

# Problem H: Last Digits

**Input:** digits.in

**Output:** digits.out

Exponentiation of one integer by another often produces very large results. In this problem, we will compute a function based on repeated exponentiation, but output only the last  $n$  digits of the result. Doing this efficiently requires careful thought about how to avoid computing the full answer.

Given integers  $b$ ,  $n$ , and  $i$ , we define the function  $f(x)$  recursively by  $f(x) = b^{f(x-1)}$  if  $x > 0$ , and  $f(0)=1$ . Your job is to efficiently compute the last  $n$  decimal digits of  $f(i)$ .

## Input

The input consists of a number of test cases. Each test case starts with the integer  $b$  ( $1 \leq b \leq 100$ ) called the **base**. On the next line is the integer  $i$  ( $1 \leq i \leq 100$ ) called the **iteration count**. And finally, the last line contains the number  $n$  ( $1 \leq n \leq 7$ ), which is the number of decimal digits to output. The input is terminated when  $b = 0$ .

## Output

For each test case, print on one line the last  $n$  digits of  $f(i)$  for the base  $b$  specified. If the result has fewer than  $n$  digits, pad the result with zeroes on the left so that there are exactly  $n$  digits.

## Sample input

```
2
4
7
10
10
6
3
10
7
0
```

## Output for sample input

```
0065536
000000
4195387
```