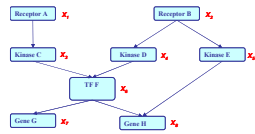


Graphical Models (IV)

Applications in IR

— Probabilistic Topic Models

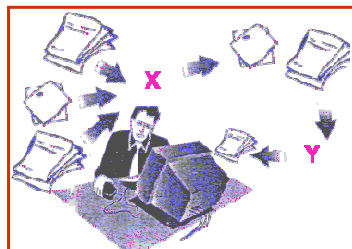


Eric Xing

Carnegie Mellon University
June 7, 2007

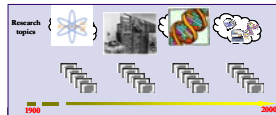
Eric Xing,
A lecture series at the Institute of Theoretical Computer
Science, Tsinghua University, May 31-June 7, 2007

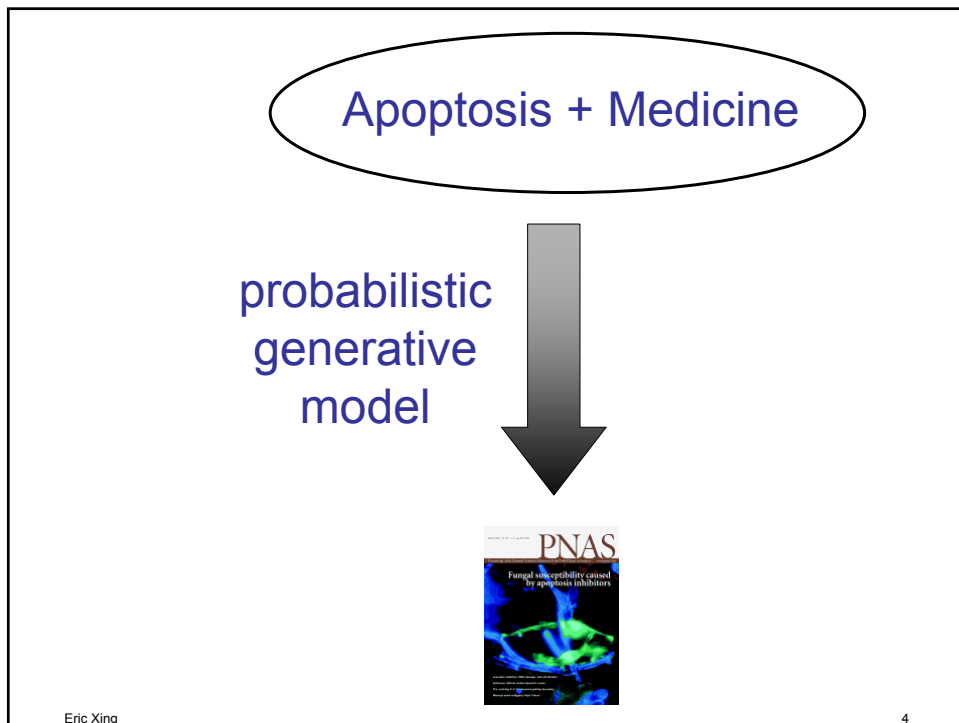
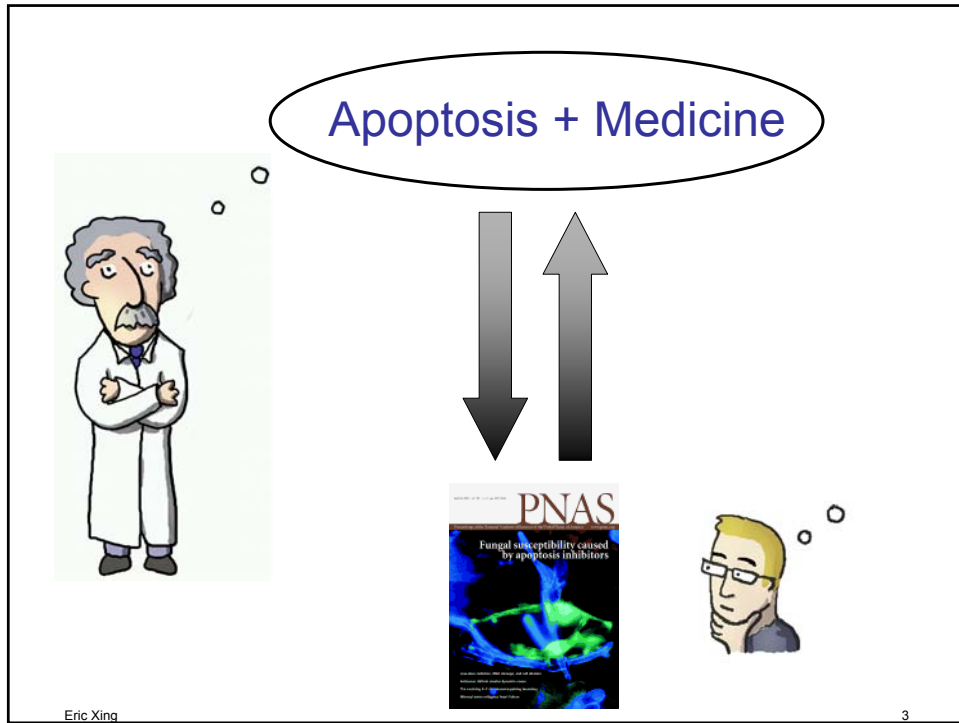
NLP and Data Mining

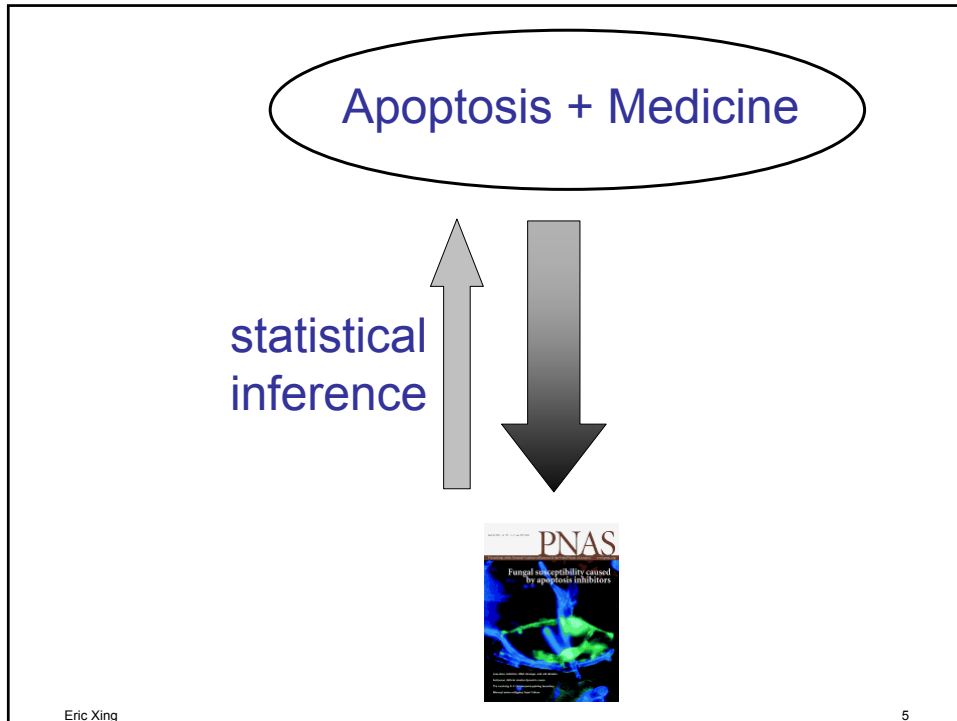


We want:

- Semantic-based search
- infer topics and categorize documents
- Multimedia inference
- Automatic translation
- Predict how topics evolve
- ...







“...probability theory is more fundamentally concerned with the structure of reasoning and causation than with numbers.”

Glenn Shafer and Judea Pearl
Introduction to Readings in Uncertain Reasoning,
Morgan Kaufmann, 1990

Eric Xing 6

This Talk

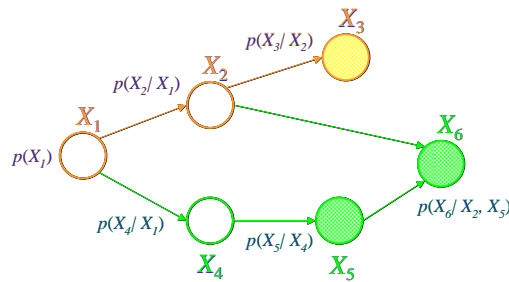


- A recap of graphical model
- Two families of probabilistic topics models and approximate inference
 - Bayesian admixture models
 - Random models
- Three applications
 - Topic evolution
 - Machine translation
 - Multimedia inference

Probabilistic Graphical Models



- Graph-theoretic representations of probabilistic distributions



$$p(X_1, X_2, X_3, X_4, X_5, X_6) = p(X_1) p(X_2 | X_1) p(X_3 | X_2) p(X_4 | X_1) p(X_5 | X_4) p(X_6 | X_2, X_5)$$

- Bayesian philosophy



- Modular combination of heterogeneous parts -- **divide and conquer**

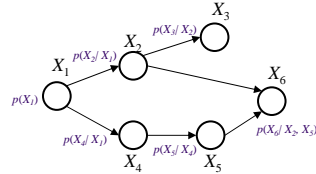
Probabilistic Inference



- Many modern problems in data mining/NLP can be formulated as probabilistic inference problems

$P(\text{query variable} \mid \text{query data \& KB})$

- Is this text document relevant to my query?
- Which category is this image in?
- What movies would I probably like?
- Create a caption for this image.
- Modeling document collections



- General purpose algorithms exist to fully automate such computation
 - Computational cost depends on the topology of the network
 - Exact inference:
 - The junction tree algorithm
 - Approximate inference;
 - Loopy belief propagation, variational inference, Monte Carlo sampling

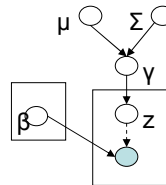
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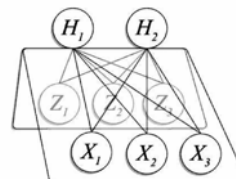
Two types of GMs



- Directed edges give causality relationships (**Bayesian Network or Directed Graphical Model**):



- Undirected edges simply give correlations between variables (**Markov Random Field or Undirected Graphical model**):



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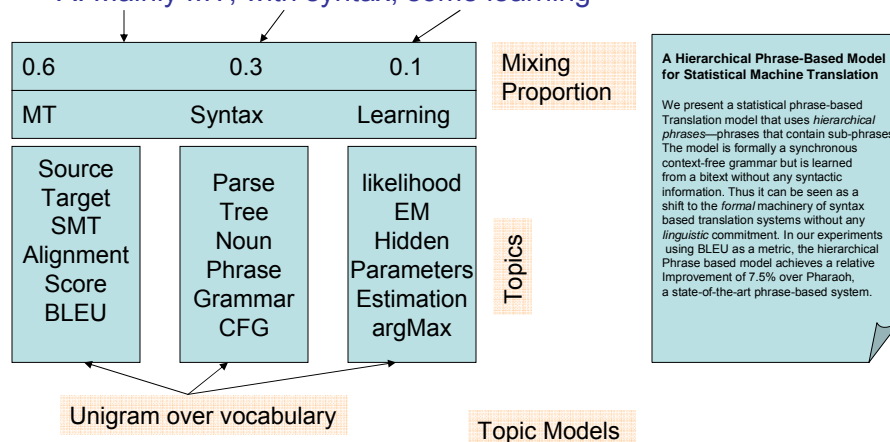
10

This Talk

- A graphical model primer
- Two families of probabilistic topics models and approximate inference
 - Bayesian admixture models
 - Random models
- Three applications
 - Topic evolution
 - Machine translation
 - Multimedia inference

How to Model Semantic?

- Q: What is it about?
- A: Mainly MT, with syntax, some learning



Why this is Useful?

- Q: What is it about?
- A: Mainly MT, with syntax, some learning

| | | |
|-----|--------|----------|
| 0.6 | 0.3 | 0.1 |
| MT | Syntax | Learning |

Mixing
Proportion

A Hierarchical Phrase-Based Model for Statistical Machine Translation

We present a statistical phrase-based Translation model that uses *hierarchical phrases*—phrases that contain sub-phrases. The model is formally a synchronous context-free grammar but is learned from a bitext without any syntactic information. Thus it can be seen as a shift to the *formal* machinery of syntax based translation systems without any *linguistic* commitment. In our experiments using BLEU as a metric, the hierarchical Phrase based model achieves a relative Improvement of 7.5% over Pharaoh, a state-of-the-art phrase-based system.

- Q: give me similar document?
 - Structured way of browsing the collection
- Other tasks
 - Dimensionality reduction
 - TF-IDF vs. topic mixing proportion
 - Classification, clustering, and more ...

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Words in Contexts

- “It was a nice **shot.** ”



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Words in Contexts (con'd)



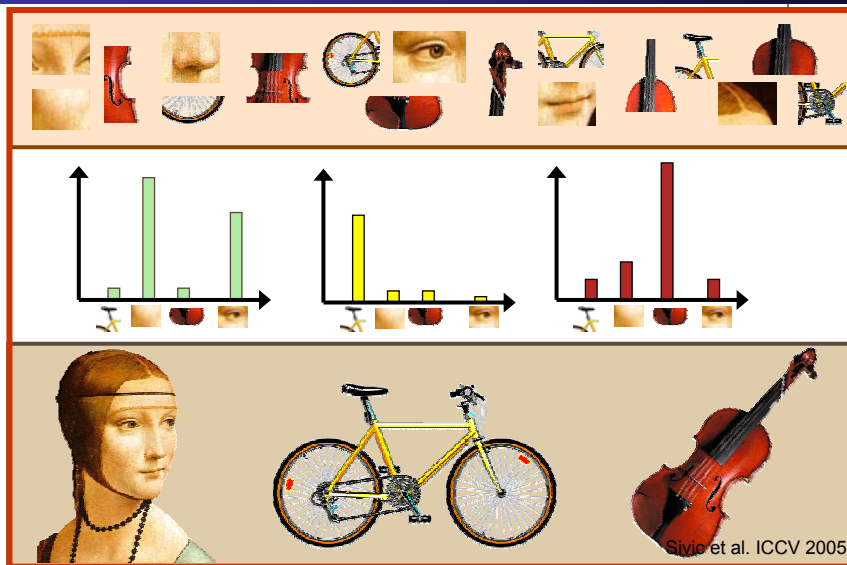
- the opposition Labor Party fared even worse, with a predicted 35 **seats**, seven less than last election.



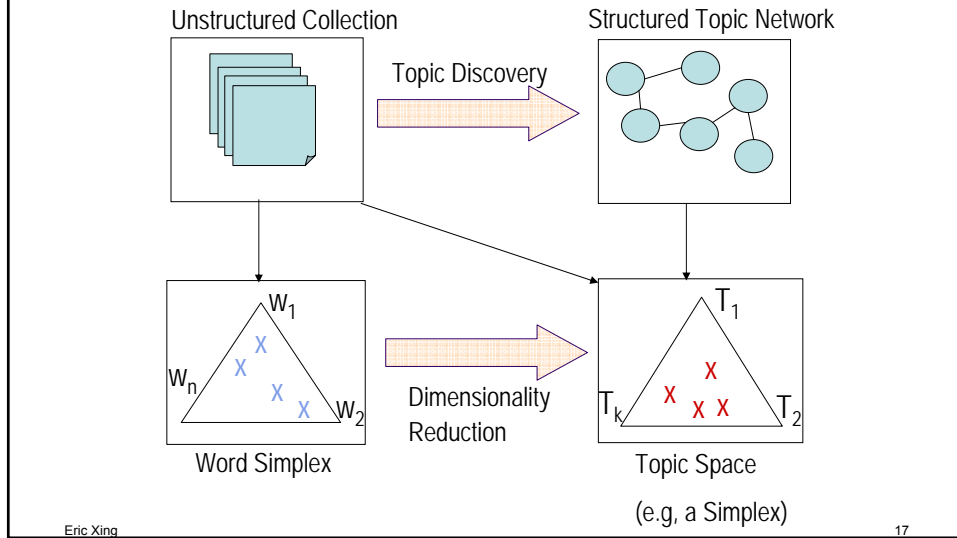
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"Words" in Contexts (con'd)



Topic Models: The Big Picture



Method One:

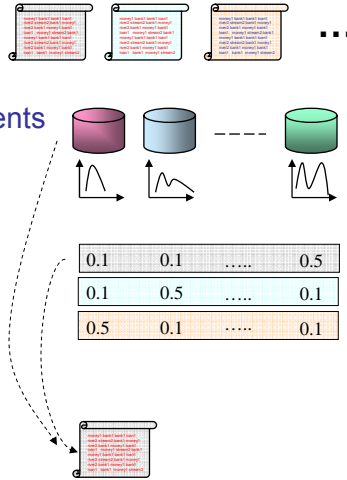


- **Hierarchical Bayesian Admixture**

A. Ahmed and E.P. Xing
AISTAT 2007

Admixture Models

- Objects are **bags** of elements
- Mixtures are **distributions** over elements
- Objects have **mixing vector** θ
 - Represents each mixtures' contributions
- Object is **generated** as follows:
 - Pick a mixture component from θ
 - Pick an element from that component



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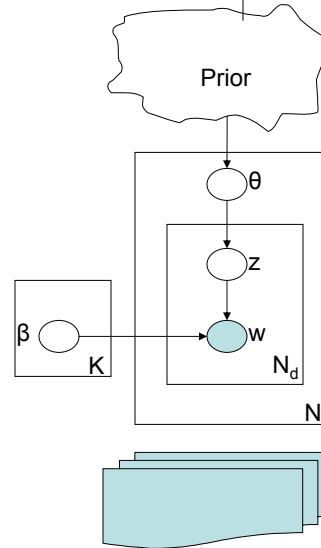
19

Topic Models = Admixture Models

Generating a document

- Draw θ from the prior
- For each word n
- Draw z_n from $multinomial(\theta)$
 - Draw $w_n | z_n, \{\beta_{1,k}\}$ from $multinomial(\beta_{z_n})$

Which prior to use?

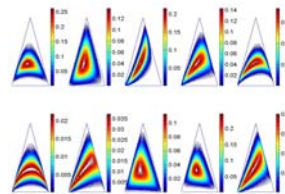
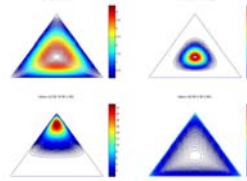


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Prior Comparison

- Dirichlet (LDA) (Blei et al. 2003)
 - Conjugate prior means efficient inference
 - Can **only** capture variations in each topic's intensity **independently**
- Logistic Normal (CTM=LoNTAM) (Blei & Lafferty 2005, Ahmed & Xing 2006)
 - Capture the intuition that some topics are highly correlated and can rise up in intensity together
 - **Not** a conjugate prior implies **hard** inference

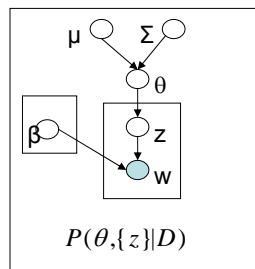


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Approximate Inference

(e.g., MF, Jordan et al 1999, GMF, Xing et al 2004)

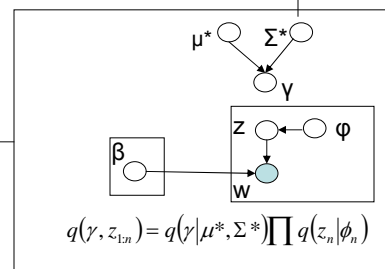


Σ^* is full matrix

Multivariate Quadratic Approx.

Closed Form Solution for μ^* , Σ^*

Ahmed&Xing



Σ^* is assumed to be diagonal

Tangent Approx.

Numerical Optimization to fit μ^* , $\text{Diag}(\Sigma^*)$

Blei&Lafferty

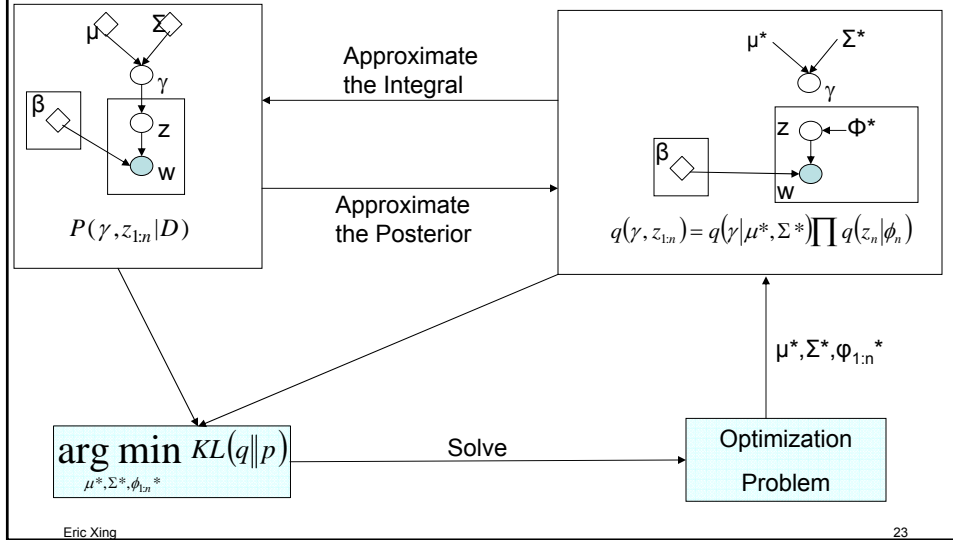
Log Partition Function

$$\log \left(1 + \sum_{i=1}^{K-1} e^{\gamma_i} \right)$$

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Variational Inference



Variational Inference With no Tears

$P(\gamma, \{z\} | D)$

Iterate until Convergence

- Pretend you know $E[Z_{1:n}]$
 - $P(\gamma | E[z_{1:n}], \mu, \Sigma)$
- Now you know $E[\gamma]$
 - $P(z_{1:n} | E[\gamma], w_{1:n}, \beta_{1:k})$

• More Formally: $q^*(X_C) = P(X_C | \langle S_Y \rangle_{q_y} : \forall y \in X_{MB})$

Message Passing Scheme (GMF)

Equivalent to previous method (Xing et. al.2003)

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LoNTAM Variations Inference

- Fully Factored Distribution

$$q(\gamma, z_{1:n}) = q(\gamma) \prod q(z_n)$$

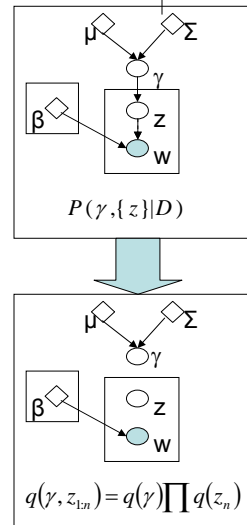
- Two clusters: λ and $Z_{1:n}$

$$q^*(X_C) = P\left(X_C \mid \langle S_Y \rangle_{q_Y} : \forall y \in X_{MB}\right)$$

- Fixed Point Equations

$$q_\gamma^*(\gamma) = P\left(\gamma \mid \langle S_z \rangle_{q_z}, \mu, \Sigma\right)$$

$$q_z^*(z) = P\left(z \mid \langle S_\gamma \rangle_{q_\gamma}, \beta_{1:k}\right)$$



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Variational γ

$$q_\lambda^*(\gamma) = P\left(\gamma \mid \langle S_z \rangle_{q_z}, \mu, \Sigma\right)$$

$$\propto P(\gamma \mid \mu, \Sigma) P\left(\langle S_z \rangle_{q_z} \mid \gamma\right)$$

Now what is $\langle S_z \rangle_{q_z}$?

$$S_z = m = \left[\sum_n I(z_n = 1), \dots, \sum_n I(z_n = k) \right]$$

$$\propto N(\gamma \mid \mu, \Sigma) \exp\left\{ \langle m \rangle_{q_z} \gamma - N \times C(\gamma) \right\}$$

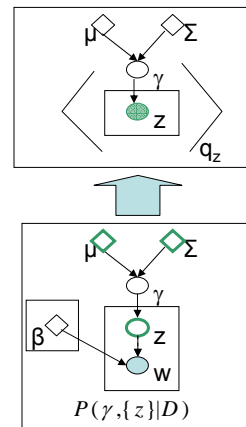
$$\propto \exp\left\{ -\frac{1}{2} \gamma' \Sigma^{-1} \gamma + \gamma \Sigma^{-1} \mu + \langle m \rangle_{q_z} \gamma - N \times C(\gamma) \right\}$$

$$C(\gamma) = C(\gamma_\lambda) + g'_\lambda (\gamma - \gamma_\lambda) + .5 (\lambda - \gamma_\lambda)' H (\gamma - \gamma_\lambda)$$

$$\rightarrow q_\lambda^*(\gamma) = N(\mu_\gamma, \Sigma_\gamma)$$

$$\Sigma_\gamma = \text{inv}(\Sigma^{-1} + NH)$$

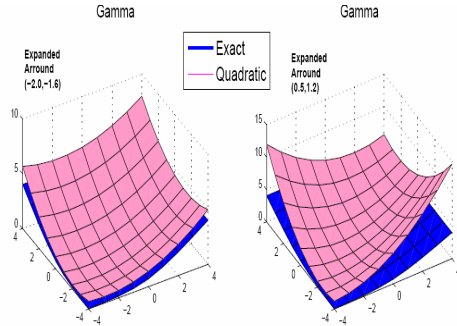
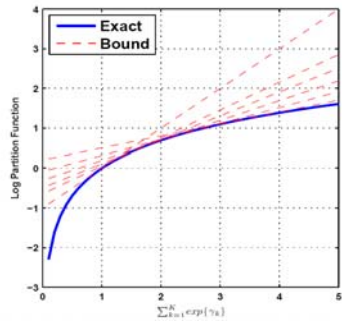
$$\mu_\gamma = \Sigma_\gamma (\Sigma^{-1} \mu + NH \gamma_\lambda + \langle m \rangle - Ng)$$



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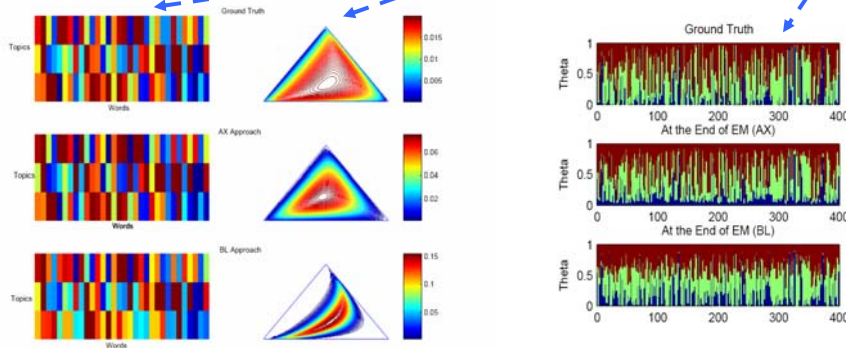
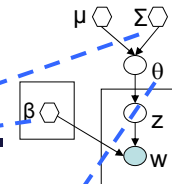
Tangent Approximation



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Test on Synthetic Text



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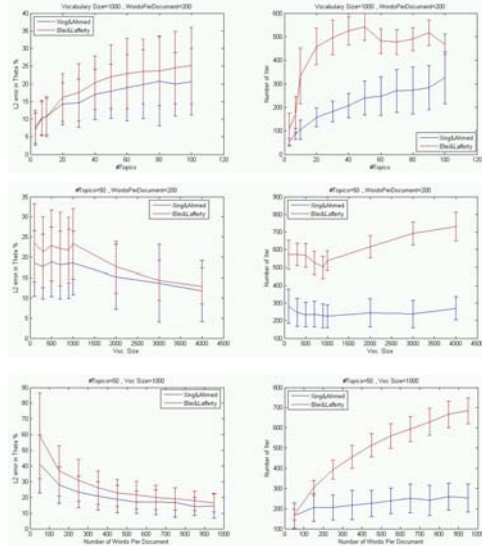
28

Comparison: accuracy and speed



L2 error in topic vector est. and # of iterations

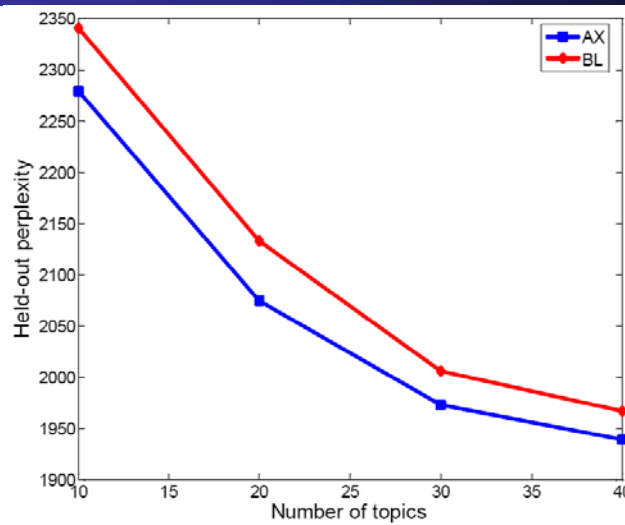
- Varying Num. of Topics
- Varying Voc. Size
- Varying Num. Words Per Document



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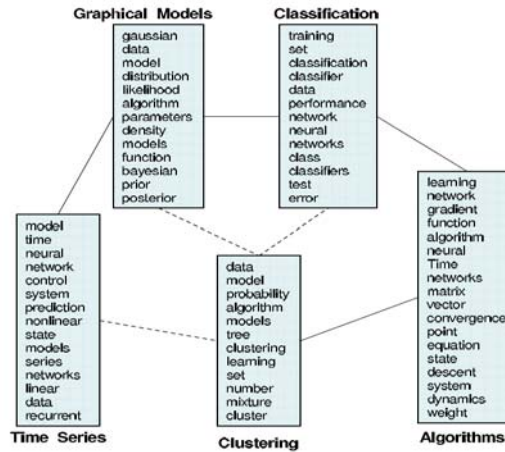
Comparison: perplexity



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Topics and topic graphs



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Result on PNAS collection



- PNAS abstracts from 1997-2002
 - 2500 documents
 - Average of 170 words per document
- Fitted 40-topics model using both approaches
- Use low dimensional representation to predict the abstract category
 - Use SVM classifier
 - 85% for training and 15% for testing

Classification Accuracy

| Category | Doc | BL | AX |
|--------------|-----|------|------|
| Genetics | 21 | 61.9 | 61.9 |
| Biochemistry | 86 | 65.1 | 77.9 |
| Immunology | 24 | 70.8 | 66.6 |
| Biophysics | 15 | 53.3 | 66.6 |
| Total | 146 | 64.3 | 72.6 |

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Method Two:



- Layered Boltzmann machines

E.P. Xing, R. Yan and A. G. Hauptmann,
UAI 2006

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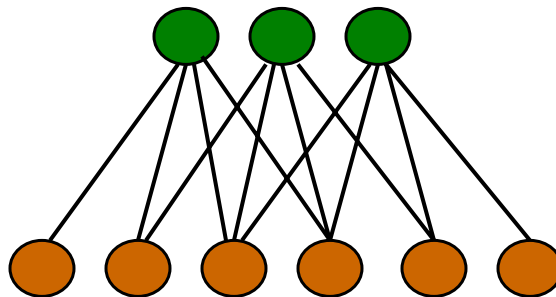
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The Harmonium



hidden units

visible units



Boltzmann machines:

$$p(x, h | \theta) = \exp \left\{ \sum_i \theta_i \phi_i(x_i) + \sum_j \theta_j \phi_j(h_j) + \sum_{i,j} \theta_{i,j} \phi_{i,j}(x_i, h_j) - A(\theta) \right\}$$

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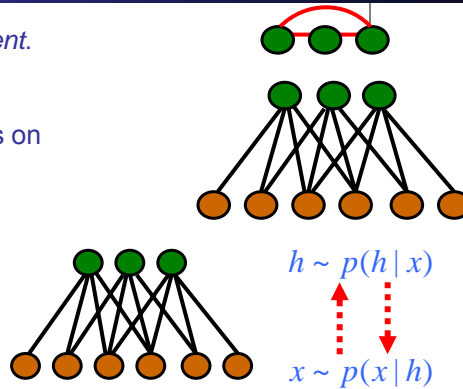
34

Properties of Harmoniums

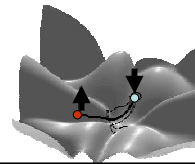
- Factors are marginally *dependent*.
- Factors are conditionally *independent* given observations on the visible nodes.

$$P(\ell | \mathbf{w}) = \prod_i P(\ell_i | \mathbf{w})$$

- Iterative Gibbs sampling.



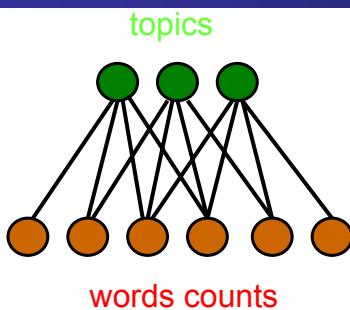
- Learning with contrastive divergence



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A Binomial Word-count Model



$h_j = 3$: topic j has strength 3

$$h_j \in \mathbf{R}, \quad \langle h_j \rangle = \sum_i W_{i,j} x_i$$

$x_i = n$: word i has count n

$$x_i \in \mathbf{I}$$

$$p(\mathbf{h} | \mathbf{x}) = \prod_j \text{Normal}_{h_j} \left[\sum_i \bar{W}_{ij} \bar{x}_i, 1 \right]$$

$$p(\mathbf{x} | \mathbf{h}) = \prod_i \text{Bi}_{x_i} \left[N, \frac{\exp(\alpha_j + \sum_j W_{ij} h_j)}{1 + \exp(\alpha_j + \sum_j W_{ij} h_j)} \right]$$

$$\text{Bi}_{x_i} [N, p] = C_{x_i}^N p^{x_i} (1-p)^{N-x_i} = C_{x_i}^N \left(\frac{p}{1-p} \right)^{x_i} (1-p)^N$$

$$\text{Let } p = \frac{\exp(\alpha_j + \sum_j W_{ij} h_j)}{1 + \exp(\alpha_j + \sum_j W_{ij} h_j)}$$

$$\text{Bi}_{x_i} [N, p] = C_{x_i}^N \frac{(\exp(\alpha_j + \sum_j W_{ij} h_j))^{x_i}}{(1 + \exp(\alpha_j + \sum_j W_{ij} h_j))^N}$$

$$\propto C_{x_i}^N \exp\left\{ (\alpha_j + \sum_j W_{ij} h_j) x_i + A_i \right\}$$

Reduce to softmax when $N=1$!

$$\Rightarrow p(\mathbf{x}) \propto \exp\left\{ \left(\sum_i \alpha_i x_i - \log \Gamma(x_i) - \log \Gamma(N - x_i) \right) + \frac{1}{2} \sum_j \left(\sum_i W_{i,j} x_i \right)^2 \right\}$$

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The Computational Trade-off



Undirected model: Learning is hard, inference is easy.

Directed Model: Learning is "easier", inference is hard.

Example: Document Retrieval.

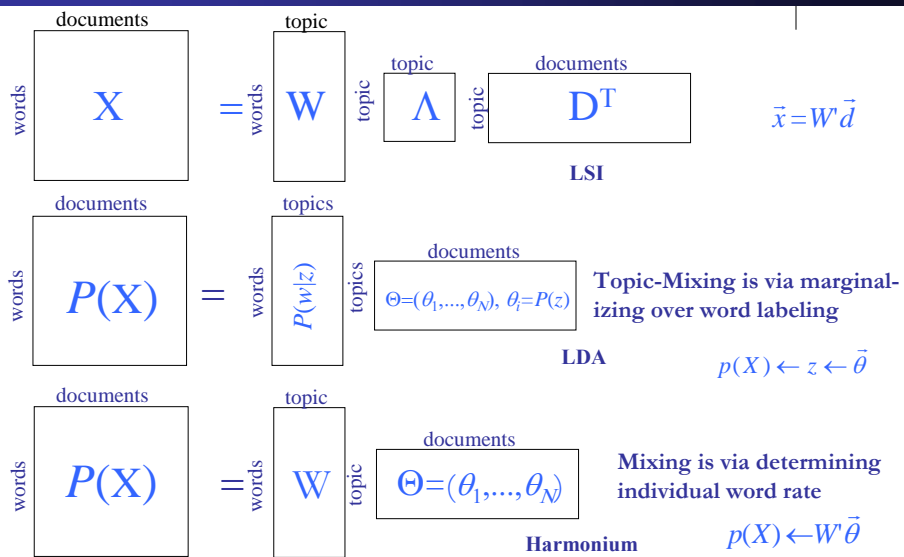


Retrieval is based on comparing (posterior) topic distributions of documents.
 - directed models: inference is slow. Learning is relatively "easy".
 - undirected model: inference is fast. Learning is slow but can be done offline.

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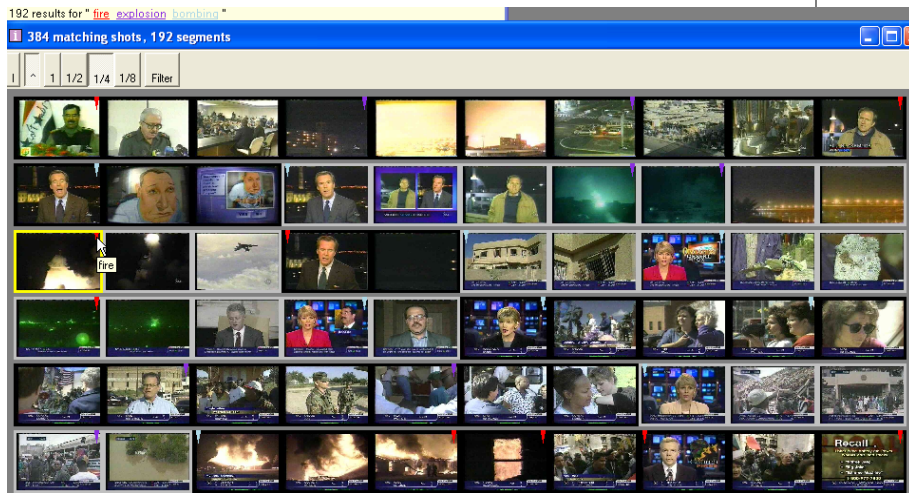
Comparison of model semantics



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Multi-Source Data

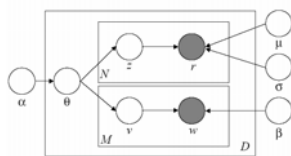


TRECVID 2004 Example Images

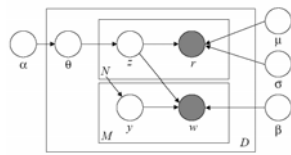
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Inter-Source Associations

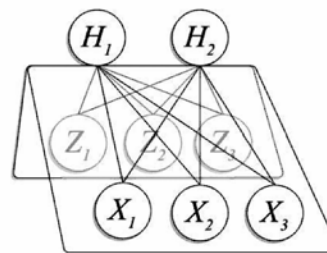


GM-LDA



Co-LDA

DWH

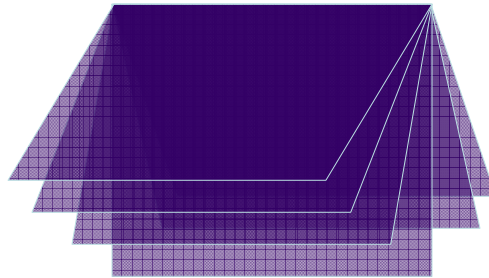


Z and X are marginally dependent (same as GM-LDA)

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Multi-wing Harmoniums



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Learning and Inference



- Maximal likelihood learning based on gradient ascent.

$$\delta\theta_i \propto \langle f_i(x_i) \rangle_{\text{data}} - \langle f_i(x_i) \rangle_p$$

- gradient computation requires model distribution $p(\cdot)$
- $p(\cdot)$ is intractable
- Contrastive Divergence
 - approximate $p(\cdot)$ with Gibbs sampling
- Variational approximation
 - GMF approximation

$$q(\mathbf{x}, \mathbf{z}, \mathbf{h}) = \prod_i q(x_i | v_i) \prod_k q(z_k | \mu_k, \sigma_k) \prod_j q(h_j | \gamma_j)$$

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Inter-source Inference



- GMF approximation to DWH

$$q(\mathbf{x}, \mathbf{z}, \mathbf{h}) = \prod_i q(x_i | N, v_i) \prod_k q(z_k | \mu_k, \sigma_k) \prod_j q(h_j | \gamma_j)$$

- Expected mean value of topic strength:

$$\gamma_j = \sum_i W_{i,j} v_i + \sum_k U_{k,j} \mu_k$$

- Expected mean value of image-feature :






$$\mu_k = \sigma_k^2 \left(\beta_k + \sum_j U_{k,j} \gamma_j \right)$$

- Expected mean count

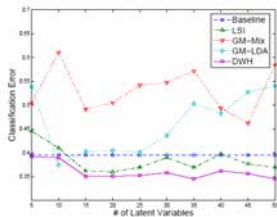
$$N v_i = N \frac{\exp(\alpha_j + \sum_j W_{ij} \gamma_j)}{1 + \exp(\alpha_j + \sum_j W_{ij} \gamma_j)}$$

Examples of Latent Topics

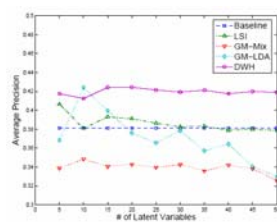


| | |
|-------|---|
| T_1 | storms gulf hawaii low forecast southeast showers  |
| T_2 | rebounds 14 shouting tests guard cut hawks  |
| T_3 | engine flying craft asteroid say hour aerodynamic  |
| T_4 | safe cross red sure dry providing services  |
| T_5 | losing jersey sixth antonio david york orlando  |

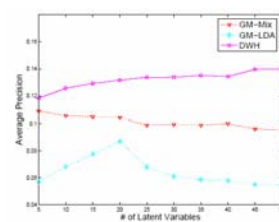
Performance



Classification



Retrieval



Annotation

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This Talk

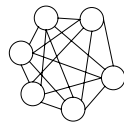


- A graphical model primer
- Two families of probabilistic topics models and approximate inference
 - Bayesian admixture models
 - Random models
- Three applications
 - Learning topic graphs and topic evolution
 - Machine translation
 - Multimedia inference

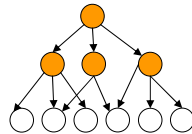
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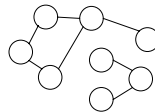
Application 1: How to model topic correlation?



(a) CTM



(b) PAM



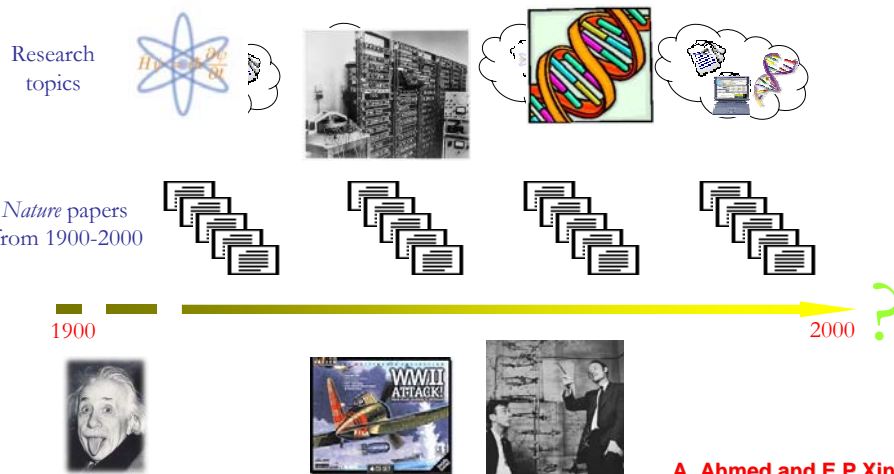
(c) sCTM

A. Ahmed and E.P Xing,
Submitted 2007

Eric Xing

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And topic evolution?

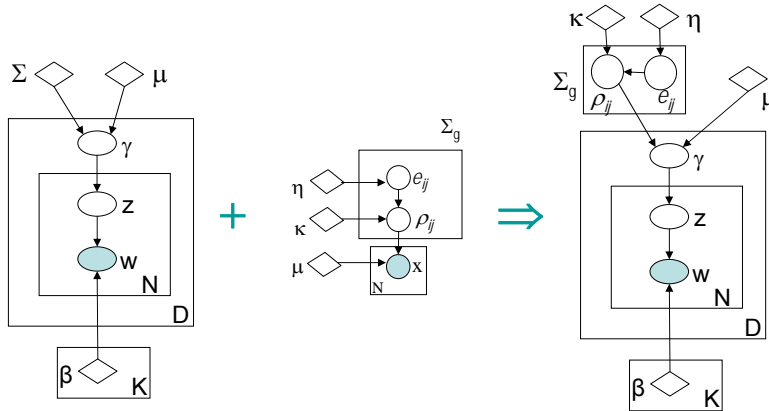


A. Ahmed and E.P Xing,
Submitted 2007

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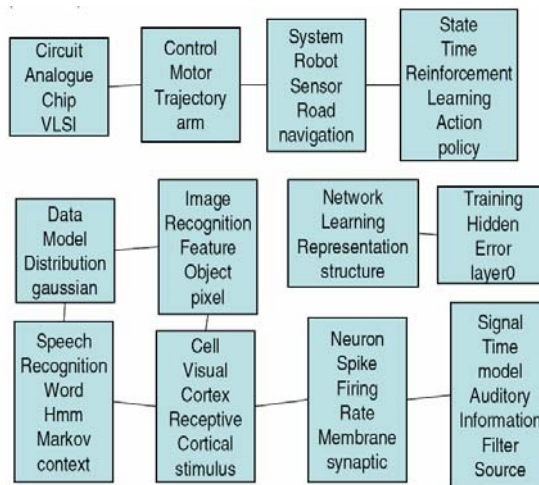
Sparse Correlated Model (SCTM)



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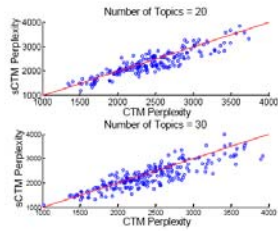
NIPS: Example Network



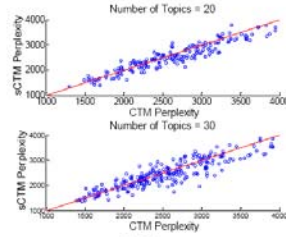
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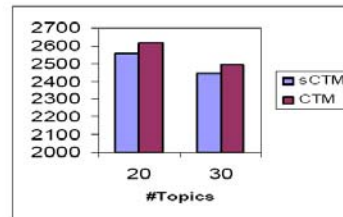
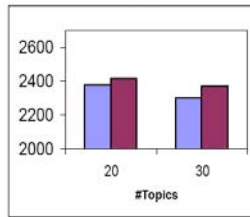
NIPS: Held-out Perplexity



(c)



(d)



How to Model Topic Evolution



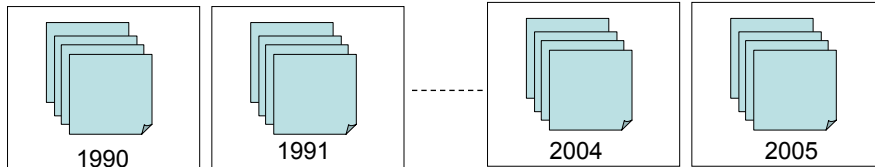
Topic Trends

Topic Keywords

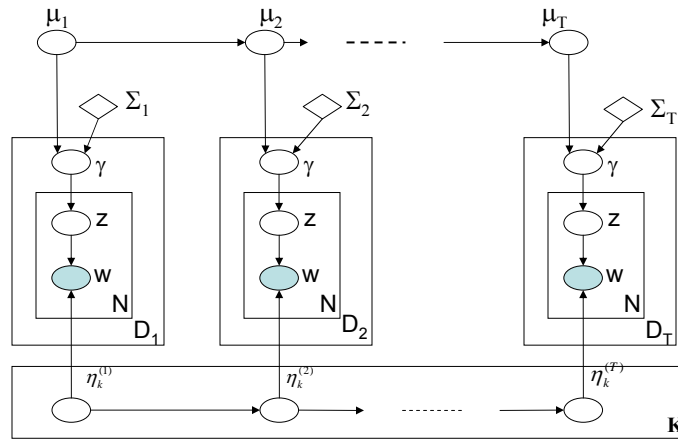
Topic correlations

~~Number of topics~~

The Dynamic Correlated Topic model



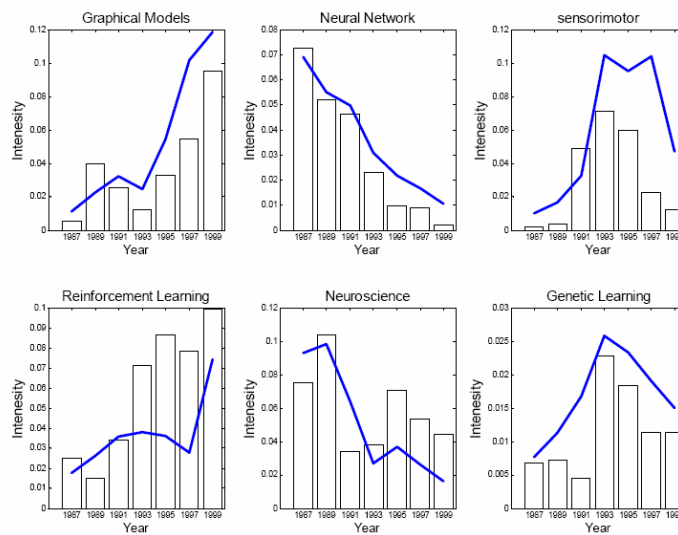
The Dynamic CTM



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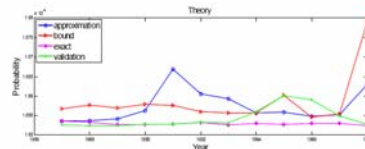
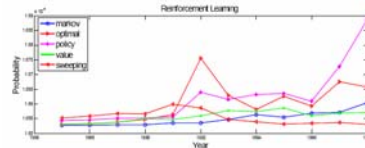
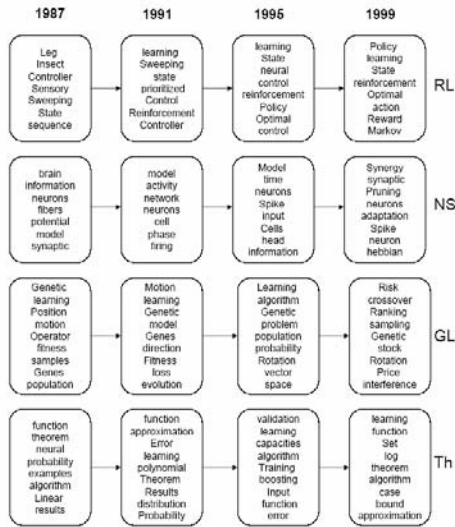
Topic Trends



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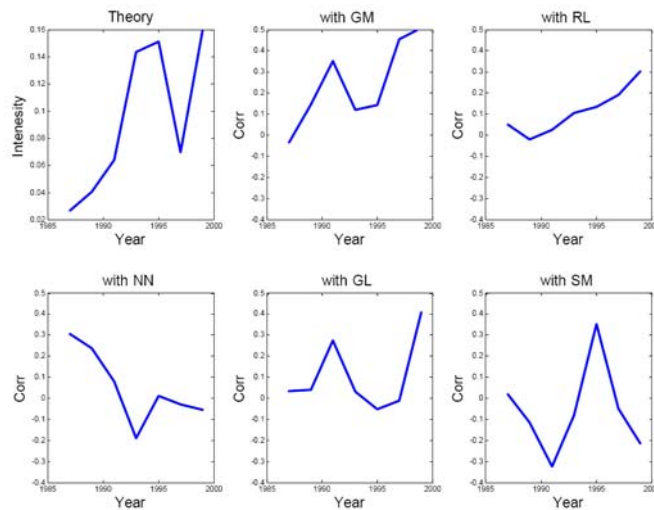
Topic Words over Time



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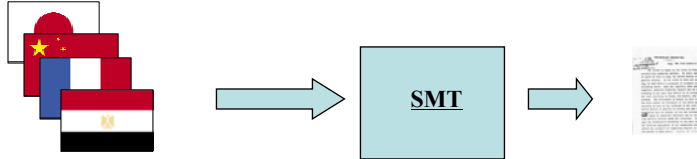
Topic Correlations Over Time



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Application 2: Machine translation



B. Zhao and E.P Xing,
ACL 2006

Eric Xing

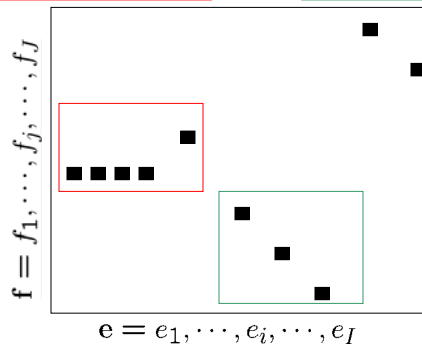
57

Word Alignment



天津 与 俄罗斯 经贸 关系 稳步 发展

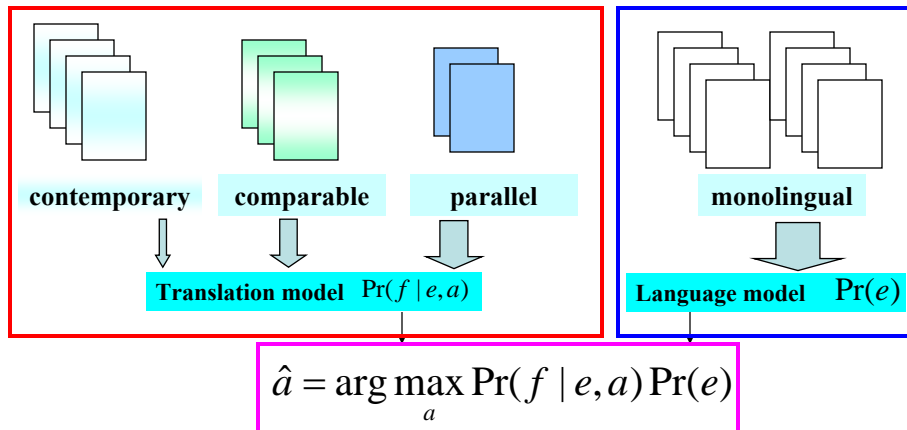
The economy and trade relations between russia and tianjin develop steadily



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The Statistical Formulation

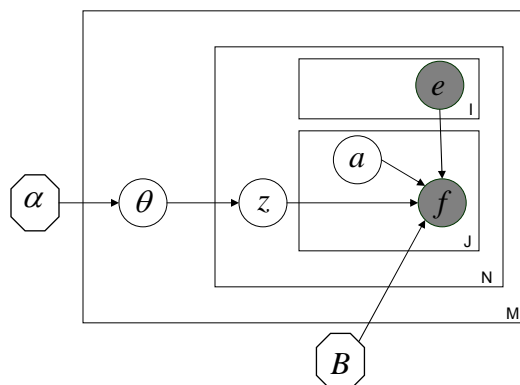


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BiTAM Model-1

- Graphical Model (a language to encode dependencies)

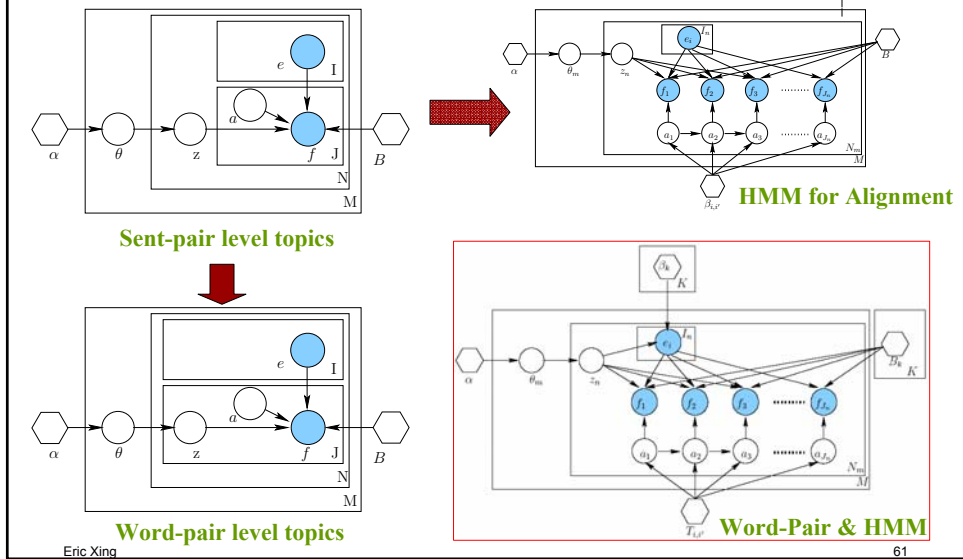


$$p(F | A, E, \alpha, B) = \int_{\theta} p(\theta | \alpha) \prod_{n=1}^N \sum_{z_n} p(z_n | \theta) p(f_n | a_n, e_n, B_{z_n}) d\theta$$

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An upgrade path for BiTAMs



Experiments

- Training data
 - Small: Treebank 316 doc-pairs (133K English words)
 - Large: FBIS-Beijing, Sinorama, XinHuaNews, (15M English words).

| Train | #Doc. | #Sent. | #Tokens | |
|----------|--------|--------|---------|---------|
| | | | English | Chinese |
| Treebank | 316 | 4172 | 133K | 105K |
| FBIS.BJ | 6,111 | 105K | 4.18M | 3.54M |
| Sinorama | 2,373 | 103K | 3.81M | 3.60M |
| XinHua | 19,140 | 115K | 3.85M | 3.93M |
| FOUO | 15,478 | 368K | 13.14M | 11.93M |
| Test | 95 | 627 | 25,500 | 19,726 |

- Word Alignment Accuracy & Translation Quality
 - F-measure
 - BLEU

Topics



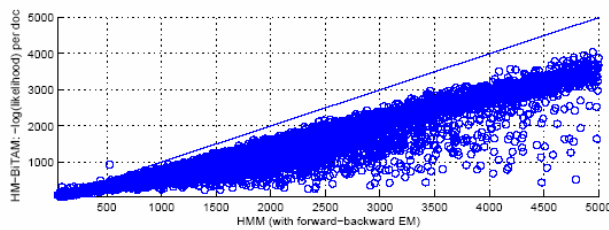
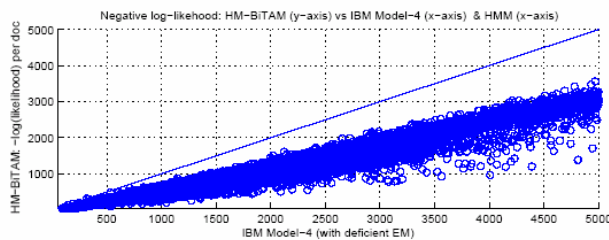
| | |
|----|---|
| T1 | Teams, sports, disabled, games members, people, cause, water, national, handicapped |
| T2 | Shenzhen, singapore, hongkong, stock, national, investment, yuan, options, million, dollar |
| T3 | Chongqing, company, takeover, shenzhen, tianjin, city, national, government, project, companies |
| T4 | Hongkong, trade, export, import, foreign, tech., high, 1998, year, technology |
| T5 | House, construction, government, employee, living, provinces, macau, anhui, yuan |
| T6 | Gas, company, energy, usa, russia, france, chongqing, resource, china, economy, oil |

| | |
|----|--|
| T1 | 人, 残疾, 体育, 事业, 水, 世界, 区, 新华社, 队员, 记者 |
| T2 | 深圳, 深, 新, 元, 有, 股, 香港, 国有, 外资, 新华社 |
| T3 | 国家, 重庆, 市, 区, 厂, 天津, 政府, 项目, 国, 深圳 |
| T4 | 香港, 贸易, 出口, 外资, 合作, 今年, 项目, 利用, 新, 技术 |
| T5 | 住房, 房, 九江, 建设, 澳门, 元, 职工, 目前, 国家, 占, 省 |
| T6 | 公司, 天然气, 两, 国, 美国, 记者, 关系, 俄, 法, 重庆 |

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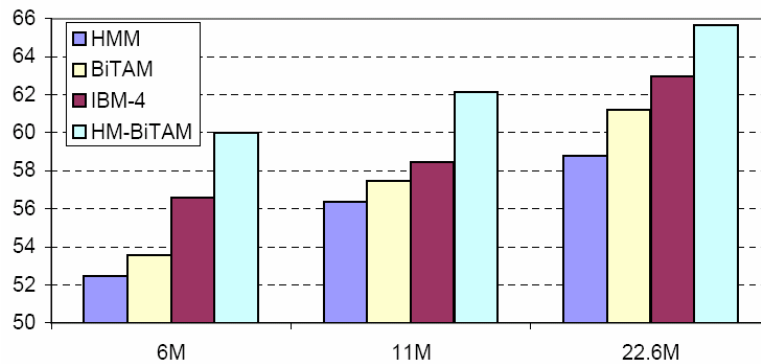
Comparison



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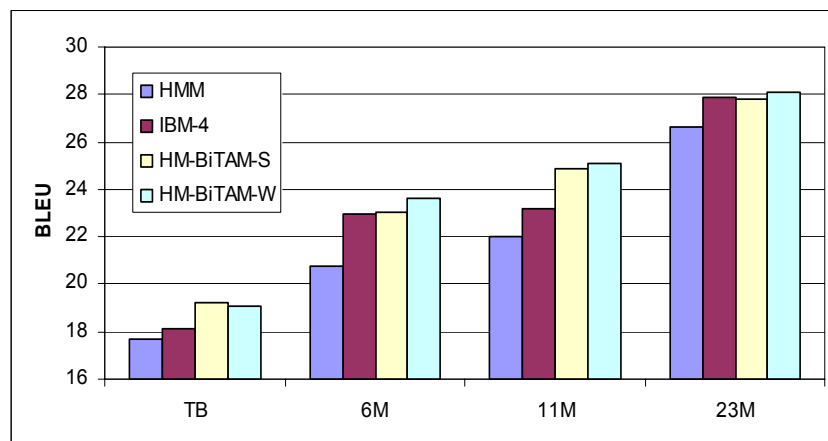
HM-BiTAM versus others



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Translation Evaluations



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Translation Evaluations



| Systems | 1-gram | 2-gram | 3-gram | 4-gram | BLEUr4 |
|--------------|--------------|--------------|--------------|--------------|--------------|
| Hiero Sys. | 73.92 | 40.57 | 23.21 | 13.84 | 30.70 |
| Gale Sys. | 75.63 | 42.71 | 25.00 | 14.30 | 32.78 |
| HM-BiTAM | 76.77 | 42.99 | 25.42 | 14.04 | 33.19 |
| Ground Truth | 76.10 | 43.85 | 26.70 | 15.73 | 34.17 |

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Application 3: video representation/classification



- Video: a **complex, multi-modal** data type for representation and classification
 - Image, text (closed-captions, speech transcript), audio
- **Goal**: classify video segments called **video shots** into semantic categories



anchor



building



meeting



speech

J. Yang, Y. Liu, E. P. Xing and A. Hauptmann,
SDM 2007, **BEST PAPER Award**

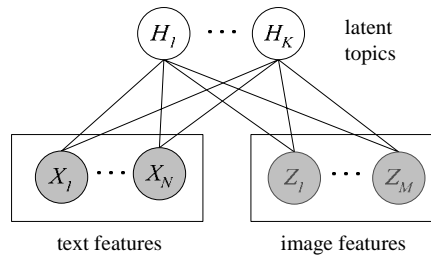
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Harmoniums for Multi-modal Data



- Dual-wing harmoniums (DWH) [Xing et al. 05]
 - modeling bi-modal data: captioned images, video
 - learning hidden topics from two "wings" of observed features



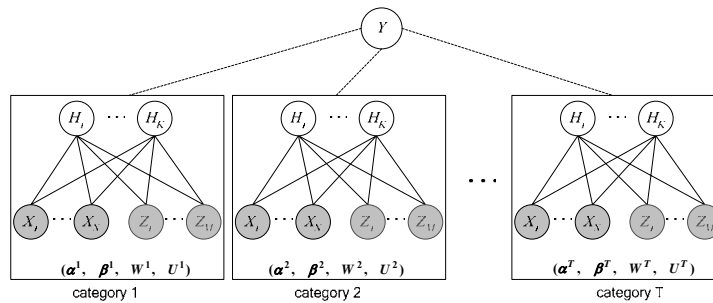
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Mixture-of-Harmoniums (MoH)



- A family of category-specific dual-wing harmoniums



- classification by finding the "best-fitting" harmonium

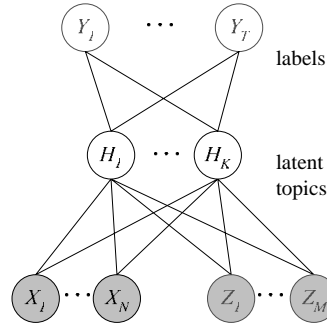
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Hierarchical Harmonium (HH)



- Incorporate category labels as a layer of hidden nodes on top of latent topic nodes



- classification by inference of label nodes

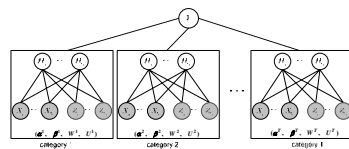
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Semantic Topics by FoH



- Revealing “sub-topics” of each category
- Co-clusters of both text and image features



| | |
|---------|--|
| Topic 1 | |
| | life, call, way, fire, know, thousands, rain, farmers, control |
| Topic 2 | |
| | space, flight, thousands, fifteen, Florida, radar, track, amount |
| Topic 3 | |
| | asteroid, scientists, destroy, miss, destruction, actually, come, course |
| Topic 4 | |
| | rain, control, area, forest, years, fires, large, burning, state, nature |
| Topic 5 | |
| | panic, sized, type, headaches, freedom, love, turning, beautiful |

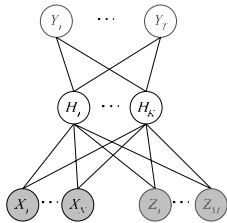
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Semantic Topics by HH





- Reveal the “common topics” of all the data




Topic 1 
news, today, tonight, world, ABC, Jennings, going, people

Topic 2 
team, dollars, money, celebrated, won, buy, best, championship, owner

Topic 3 
look, take, people, California, closer, right, say, back, know, way

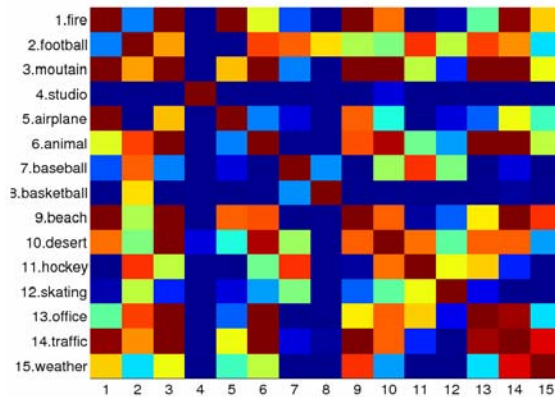
Topic 4 
new, seven, Clinton, two, president, hundred, united, york, today

Topic 5 
evening, white, news, only, world, world, today, sale

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Inter-category relationship



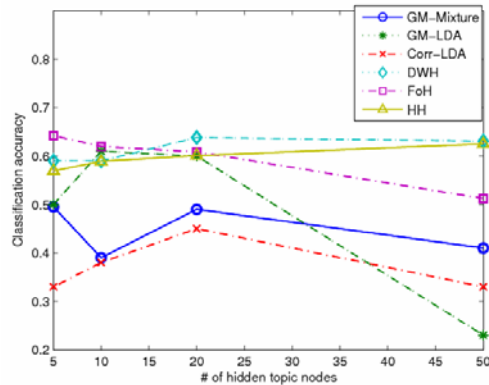
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Classification Accuracy



- Harmonium models outperform directed models (e.g., LDA)



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Conclusion



- GM-based topic models are cool
 - Flexible
 - Modular
 - Interactive
- There are many ways of implementing topic models
 - Directed
 - Undirected
- Efficient Inference/learning algorithms
 - GMF, with Laplace approx. for non-conjugate dist.
 - MCMC
- Many applications
 - ...
 - Word-sense disambiguation
 - Word-net
 - Network inference

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