10-301/601: Introduction to Machine Learning Lecture 20: Markov Decision Processes

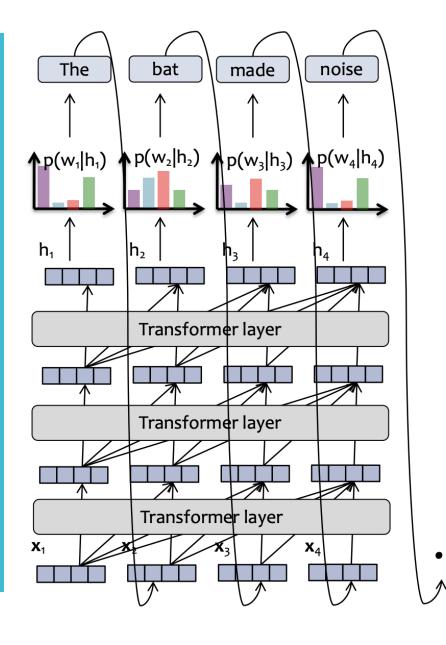
Matt Gormley & Henry Chai

11/6/24

Front Matter

- Announcements
 - Exam 2 on 11/7 (tomorrow!)
 - Please review <u>the seating chart on Piazza</u> and make sure you have a seat / know where you're going
 - HW7 to be released 11/7, due 11/17 at 11:59 PM
 - Please be mindful of your grace day usage (see <u>the course syllabus</u> for the policy)
 - If you have not used PyTorch before, I *strongly*
 - encourage you to go to recitation on Friday (11/8)

Recall: Transformers



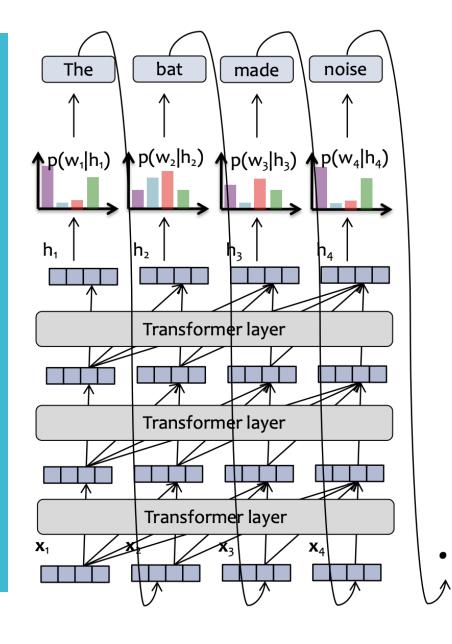
Each layer of a Transformer LM consists of several **sublayers**:

- 1. attention
- 2. feed-forward neural network
- 3. layer normalization
- 4. residual connections

Each hidden vector looks back at the hidden vectors of the **current and previous timesteps in the previous layer.**

The language model part is just like an RNN-LM.

Okay, but how on earth do we go about training these things?



Each layer of a Transformer LM consists of several **sublayers**:

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Each hidden vector looks back at the hidden vectors of the **current and previous timesteps in the previous layer.**

The language model part is just like an RNN-LM.

Recall: Mini-batch Stochastic Gradient Descent...

- Input: $\mathcal{D} = \{ (\mathbf{x}^{(n)}, y^{(n)}) \}_{n=1}^{N}, \eta_{MB}^{(0)}, B$
- 1. Initialize all weights $W_{(0)}^{(1)}, \dots, W_{(0)}^{(L)}$ to small, random numbers and set t = 0
 - . While TERMINATION CRITERION is not satisfied
 - a. Randomly sample *B* data points from $\mathcal{D}, \{(\mathbf{x}^{(b)}, \mathbf{y}^{(b)})\}_{h=1}^{B}$
 - b. Compute the gradient of the loss w.r.t. the sampled *batch*,

5

$$G^{(l)} = \frac{1}{B} \sum_{b=1}^{B} \nabla_{W^{(l)}} \ell^{(b)} \left(W_{(t)}^{(1)}, \dots, W_{(t)}^{(L)} \right) \forall l$$

- c. Update $W^{(l)}: W_{t+1}^{(l)} \leftarrow W_t^{(l)} \eta_{MB}^{(0)} G^{(l)} \forall l$
- d. Increment $t: t \leftarrow t + 1$

• Output: $W_t^{(1)}, ..., W_t^{(L)}$

Mini-batch Stochastic Gradient Descent is a lie!

- Input: $\mathcal{D} = \{ (\mathbf{x}^{(n)}, y^{(n)}) \}_{n=1}^{N}, \eta_{MB}^{(0)}, B$
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Mini-batch Stochastic Gradient Descent is a lie! just the beginning!

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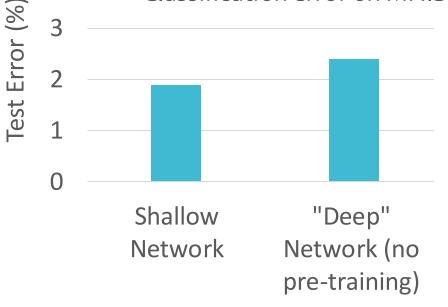
• Output: $W_t^{(1)}, ..., W_t^{(L)}$

Traditional Supervised Learning

- You have some task that you want to apply machine learning to
- You have a labelled dataset to train with
- You fit a deep learning model to the dataset

Reality

- You have some niche task that you want to apply machine learning to e.g., predicting the author of children's books
- You have a tiny labelled dataset to train with
- You fit a massive deep learning model to the dataset
- Surprise, surprise: it overfits and your test error is super high



Classification error on MNIST handwritten digit dataset

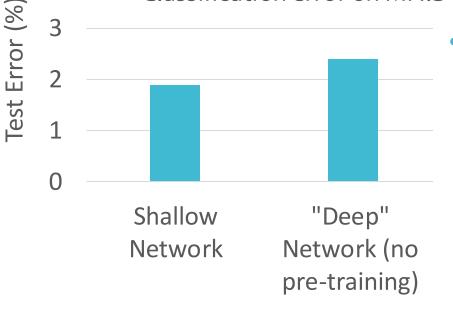
• "gradient-based

optimization starting
from random initialization
appears to often get
stuck in poor solutions for

such deep networks."

Reality

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Classification error on MNIST handwritten digit dataset

• Idea: if shallow

networks are easier to

train, let's just

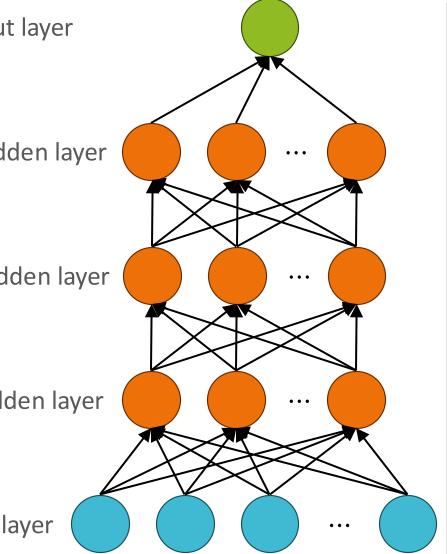
decompose our deep

network into a series

of shallow networks!

• Train each layer of the Output layer network iteratively using the training dataset 3rd hidden layer • Start at the input layer and move towards the 2nd hidden layer output layer • Once a layer has been 1st hidden layer trained, fix its weights and use those to train

Input layer

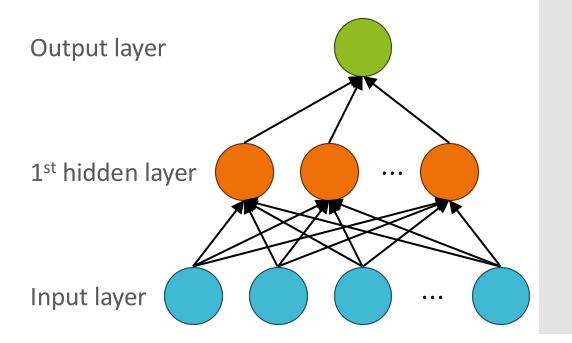


subsequent layers

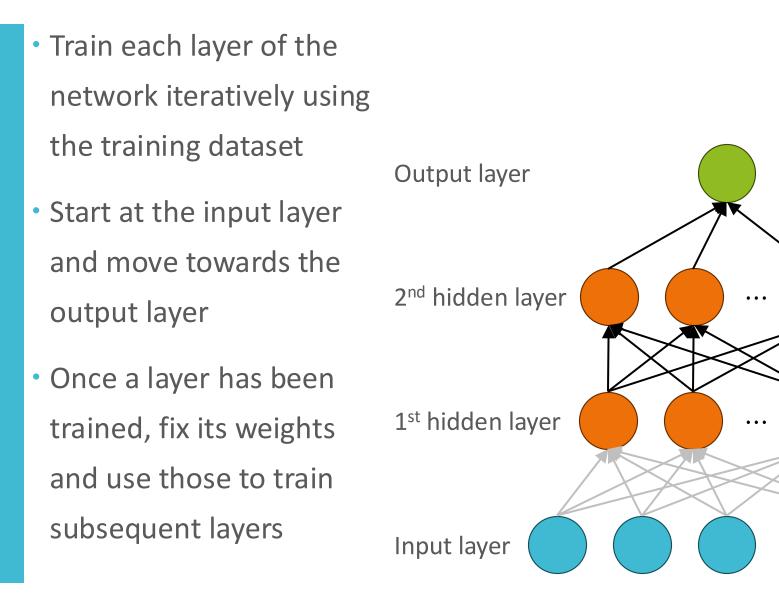
 Train each layer of the network iteratively using the training dataset

 Start at the input layer and move towards the output layer

 Once a layer has been trained, fix its weights and use those to train subsequent layers



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. . .

• Train each layer of the Output layer network iteratively using the training dataset 3rd hidden layer • Start at the input layer and move towards the 2nd hidden layer output layer • Once a layer has been 1st hidden layer trained, fix its weights and use those to train subsequent layers Input layer

. . .

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Fine-tuning (Bengio et al., 2006) • Train each layer of the Output layer network iteratively using the training dataset 3rd hidden layer • Use the pre-trained weights as an 2nd hidden layer initialization and *fine-tune* the entire network e.g., via SGD 1st hidden layer with the training dataset Input layer

• • •

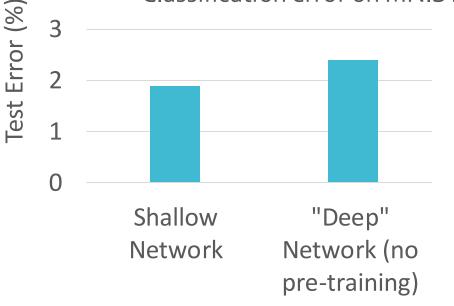
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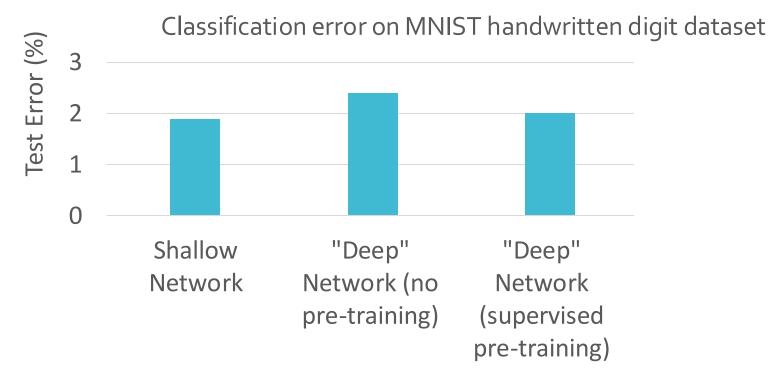
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 Train each layer of the network iteratively using the training dataset Use the pre-trained weights as an initialization and *fine-tune* the entire network e.g., via SGD with the training dataset

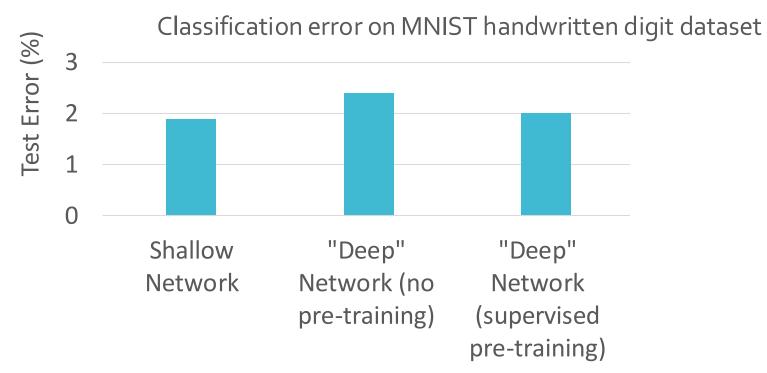
Classification error on MNIST handwritten digit dataset



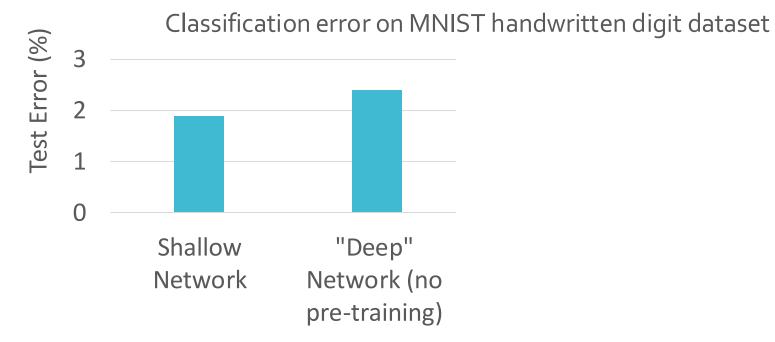
 Train each layer of the network iteratively using the training dataset to predict the labels Use the pre-trained weights as an initialization and *fine-tune* the entire network e.g., via SGD with the training dataset



Is this the only thing we could do with the training data? Train each layer of the network iteratively using the training dataset to predict the labels Use the pre-trained weights as an initialization and *fine-tune* the entire network e.g., via SGD with the training dataset

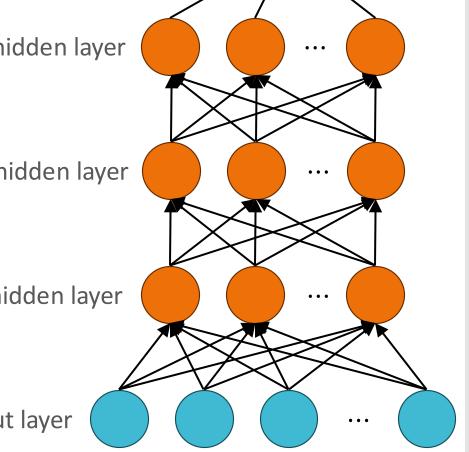


Train each layer of the
 Idea: a good representation is
 network iteratively using
 one preserves a lot of
 the training dataset *to information and could be used learn useful representations* to recreate the inputs

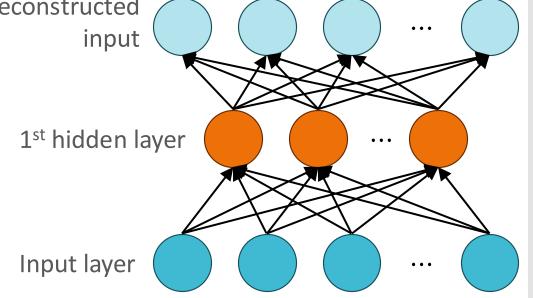


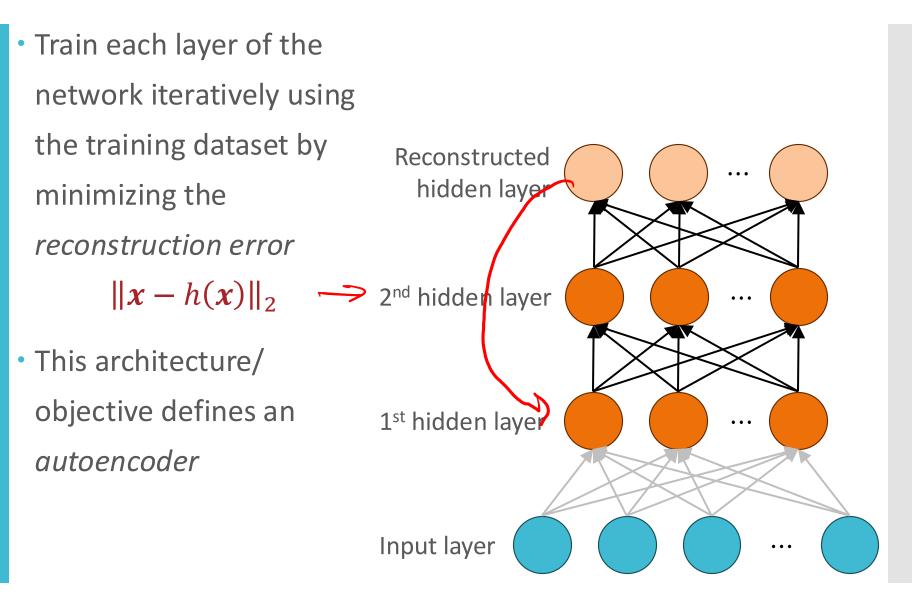
• Train each layer of the Output layer network iteratively using the training dataset by 3rd hidden layer minimizing the reconstruction error $\|x - h(x)\|_2$ 2nd hidden layer 1st hidden layer

Input layer

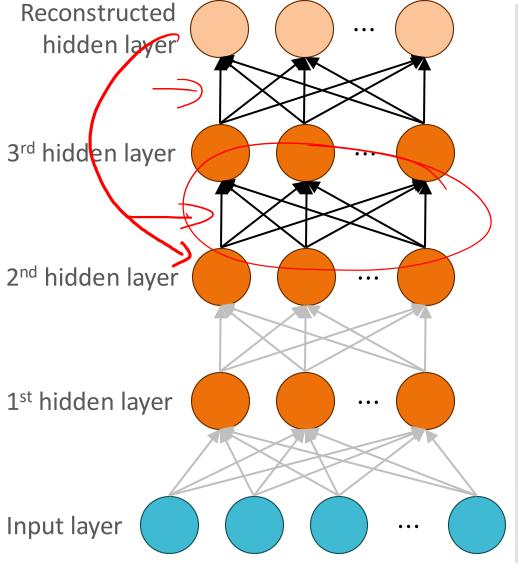


• Train each layer of the network iteratively using the training dataset by minimizing the reconstruction error Reconstructed $\|x - h(x)\|_{2}$ input This architecture/ objective defines an autoencoder

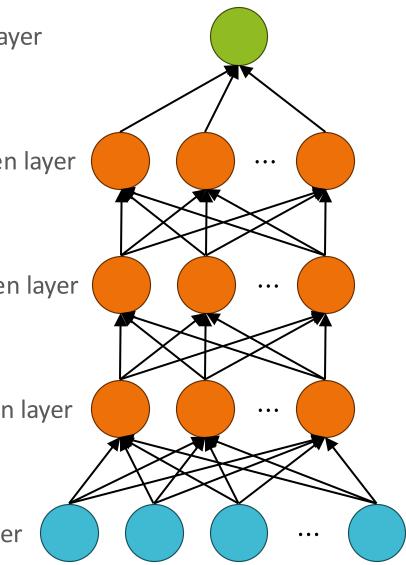




• Train each layer of the hidden laver network iteratively using the training dataset by \rightarrow 3rd hidden layer minimizing the reconstruction error $\|x - h(x)\|_{2}$ 2nd hidden layer This architecture/ objective defines an 1st hidden layer autoencoder



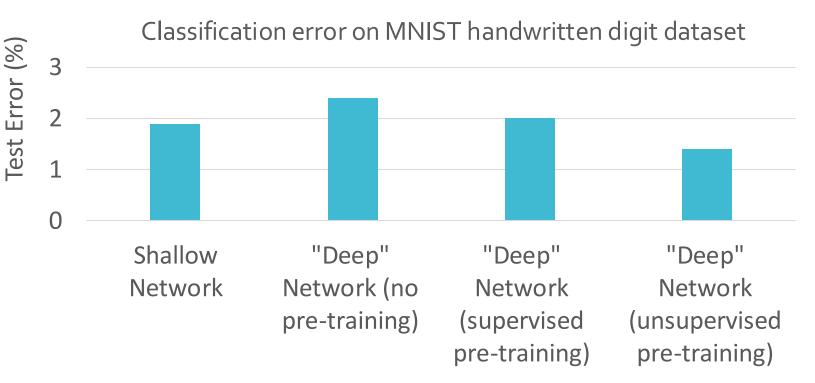
Fine-tuning (Bengio et al., 2006) • Train each layer of the Output layer network iteratively using the training dataset by 3rd hidden layer minimizing the reconstruction error $\|x - h(x)\|_{2}$ 2nd hidden layer • When fine-tuning, we're effectively swapping out 1st hidden layer the last layer and fitting all the weights to the Input layer training dataset



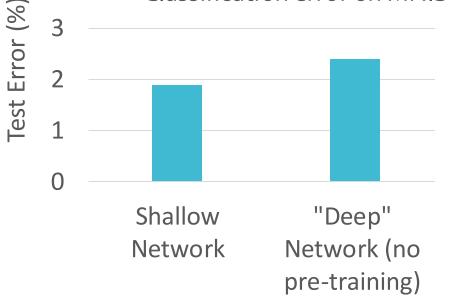
 Train each layer of the network iteratively using the training dataset by minimizing the

reconstruction error

 Idea: a good representation is one preserves a lot of information and could be used to recreate the inputs



- You have some niche task that you want to apply machine learning to e.g., predicting the author of children's books
- You have a tiny labelled dataset to train with
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Classification error on MNIST handwritten digit dataset

• Problem: what if you

don't even have

enough data to train a

single layer/fine-tune

the pre-trained

network?

- You have some niche task that you want to apply machine learning to e.g., predicting the author of children's books
- You have a tiny labelled dataset to train with
- You fit a massive deep learning model to the dataset
- Surprise, surprise: it overfits and your test error is super high
- Key observation: you can pre-train on basically any labelled or unlabelled dataset!
 - Ideally, you want to use a *large* dataset *related* to your goal task

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• GPT-3 pre-training data:

	Quantity	Weight in
Dataset	(tokens)	training mix
Common Crawl (filtered)	410 billion	60%
WebText2	19 billion	22%
Books1	12 billion	8%
Books2	55 billion	8%
Wikipedia	3 billion	3%

- You have some niche task that you want to apply machine learning to e.g., predicting the author of children's books
- You have a tiny labelled dataset to train with
- You fit a massive deep learning model to the dataset
- Surprise, surprise: it overfits and your test error is super high
- Key observation: you can pre-train on basically any labelled or unlabelled dataset!
- Okay that's great for pre-training and all, but what if
 - A. you don't have enough data to fine-tune your model?
 - B. the concept of labelled data doesn't apply to your task
 - i.e., not every input has a "correct" label e.g., chatbots?

In-context Learning

- Problem: given their size, effectively fine-tuning LLMs can require lots of labelled data points.
- Idea: leverage the LLM's context window by passing a few examples to the model as input, without performing any updates to the parameters
- Intuition: during training, the LLM is exposed to a massive number of examples/tasks and the input conditions the model to "locate" the relevant concepts

 Idea: leverage the LLM's context window by passing a few examples to the model as input,

without performing any updates to the parameters

The three settings we explore for in-context learning

Few-shot

In addition to the task description, the model sees a few examples of the task. No gradient updates are performed.



Traditional fine-tuning (not used for GPT-3)

Fine-tuning

The model is trained via repeated gradient updates using a large corpus of example tasks.



 Idea: leverage the LLM's context window by passing a few one examples to the model as input,

without performing any updates to the parameters

The three settings we explore for in-context learning

One-shot

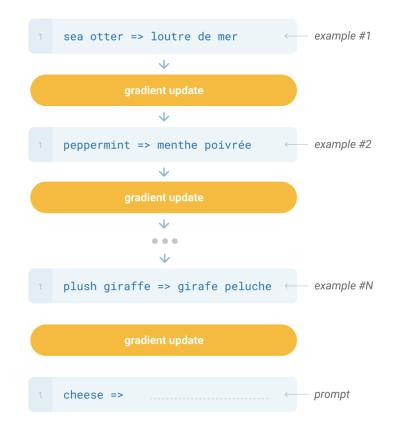
In addition to the task description, the model sees a single example of the task. No gradient updates are performed.

Translate English to French:	← task description
sea otter => loutre de mer	example
cheese =>	←— prompt

Traditional fine-tuning (not used for GPT-3)

Fine-tuning

The model is trained via repeated gradient updates using a large corpus of example tasks.



 Idea: leverage the LLM's context window by passing a few one zero(!) examples to the model as input, without performing any updates to the parameters

The three settings we explore for in-context learning

Zero-shot

The model predicts the answer given only a natural language description of the task. No gradient updates are performed.

Translate English to French:	task description
cheese =>	← prompt

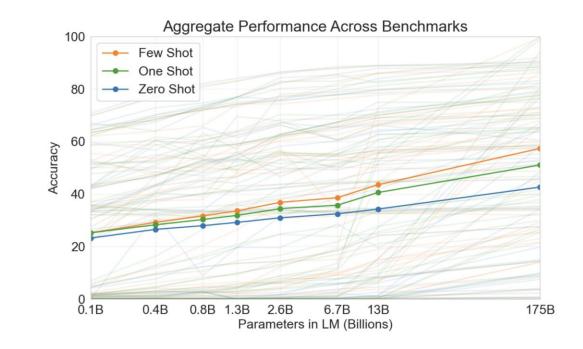
Traditional fine-tuning (not used for GPT-3)

Fine-tuning

The model is trained via repeated gradient updates using a large corpus of example tasks.



 Idea: leverage the LLM's context window by passing a few one zero(!) examples to the model as input, without performing any updates to the parameters



• Key Takeaway: LLMs can perform well on novel tasks without having to fine-tune the model, sometimes even with just one or zero labelled training data points! Reinforcement Learning from Human Feedback (RLHF)

- Insight: for many machine learning tasks, there is no universal ground truth, e.g., there are lots of possible ways to respond to a question or prompt.
- Idea: use human feedback to determine how good or bad some prediction/response is!
- Issue: if the input space is huge (e.g., all possible chat prompts), to train a good model, we might need tons and tons of (potentially expensive) human annotation...
- Idea: use a small number of annotations to learn a "reward" function!

Reinforcement Learning from Human Feedback (RLHF)

Step 1 Collect demonstration data and train a supervised policy. A prompt is sampled from our

prompt dataset.

A labeler

behavior.

desired output

This data is used to

fine-tune GPT-3.5

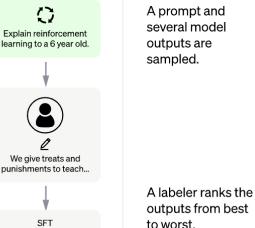
with supervised

learning.

Explain reinforcement learning to a 6 year old.



SFT



Step 2

Collect comparison data and train a reward model.

A prompt and several model outputs are sampled.

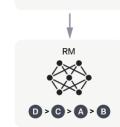
This data is used to train our

reward model.



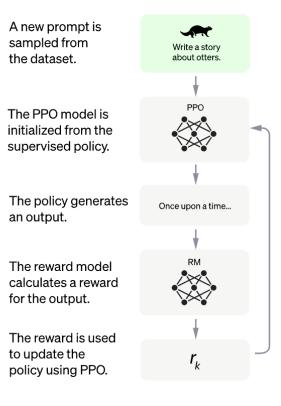
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D > C > A > B



Step 3

Optimize a policy against the reward model using the PPO reinforcement learning algorithm.

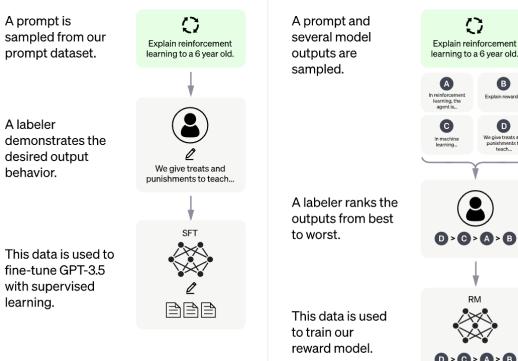


• RLHF is a form of fine-tuning that uses reinforcement learning where the reward function is learned from human preferences

What the heck is "Reinforcement Learning"?

Step 1

Collect demonstration data and train a supervised policy.



Step 2

Collect comparison data and train a reward model.

> Explain reinforcement learning to a 6 year old. learning, the D We give treats and unishments to

 \bigcirc

Step 3

A new prompt is

sampled from

Optimize a policy against the

reward model using the PPO reinforcement learning algorithm.

the dataset. The PPO model is initialized from the supervised policy. The policy generates Once upon a time... an output. The reward model calculates a reward for the output. The reward is used to update the policy using PPO.

Write a story

about otters.

• RLHF is a form of fine-tuning that uses *reinforcement learning* where the reward function is learned from human preferences

Learning Paradigms

• Supervised learning - $\mathcal{D} = \{(\mathbf{x}^{(n)}, y^{(n)})\}_{n=1}^{N}$ • Regression - $y^{(n)} \in \mathbb{R}$

• Classification -
$$y^{(n)} \in \{1, \dots, C\}$$

• Reinforcement learning - $\mathcal{D} = \{(\mathbf{s}^{(n)}, \mathbf{a}^{(n)}, r^{(n)})\}_{n=1}^{N}$

Source: <u>https://techobserver.net/2019/06/argo-ai-self-driving-car-research-center/</u> Source: <u>https://www.wired.com/2012/02/high-speed-trading/</u>

Reinforcement Learning: Examples



Source: https://www.cnet.com/news/boston-dynamics-robot-dog-spot-finally-goes-on-sale-for-74500/

Reinforcement Learning: Problem Formulation

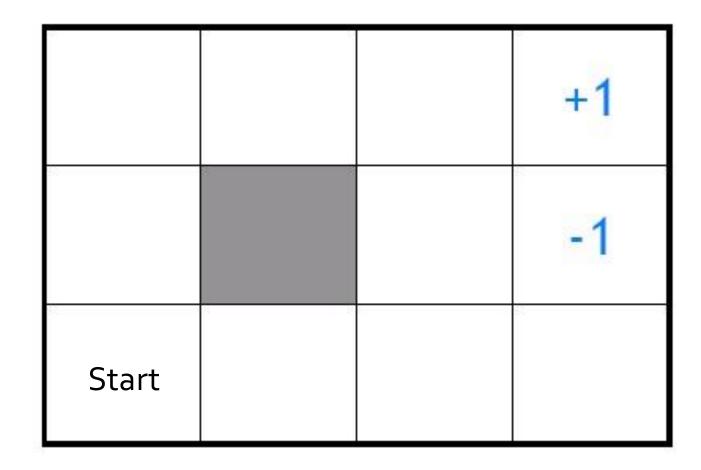
- State space, *S*
- Action space, \mathcal{A}
- Reward function
 - Stochastic, $p(r \mid s, a)$
 - Deterministic, $R: \mathcal{S} \times \mathcal{A} \to \mathbb{R}$
- Transition function
 - Stochastic, p(s' | s, a)
 - Deterministic, $\delta: \mathcal{S} \times \mathcal{A} \to \mathcal{S}$

Reinforcement Learning: Problem Formulation • Policy, $\pi : S \to A$

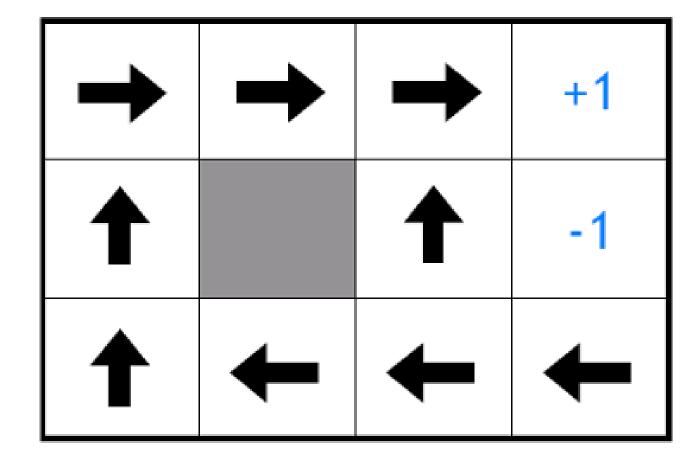
- Specifies an action to take in *every* state
- Value function, $V^{\pi}: S \to \mathbb{R}$
 - Measures the expected total payoff of starting in some state *s* and executing policy π , i.e., in every state, taking the action that π returns

Toy Example

- $\mathcal{S} =$ all empty squares in the grid
- $\mathcal{A} = \{up, down, left, right\}$
- Deterministic transitions
- Rewards of +1 and -1 for entering the labelled squares
- Terminate after receiving either reward

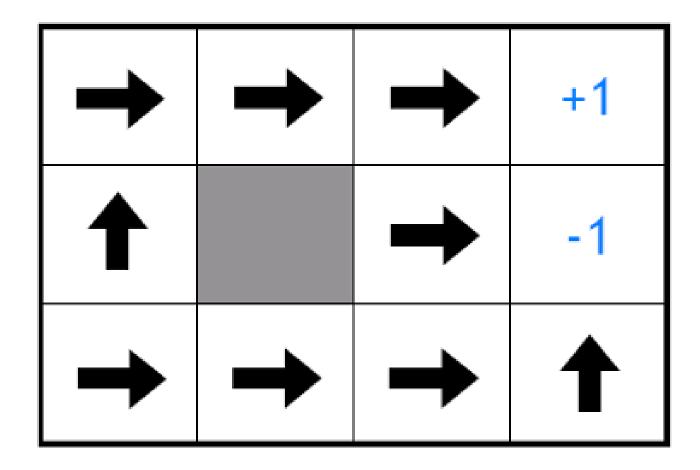


Toy Example: Policy



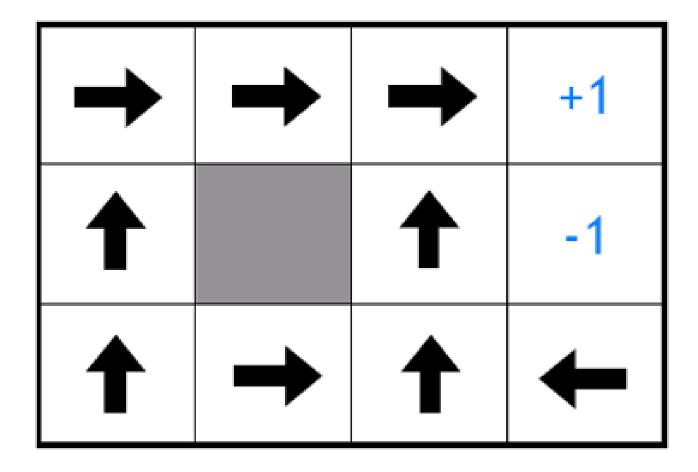
Toy Example

Optimal policy given a reward of -2 per step



Toy Example

Optimal policy given a reward of -0.1 per step



Markov Decision Process (MDP) • Assume the following model for our data:

- 1. Start in some initial state s₀
- 2. For time step *t*:
 - 1. Agent observes state s_t
 - 2. Agent takes action $a_t = \pi(s_t)$
 - 3. Agent receives reward $r_t \sim p(r \mid s_t, a_t)$
 - 4. Agent transitions to state $s_{t+1} \sim p(s' | s_t, a_t)$

3. Total reward is
$$\sum_{t=0}^{\infty} \gamma^t r_t \qquad \bigcirc \qquad \gamma < \end{pmatrix}$$

• MDPs make the *Markov assumption*: the reward and next state only depend on the current state and action.