

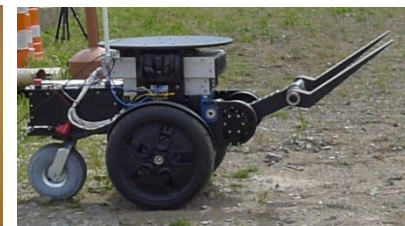
*16-350 Spring'24*  
*Planning Techniques for Robotics*

*Introduction;*  
*What is Planning for Robotics?*

*Maxim Likhachev*  
*Robotics Institute*  
*Carnegie Mellon University*

# About Me

- My Research Interests:
  - Planning, Decision-making, Learning
  - Applications: planning for complex robotic systems including aerial and ground robots, manipulation platforms, small teams of heterogeneous robots
- More info: <http://www.cs.cmu.edu/~maxim>
- Search-based Planning Lab: <http://www.sbpl.net>



# About Me

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- Also, currently split between CMU and [Waymo](#), where I'm heavily involved in planning for self-driving vehicles

# Class Logistics

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- Instructor:

Maxim Likhachev – [maxim@cs.cmu.edu](mailto:maxim@cs.cmu.edu)

- TA:

Itamar Mishani – [imishani@andrew.cmu.edu](mailto:imishani@andrew.cmu.edu)

Siddharth Saha - [ssaha3@cs.cmu.edu](mailto:ssaha3@cs.cmu.edu)

- Website:

<http://www.cs.cmu.edu/~maxim/classes/robotplanning>

- Piazza for Announcements and Questions:

You should have received an email

# Class Logistics

- Books (optional):
  - Planning Algorithms *by Steven M. LaValle*
  - Heuristic Search, Theory and Applications *by Stefan Edelkamp and Stefan Schroedl*
  - Principles of Robot Motion, Theory, Algorithms, and Implementations *by Howie Choset, Kevin M. Lynch, Seth Hutchinson, George A. Kantor, Wolfram Burgard, Lydia E. Kavraki and Sebastian Thrun*
  - Artificial Intelligence: A Modern Approach *by Stuart Russell and Peter Norvig*

# Class Prerequisites

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- Knowledge of programming (e.g., C, C++)
- Knowledge of data structures
- Some prior exposure to robotics (e.g., Intro to Robotics class) is preferred

# Class Objectives

- Understand and learn how to implement most popular planning algorithms in robotics including heuristic search-based planning algorithms, sampling-based planning algorithms, task planning, planning under uncertainty and multi-robot planning
- Learn basic principles behind the design of planning representations
- Understand core theoretical principles that many planning algorithms rely on and learn how to analyze theoretical properties of the algorithms
- Understand the challenges and basic approaches to interleaving planning and execution in robotic systems
- Learn common uses of planning in robotics

# Tentative Class Schedule

## TENTATIVE SCHEDULE FOR Robot Planning CLASS Spring 2024

Date	Day	Topic	HW out	HW due
17-Jan	Wed	Introduction; What is Planning?		
22-Jan	Mon	planning representations: explicit vs. implicit graphs, skeletonization-, grid- and lattice-based graphs		
24-Jan	Wed	planning representations: explicit vs. implicit graphs, skeletonization-, grid- and lattice-based graphs (cont'd)		
29-Jan	Mon	search algorithms: Uninformed A*	HW1	
31-Jan	Wed	search algorithms: A*, Multi-goal A*		
5-Feb	Mon	heuristics, weighted A*, Backward A*		
7-Feb	Wed	interleaving planning and execution: Anytime heuristic search		
12-Feb	Mon	TBD		
14-Feb	Wed	interleaving planing and execution: Freespace assumption, Incremental heuristic search		HW1
19-Feb	Mon	interleaving planning and execution: Limited Horizon search, LRTA*		
21-Feb	Wed	case study: planning for autonomous driving	HW2	
26-Feb	Mon	planning representations: PRM for continuous spaces		
28-Feb	Wed	planning representations/search algorithms: RRT, RRT-Connect, RRT*		
4-Mar	Mon	SPRING BREAK; NO CLASSES		
6-Mar	Wed	SPRING BREAK; NO CLASSES		
11-Mar	Mon	planning representations/search algorithms: RRT, RRT-Connect, RRT* (cont'd)		
13-Mar	Wed	case study: planning for mobile manipulation and articulated robots		HW2
18-Mar	Mon	search algorithms: Markov Property, dependent vs. independent variables		
20-Mar	Wed	final project proposal presentations		
25-Mar	Mon	case study: planning for exploration and surveillance tasks		
27-Mar	Wed	planning representations: state-space vs. symbolic representation for task planning	HW3	
1-Apr	Mon	search algorithms: symbolic task planning algorithms		
3-Apr	Wed	planning under uncertainty: Minimax formulation		
8-Apr	Mon	planning under uncertainty: Expected Cost Minimization formulation		HW3
10-Apr	Wed	planning under uncertainty: Solving Markov Decision Processes		
15-Apr	Mon	exam		
17-Apr	Wed	multi-robot planning		
22-Apr	Mon	multi-robot planning		
24-Apr	Wed	final project presentations		



# Class Structure

- Grading

Three homeworks	33%
Exam	20%
In-class pop quizzes	10%
Final project	32%
Participation	5%

- Exam is tentatively scheduled for April 15 (no final exam)
- Late Policy
  - 3 free late days
  - No late days may be used for the final project!
  - Each additional late day incurs 10% penalty with 50% being the upper limit (grade of 90 becomes 81 for one additional late day)

# Three Homeworks + Final Project

- All homeworks are individual (no groups)
- Final project are in groups of 2-3 students
- Homeworks are programming assignments
- Final project is a research-like project. For example:
  - to develop a planner for a robot planning problem of your choice
  - to extend an existing or develop a new planning algorithm
  - to prove novel properties of a planning algorithm
  - Get a feel for doing research: Individual meetings with groups,  
Two class presentations (initial idea and final)

# Three Homeworks + Final Project

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- Homework assignments for Masters students will have additional scope
- Undergraduate students will have an option to tackle this additional scope and receive bonus points

# What is Planning?

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- According to Wikipedia: *“Planning is the process of thinking about an organizing the activities required to achieve a desired goal.”*

# What is Planning for Robotics?

- According to Wikipedia: *“Planning is the process of thinking about an organizing the activities required to achieve a desired goal.”*

- **Given**

- model (states and actions) of the robot(s)  $M^R = \langle S^R, A^R \rangle$
- a model of the world  $M^W$
- current state of the robot  $s_{current}^R$
- current state of the world  $s_{current}^W$
- cost function  $C$  of robot actions
- desired set of states for robot and world  $G$

- **Compute a plan  $\pi$  that**

- prescribes a set of actions  $a_1, \dots, a_K$  in  $A^R$  the robot should execute
- reaches one of the desired states in  $G$
- (preferably) minimizes the cumulative cost of executing actions  $a_1, \dots, a_K$

# Example

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Planning for omnidirectional robot:

What is  $M^R$ ?

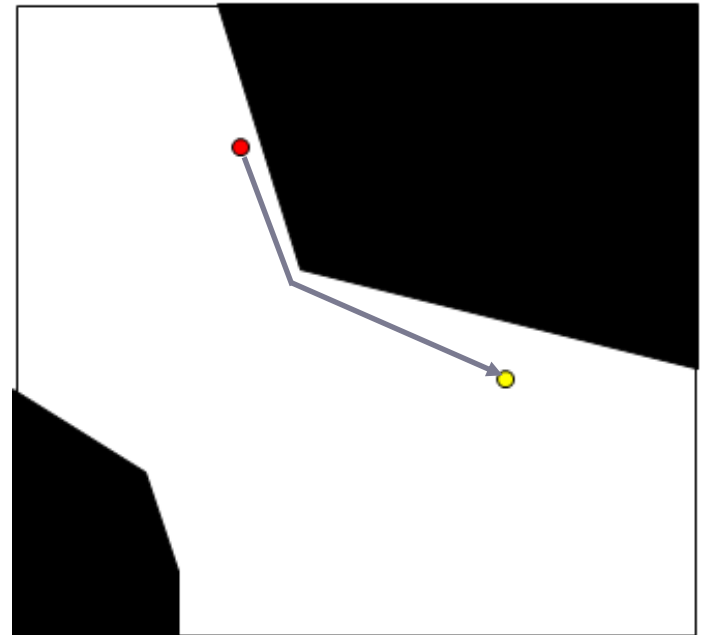
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What is  $s_{current}^R$ ?

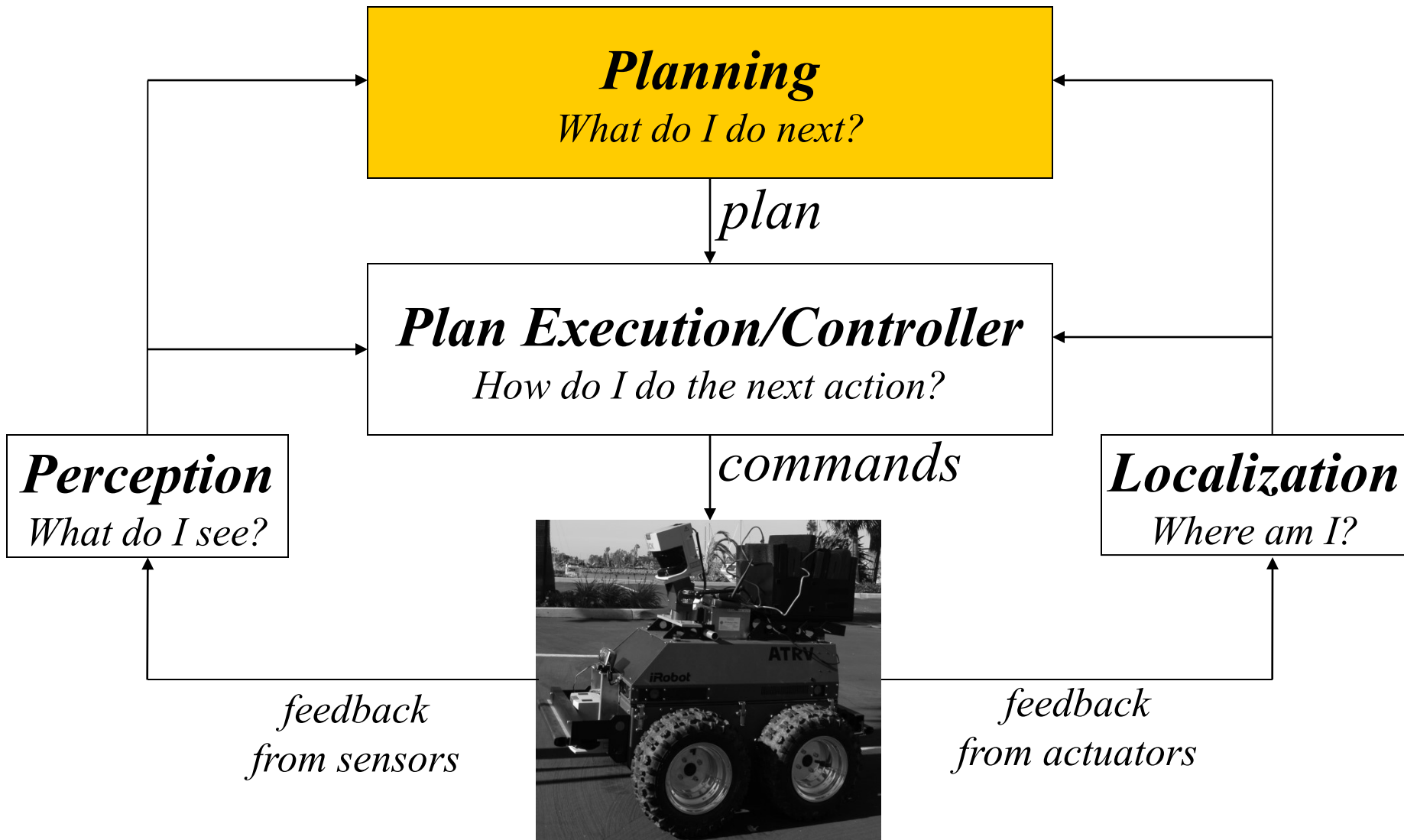
What is  $s_{current}^W$ ?

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# Planning within a Typical Autonomy Architecture



# Few More Examples

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Planning for omnidirectional drone:

What is  $M^R$ ?

What is  $M^W$ ?

What is  $s_{current}^R$ ?

What is  $s_{current}^W$ ?

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MacAllister et al., 2013



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Planning for autonomous navigation:

*What is  $M^R$ ?*

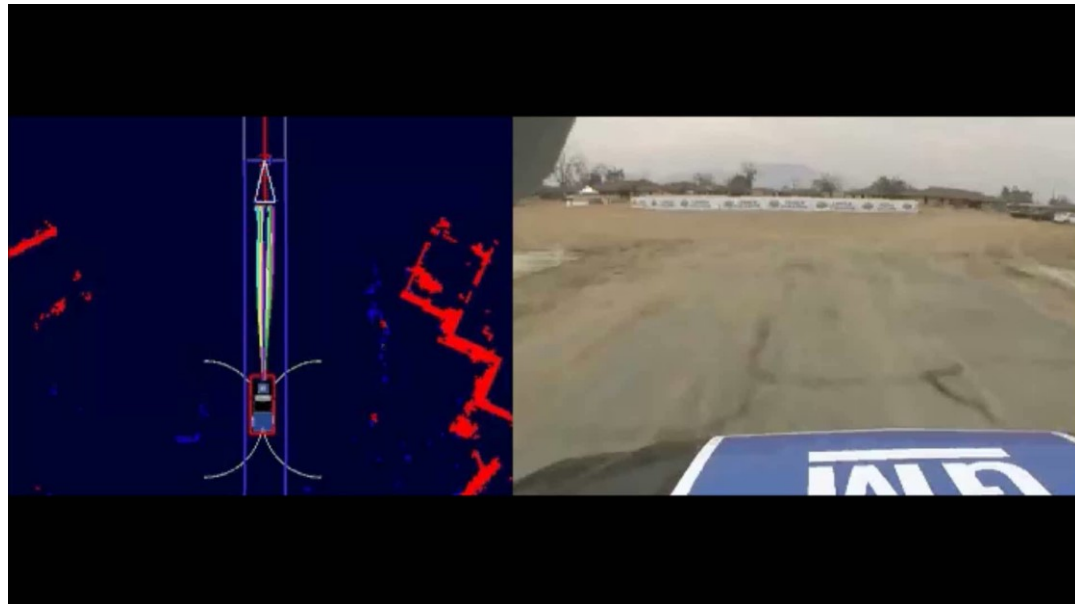
*What is  $M^W$ ?*

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*Likhachev & Ferguson, '09; part of Tartanracing team from CMU for the Urban Challenge 2007 race*

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Planning for autonomous flight among people :

Narayanan et al., 2012

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Planning for a mobile manipulator robot opening a door:

Gray et al., 2013

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Planning for a mobile manipulator robot assembling a birdcage: Cohen et al., 2015

What is  $M^R$ ?

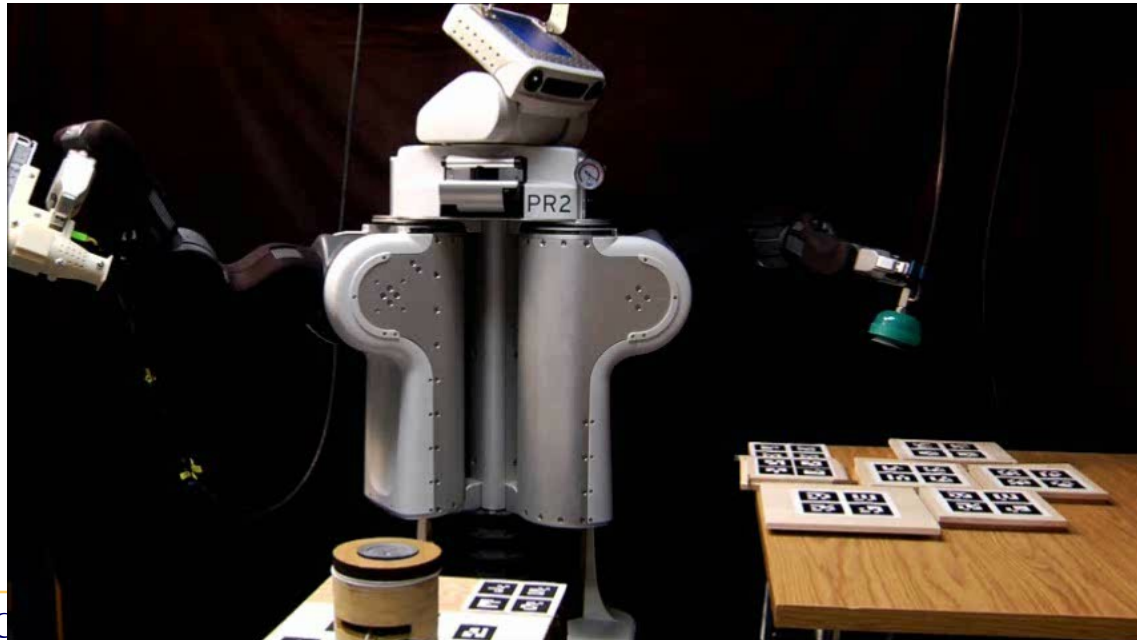
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Planning for a mobile manipulator unloading a truck:

What is  $M^R$ ?

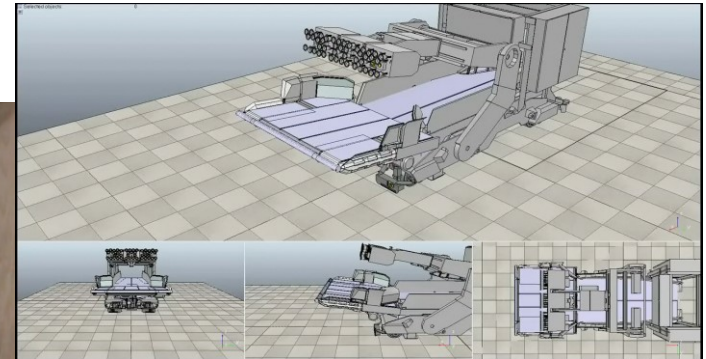
What is  $M^W$ ?

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# Assuming Infinite Computational Resources...

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*Where does Planning break?*

# Assuming Infinite Computational Resources...

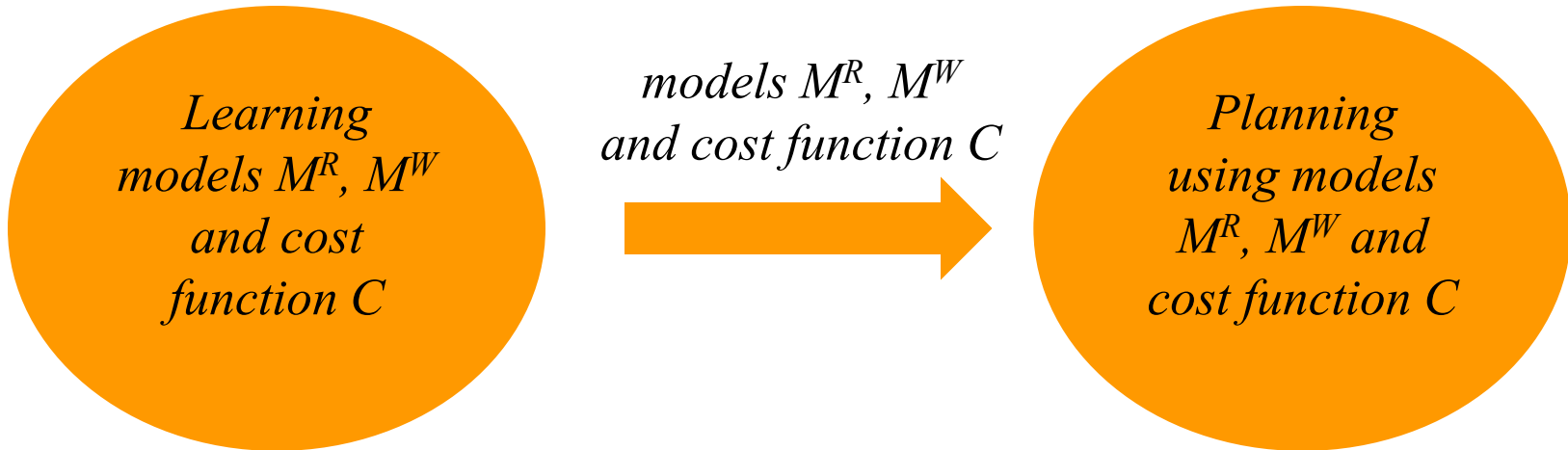
*Where does Planning break?*

*Reliance on the knowledge/accuracy of the model!*

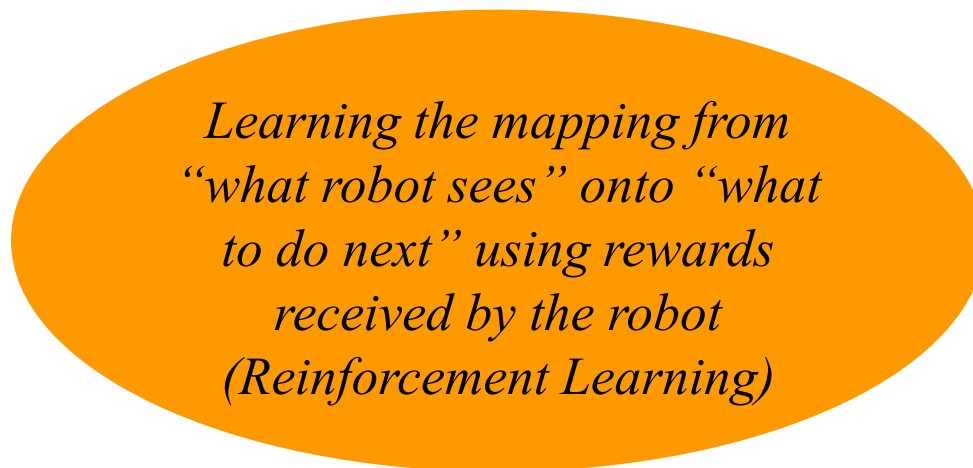
*Role of Learning in Planning?*

# Planning vs. Learning

## *Model-based approach*

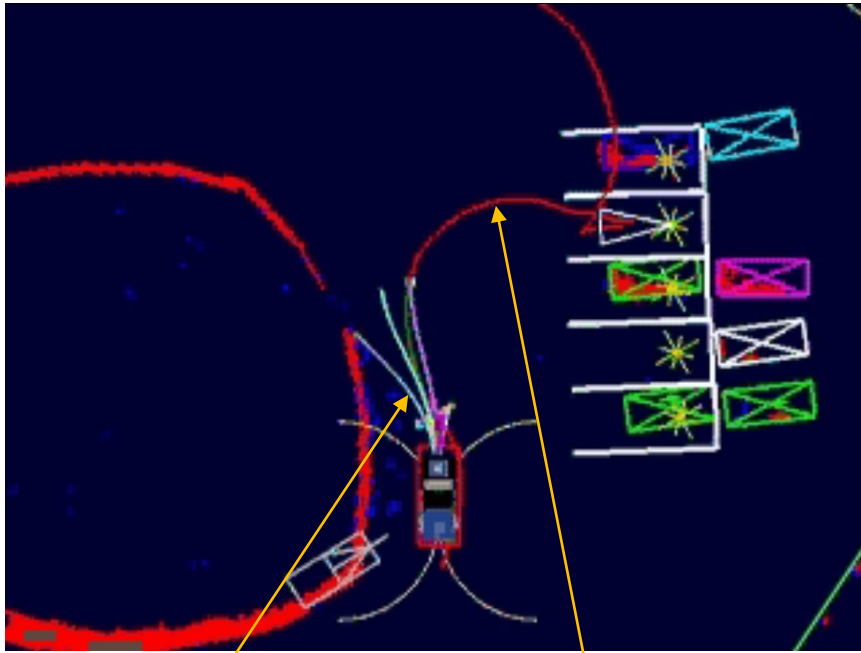


## *Model-free approach*



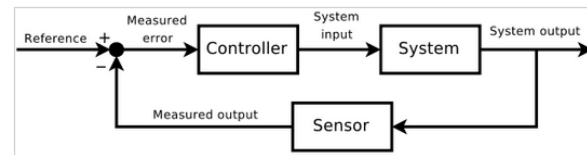


# Planning vs. Trajectory Following vs. Control

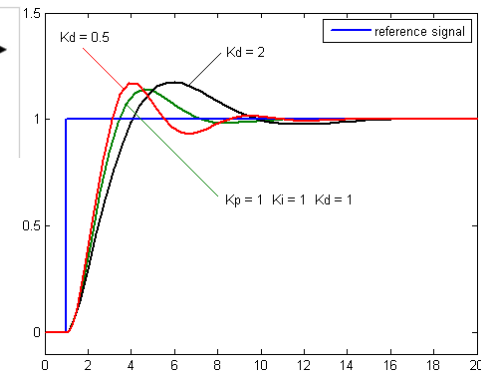


*local planning  
(trajectory following)*

*global planning*



*controller*



*Images from wikipedia*

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Questions about the class?