

Anomaly detection in large graphs

Christos Faloutsos

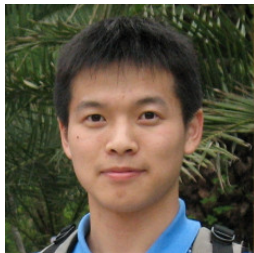
CMU

Thank you!

- Annette Jiang (IEEE)



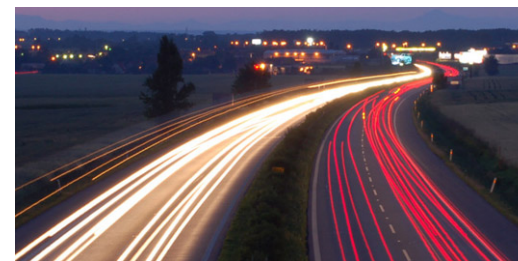
- Evan Butterfield (IEEE)



- Lei Li

Roadmap

- ➔ • Introduction – Motivation
 - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
- Conclusions



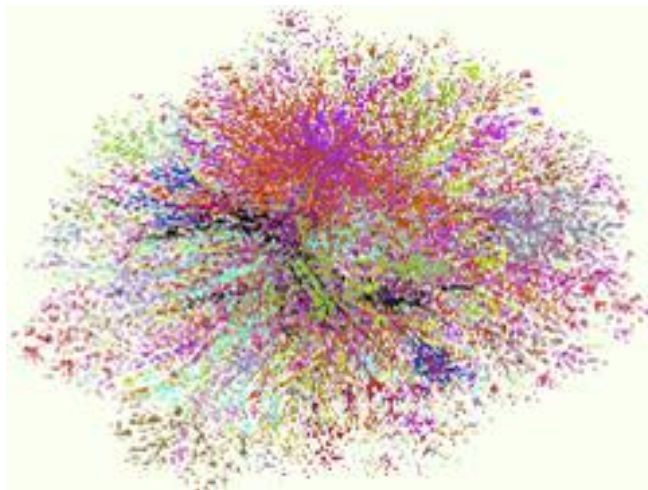
Graphs - why should we care?



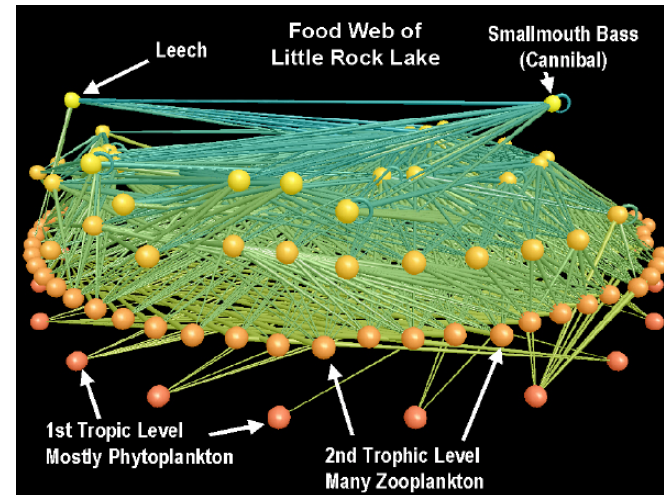
>\$10B; ~1B users



Graphs - why should we care?





Internet Map
[lumeta.com]



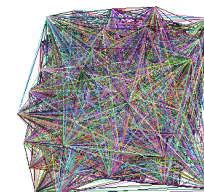
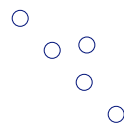
Food Web
[Martinez '91]

Graphs - why should we care?

- web-log ('blog') news propagation 
- computer network security: email/IP traffic and anomaly detection
- Recommendation systems 
-
- Many-to-many db relationship -> graph

Motivating problems

- P1: patterns? Fraud detection?



- P2: patterns in time-evolving graphs / tensors

destination

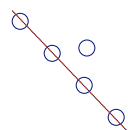


source

time

Motivating problems

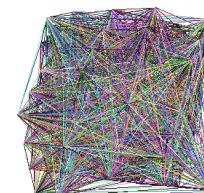
- P1: patterns? Fraud detection?



Patterns



anomalies



- P2: patterns in time-evolving graphs / tensors

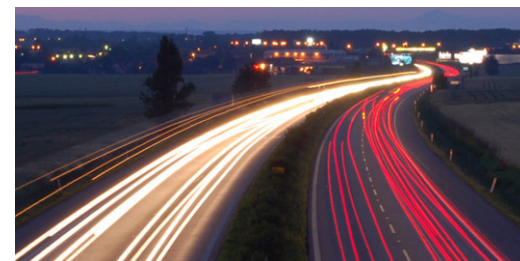
destination



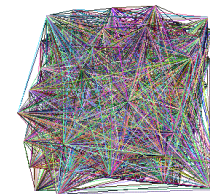
source

time

Roadmap



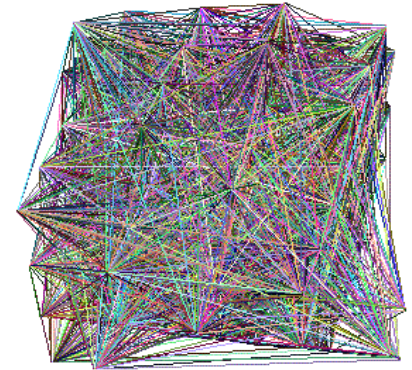
- Introduction – Motivation
 - Why study (big) graphs?
- ➔ • Part#1: Patterns & fraud detection
- Part#2: time-evolving graphs; tensors
- Conclusions



Part 1: Patterns, & fraud detection

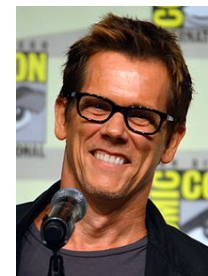
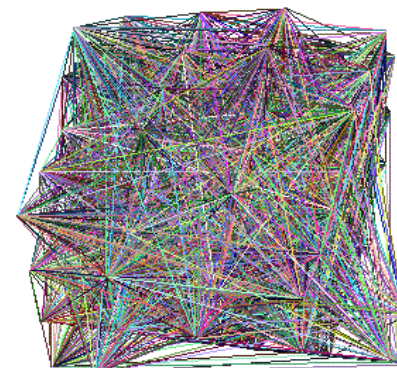
Laws and patterns

- Q1: Are real graphs random?



Laws and patterns

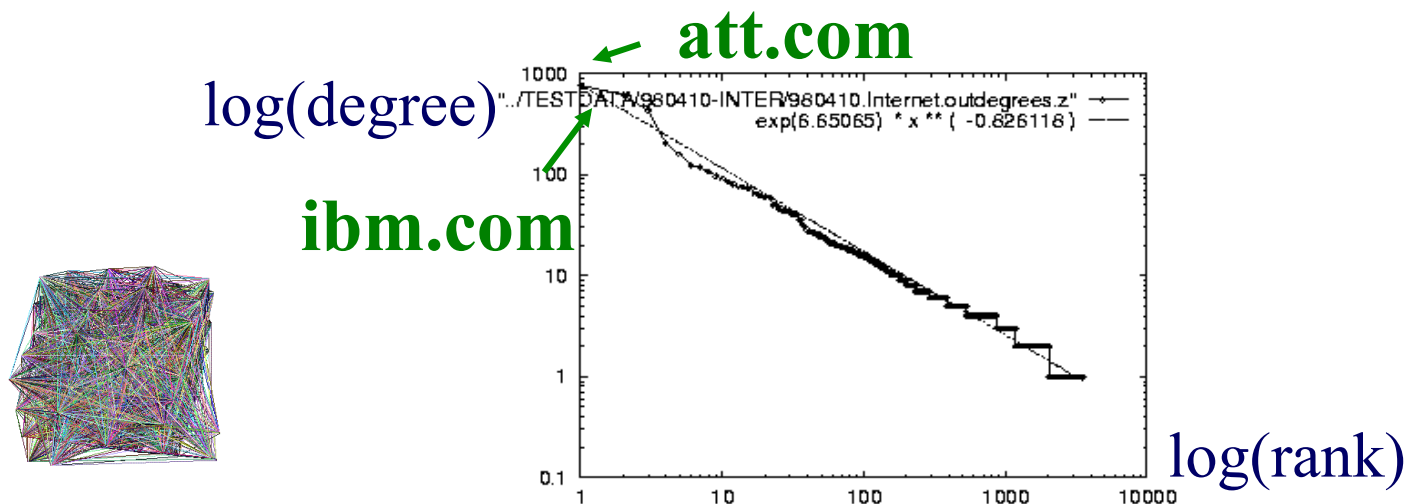
- Q1: Are real graphs random?
- A1: NO!!
 - Diameter ('6 degrees'; 'Kevin Bacon')
 - in- and out- degree distributions
 - other (surprising) patterns
- So, let's look at the data



Solution# S.1

- Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

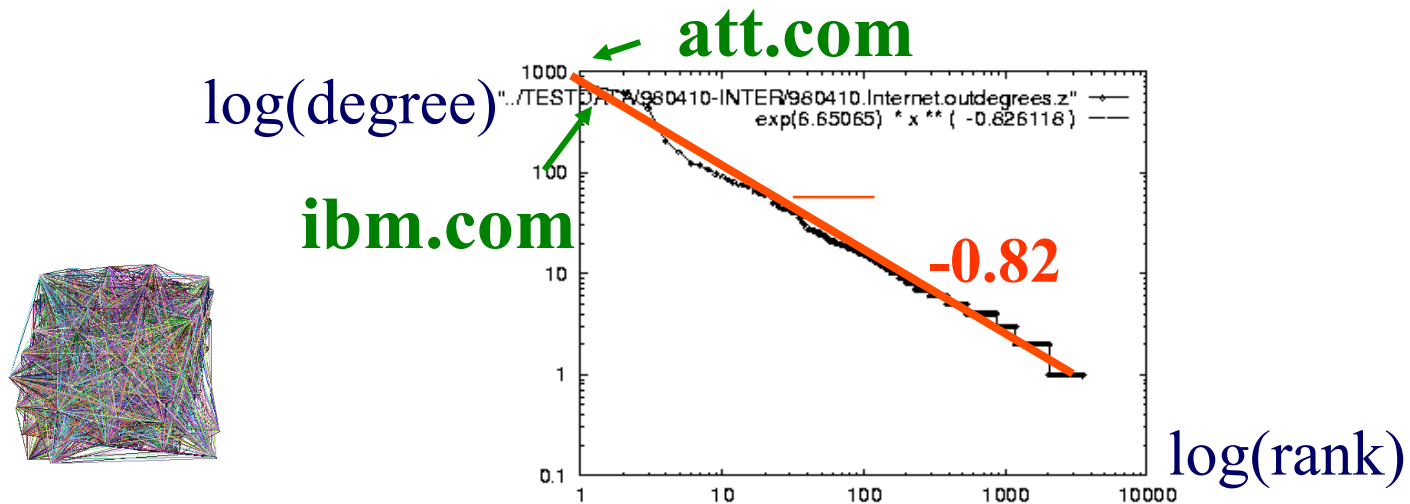
internet domains



Solution# S.1

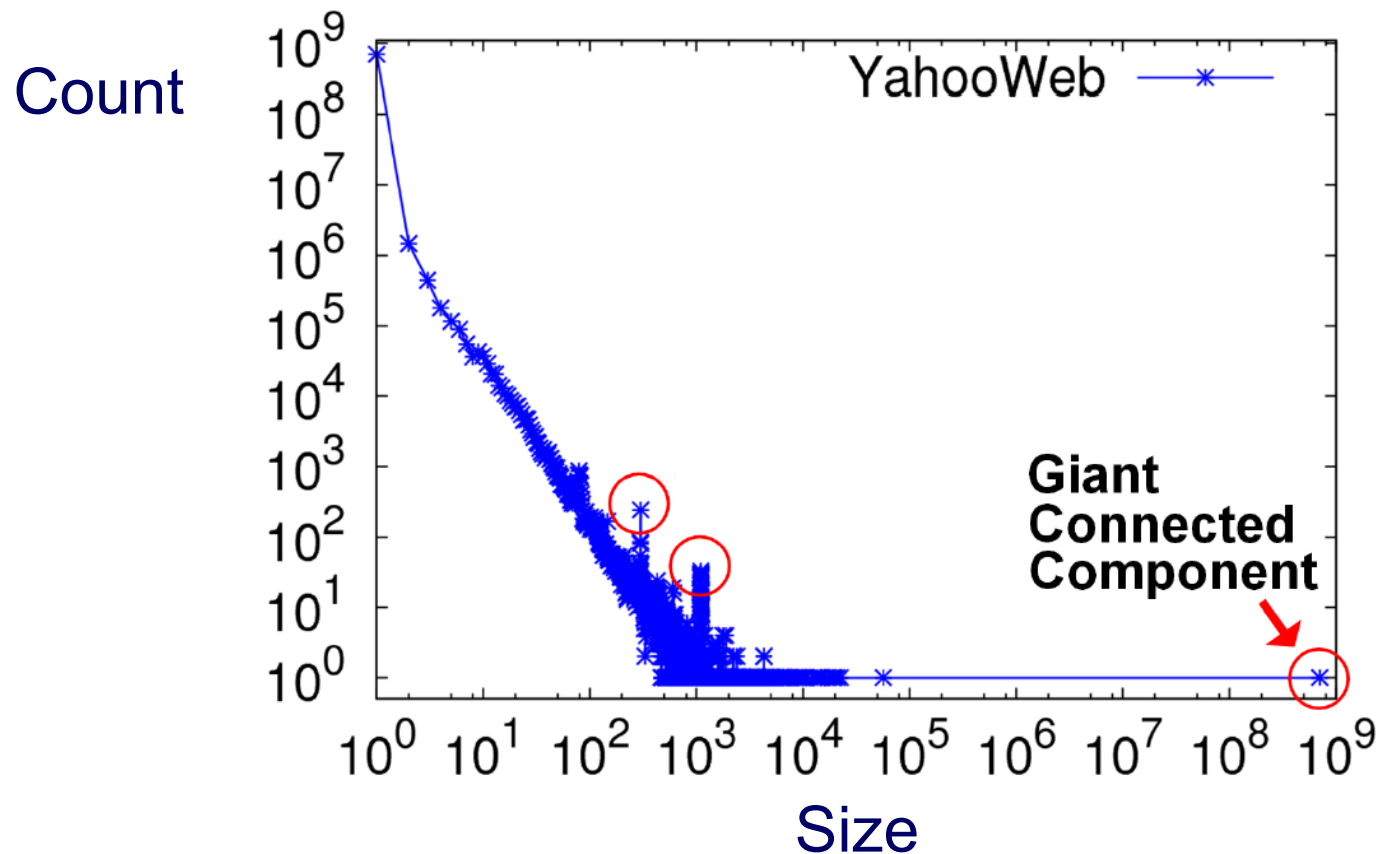
- Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

internet domains



S2: connected component sizes

- Connected Components – 4 observations:

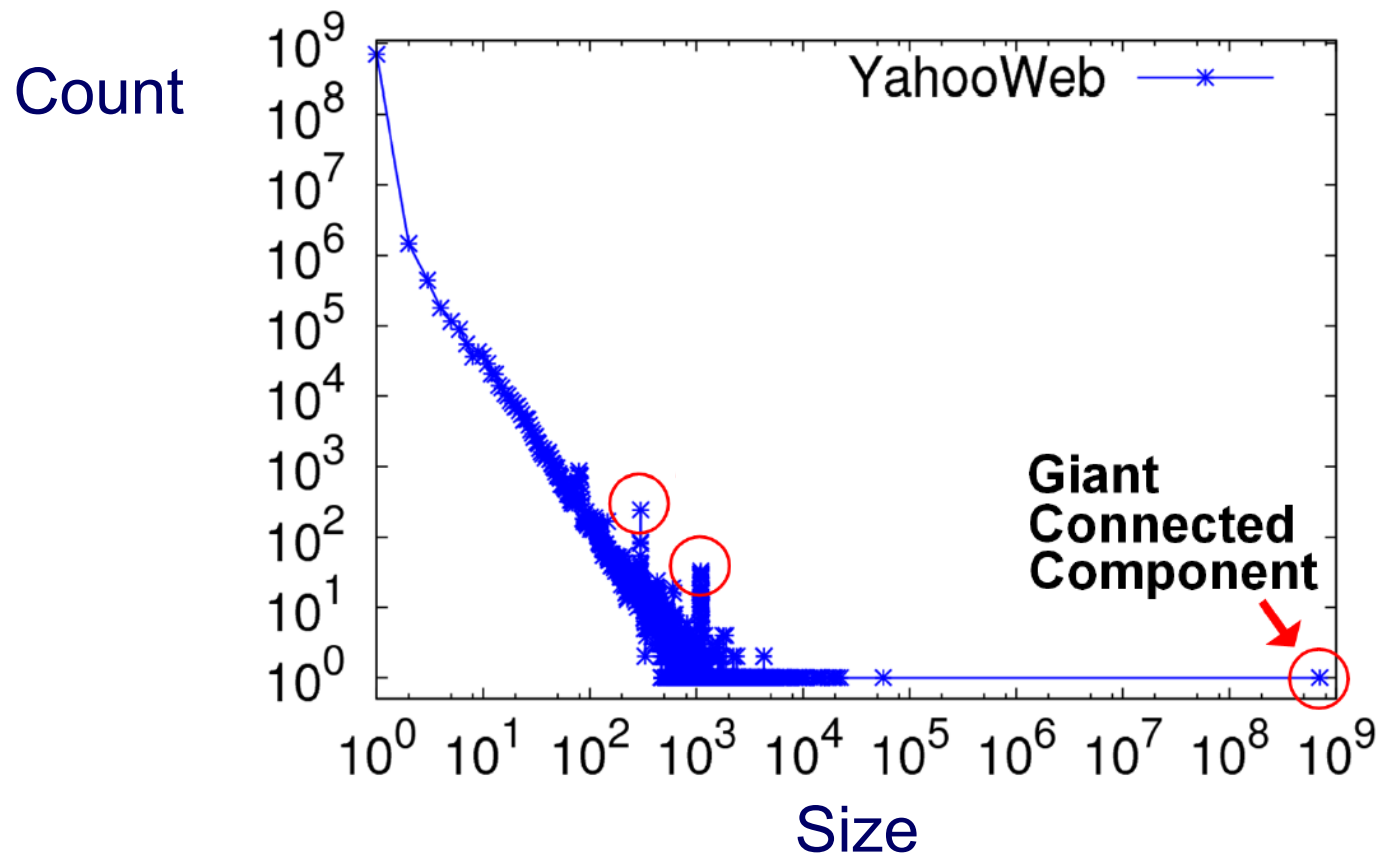


1.4B nodes
6B edges

S2: connected component sizes



- Connected Components

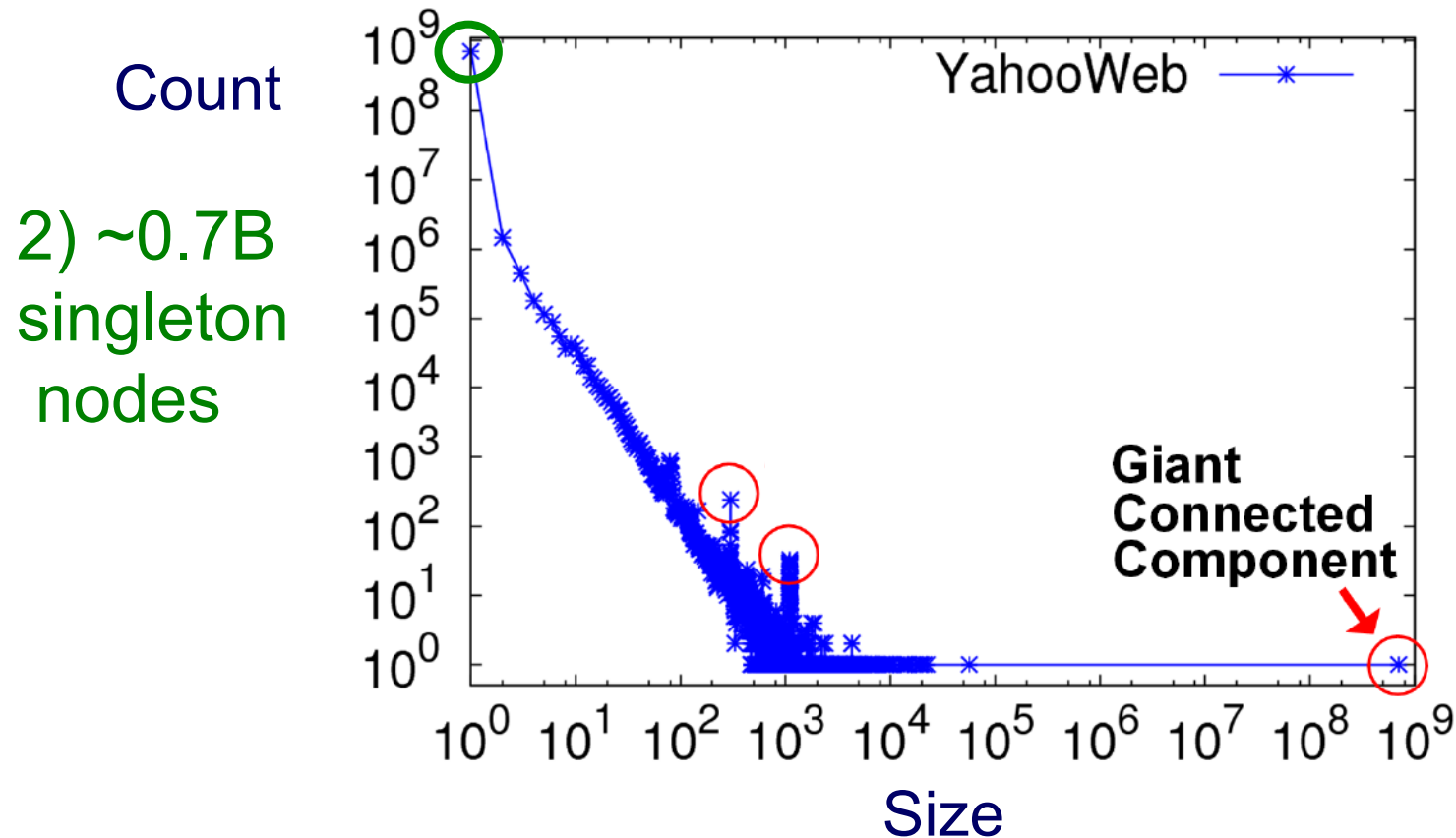


1) 10K x
larger
than next

S2: connected component sizes



- Connected Components

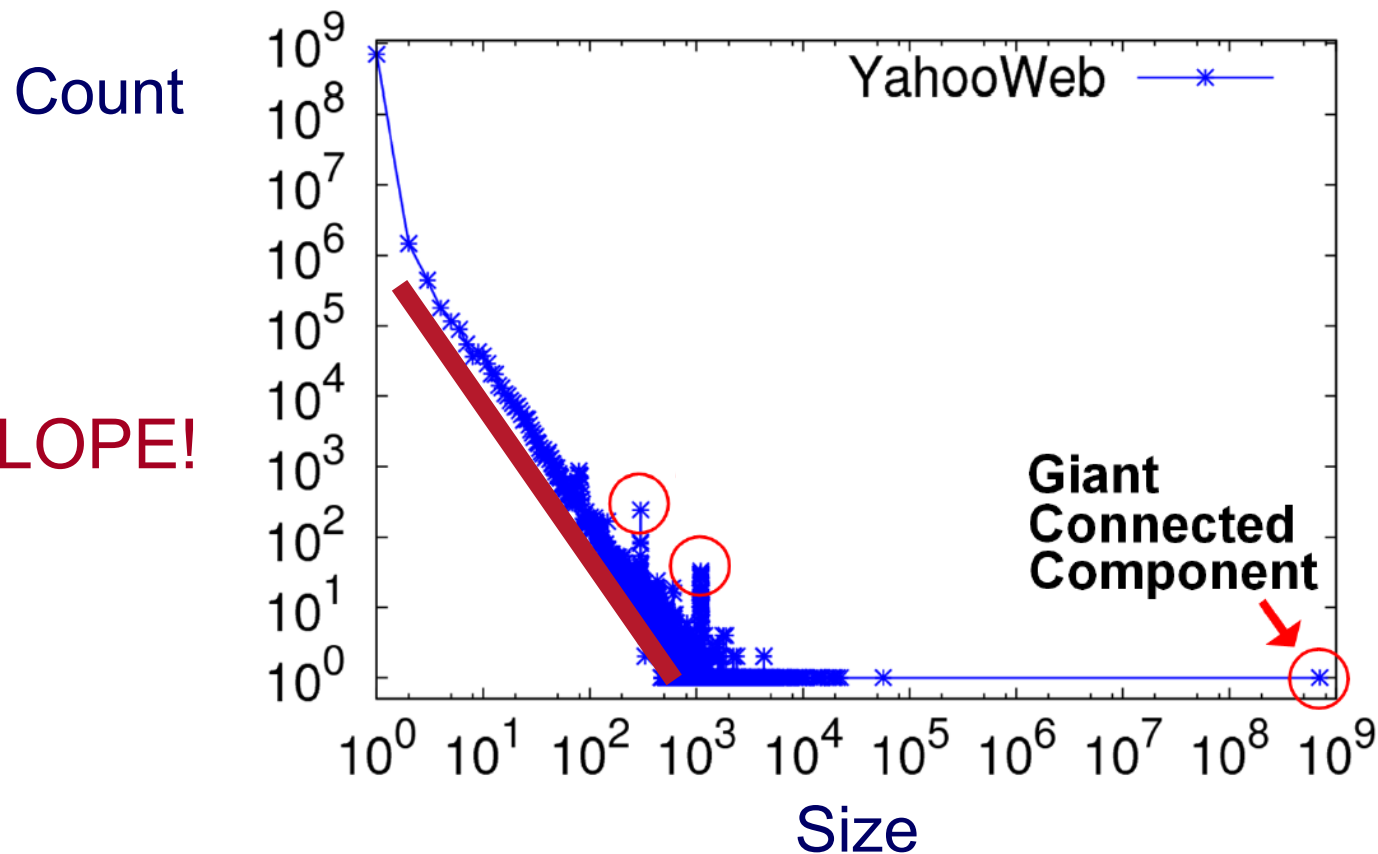


S2: connected component sizes



- Connected Components

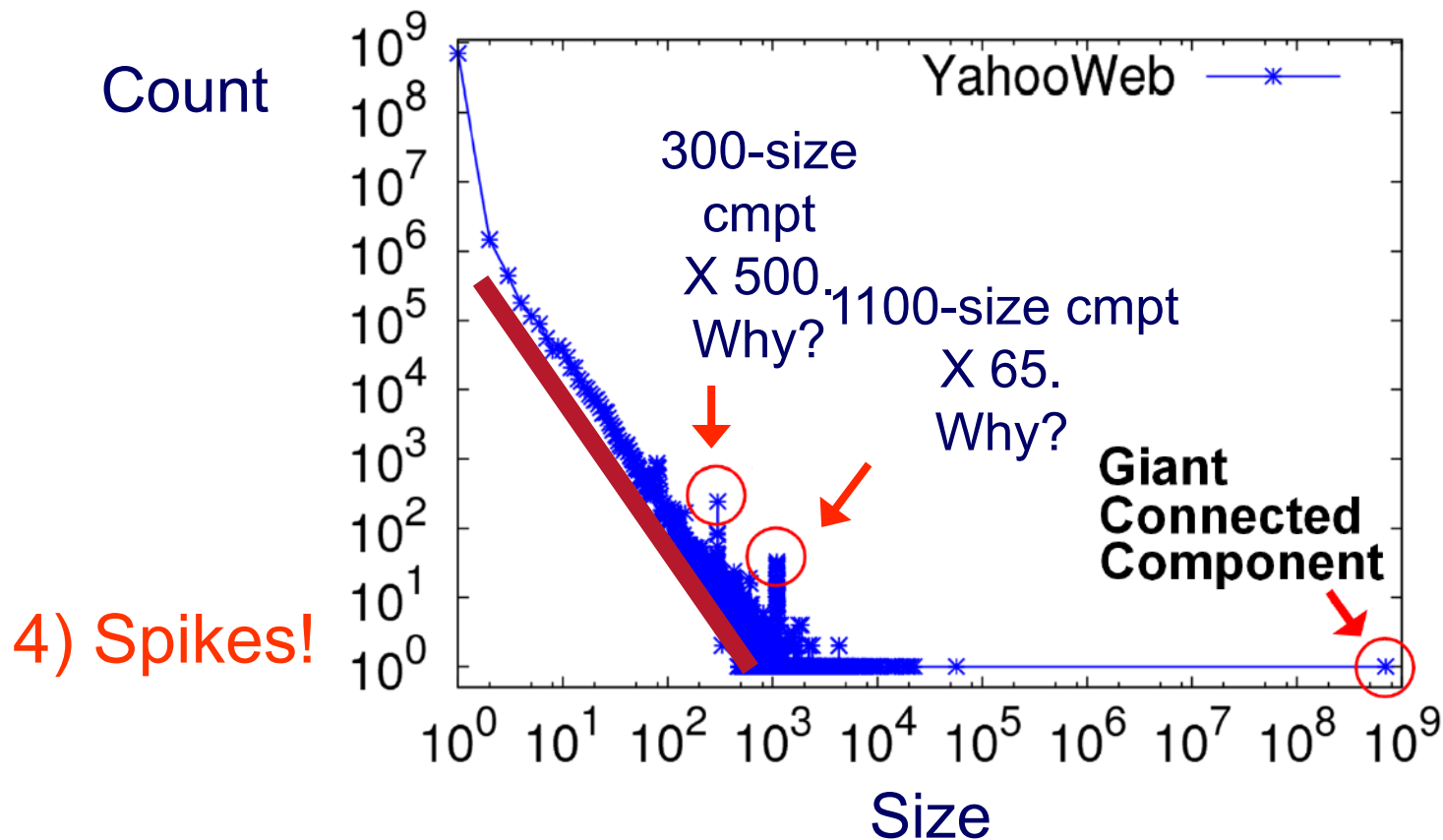
3) SLOPE!



S2: connected component sizes



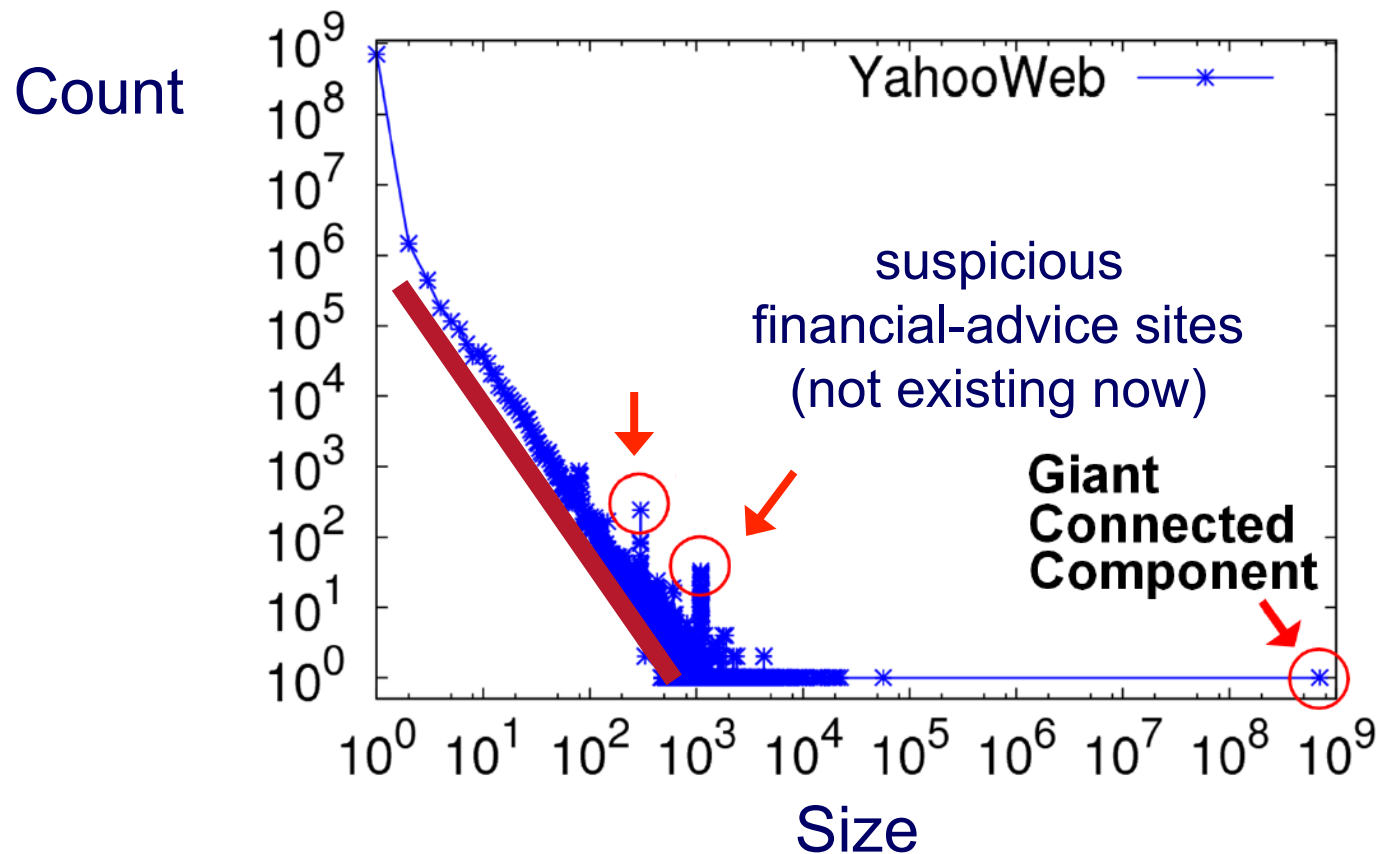
- Connected Components



S2: connected component sizes



- Connected Components

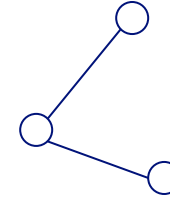


Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
 - ➔ – P1.1: Patterns: Degree; Triangles
 - P1.2: Anomaly/fraud detection
- Part#2: time-evolving graphs; tensors
- Conclusions

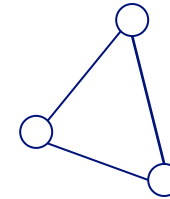


Solution# S.3: Triangle ‘Laws’

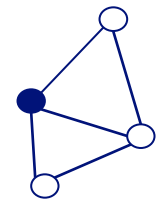


- Real social networks have a lot of triangles

Solution# S.3: Triangle ‘Laws’



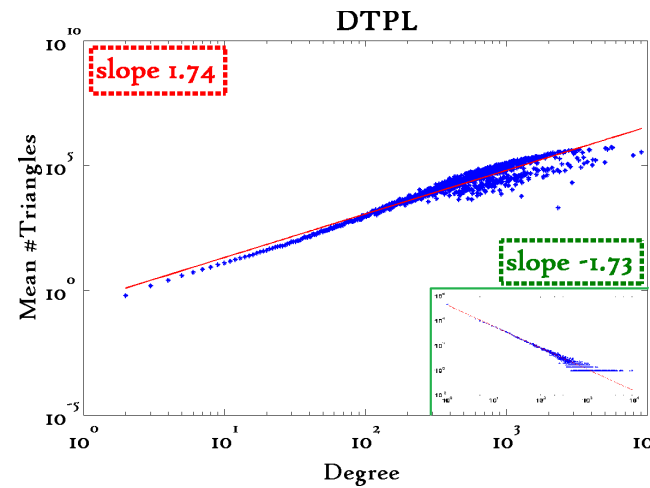
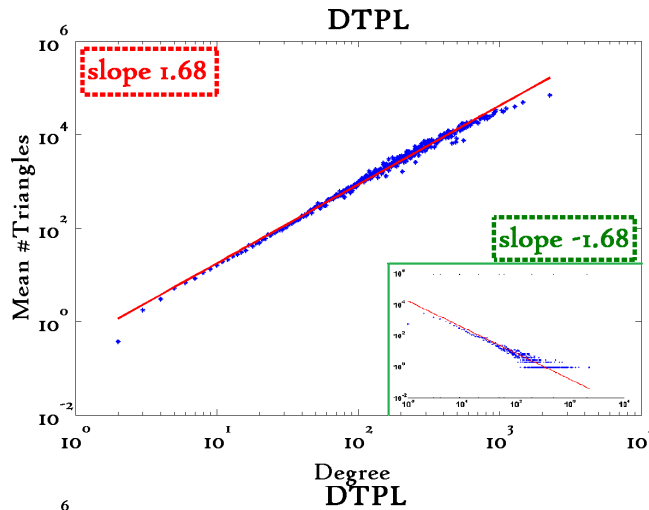
- Real social networks have a lot of triangles
 - Friends of friends are friends
- Any patterns?
 - 2x the friends, 2x the triangles ?



Triangle Law: #S.3

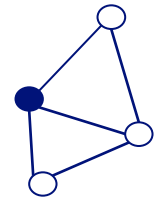
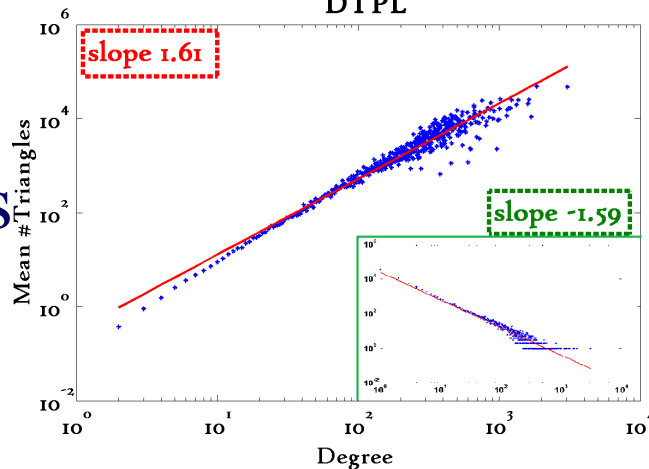
[Tsourakakis ICDM 2008]

Reuters



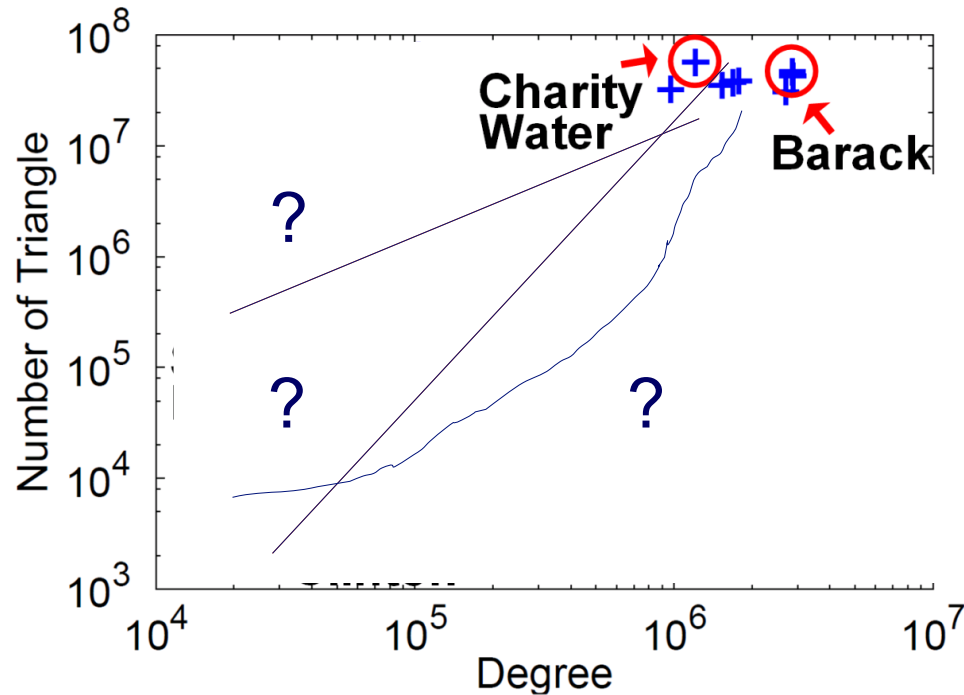
SN

Epinions



X-axis: degree
 Y-axis: mean # triangles
 n friends $\rightarrow \sim n^{1.6}$ triangles

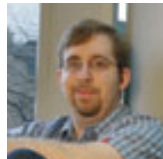
Triangle counting for large graphs?



Anomalous nodes in Twitter (~ 3 billion edges)

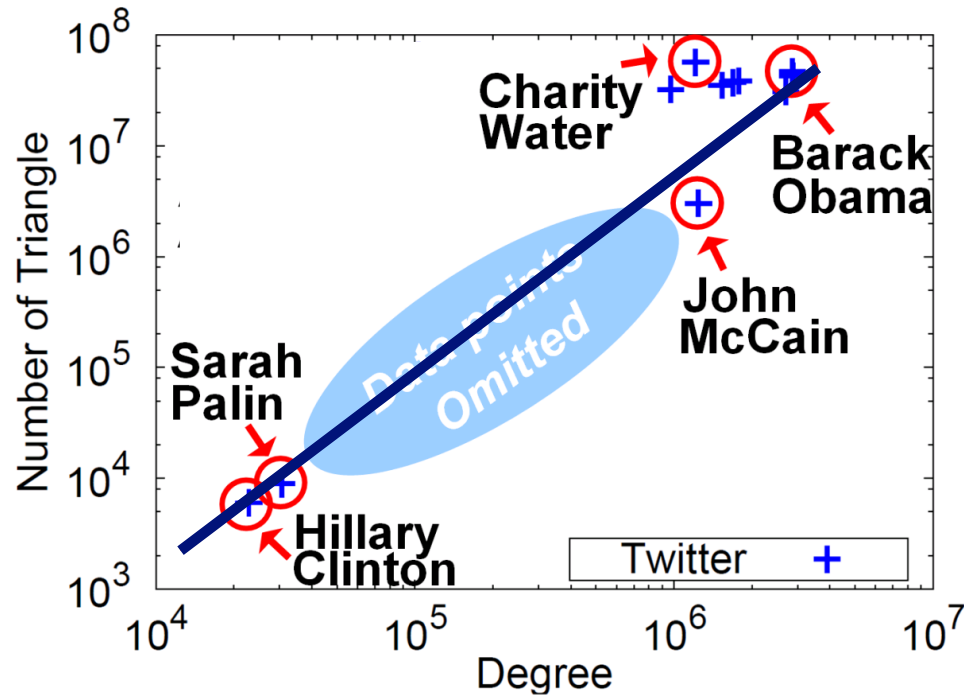
[U Kang, Brendan Meeder, +, PAKDD'11]

Toutiao/Byte-Dance



(c) C. Faloutsos, 2017

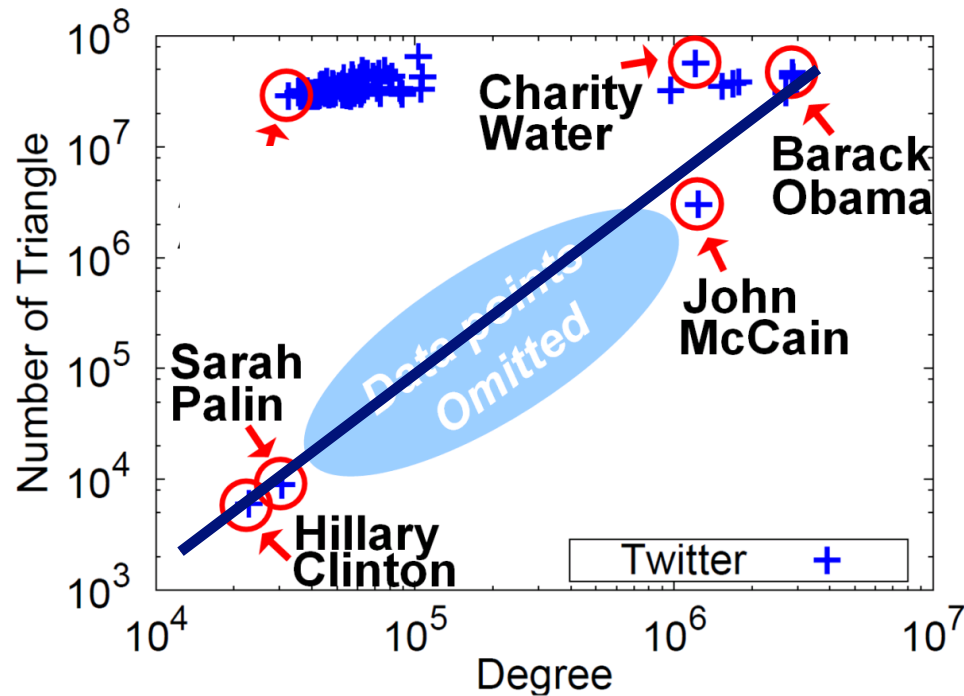
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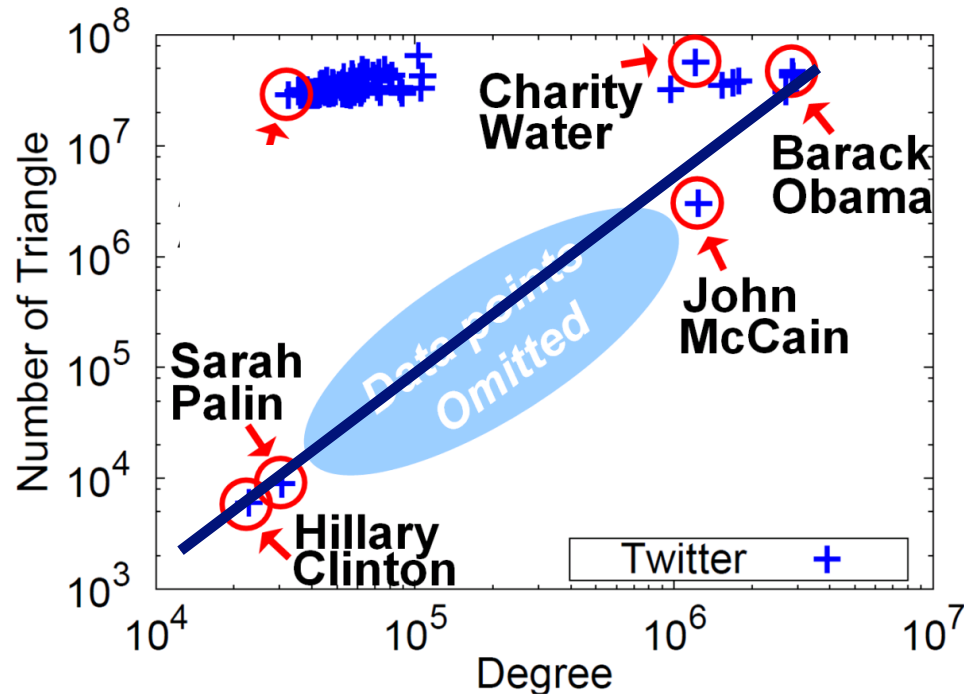
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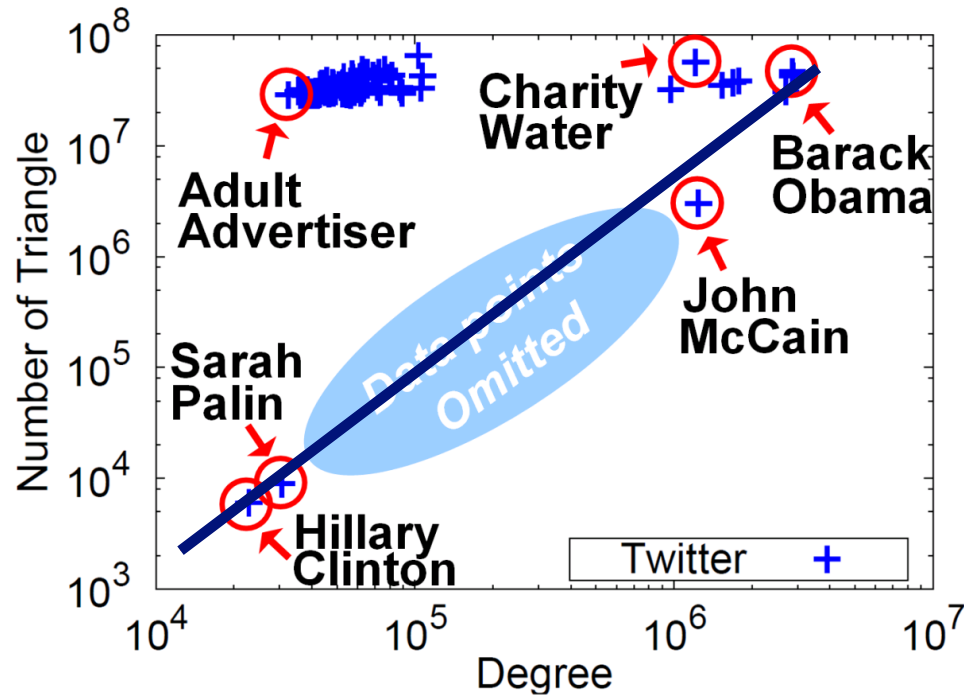
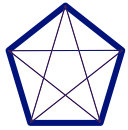
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Triangle counting for large graphs?

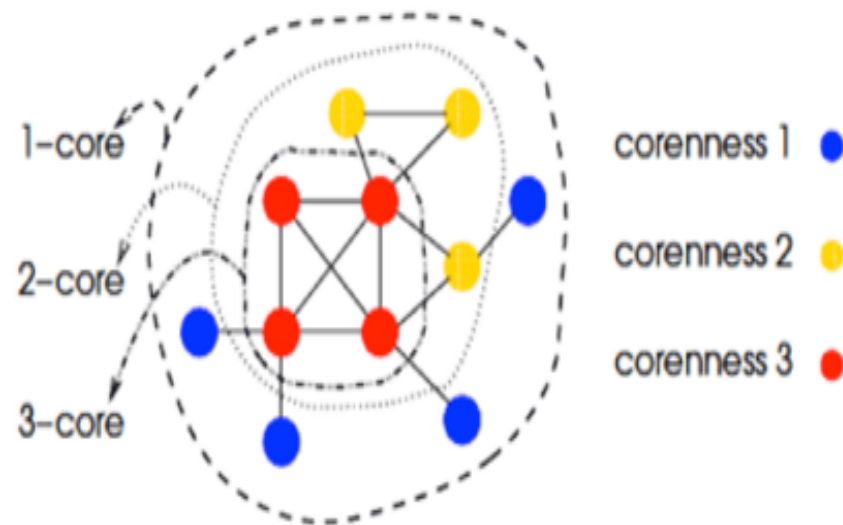


Anomalous nodes in Twitter (~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]

S4: k-core patterns - defn

- **k-core** (of a graph)
- **degeneracy** (of a graph)
- **coreness** (of a vertex)



CoreScope: Graph Mining Using k- Core Analysis - Patterns, Anomalies, and Algorithms

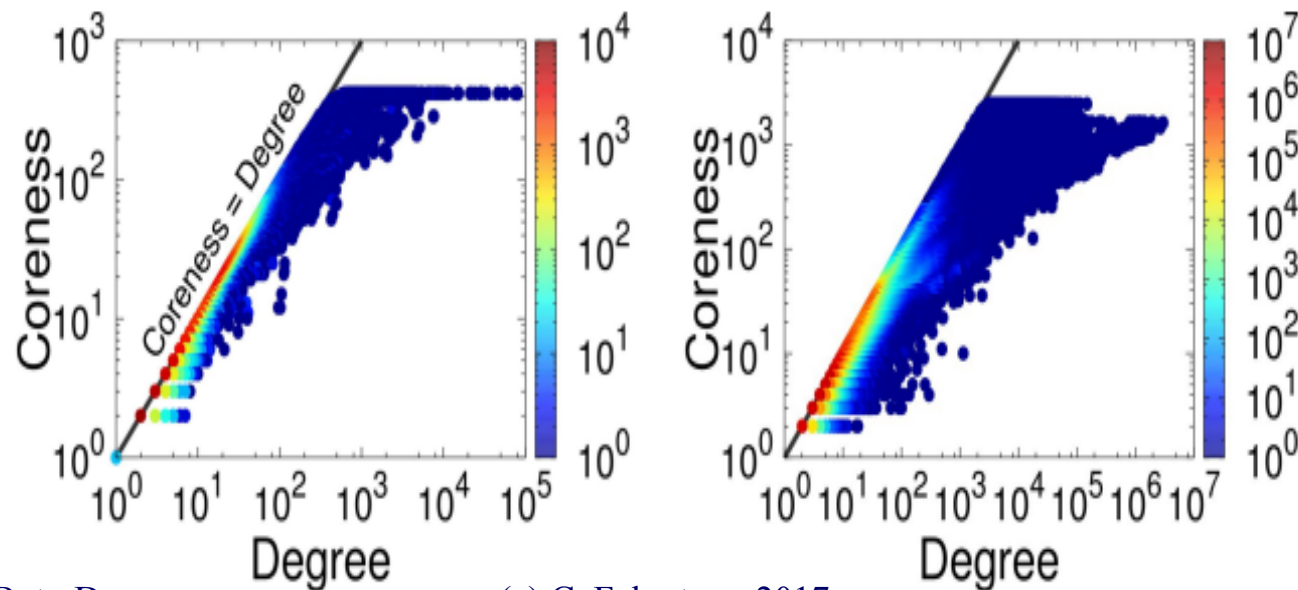
ICDM'16 (to appear)

Kijung Shin, Tina Eliassi-Rad and CF



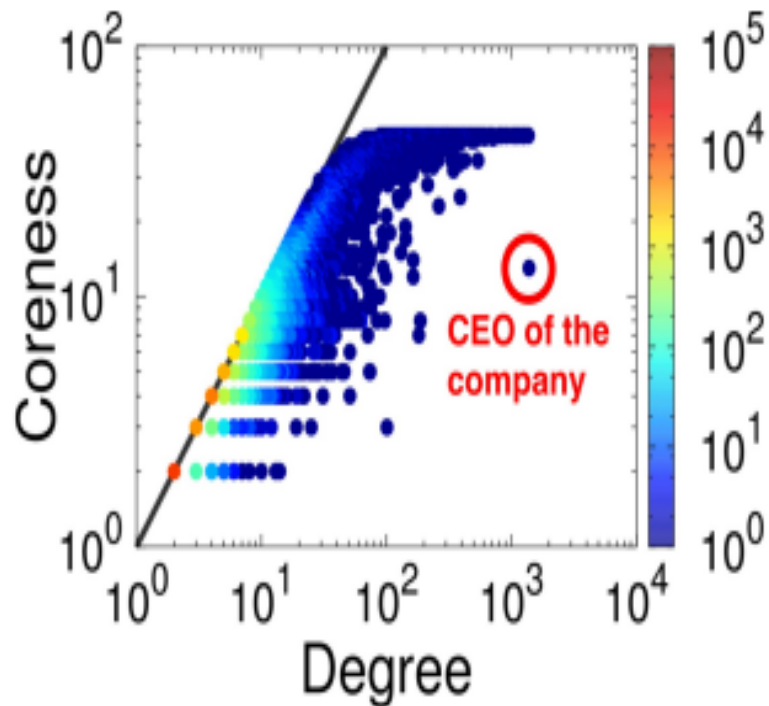
Mirror Pattern: Observation

- **coreness** (of a vertex): maximum k such that the vertex belongs to the k -core
- Definition: [Mirror Pattern] *degree* \sim *coreness*

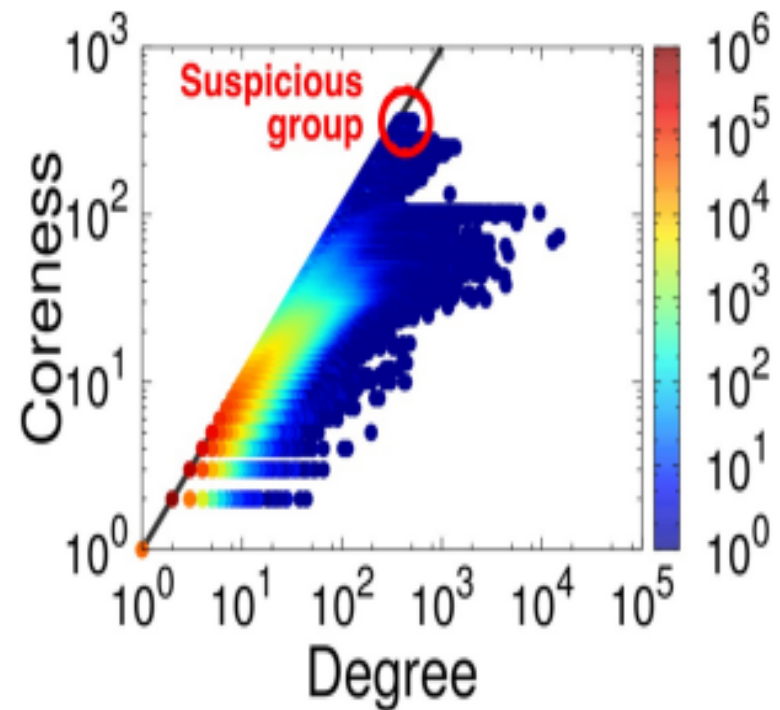


Mirror Pattern: Application

- Exceptions are ‘strange’



Email ($\rho = 0.98$)



LiveJournal ($\rho = 0.99$)

MORE Graph Patterns

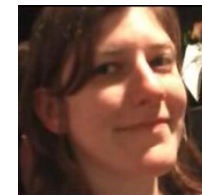
	Unweighted	Weighted
Static	<p>L01. Power-law degree distribution [Faloutsos et al. '99, Kleinberg et al. '99, Chakrabarti et al. '04, Newman '04]</p> <p>L02. Triangle Power Law (TPL) [Tsourakakis '08]</p> <p>L03. Eigenvalue Power Law (EPL) [Siganos et al. '03]</p> <p>L04. Community structure [Flake et al. '02, Girvan and Newman '02]</p>	<p>L10. Snapshot Power Law (SPL) [McGlohon et al. '08]</p>
Dynamic	<p>L05. Densification Power Law (DPL) [Leskovec et al. '05]</p> <p>L06. Small and shrinking diameter [Albert and Barabási '99, Leskovec et al. '05]</p> <p>L07. Constant size 2nd and 3rd connected components [McGlohon et al. '08]</p> <p>L08. Principal Eigenvalue Power Law (λ_1PL) [Akoglu et al. '08]</p> <p>L09. Bursty/self-similar edge/weight additions [Gomez and Santonja '98, Gribble et al. '98, Crovella and</p>	<p>L11. Weight Power Law (WPL) [McGlohon et al. '08]</p>

RTG: A Recursive Realistic Graph Generator using Random Typing Leman Akoglu and Christos Faloutsos. *PKDD'09*.

MORE Graph Patterns

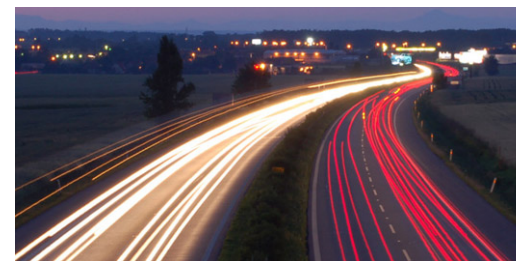
	Unweighted	Weighted
Static	<p>L01. Power-law degree distribution [Faloutsos et al. '99, Kleinberg et al. '99, Chakrabarti et al. '04, Newman '04]</p> <p>L02. Triangle Power Law (TPL) [Tsourakakis '08]</p> <p>L03. Eigenvalue Power Law (EPL) [Siganos et al. '03]</p> <p>L04. Community structure [Flake et al. '02, Girvan and Newman '02]</p>	<p>L10. Snapshot Power Law (SPL) [McGlohon et al. '08]</p>
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- Mary McGlohon, Leman Akoglu, Christos Faloutsos. *Statistical Properties of Social Networks*. in "Social Network Data Analytics" (Ed.: Charu Aggarwal)
- Deepayan Chakrabarti and Christos Faloutsos, [*Graph Mining: Laws, Tools, and Case Studies*](#) Oct. 2012, Morgan Claypool.



Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
 - P1.1: Patterns
 - – P1.2: Anomaly / fraud detection
 - No labels – spectral
 - With labels: Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions



Patterns

anomalies

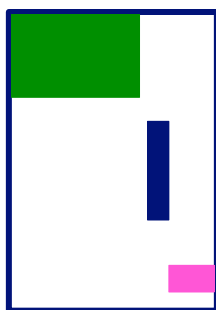
How to find ‘suspicious’ groups?

- ‘blocks’ are normal, right?



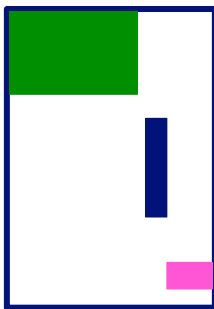
idols

fans



Except that:

- ‘blocks’ are normal, ~~right?~~
- ‘hyperbolic’ communities are more realistic [Araujo+, PKDD’14]



Toutiao/Byte-Dance



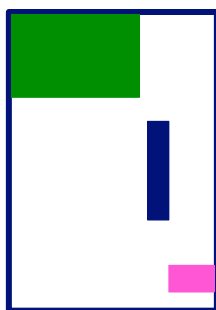
(c) C. Faloutsos, 2017

Except that:

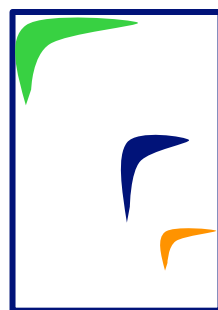
- ‘blocks’ are usually **suspicious**
- ‘hyperbolic’ communities are more realistic [Araujo+, PKDD’14]



Q: Can we spot blocks, easily?



Toutiao/Byte-Dance



(c) C. Faloutsos, 2017

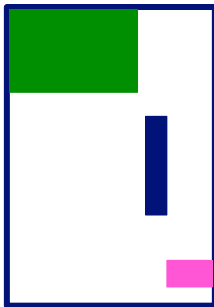
Except that:



- ‘blocks’ are usually **suspicious**
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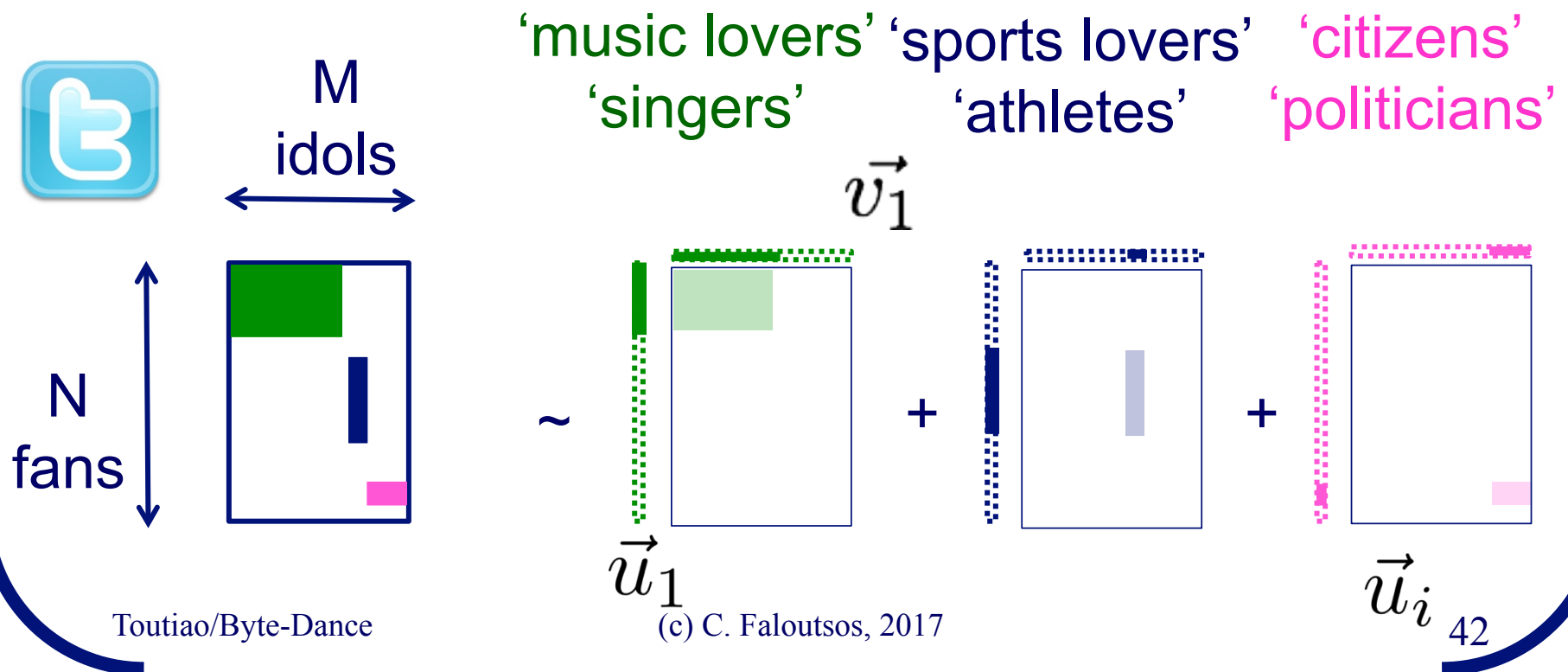
Q: Can we spot blocks, easily?

A: Silver bullet: SVD!



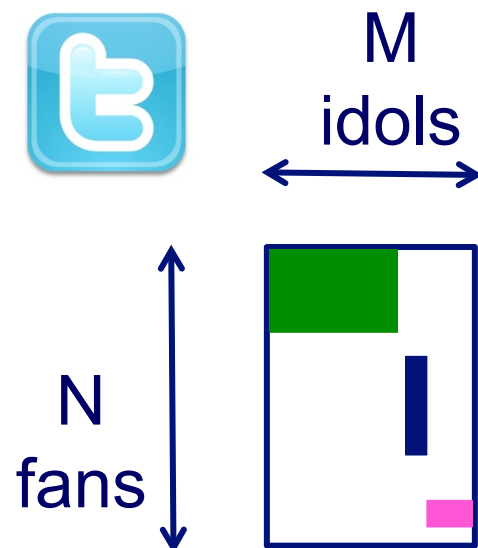
Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks

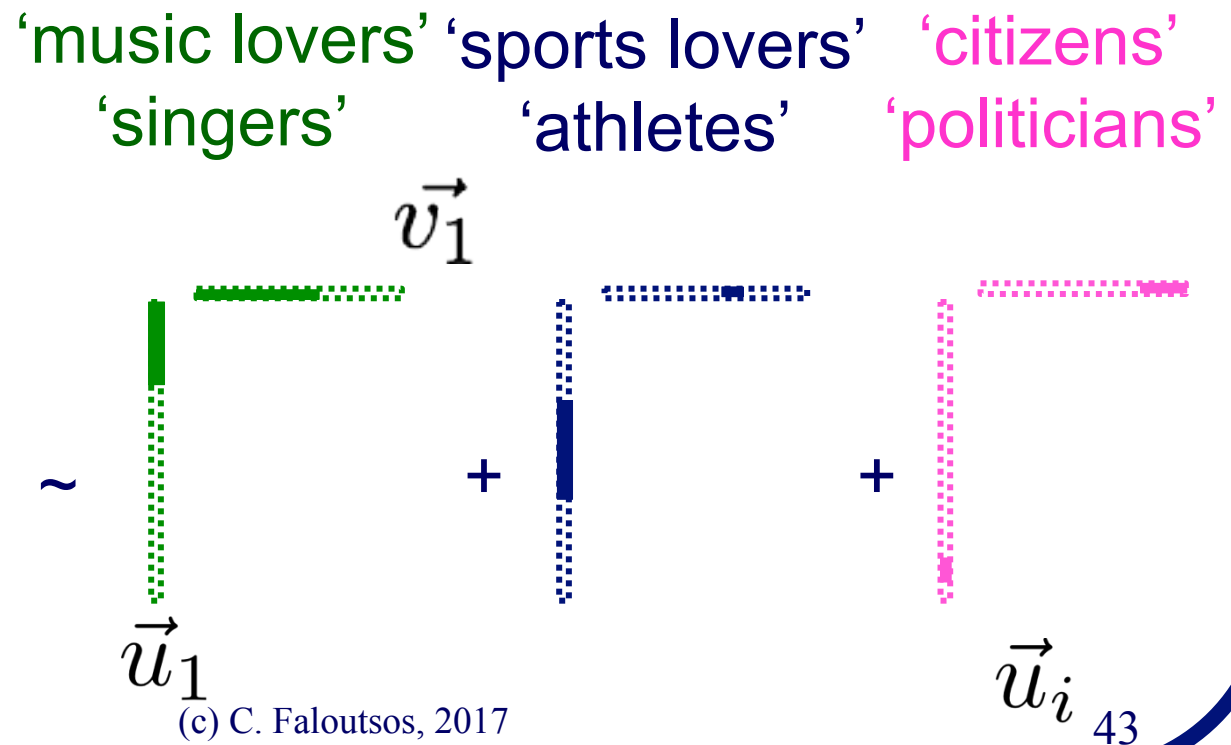


Crush intro to SVD

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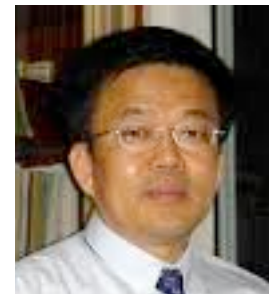


Toutiao/Byte-Dance



Inferring Strange Behavior from Connectivity Pattern in Social Networks

PAKDD'14



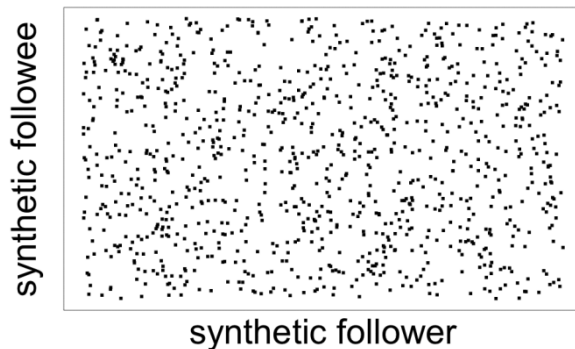
Meng Jiang, Peng Cui, Shiqiang Yang (Tsinghua)
Alex Beutel, Christos Faloutsos (CMU)



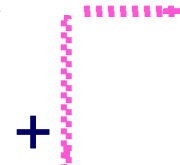
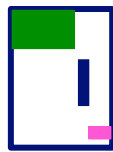
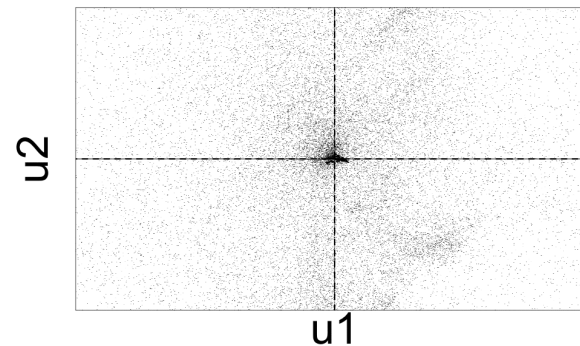
Lockstep and Spectral Subspace Plot

- Case #0: No lockstep behavior in random power law graph of 1M nodes, 3M edges
- Random \longleftrightarrow “Scatter”

Adjacency Matrix



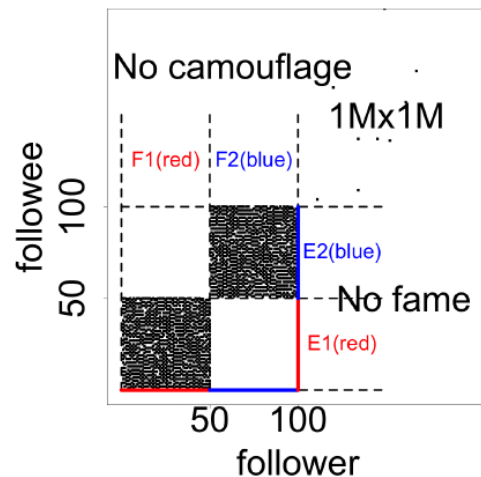
Spectral Subspace Plot



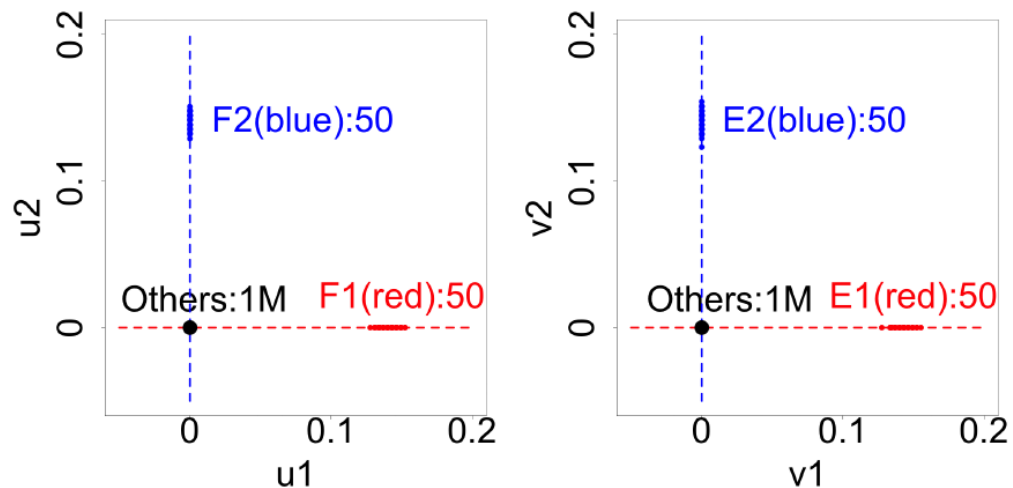
Lockstep and Spectral Subspace Plot

- Case #1: non-overlapping lockstep
- “Blocks” \longleftrightarrow “Rays”

Adjacency Matrix



Spectral Subspace Plot

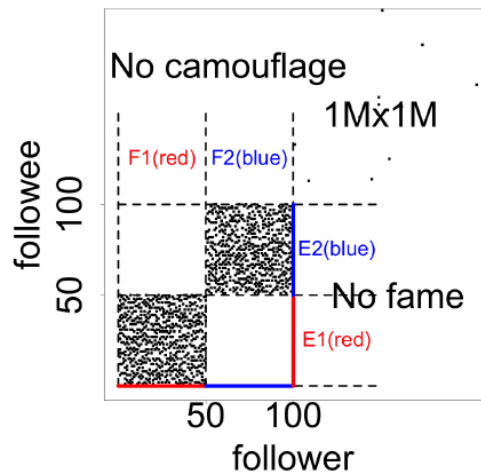


Rule 1 (short “rays”): two blocks, high density (90%), no “camouflage”, no “fame”

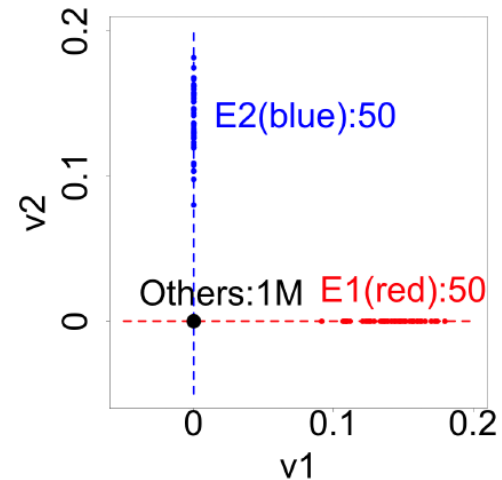
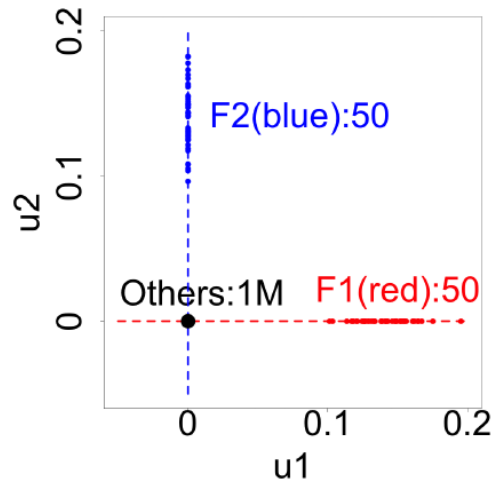
Lockstep and Spectral Subspace Plot

- Case #2: non-overlapping lockstep
- “Blocks; low density” \longleftrightarrow Elongation

Adjacency Matrix



Spectral Subspace Plot



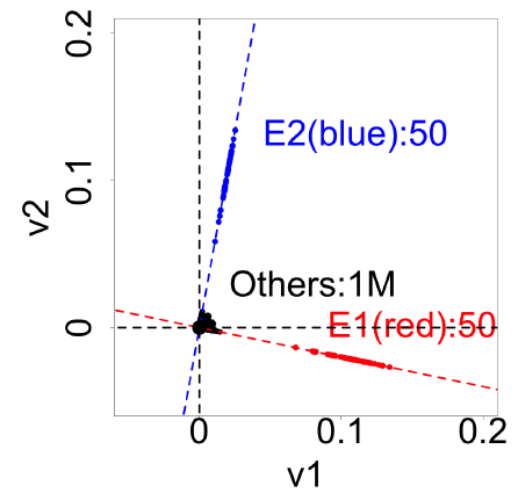
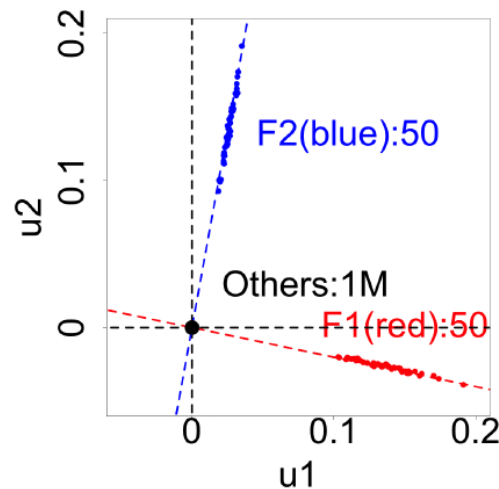
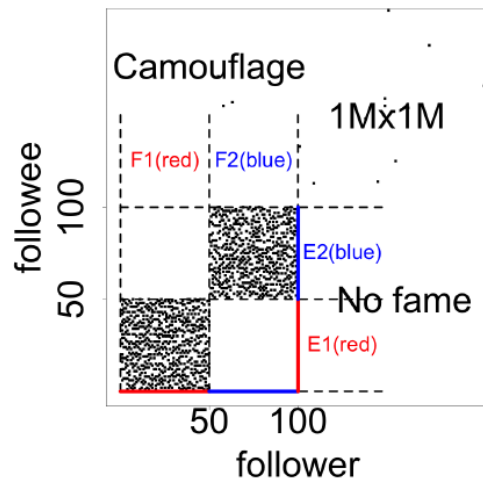
Rule 2 (long “rays”): two blocks, low density (50%), no “camouflage”, no “fame”

Lockstep and Spectral Subspace Plot

- Case #3: non-overlapping lockstep
- “Camouflage” (or “Fame”) \longleftrightarrow Tilting
“Rays”

Adjacency Matrix

Spectral Subspace Plot

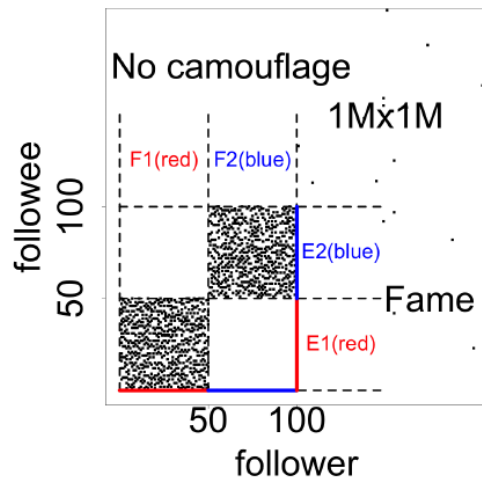


Rule 3 (tilting “rays”): two blocks, with “camouflage”, no “fame”

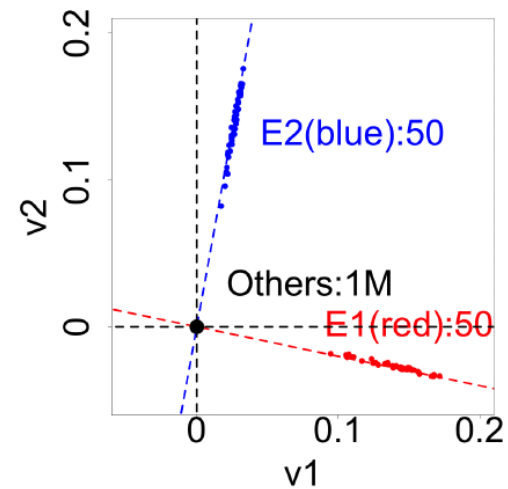
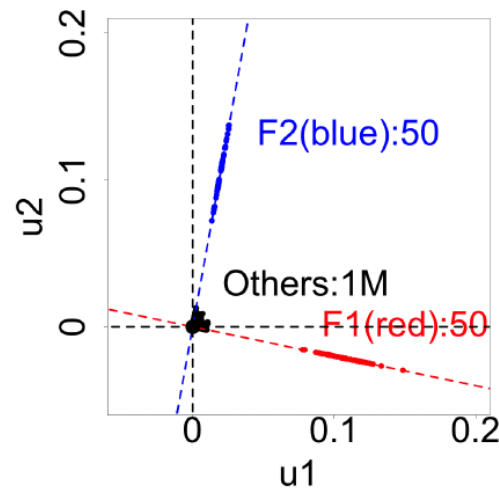
Lockstep and Spectral Subspace Plot

- Case #3: non-overlapping lockstep
- “Camouflage” (or “**Fame**”) \longleftrightarrow Tilting
“Rays”

Adjacency Matrix



Spectral Subspace Plot



Rule 3 (tilting “rays”): two blocks, no “camouflage”, with “fame”

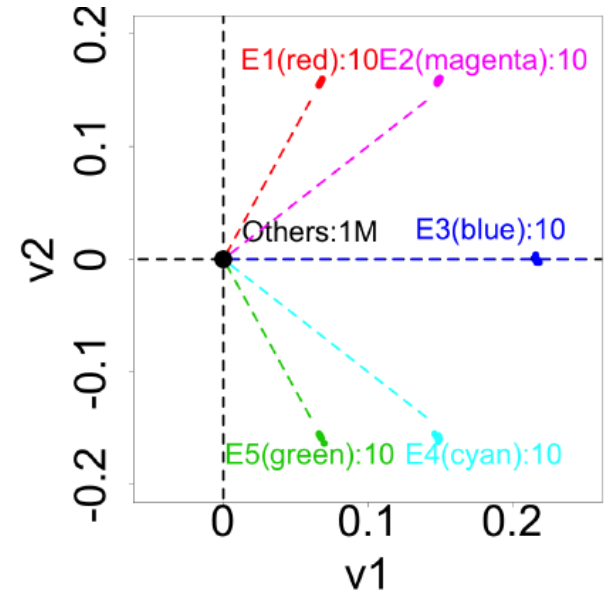
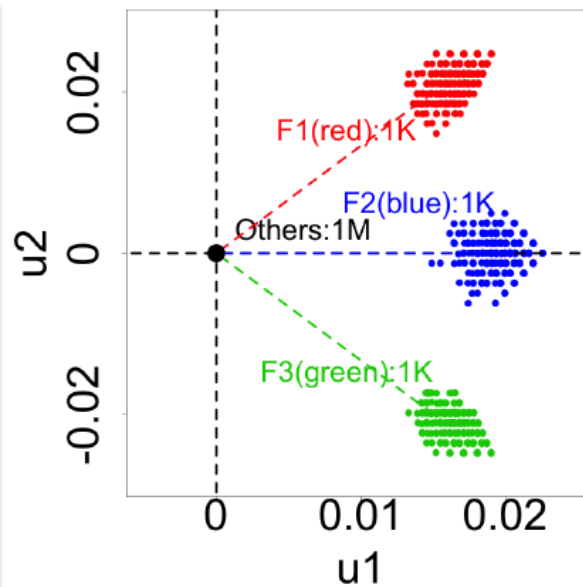
Lockstep and Spectral Subspace Plot

- Case #4: ? lockstep
- “?” \longleftrightarrow “Pearls”

Adjacency Matrix

Spectral Subspace Plot

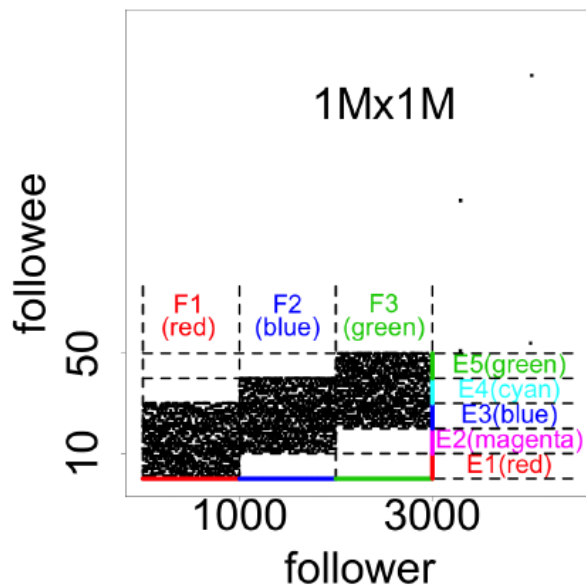
?



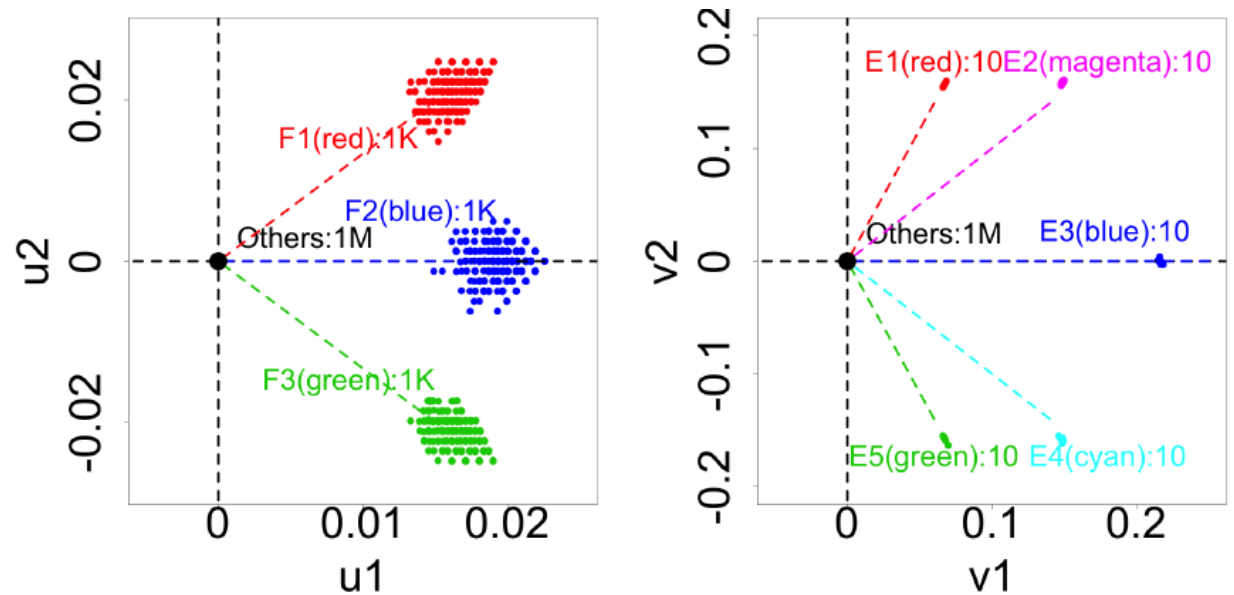
Lockstep and Spectral Subspace Plot

- Case #4: **overlapping lockstep**
- “Staircase” ↔ “Pearls”

Adjacency Matrix




Spectral Subspace Plot



Rule 4 (“pearls”): a “staircase” of three partially overlapping blocks.

Dataset

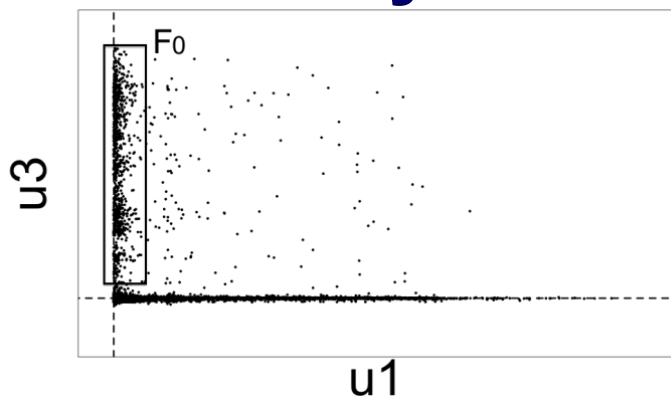
- Tencent Weibo 
- 117 million nodes (with profile and UGC data)
- 3.33 billion directed edges



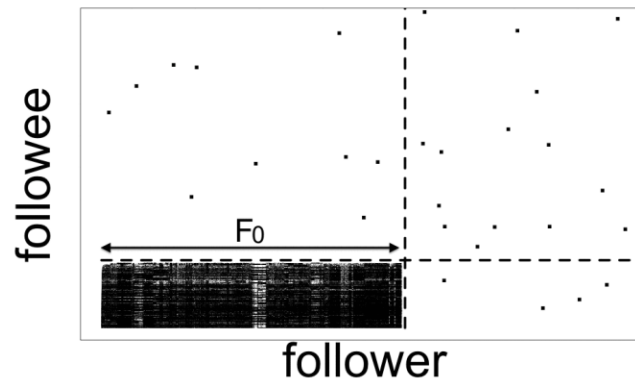
Real Data



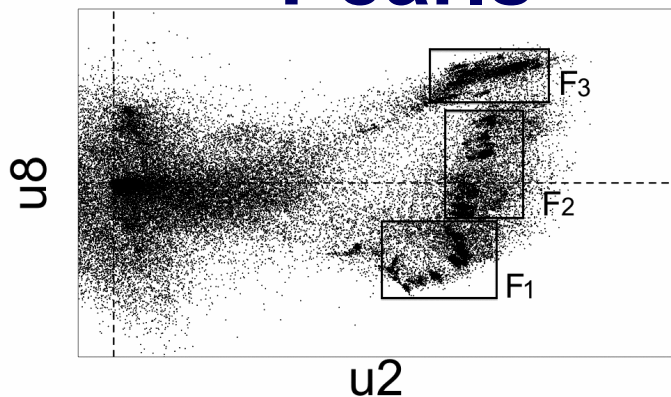
“Rays”



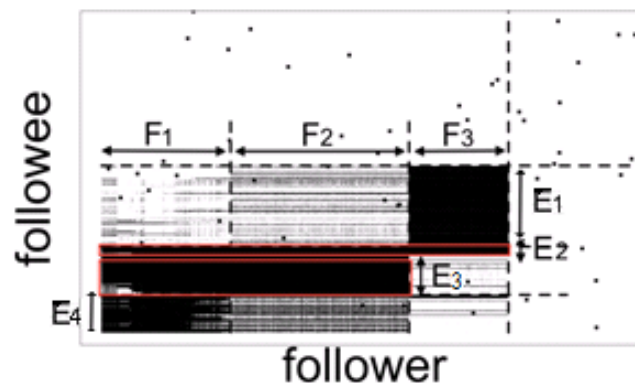
“Block”



“Pearls”

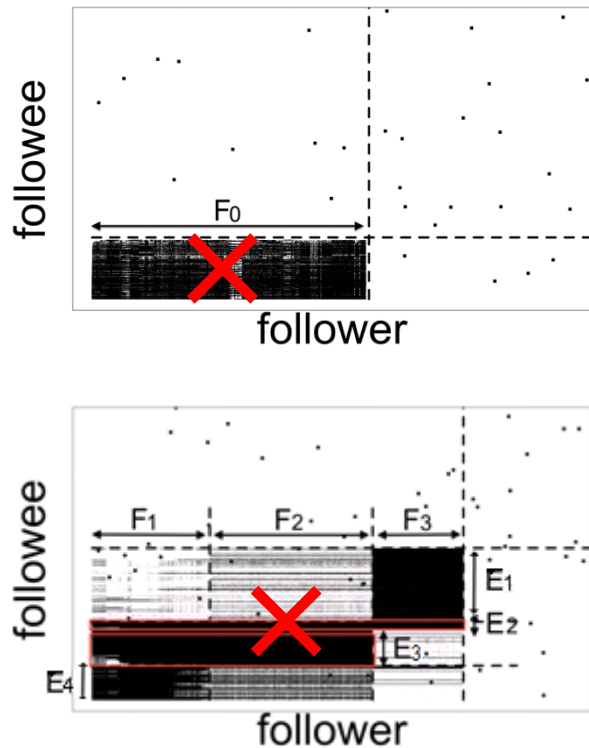


“Staircase”

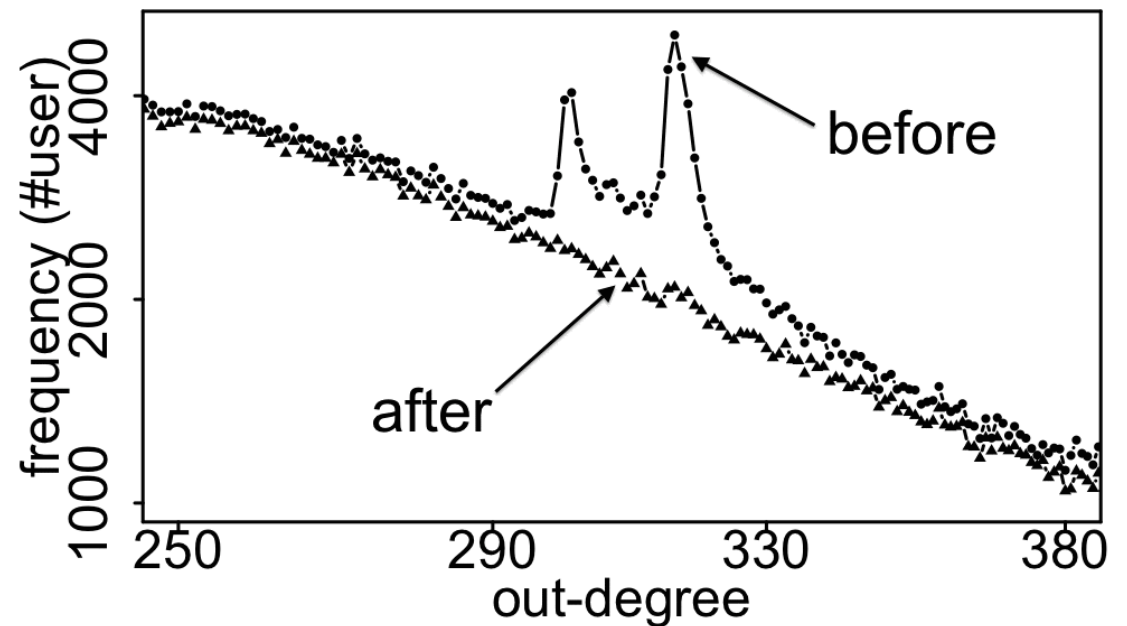


Real Data

- Spikes on the out-degree distribution



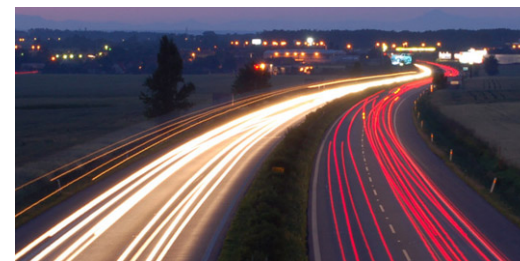
Toutiao/Byte-Dance



(c) C. Faloutsos, 2017

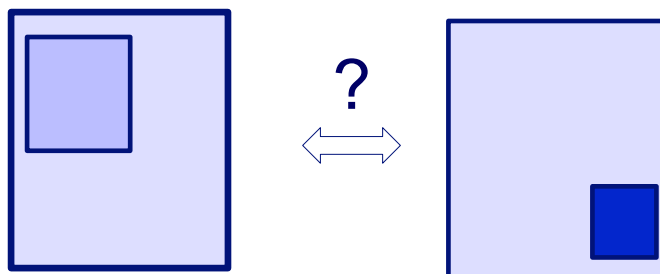
Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
 - P1.1: Patterns
 - P1.2: Anomaly / fraud detection
 - No labels – spectral methods
 - **Suspiciousness**
 - With labels: Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions

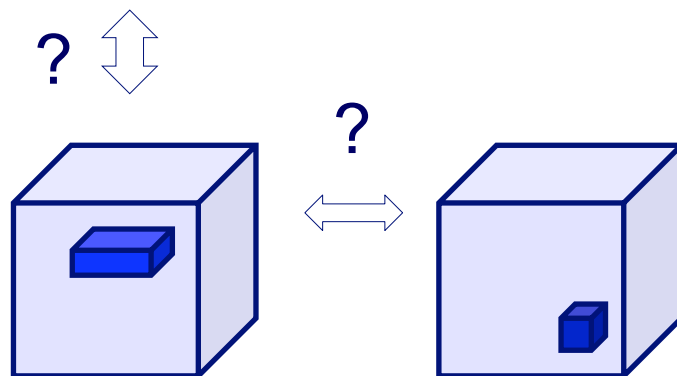


Suspicious Patterns in Event Data

2-modes



n -modes



A General Suspiciousness Metric for Dense Blocks in Multimodal Data, Meng Jiang, Alex Beutel, Peng Cui, Bryan Hooi, Shiqiang Yang, and Christos Faloutsos, *ICDM*, 2015.

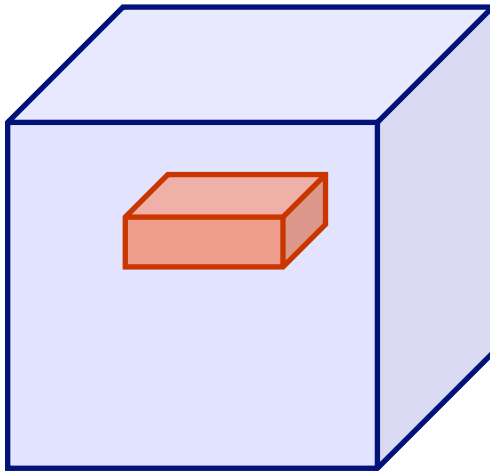
Suspicious Patterns in Event Data

Which is more suspicious?

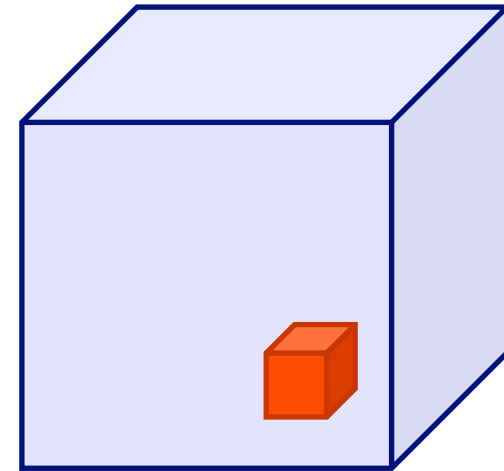
20,000 Users
Retweeting same 20 tweets
6 times each
All in 10 hours

↔
↔
vs.
↔

225 Users
Retweeting same 1 tweet
15 times each
All in 3 hours
All from 2 IP addresses



Toutiao/Byte-Dance



(c) C. Faloutsos, 2017

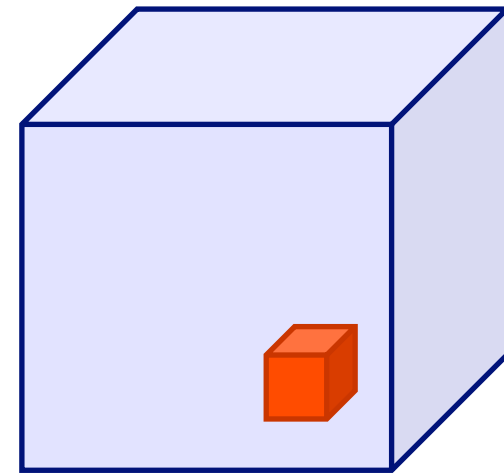
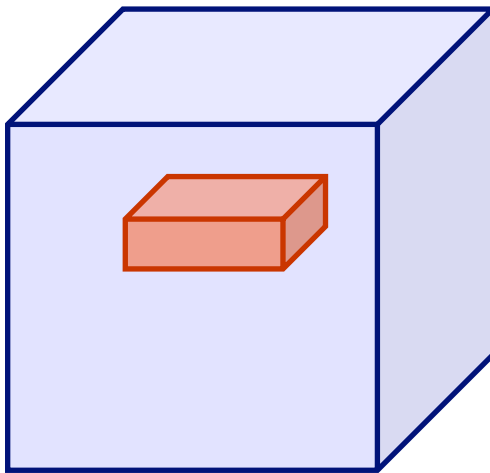
Suspicious Patterns in Event Data

Which is more suspicious?

20,000 Users
Retweeting same 20 tweets
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↔
vs.
↔

225 Users
Retweeting same 1 tweet
15 times each
All in 3 hours
All from 2 IP addresses



Toutiao

Answer: volume * $D_{KL}(p || p_{background})$

58

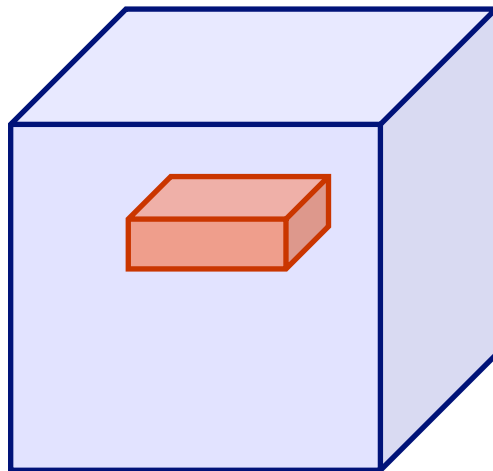
Suspicious Patterns in Event Data

Which is more suspicious?

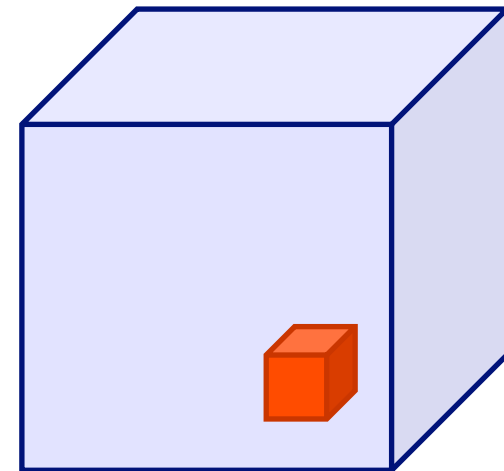
20,000 Users
Retweeting same 20 tweets
6 times each
All in 10 hours

↔
↔
vs.
↔

225 Users
Retweeting same 1 tweet
15 times each
All in 3 hours
All from 2 IP addresses



size



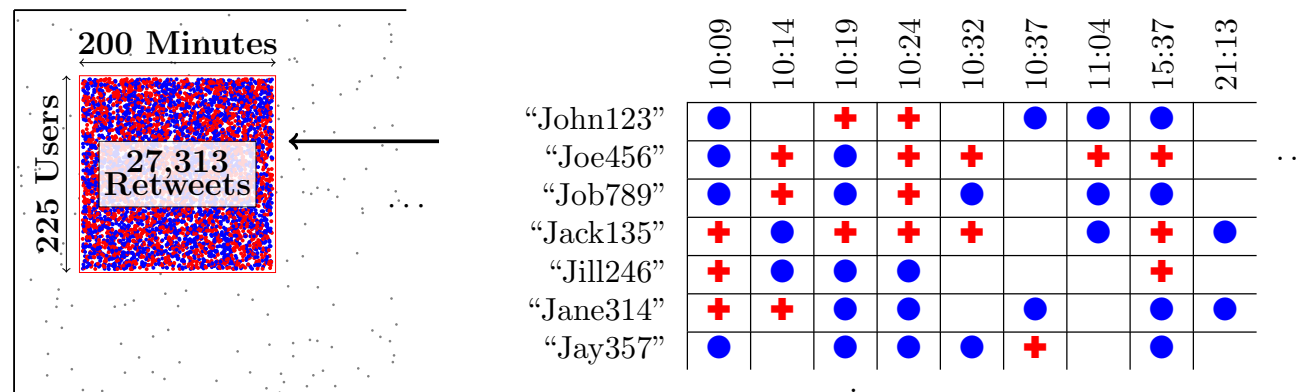
contrast

Toutiao

Answer: volume * $D_{KL}(p || p_{background})$

59

Suspicious Patterns in Event Data

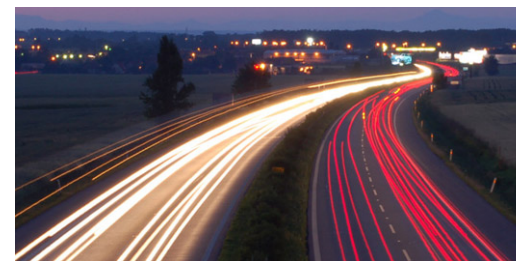


Retweeting: "Galaxy Note Dream Project:
Happy Happy Life Traveling the World"

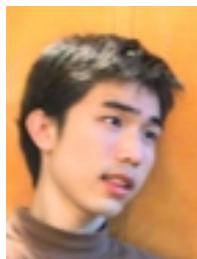
	#	User \times tweet \times IP \times minute	Mass c	Suspiciousness
CROSSPOT	1	$14 \times 1 \times 2 \times 1,114$	41,396	1,239,865
	2	$225 \times 1 \times 2 \times 200$	27,313	777,781
	3	$8 \times 2 \times 4 \times 1,872$	17,701	491,323
HOSVD	1	$24 \times 6 \times 11 \times 439$	3,582	131,113
	2	$18 \times 4 \times 5 \times 223$	1,942	74,087
	3	$14 \times 2 \times 1 \times 265$	9,061	381,211

Roadmap

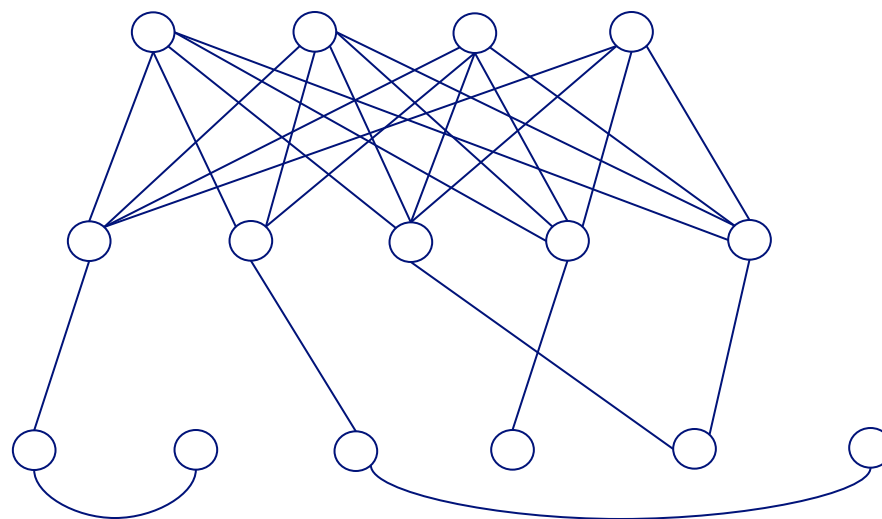
- Introduction – Motivation
- Part#1: Patterns in graphs
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 - No labels – spectral methods
 - With labels: Belief Propagation
- ➔ • Part#2: time-evolving graphs; tensors
- Conclusions



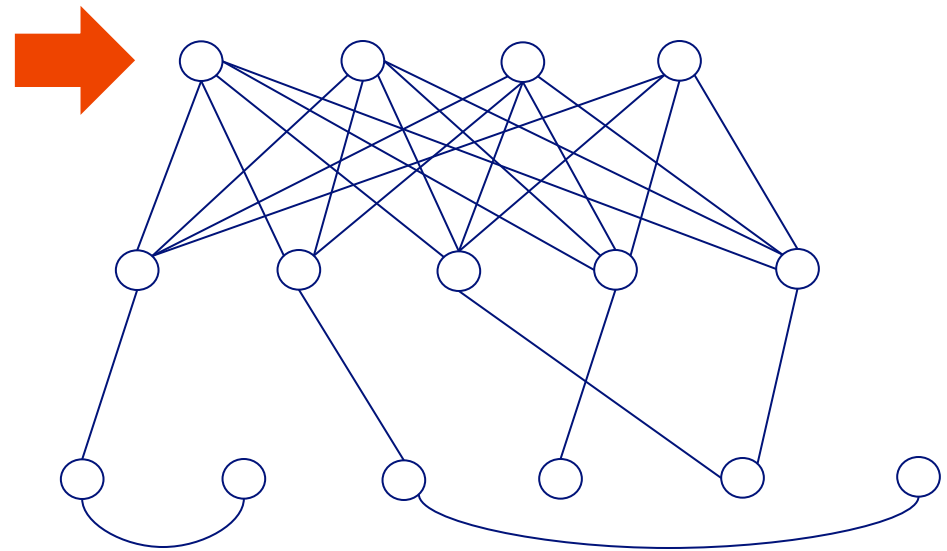
E-bay Fraud detection



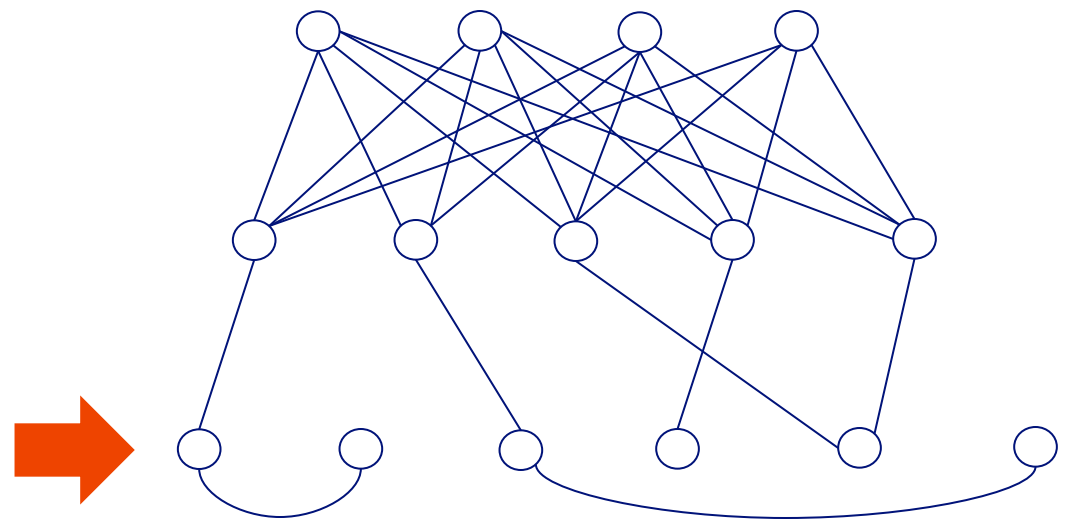
w/ Polo Chau &
Shashank Pandit, CMU
[www'07]



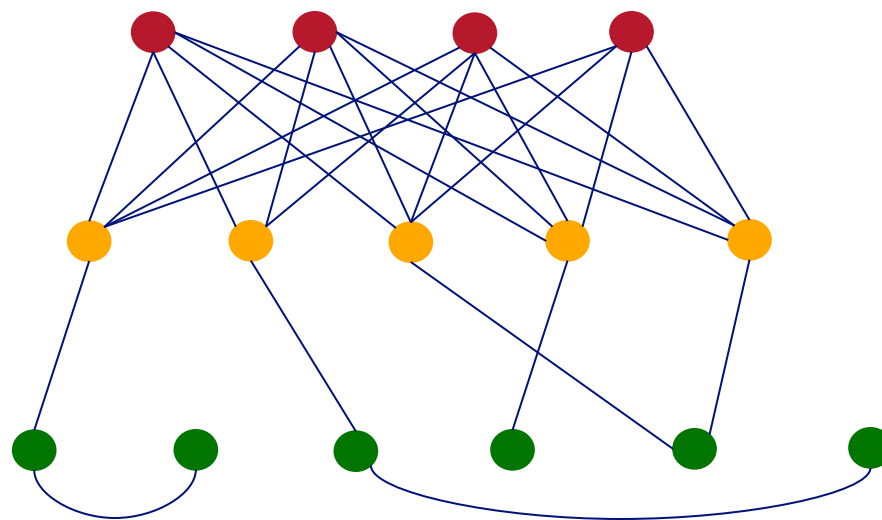
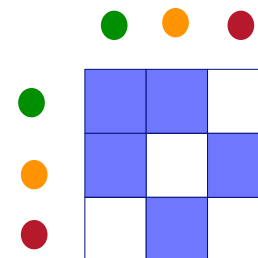
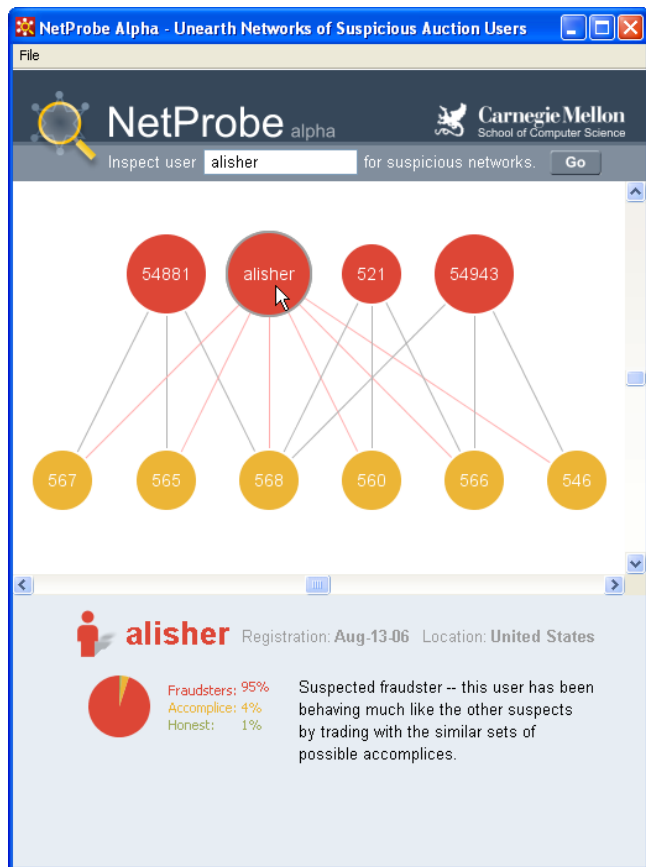
E-bay Fraud detection



E-bay Fraud detection



E-bay Fraud detection - NetProbe



Popular press



The Washington Post

Los Angeles Times

And less desirable attention:

- E-mail from ‘Belgium police’ (‘copy of your code?’)

Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
 - Patterns
 - Anomaly / fraud detection
 - No labels - Spectral methods
 - w/ labels: Belief Propagation – closed formulas
- Part#2: time-evolving graphs; tensors
- Conclusions



Unifying Guilt-by-Association Approaches: Theorems and Fast Algorithms

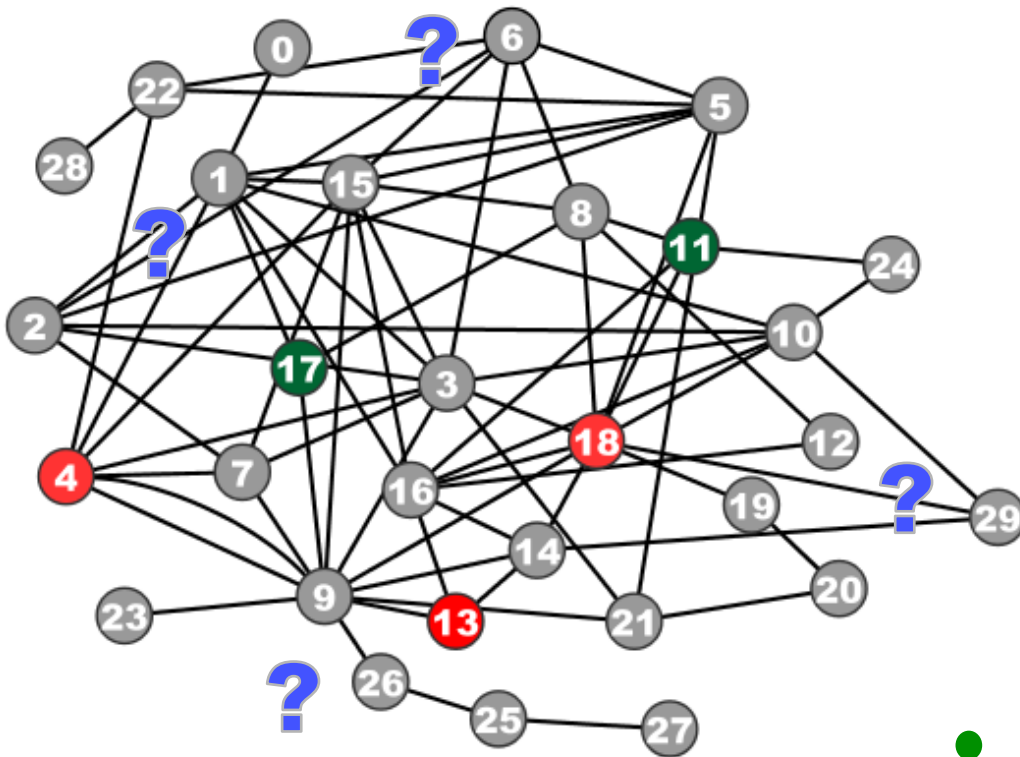


Danai Koutra
U Kang
Hsing-Kuo Kenneth Pao

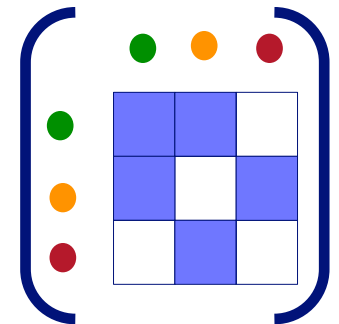
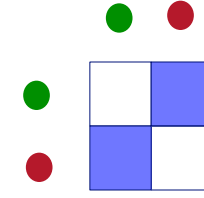
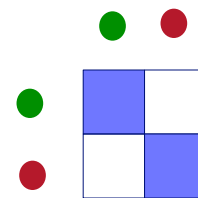
Tai-You Ke
Duen Horng (Polo) Chau
Christos Faloutsos

ECML PKDD, 5-9 September 2011, Athens, Greece

Problem Definition: GBA techniques



Given: Graph; &
few labeled nodes
Find: labels of rest
(assuming network effects)



Are they related?

- RWR (Random Walk with Restarts)
 - google's pageRank (*'if my friends are important, I'm important, too'*)
- SSL (Semi-supervised learning)
 - minimize the differences among neighbors
- BP (Belief propagation)
 - send messages to neighbors, on what you believe about them



Are they related?

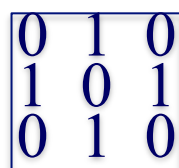
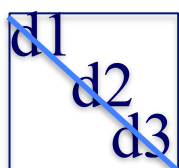
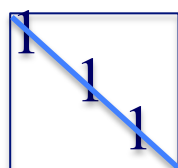
YES!

- RWR (Random Walk with Restarts)
 - google's pageRank (*'if my friends are important, I'm important, too'*)
- SSL (Semi-supervised learning)
 - minimize the differences among neighbors
- BP (Belief propagation)
 - send messages to neighbors, on what you believe about them



Correspondence of Methods

Method	Matrix		Unknown	=	known
RWR	$[\mathbf{I} - c \underline{\mathbf{A}}\mathbf{D}^{-1}]$	\times	\mathbf{x}	=	$(1-c)\mathbf{y}$
SSL	$[\mathbf{I} + a(\mathbf{D} - \underline{\mathbf{A}})]$	\times	\mathbf{x}	=	\mathbf{y}
FABP	$[\mathbf{I} + a \mathbf{D} - c' \underline{\mathbf{A}}]$	\times	\mathbf{b}_h	=	ϕ_h



adjacency
matrix

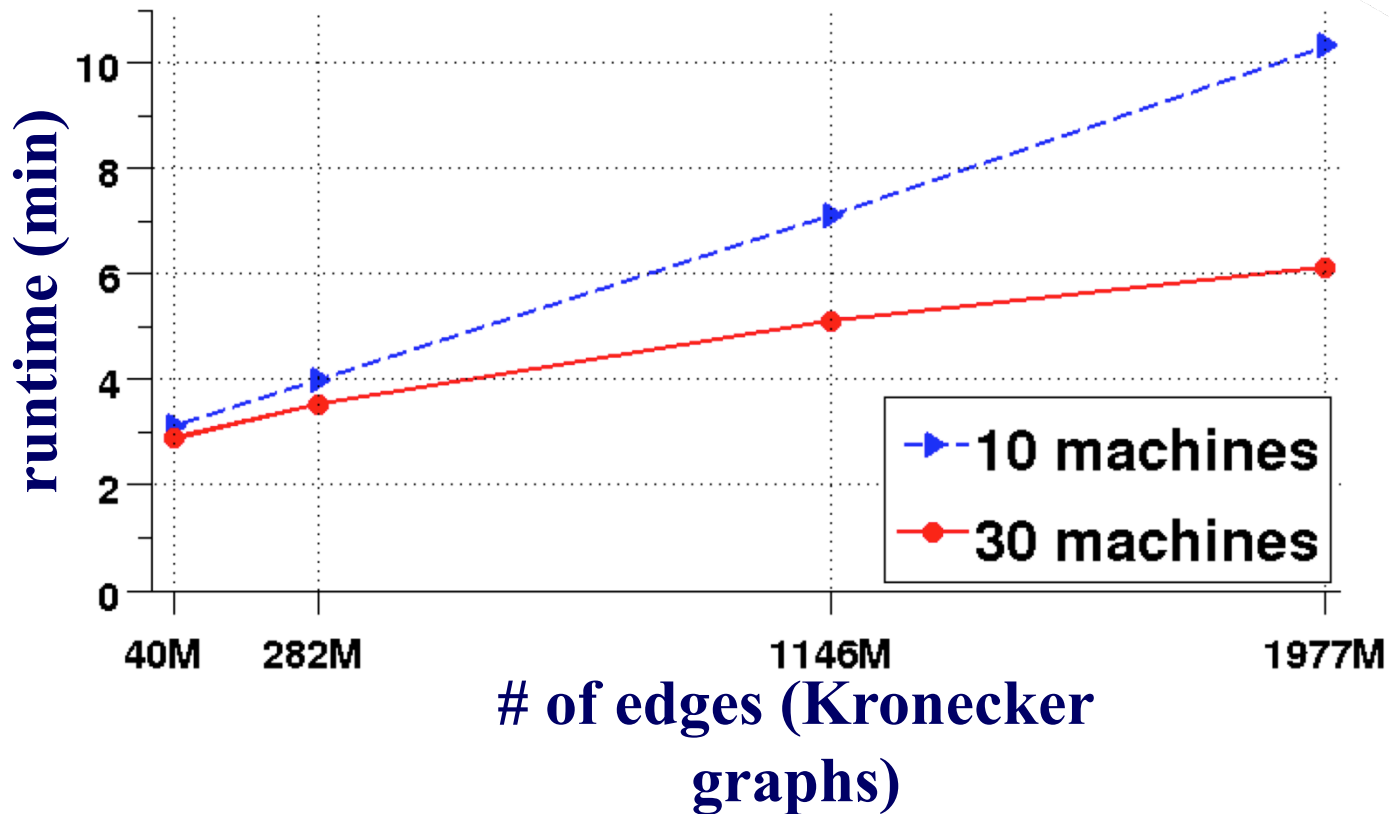
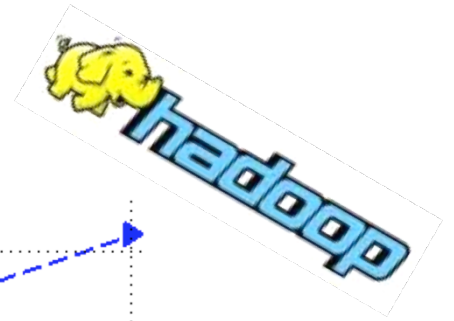


final
labels/
beliefs



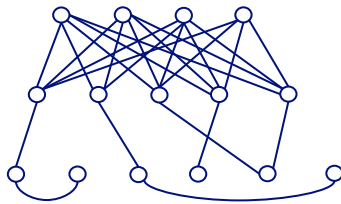
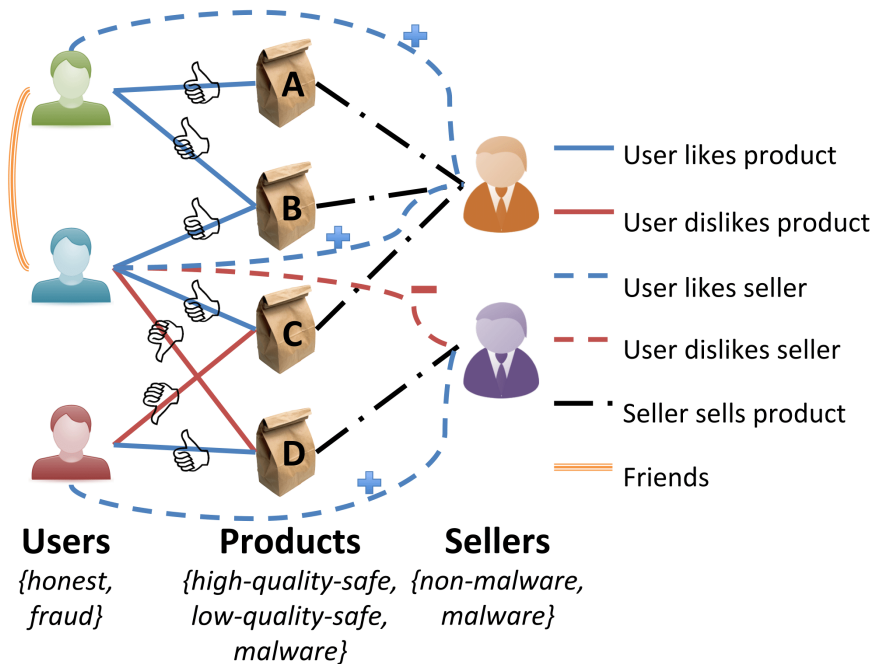
prior
labels/
beliefs

Results: Scalability



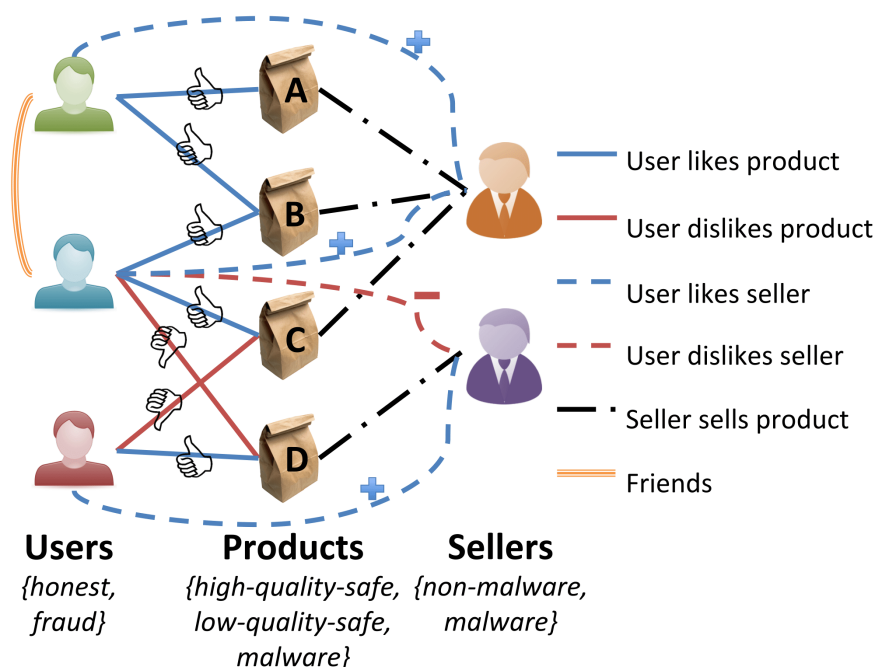
FABP is **linear** on the number of edges.

Problem: e-commerce ratings fraud



- **Given a heterogeneous graph on users, products, sellers and positive/negative ratings with “seed labels”**
- **Find the top k most fraudulent users, products and sellers**

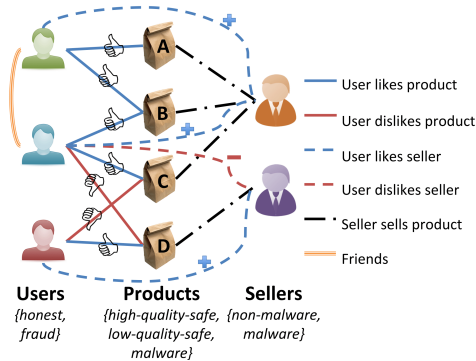
Problem: e-commerce ratings fraud



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Dhivya Eswaran, Stephan Günnemann, Christos Faloutsos,
 “ZooBP: Belief Propagation for Heterogeneous Networks”, In
 submission to VLDB 2017

Problem: e-commerce ratings fraud



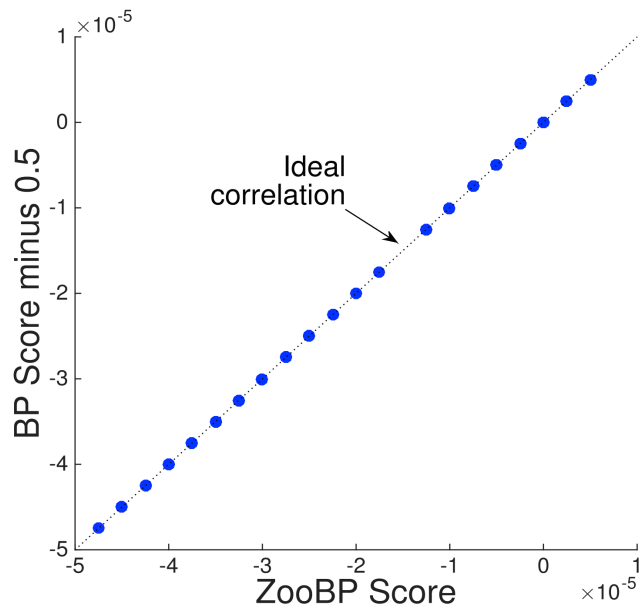
Theorem 1 (ZooBP). *If $\mathbf{b}, \mathbf{e}, \mathbf{P}, \mathbf{Q}$ are constructed as described above, the linear equation system approximating the final node beliefs given by BP is:*

$$\mathbf{b} = \mathbf{e} + (\mathbf{P} - \mathbf{Q})\mathbf{b} \quad (\text{ZooBP}) \quad (10)$$

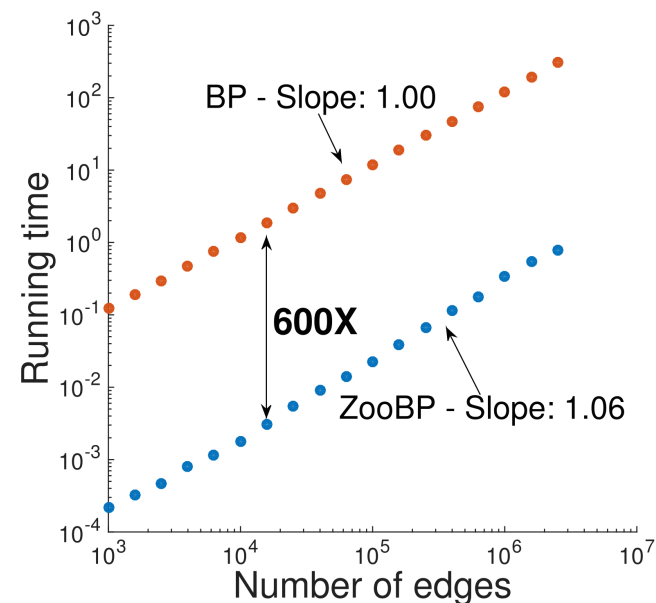
Dhivya Eswaran, Stephan Günnemann, Christos Faloutsos, “ZooBP: Belief Propagation for Heterogeneous Networks”, In submission to VLDB 2017

ZooBP: features

Fast; convergence guarantees.



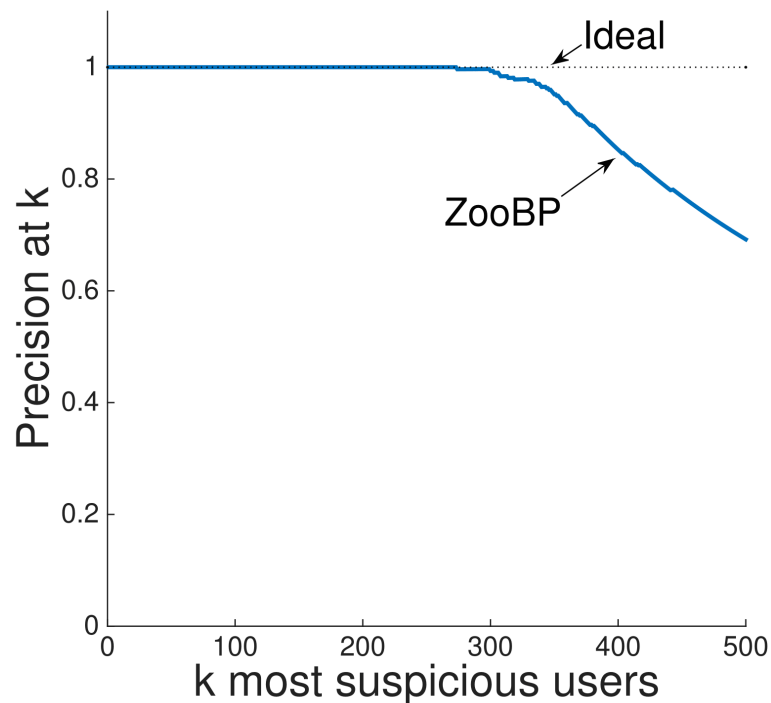
Near-perfect accuracy



linear in graph size

Dhivya Eswaran, Stephan Günnemann, Christos Faloutsos,
“ZooBP: Belief Propagation for Heterogeneous Networks”, In
submission to VLDB 2017

ZooBP in the real world

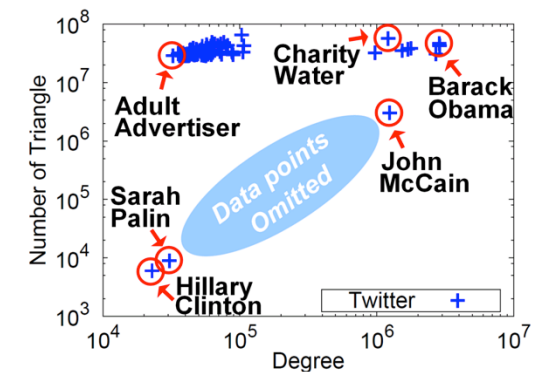


- Near 100% precision on top 300 users (Flipkart)
- Flagged users: suspicious
 - 400 ratings in 1 sec
 - 5000 good ratings and no bad ratings

Dhivya Eswaran, Stephan Günnemann, Christos Faloutsos, “ZooBP: Belief Propagation for Heterogeneous Networks”, In submission to VLDB 2017

Summary of Part#1

- ***many*** patterns in real graphs
 - Power-laws everywhere
 - Long (and growing) list of tools for anomaly/ fraud detection



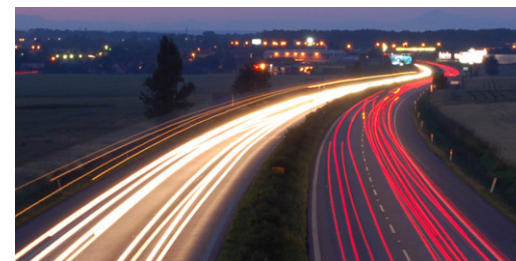
Patterns



anomalies

Roadmap

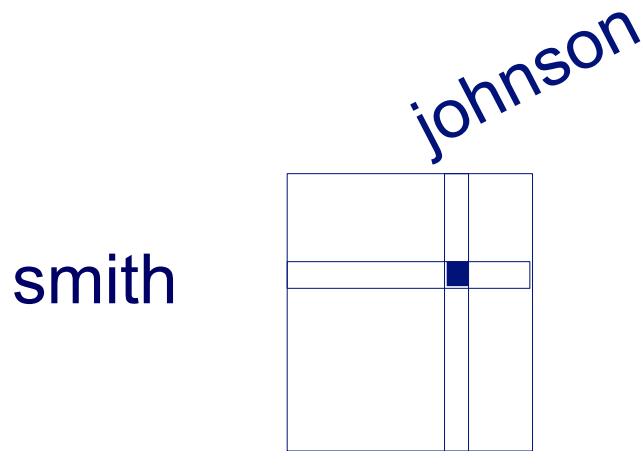
- Introduction – Motivation
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs
 - ➔ – P2.1: tools/tensors
 - P2.2: other patterns
- Conclusions



Part 2: Time evolving graphs; tensors

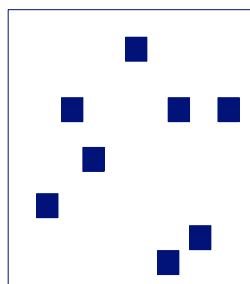
Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



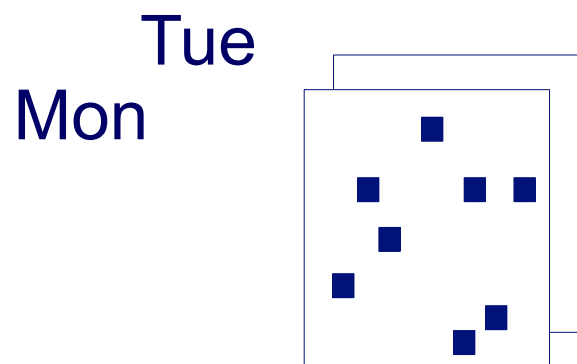
Graphs over time \rightarrow tensors!

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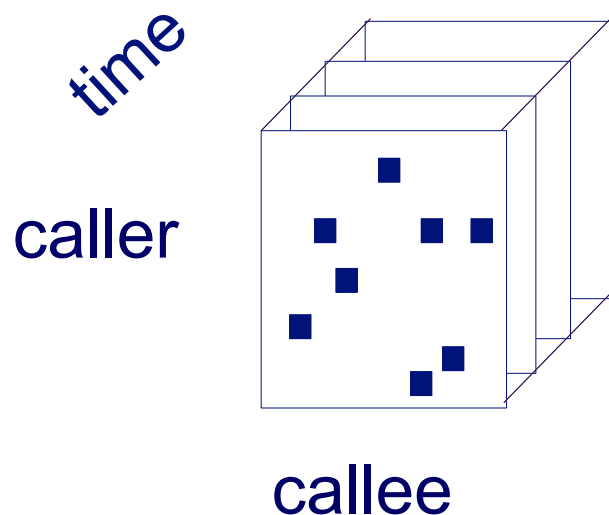
Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



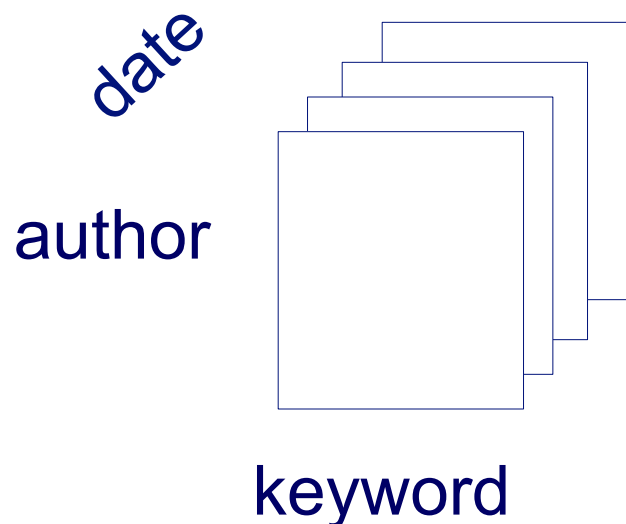
Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



Graphs over time -> tensors!

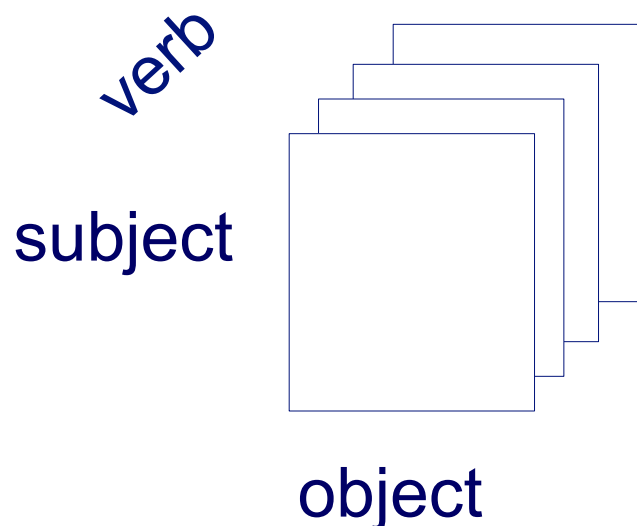
- Problem #2.1':
 - Given author-keyword-date
 - Find patterns / anomalies



MANY more settings,
with >2 'modes'

Graphs over time -> tensors!

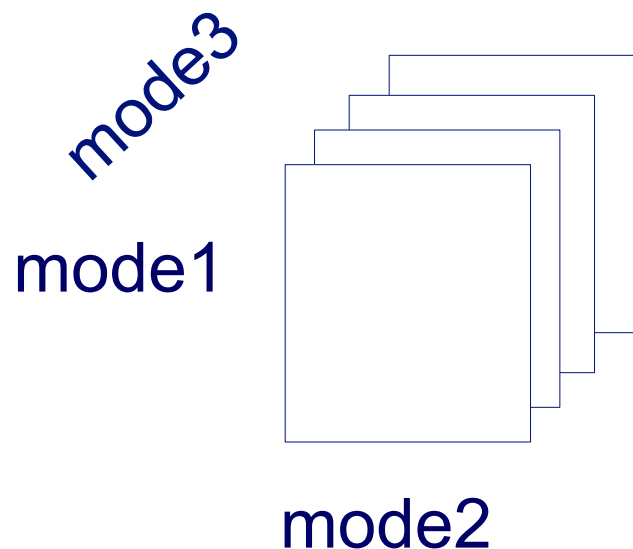
- Problem #2.1’’:
 - Given subject – verb – object facts
 - Find patterns / anomalies



MANY more settings,
with >2 ‘modes’

Graphs over time -> tensors!

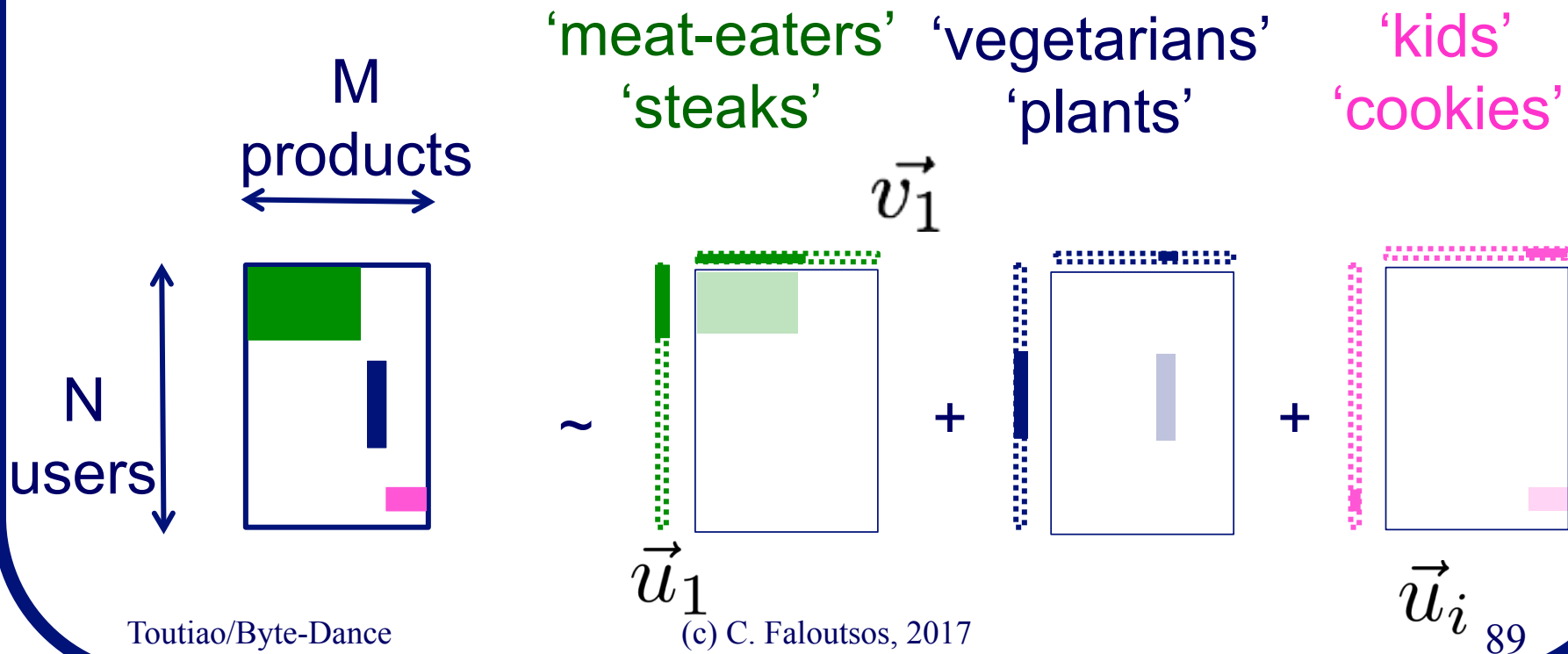
- Problem #2.1''':
 - Given <triplets>
 - Find patterns / anomalies



MANY more settings,
with >2 'modes'
(and 4, 5, etc modes)

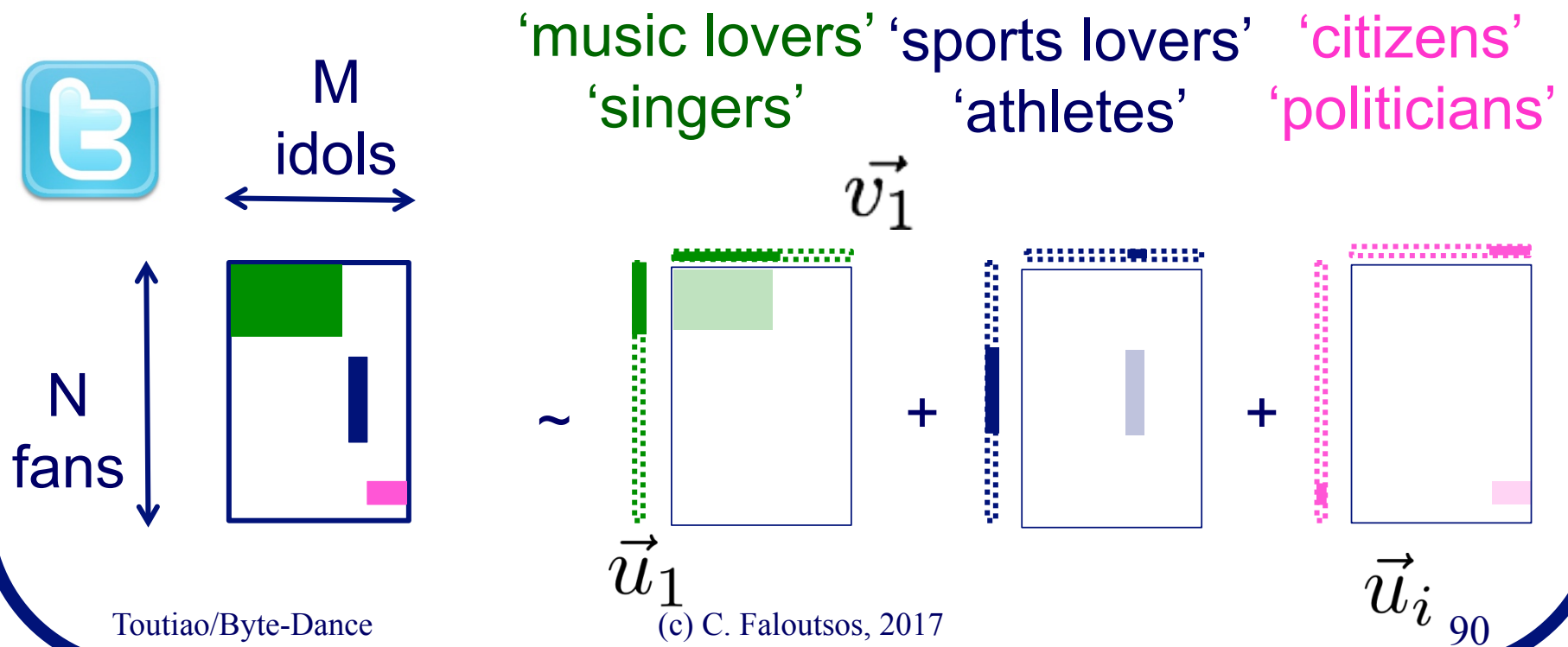
Answer : tensor factorization

- Recall: (SVD) matrix factorization: finds blocks



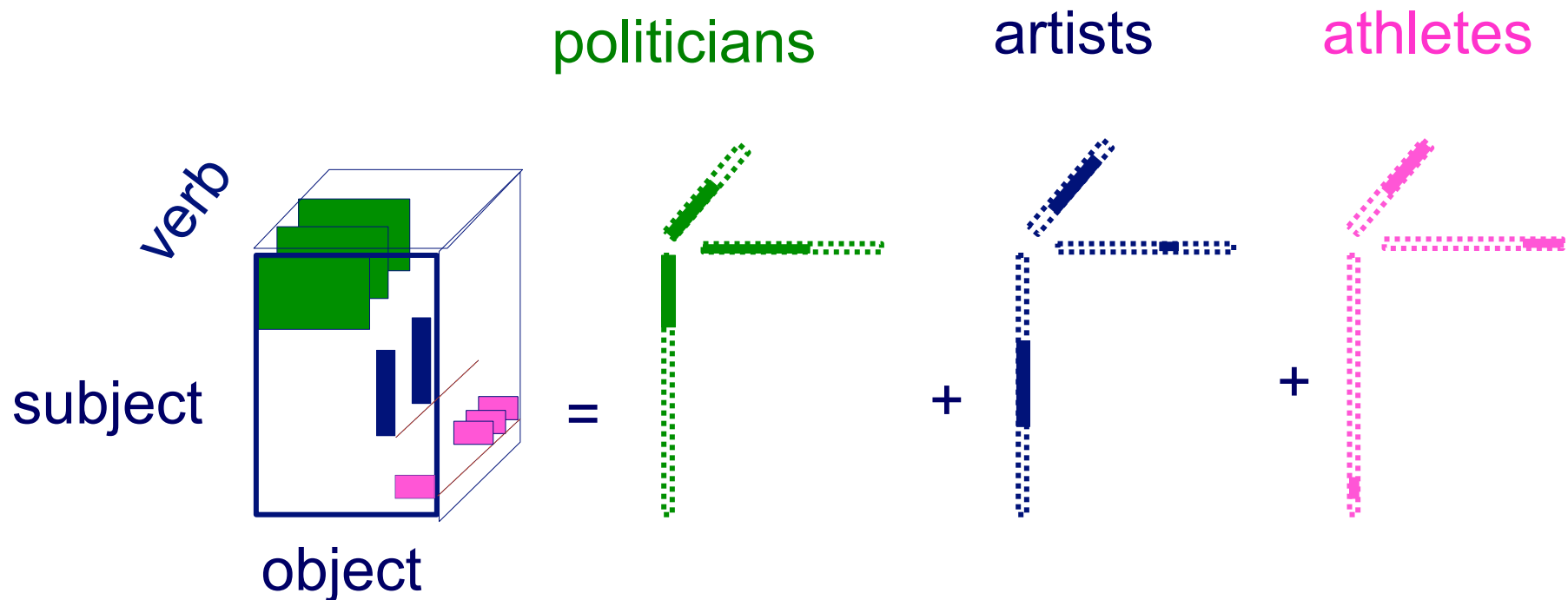
Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks



Answer: tensor factorization

- PARAFAC decomposition

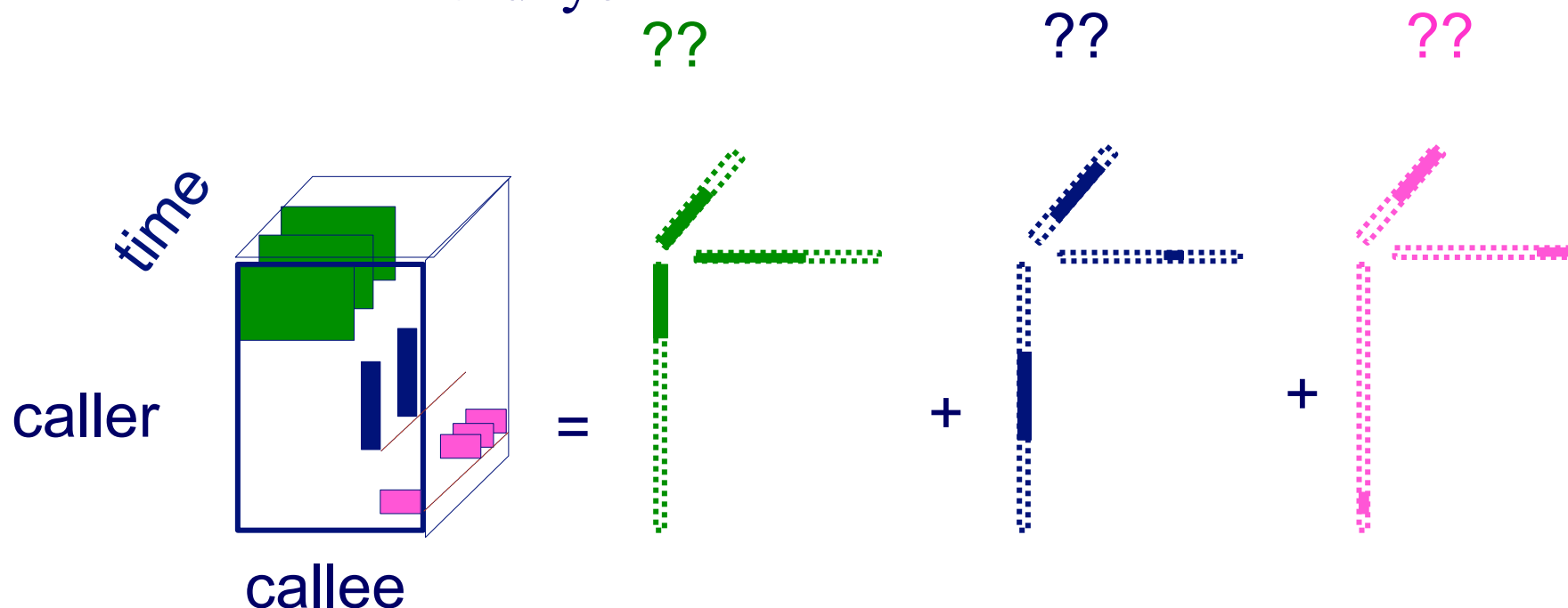


Toutiao/Byte-Dance

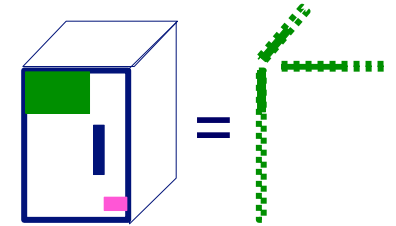
(c) C. Faloutsos, 2017

Answer: tensor factorization

- PARAFAC decomposition
- Results for who-calls-whom-when
 - 4M x 15 days

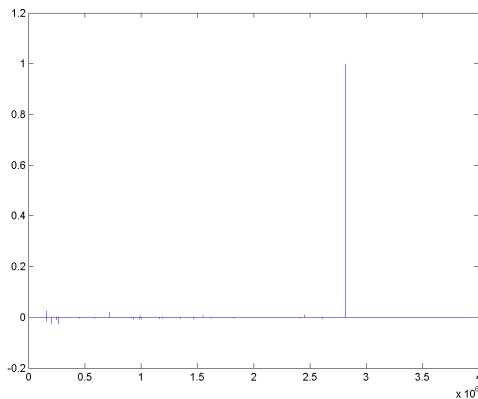


Anomaly detection in time-evolving graphs

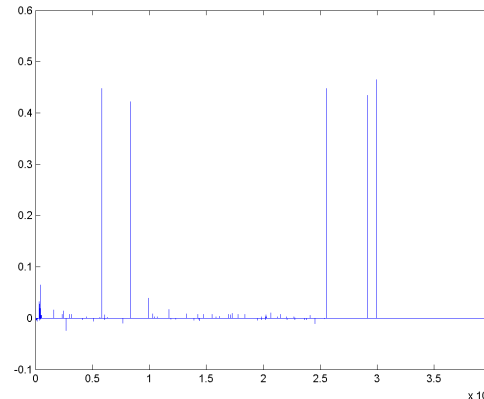


- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks

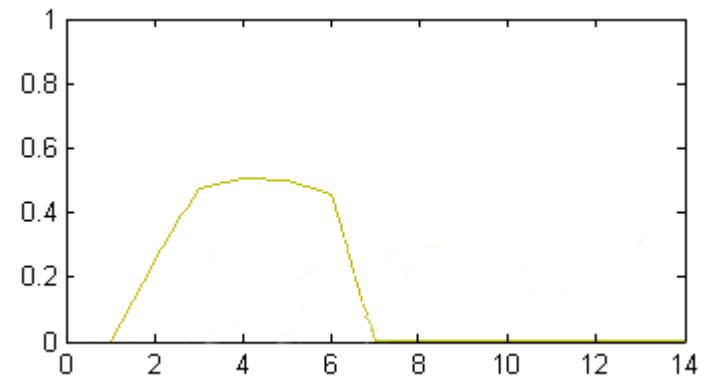
1 caller



5 receivers

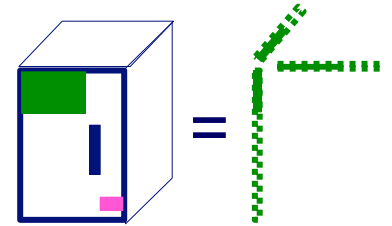


4 days of activity



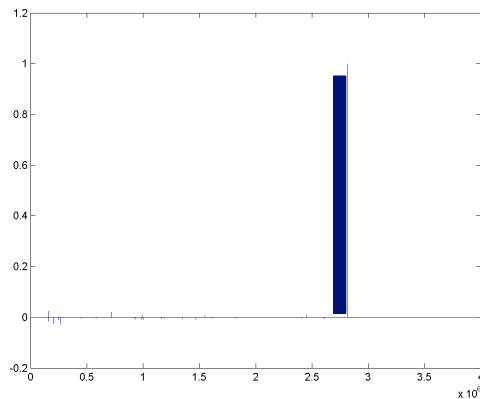
~200 calls to EACH receiver on EACH day!

Anomaly detection in time-evolving graphs

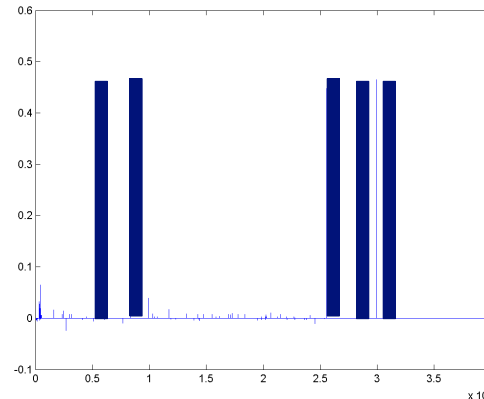


- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks

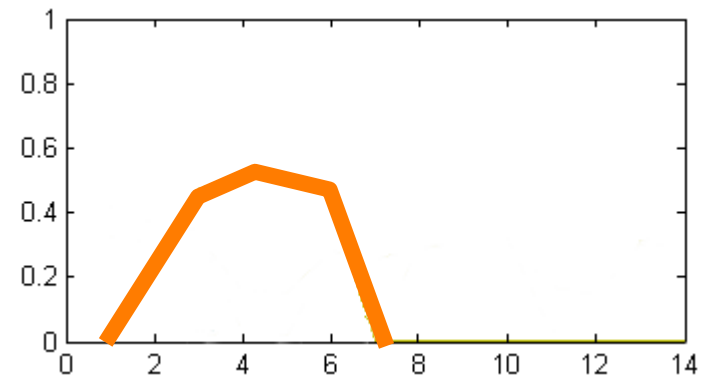
1 caller



5 receivers

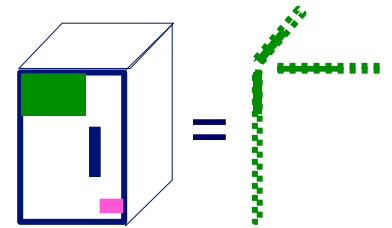


4 days of activity



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Anomaly detection in time-evolving graphs



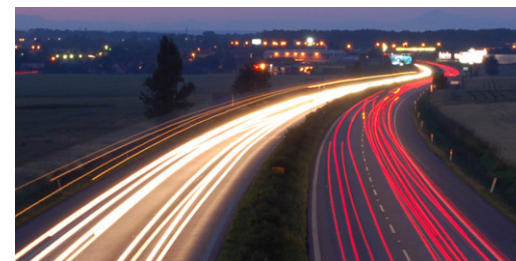
- Anomalous communities in phone call data:
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Miguel Araujo, Spiros Papadimitriou, Stephan Günnemann, Christos Faloutsos, Prithwish Basu, Ananthram Swami, Evangelos Papalexakis, Danai Koutra. *Com2: Fast Automatic Discovery of Temporal (Comet) Communities*. PAKDD 2014, Tainan, Taiwan.

Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs
 - P2.1: tools/tensors
 - ➔ – P2.2: other patterns – inter-arrival time
- Conclusions



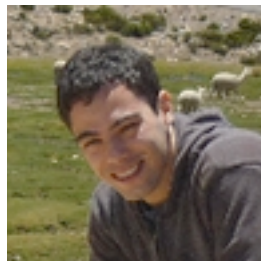
Carnegie Mellon



Carnegie
Mellon
University

KDD 2015 – Sydney,
Australia

RSC: Mining and Modeling Temporal Activity in Social Media



Alceu F. Costa* Yuto Yamaguchi Agma J. M. Traina

Caetano Traina Jr. Christos Faloutsos

*alceufc@icmc.usp.br

Pattern Mining: Datasets

Reddit Dataset

Time-stamp from comments
21,198 users
20 Million time-stamps

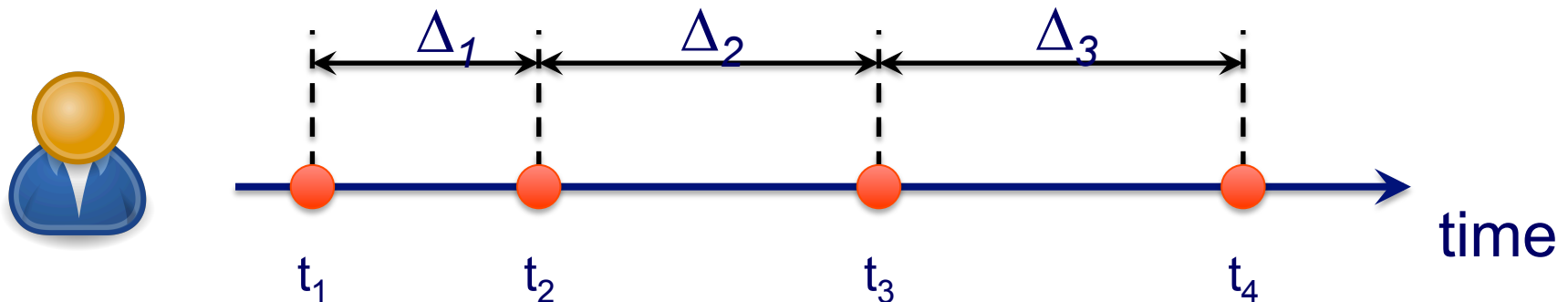
Twitter Dataset

Time-stamp from tweets
6,790 users
16 Million time-stamps

For each user we have:

Sequence of postings time-stamps: $T = (t_1, t_2, t_3, \dots)$

Inter-arrival times (IAT) of postings: $(\Delta_1, \Delta_2, \Delta_3, \dots)$



Toutiao/Byte-Dance

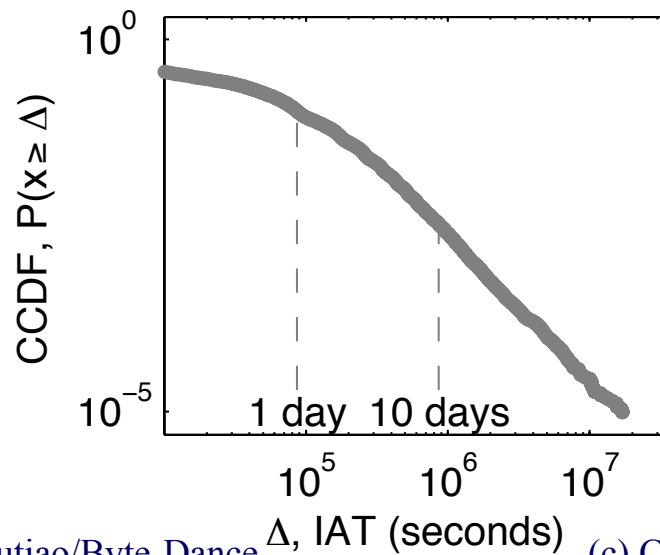
(c) C. Faloutsos, 2017

Pattern Mining

Pattern 1: Distribution of IAT is heavy-tailed

Users can be inactive for long periods of time before making new postings

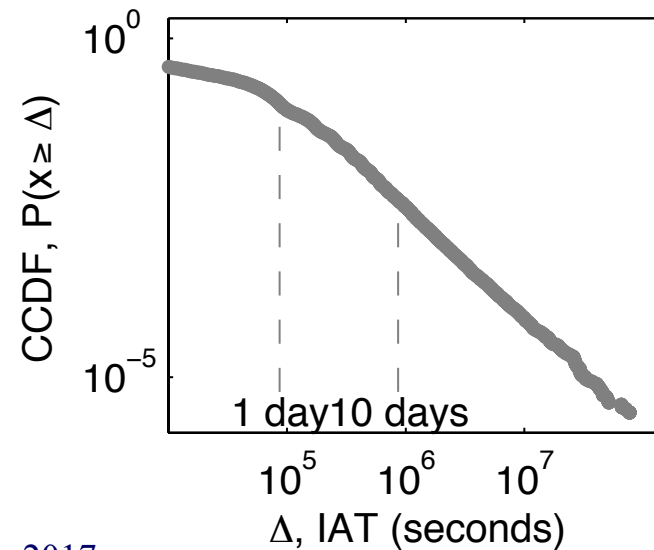
IAT Complementary Cumulative Distribution Function (CCDF)
(log-log axis)



Toutiao/Byte-Dance

Δ , IAT (seconds) (c) C. Faloutsos, 2017

Reddit Users



Twitter Users

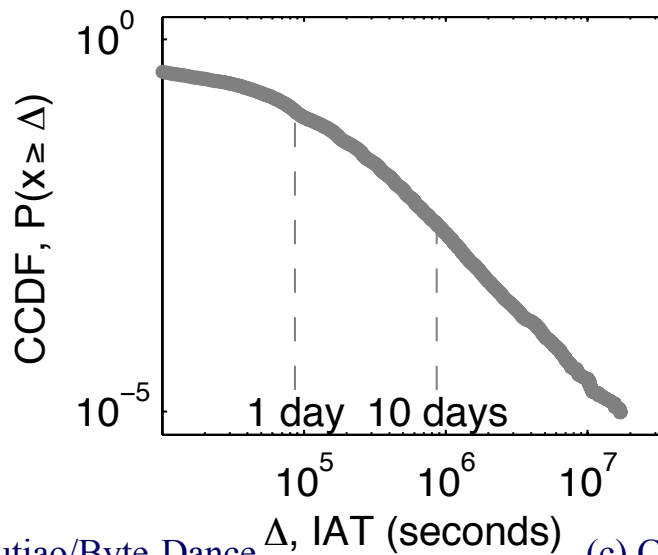
Pattern Mining

Pattern 1: Distribution of IAT is heavy-tailed

Users can be inactive for long periods of time before making new postings

**No surprises –
Should we give up?**

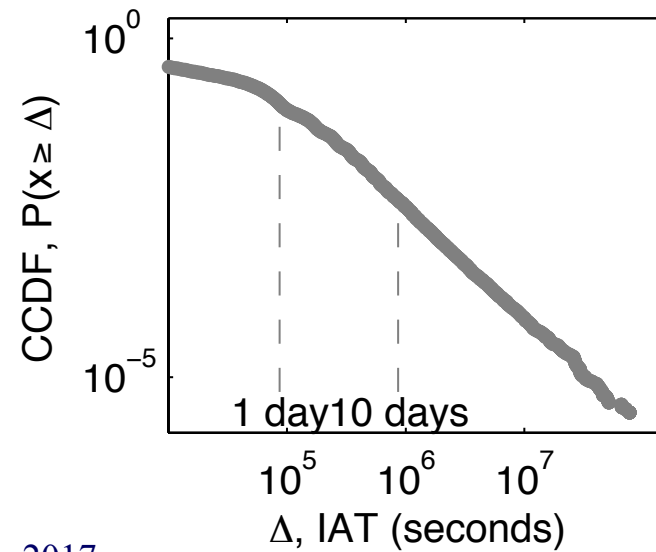
IAT Com... n (CCDF)



Toutiao/Byte-Dance

(c) C. Faloutsos, 2017

Reddit Users

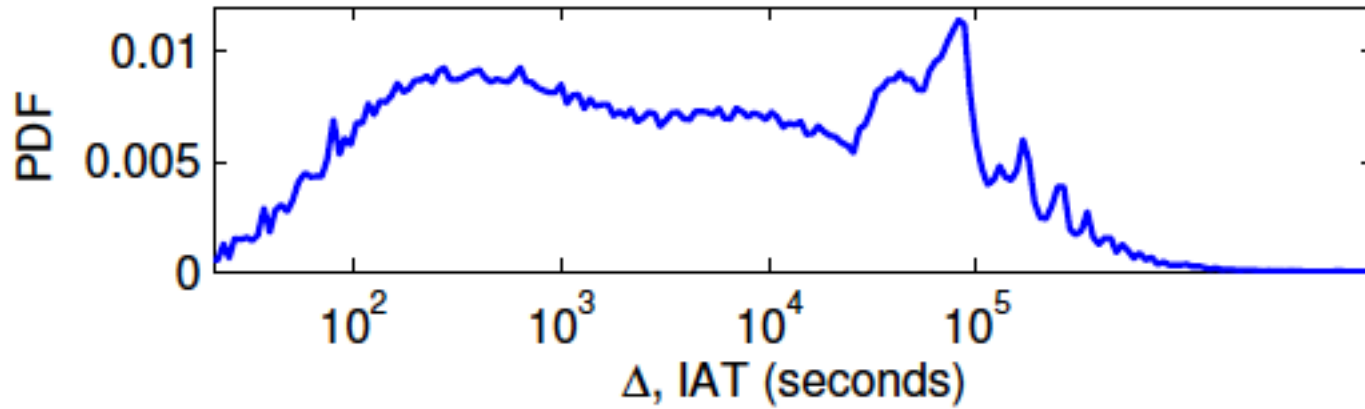


Twitter Users

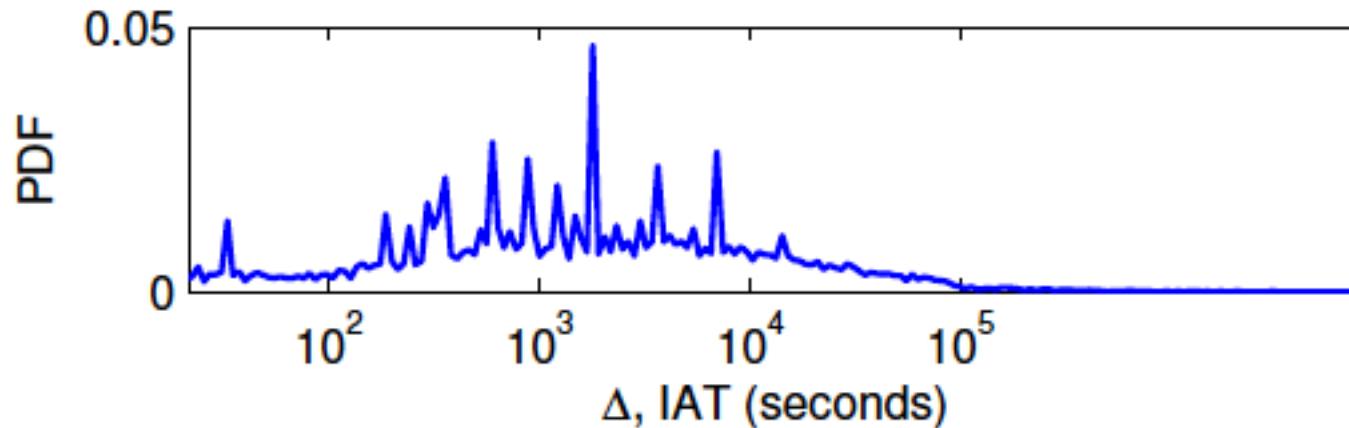


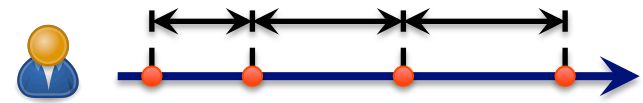
Human? Robots?

linear



log

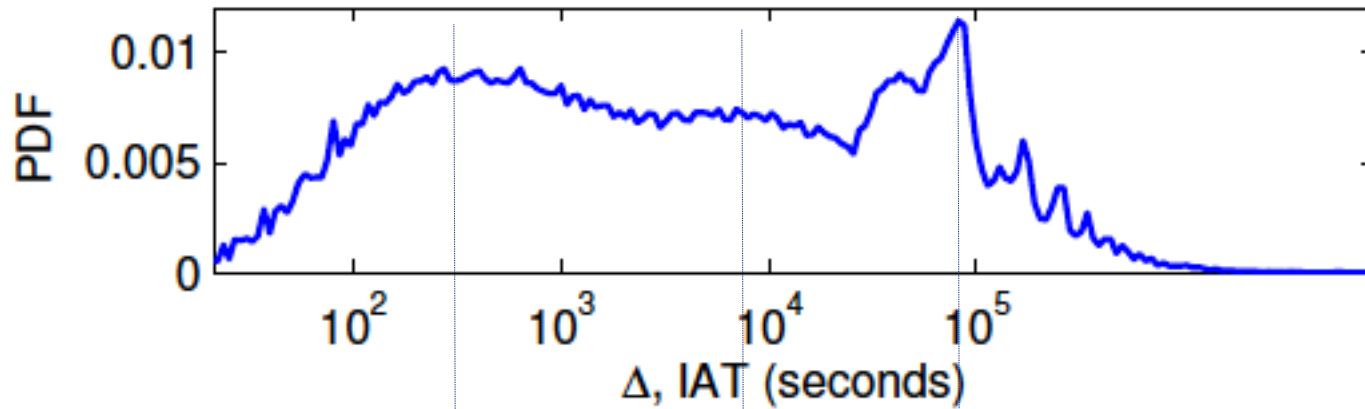




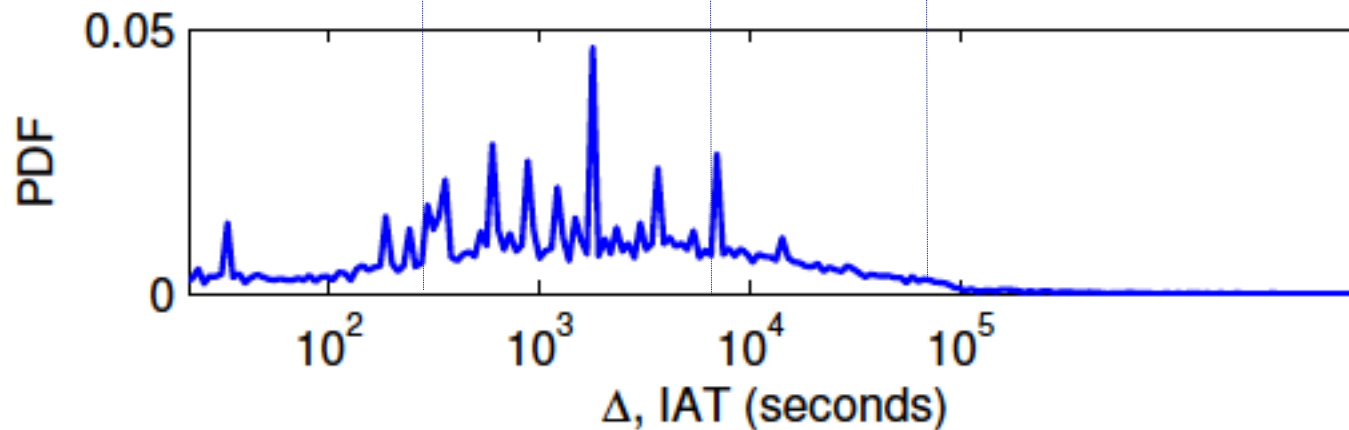
Human? Robots?

2' 3h 1day

linear



log

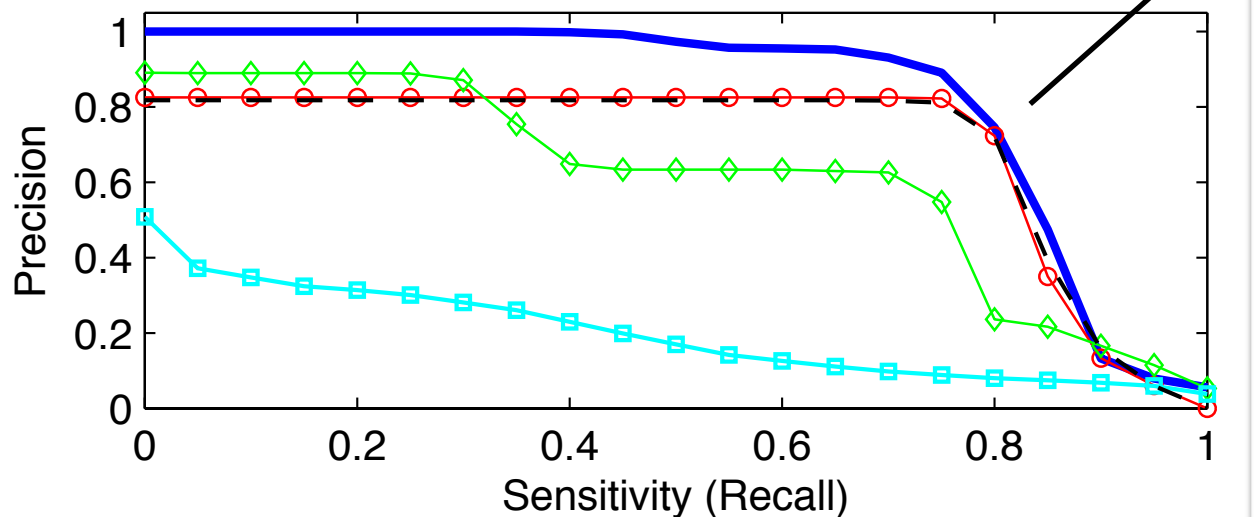


Experiments: Can RSC-Spotter Detect Bots?

Precision vs. Sensitivity Curves

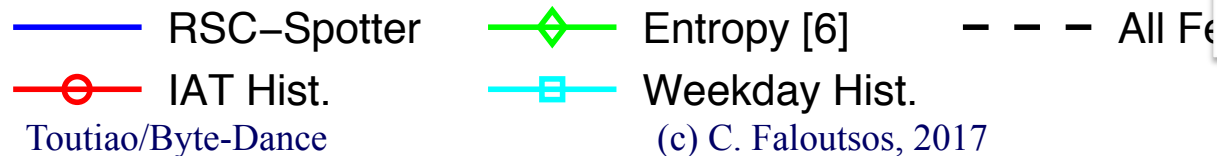
Good performance: curve close to the top

Twitter



Precision > 94%
Sensitivity > 70%

With strongly imbalanced datasets
humans \gg # bots



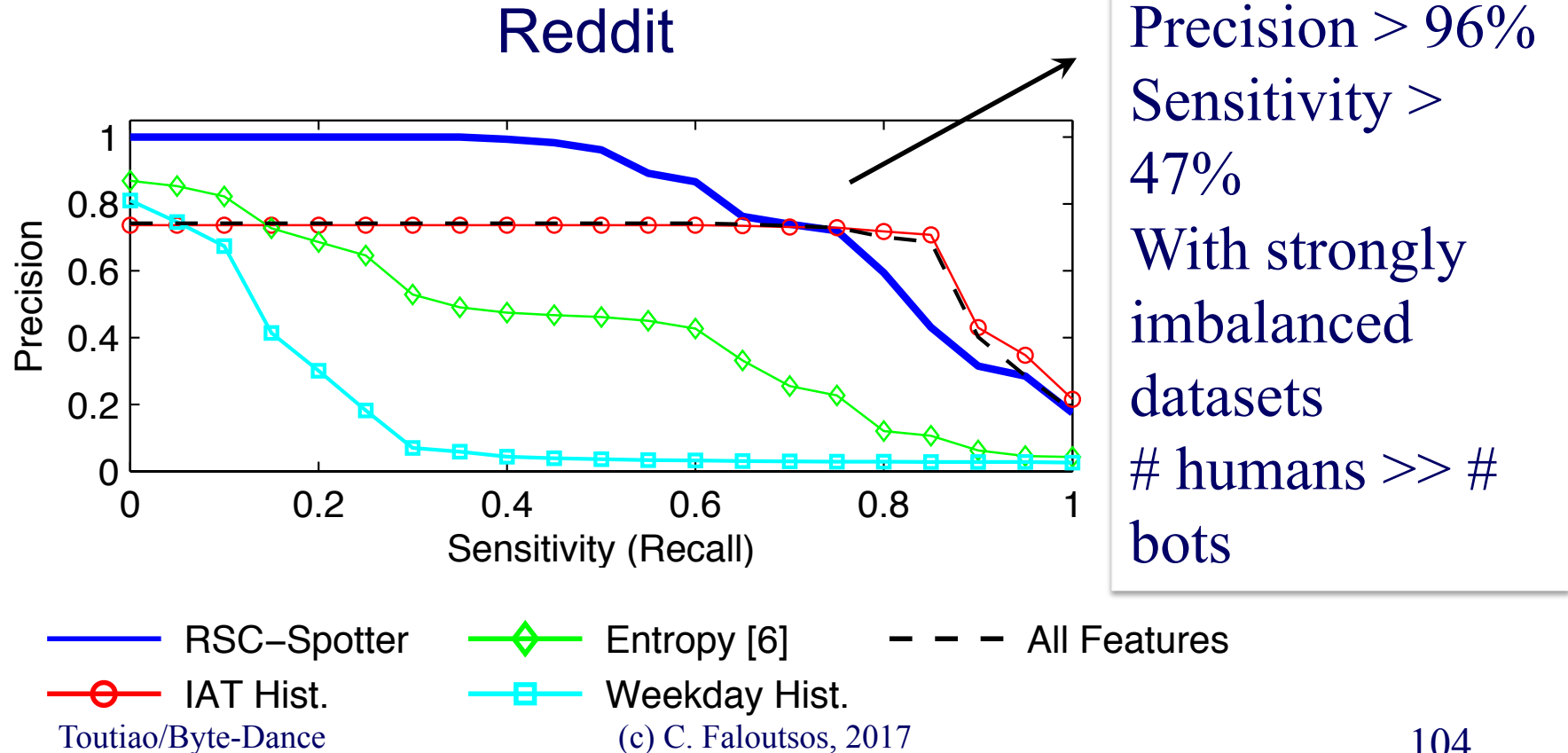
Toutiao/Byte-Dance

(c) C. Faloutsos, 2017

Experiments: Can RSC-Spotter Detect Bots?

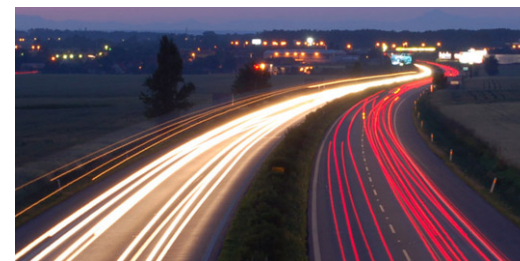
Precision vs. Sensitivity Curves

Good performance: curve close to the top



Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs
 - P2.1: tools/tensors
 - P2.2: other patterns
 - inter-arrival time
 - Network growth
- Conclusions





Beyond Sigmoids: the NetTide Model for Social Network Growth and its Applications

KDD'16

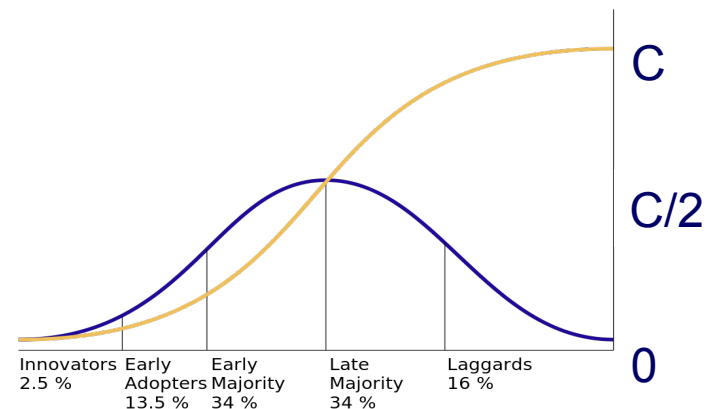
Chengxi Zang 臧承熙, Peng Cui, CF



PROBLEM: $n(t)$ and $e(t)$, over time?

- $n(t)$: the number of nodes.
- $e(t)$: the number of edges.
- E.g.:
 - How many members will  have next month?
 - How many friendship links will  have next year?

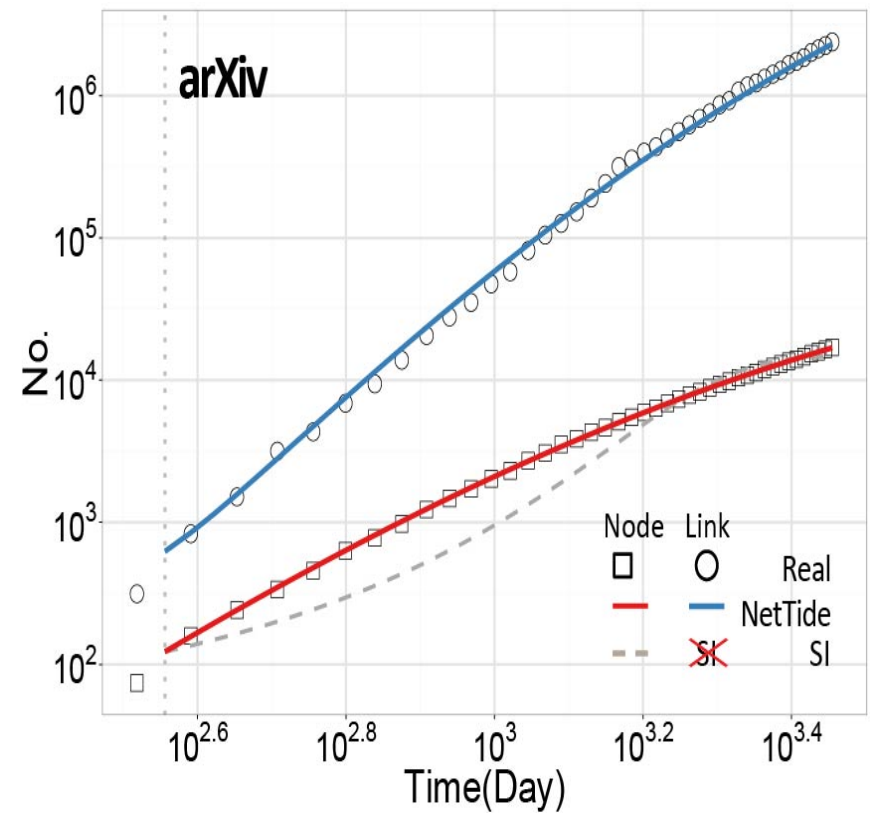
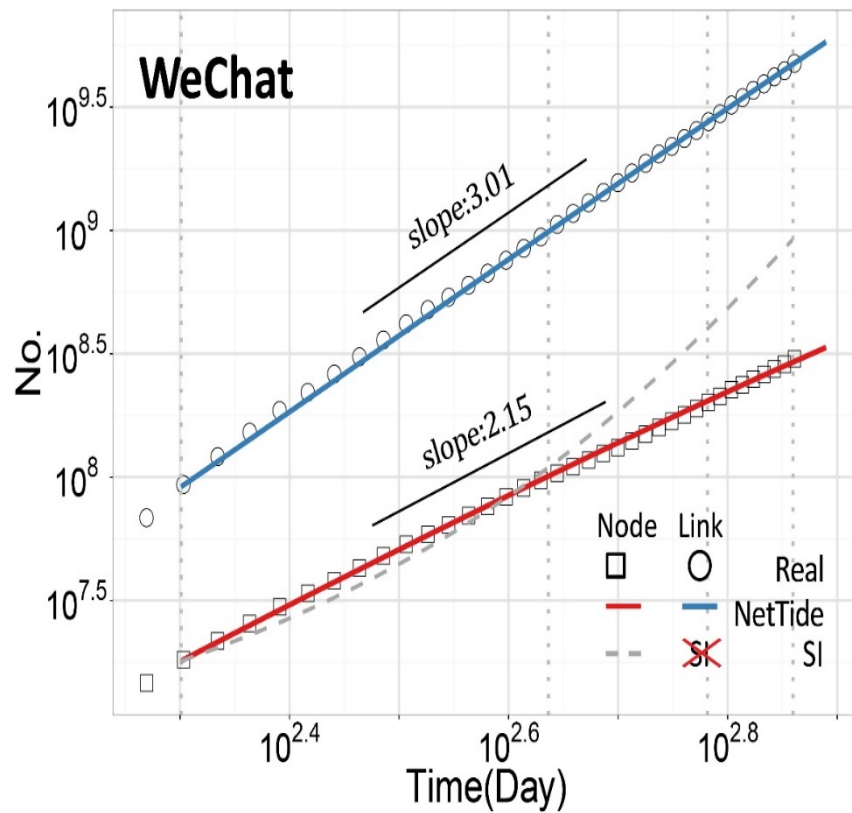
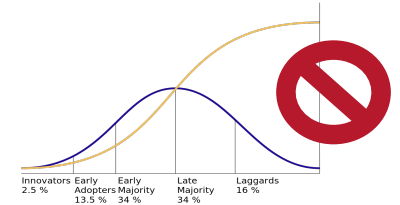
- Linear?
- Exponential?
- Sigmoid?



Datasets

- **WeChat 2011/1-2013/1 300M nodes, 4.75B links**
- ArXiv 1992/3-2002/3 17k nodes, 2.4M links
- Enron 1998/1-2002/7 86K nodes, 600K links
- Weibo 2006 165K nodes, 331K links

A: Power Law Growth



Cumulative growth (Log-Log scale)

Proposed: NetTide Model

- Nodes $n(t)$

$$\frac{dn(t)}{dt} = \frac{\beta}{t^\theta} n(t)(N - n(t))$$

- Links $e(t)$

$$\frac{de(t)}{dt} = \frac{\beta'}{t^\theta} n(t) \left(\alpha(n(t) - 1)^\gamma - \frac{e(t)}{n(t)} \right) + 2 \frac{dn(t)}{dt}$$

NetTide-Node Model

$$\frac{dn(t)}{dt} = \frac{\beta}{t^\theta} n(t) (N - n(t))$$

#nodes(t)
Total population

- Intuition:
 - **Rich-get-richer**
 - **Limitation**
 - **Fizzling nature**
- } = SI; ~Bass

NetTide-Node Model

$$\frac{dn(t)}{dt} = \frac{\beta}{t^\theta} n(t) (N - n(t))$$

#nodes(t)
Total population

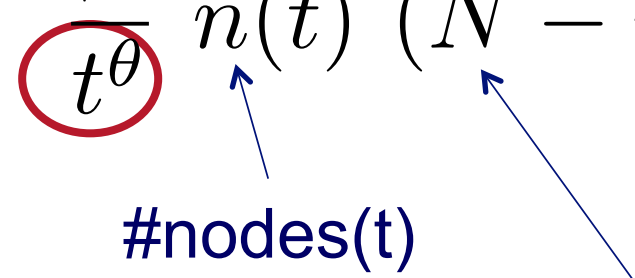
- Intuition:

- Rich-get-richer
- **Limitation**
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NetTide-Node Model

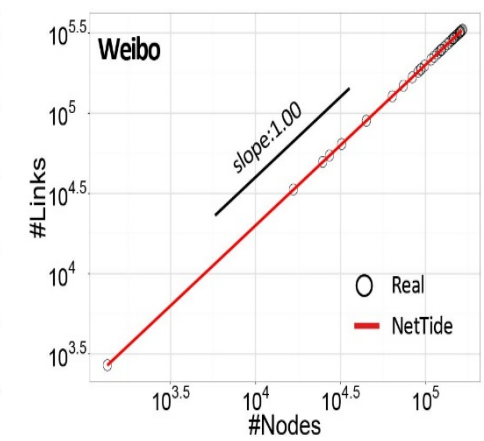
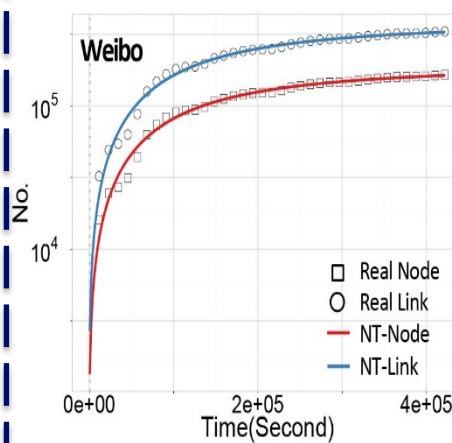
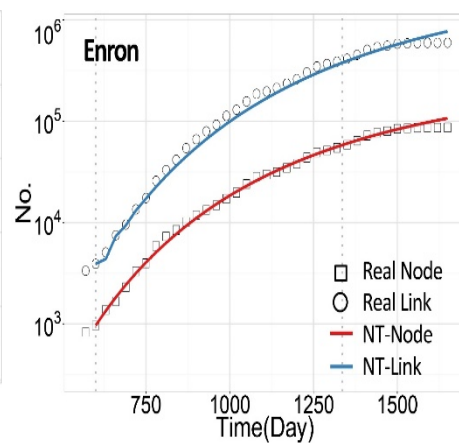
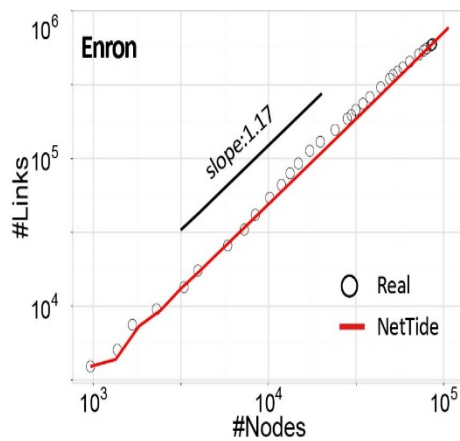
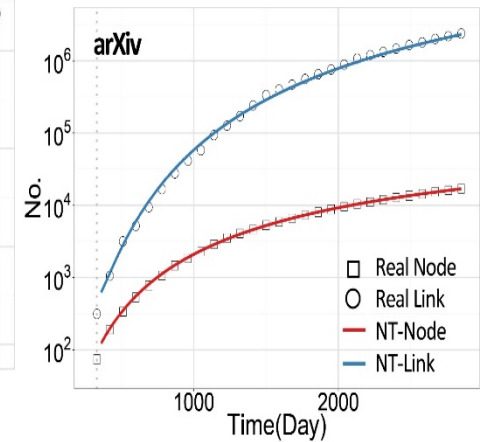
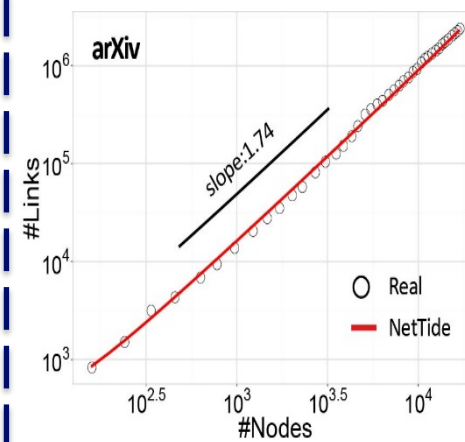
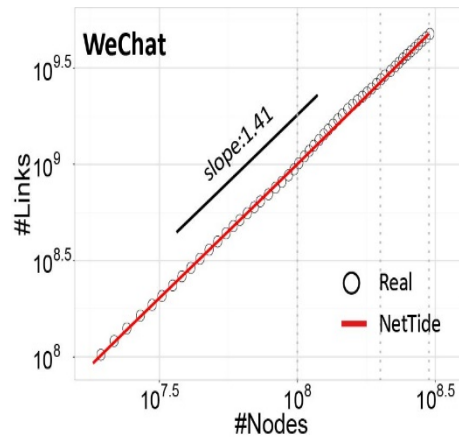
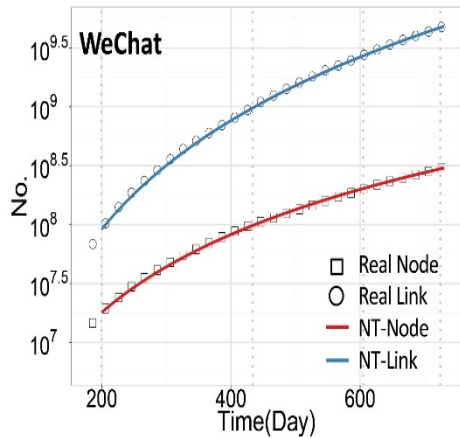
$$\frac{dn(t)}{dt} = \frac{\beta}{t^\theta} n(t) (N - n(t))$$



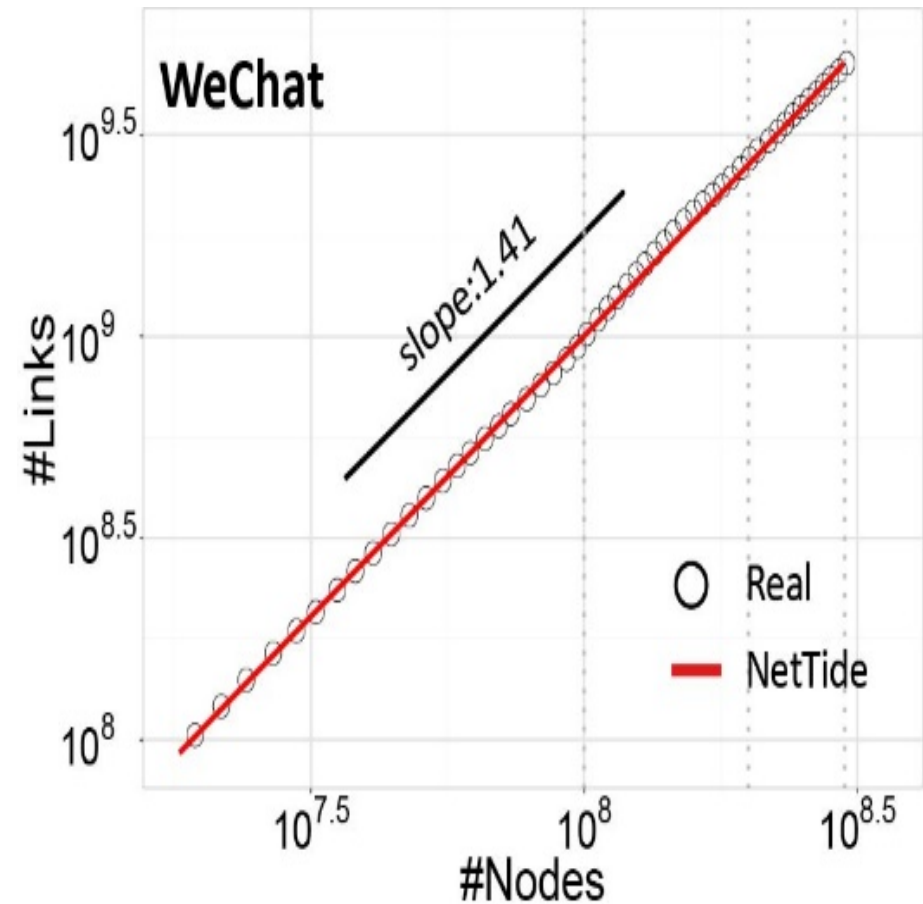
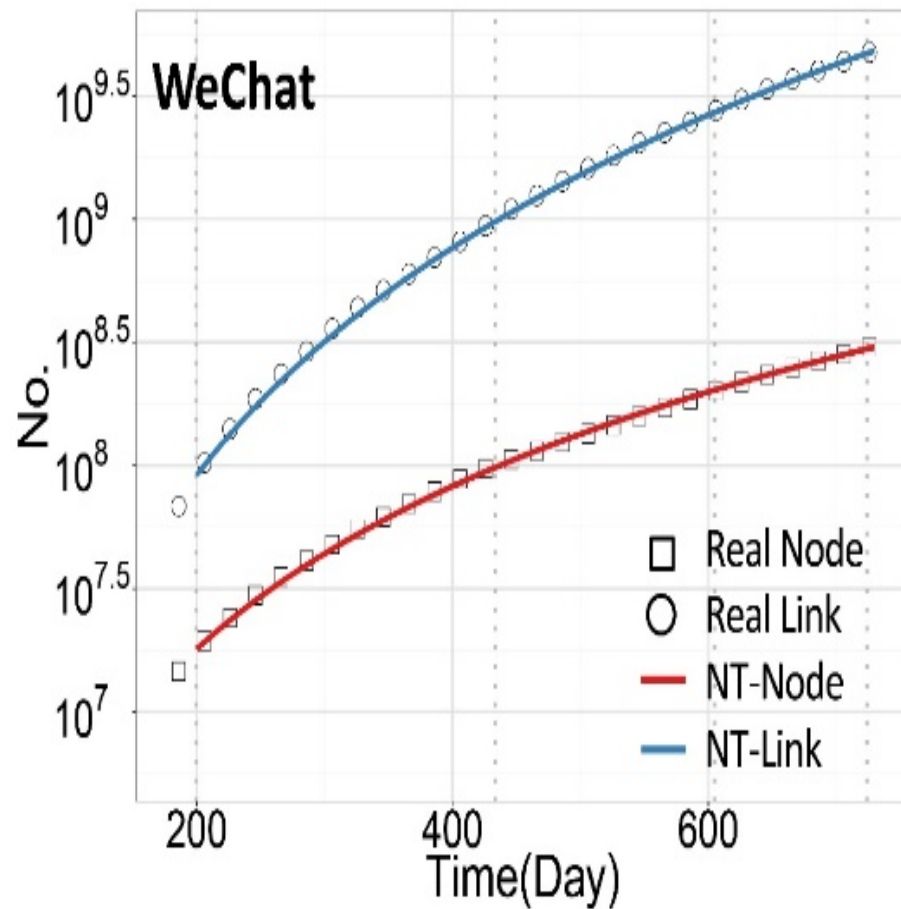
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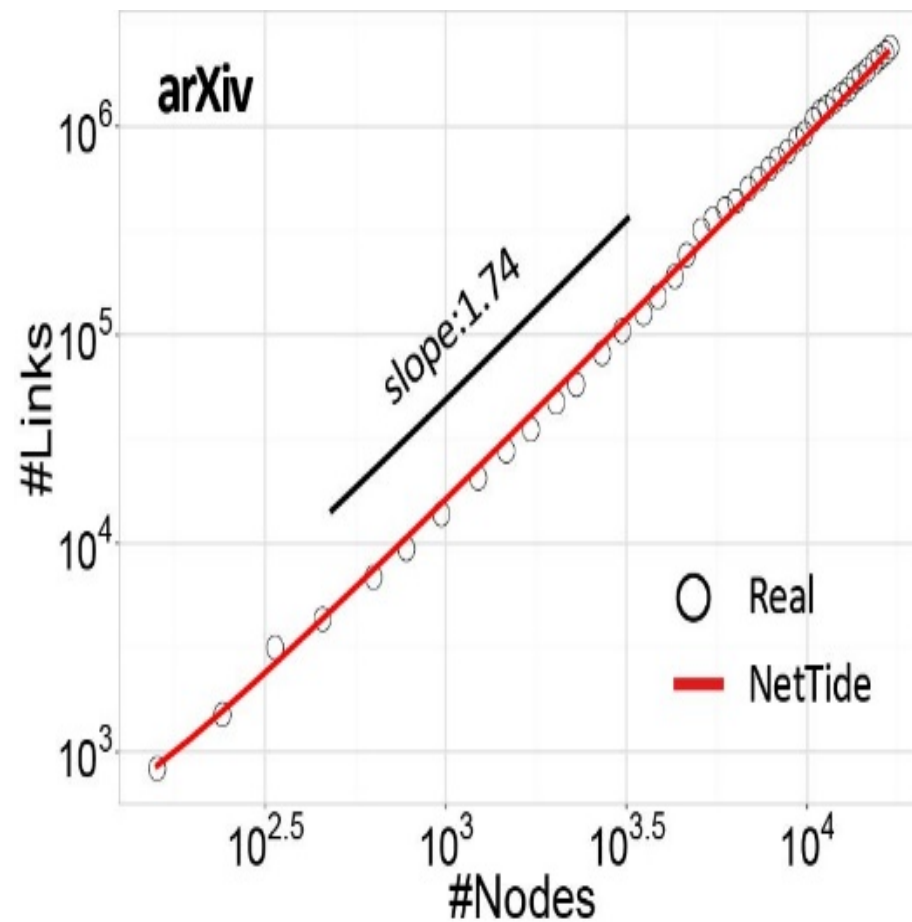
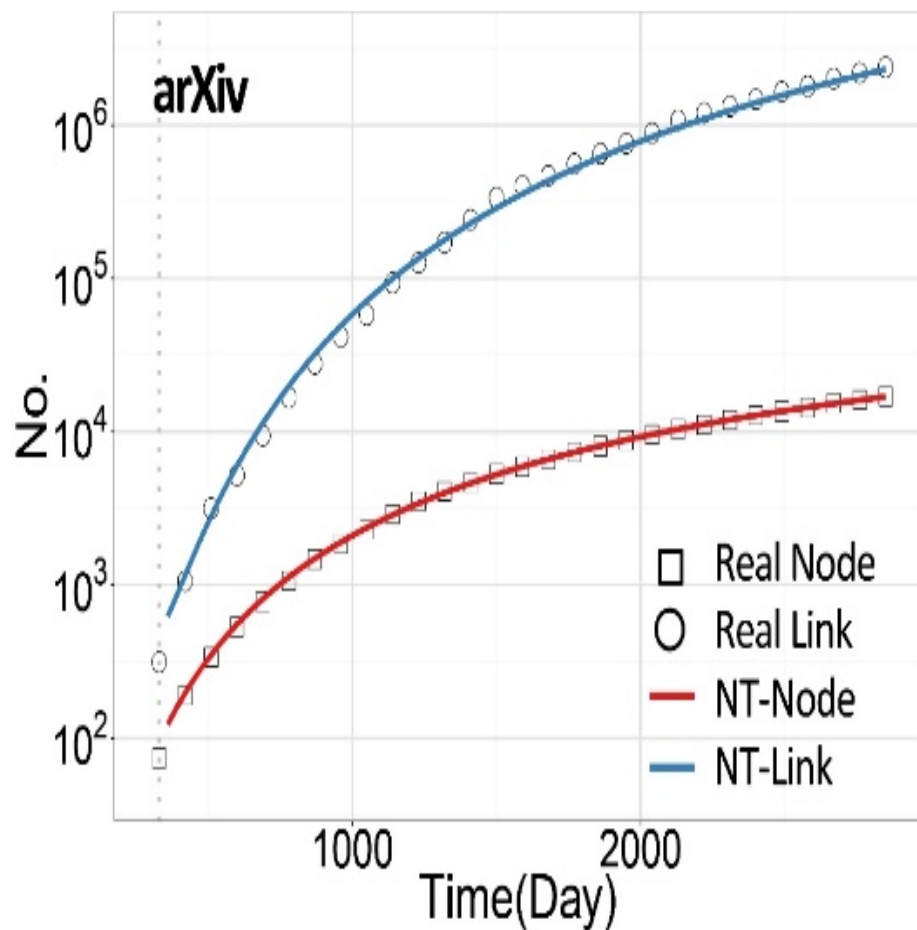
Results: Accuracy



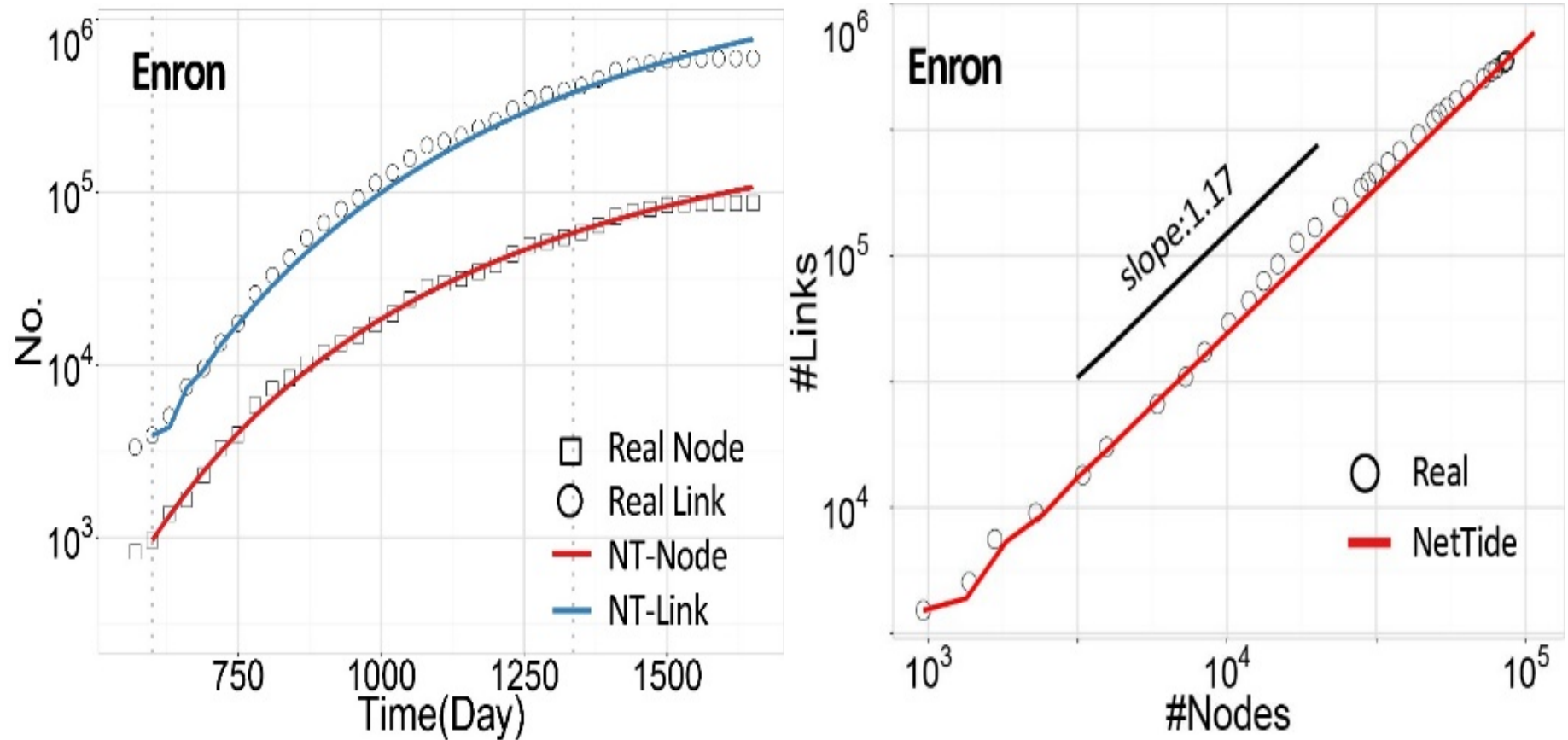
Results: Accuracy



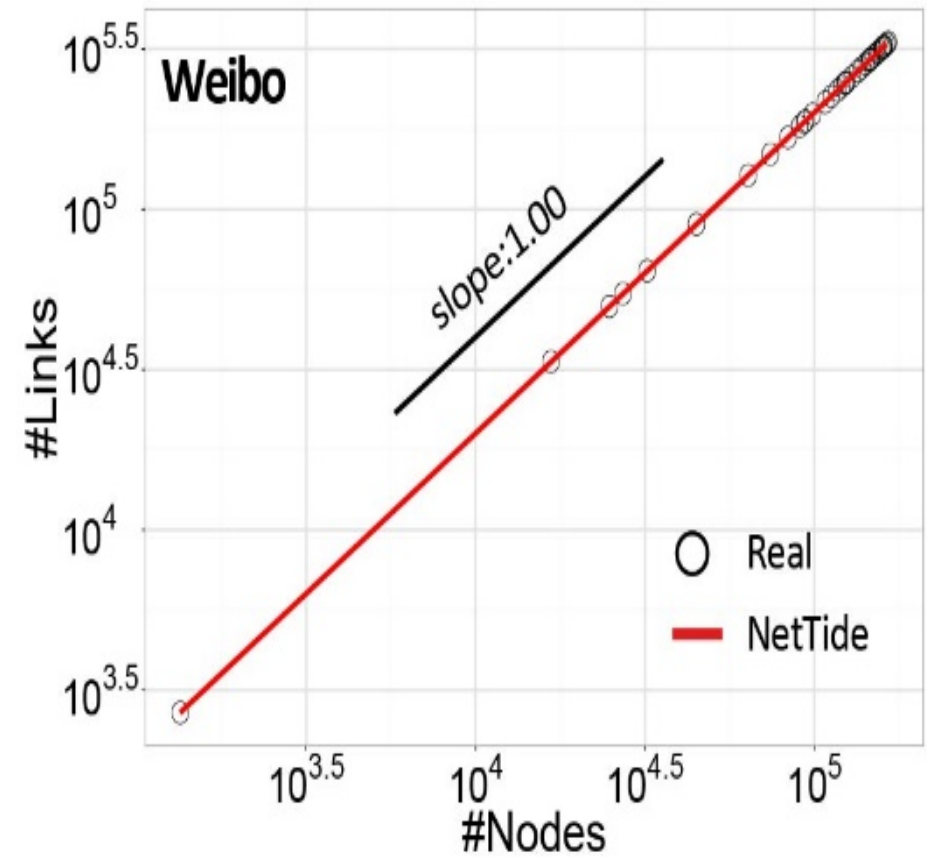
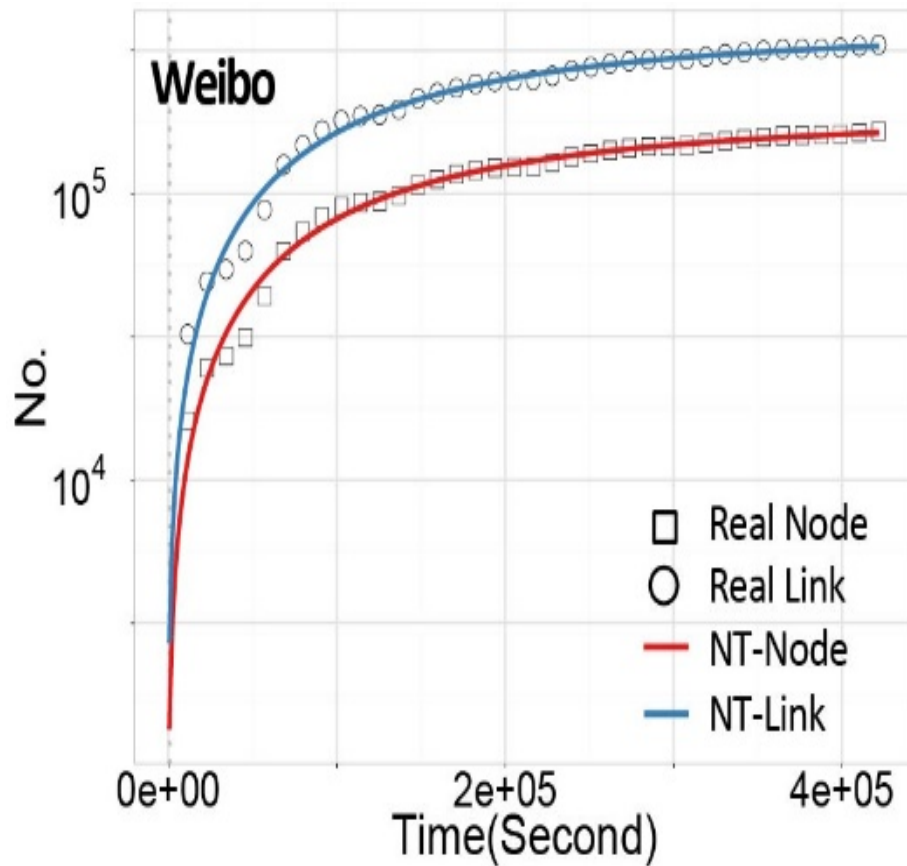
Results: Accuracy



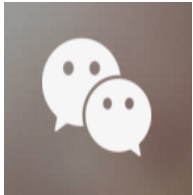
Results: Accuracy



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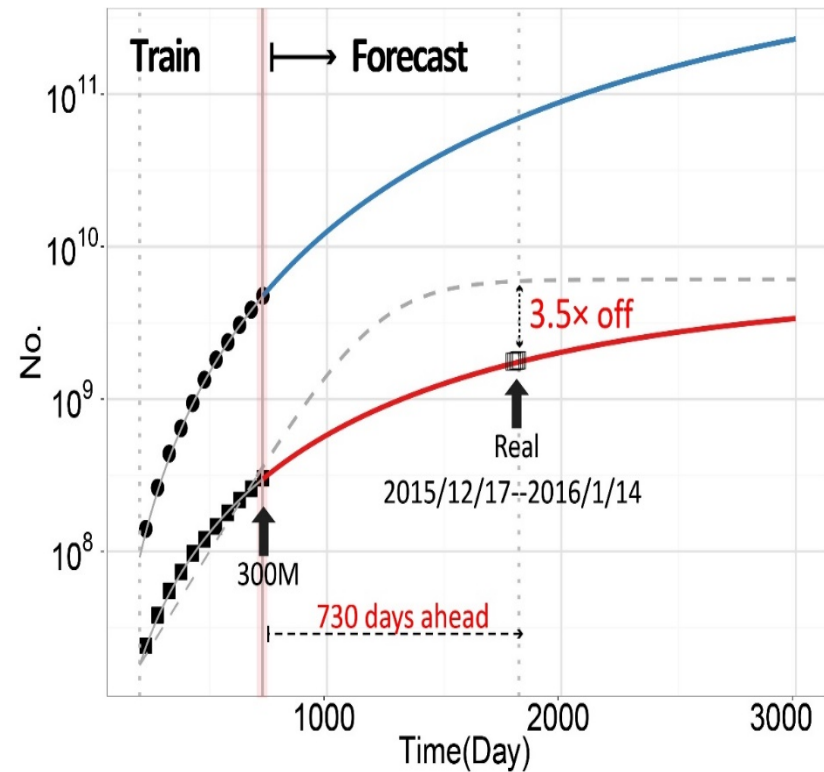
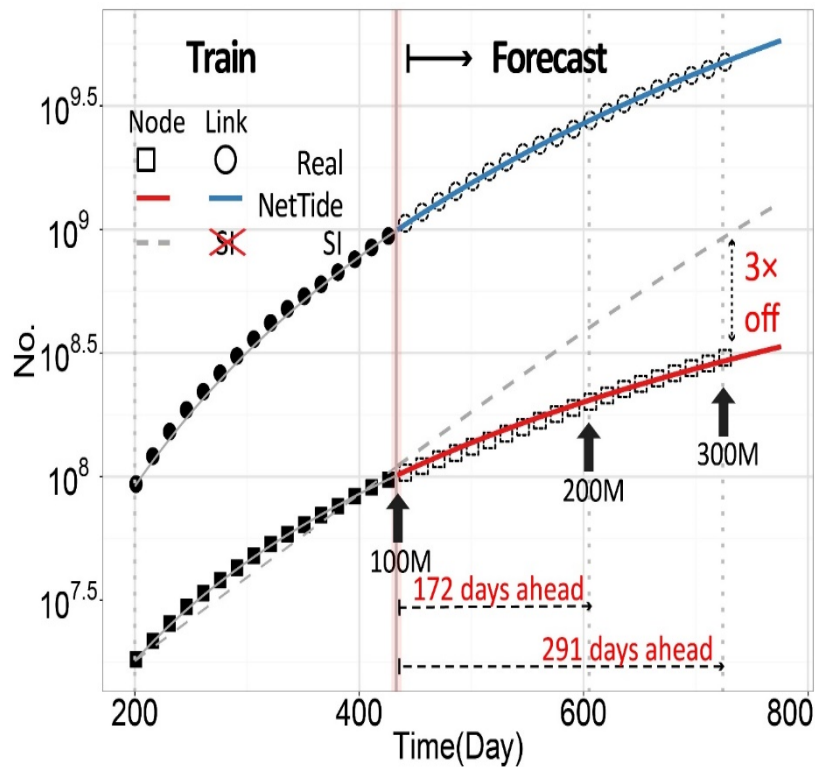


Results: Forecast



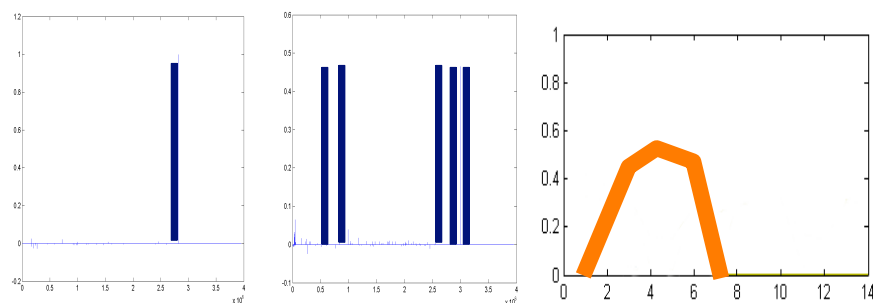
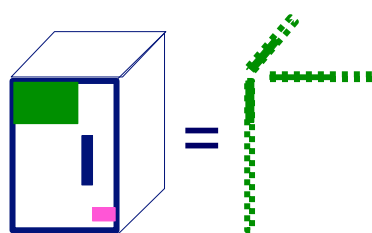
WeChat from 100 million to 300 million

730 days ahead

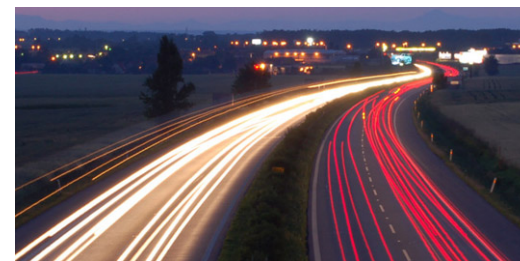


Part 2: Conclusions

- Time-evolving / heterogeneous graphs \rightarrow tensors
- PARAFAC finds patterns
- Surprising temporal patterns (P.L. growth)



Roadmap



- Introduction – Motivation
 - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
- ➔ • Acknowledgements and Conclusions

Thanks



Disclaimer: All opinions are mine; not necessarily reflecting the opinions of the funding agencies

Thanks to: NSF IIS-0705359, IIS-0534205, CTA-INARC; Yahoo (M45), LLNL, IBM, SPRINT, Google, INTEL, HP, iLab

Cast



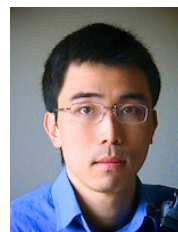
Akoglu,
Leman



Araujo,
Miguel



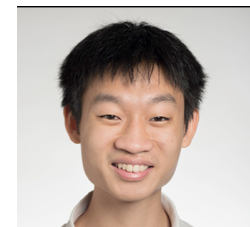
Beutel,
Alex



Chau,
Polo



Eswaran,
Dhivya



Hooi,
Bryan



Kang, U



Koutra,
Danai



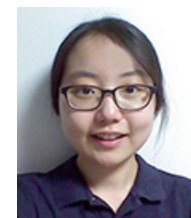
Papalexakis,
Vagelis



Shah,
Neil




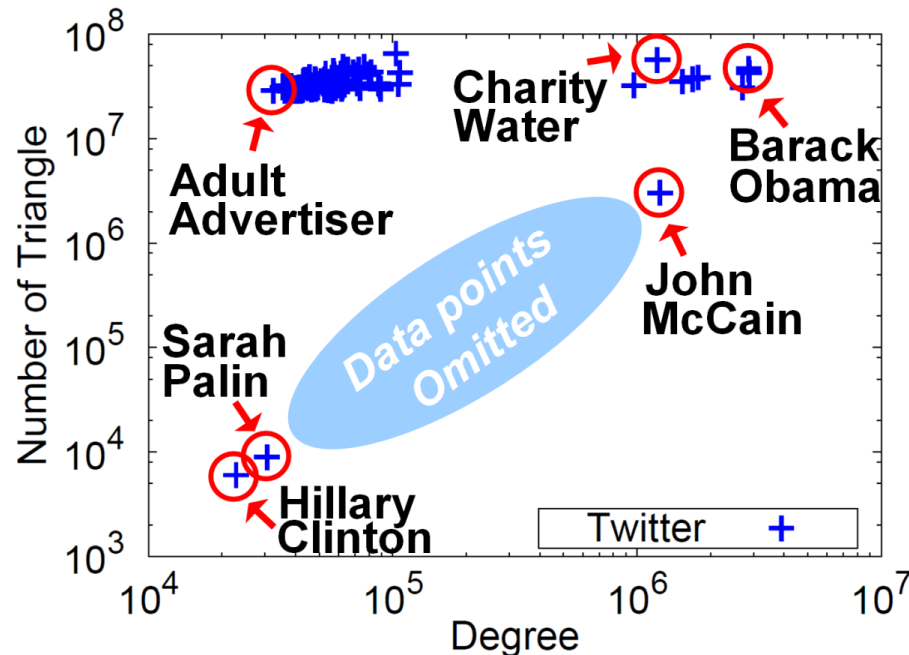
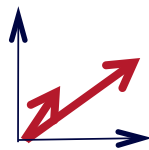
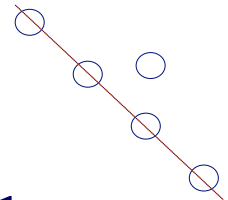
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Kijung



Song,
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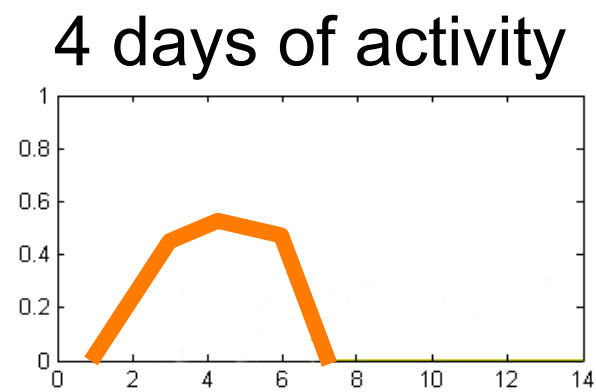
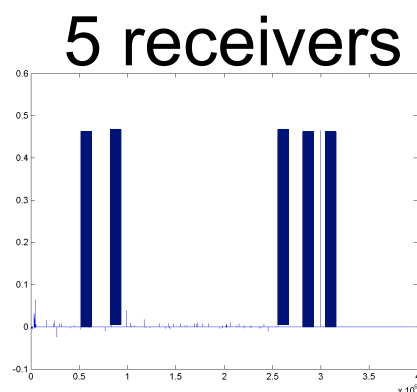
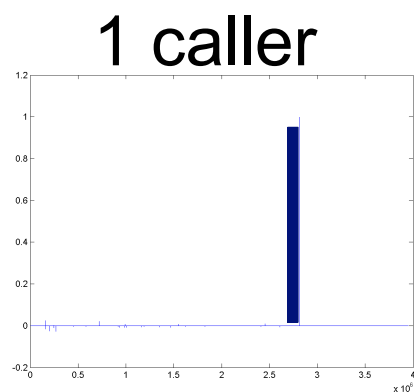
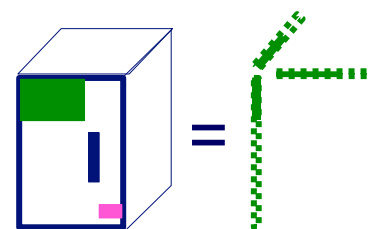
CONCLUSION#1 – Big data

- **Patterns**  **Anomalies**
- **Large datasets reveal patterns/outliers that are invisible otherwise**



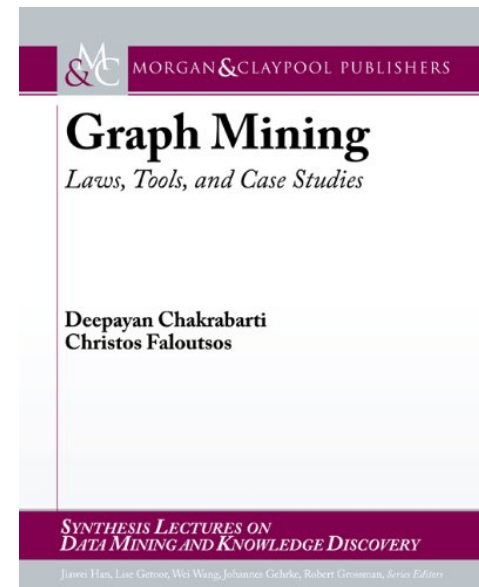
CONCLUSION#2 – tensors

- powerful tool

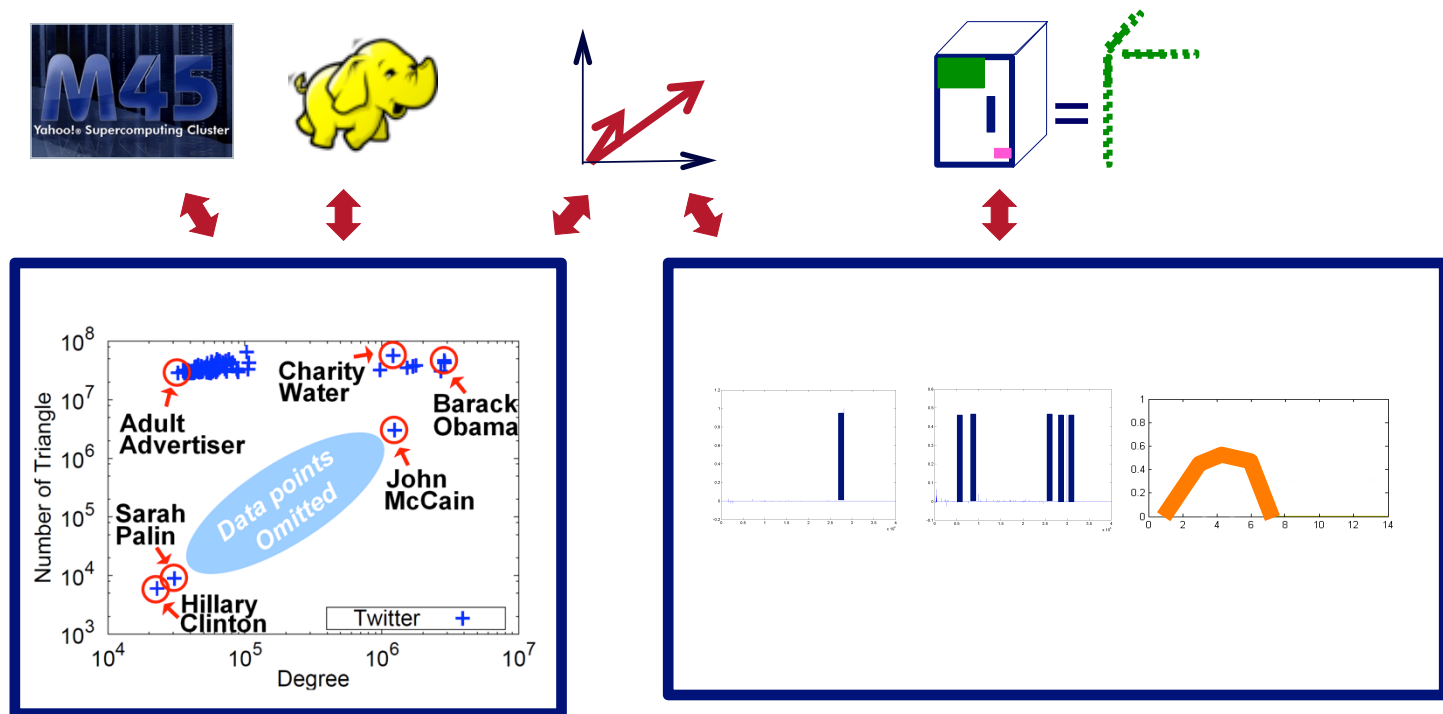


References

- D. Chakrabarti, C. Faloutsos: *Graph Mining – Laws, Tools and Case Studies*, Morgan Claypool 2012
- <http://www.morganclaypool.com/doi/abs/10.2200/S00449ED1V01Y201209DMK006>



TAKE HOME MESSAGE: Cross-disciplinarity



Thank you!

Cross-disciplinarity

