

Problem 2

Write efficient algorithms for converting (a) an adjacency-list representation of a graph into an adjacency matrix and (b) an adjacency matrix into adjacency lists.

We denote the adjacency list of a vertex u by $Adj-List[u]$, and the adjacency-matrix element for vertices u and v by $Adj-Matrix[u, v]$. The time complexity of both algorithms is $\Theta(V^2)$.

(a) Converting adjacency lists into a matrix.

LISTS-TO-MATRIX(G) \triangleright G is represented by adjacency lists

```
for each  $u \in V[G]$ 
  do for each  $v \in V[G]$ 
    do  $Adj-Matrix[u, v] \leftarrow 0$ 
for each  $u \in V[G]$ 
  do for each  $v \in Adj-List[u]$ 
    do  $Adj-Matrix[u, v] \leftarrow 1$ 
```

(b) Converting an adjacency matrix into lists.

MATRIX-TO-LISTS(G) \triangleright G is represented by an adjacency matrix

```
for each  $u \in V[G]$ 
  do initialize an empty list  $Adj-List[u]$ 
for each  $u \in V[G]$ 
  do for each  $v \in V[G]$ 
    do if  $Adj-Matrix[u, v] = 1$ 
      then add  $v$  to  $Adj-List[u]$ 
```

Problem 3

Using Figure 23.3 in the textbook as a model, illustrate the steps of breadth-first search on the directed graph of Figure 23.2(a), with vertex 3 as the source.

The order of painting the vertices is as follows:

gray 3	black 5
gray 5	black 6
gray 6	gray 2
black 3	black 4
gray 4	black 2