Constructive Logic (15-317), Spring 2023 Recitation 1

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January 24, 2023

1 Dcheck

In this class, we will be using Dcheck to type out derivations. Therefore, we will spend part of this recitation familiarizing everyone with this system.

Here are some useful links related to Dcheck.

- The documentation for Dcheck is http://www.cs.cmu.edu/~crary/dcheck/dcheck.pdf
- An example file for Dcheck is http://www.cs.cmu.edu/~crary/dcheck/example.deriv

The main commands that you will need for Dcheck are below. All these commands are executed on the Andrew machine.

• Run the sanity checks. ~ crary/bin/dsanity <filename>

This will check for basic syntactic errors. However, the correctness of your derivation will not be checked.

• Visualize your program. ~crary/bin/dvis <filename>

Running the visualizer will not run the sanity check, so it is recommended that you run the sanity check before the visualizer.

Dcheck syntax can be found in the documentation. In this recitation we will demonstrate how to convert natural deduction derivations into Dcheck.

Task 1. Write the derivation for the following judgment in Dcheck. You can find the corresponding derivations in the lecture notes¹.

$$((A \lor B) \supset C) \supset ((A \supset C) \land (B \supset C))$$
 true

¹http://www.cs.cmu.edu/~fp/courses/15317-s23/lectures/02-natded.pdf

2 Harmony

A connective is harmonious if its elimination rules are neither too strong nor too weak in relation to its introduction rules. The first property relates to local soundness, and the second property relates to local completeness.

Proving local soundness is usually done by local reduction. The main idea is to simplify a proof, or demonstrate a more direct proof.

Proving local completeness is usually done by local expansion. The main idea is to expand a proof into a proof which ends with an introduction rule.

Task 2. Consider the following new connective o.

$$\frac{A \text{ true}}{A \circ B \text{ true}} \circ I_1 \qquad \frac{B \text{ true}}{A \circ B \text{ true}} \circ I_2 \qquad \frac{A \circ B \text{ true}}{C \text{ true}} C \text{ true} C \text{ true} \circ E_1^u \qquad \frac{A \circ B \text{ true}}{C \text{ true}} \circ E_2^v$$

Answer the following questions.

- a. If we want to show \circ is locally sound, how many local reductions should we provide?
- b. Is this connective locally sound? If so, provide the local reductions. If not, provide a derivation to show that this connective can prove judgments that are not provable, for instance $\perp true$.
- c. If we want to show \circ is locally complete, how many local expansions should we provide?
- d. Is this connective locally complete? If so, provide the local expansion. If not, briefly explain why local expansion fails.