

15-826: Multimedia Databases and Data Mining

Primary key indexing – B-trees Christos Faloutsos - CMU www.cs.cmu.edu/~christos



Problem

Given a large collection of (multimedia) records, find similar/interesting things, ie:

- Allow fast, approximate queries, and
- Find rules/patterns

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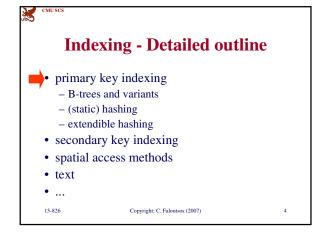
Outline

Goal: 'Find similar / interesting things'

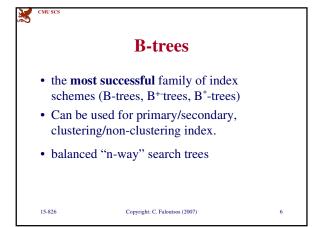
- Intro to DB

Indexing - similarity search

• Data Mining







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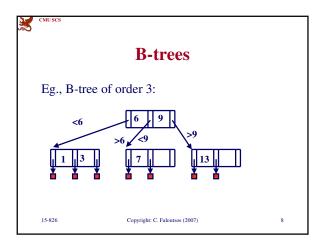
Citation

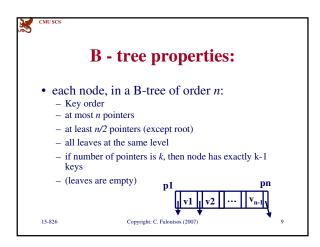


 Rudolf Bayer and Edward M. McCreight, Organization and Maintenance of Large Ordered Indices, Acta Informatica, 1:173-189, 1972.

- Received the 2001 SIGMOD innovations award
- among the most cited db publications
 - •www.informatik.uni-trier.de/~ley/db/about/top.html

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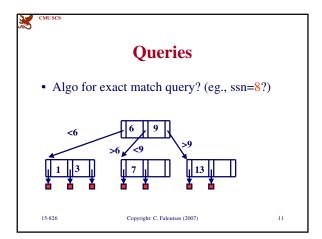
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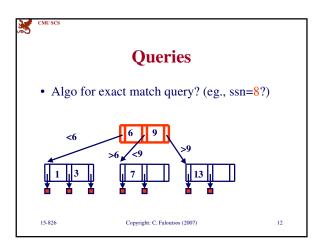
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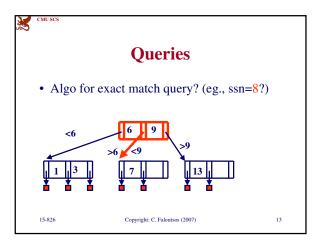
Properties

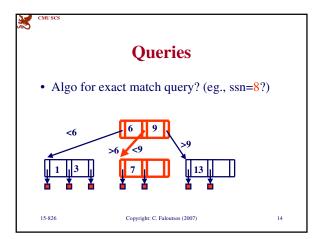
- "block aware" nodes: each node -> disk page
- O(log (N)) for everything! (ins/del/search)
- typically, if m = 50 100, then 2 3 levels
- utilization >= 50%, guaranteed; on average 69%

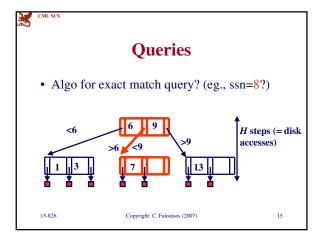
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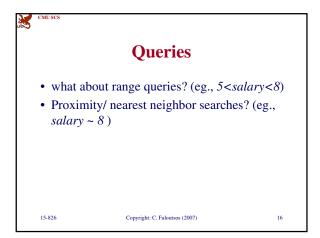


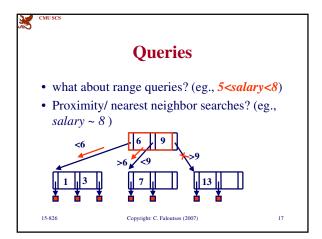


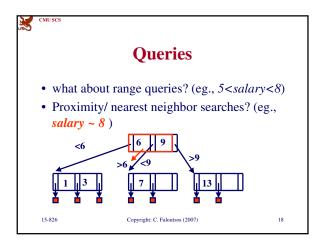


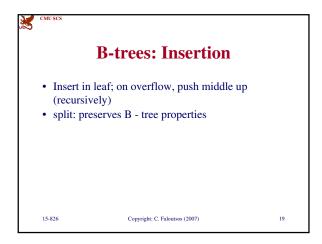


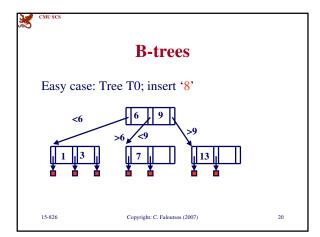
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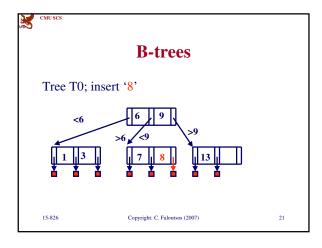


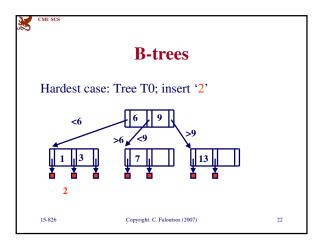


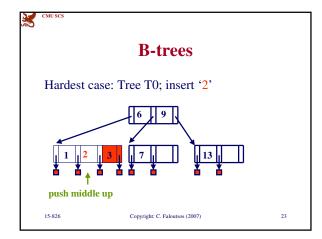


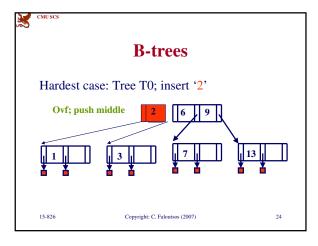


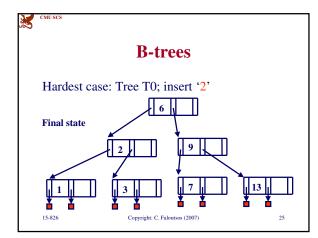












B-trees: Insertion

• Q: What if there are two middles? (eg, order 4)

• A: either one is fine

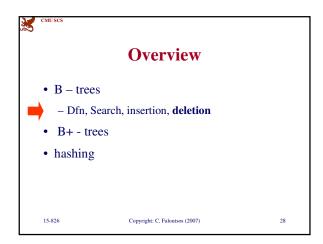
B-trees: Insertion

Insert in leaf; on overflow, push middle up (recursively – 'propagate split')

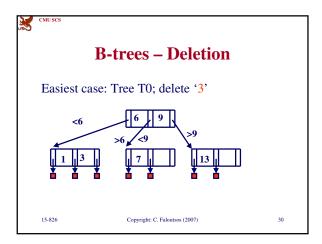
split: preserves all B - tree properties (!!)

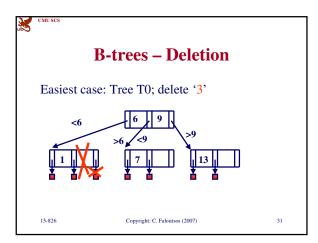
notice how it grows: height increases when root overflows & splits

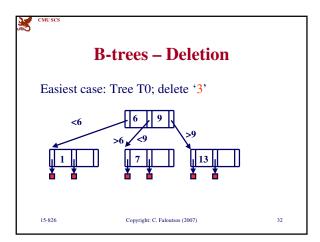
Automatic, incremental re-organization

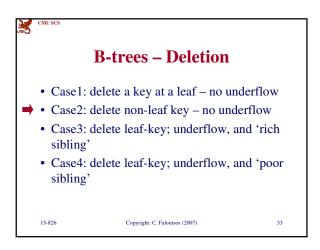


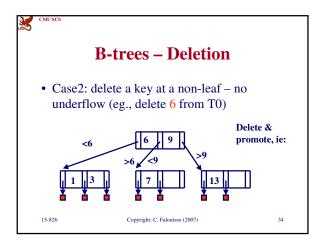


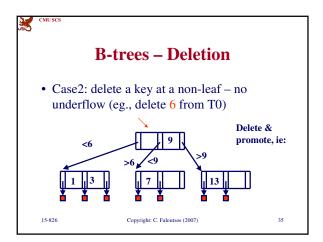


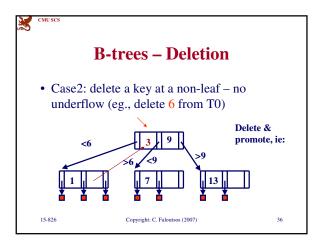


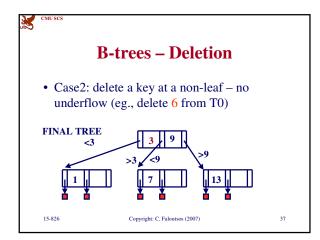












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B-trees – Deletion

- Case2: delete a key at a non-leaf no underflow (eg., delete 6 from T0)
- Q: How to promote?
- A: pick the largest key from the left sub-tree (or the smallest from the right sub-tree)
- Observation: every deletion eventually becomes a deletion of a leaf key

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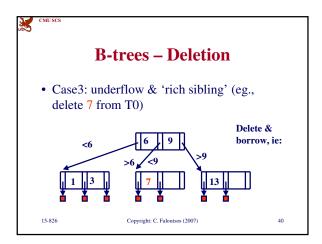


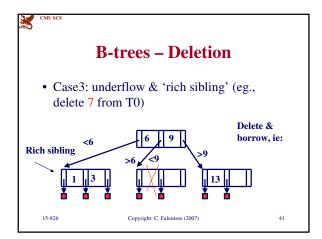
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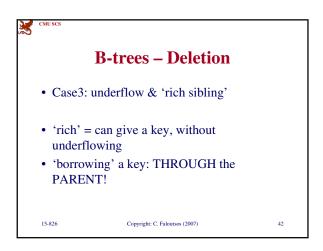
B-trees – Deletion

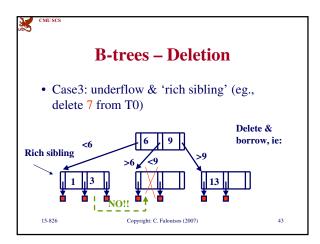
- Case1: delete a key at a leaf no underflow
- Case2: delete non-leaf key no underflow
- Case3: delete leaf-key; underflow, and 'rich sibling'
 - Case4: delete leaf-key; underflow, and 'poor sibling'

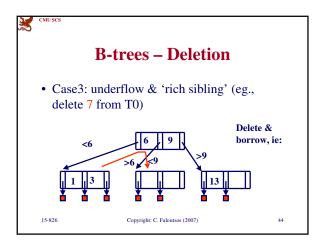
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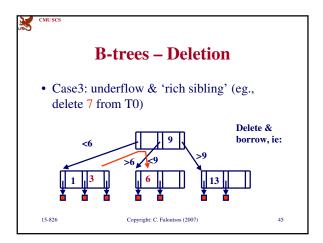


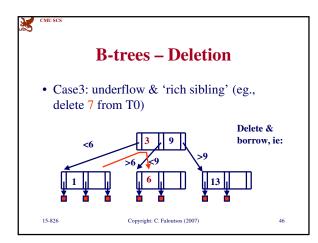


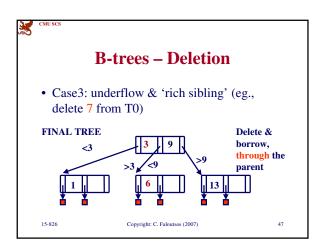




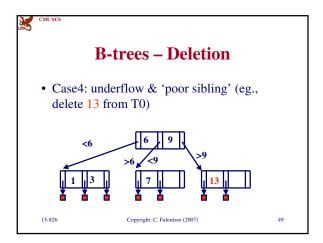


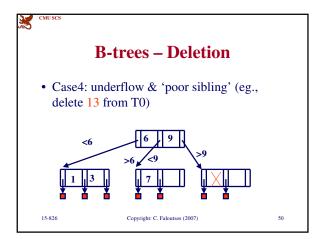


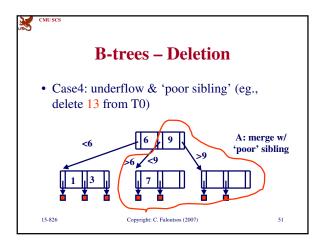


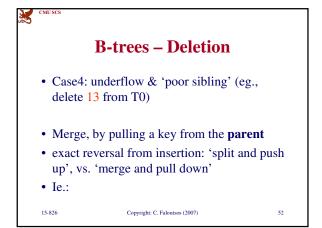


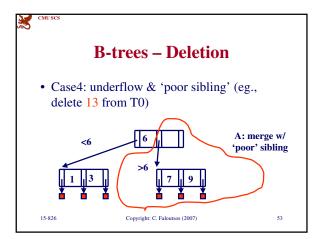
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	B-trees – Deletion		
→	Case2: deleteCase3: delete sibling'	a key at a leaf – no underflow non-leaf key – no underflow leaf-key; underflow, and 'ric leaf-key; underflow, and 'po	h
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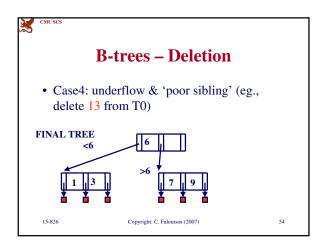


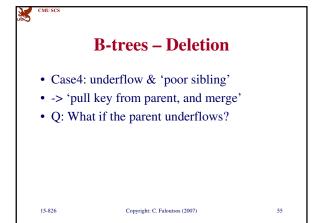












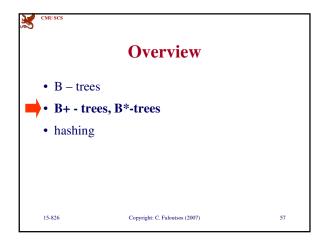
B-trees – Deletion

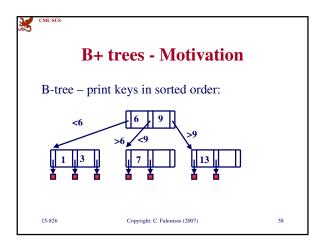
• Case4: underflow & 'poor sibling'

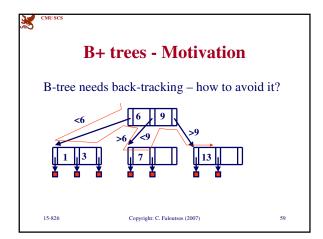
• -> 'pull key from parent, and merge'

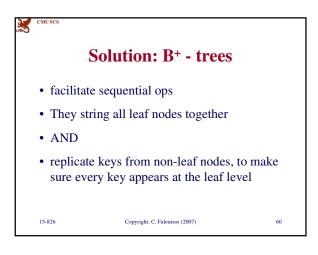
• Q: What if the parent underflows?

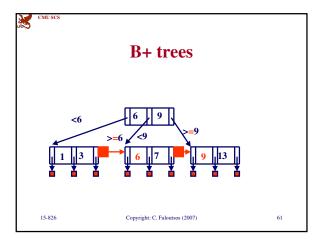
• A: repeat recursively

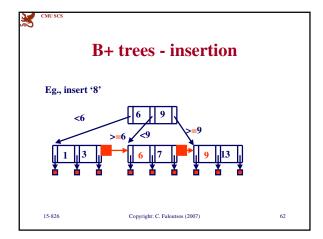


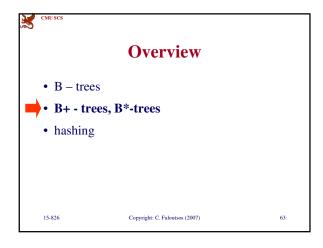


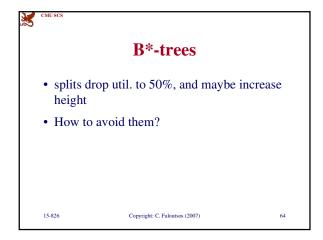


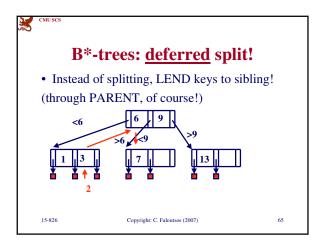


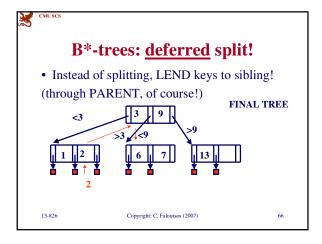














B*-trees: <u>deferred</u> split!

- Notice: shorter, more packed, faster tree
- It's a rare case, where space utilization and speed improve together
- BUT: What if the sibling has no room for our 'lending'?

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B*-trees: deferred split!

- BUT: What if the sibling has no room for our 'lending'?
- A: 2-to-3 split: get the keys from the sibling, pool them with ours (and a key from the parent), and split in 3.
- Details: too messy (and even worse for deletion)

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Conclusions

- Main ideas: recursive; block-aware; on overflow -> split; defer splits
- All B-tree variants have excellent, O(logN) worst-case performance for ins/del/search
- B+ tree is the prevailing indexing method
- More details: [Knuth vol 3.] or [Ramakrishnan & Gehrke, 3rd ed, ch. 10]

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