## 10-423/623: Generative Al Lecture 5 – Vision Transformers

Henry Chai & Matt Gormley 9/11/24

#### Front Matter

• Announcements:

- HW1 released 9/9, due 9/23 at 11:59 PM
  - Recitation on 9/13 (this Friday) will be on HW1 topics

Convolutional Neural Networks

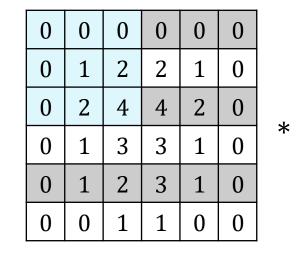
- Neural networks are frequently applied to inputs with some inherent spatial structure, e.g., images
- Idea: use the first few layers to identify relevant macrofeatures, e.g., edges
- Insight: for spatially-structured inputs, many useful macro-features are shift or location-invariant, e.g., an edge in the upper left corner of a picture looks like an edge in the center
- Strategy: learn a *filter* for macro-feature detection in a small window and apply it over the entire image

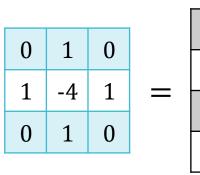
- Images can be represented as matrices: each element corresponds to a pixel and its value is the intensity
- A filter is just a small matrix that is convolved with same-sized sections of the image matrix

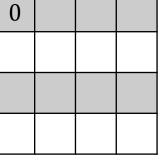
0	0	0	0	0	0	
0	1	2	2	1	0	
0	2	4	4	2	0	
0	1	3	3	1	0	*
0	1	2	3	1	0	
0	0	1	1	0	0	

0	1	0			
1	-4	1			
0	1	0			

- Images can be represented as matrices: each element corresponds to a pixel and its value is the intensity
- A filter is just a small matrix that is convolved with same-sized sections of the image matrix



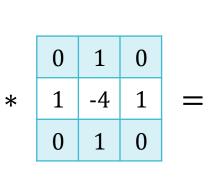


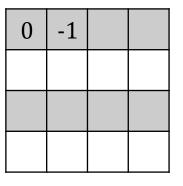


(0\*0) + (0\*1) + (0\*0) + (0\*1) + (1\*-4)+ (2\*1) + (0\*0) + (2\*1) + (4\*0) = 0

- Images can be represented as matrices: each element corresponds to a pixel and its value is the intensity
- A filter is just a small matrix that is convolved with same-sized sections of the image matrix

0	0	0	0	0	0	
0	1	2	2	1	0	
0	2	4	4	2	0	
0	1	3	3	1	0	
0	1	2	3	1	0	
0	0	1	1	0	0	





(0 \* 0) + (0 \* 1) + (0 \* 0) + (1 \* 1) + (2 \* -4)+ (2 \* 1) + (2 \* 0) + (4 \* 1) + (4 \* 0) = -1

- Images can be represented as matrices: each element corresponds to a pixel and its value is the intensity
- A filter is just a small matrix that is convolved with same-sized sections of the image matrix

0	0	0	0	0	0	
0	1	2	2	1	0	
0	2	4	4	2	0	- No
0	1	3	3	1	0	*
0	1	2	3	1	0	
0	0	1	1	0	0	

0101-41010

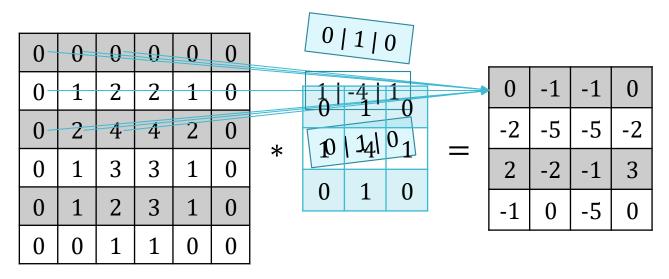
0	-1	-1	0
-2	-5	-5	-2
2	-2	-1	3
-1	0	-5	0

Operation	Kernel ω	Image result g(x,y)
Identity	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
	$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 0 & 0 \\ -1 & 0 & 1 \end{bmatrix}$	
Edge detection	$\begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$	
	$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$	

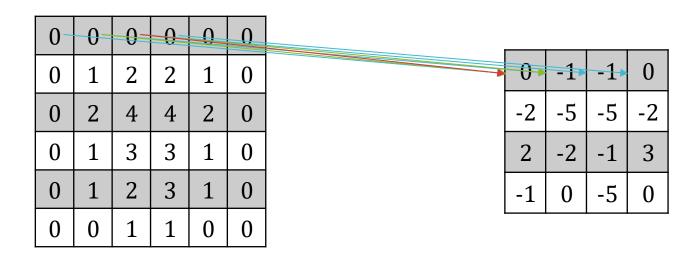
## More Filters

Operation	Kernel ω	Image result g(x,y)
Identity	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
Sharpen	$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$	
<b>Box blur</b> (normalized)	$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$	

- Images can be represented as matrices: each element corresponds to a pixel and its value is the intensity
- A filter is just a small matrix that is convolved with same-sized sections of the image matrix



- Convolutions can be represented by a feed forward neural network where:
  - Nodes in the input layer are only connected to some nodes in the next layer but not all nodes.
  - 2. Many of the weights have the same value.



- Many fewer weights than a fully connected layer!
- Convolution weights are learned using gradient descent/ backpropagation, not prespecified

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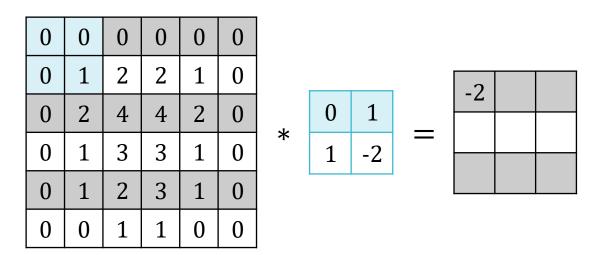
Convolutional Filters: Padding

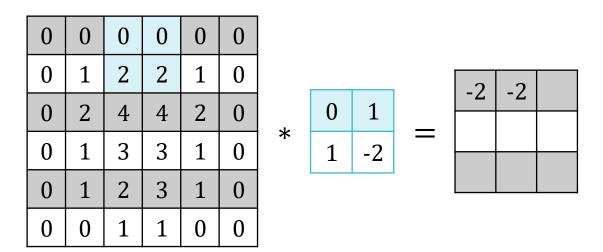
- What if relevant features exist at the border of our image?
- Add zeros around the image to allow for the filter to be applied "everywhere" e.g. a *padding* of 1 with a 3x3 filter preserves image size and allows every pixel to be the center

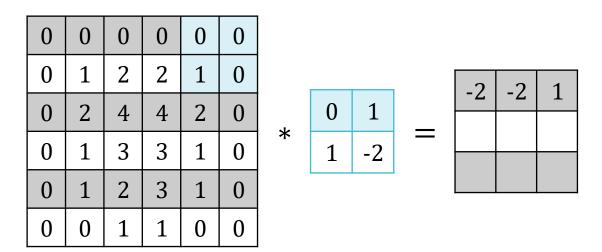
0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	
0	0	1	2	2	1	0	0	
0	0	2	4	4	2	0	0	
0	0	1	3	3	1	0	0	
0	0	1	2	3	1	0	0	
0	0	0	1	1	0	0	0	
0	0	0	0	0	0	0	0	

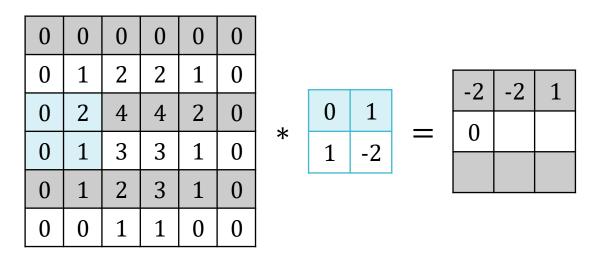
\* 0 1 0 \* 1 -4 1 0 1 0

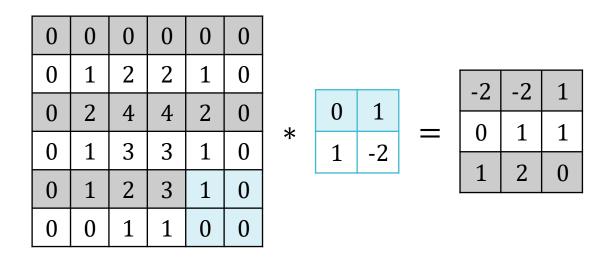
0	1	2	2	1	0
1	0	-1	-1	0	1
2	-2	-5	-5	-2	2
1	2	-2	-1	3	1
1	-1	0	-5	0	1
0	2	-1	0	2	0







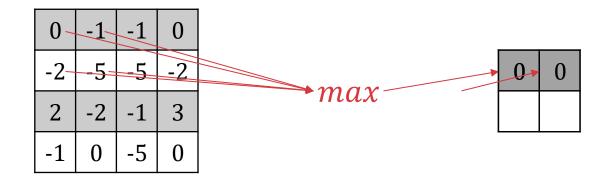




- Reduces the dimensionality of the input to subsequent layers and thus, the number of weights to be learned
- Many relevant macro-features will tend to span large portions of the image, so taking strides with the convolution tends not to miss out on too much

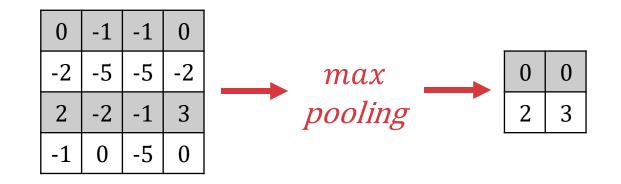
#### Downsampling: Pooling

• Combine multiple adjacent nodes into a single node

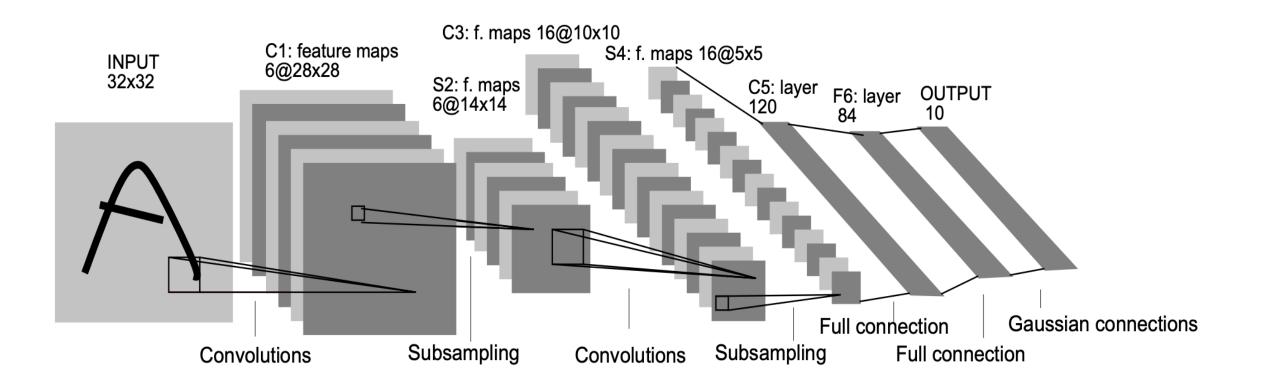


### Downsampling: Pooling

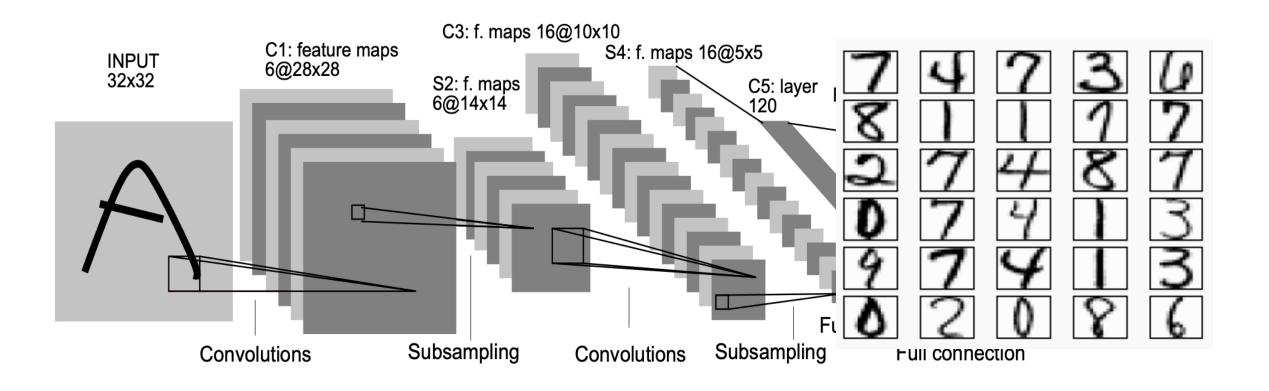
Combine multiple adjacent nodes into a single node



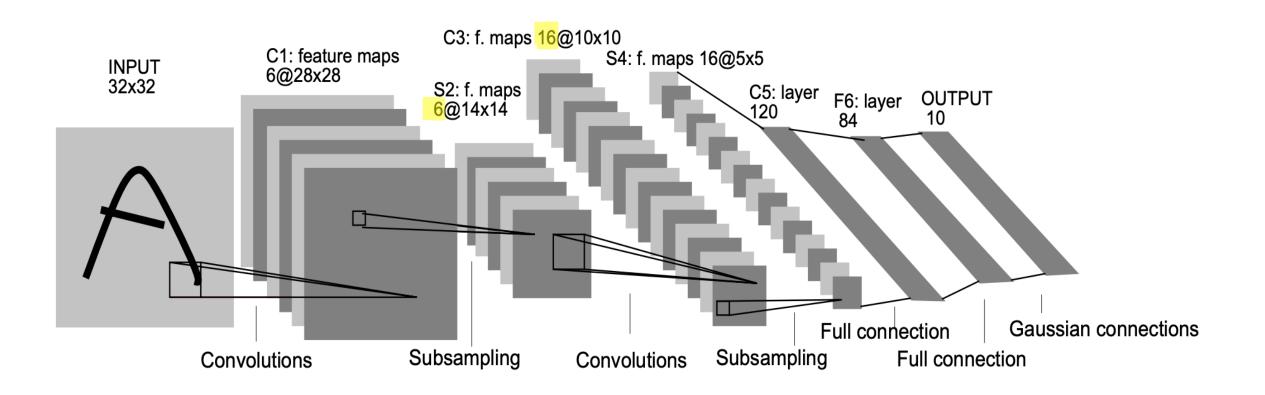
- Reduces the dimensionality of the input to subsequent layers and thus, the number of weights to be learned
  - Protects the network from (slightly) noisy inputs



## LeNet (LeCun et al., 1998)



- One of the earliest, most famous deep learning models achieved remarkable performance at handwritten digit recognition (< 1% test error rate on MNIST)
- Used sigmoid (or logistic) activation functions between layers and mean-pooling, both of which are pretty uncommon in modern architectures



## Wait how did we go from 6 to 16?



## Channels

A																		
	4	1	2	16	3	6	5	2	6	14	15	8	4	6	8	9	5	3
	1	7	5	8	19	27	26	3	6	8	4	9	16	5	2	8	2	1
	5	2	5	12	17	8	0	15	24	6	1	8	5	2	14	11	7	8
	0	4	9	9	6	11	7	4	9	5	24	17	15	2	5	0	9	8

• An image can be represented as the sum of red, green and blue pixel intensities

• Each color corresponds to a *channel* 

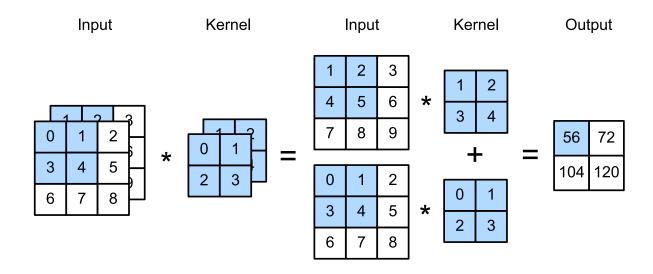


Example:  $3 \times 4 \times 6$  tensor

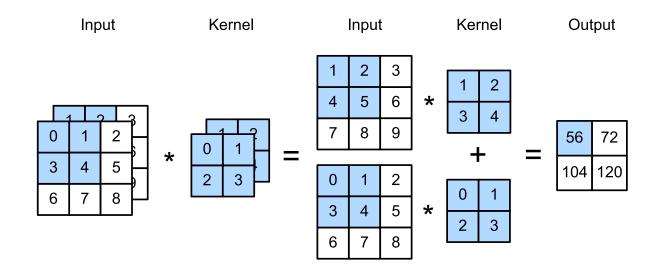
4	1	1 2		16		3			6							
1	5		2		(	6	14			15			8			
5	26	;	4			6			8		9		5		3	
0	0		16		;	5		2		8			2		1	
	7			5		2		14			11		7		8	
				15		2			5		0		9		8	_

• An image can be represented as a *tensor* or multidimensional array

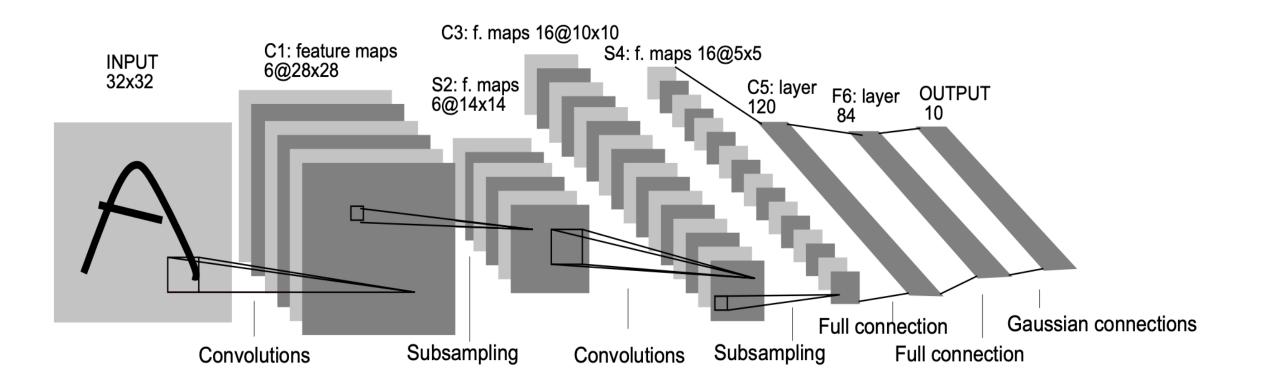
Convolutions on Multiple Input Channels • Given multiple input channels, we can specify a filter for each one and sum the results to get a 2-D output tensor



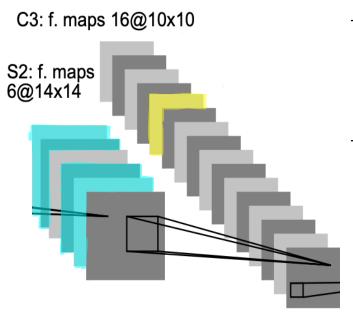
• For *c* channels and  $h \times w$  filters, we have chw + clearnable parameters (each filter has a bias term) Convolutions on Multiple Input Channels • Given multiple input channels, we can specify a filter for each one and sum the results to get a 2-D output tensor

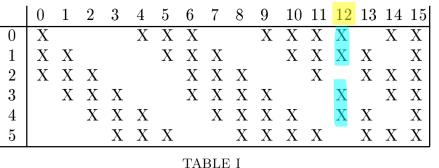


- Questions:
  - 1. Why might we want a different filter for each input?
  - 2. Why do we combine them together into a single output channel?



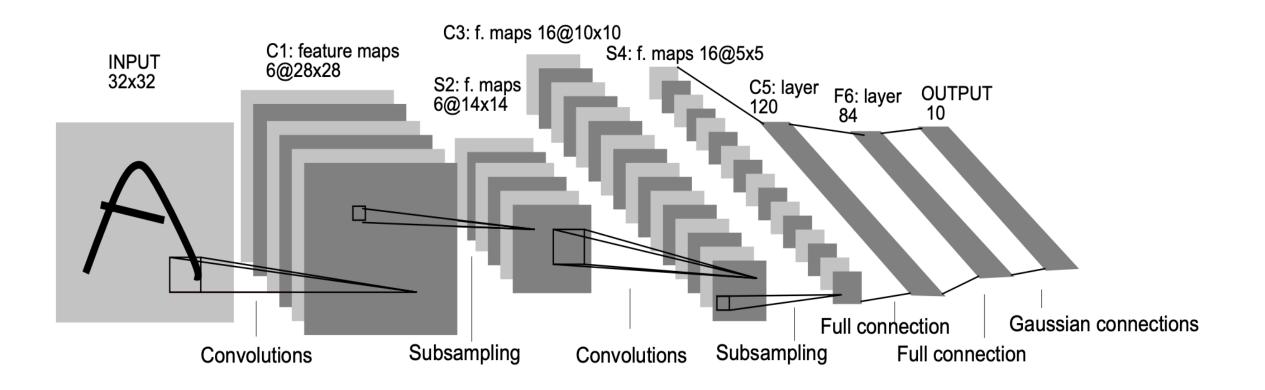
 Channels in hidden layers correspond to different macro-features, which we might want to manipulate differently → one filter per channel





Each column indicates which feature map in S2 are combined by the units in a particular feature map of C3.

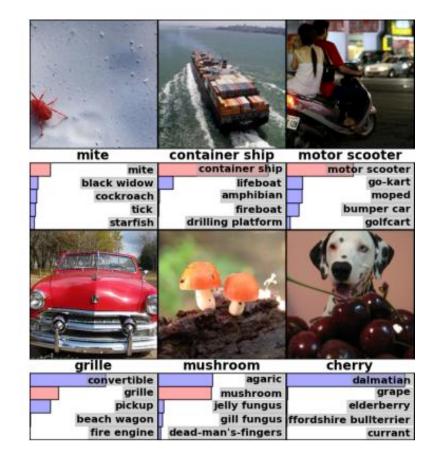
- We can combine these macro-features into a new, interesting, "higher-level" feature
  - But we don't always need to combine all of them!
  - Different combinations  $\rightarrow$  multiple output channels
  - Common architecture: more output channels and smaller outputs in deeper layers



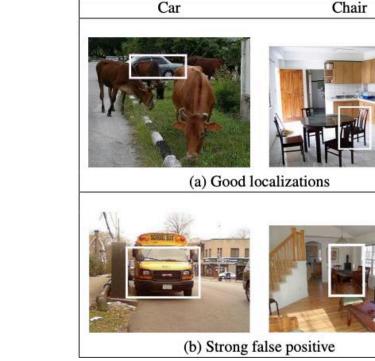
# Alright, so what kind of stuff can we actually do with this thing?

- Image Classification
- Object Localization
- Object Detection
- Semantic Segmentation
- Instance Segmentation
- Image Captioning
- Image Generation

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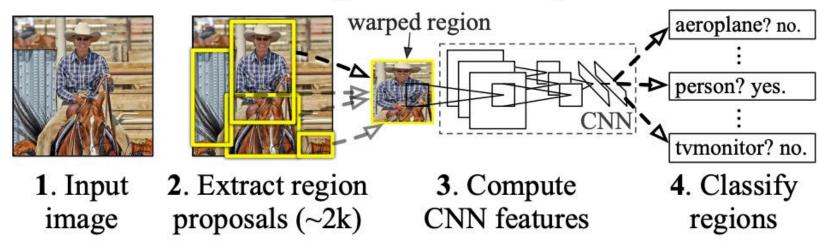


Given an image, predict a single label and a bounding box,
represented as position (x, y)
and height/width (h, w).

- Image Classification
- Object Localization
- Object Detection

Given an image, for each
 object predict a bounding box
 and a label, *l*: (*x*, *y*, *w*, *h*, *l*)

#### **R-CNN:** Regions with CNN features



- Image Classification
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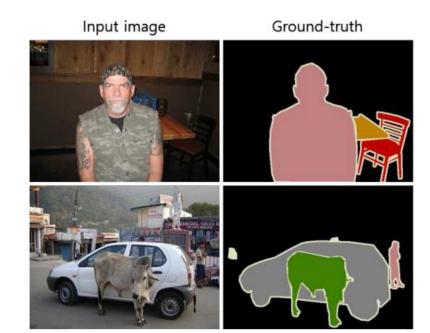


Input image

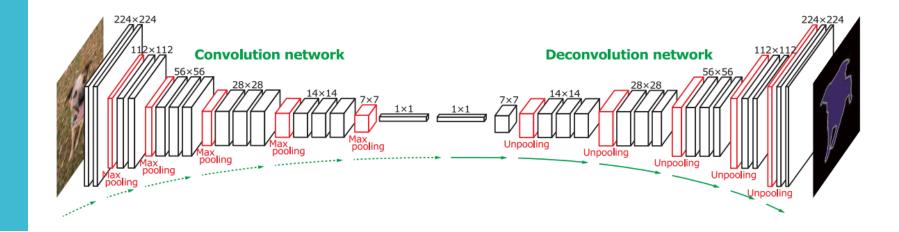
• Given an image, predict a label for every pixel in the image

Ground-truth

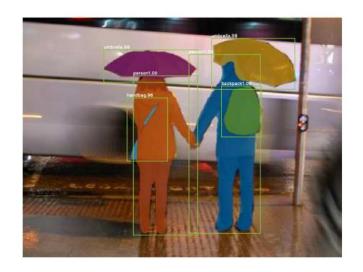
- Image Classification
- Object Localization
- Object Detection
- Semantic Segmentation



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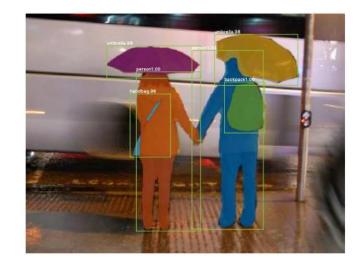


- Image Classification
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 Predict per-pixel labels as in semantic segmentation, but differentiate between different instances of the same label
 e.g., given two people, one should be labeled person-1 and one should be labeled person-2

- Image Classification
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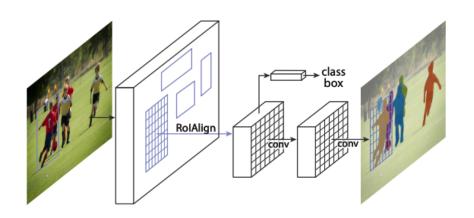
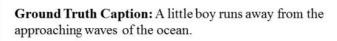


Figure 1. The Mask R-CNN framework for instance segmentation.

- Image Classification
- Object Localization
- Object Detection
- Semantic Segmentation
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- Image Captioning
- Image Generation



Generated Caption: A young boy is running on the beach.

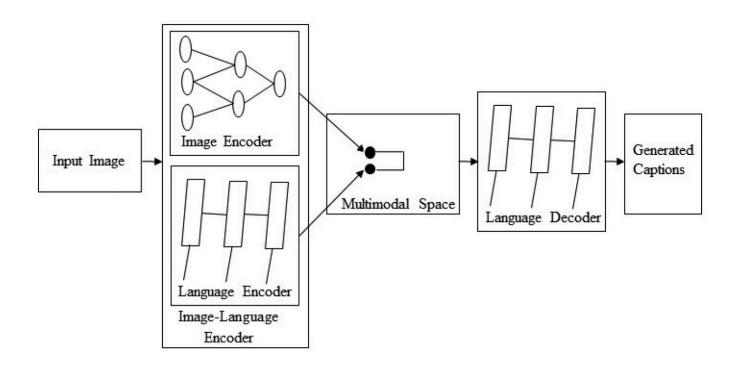


Ground Truth Caption: A brunette girl wearing sunglasses and a yellow shirt.

Generated Caption: A woman in a black shirt and sunglasses smiles.

- Take an image as input, and generate a sentence describing it as output
  - Dense captioning

generates one description



- Instance Segmentation
- Image Captioning
- Image Generation

 Typical architectures will combine a CNN and an RNNlike language model

Table 1. An Overview of the Deep-Learning-Based Approaches for Image Captioning

Reference	Image Encoder	Language Model	Category
Kiros et al. 2014 [69]	AlexNet	LBL	MS, SL, WS, EDA
Kiros et al. 2014 [70]	AlexNet, VGGNet	1. LSTM 2. SC-NLM	MS, SL, WS, EDA
Mao et al. 2014 [95]	AlexNet	2. SC-NLM RNN	MS, SL, WS
Karpathy et al. 2014 [66]	AlexNet	DTR	MS, SL, WS, EDA
Mao et al. 2015 [94]	AlexNet, VGGNet		MS, SL, WS, EDA MS, SL, WS
	VGGNet	RNN	
Chen et al. 2015 [23]	AlexNet, VGGNet		VS, SL, WS, EDA VS, SL, WS, CA
Fang et al. 2015 [33]			
Jia et al. 2015 [59]	VGGNet	LSTM	VS, SL, WS, EDA
Karpathy et al. 2015 [65]	VGGNet	RNN	MS, SL, WS, EDA
Vinyals et al. 2015 [142]	GoogLeNet	LSTM	VS, SL, WS, EDA
Xu et al. 2015 [152]	AlexNet	LSTM	VS, SL, WS, EDA, AB
Jin et al. 2015 [61]	VGGNet	LSTM	VS, SL, WS, EDA, AB
Wu et al. 2016 [151]	VGGNet	LSTM	VS, SL, WS, EDA, AP
Sugano et at. 2016 [129]	VGGNet	LSTM	VS, SL, WS, EDA, AB
Mathews et al. 2016 [97]	GoogLeNet	LSTM	VS, SL, WS, EDA, SC
Wang et al. 2016 [144]	AlexNet, VGGNet		VS, SL, WS, EDA
Johnson et al. 2016 [62]	VGGNet	LSTM	VS, SL, DC, EDA
Mao et al. 2016 [92]	VGGNet	LSTM	VS, SL, WS, EDA
Wang et al. 2016 [146]	VGGNet	LSTM	VS, SL, WS, CA
Tran et al. 2016 [135]	ResNet	MELM	VS, SL, WS, CA
Ma et al. 2016 [90]	AlexNet	LSTM	VS, SL, WS, CA
You et al. 2016 [156]	GoogLeNet	RNN	VS, SL, WS, EDA, SC
Yang et al. 2016 [153]	VGGNet	LSTM	VS, SL, DC, EDA
Anne et al. 2016 [6]	VGGNet	LSTM	VS, SL, WS, CA, NOI
Yao et al. 2017 [155]	GoogLeNet	LSTM	VS, SL, WS, EDA, SC
Lu et al. 2017 [88]	ResNet	LSTM	VS, SL, WS, EDA, AB
Chen et al. 2017 [21]	VGGNet, ResNet	LSTM	VS, SL, WS, EDA, AB
Gan et al. 2017 [41]	ResNet	LSTM	VS, SL, WS, CA, SCB
Pedersoli et al. 2017 [112]	VGGNet	RNN	VS, SL, WS, EDA, AB
Ren et al. 2017 [119]	VGGNet	LSTM	VS, ODL, WS, EDA
Park et al. 2017 [111]	ResNet	LSTM	VS, SL, WS, EDA, AB
Wang et al. 2017 [148]	ResNet	LSTM	VS, SL, WS, EDA
Tavakoli et al. 2017 [134]	VGGNet	LSTM	VS, SL, WS, EDA, AB
Liu et al. 2017 [84]	VGGNet	LSTM	VS, SL, WS, EDA, AF
Gan et al. 2017 [39]	ResNet	LSTM	VS, SL, WS, EDA, SC
Dai et al. 2017 [26]	VGGNet	LSTM	VS, ODL, WS, EDA
Shetty et al. 2017 [126]	GoogLeNet	LSTM	VS, ODL, WS, EDA
Liu et al. 2017 [85]	Inception-V3	LSTM	VS, ODL, WS, EDA
Gu et al. 2017 [51]	VGGNet	1. Language CNN 2. LSTM	VS, SL, WS, EDA

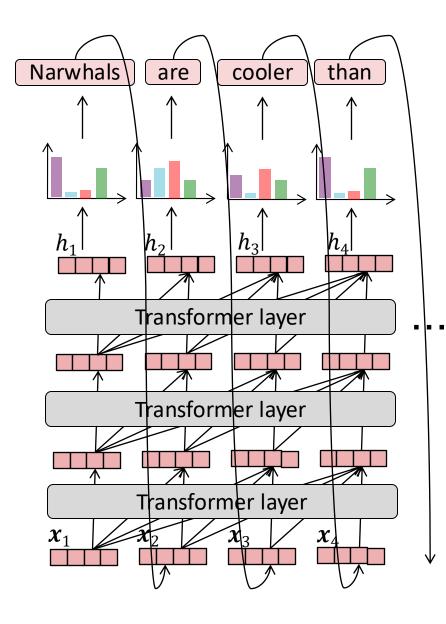
Common Tasks in Computer Vision

- Instance Segmentation
- Image Captioning
- Image Generation

(Continued)

- Image Classification
- Object Localization
- Object Detection
- Semantic Segmentation
- Instance Segmentation
- Image Captioning
- Image Generation?

Recall: Transformer Language Model



Each layer of a

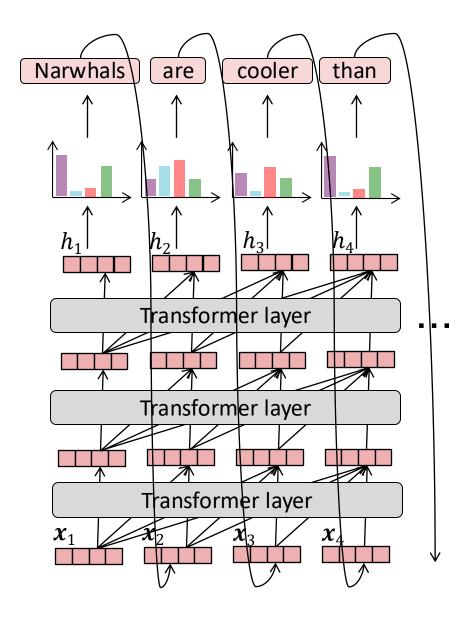
Transformer LM

consists of:

1. causal attention

- feed-forward neural network
- 3. layer normalization
- 4. residual connections

Each hidden vector looks back at the hidden vectors of the current and previous timesteps in the previous layer. Recall: Transformer Language Model a.k.a. Decoder-only Transformer



Each layer of a

Transformer LM

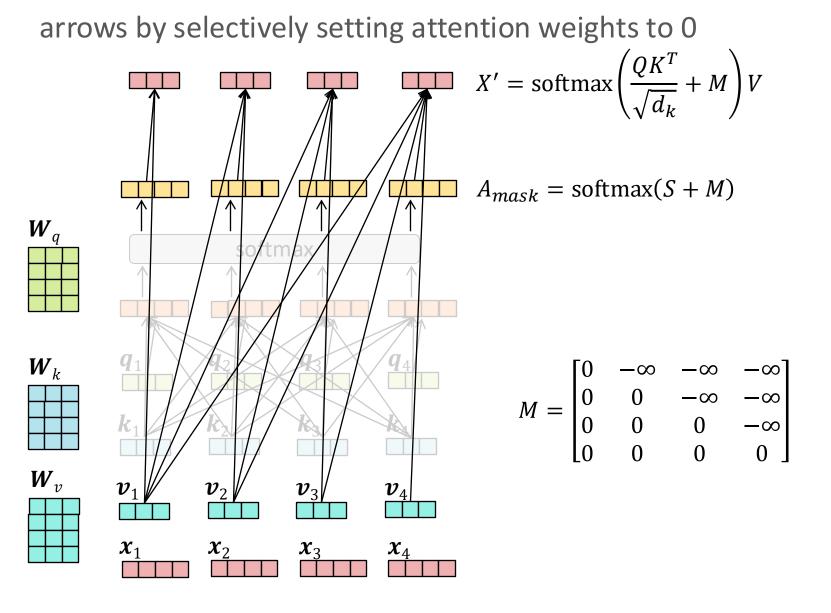
consists of:

**1.** causal attention

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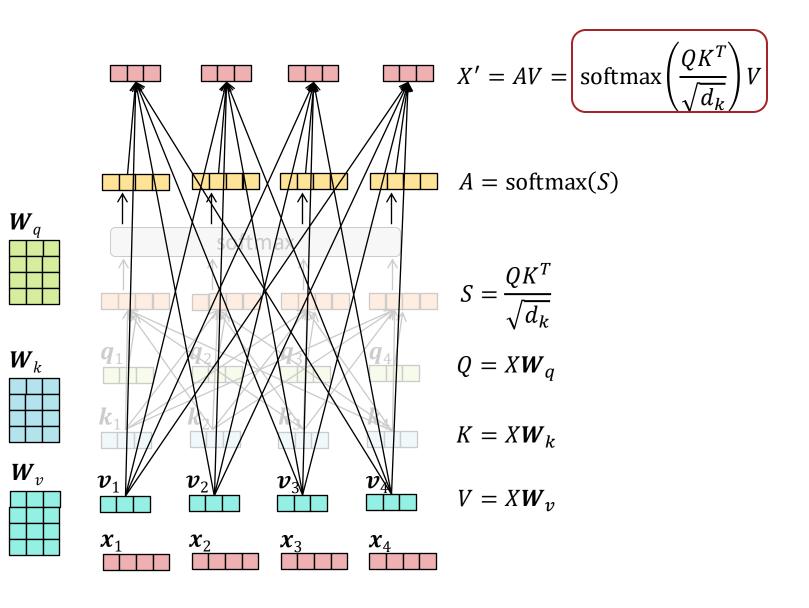
Each hidden vector looks back at the hidden vectors of the **current and previous timesteps in the previous layer.**  Idea: we can effectively delete or "mask" some of these

Recall: Causal Attention



Holy cow, that's a lot of new arrows... do we always want/need all of those?

No...



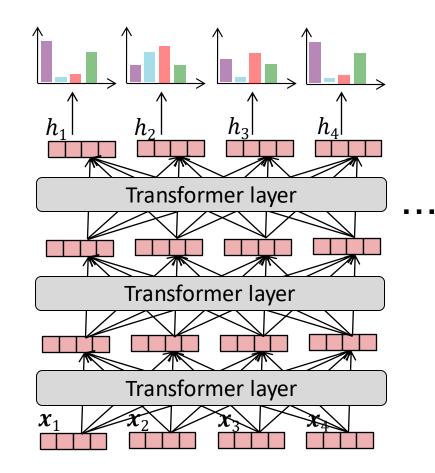
Holy cow, that's a lot of new arrows... do we sometimes want/need all of those?

X' = AV =softmax  $A = \operatorname{softmax}(S)$  $\boldsymbol{W}_q$  $S = \frac{QK^T}{\sqrt{d_k}}$  $\boldsymbol{W}_k$  $Q = X W_q$  $K = X \boldsymbol{W}_k$  $\boldsymbol{W}_{v}$  $\boldsymbol{v}_1$  $\boldsymbol{v}_2$  $V = X \boldsymbol{W}_{v}$  $x_4$  $\boldsymbol{x}_1$  $\boldsymbol{x}_2$  $\boldsymbol{x}_3$ 

Yes!

 $\left(\frac{QK^T}{\overline{d_k}}\right)V$ 

### Encoder-only Transformer



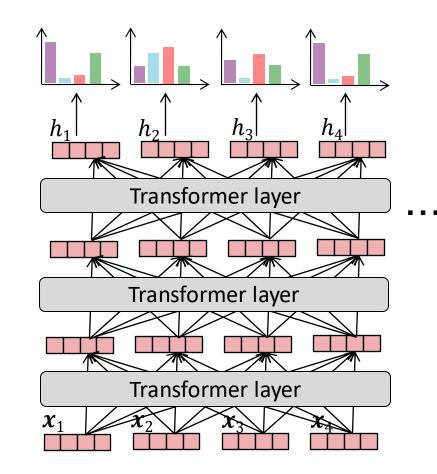
Each layer of a

Transformer LM

consists of:

- **1.** non-causal attention
- 2. feed-forward neural network
- 3. layer normalization
- 4. residual connections

Each hidden vector looks back at the hidden vectors of all timesteps in the previous layer. Okay, but how would we train one of these things?



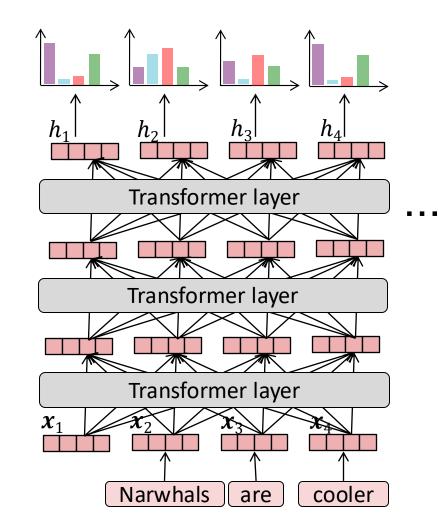
Each layer of a

Transformer LM

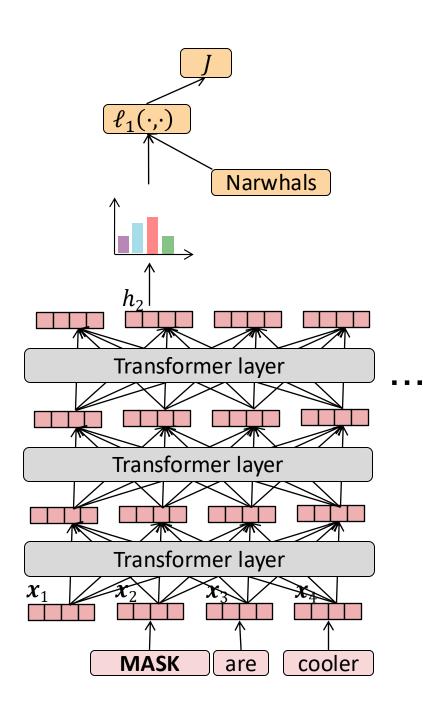
consists of:

- **1.** non-causal attention
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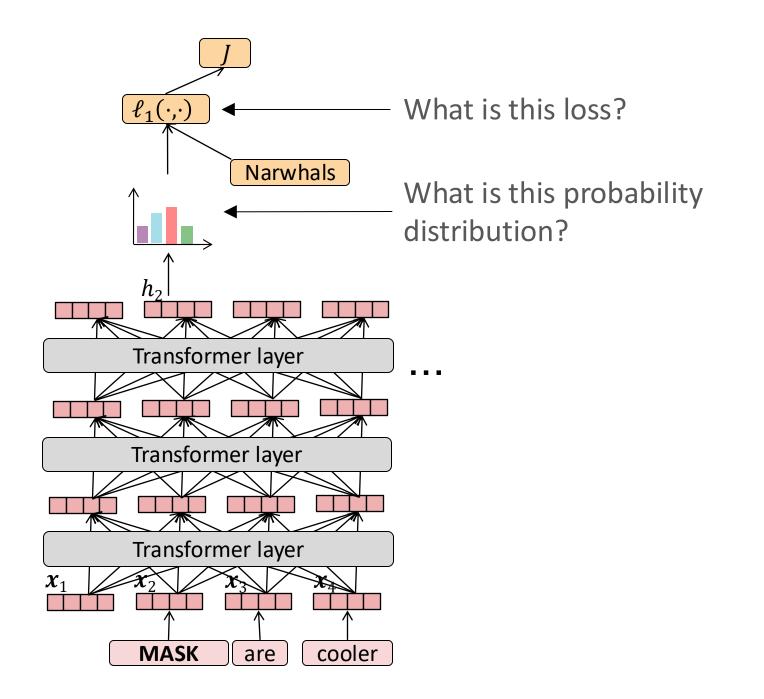
Each hidden vector looks back at the hidden vectors of **all timesteps in the previous layer.** 

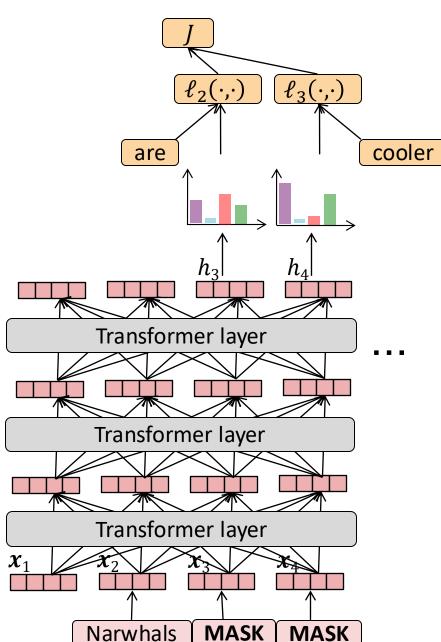


Rather than trying to predict the next token, *mask* out a few tokens in the sequence and train the model to predict the masked tokens.



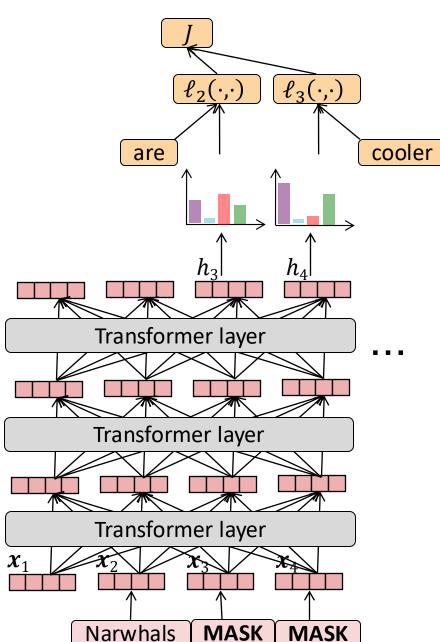
Rather than trying to predict the next token, *mask* out a few tokens in the sequence and train the model to predict the masked tokens.





Rather than trying to predict the next token, mask out a few tokens in the sequence and train the model to predict the masked tokens.

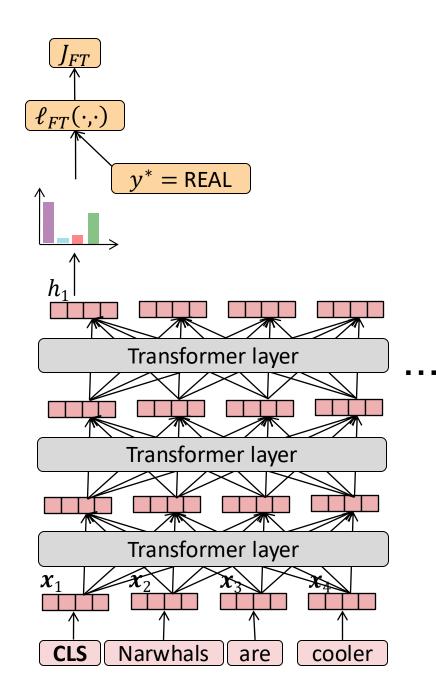
> This kind of pre-training was popularized by the BERT language model



Rather than trying to predict the next token, mask out a few tokens in the sequence and train the model to predict the masked tokens.

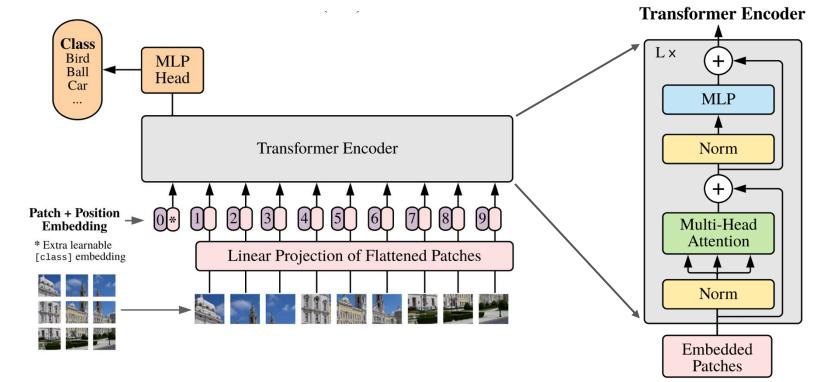
> This kind of **pre-training** was popularized by the BERT language model

## Supervised Fine-tuning



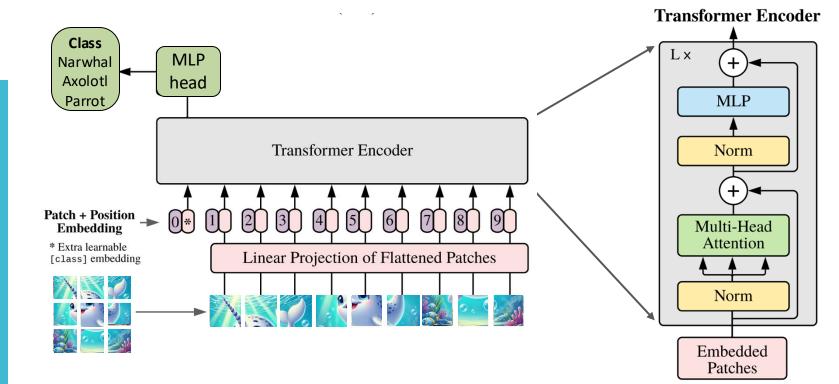
Prepend a special class token and fine*tune* the (pre-trained) model to predict the label for each sequence This model is not

This model is not generative but has been shown to be a highly effective discriminator on a variety of tasks Vision Transformer (ViT)



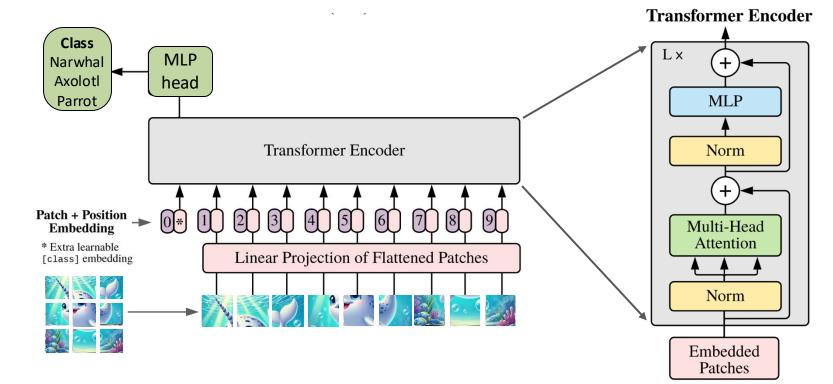
- Instead of words as input, the inputs are  $P \times P$  pixel *patches*
- Each patch is embedded linearly into a vector of size 1024
- Uses 1D positional embeddings
- Pre-trained on a large, supervised dataset (e.g., ImageNet 21K, JFT-300M)

# Vision Transformer (ViT)



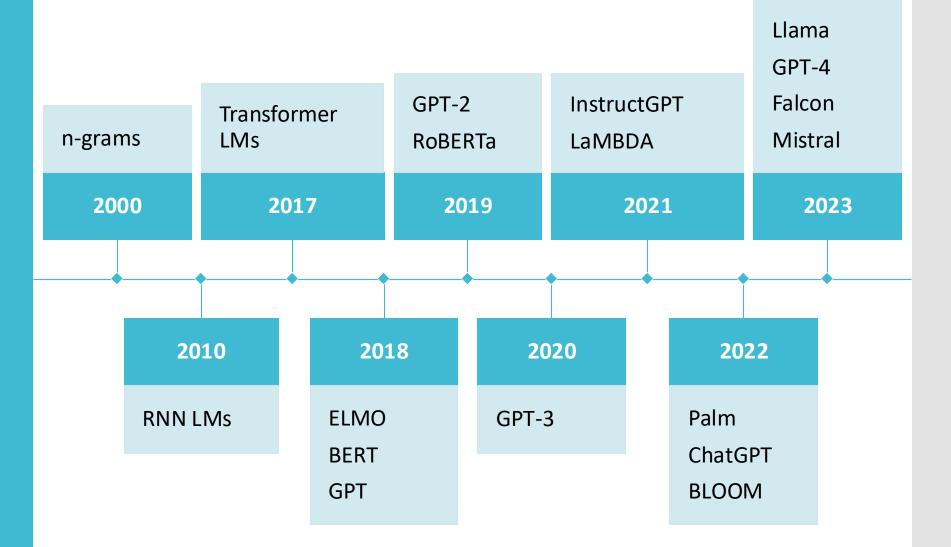
- Instead of words as input, the inputs are  $P \times P$  pixel *patches*
- Each patch is embedded linearly into a vector of size 1024
- Uses 1D positional embeddings
- Can be fine-tuned by learning a new classification head on some (small) target dataset (e.g., CIFAR-100)

How can a ViT learn 2D positional information from a 1D positional embedding?

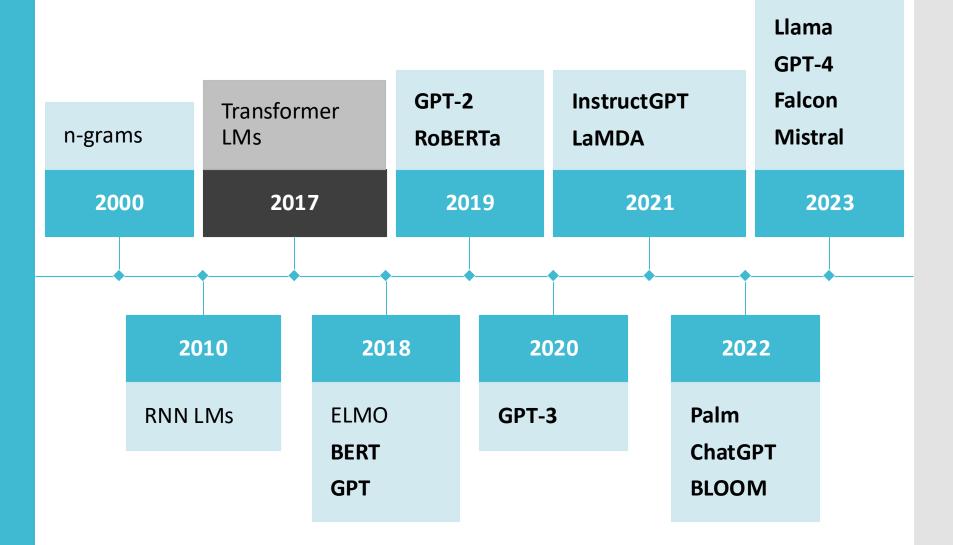


- Instead of words as input, the inputs are  $P \times P$  pixel *patches*
- Each patch is embedded linearly into a vector of size 1024
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- Can be fine-tuned by learning a new classification head on some (small) target dataset (e.g., CIFAR-100)

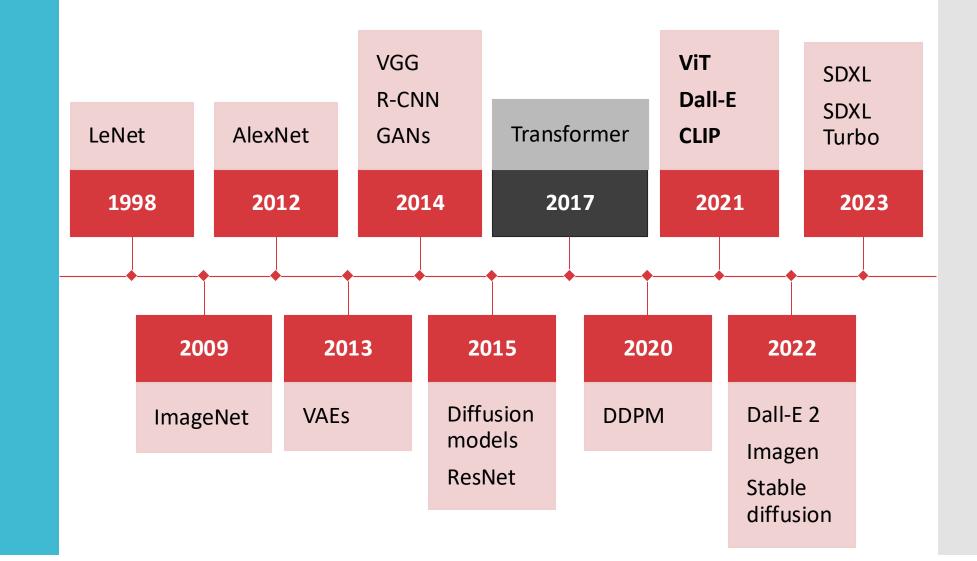
### Language Modelling: Timeline



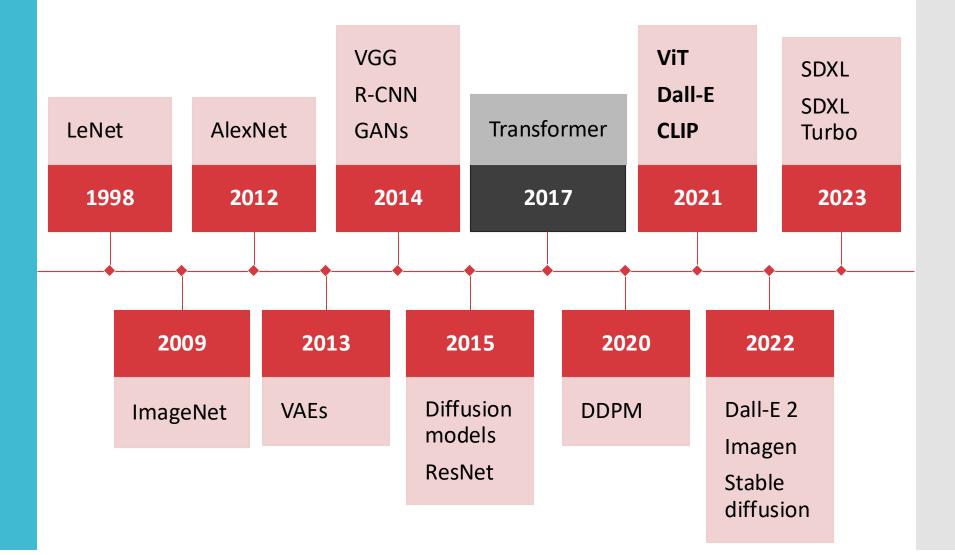
### Language Modelling: Timeline



### Language Modelling: Timeline



Why did Transformers take so long to gain traction in computer vision?



Why did Transformers take so long to gain traction in computer vision?

#### AN IMAGE IS WORTH 16x16 WORDS: TRANSFORMERS FOR IMAGE RECOGNITION AT SCALE

Alexey Dosovitskiy<sup>\*,†</sup>, Lucas Beyer<sup>\*</sup>, Alexander Kolesnikov<sup>\*</sup>, Dirk Weissenborn<sup>\*</sup>, Xiaohua Zhai<sup>\*</sup>, Thomas Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, Jakob Uszkoreit, Neil Houlsby<sup>\*,†</sup> <sup>\*</sup>equal technical contribution, <sup>†</sup>equal advising Google Research, Brain Team {adosovitskiy, neilhoulsby}@google.com

When trained on mid-sized datasets such as ImageNet without strong regularization, these models yield modest accuracies of a few percentage points below ResNets of comparable size. This seemingly discouraging outcome may be expected: Transformers lack some of the inductive biases inherent to CNNs, such as translation equivariance and locality, and therefore do not generalize well when trained on insufficient amounts of data.

However, the picture changes if the models are trained on larger datasets (14M-300M images). We find that large scale training trumps inductive bias. Our Vision Transformer (ViT) attains excellent results when pre-trained at sufficient scale and transferred to tasks with fewer datapoints. When pre-trained on the public ImageNet-21k dataset or the in-house JFT-300M dataset, ViT approaches or beats state of the art on multiple image recognition benchmarks. In particular, the best model reaches the accuracy of 88.55% on ImageNet, 90.72% on ImageNet-ReaL, 94.55% on CIFAR-100, and 77.63% on the VTAB suite of 19 tasks.

Why did Transformers take so long to gain traction in computer vision?

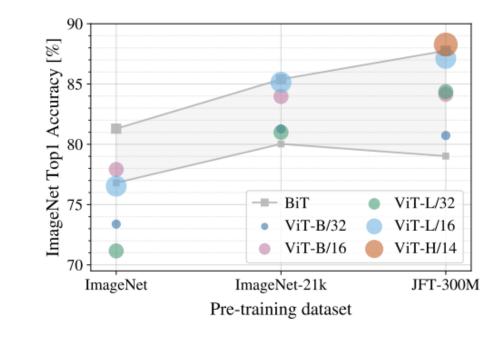


Figure 3: Transfer to ImageNet. While large ViT models perform worse than BiT ResNets (shaded area) when pre-trained on small datasets, they shine when pre-trained on larger datasets. Similarly, larger ViT variants overtake smaller ones as the dataset grows. Wait, hang on: is this even a generative model?

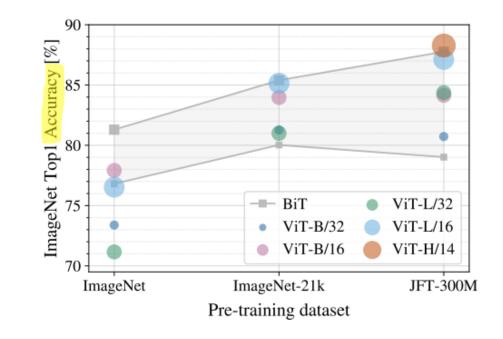


Figure 3: Transfer to ImageNet. While large ViT models perform worse than BiT ResNets (shaded area) when pre-trained on small datasets, they shine when pre-trained on larger datasets. Similarly, larger ViT variants overtake smaller ones as the dataset grows.