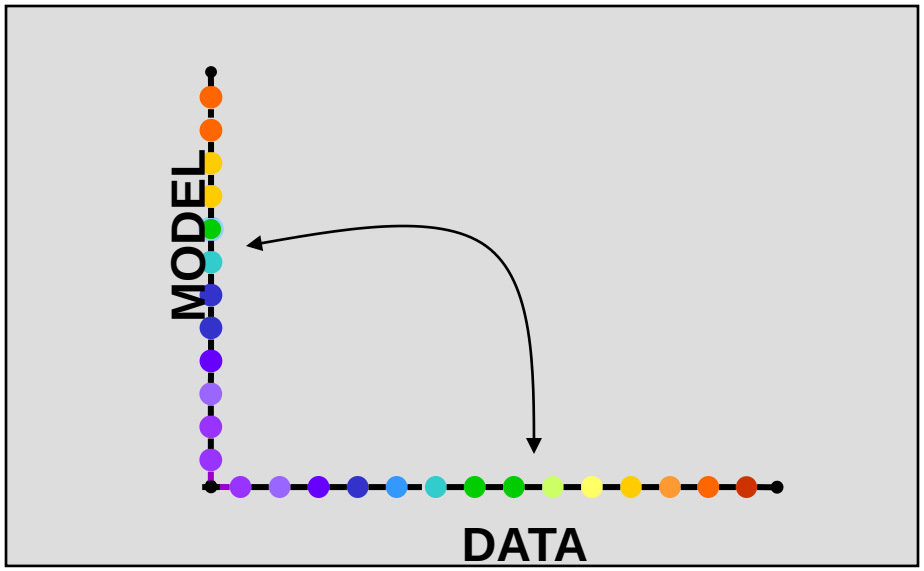
$$P_u(s,t) = \max_{s'} \left(P_u(s',t-1) P(s \mid s') \mid_{s' \in \{emitting\}}, P_u(s',t) P(s \mid s') \mid_{s' \in \{nonemitting\}} \right)$$

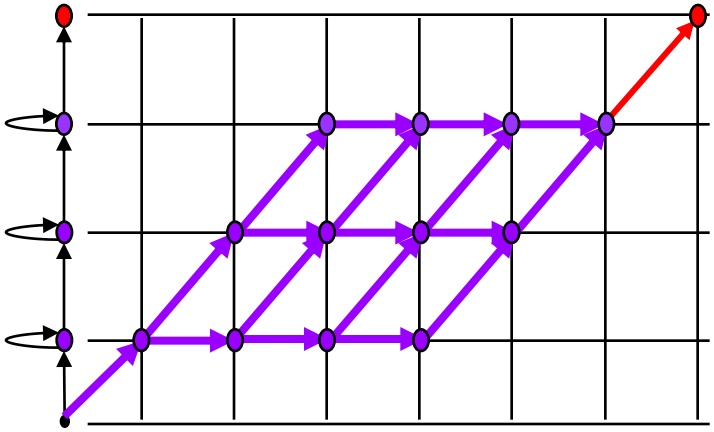
- Using log probabilities

$$\log\left(P_u(s,t)\right) = \log\left(P(x_{u,t} \mid s)\right) + \max_{s'} \left(\log\left(P_u(s',t-1)\right) + \log\left(P(s \mid s')\right) \mid_{s' \in \{emitting\}}, \log\left(P_u(s',t)\right) + \log\left(P(s \mid s')\right) \mid_{s' \in \{nonemitting\}} \right)$$

$$\log\left(P_u(s,t)\right) = \max_{s'} \left(\log\left(P_u(s',t-1)\right) + \log\left(P(s \mid s')\right) \mid_{s' \in \{emitting\}}, \log\left(P_u(s',t)\right) + \log\left(P(s \mid s')\right) \mid_{s' \in \{nonemitting\}} \right)$$

Speech Recognition as String Matching





- We find the distance of the data from the "model" using the Trellis for the word
- Pick the word for which this distance is lowest
- Word = argmin $_{word}$ distance(data, model(word))
- Using the DTW / HMM analogy
  - Word = argmax $_{word}$ probability(data | model(word))
    - Alternately, argmax$_{word}$ logprobability(data | model)
      - Alternately still: argmin$_{word}$ –logprobability(data | model)

Speech Recognition as Bayesian Classification

- Different words may occur with different frequency
  - E.g. a person may say "SEE" much more frequently than "ZEE"
- This must be factored in
  - If we are not very sure they said "SEE" or "ZEE", choose "SEE"
    - We are more likely to be right than if we chose ZEE
- The basic DTW equation does not factor this in
  - Word = argmax $_{word}$ probability(data | word) does not account for prior bias
- Cast the problem instead as a Bayesian classification problem
  - Word = argmax $_{word}$ p(word) probability(data | word)
  - "p(word)" is the *a priori* probability of the word
  - Naturally accounts for prior bias

Statistical pattern classification

- Given data X, find which of a number of classes C_1, C_2,…C_N it belongs to, based on known distributions of data from C_1, C_2, etc.
  - Bayesian Classification:

$$\text{Class} = C_i : i = \text{argmax}_j \log(P(C_j)) + \log(P(X|C_j))$$

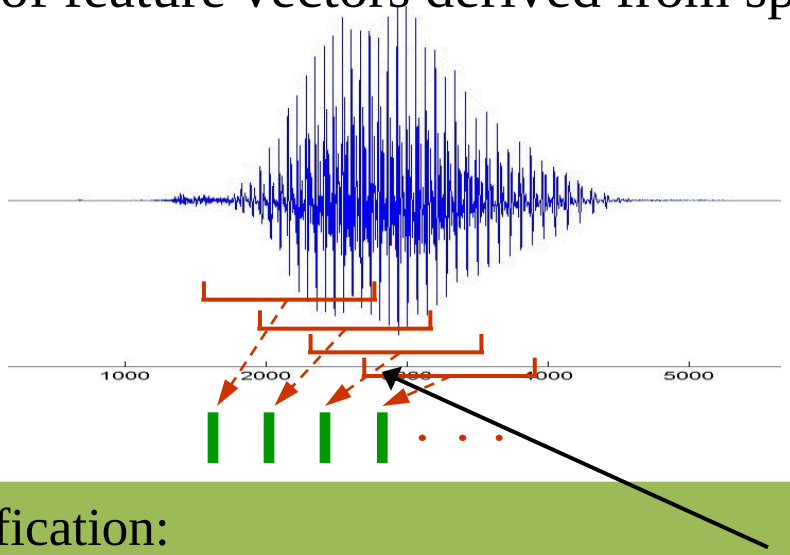
a priori probability of C_j

Probability of X as given by the probability distribution of C_j

- The *a priori* probability accounts for the relative proportions of the classes
  - If you never saw any data, you would guess the class based on these probabilities alone
- $P(X|C_j)$ accounts for evidence obtained from observed data X

Isolated Word Recognition as Bayesian Classification

- Classes are words
- Data are instances of spoken words
  - Sequence of feature vectors derived from speech signal



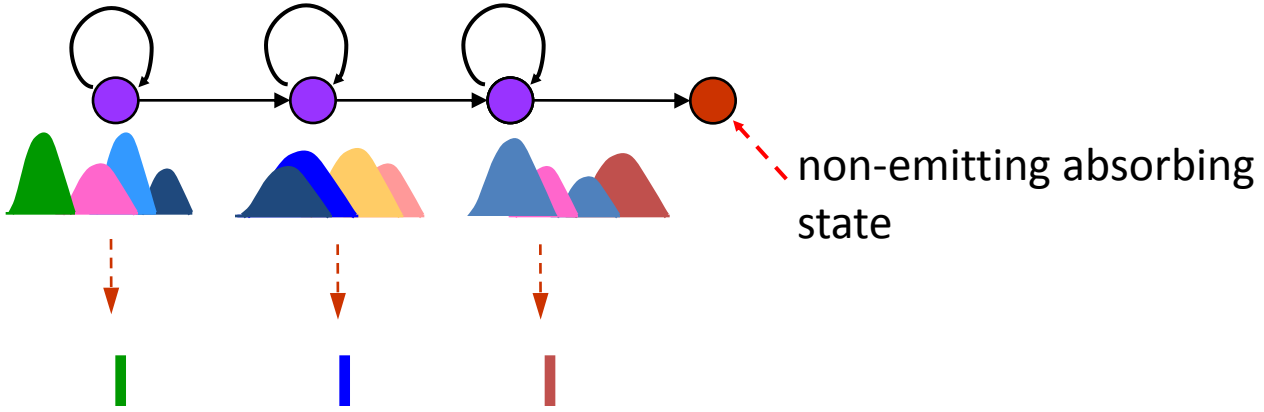
- Bayesian classification:

Recognized_Word = argmax_{word} log(P(*word*)) + log(P(*X*| *word*))

- P(*word*) is *a priori* probability of *word*
  - Obtained from our expectation of the relative frequency of occurrence of the word
- P(*X*|*word*) is the probability of *X* computed on the probability distribution function of *word*

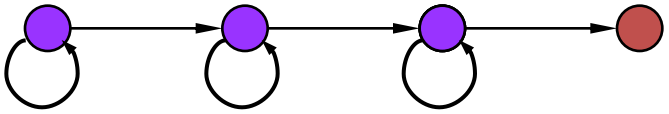
Computing P(X | *word*)

- P(*X*|*word*) is computed from the HMM for the word
  - HMMs are actually probability distributions
- Ideally P(X|word)is computed using the forward algorithm
- In reality computed as the best path through a Trellis
  - A priori probability P(word) is factored into the Trellis

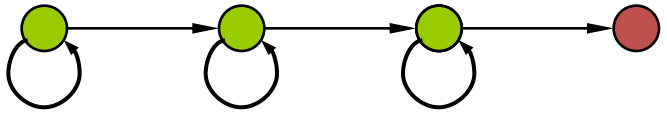


Factoring in *a priori* probability into Trellis

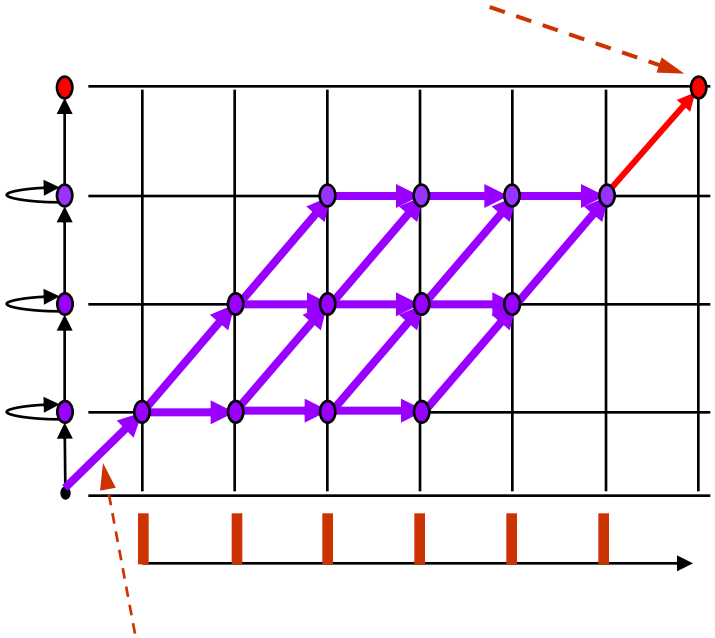
HMM for *Odd*



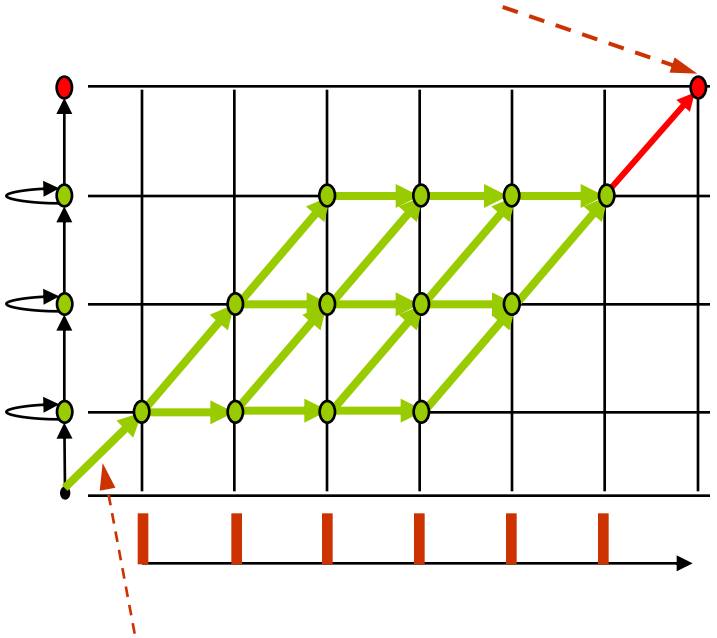
HMM for *Even*



BestPathLogProb(X,Odd)



BestPathLogProb(X,Even)

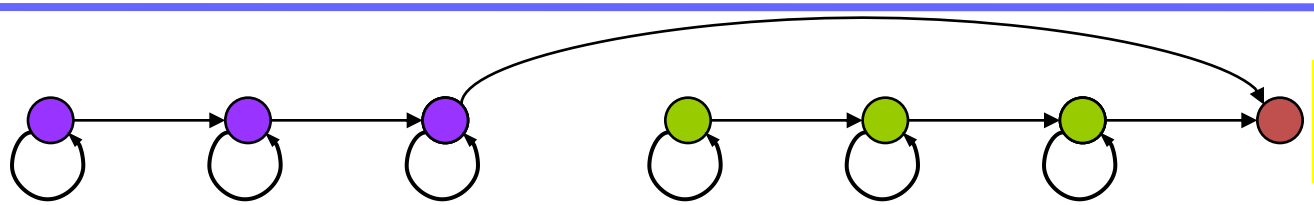


Log(P(*Odd*))

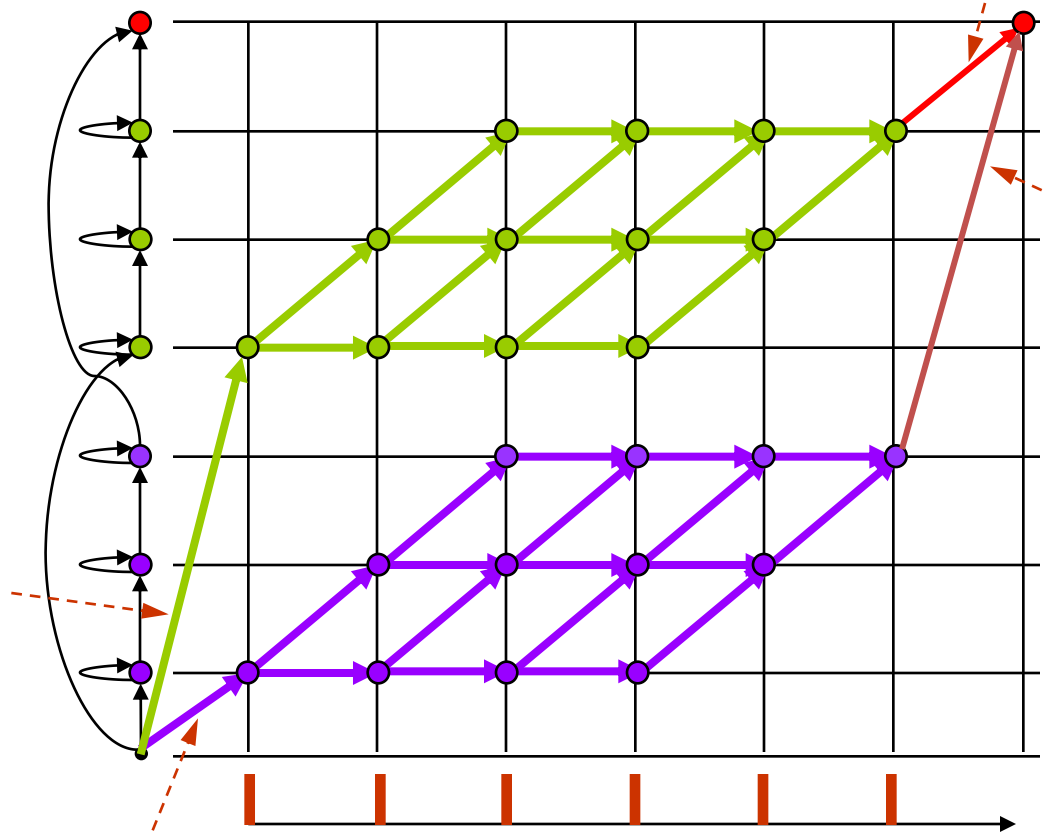
Log(P(*Even*))

The prior bias is factored in as the edge penalty at the entry to the trellis

Time-Synchronous Trellis: *Odd* and *Even*



BestPathLogProb(X,Odd)



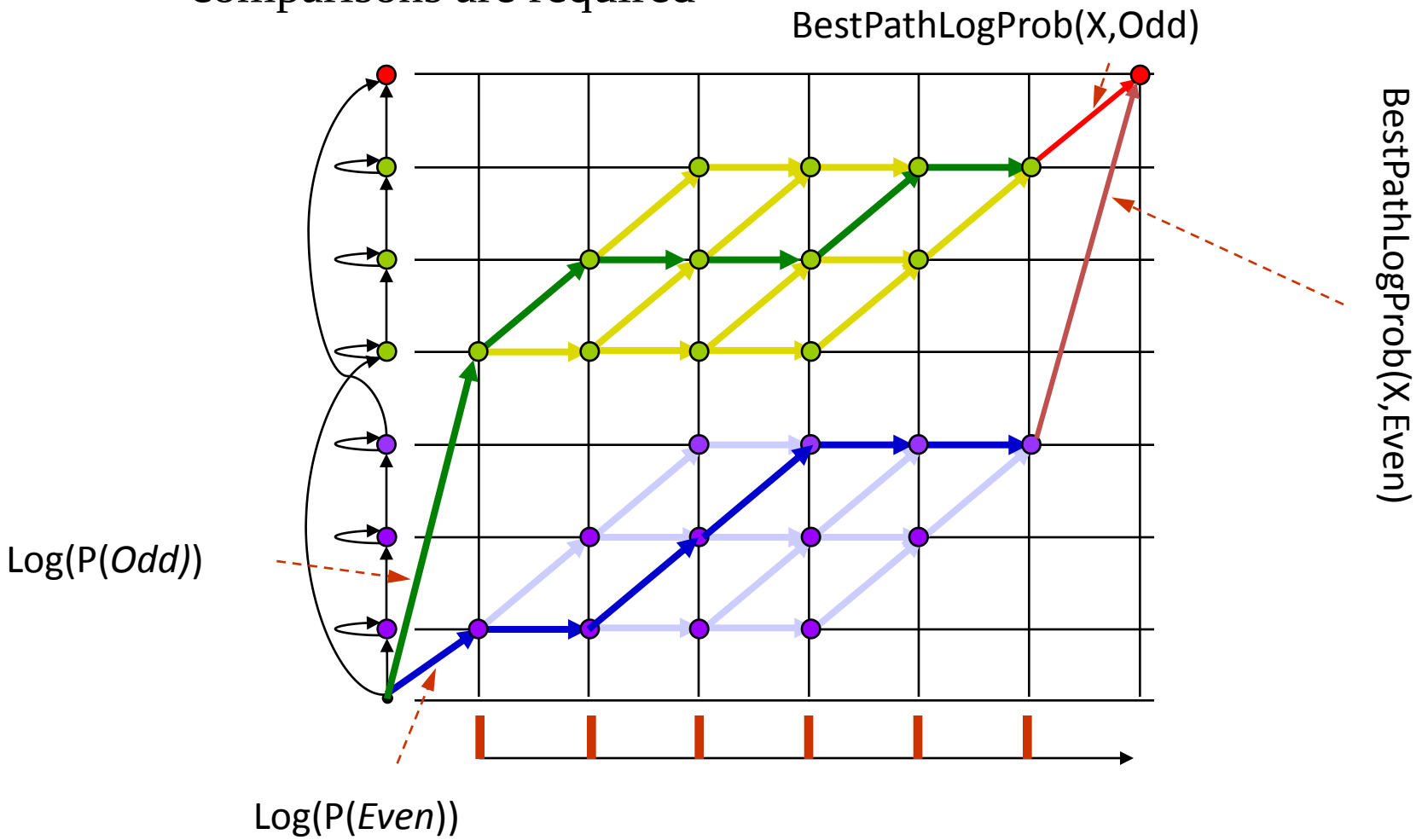
BestPathLogProb(X,Even)

Log(P(*Odd*))

Log(P(*Even*))

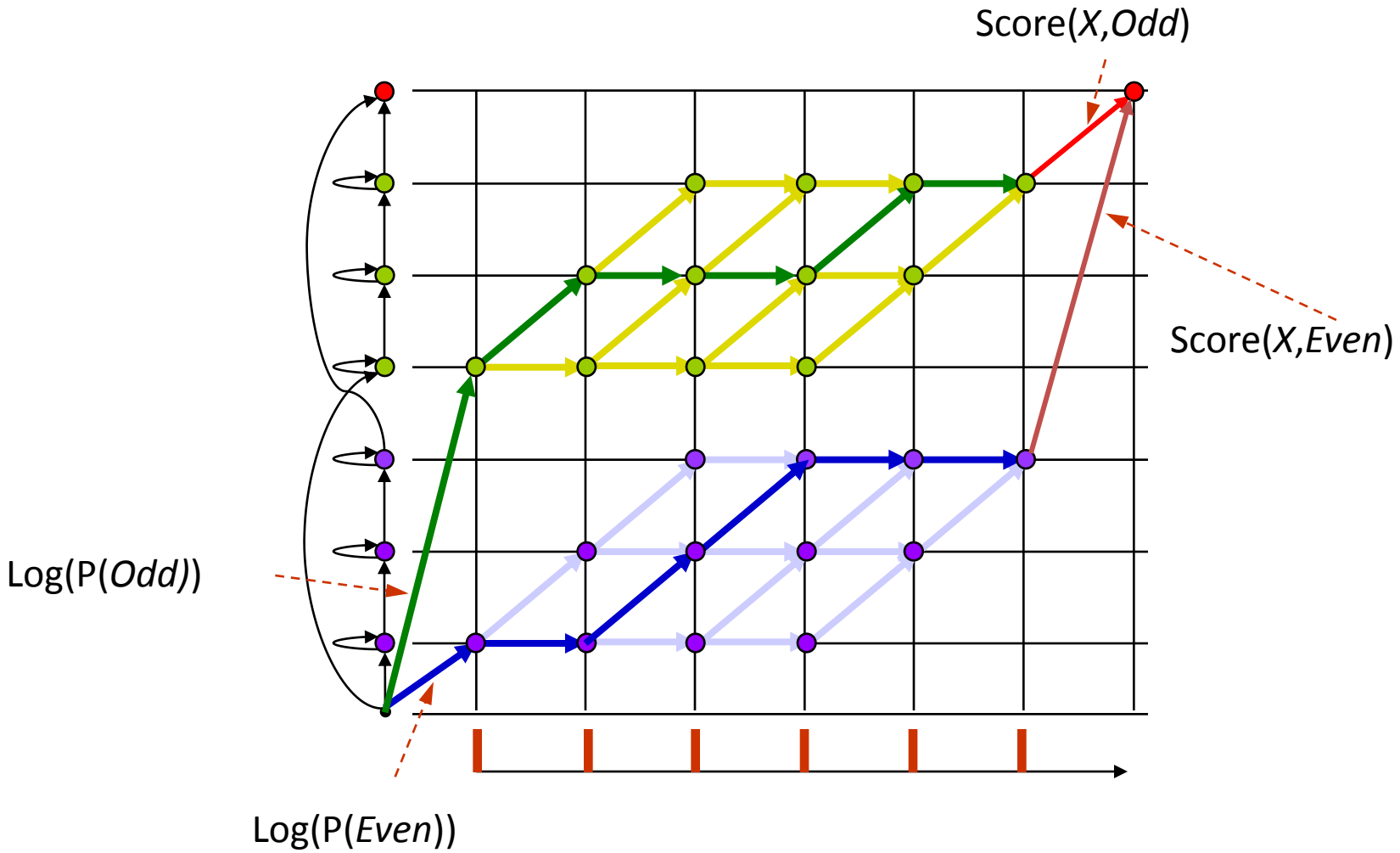
Time Synchronous Decode*Odd* and *Even*

- Compute the probability of best path
  - Computations can be done in the log domain. Only additions and comparisons are required



Decoding to classify between *Odd* and *Even*

- Compare scores (best state sequence probabilities) of all competing words
- Select the word sequence corresponding to the path with the best score



Decoding isolated words with word HMMs

- Construct a trellis (search graph) based on the HMM for each word
  - Alternately construct a single, common trellis
- Select the word corresponding to the best scoring path through the combined trellis

Why Scores and not Probabilities

- Trivial reasons
  - Computational efficiency: Use log probabilities and perform additions instead of multiplications
    - Use *log* transition probabilities and *log* node probabilities
    - *Add* log probability terms – do not multiply
  - Underflow: Log probability terms add – no underflow
    - Probabilities will multiply and underflow rather quickly

- Deeper reason
  - Using scores enables us to ***collapse parts of the trellis***
  - This is ***not*** possible using forward probabilities
  - We will see why in the next few slides

Statistical classification of word sequences

- Given data *X*, find which of a number of classes C_1, C_2,…C_N it belongs to, based on known distributions of data from C_1, C_2, etc.
- Bayesian Classification:

$$\text{Class} = C_i : i = \text{argmax}_j \, P(C_j)P(X|C_j)$$

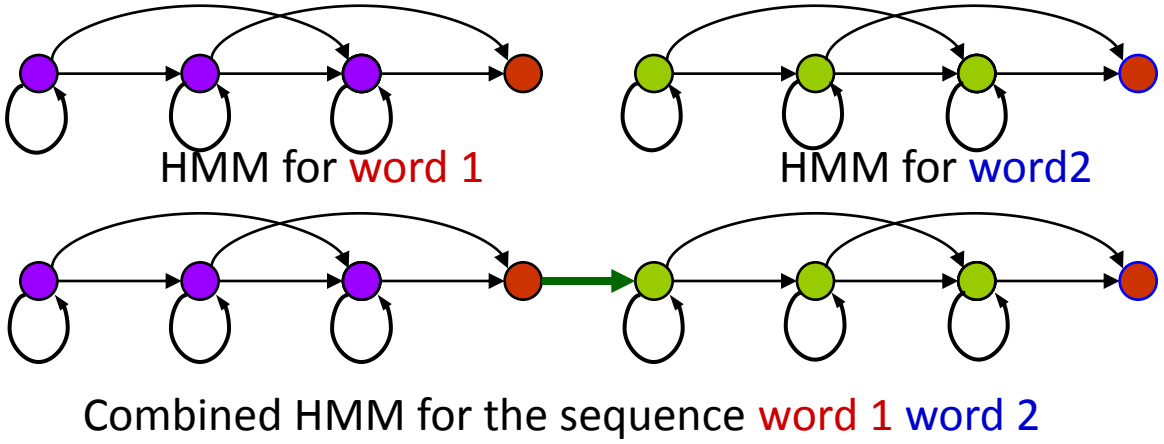
- Classes are word sequences
- Data are spoken recordings of word sequences
- Bayesian classification

$$word_1, word_2, ..., word_N =$$
$$\arg\max_{wd_1, wd_2, ..., wd_N} \{P(X \mid wd_1, wd_2, ..., wd_N)P(wd_1, wd_2, ..., wd_N)\}$$

- P(wd_1,wd_2,wd_3..) is *a priori* probability of word sequence wd_1,wd_2,wd_3..
  - Is the word sequence "close file" more common than "delete file"..
- P(X| wd_1,wd_2,wd_3..) is the probability of X computed on the HMM for the word sequence wd_1,wd_2,wd_3
  - Ideally must be computed using the forward algorithm

Decoding continuous speech

First step: construct an HMM for each possible word sequence

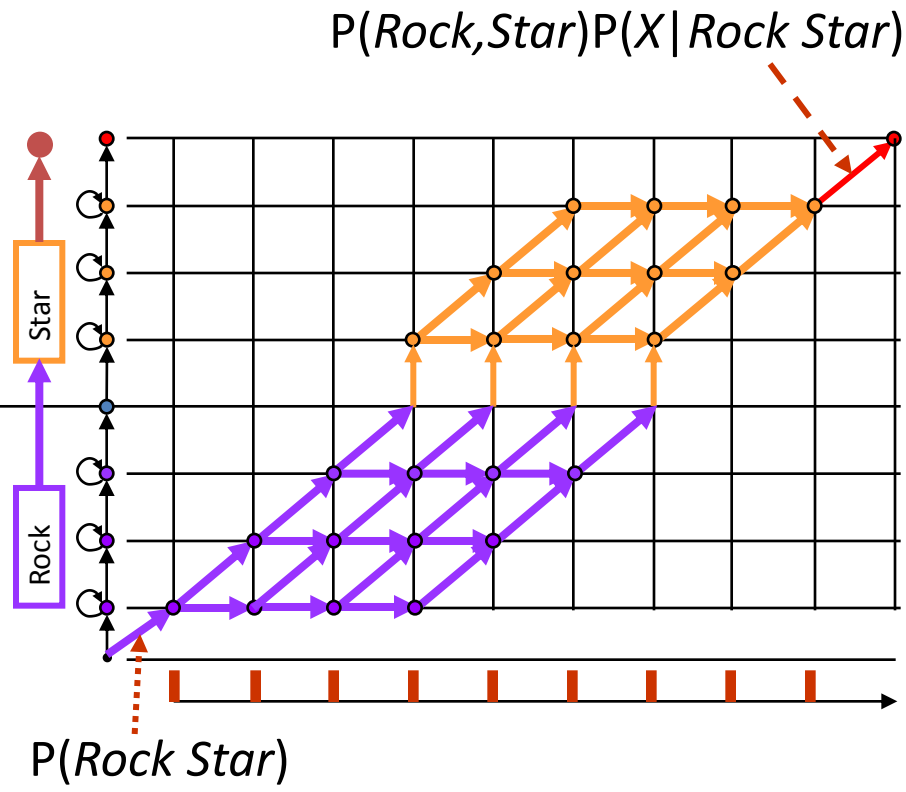


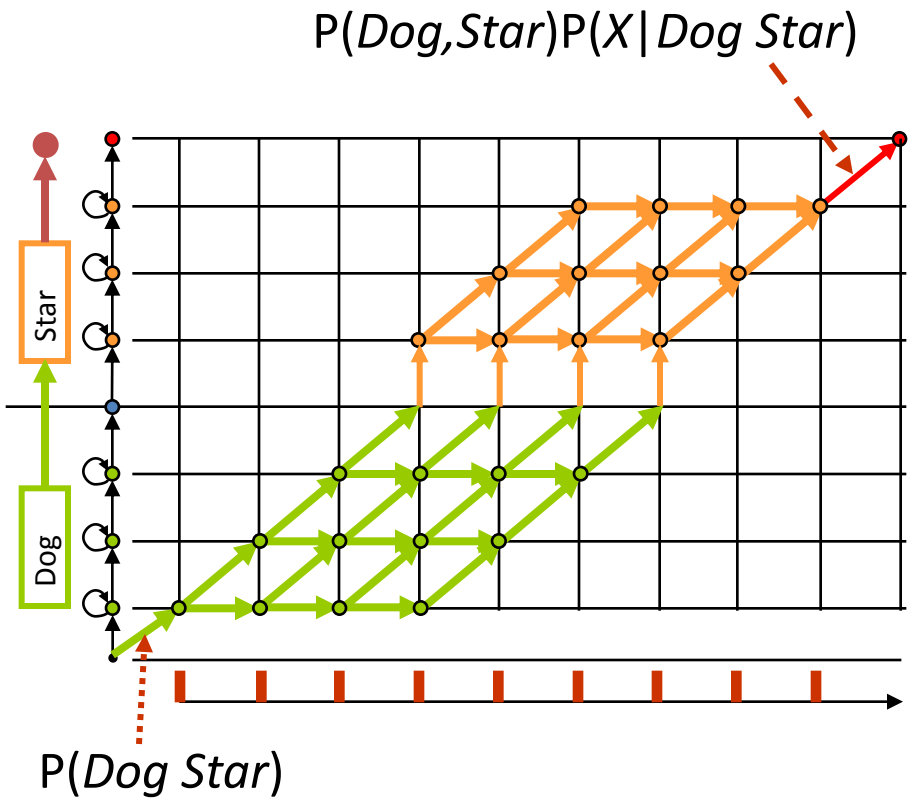
Second step: find the probability of the given utterance on the HMM for each possible word sequence

- P(X| wd_1,wd_2,wd_3..) is the probability of X computed on the probability distribution function of the word sequence wd_1,wd_2,wd_3..
  - HMMs now represent probability distributions of word sequences
  - Once again, this term must be computed by the forward algorithm

Bayesian Classification between word sequences

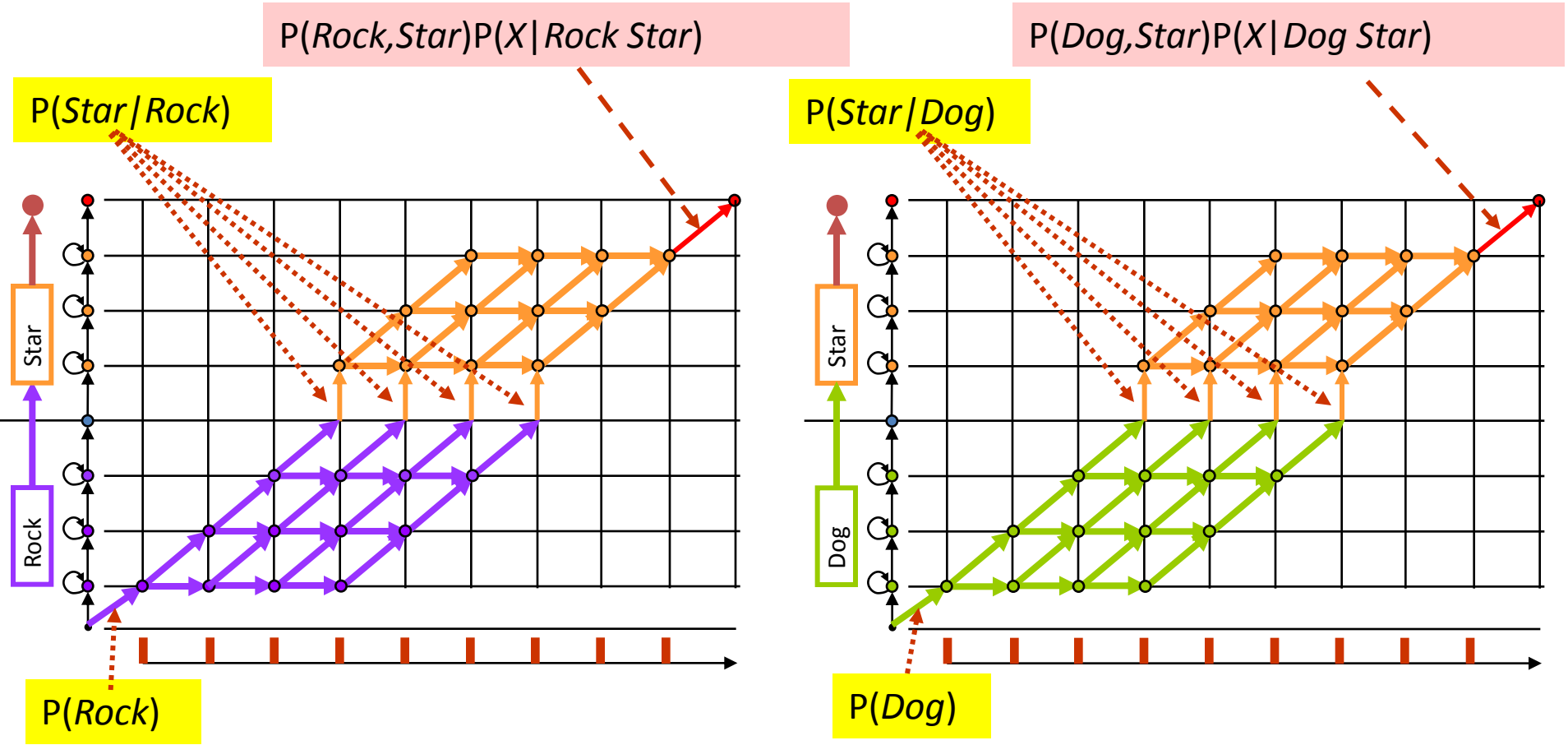
- Classifying an utterance as either "Rock Star" or "Dog Star"
  - Must compare P(Rock,Star)P(X|Rock Star) with P(Dog,Star)P(X|Dog Star)
  - This is the complete forward score at the final trellis node





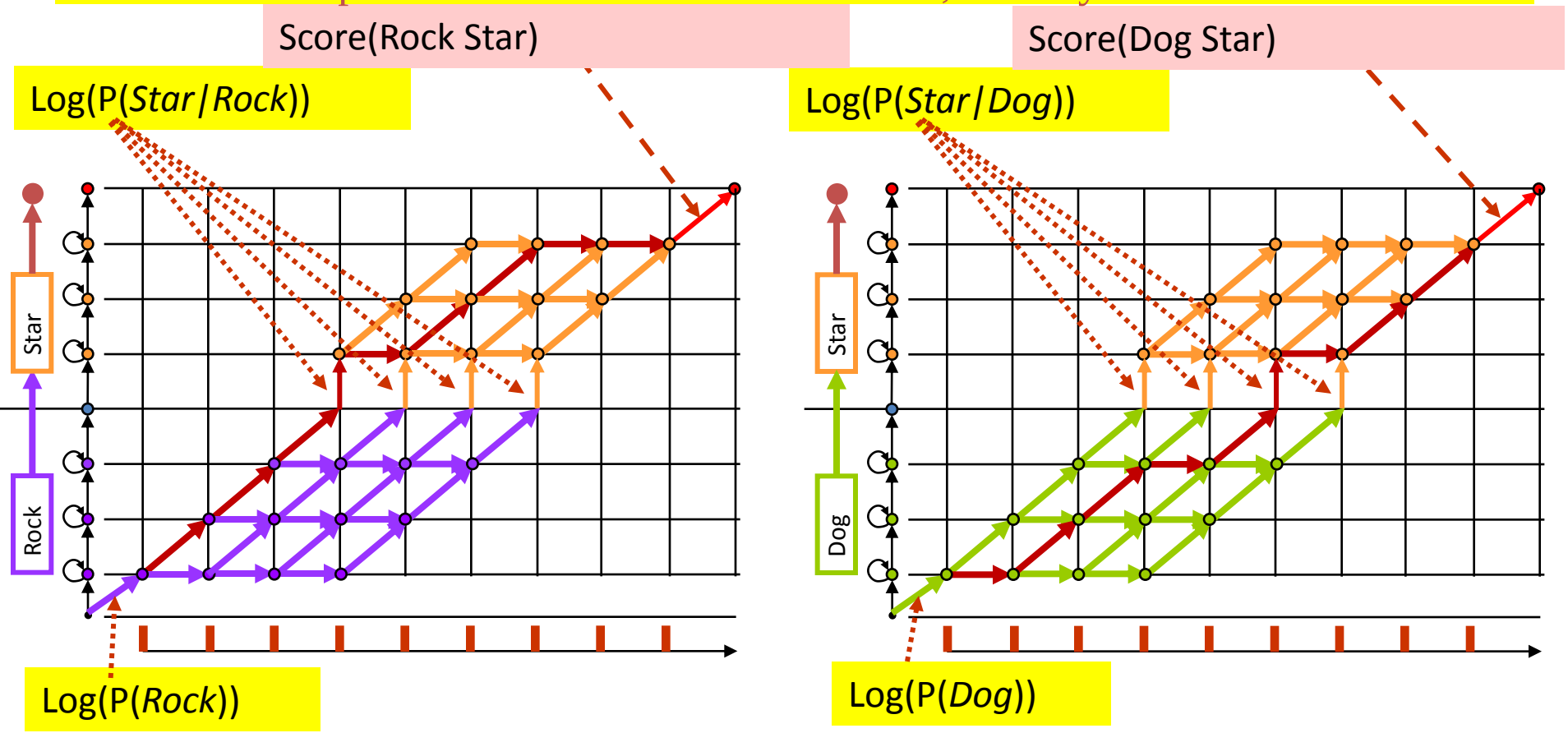
Bayesian Classification between word sequences

- The *a priori* probability of the word sequences (P(Rock Star), P(Dog Star)) can be spread across the Trellis without changing final probabilities

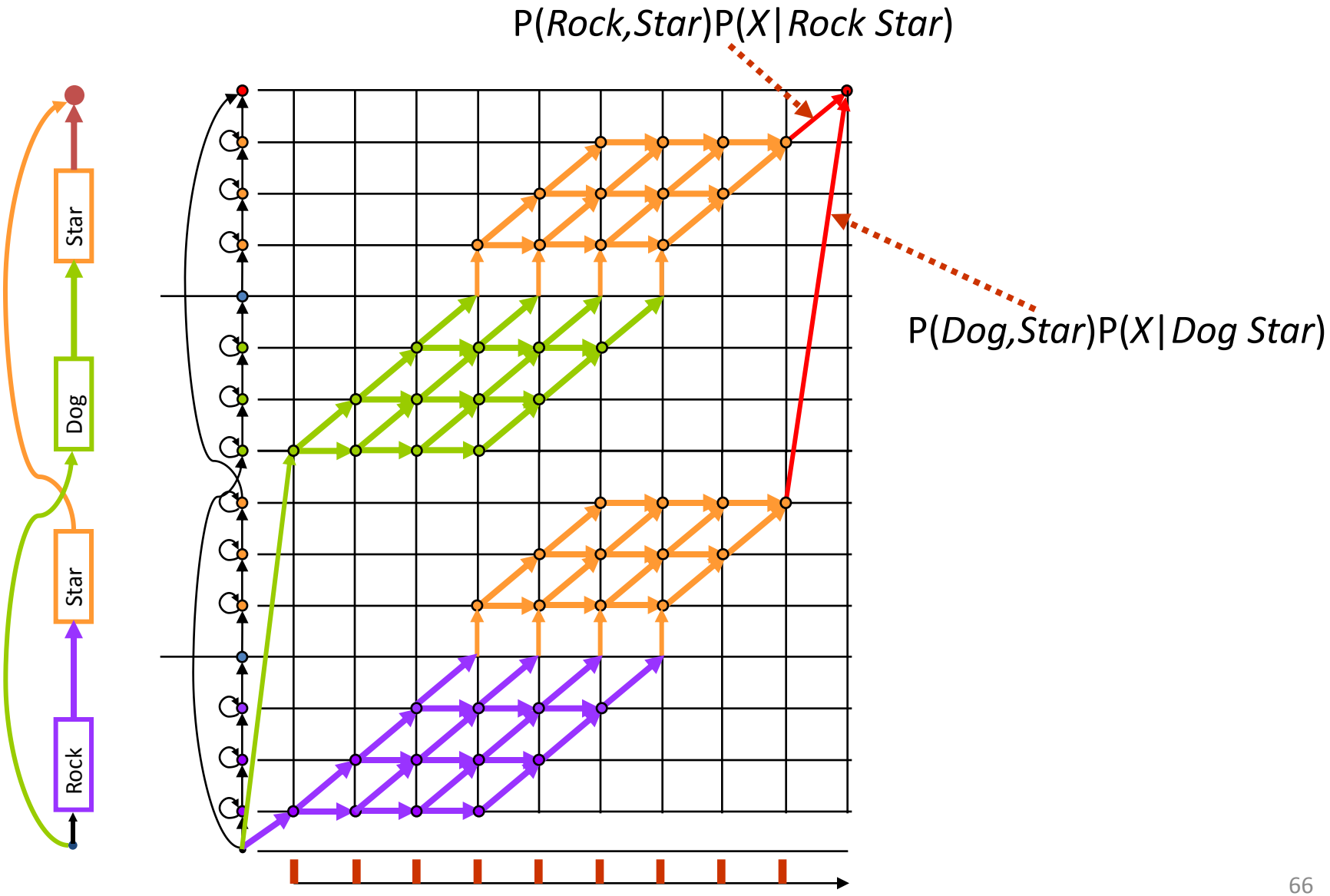


Decoding between word sequences

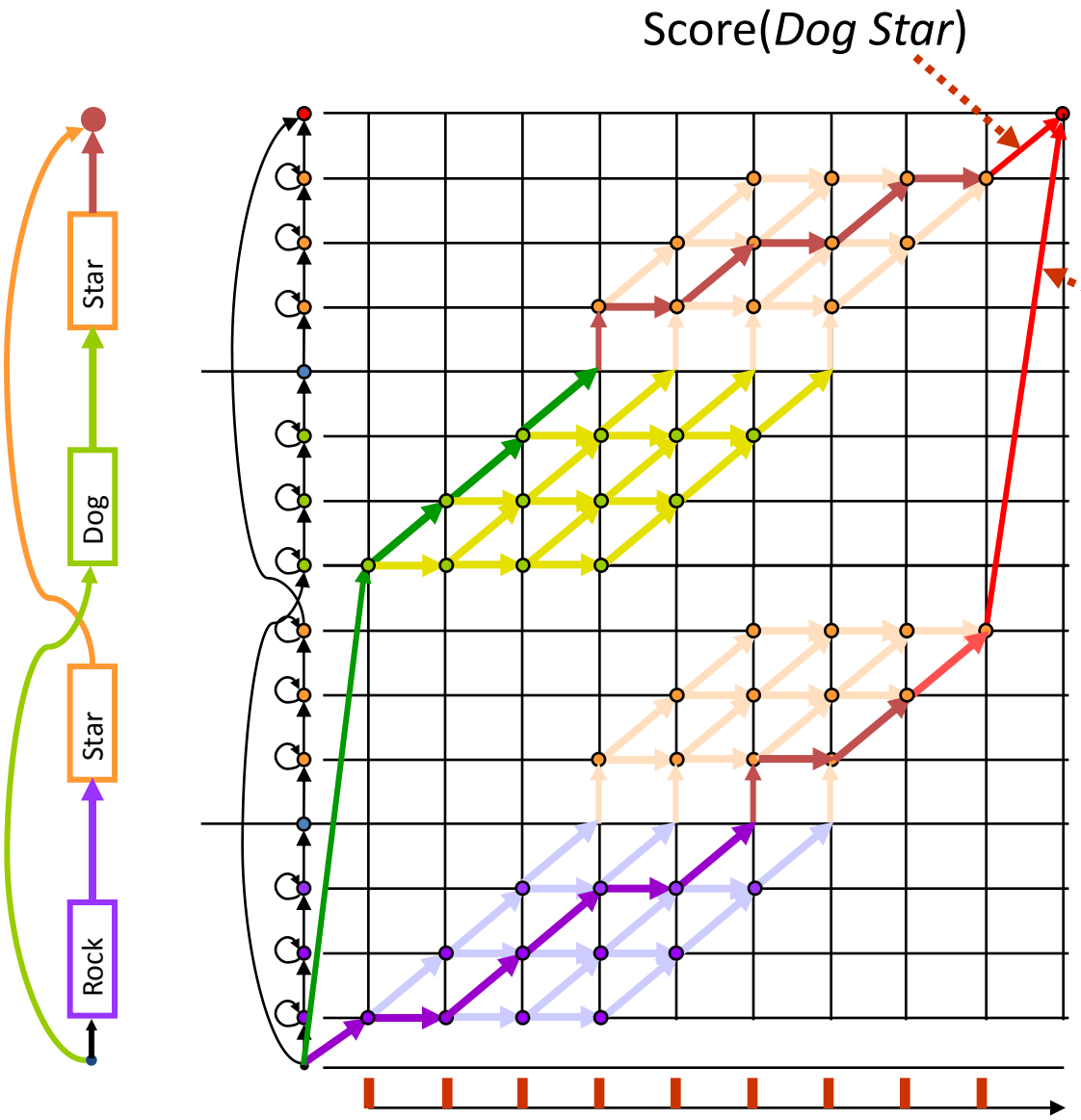
- In reality we find the score/cost of the best paths through the trellises
  - Not the full forward score
  - I.e. we perform DTW based classification, not Bayesian classification



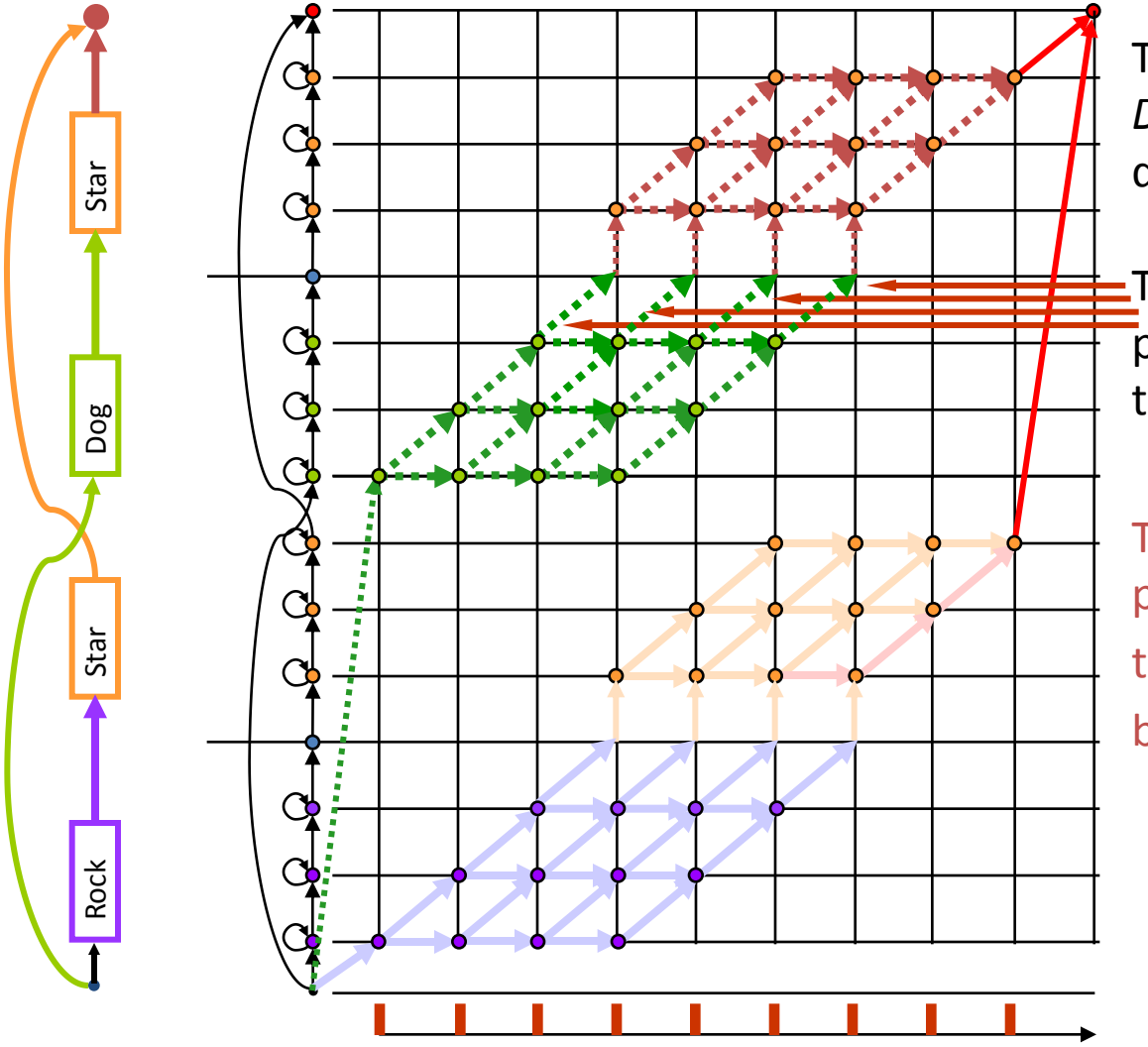
Time Synchronous Bayesian Classification between word sequences



Time synchronous decoding to classify between word sequences



Decoding to classify between word sequences

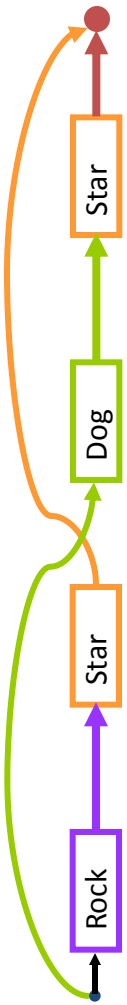


The best path through *Dog Star* lies within the dotted portions of the trellis

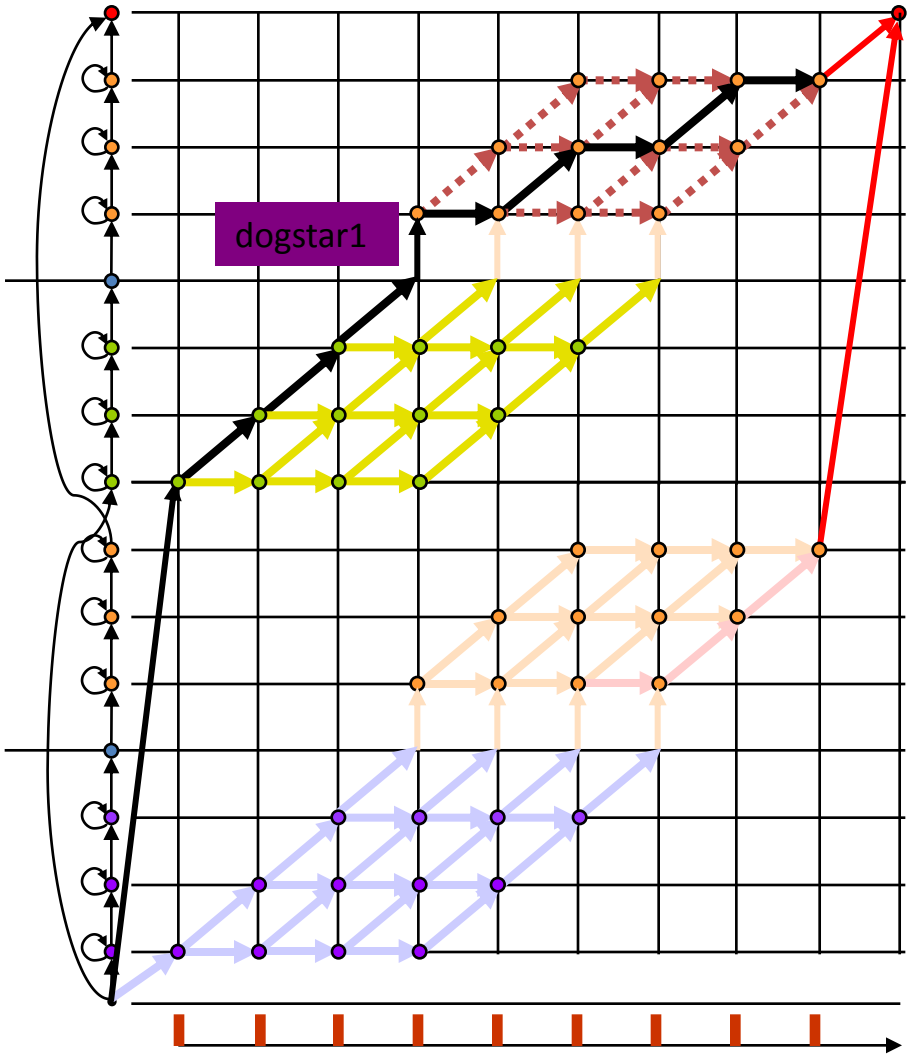
There are four transition points from *Dog* to *Star* in this trellis

There are four different sets paths through the dotted trellis, each with its own best path

Decoding to classify between word sequences



SET 1 and its best path



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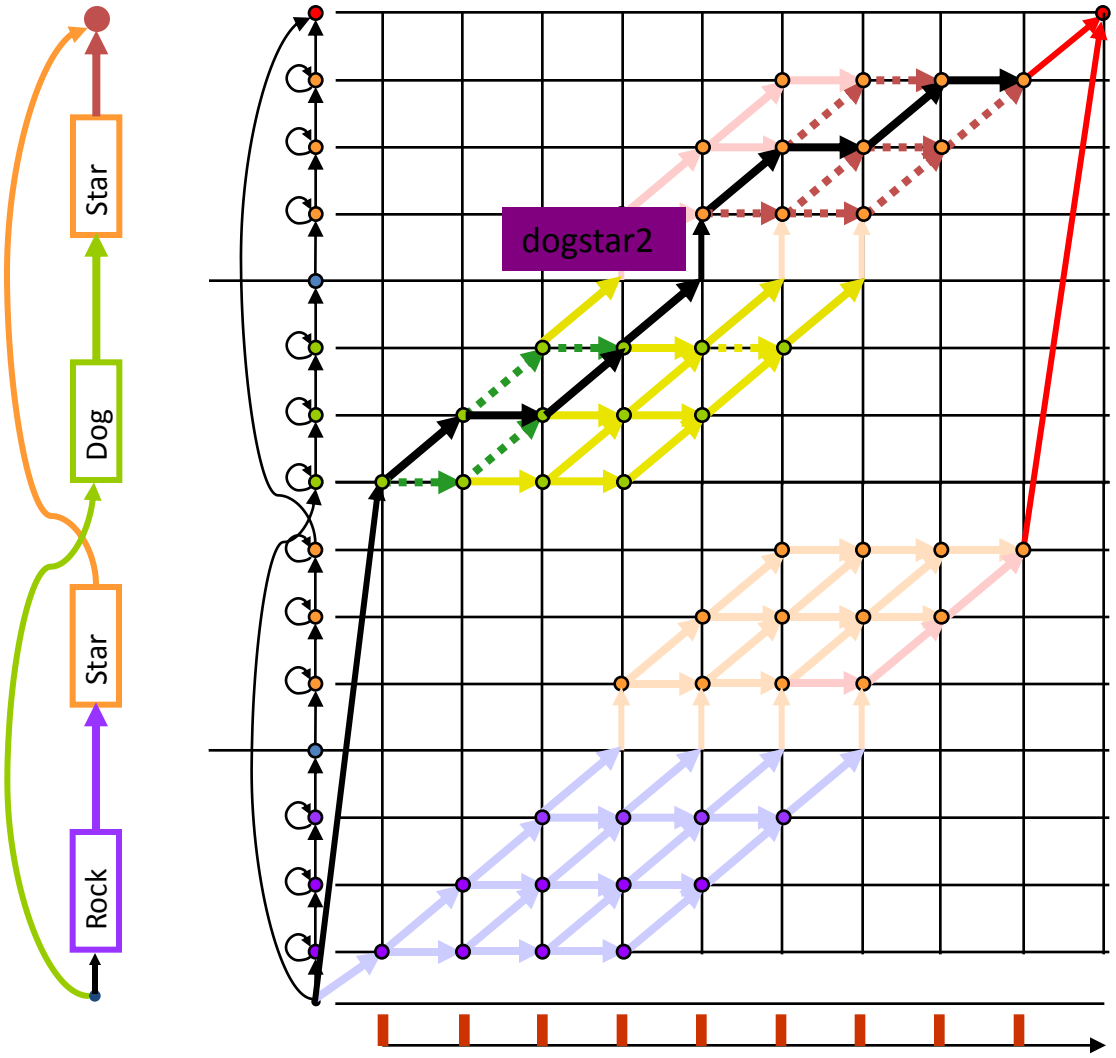
Decoding to classify between word sequences



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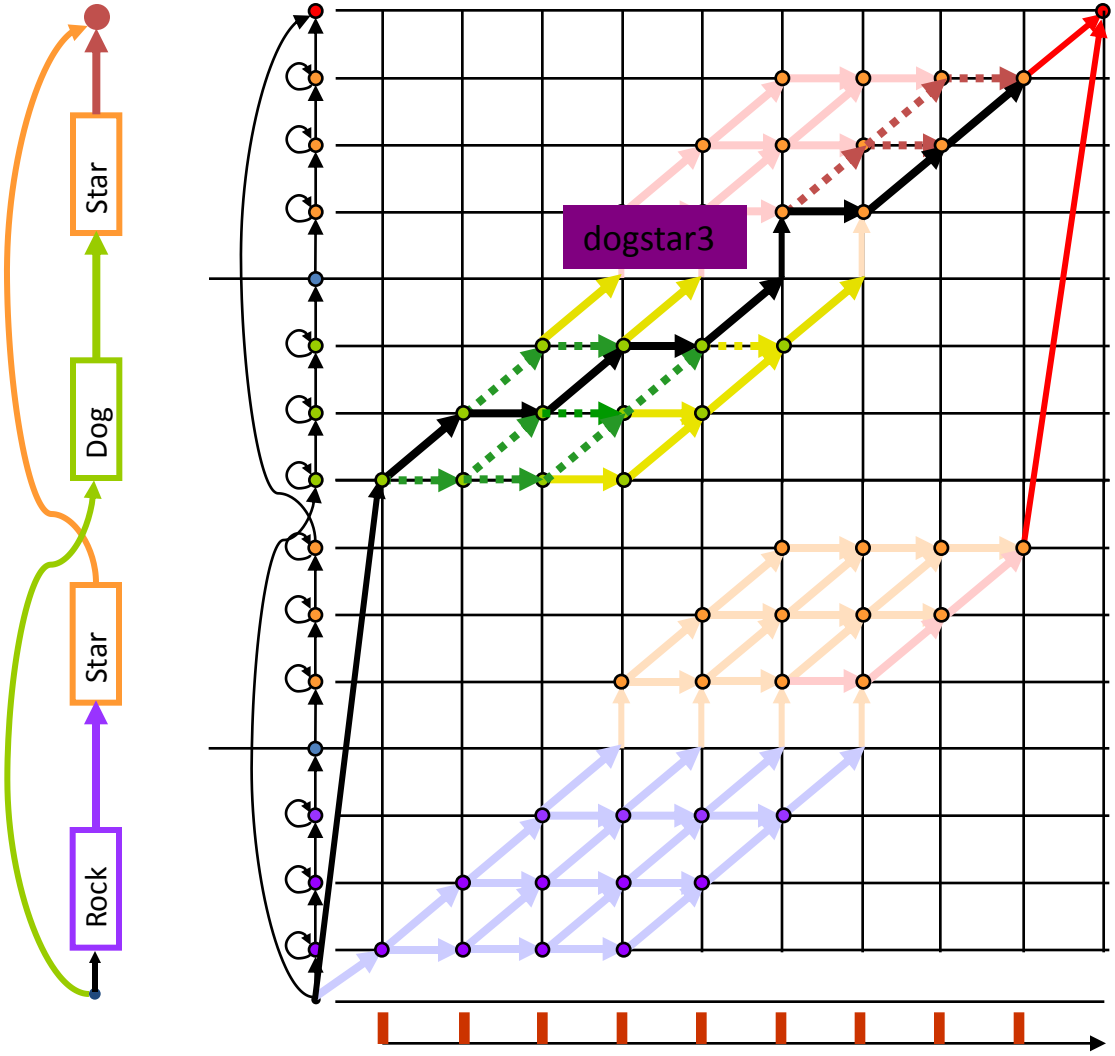

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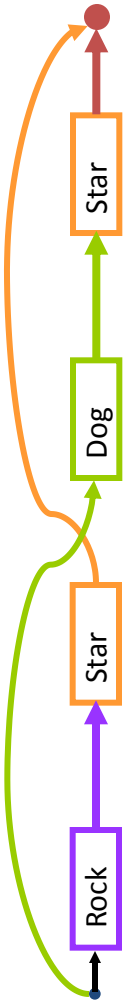
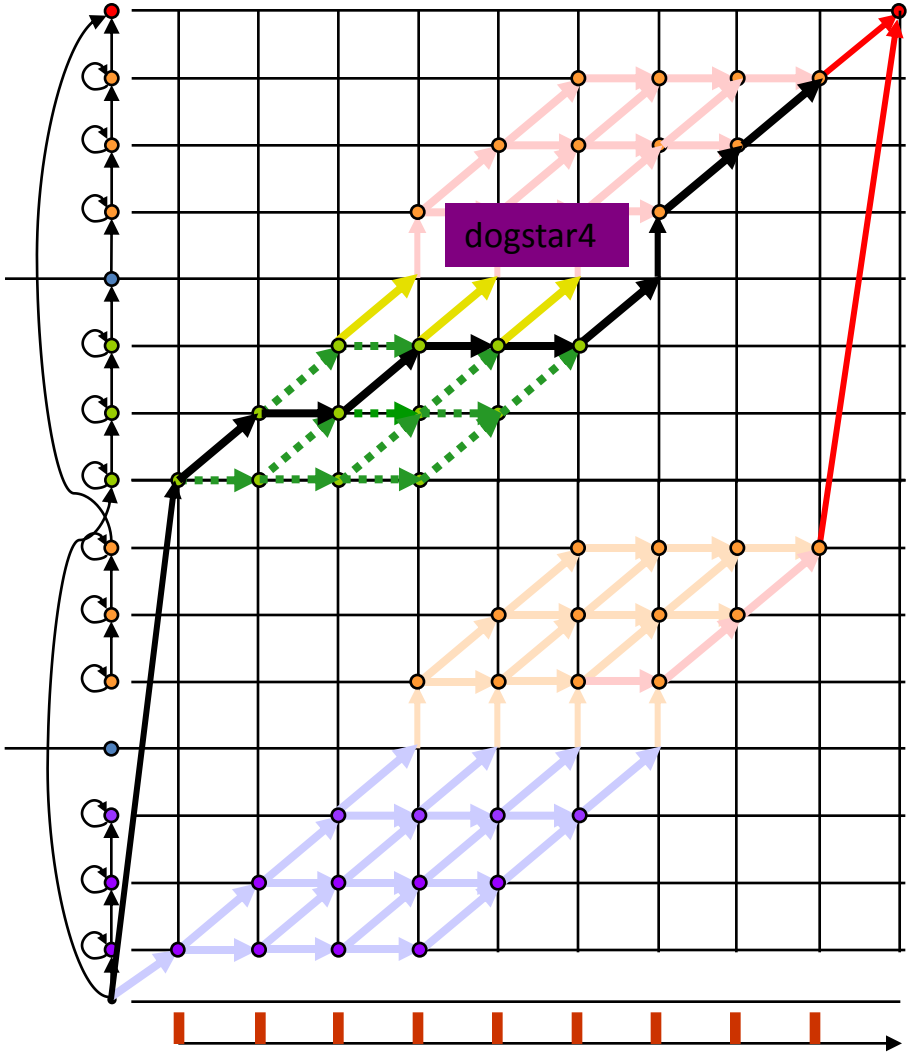
Decoding to classify between word sequences



SET 4 and its best path

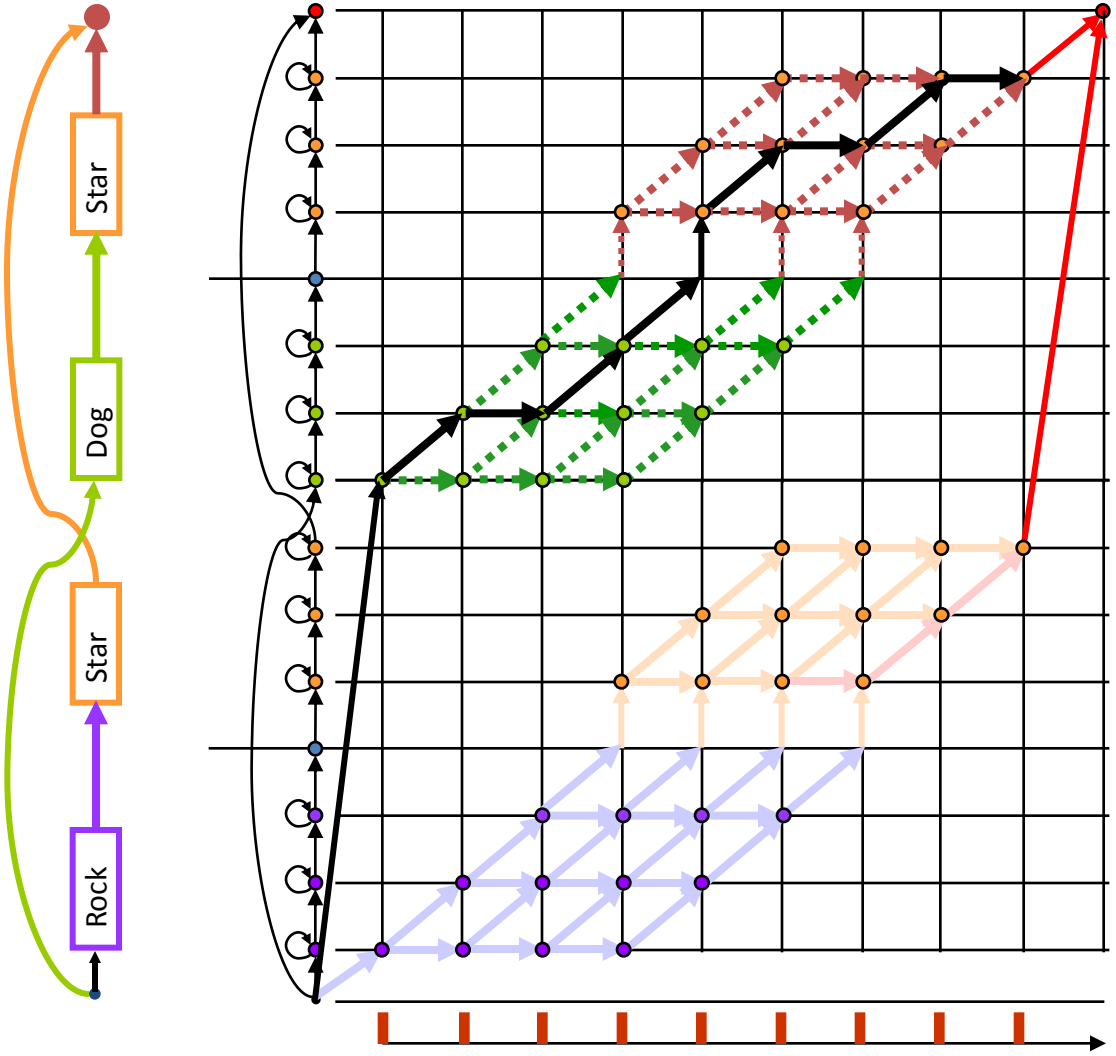


The best path through *Dog Star* lies within the dotted portions of the trellis

There are four transition points from *Dog* to *Star* in this trellis

There are four different sets paths through the dotted trellis, each with its own best path

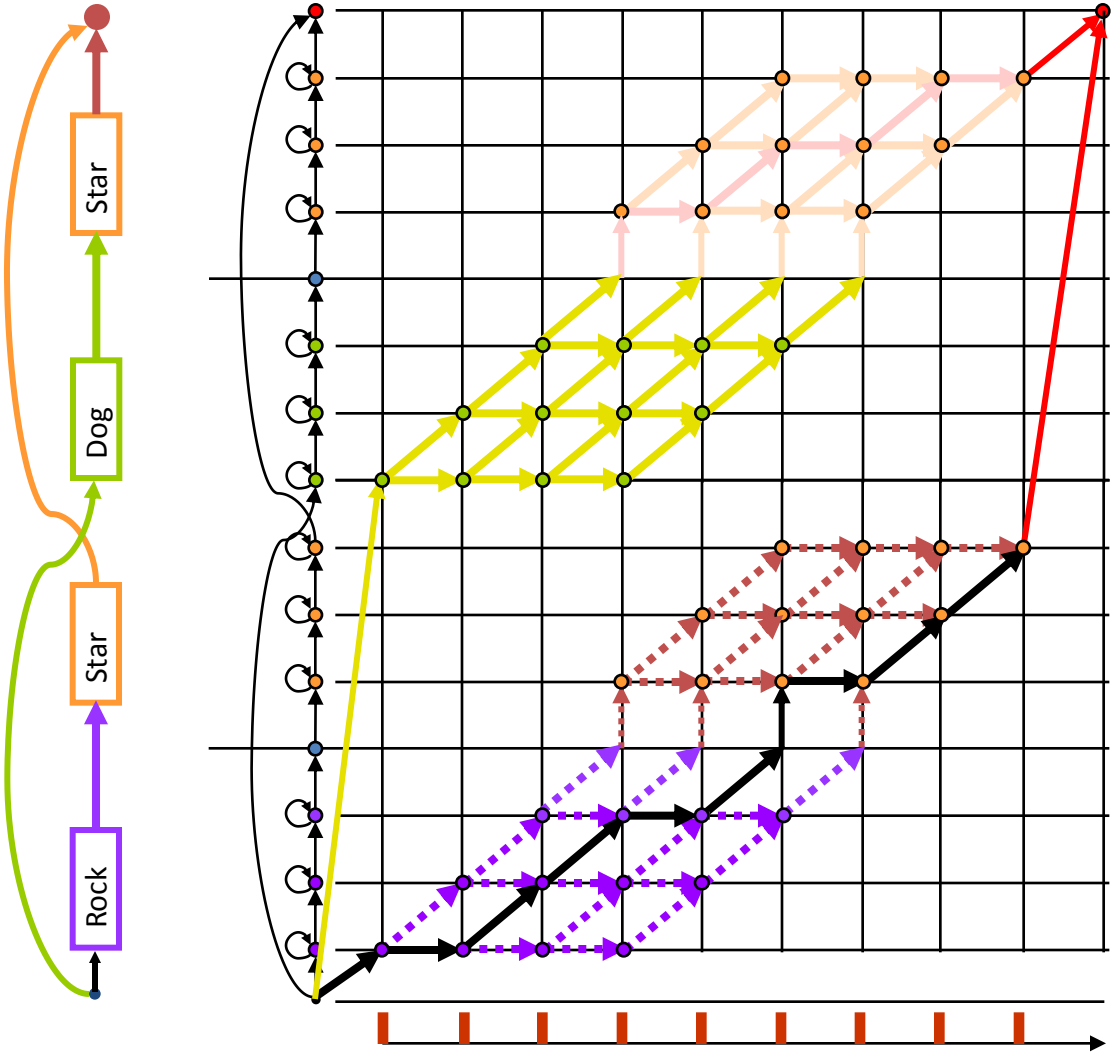
Decoding to classify between word sequences



The best path through *Dog Star* is the best of the four transition-specific best paths

max(dogstar) =
max (dogstar1, dogstar2,
dogstar3, dogstar4)

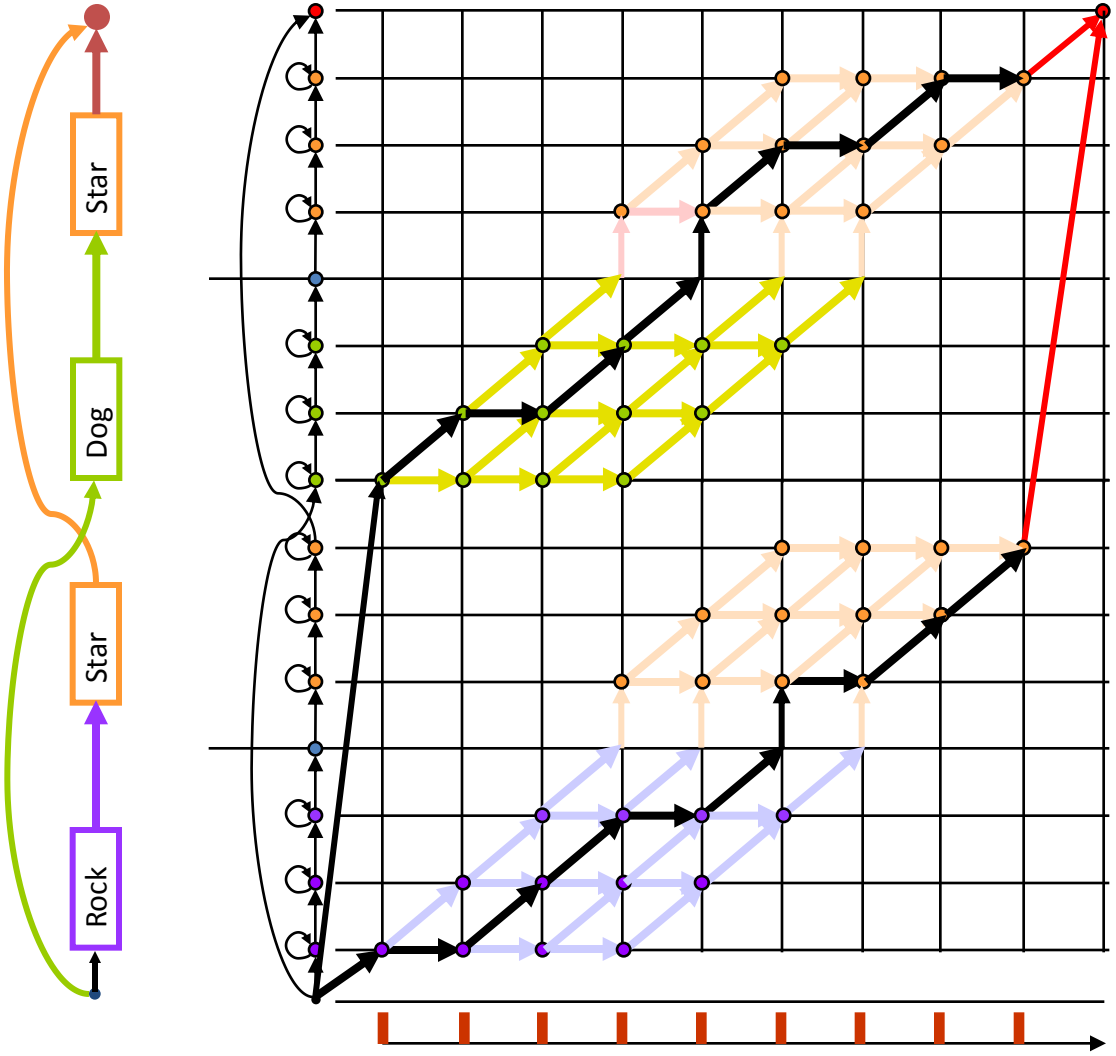
Decoding to classify between word sequences



Similarly, for *Rock Star* the best path through the trellis is the best of the four transition-specific best paths

max(rockstar) =
max (rockstar1, rockstar2,
rockstar3, rockstar4)

Decoding to classify between word sequences



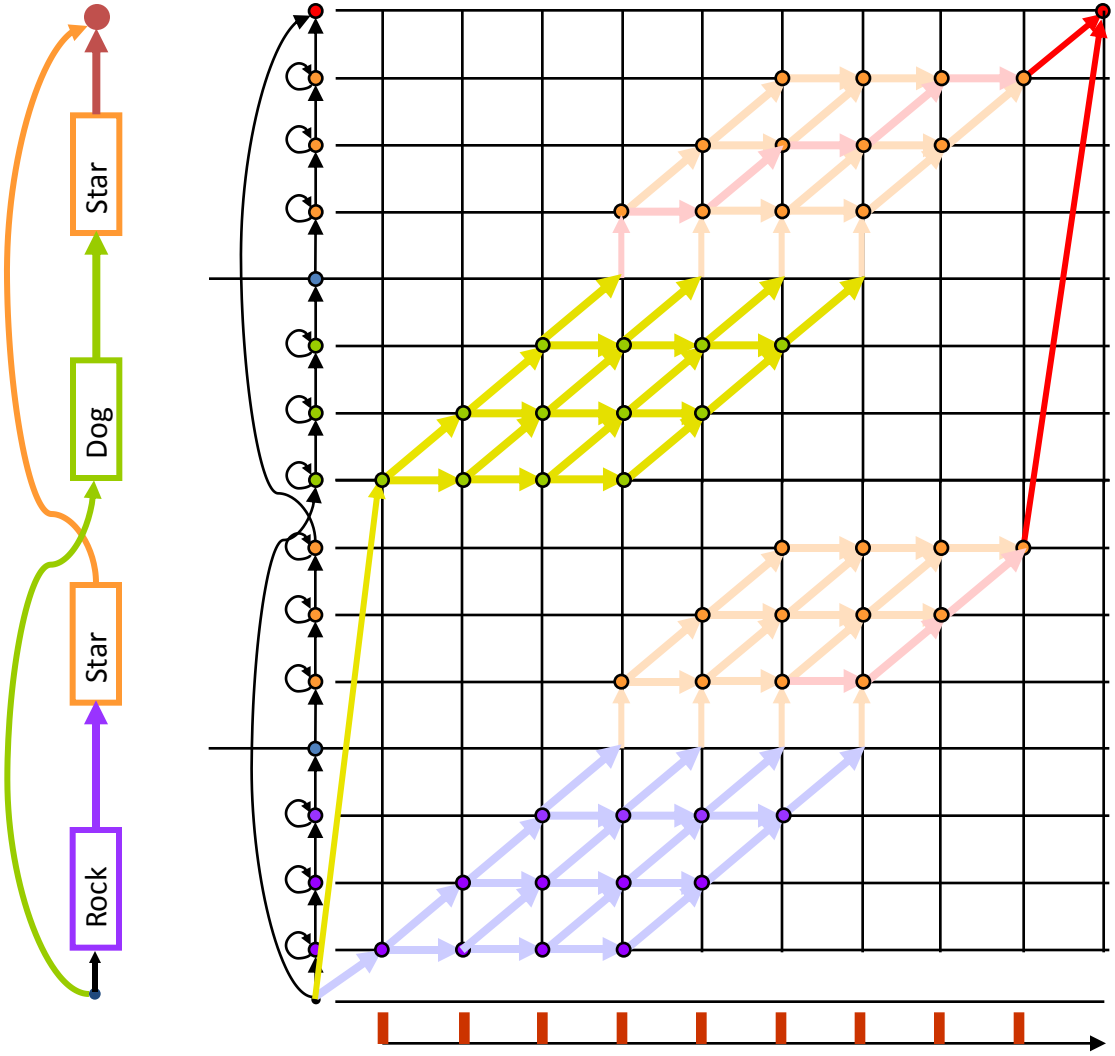
Then we'd compare the best paths through *Dog Star* and *Rock Star*

max(dogstar) =
max (dogstar1, dogstar2,
dogstar3, dogstar4)

max(rockstar) =
max (rockstar1, rockstar2,
rockstar3, rockstar4)

Viterbi =
max(max(dogstar),
max(rockstar))

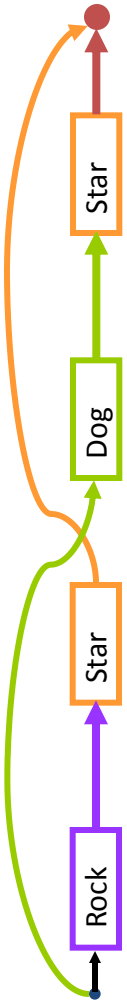
Decoding to classify between word sequences

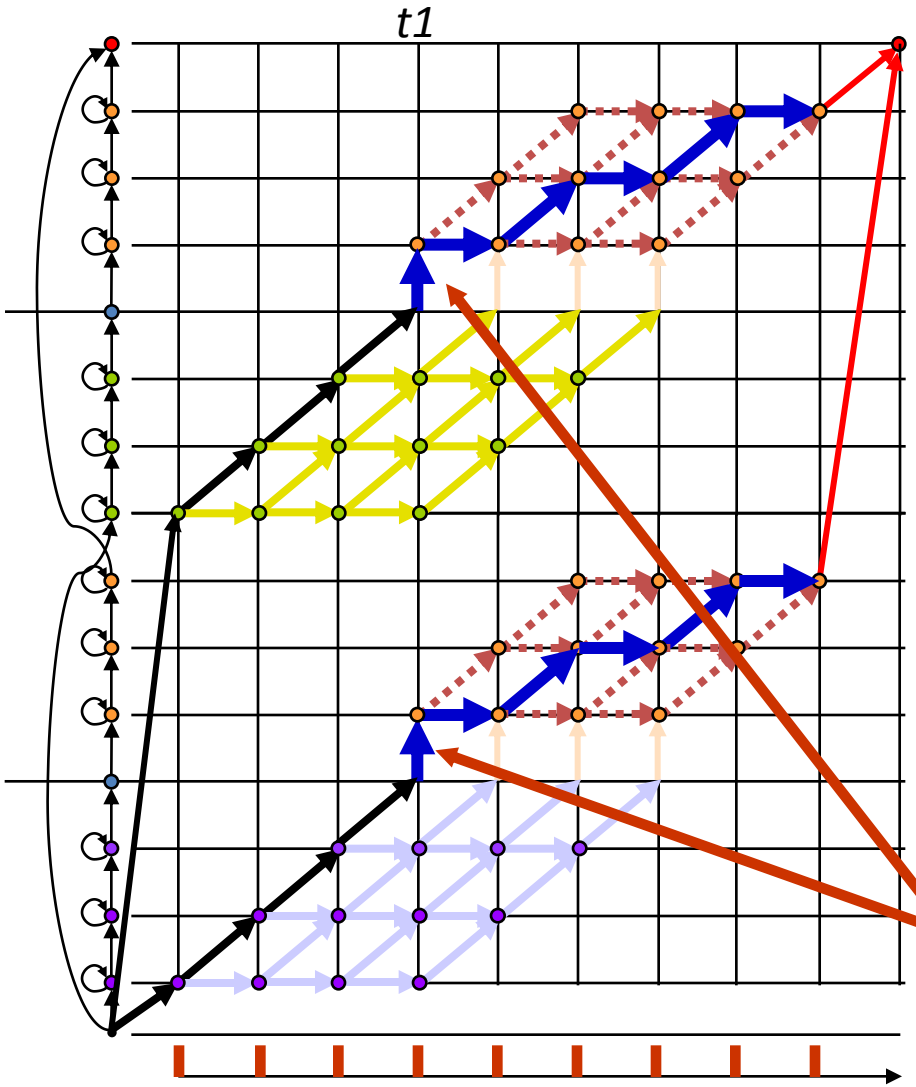


argmax is commutative:

max(max(dogstar), max(rockstar)
)
=
max (
max(dogstar1, rockstar1),
max(dogstar2, rockstar2),
max (dogstar3,rockstar3),
max(dogstar4,rockstar4)
)

Max (dogstar1, rockstar1)



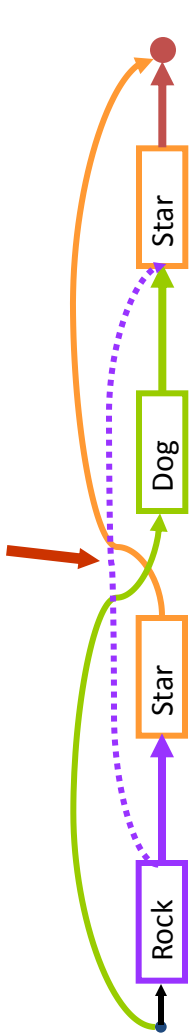


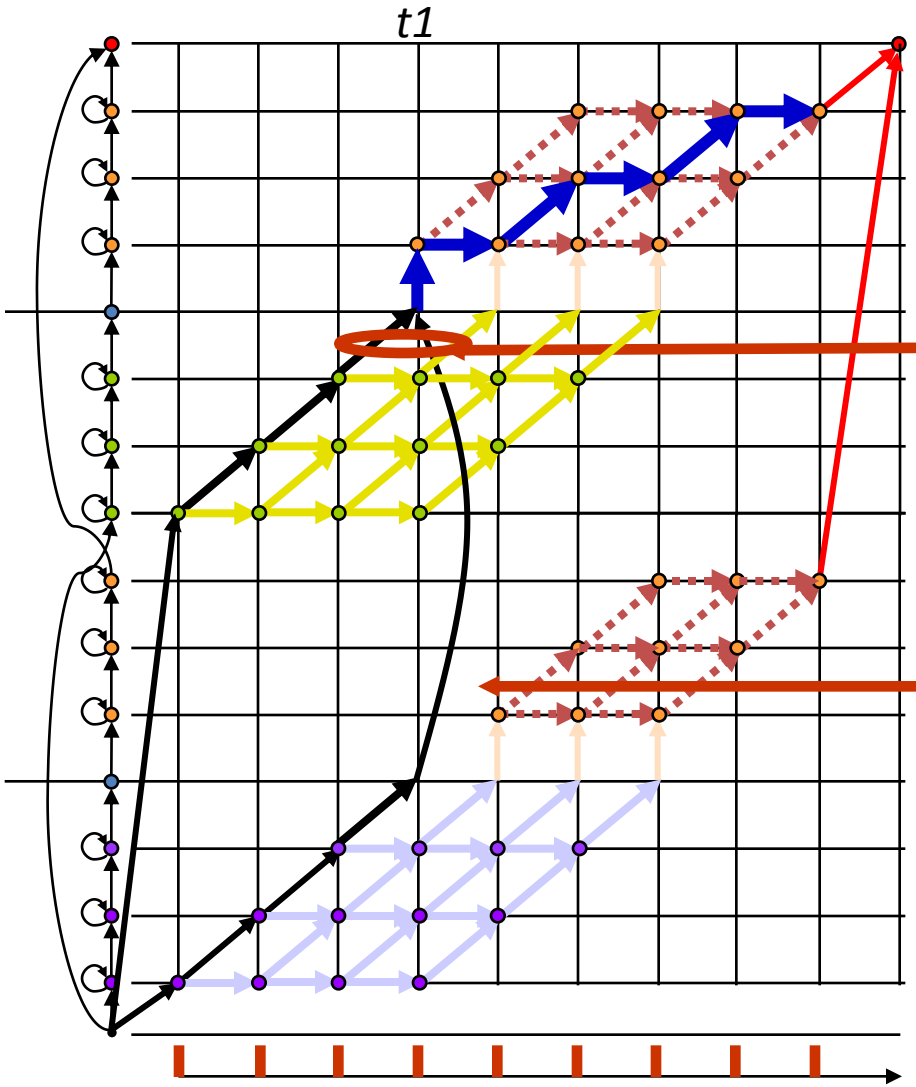
For a given entry point the best path through STAR is the same for both trellises

max(max(dogstar), max(rockstar))
=
max (
max(dogstar1, rockstar1),
max(dogstar2, rockstar2),
max (dogstar3,rockstar3),
max(dogstar4,rockstar4)
)

We can choose between Dog and Rock right here because the futures of these paths are identical

Max (dogstar1, rockstar1)

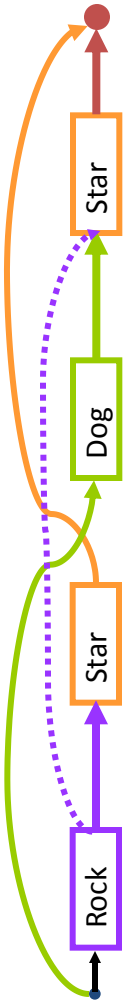


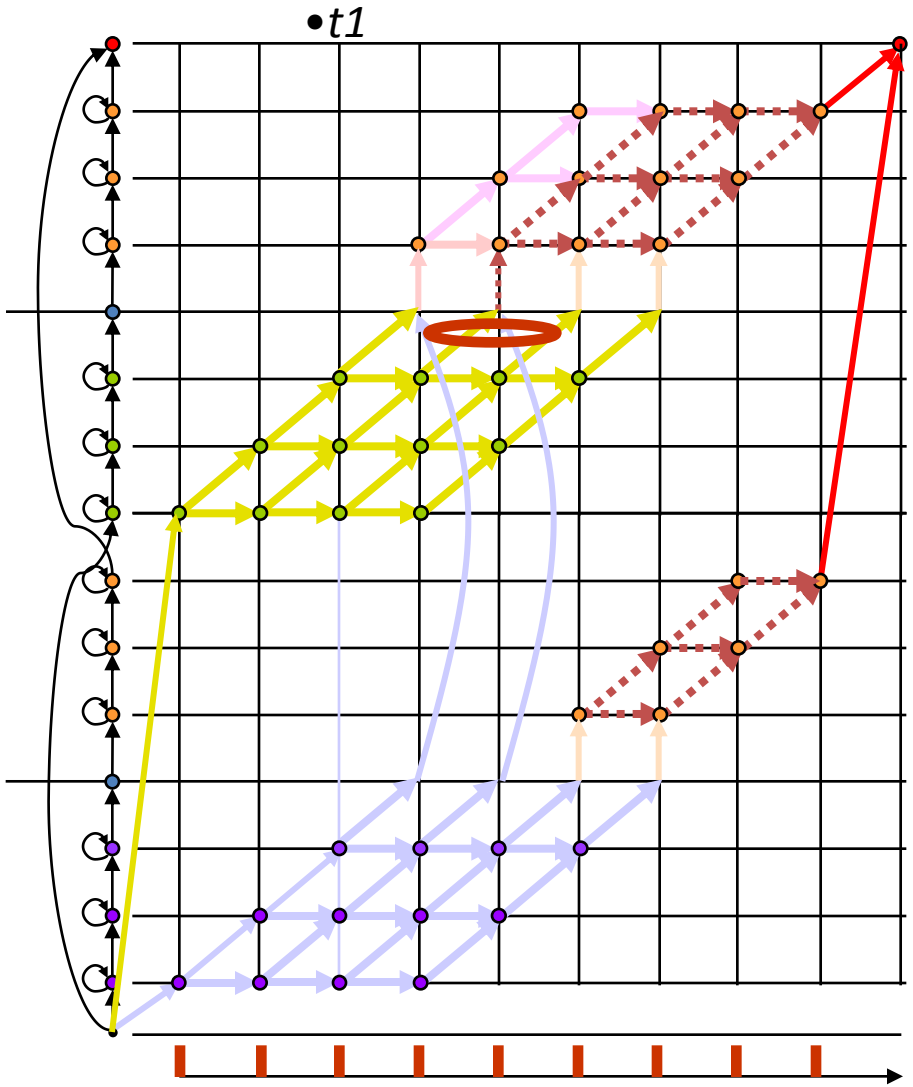


We select the higher scoring of the two incoming edges here

This portion of the trellis is now deleted

Max (dogstar2, rockstar2)

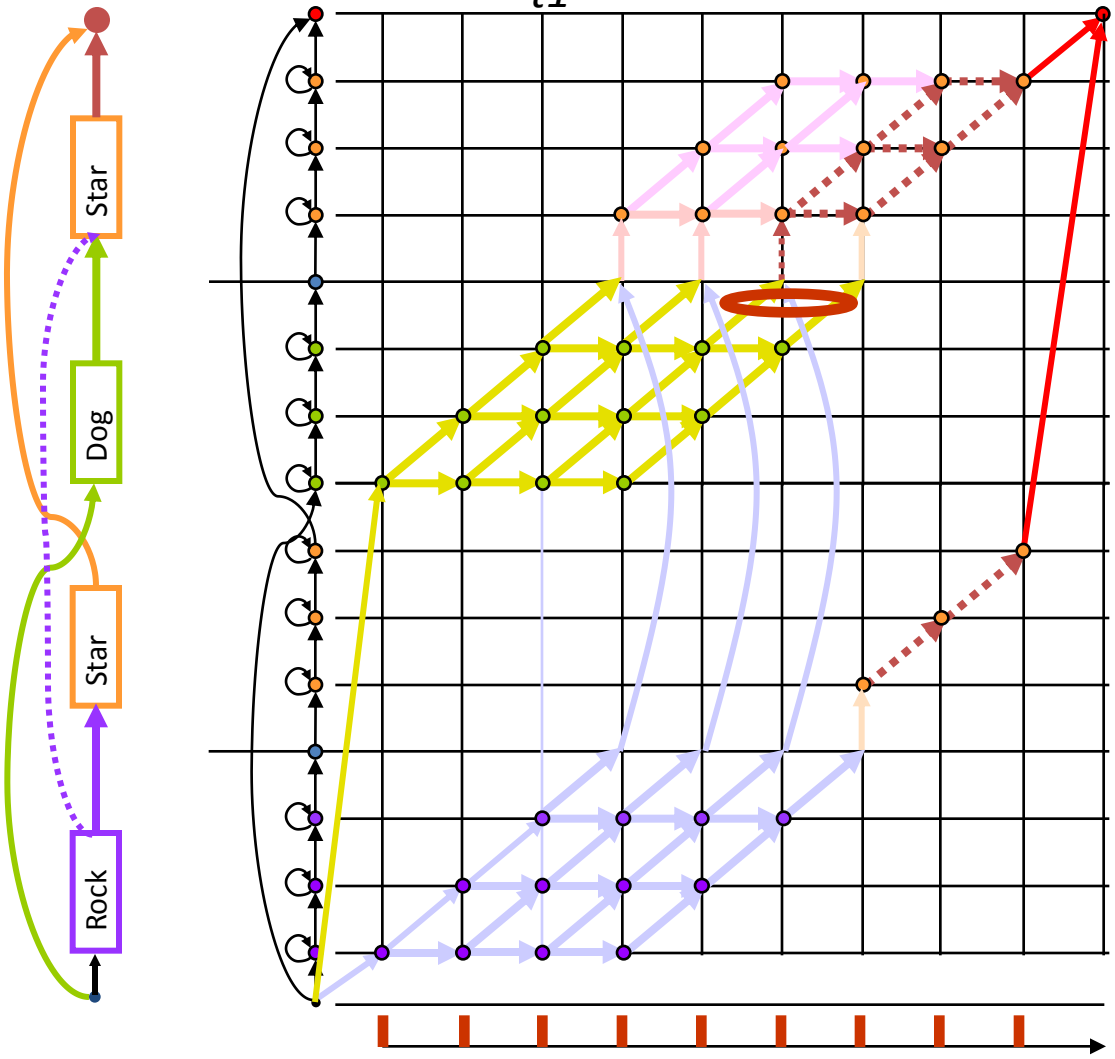




Similar logic can be applied at other entry points to *Star*

max(max(dogstar), max(rockstar))
=
max (
max(dogstar1, rockstar1),
max(dogstar2, rockstar2),
max (dogstar3,rockstar3),
max(dogstar4,rockstar4)
)

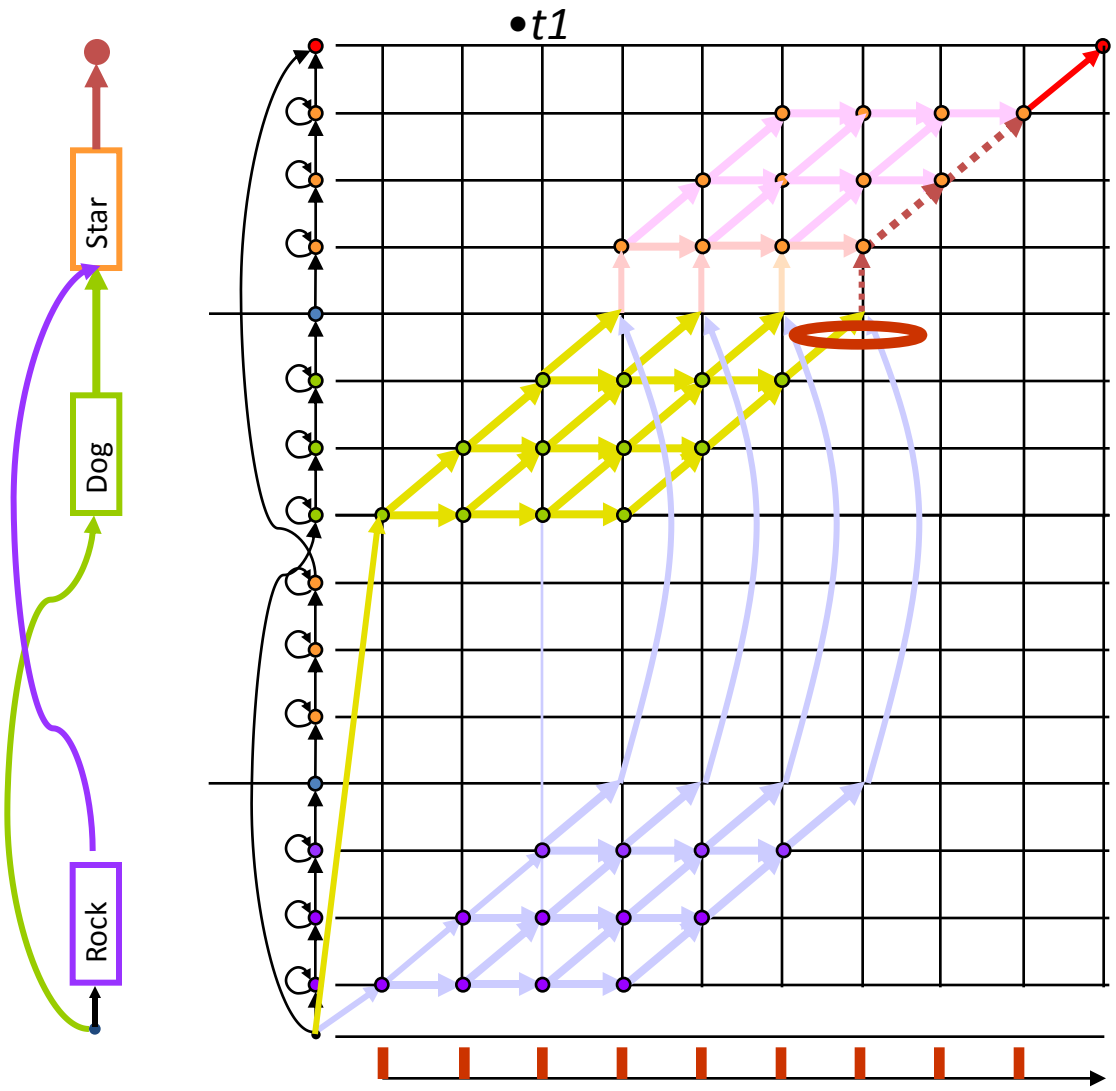
Max (dogstar3, rockstar3)



Similar logic can be applied at other entry points to *Star*

max(max(dogstar), max(rockstar))
=
max (
max(dogstar1, rockstar1),
max(dogstar2, rockstar2),
max (dogstar3,rockstar3),
max(dogstar4,rockstar4)
)

Max (dogstar4, rockstar4)



Similar logic can be applied at other entry points to *Star*

max(max(dogstar), max(rockstar))
=
max (
max(dogstar1, rockstar1),
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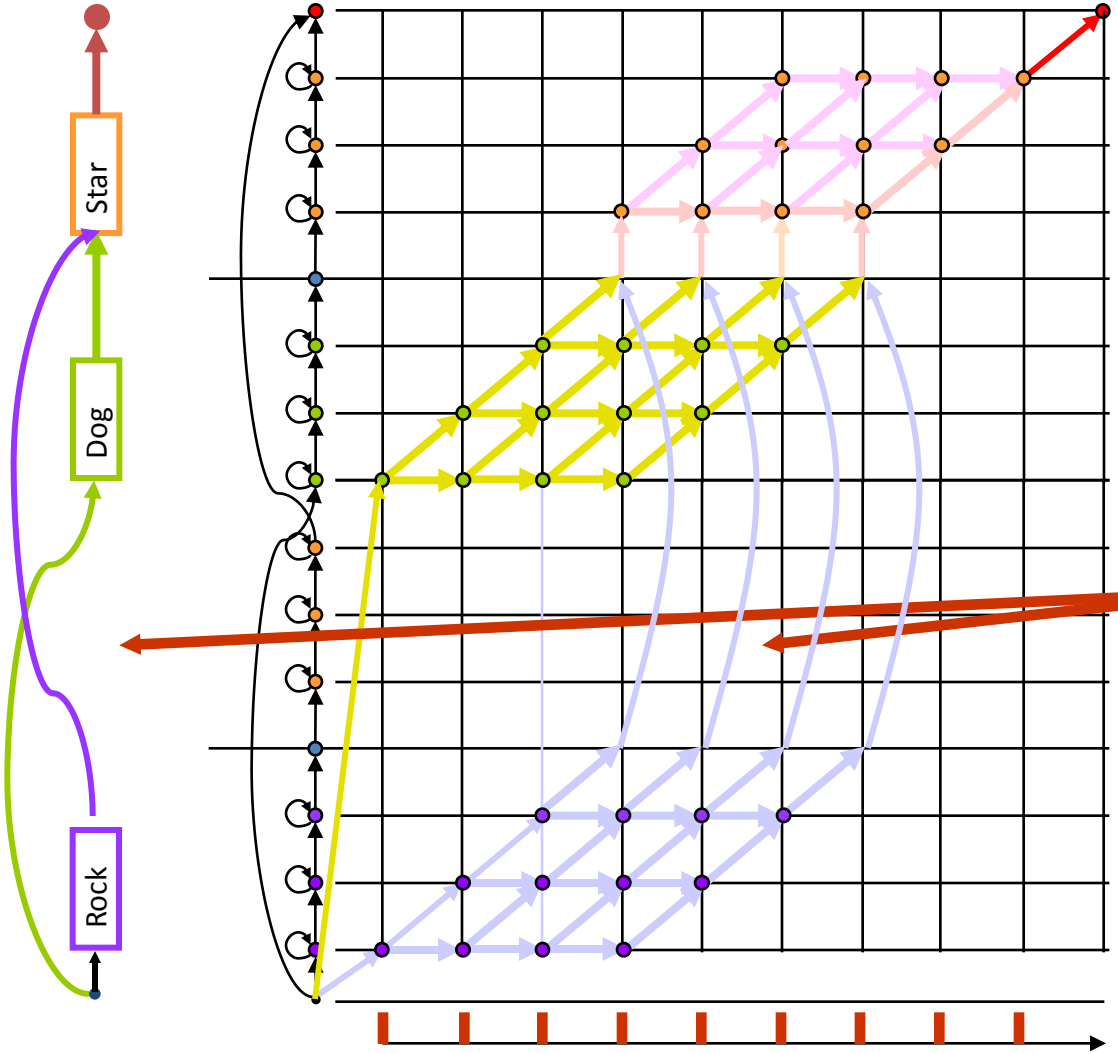
max (dogstar3,rockstar3),
max(dogstar4,rockstar4)
)

Decoding to classify between word sequences

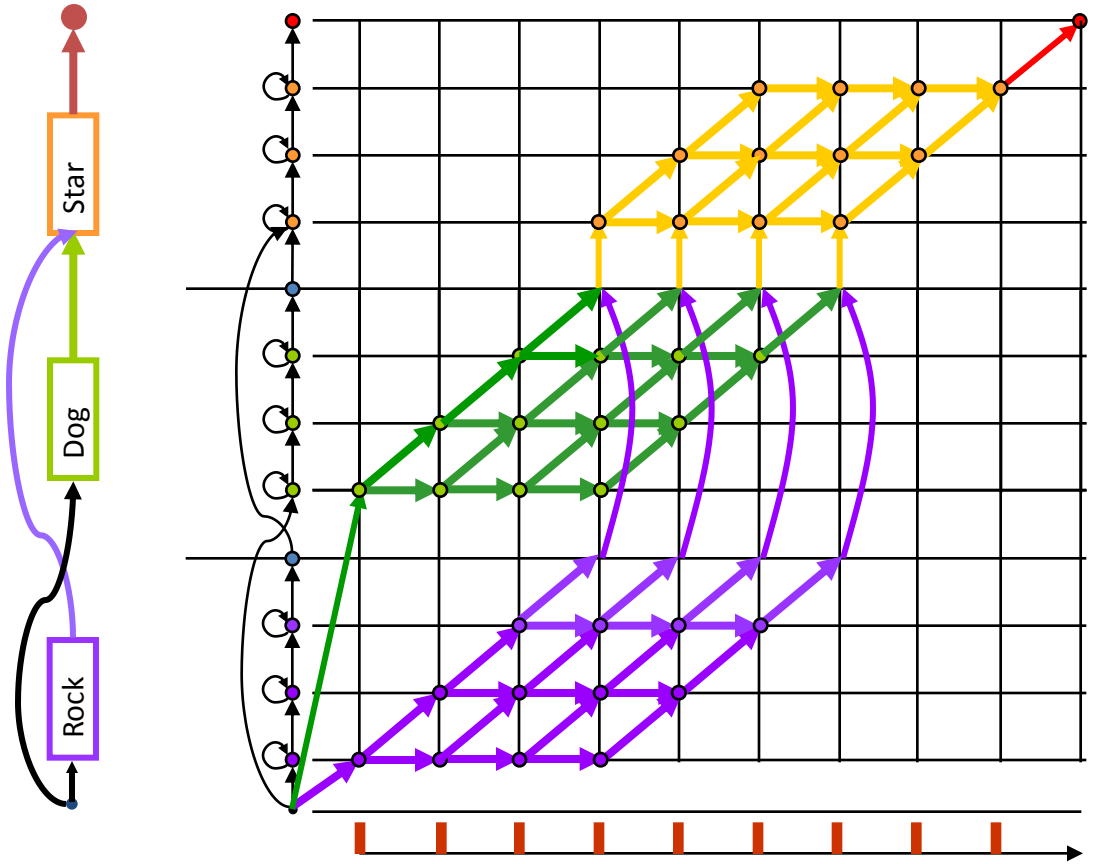


Similar logic can be applied at other entry points to *Star*

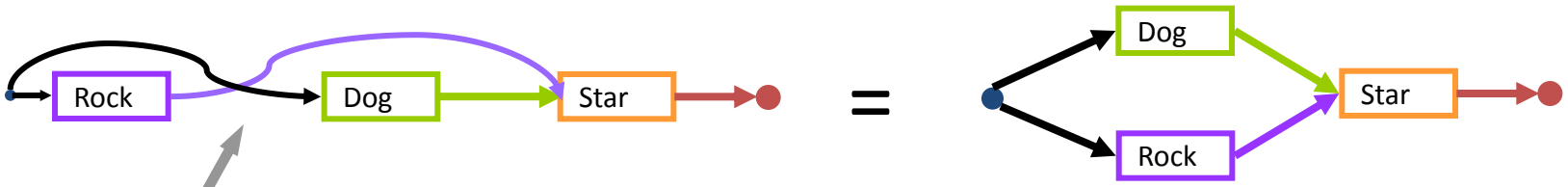
This copy of the trellis for *STAR* is completely removed

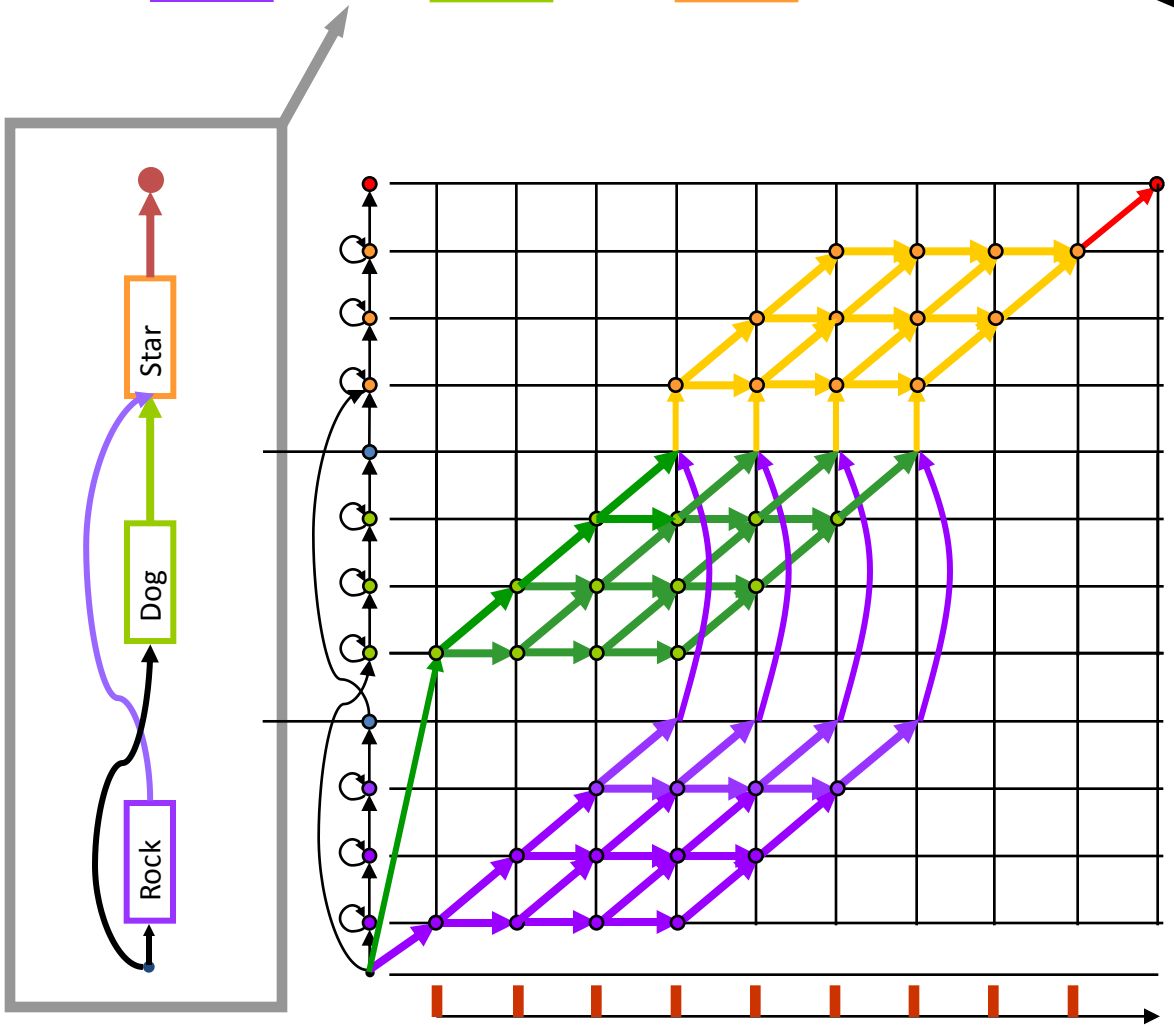
Decoding to classify between word sequences

- The two instances of *Star* can be collapsed into one to form a smaller trellis



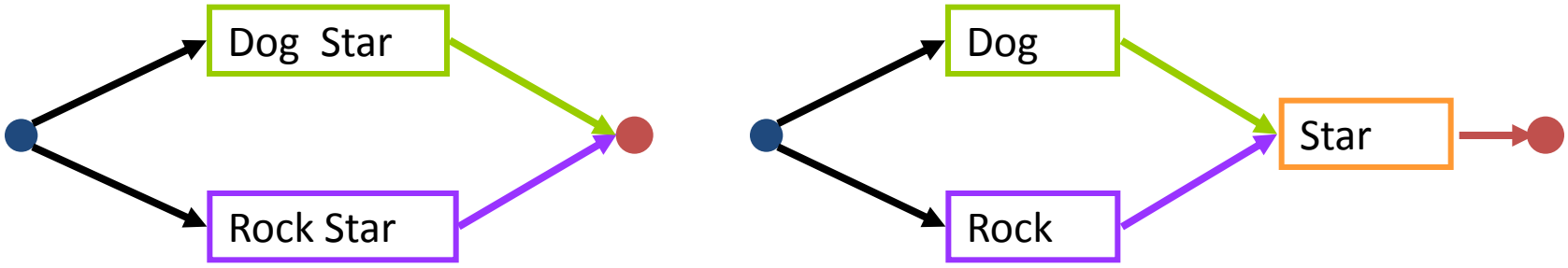
Language-HMMs for fixed length word sequences





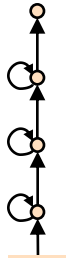
We will represent the vertical axis of the trellis in this simplified manner

The Real "Classes"

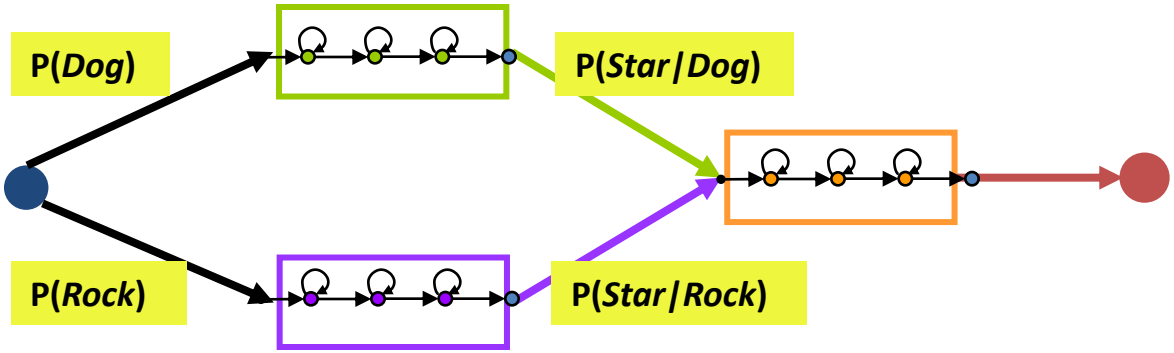


- The actual recognition is DOG STAR vs. ROCK STAR
  - i.e. the two items that form our "classes" are entire phrases
- The reduced graph to the right is merely an engineering reduction obtained by utilizing commonalities in the two phrases (STAR)
  - **Only possible because we use the best path score and not the entire forward probability**
- This distinction affects the design of the recognition system

Language-HMMs for fixed length word sequences



Each word is an HMM

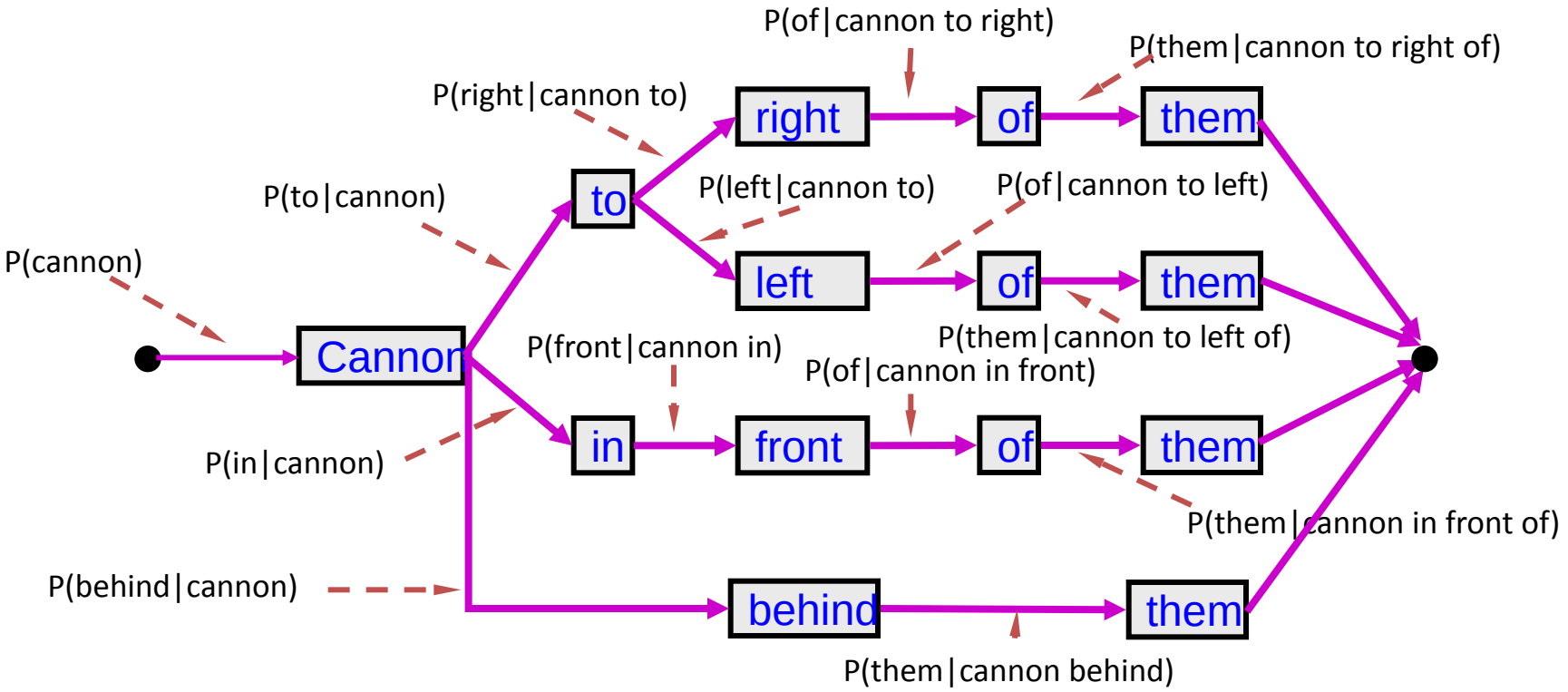


- The word graph represents all allowed word sequences in our example
  - The set of all allowed word sequences represents the allowed "language"
- At a more detailed level, the figure represents an HMM composed of the HMMs for all words in the word graph
  - This is the "Language HMM" – the HMM for the entire allowed language
- The language HMM represents the vertical axis of the trellis
  - It is the trellis, and NOT the language HMM, that is searched for the best path

Language-HMMs for fixed length word sequences

- Recognizing one of four lines from "charge of the light brigade"
  - Cannon to right of them
  - Cannon to left of them
  - Cannon in front of them
  - Cannon behind them

Each word is an HMM

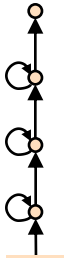


Where does the graph come from

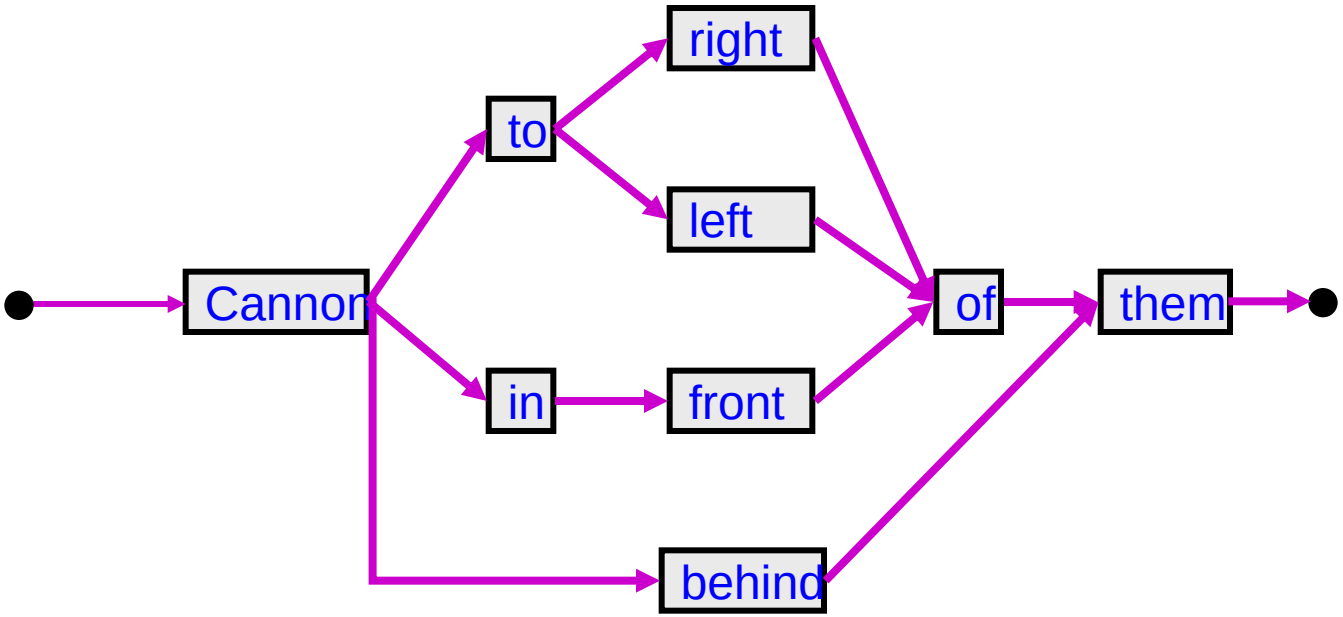
- The graph must be specified to the recognizer
  - What we are actually doing is to specify the complete set of "allowed" sentences in graph form
- May be specified as an FSG or a Context-Free Grammar
  - CFGs and FSG do not have probabilities associated with them
  - We could factor in prior biases through *probabilistic* FSG/CFGs
  - In probabilistic variants of FSGs and CFGs we associate probabilities with options
    - E.g. in the last graph

Simplification of the language HMM through lower context language models

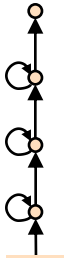
- Recognizing one of four lines from “charge of the light brigade”
- If we do not associate probabilities with FSG rules/transitions



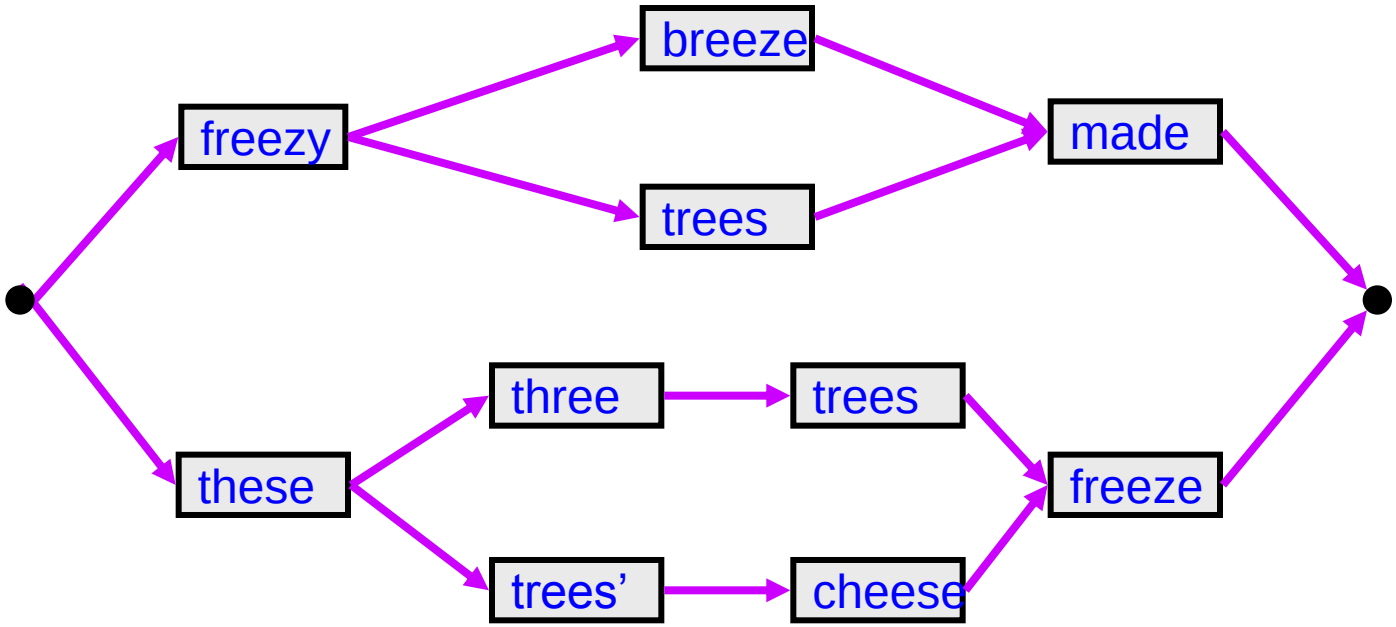
Each word is an HMM



Language HMMs for fixed-length word sequences: based on a grammar for Dr. Seuss

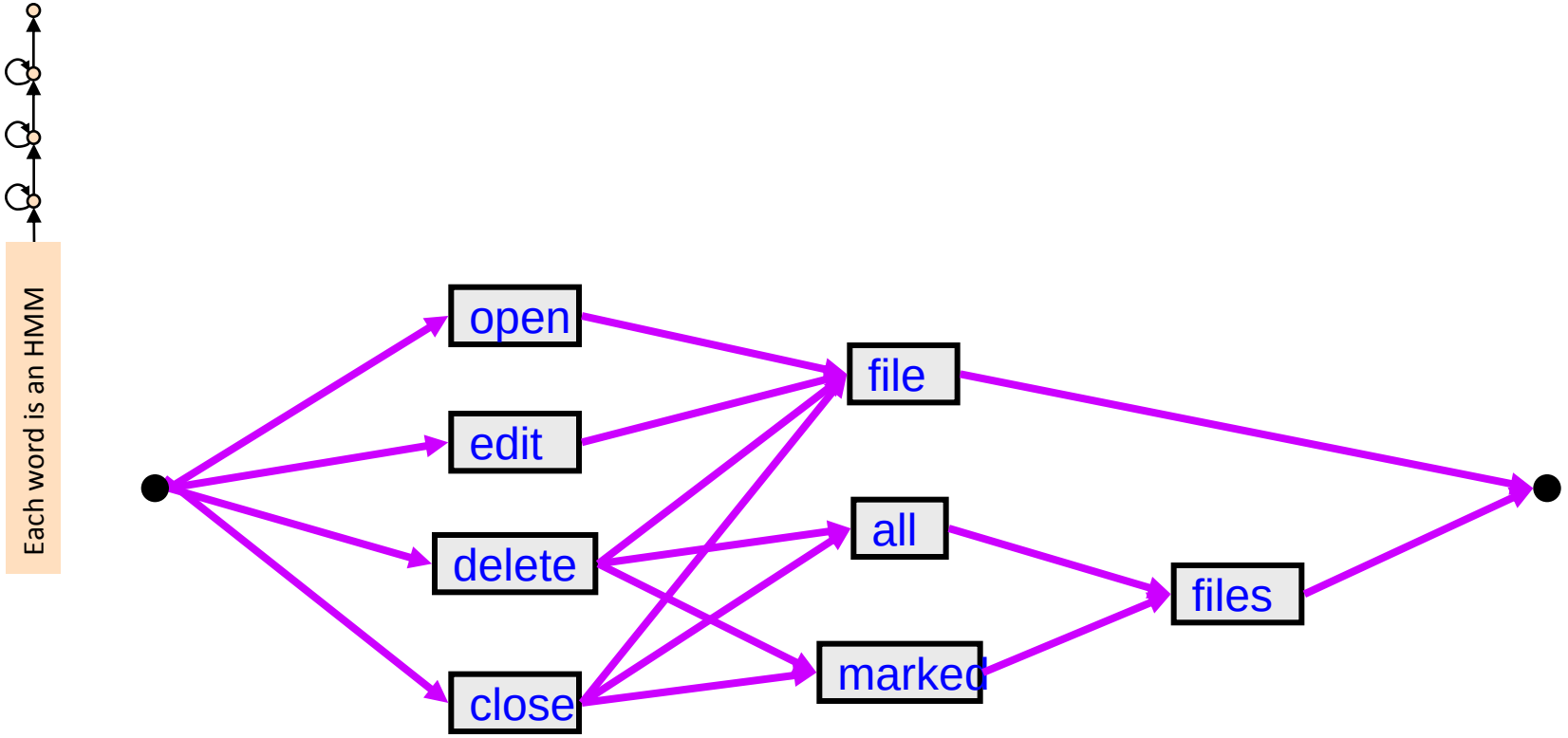


Each word is an HMM



No probabilities specified – a person may utter any of these phrases at any time

Language HMMs for fixed-length word sequences: command and control grammar



No probabilities specified – a person may utter any of these phrases at any time

Language HMMs for arbitrarily long word sequences

- Previous examples chose between a finite set of known word sequences
- Word sequences can be of arbitrary length
  - E.g. set of all word sequences that consist of an arbitrary number of repetitions of the word bang

    bang

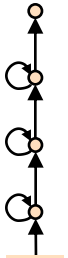
    bang bang

    bang bang bang

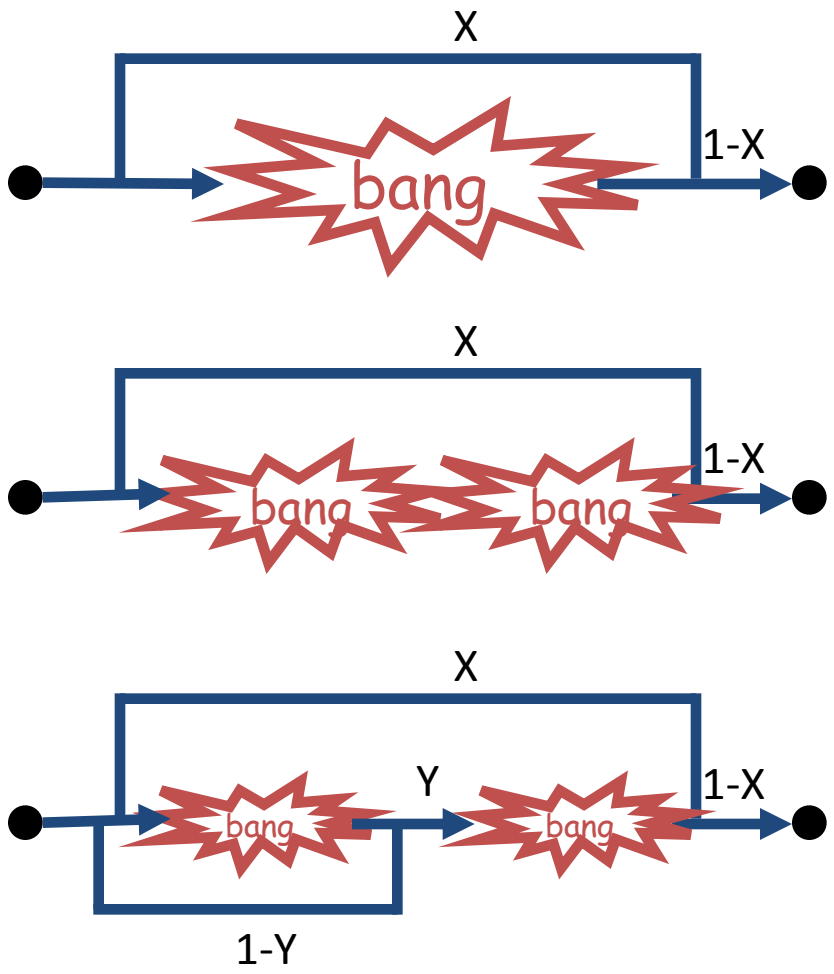
    bang bang bang bang

    ……
  - Forming explicit word-sequence graphs of the type we've seen so far is not possible
    - The number of possible sequences (with non-zero *a-priori* probability) is potentially infinite
    - Even if the longest sequence length is restricted, the graph will still be large

Language HMMs for arbitrarily long word sequences



- Arbitrary word sequences can be modeled with loops under some assumptions. E.g.:
- A "bang" can be followed by another "bang" with probability P("bang").
  - P("bang") = X;
    P(Termination) = 1-X;
- Bangs can occur only in pairs with probability X
- A more complex graph allows more complicated patterns
- You can extend this logic to other vocabularies where the speaker says other words in addition to "bang"
  - e.g. "bang bang you're dead"



Language HMMs for arbitrarily long word sequences

- Constrained set of word sequences with constrained vocabulary are realistic
  - Typically in command-and-control situations
    - Example: operating TV remote
  - Simple dialog systems
    - When the set of permitted responses to a query is restricted
- Unconstrained word sequences : Natural Language
  - State-of-art large vocabulary decoders
  - Later in the program..

QUESTIONS?

- Next up:
- Specifying grammars
- Pruning
- Simple continuous unrestrcted speech
- Backpointer table

- Any questions on topics so far?