



# 10-301/10-601 Introduction to Machine Learning

Machine Learning Department  
School of Computer Science  
Carnegie Mellon University

# Regularization + Neural Networks

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Lecture 11  
Feb. 22, 2023

# Reminders

- Homework 4: Logistic Regression
  - Out: Fri, Feb 17
  - Due: Sun, Feb. 26 at 11:59pm

# **REGULARIZATION**

# Overfitting

**Definition:** The problem of **overfitting** is when the model captures the noise in the training data instead of the underlying structure

Overfitting can occur in all the models we've seen so far:

- Decision Trees (e.g. when tree is too deep)
- KNN (e.g. when  $k$  is small)
- Perceptron (e.g. when sample isn't representative)
- Linear Regression (e.g. with nonlinear features)
- Logistic Regression (e.g. with many rare features)

# Motivation: Regularization

- **Occam’s Razor:** prefer the simplest hypothesis
- What does it mean for a hypothesis (or model) to be **simple**?
  1. small number of features (**model selection**)
  2. small number of “important” features (**shrinkage**)

# Regularization

- **Given** objective function:  $J(\theta)$
- **Goal** is to find:  $\hat{\theta} = \operatorname{argmin}_{\theta} J(\theta) + \lambda r(\theta)$
- **Key idea:** Define regularizer  $r(\theta)$  s.t. we tradeoff between fitting the data and keeping the model simple
- **Choose form of  $r(\theta)$ :**
  - Example: q-norm (usually p-norm):  $\|\theta\|_q = \left( \sum_{m=1}^M |\theta_m|^q \right)^{\frac{1}{q}}$

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$q$	$r(\theta)$	yields parameters that are...	name	optimization notes
0	$\ \theta\ _0 = \sum \mathbb{1}(\theta_m \neq 0)$	zero values	Lo reg.	no good computational solutions
1	$\ \theta\ _1 = \sum  \theta_m $	zero values	L1 reg.	subdifferentiable
2	$(\ \theta\ _2)^2 = \sum \theta_m^2$	small values	L2 reg.	differentiable

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# Regularization Examples

Add an **L2 regularizer** to Linear Regression (aka. Ridge Regression)

$$\begin{aligned} J_{\text{RR}}(\boldsymbol{\theta}) &= J(\boldsymbol{\theta}) + \boxed{\lambda ||\boldsymbol{\theta}||_2^2} \\ &= \frac{1}{N} \sum_{i=1}^N \frac{1}{2} (\boldsymbol{\theta}^T \mathbf{x}^{(i)} - y^{(i)})^2 + \boxed{\lambda \sum_{m=1}^M \theta_m^2} \end{aligned}$$

Add an **L1 regularizer** to Linear Regression (aka. LASSO)

$$\begin{aligned} J_{\text{LASSO}}(\boldsymbol{\theta}) &= J(\boldsymbol{\theta}) + \boxed{\lambda ||\boldsymbol{\theta}||_1} \\ &= \frac{1}{N} \sum_{i=1}^N \frac{1}{2} (\boldsymbol{\theta}^T \mathbf{x}^{(i)} - y^{(i)})^2 + \boxed{\lambda \sum_{m=1}^M |\theta_m|} \end{aligned}$$

# Regularization Examples

Add an **L2 regularizer** to Logistic Regression

$$\begin{aligned} J'(\boldsymbol{\theta}) &= J(\boldsymbol{\theta}) + \boxed{\lambda \|\boldsymbol{\theta}\|_2^2} \\ &= \frac{1}{N} \sum_{i=1}^N -\log p(y^{(i)} \mid \mathbf{x}^{(i)}, \boldsymbol{\theta}) + \boxed{\lambda \sum_{m=1}^M \theta_m^2} \end{aligned}$$

Add an **L1 regularizer** to Logistic Regression

$$\begin{aligned} J'(\boldsymbol{\theta}) &= J(\boldsymbol{\theta}) + \boxed{\lambda \|\boldsymbol{\theta}\|_1} \\ &= \frac{1}{N} \sum_{i=1}^N -\log p(y^{(i)} \mid \mathbf{x}^{(i)}, \boldsymbol{\theta}) + \boxed{\lambda \sum_{m=1}^M |\theta_m|} \end{aligned}$$

# Regularization

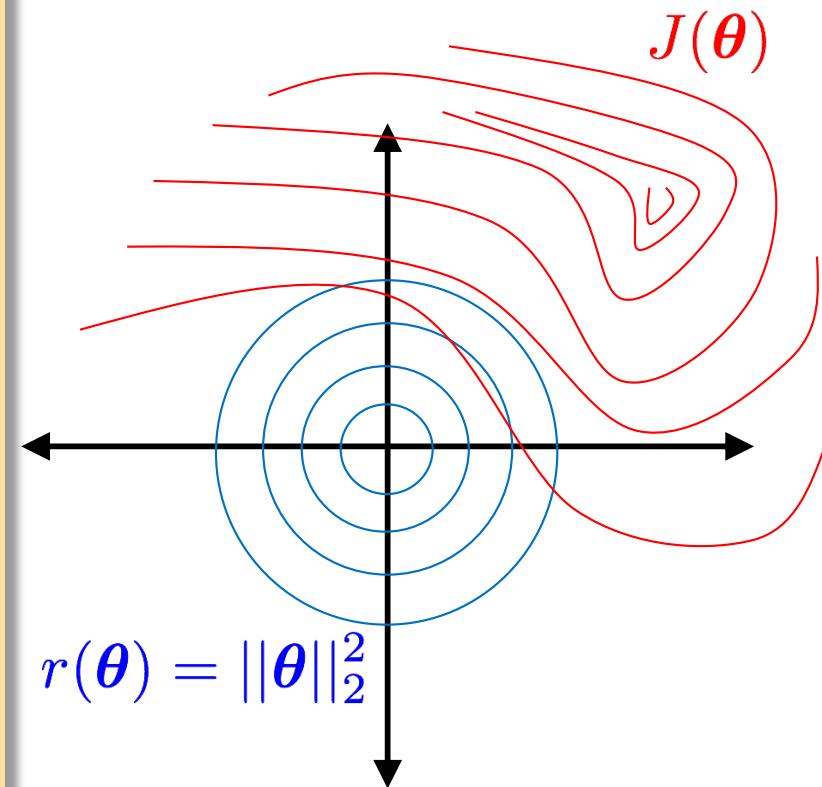
## Question:

Suppose we are minimizing  $J'(\theta)$  where

$$J'(\theta) = J(\theta) + \lambda r(\theta)$$

As  $\lambda$  increases, the minimum of  $J'(\theta)$  will...

- A. ... move towards the midpoint between  $J(\theta)$  and  $r(\theta)$
- B. ... move towards the minimum of  $J(\theta)$
- C. ... move towards the minimum of  $r(\theta)$
- D. ... move towards a theta vector of positive infinities
- E. ... move towards a theta vector of negative infinities
- F. ... stay the same



# Regularization

## Don't Regularize the Bias (Intercept) Parameter!

- In our models so far, the bias / intercept parameter is usually denoted by  $\theta_0$  -- that is, the parameter for which we fixed  $x_0 = 1$
- Regularizers always avoid penalizing this bias / intercept parameter
- Why? Because otherwise the learning algorithms wouldn't be invariant to a shift in the y-values

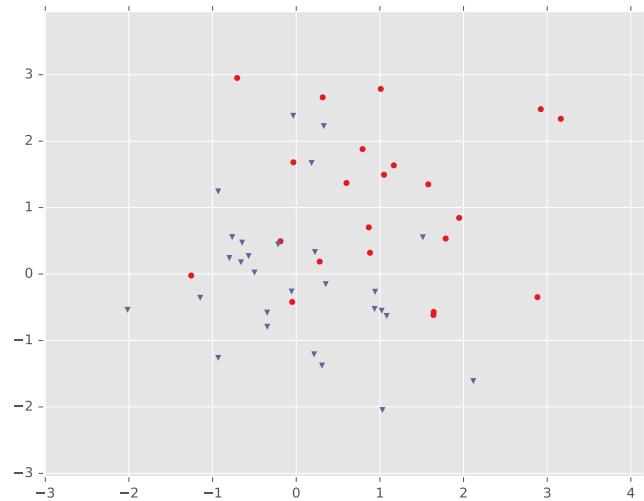
## Standardizing Data

- It's common to *standardize* each feature by subtracting its mean and dividing by its standard deviation
- For regularization, this helps all the features be penalized in the same units  
(e.g. convert both centimeters and kilometers to z-scores)

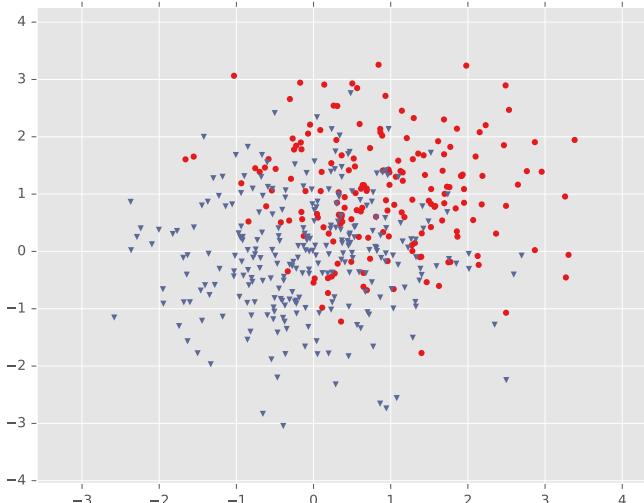
# **REGULARIZATION EXAMPLE: LOGISTIC REGRESSION**

# Example: Logistic Regression

Training Data

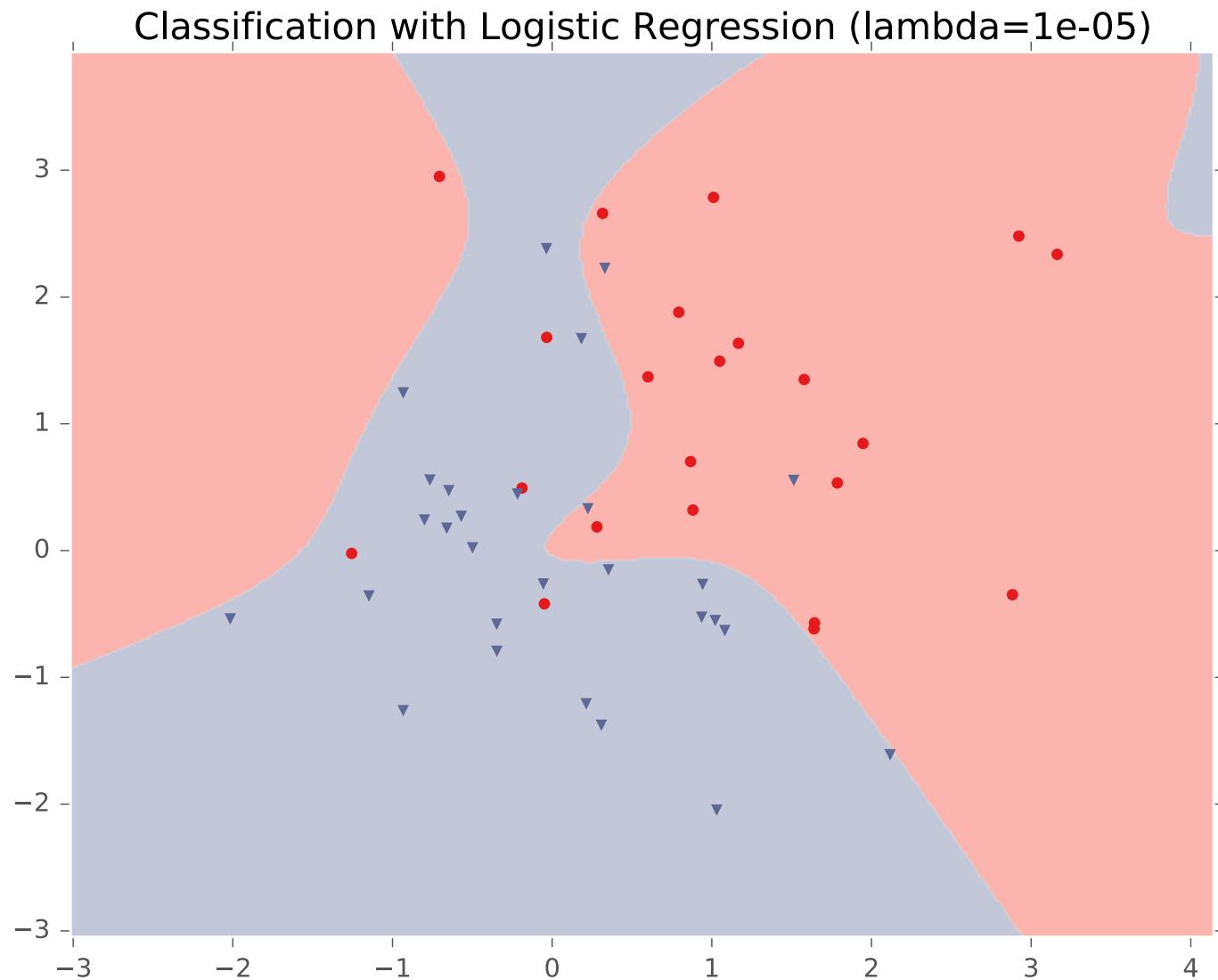


Test Data

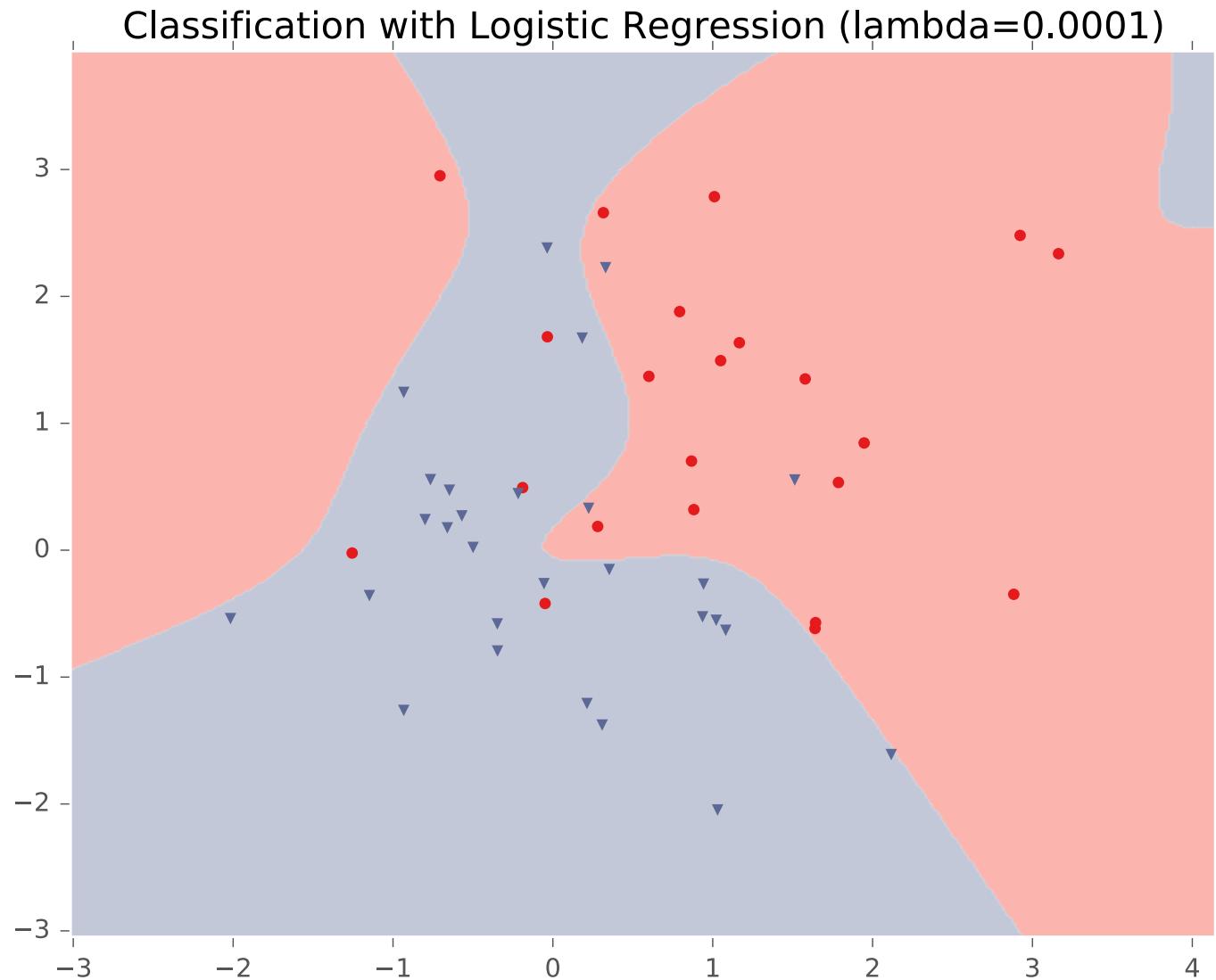


- For this example, we construct **nonlinear features** (i.e. feature engineering)
- Specifically, we add **polynomials up to order 9** of the two original features  $x_1$  and  $x_2$
- Thus our classifier is **linear in the high-dimensional feature space**, but the decision boundary is **nonlinear** when visualized in **low-dimensions** (i.e. the original two dimensions)

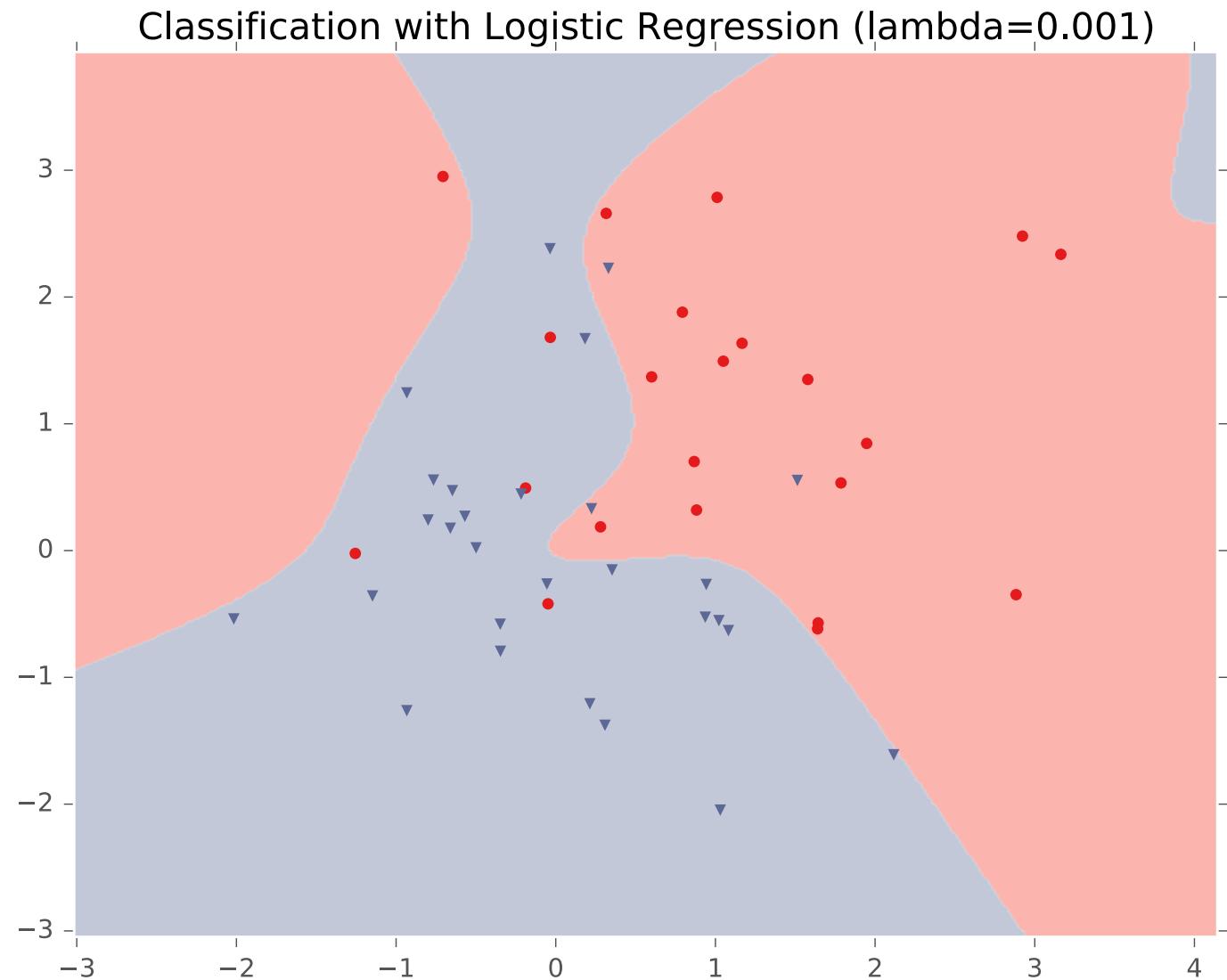
# Example: Logistic Regression



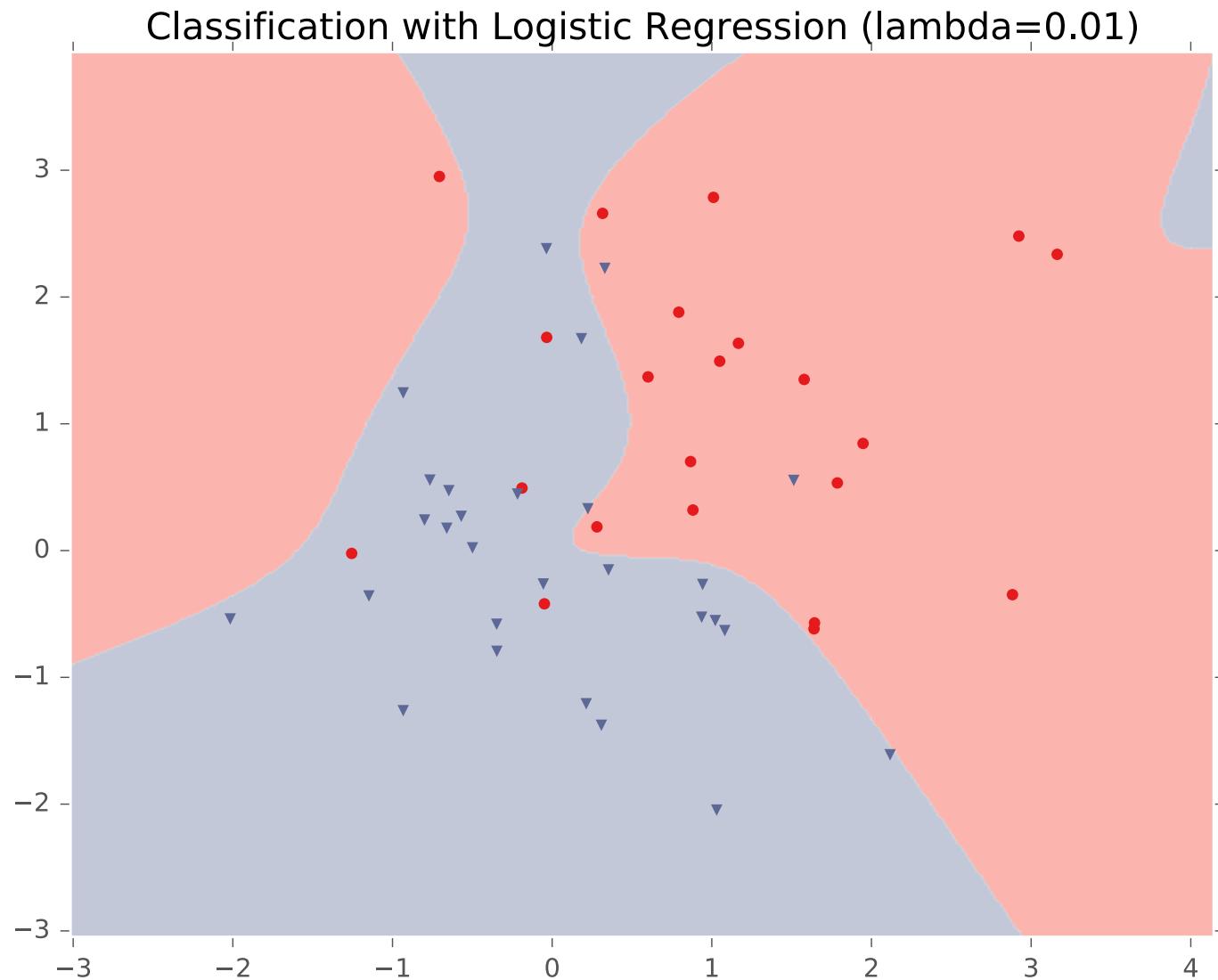
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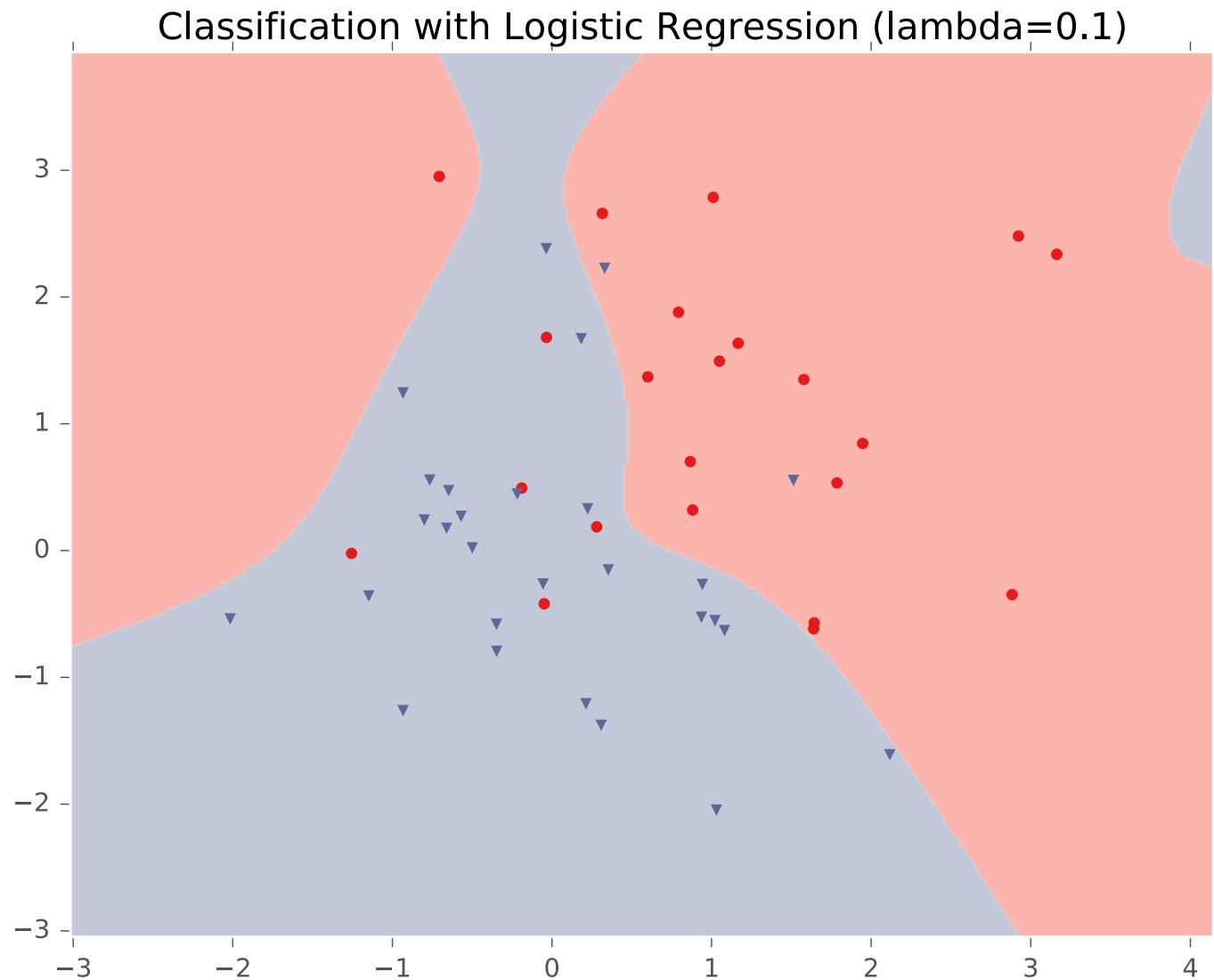
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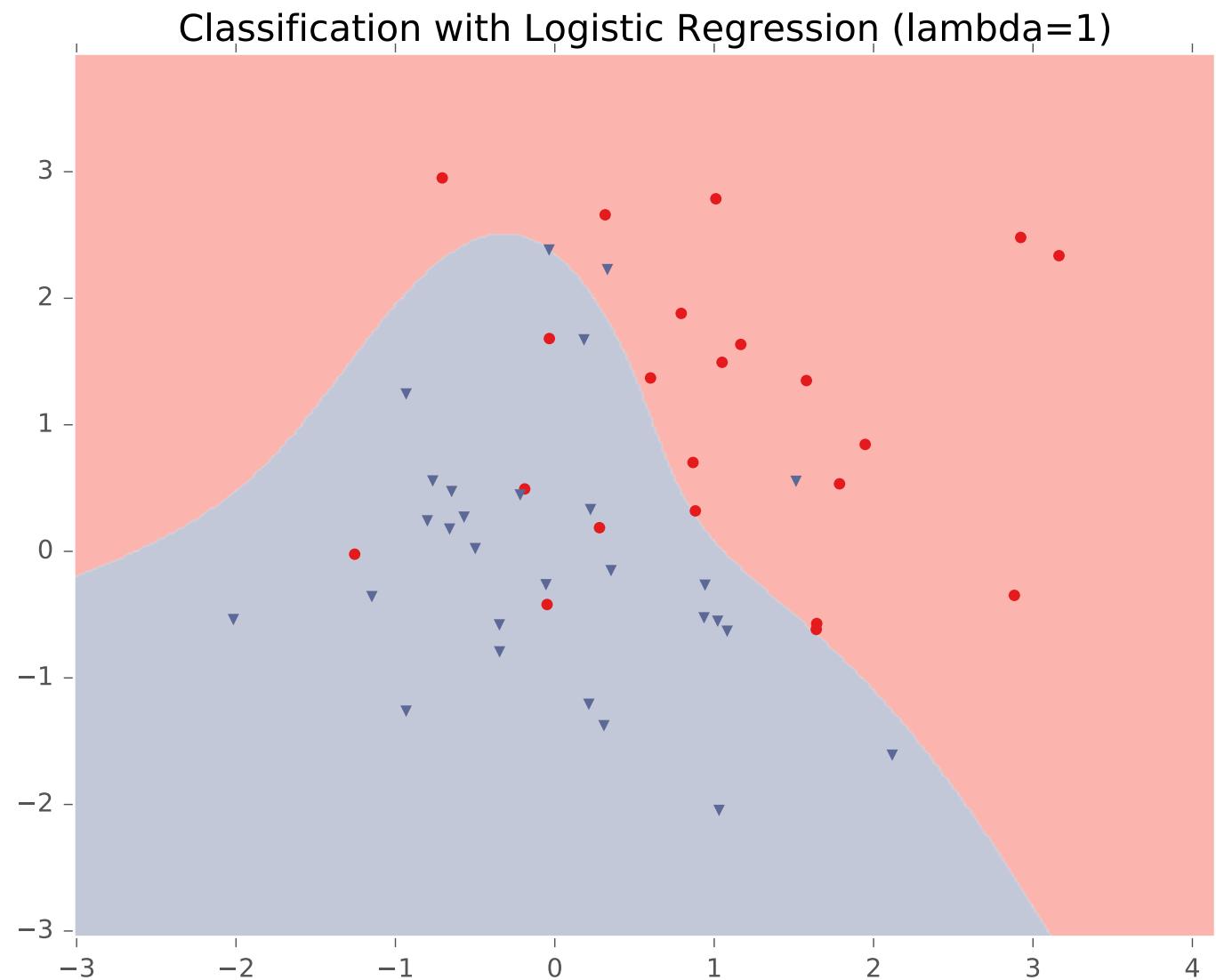
# Example: Logistic Regression



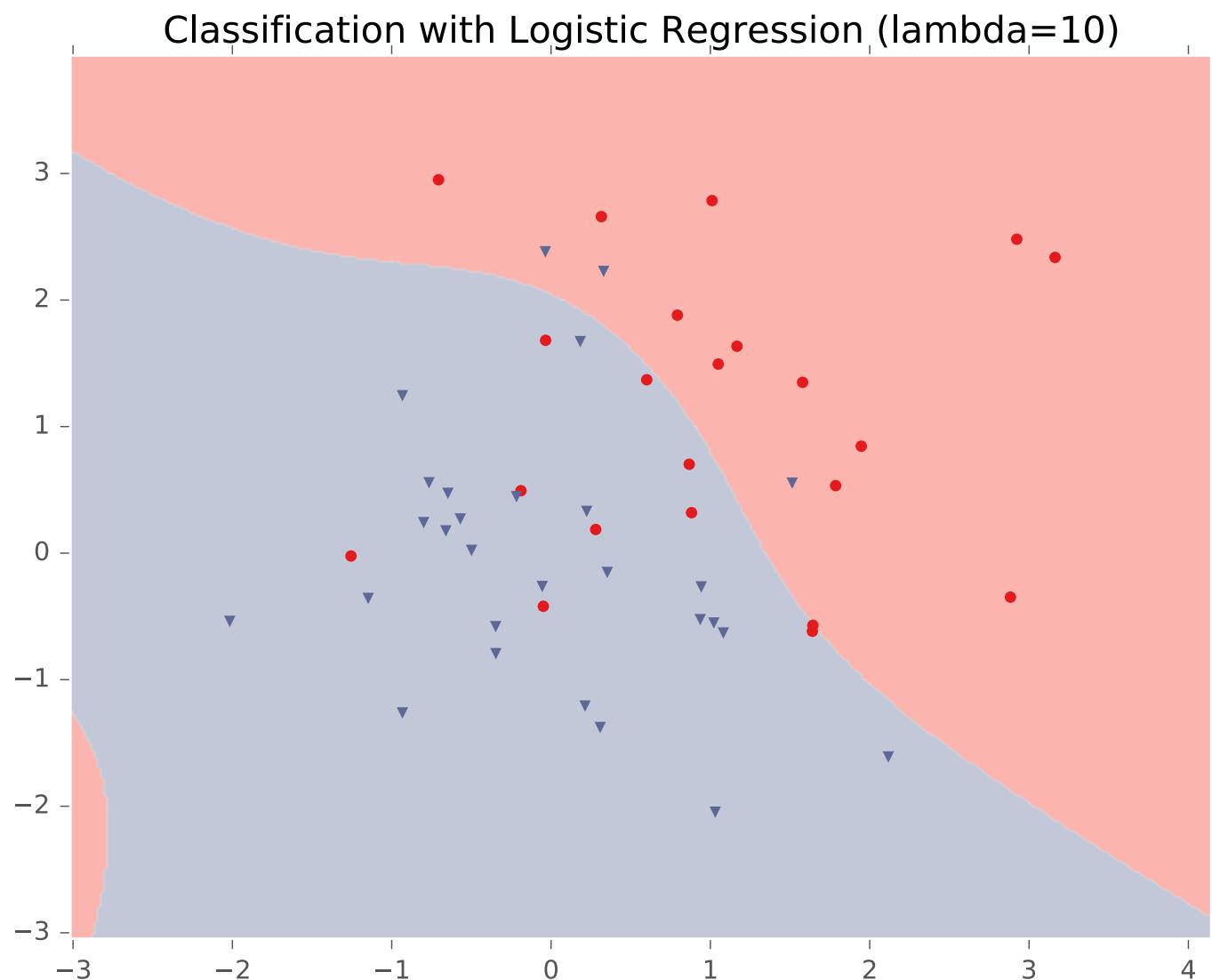
# Example: Logistic Regression



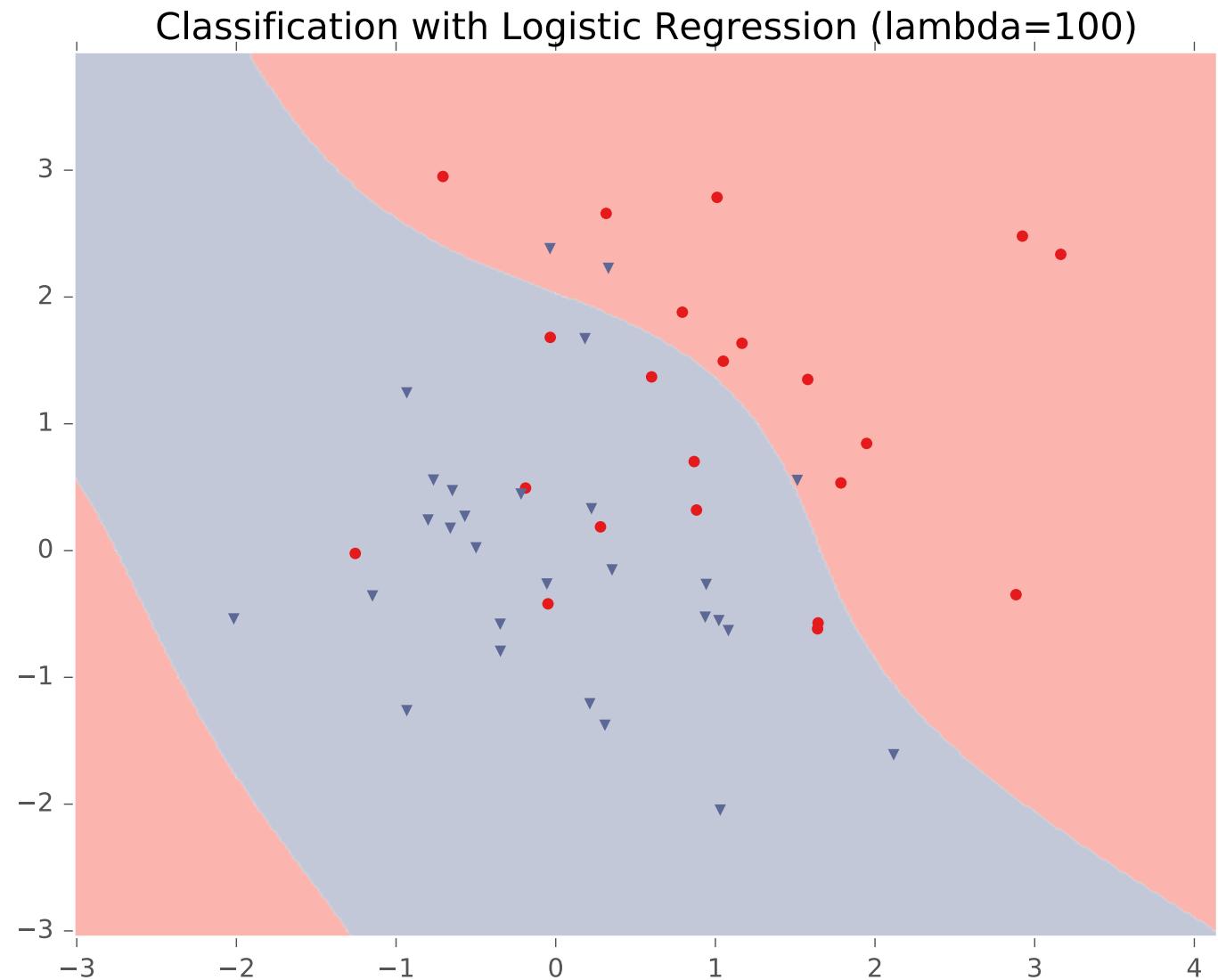
# Example: Logistic Regression



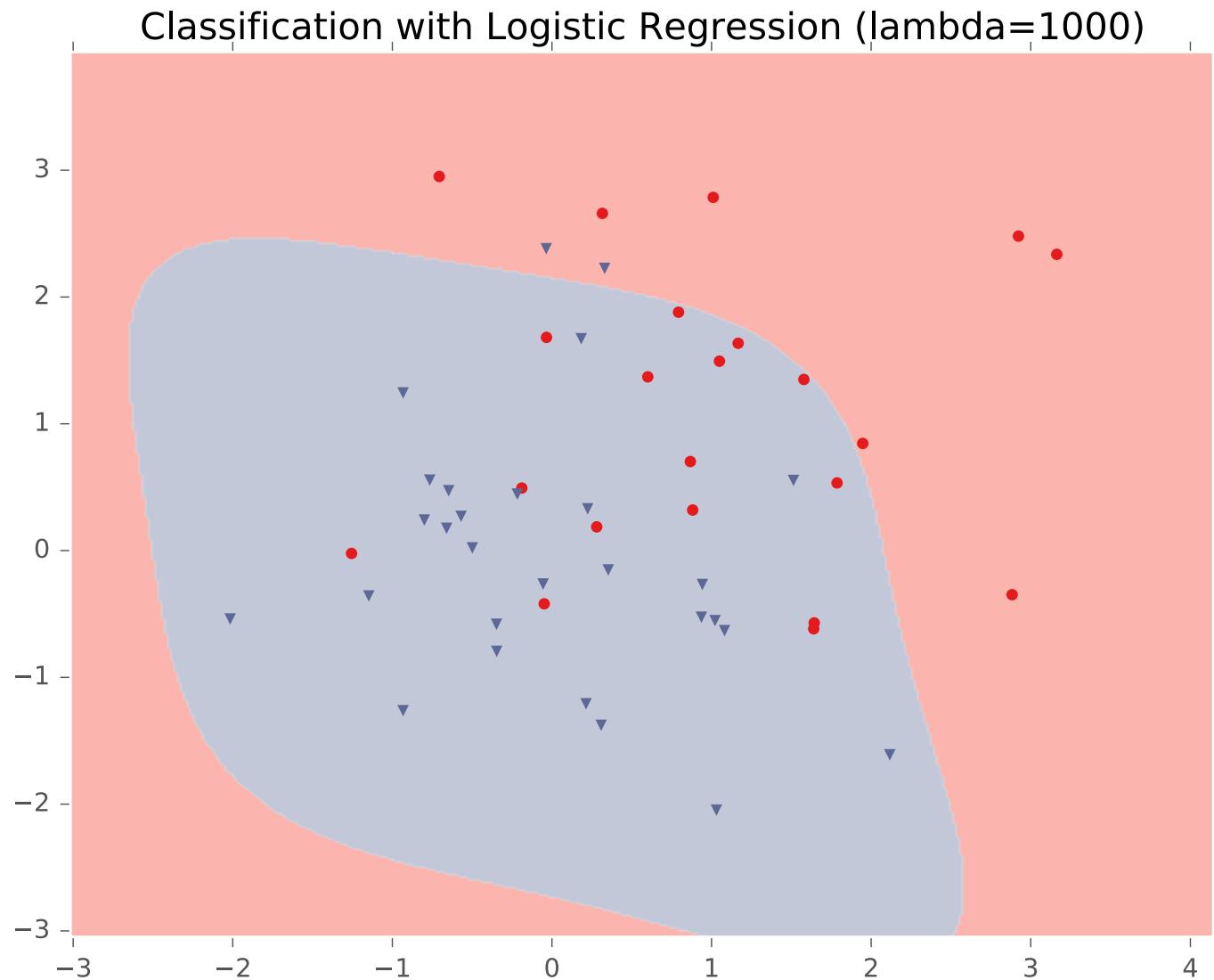
# Example: Logistic Regression



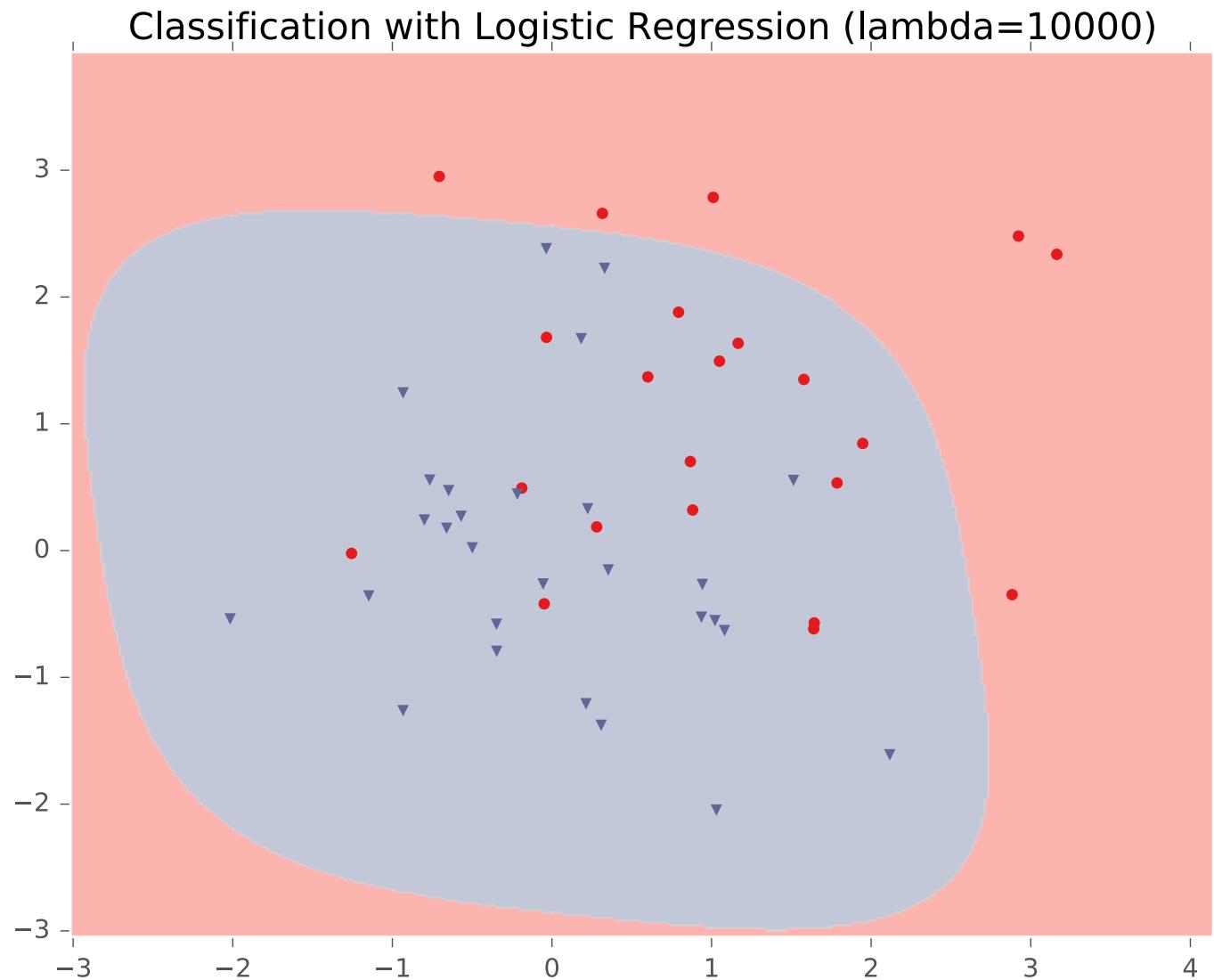
# Example: Logistic Regression



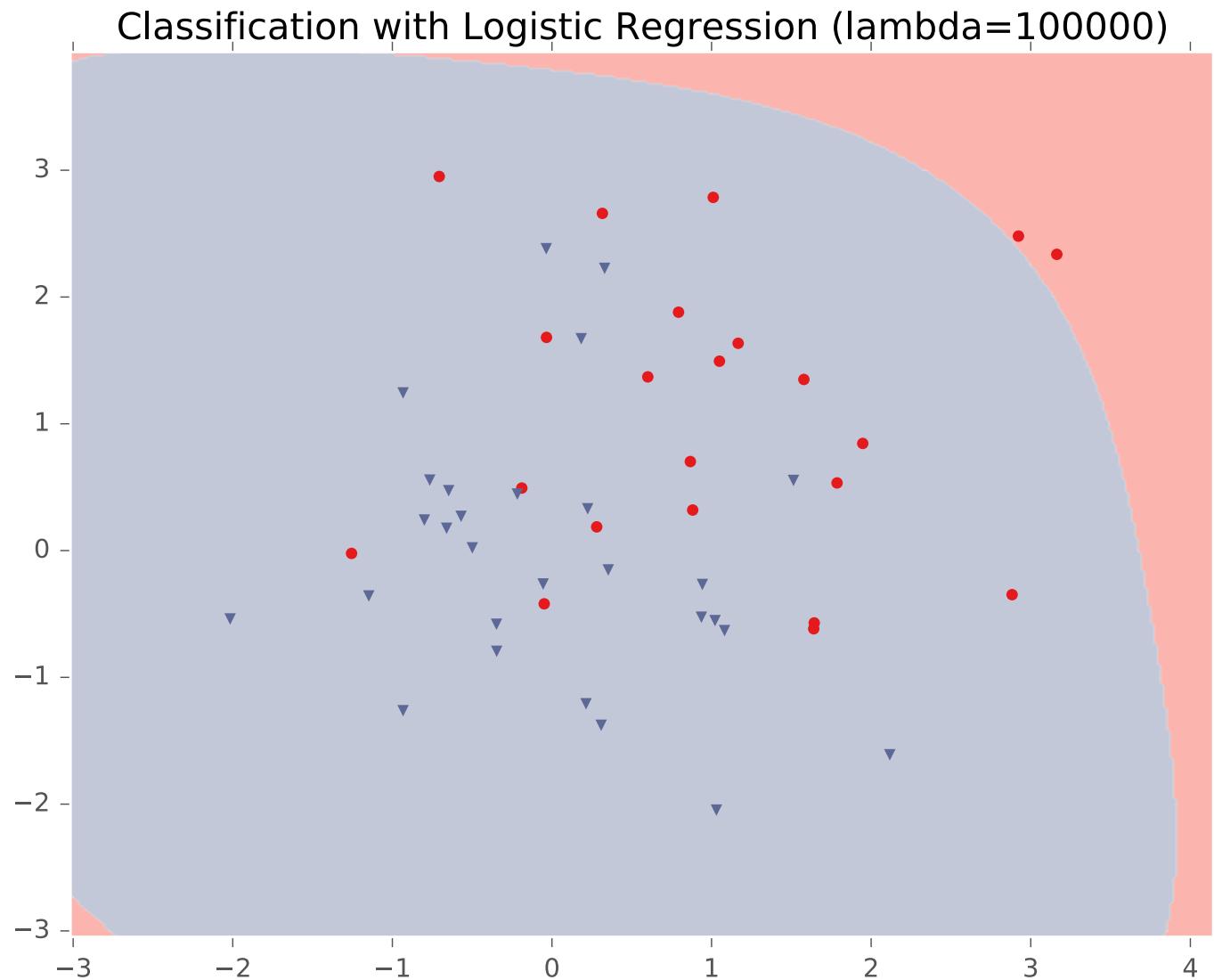
# Example: Logistic Regression



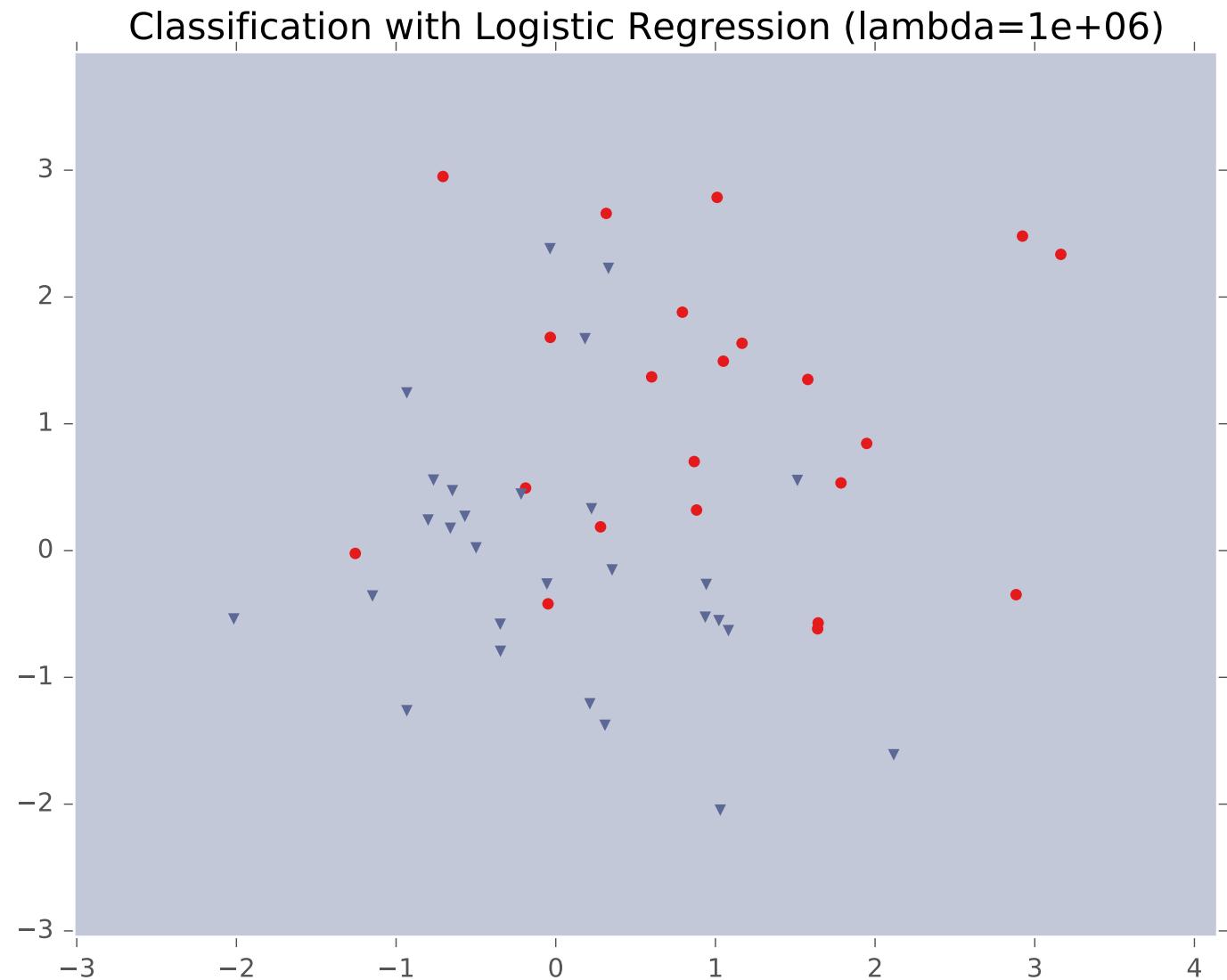
# Example: Logistic Regression



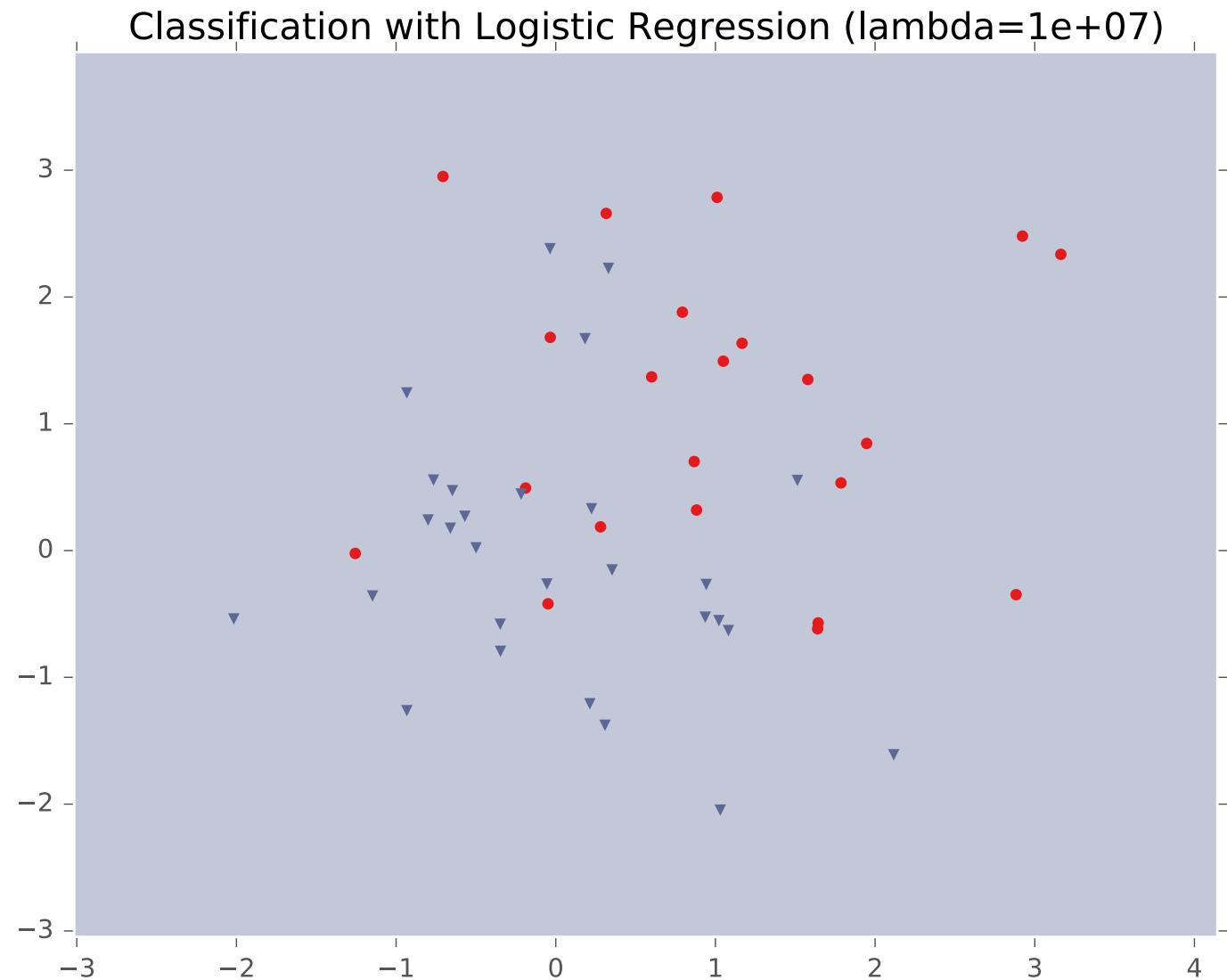
# Example: Logistic Regression



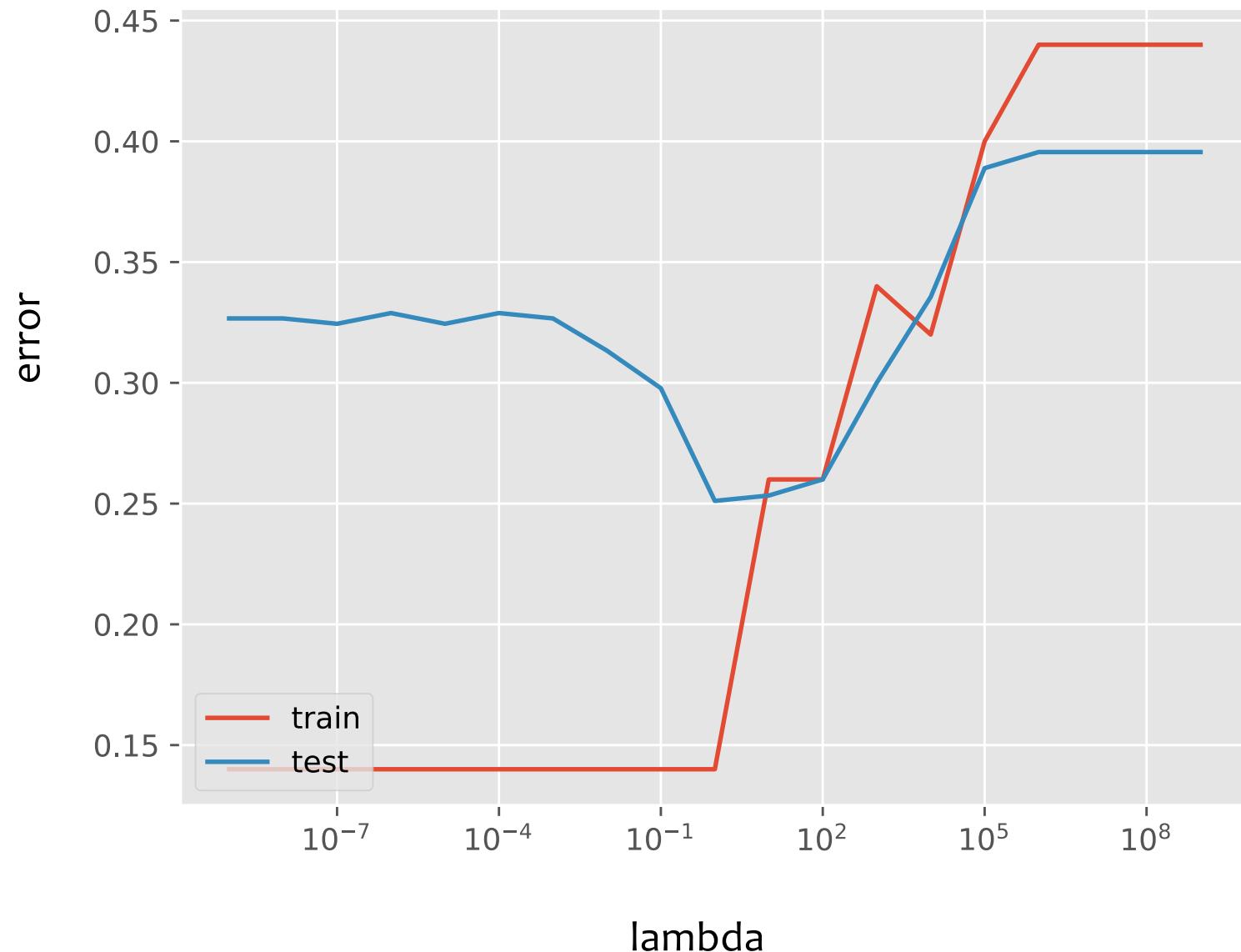
# Example: Logistic Regression



# Example: Logistic Regression



# Example: Logistic Regression



# **OPTIMIZATION FOR L<sub>1</sub> REGULARIZATION**

# Optimization for L1 Regularization

Can we apply SGD to the LASSO learning problem?

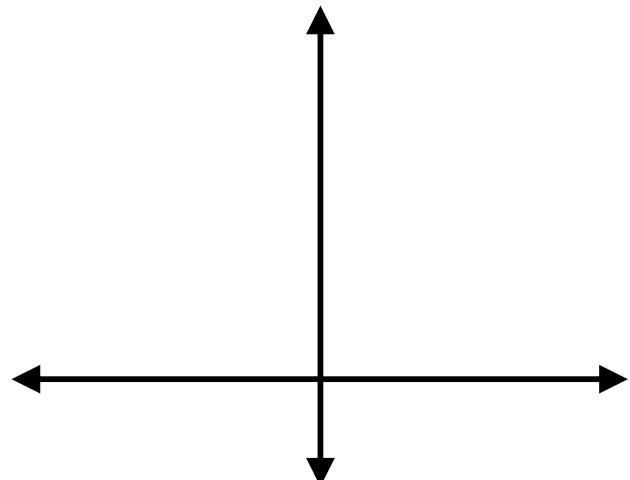
$$\operatorname{argmin}_{\theta} J_{\text{LASSO}}(\theta)$$

$$\begin{aligned} J_{\text{LASSO}}(\theta) &= J(\theta) + \boxed{\lambda ||\theta||_1} \\ &= \frac{1}{2} \sum_{i=1}^N (\theta^T \mathbf{x}^{(i)} - y^{(i)})^2 + \boxed{\lambda \sum_{k=1}^K |\theta_k|} \end{aligned}$$

# Optimization for L1 Regularization

- Consider the absolute value function:

$$r(\theta) = \lambda \sum_{k=1}^K |\theta_k|$$



- The L1 penalty is subdifferentiable (i.e. not differentiable at 0)

**Def:** A vector  $g \in \mathbb{R}^M$  is called a **subgradient** of a function  $f(\mathbf{x}) : \mathbb{R}^M \rightarrow \mathbb{R}$  at the point  $\mathbf{x}$  if, for all  $\mathbf{x}' \in \mathbb{R}^M$ , we have:

$$f(\mathbf{x}') \geq f(\mathbf{x}) + \mathbf{g}^T (\mathbf{x}' - \mathbf{x})$$

# Optimization for L1 Regularization

- The L1 penalty is subdifferentiable (i.e. not differentiable at 0)
- An array of optimization algorithms exist to handle this issue:
  - Subgradient descent
  - Stochastic subgradient descent
  - Coordinate Descent
  - Orthant-Wise Limited memory Quasi-Newton (OWL-QN) (Andrew & Gao, 2007) and provably convergent variants
  - Block coordinate Descent (Tseng & Yun, 2009)
  - Sparse Reconstruction by Separable Approximation (SpaRSA) (Wright et al., 2009)
  - Fast Iterative Shrinkage Thresholding Algorithm (FISTA) (Beck & Teboulle, 2009)



Basically the same as GD and SGD, but you use one of the subgradients when necessary

# Regularization as MAP

- L1 and L2 regularization can be interpreted as **maximum a-posteriori (MAP) estimation** of the parameters
- To be discussed later in the course...

# Takeaways

1. **Nonlinear basis functions** allow **linear models** (e.g. Linear Regression, Logistic Regression) to capture **nonlinear** aspects of the original input
2. Nonlinear features are **require no changes to the model** (i.e. just preprocessing)
3. **Regularization** helps to avoid **overfitting**
4. **Regularization** and **MAP estimation** are equivalent for appropriately chosen priors

# Feature Engineering / Regularization Objectives

You should be able to...

- Engineer appropriate features for a new task
- Use feature selection techniques to identify and remove irrelevant features
- Identify when a model is overfitting
- Add a regularizer to an existing objective in order to combat overfitting
- Explain why we should **not** regularize the bias term
- Convert linearly inseparable dataset to a linearly separable dataset in higher dimensions
- Describe feature engineering in common application areas

# **NEURAL NETWORKS**

## Background

# A Recipe for Machine Learning

1. Given training data:

$$\{\mathbf{x}_i, \mathbf{y}_i\}_{i=1}^N$$

2. Choose each of these:

- Decision function

$$\hat{\mathbf{y}} = f_{\theta}(\mathbf{x}_i)$$

- Loss function

$$\ell(\hat{\mathbf{y}}, \mathbf{y}_i) \in \mathbb{R}$$

Face



Face



Not a face



**Examples:** Linear regression,  
Logistic regression, Neural Network

**Examples:** Mean-squared error,  
Cross Entropy

## Background

# A Recipe for Machine Learning

1. Given training data:

$$\{\mathbf{x}_i, \mathbf{y}_i\}_{i=1}^N$$

2. Choose each of these:

- Decision function

$$\hat{\mathbf{y}} = f_{\boldsymbol{\theta}}(\mathbf{x}_i)$$

- Loss function

$$\ell(\hat{\mathbf{y}}, \mathbf{y}_i) \in \mathbb{R}$$

3. Define goal:

$$\boldsymbol{\theta}^* = \arg \min_{\boldsymbol{\theta}} \sum_{i=1}^N \ell(f_{\boldsymbol{\theta}}(\mathbf{x}_i), \mathbf{y}_i)$$

4. Train with SGD:

(take small steps  
opposite the gradient)

$$\boldsymbol{\theta}^{(t+1)} = \boldsymbol{\theta}^{(t)} - \eta_t \nabla \ell(f_{\boldsymbol{\theta}}(\mathbf{x}_i), \mathbf{y}_i)$$

# Background

1. Given training data

$$\{\mathbf{x}_i, \mathbf{y}_i\}_{i=1}^N$$

2. Choose each of the

- Decision function

$$\hat{\mathbf{y}} = f_{\boldsymbol{\theta}}(\mathbf{x}_i)$$

- Loss function

$$\ell(\hat{\mathbf{y}}, \mathbf{y}_i) \in \mathbb{R}$$

# A Recipe for Gradients

**Backpropagation** can compute this gradient!

And it's a **special case of a more general algorithm** called reverse-mode automatic differentiation that can compute the gradient of any differentiable function efficiently!

(opposite the gradient)

$$\boldsymbol{\theta}^{(t)} \rightarrow^{(t)} -\eta_t \nabla \ell(f_{\boldsymbol{\theta}}(\mathbf{x}_i), \mathbf{y}_i)$$

B

# A Recipe for

## Goals for Today's Lecture

1. 1. Explore a **new class of decision functions**  
(Neural Networks)
2. Consider **variants of this recipe** for training

2. Choose each of these.

– Decision function

$$\hat{y} = f_{\theta}(x_i)$$

– Loss function

$$\ell(\hat{y}, y_i) \in \mathbb{R}$$

4. Train with SGD:  
(take small steps  
opposite the gradient)

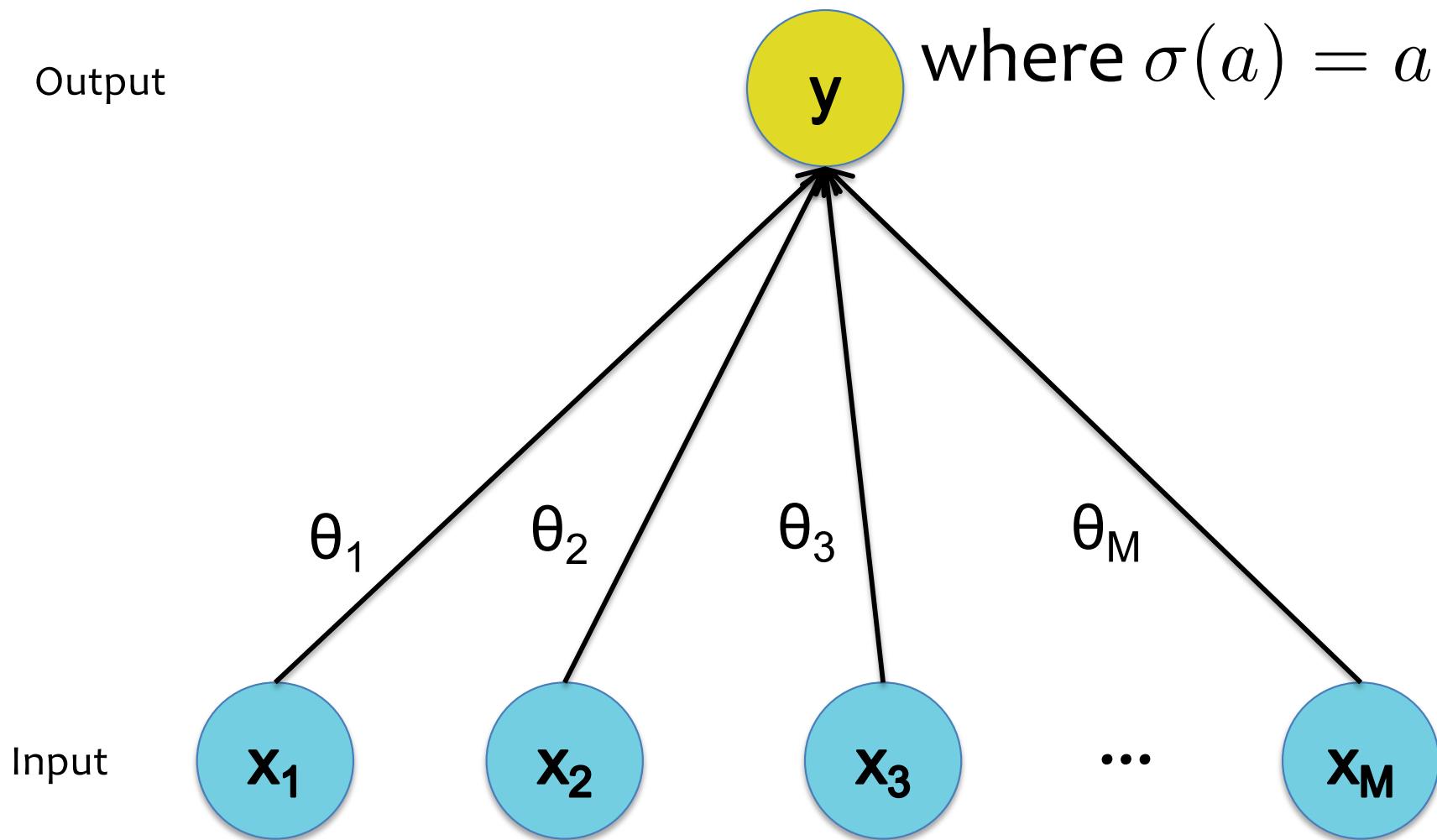
$$\theta^{(t+1)} = \theta^{(t)} - \eta_t \nabla \ell(f_{\theta}(x_i), y_i)$$

# Linear Regression

$$y = h_{\theta}(x) = \sigma(\theta^T x)$$

where  $\sigma(a) = a$

Output

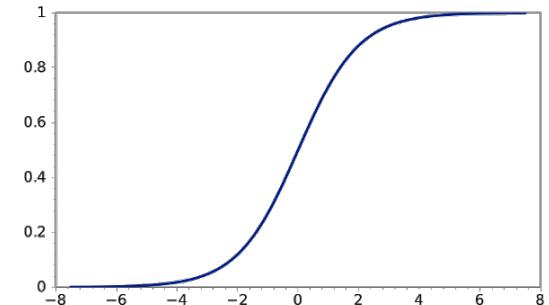
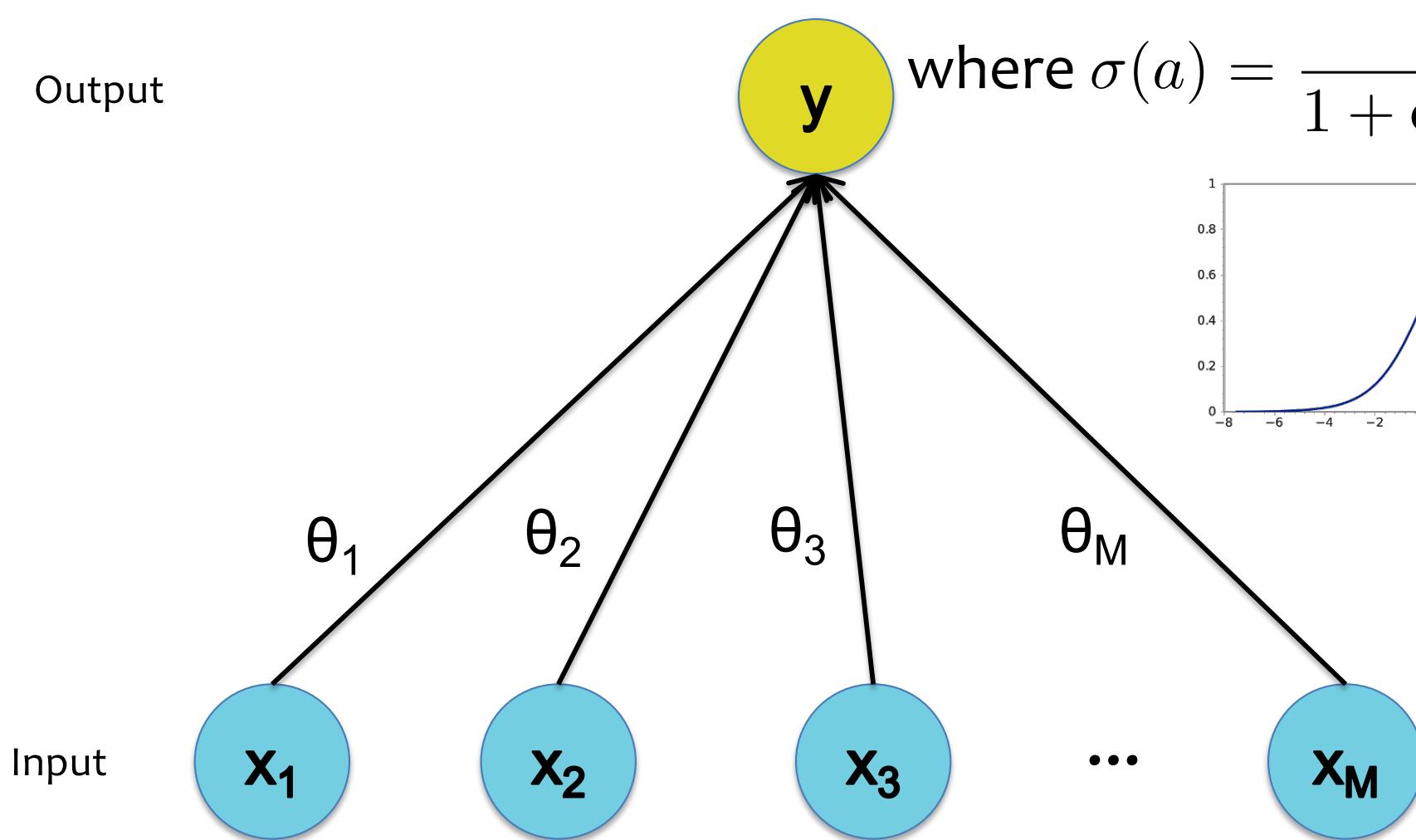


# Logistic Regression

$$y = h_{\theta}(x) = \sigma(\theta^T x)$$

where  $\sigma(a) = \frac{1}{1 + \exp(-a)}$

Output



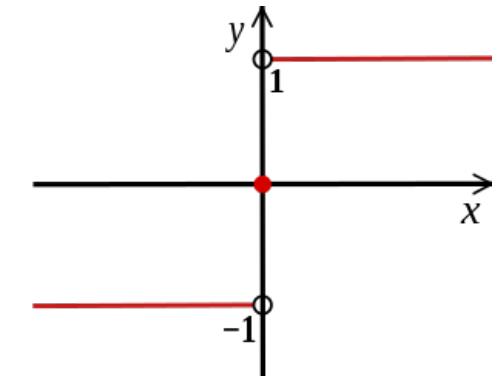
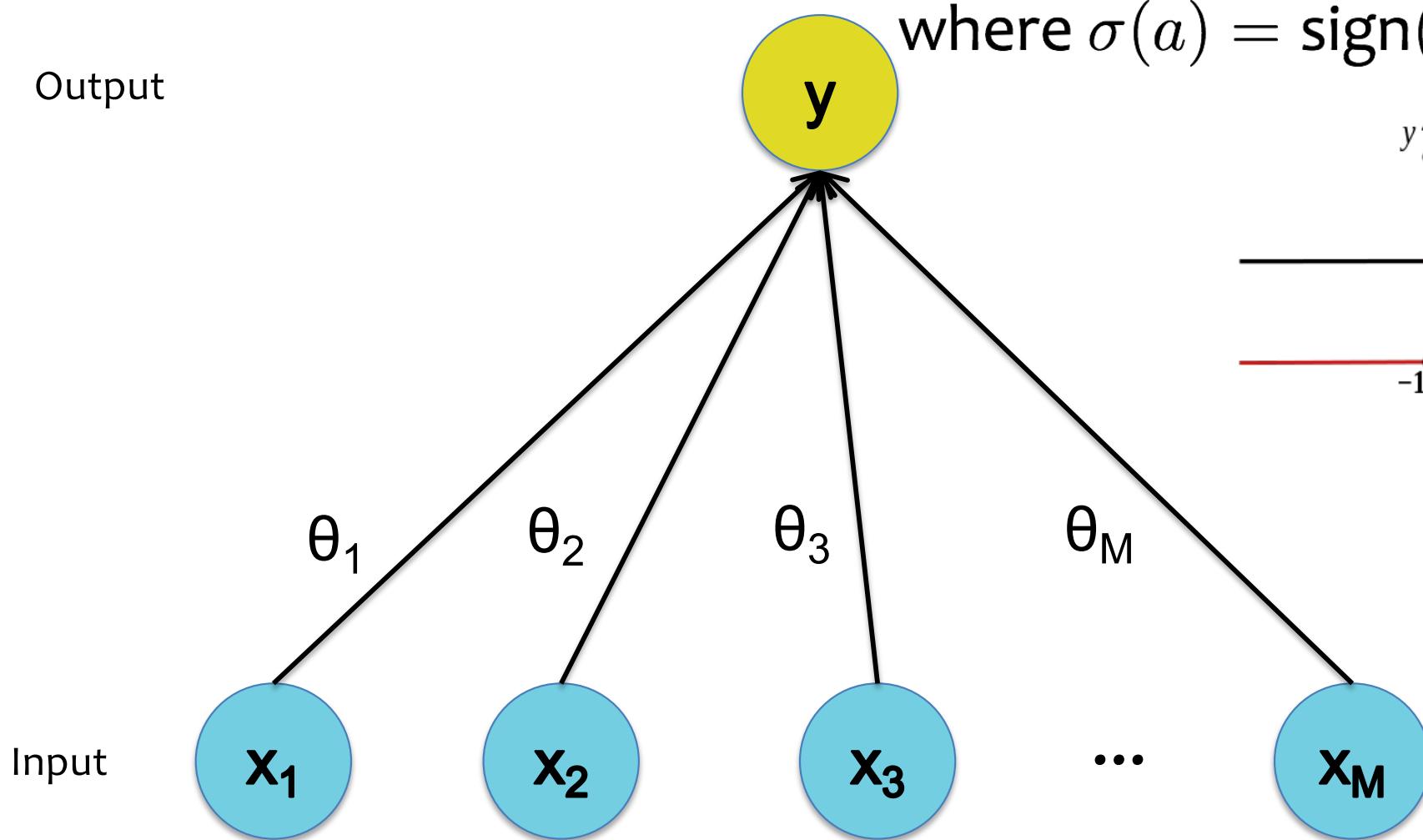
Input

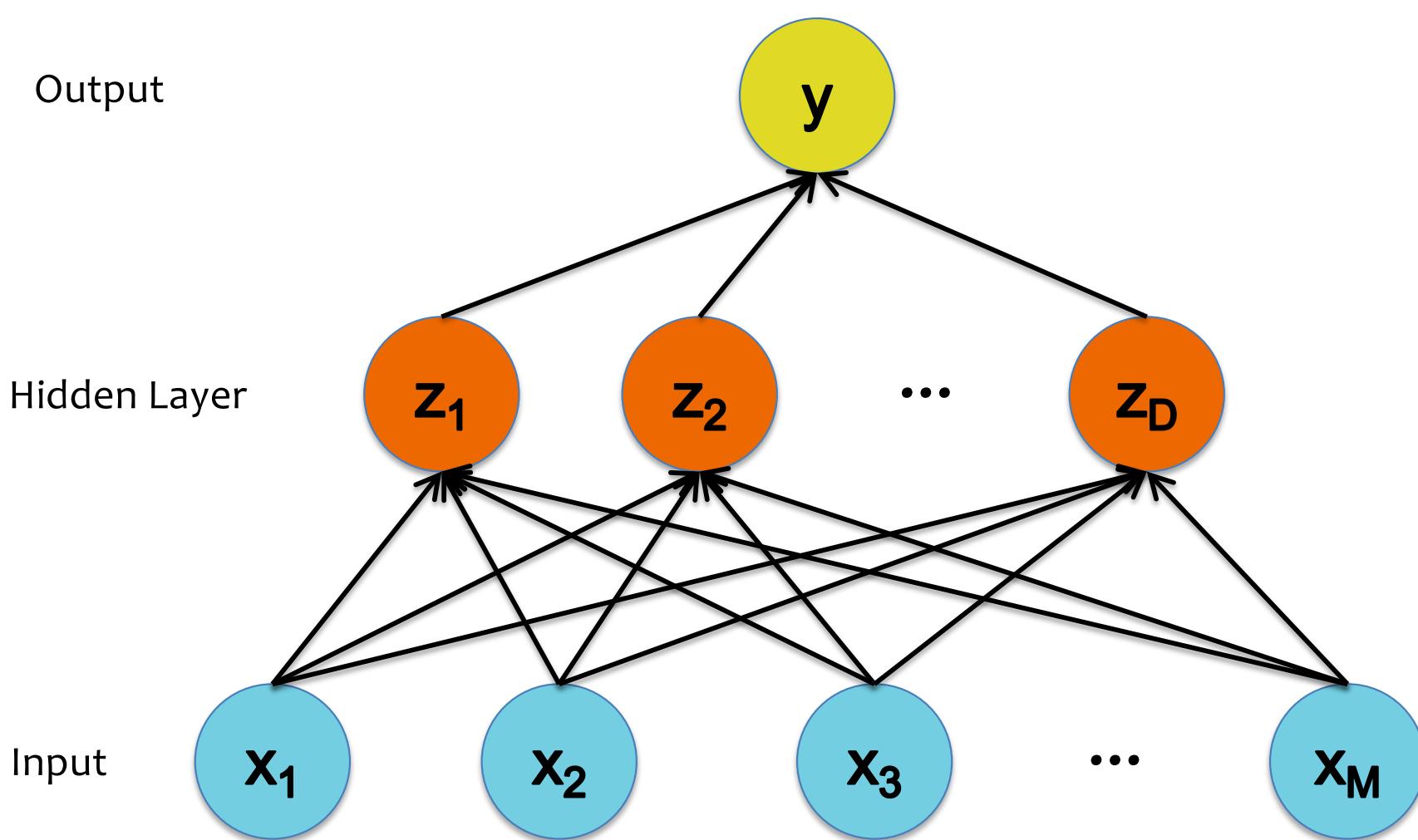
# Perceptron

$$y = h_{\theta}(x) = \sigma(\theta^T x)$$

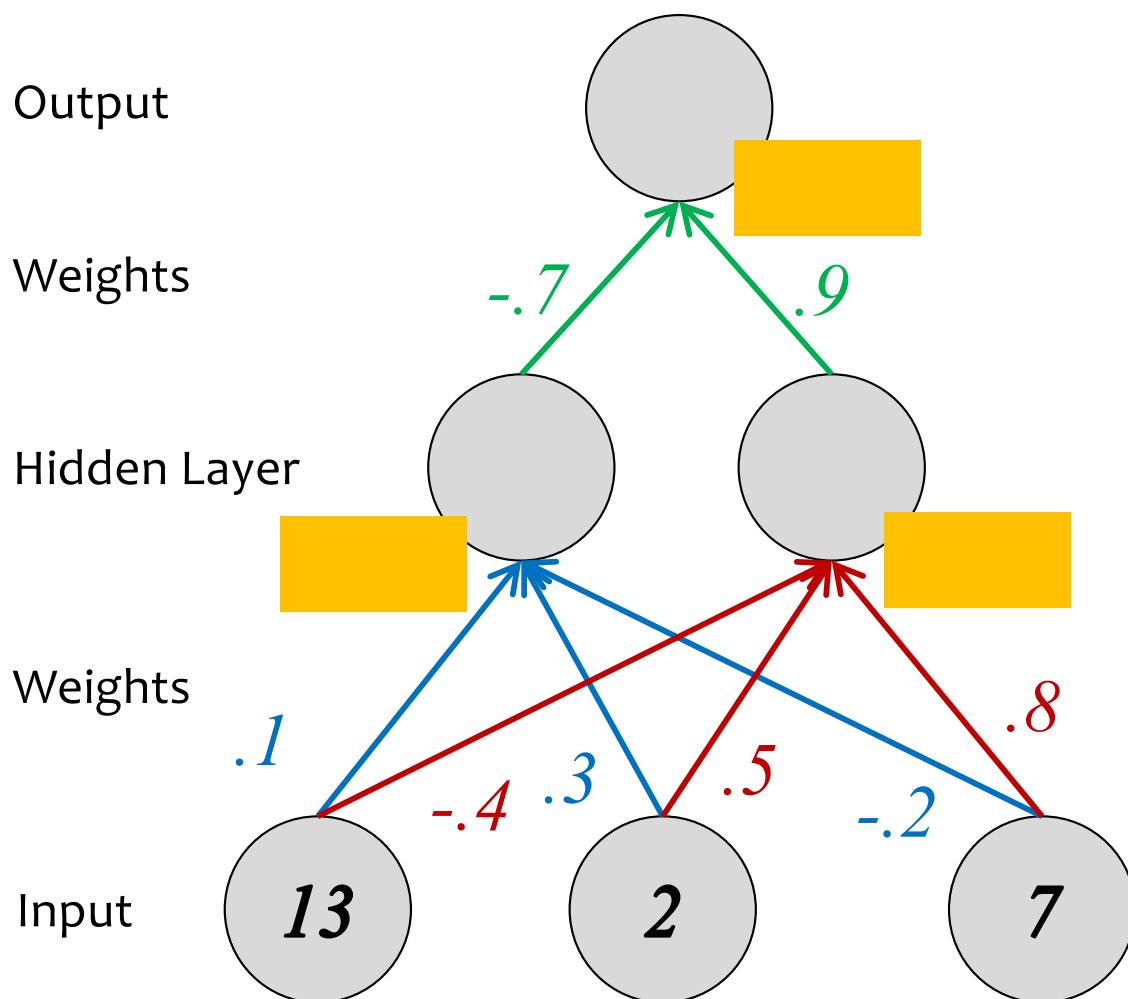
where  $\sigma(a) = \text{sign}(a)$

Output



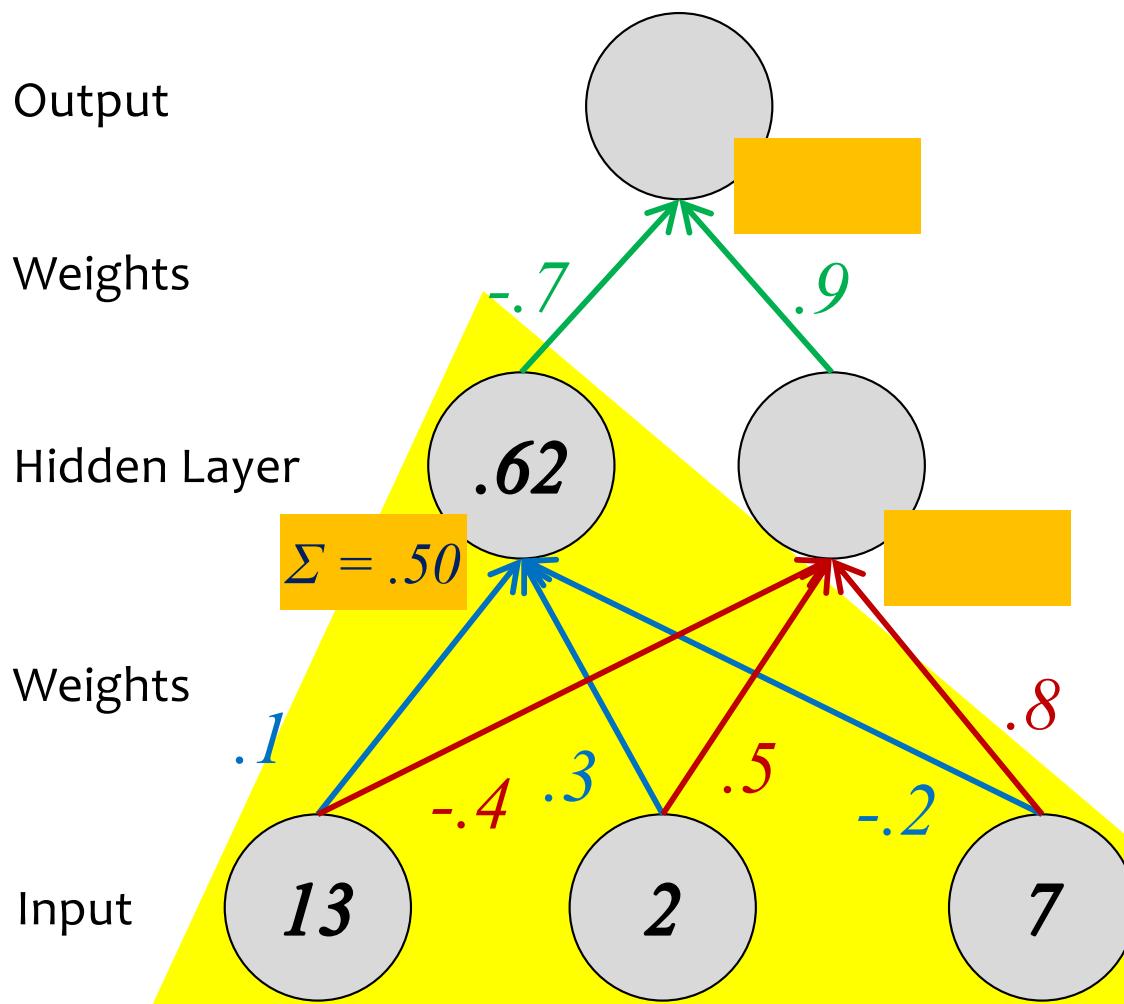


# **COMPONENTS OF A NEURAL NETWORK**



Suppose we already learned the weights of the neural network.

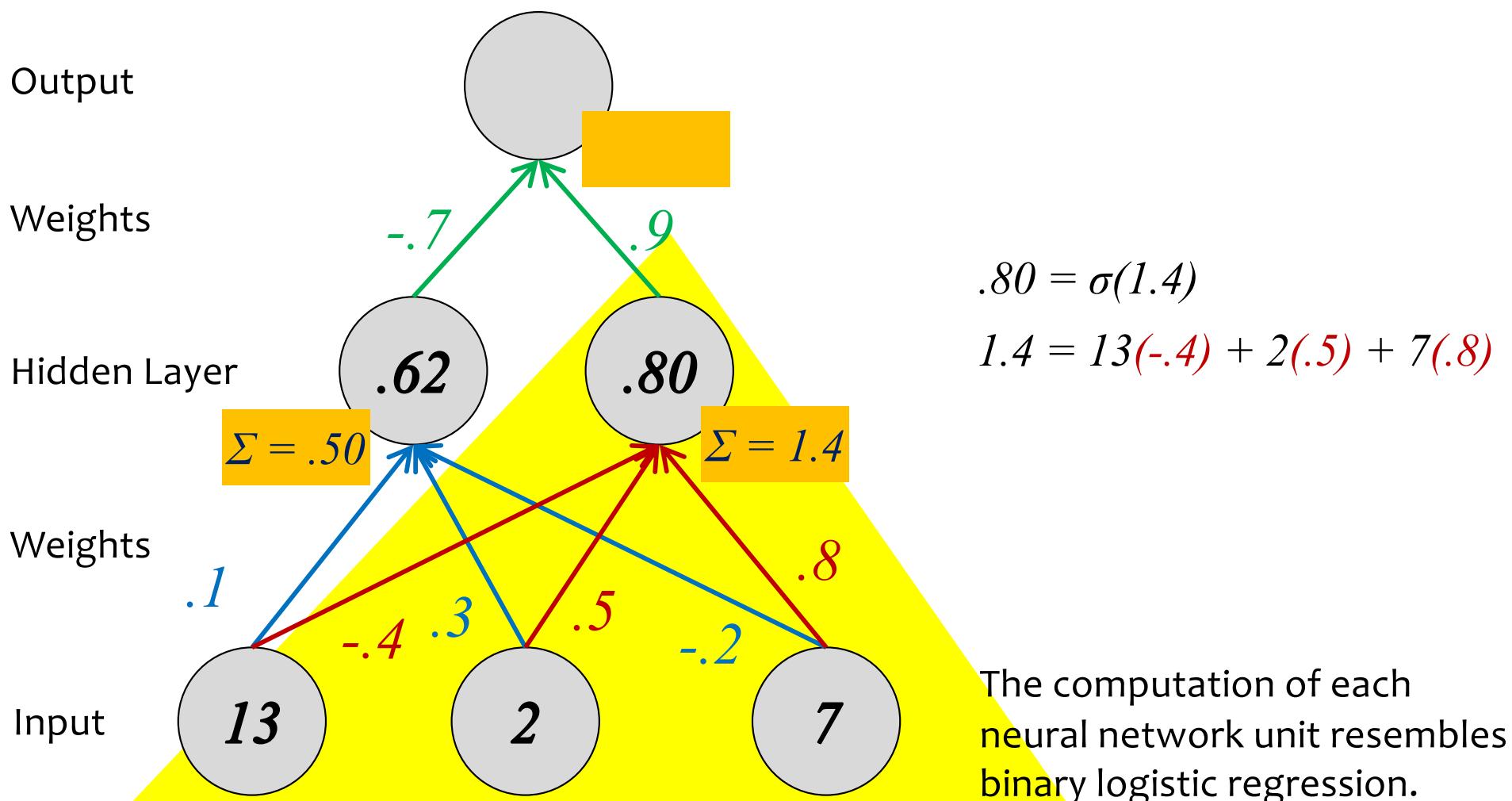
To make a new prediction, we take in some new features (aka. the input layer) and perform the feed-forward computation.



$$.62 = \sigma(.50)$$

$$.50 = 13(.1) + 2(.3) + 7(-.2)$$

The computation of each neural network unit resembles binary logistic regression.



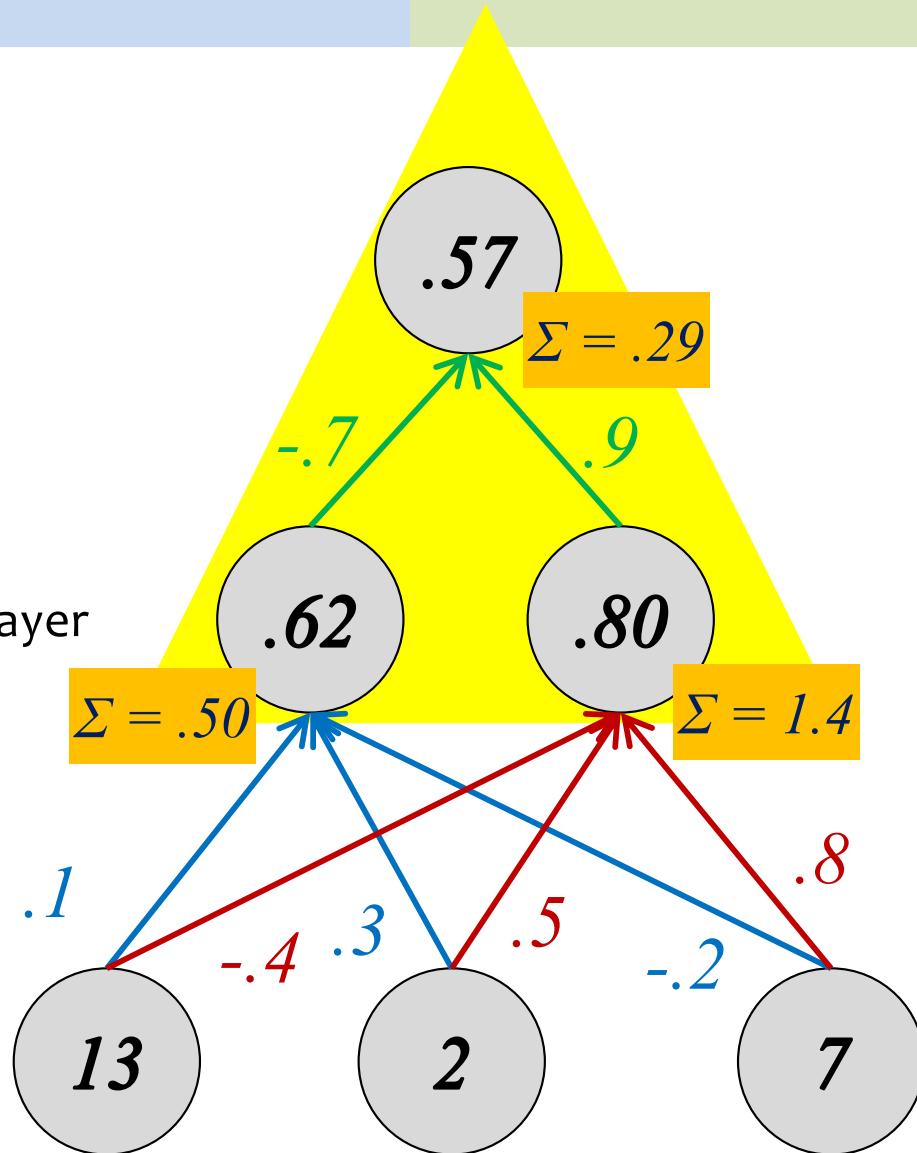
Output

Weights

Hidden Layer

Weights

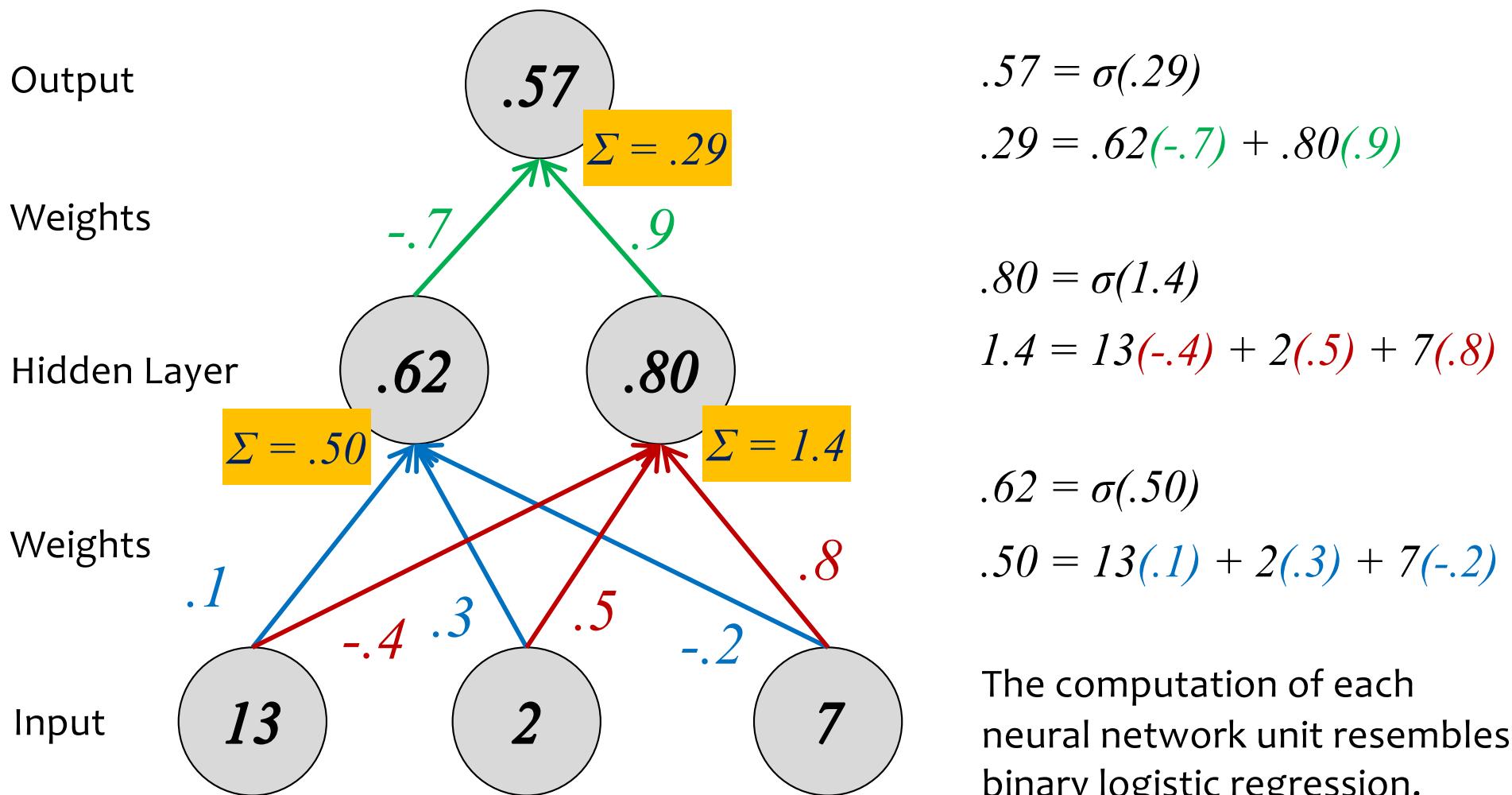
Input

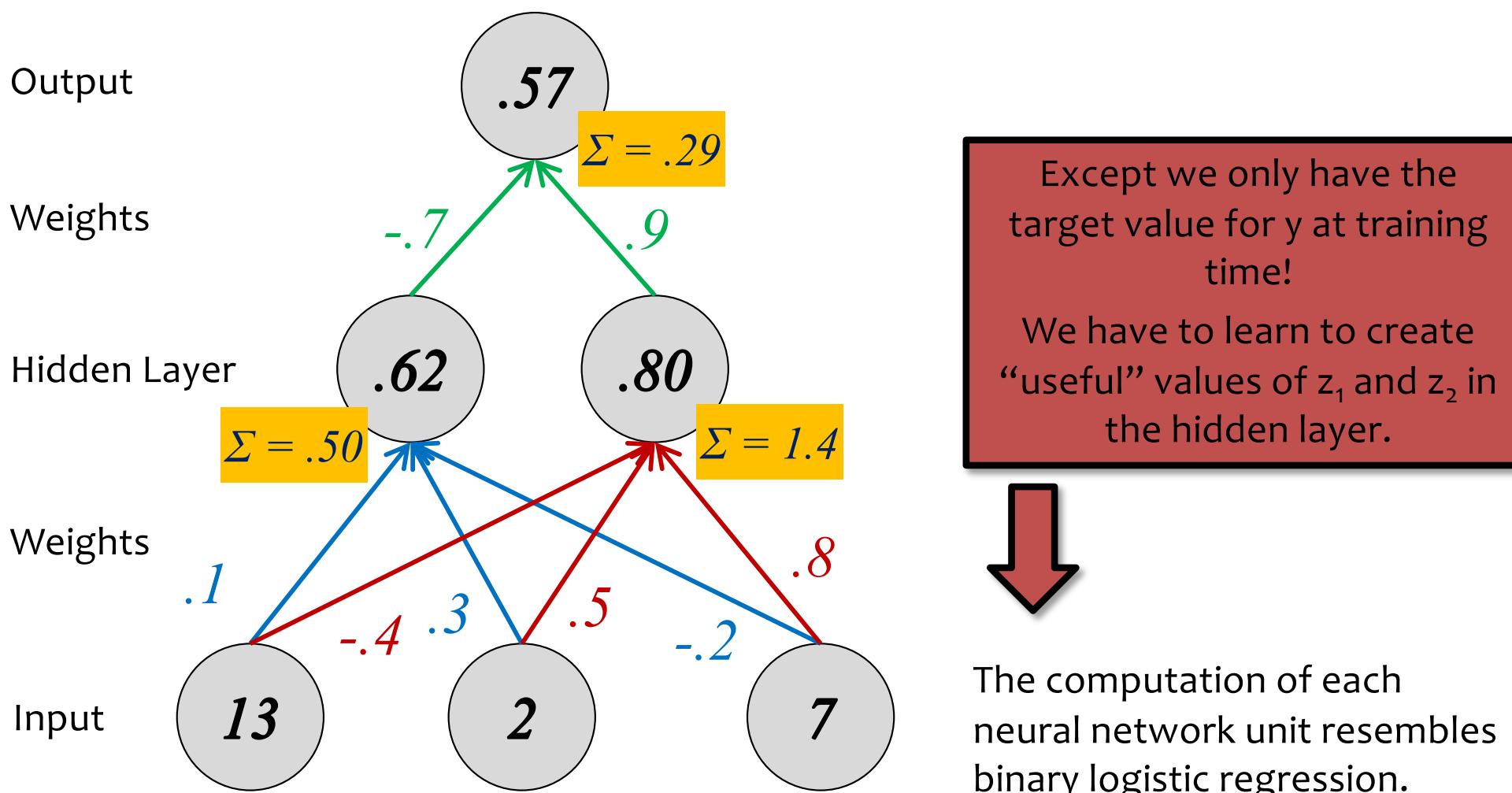


$$.57 = \sigma(.29)$$

$$.29 = .62(-.7) + .80(.9)$$

The computation of each neural network unit resembles binary logistic regression.





# From Biological to Artificial

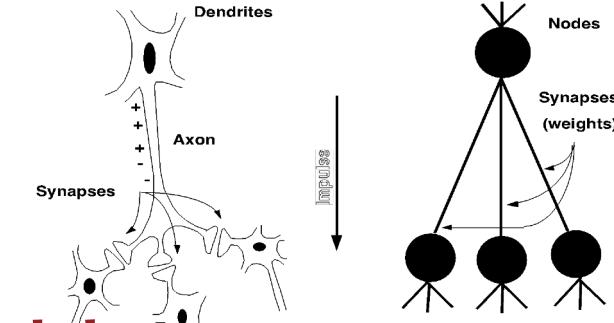
The motivation for Artificial Neural Networks comes from biology...

## Biological “Model”

- **Neuron:** an excitable cell
- **Synapse:** connection between neurons
- A neuron sends an **electrochemical pulse** along its synapses when a sufficient voltage change occurs
- **Biological Neural Network:** collection of neurons along some pathway through the brain

## Biological “Computation”

- Neuron switching time :  $\sim 0.001$  sec
- Number of neurons:  $\sim 10^{10}$
- Connections per neuron:  $\sim 10^{4-5}$
- Scene recognition time:  $\sim 0.1$  sec



## Artificial Model

- **Neuron:** node in a directed acyclic graph (DAG)
- **Weight:** multiplier on each edge
- **Activation Function:** nonlinear thresholding function, which allows a neuron to “fire” when the input value is sufficiently high
- **Artificial Neural Network:** collection of neurons into a DAG, which define some differentiable function

## Artificial Computation

- Many neuron-like threshold switching units
- Many weighted interconnections among units
- Highly parallel, distributed processes

# **DEFINING A 1-HIDDEN LAYER NEURAL NETWORK**

# Neural Networks

## *Chalkboard*

- Example: Neural Network w/1 Hidden Layer

Output

$$y = \sigma(\beta_1 z_1 + \beta_2 z_2)$$

Weights

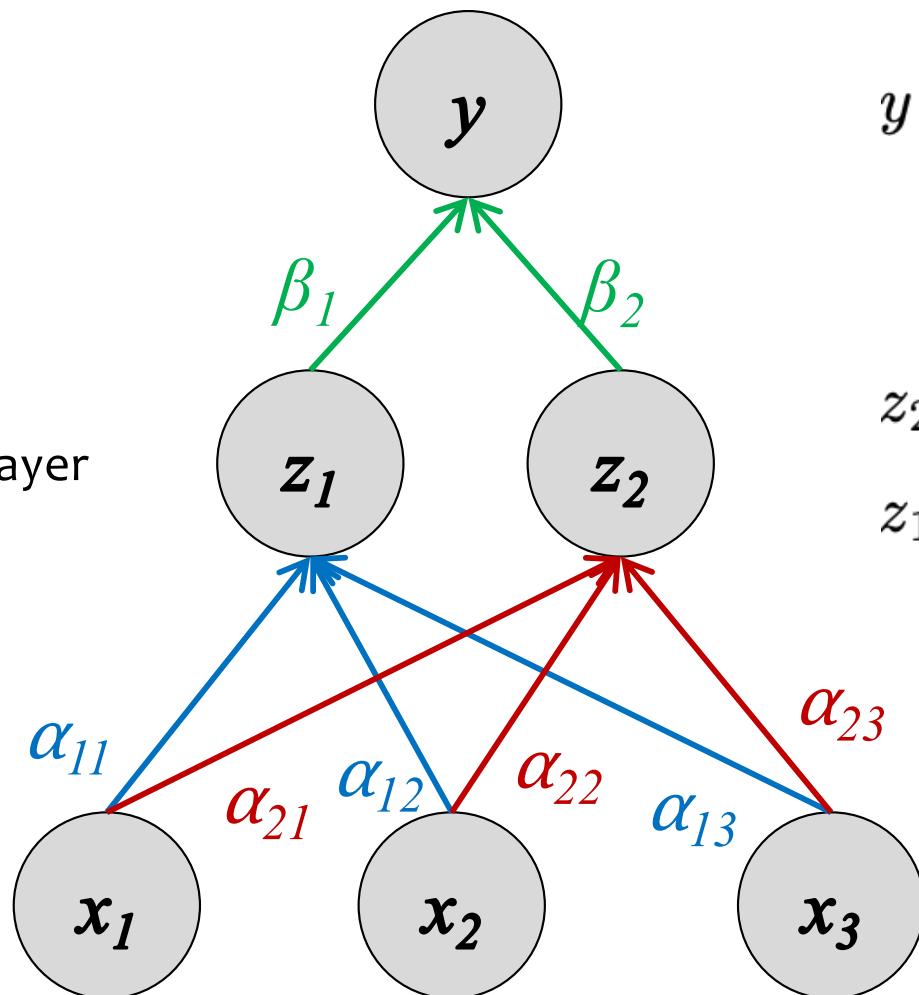
$$z_2 = \sigma(\alpha_{21}x_1 + \alpha_{22}x_2 + \alpha_{23}x_3)$$

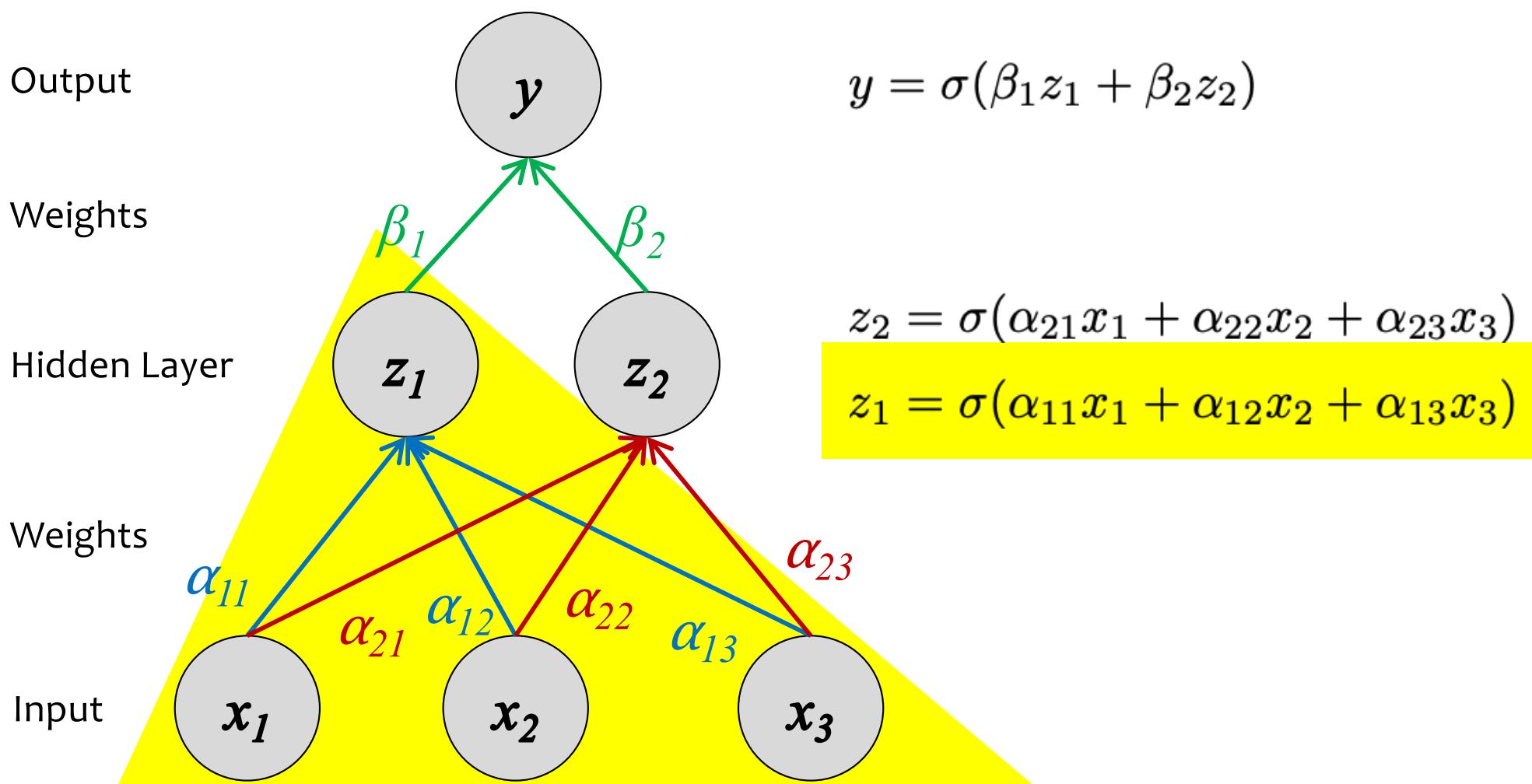
Hidden Layer

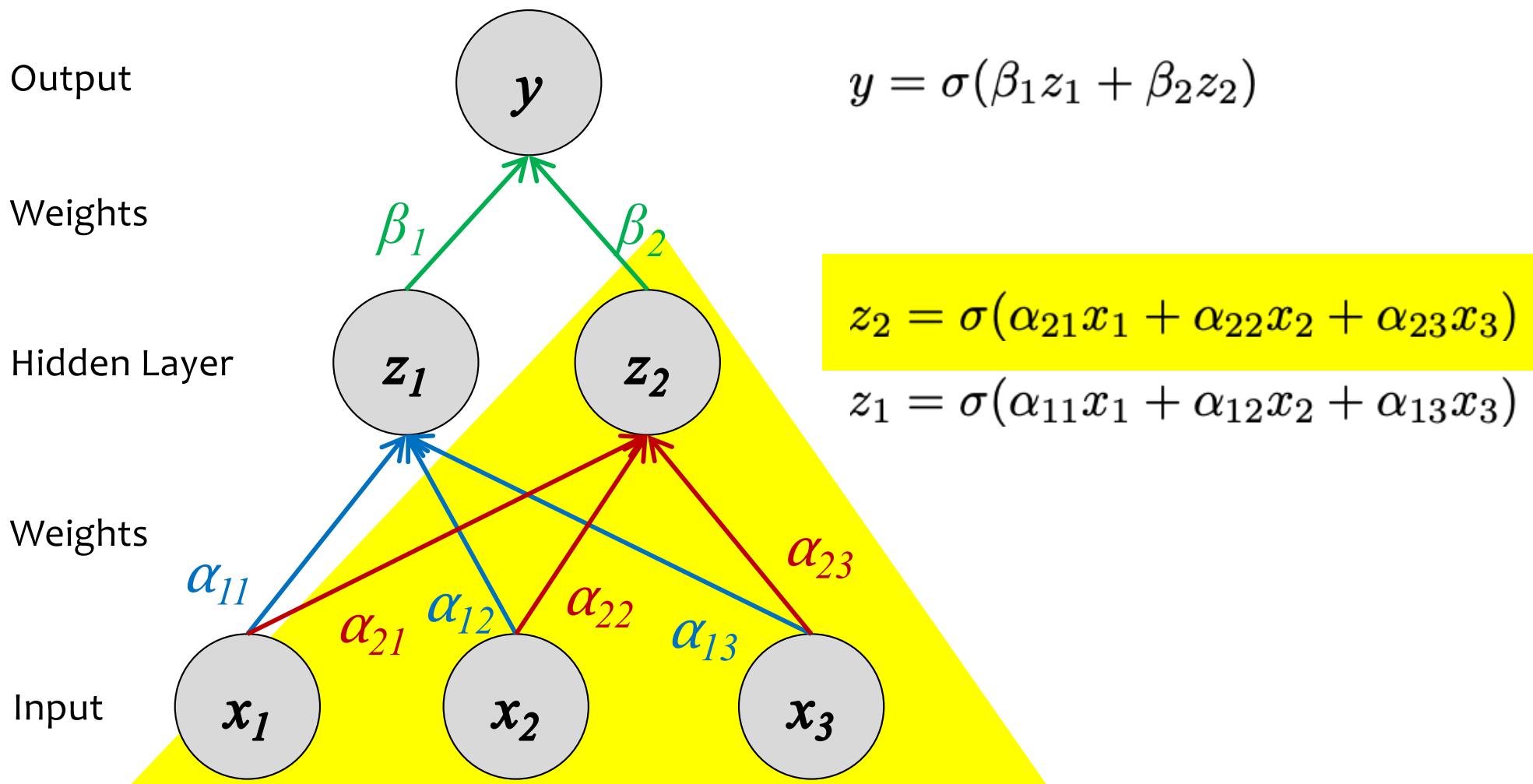
$$z_1 = \sigma(\alpha_{11}x_1 + \alpha_{12}x_2 + \alpha_{13}x_3)$$

Weights

Input







Output

$$y = \sigma(\beta_1 z_1 + \beta_2 z_2)$$

Weights

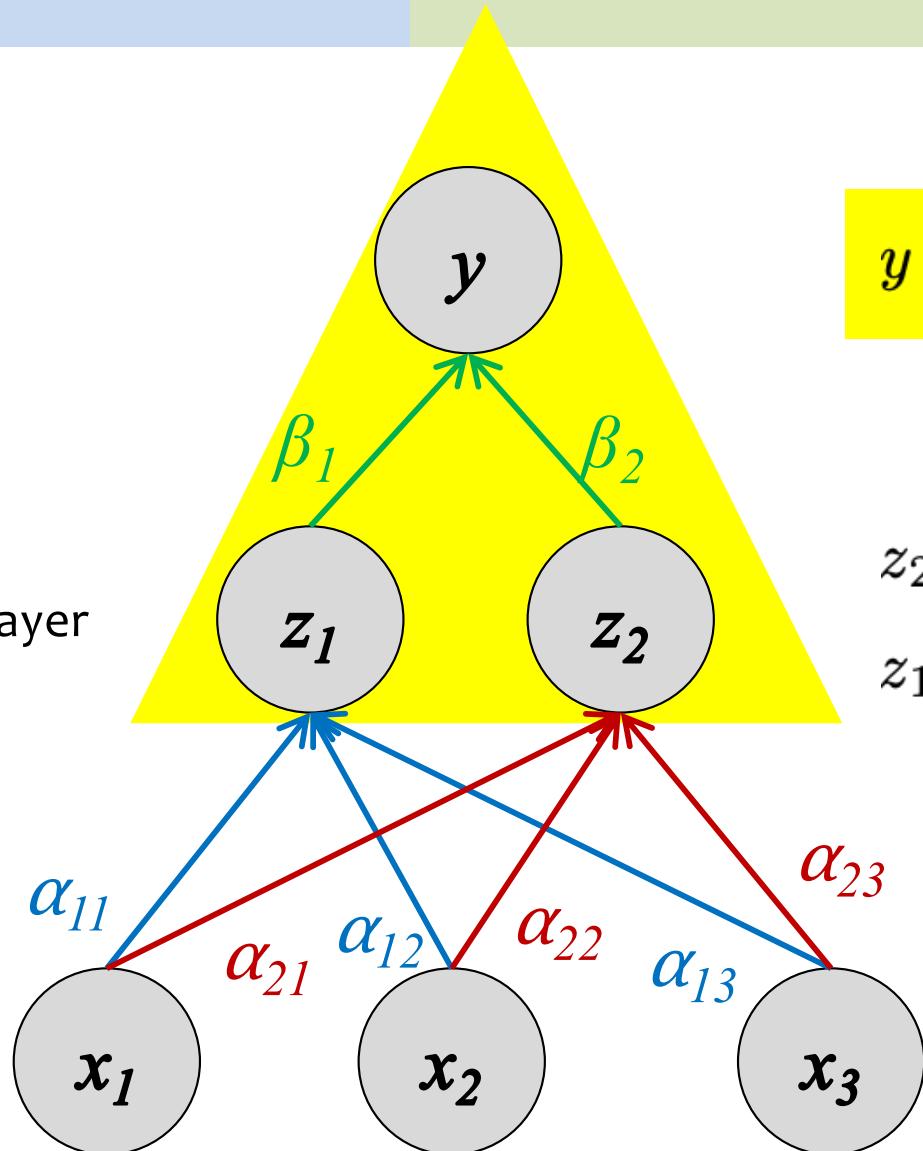
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$$z_1 = \sigma(\alpha_{11}x_1 + \alpha_{12}x_2 + \alpha_{13}x_3)$$

Hidden Layer

Weights

Input



Output

$$y = \sigma(\beta_1 z_1 + \beta_2 z_2)$$

Weights

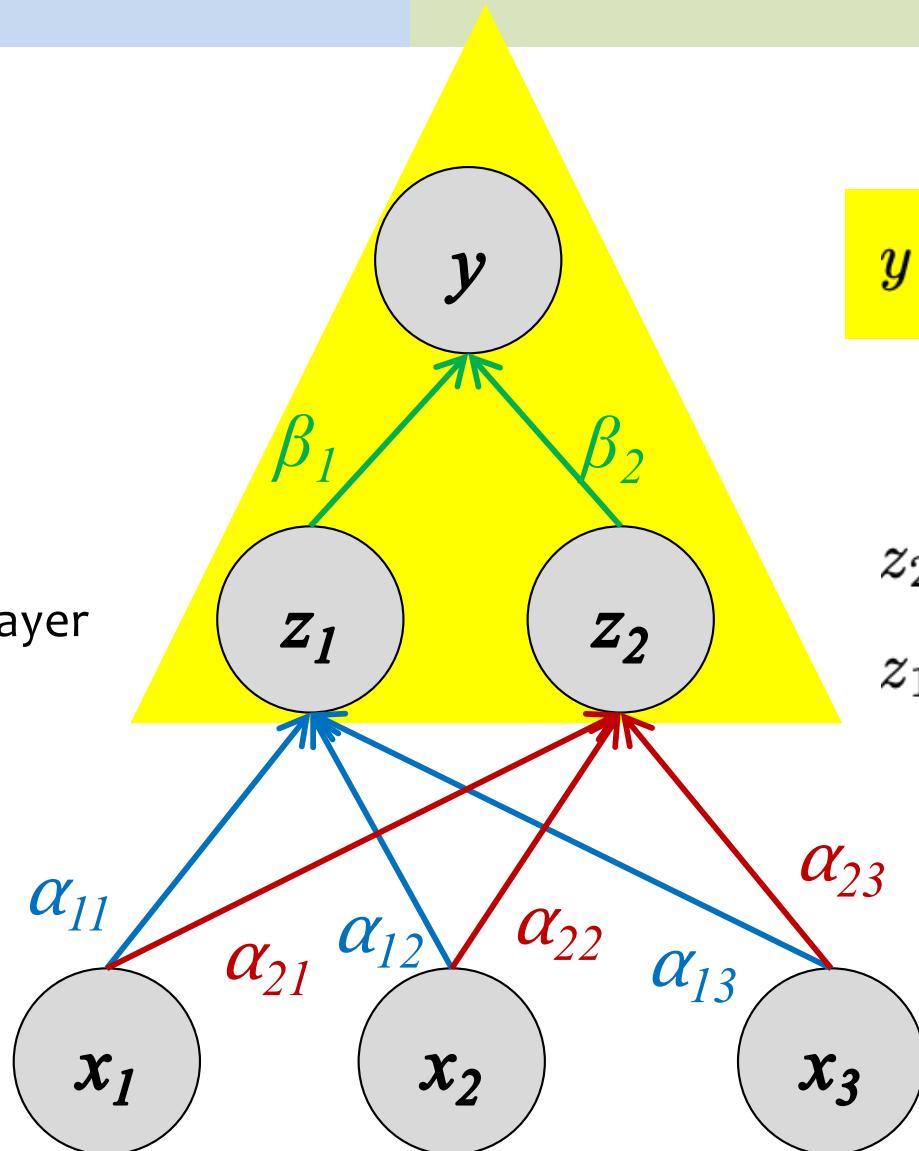
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Hidden Layer

$$z_1 = \sigma(\alpha_{11}x_1 + \alpha_{12}x_2 + \alpha_{13}x_3)$$

Weights

Input



# **NONLINEAR DECISION BOUNDARIES AND NEURAL NETWORKS**

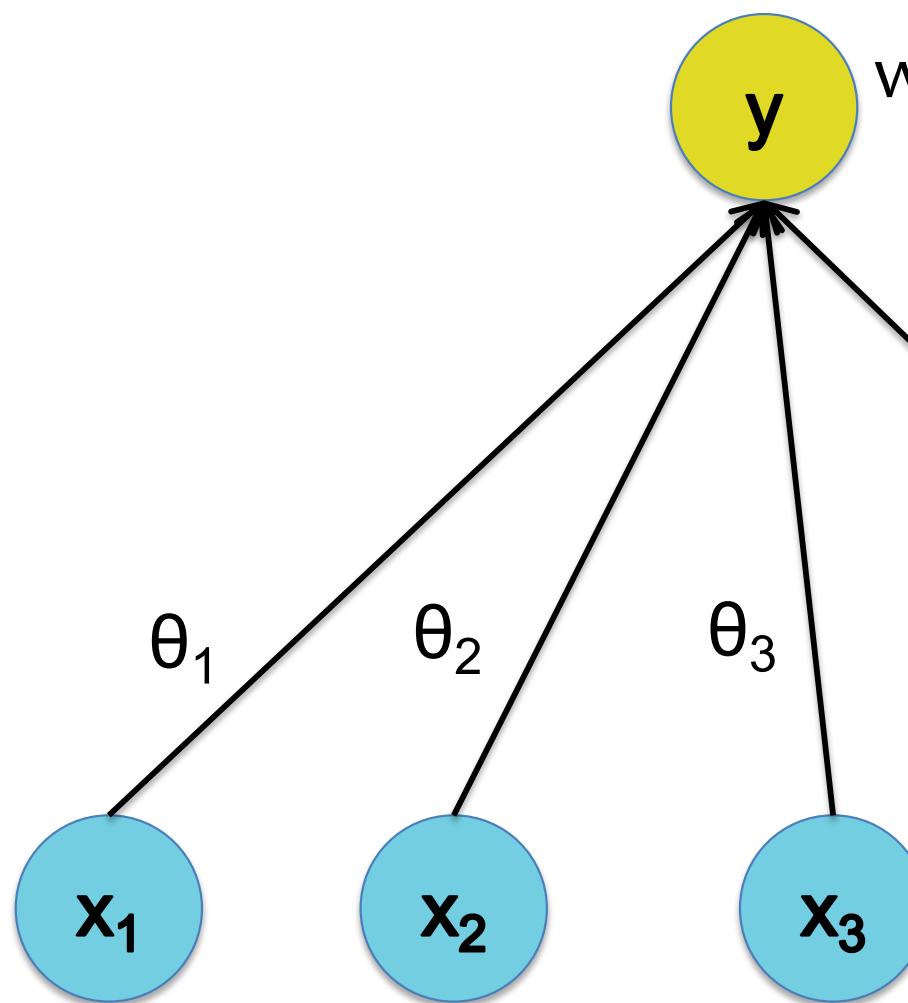
# Logistic Regression

$$y = h_{\theta}(x) = \sigma(\theta^T x)$$

$$\text{where } \sigma(a) = \frac{1}{1 + \exp(-a)}$$

Output

Input



Face



Face



Not a face



## Decision Functions

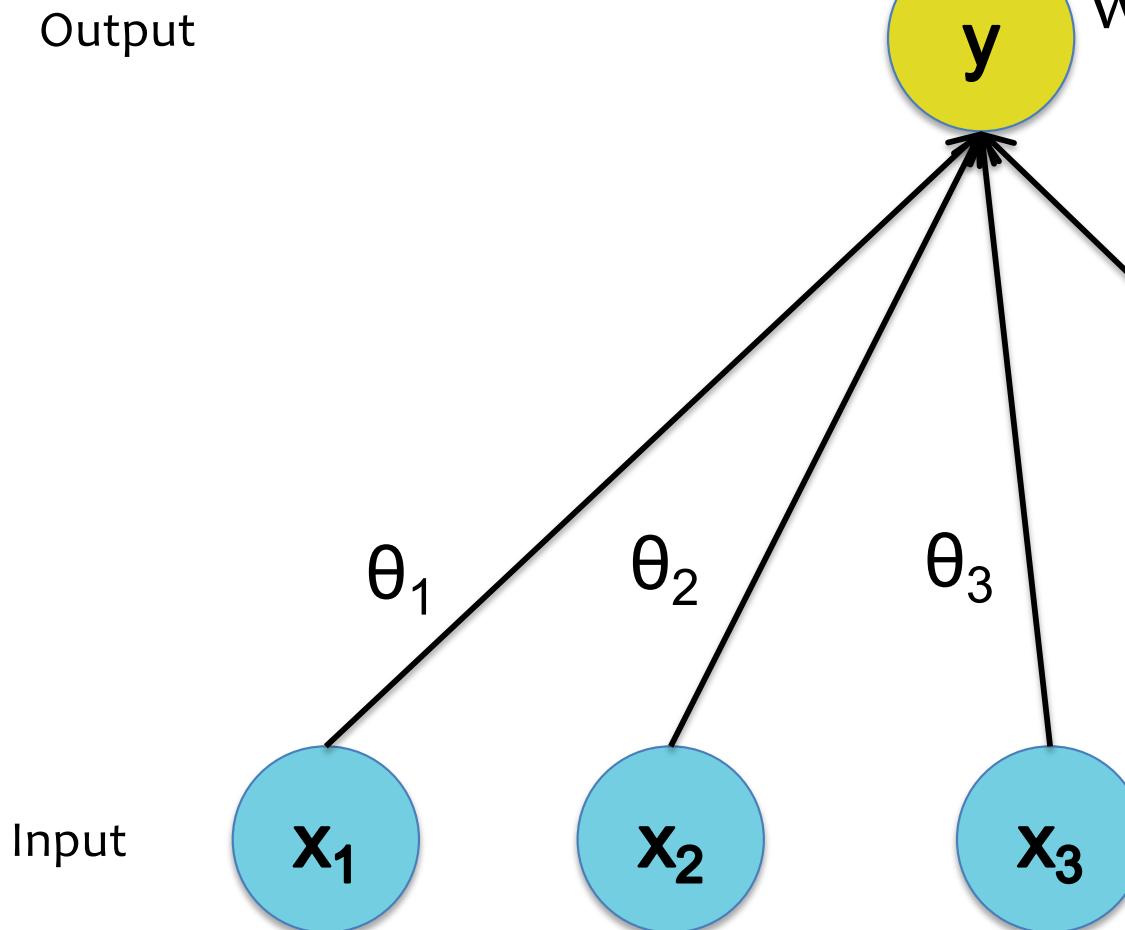
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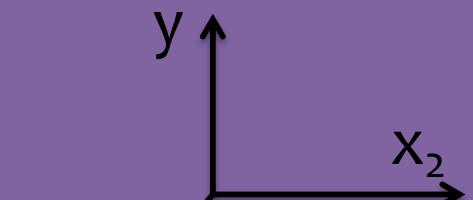
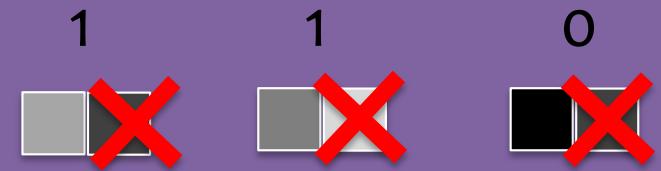
Output

y

w



In-Class Example



# Neural Networks

## *Chalkboard*

- 1D Example from linear regression to logistic regression
- 1D Example from logistic regression to a neural network

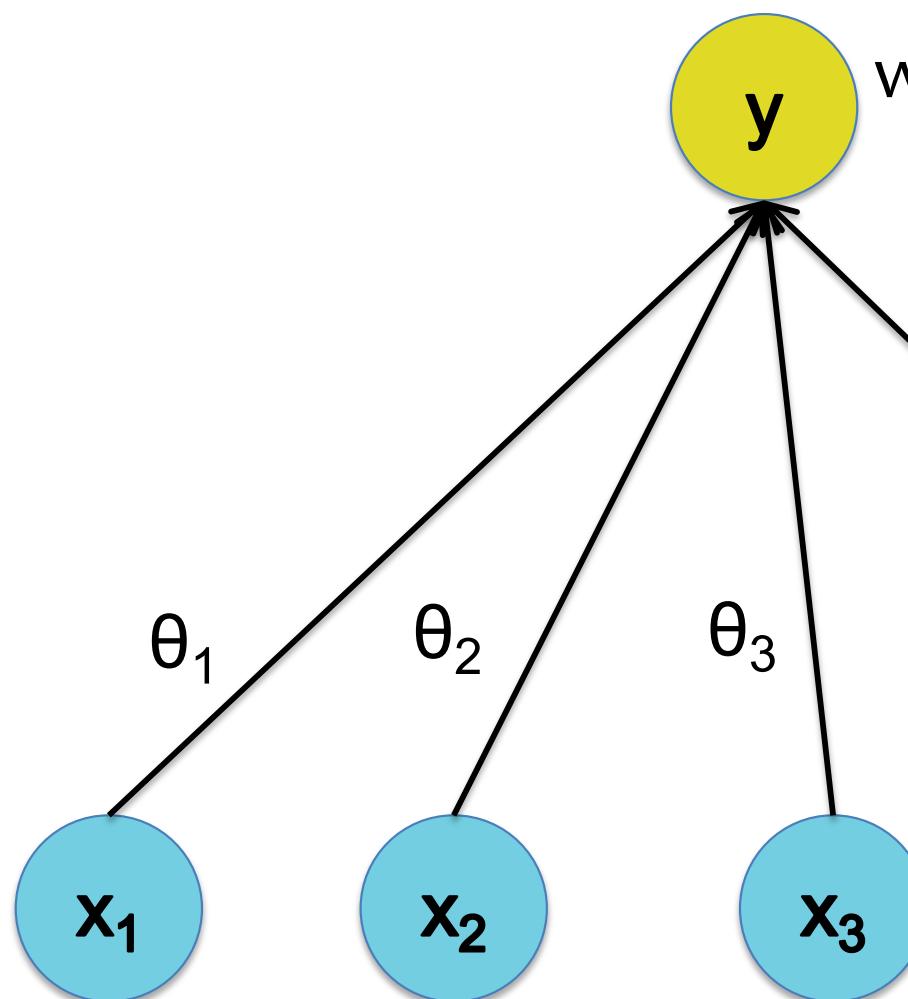
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$$y = h_{\theta}(x) = \sigma(\theta^T x)$$

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Output

Input



Face



Face



Not a face



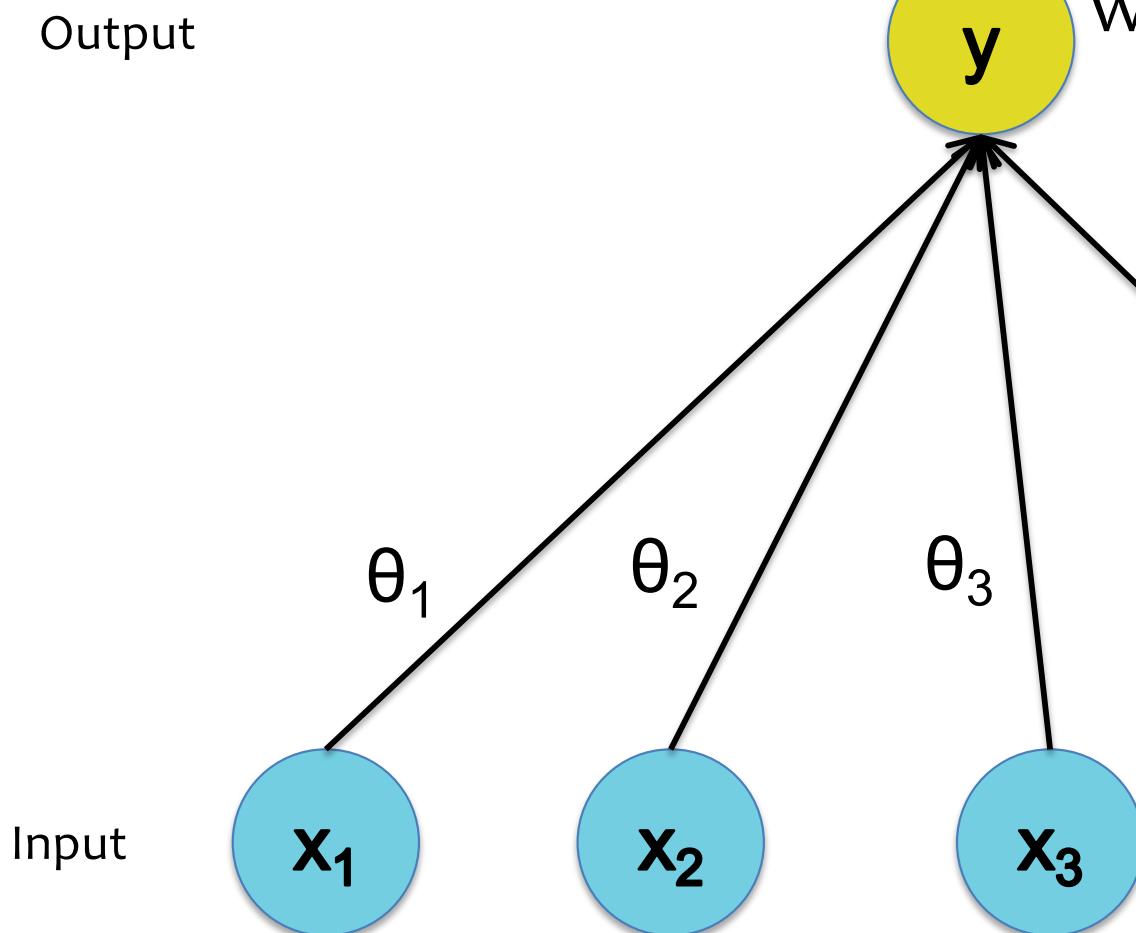
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$$y = h_{\theta}(x) = \sigma(\theta^T x)$$

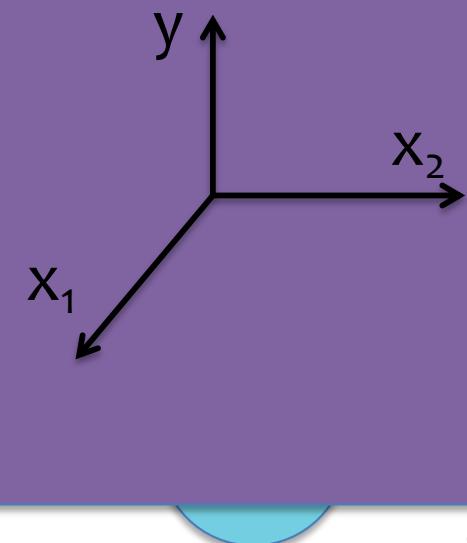
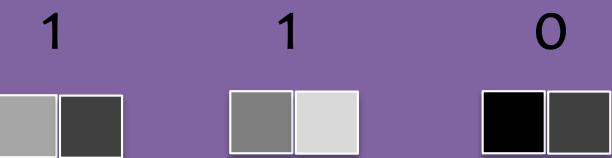
Output

y

w



In-Class Example



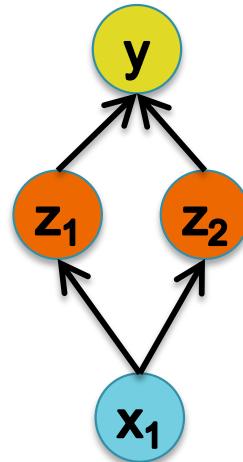
# Neural Network Parameters

## Question:

Suppose you are training a one-hidden layer neural network with sigmoid activations for binary classification.



**True or False:** There is a unique set of parameters that maximize the likelihood of the dataset above.



## Answer:

# **ARCHITECTURES**

# Neural Network Architectures

Even for a basic Neural Network, there are many design decisions to make:

1. # of hidden layers (depth)
2. # of units per hidden layer (width)
3. Type of activation function (nonlinearity)
4. Form of objective function
5. How to initialize the parameters

# **BUILDING WIDER NETWORKS**

$D = M$

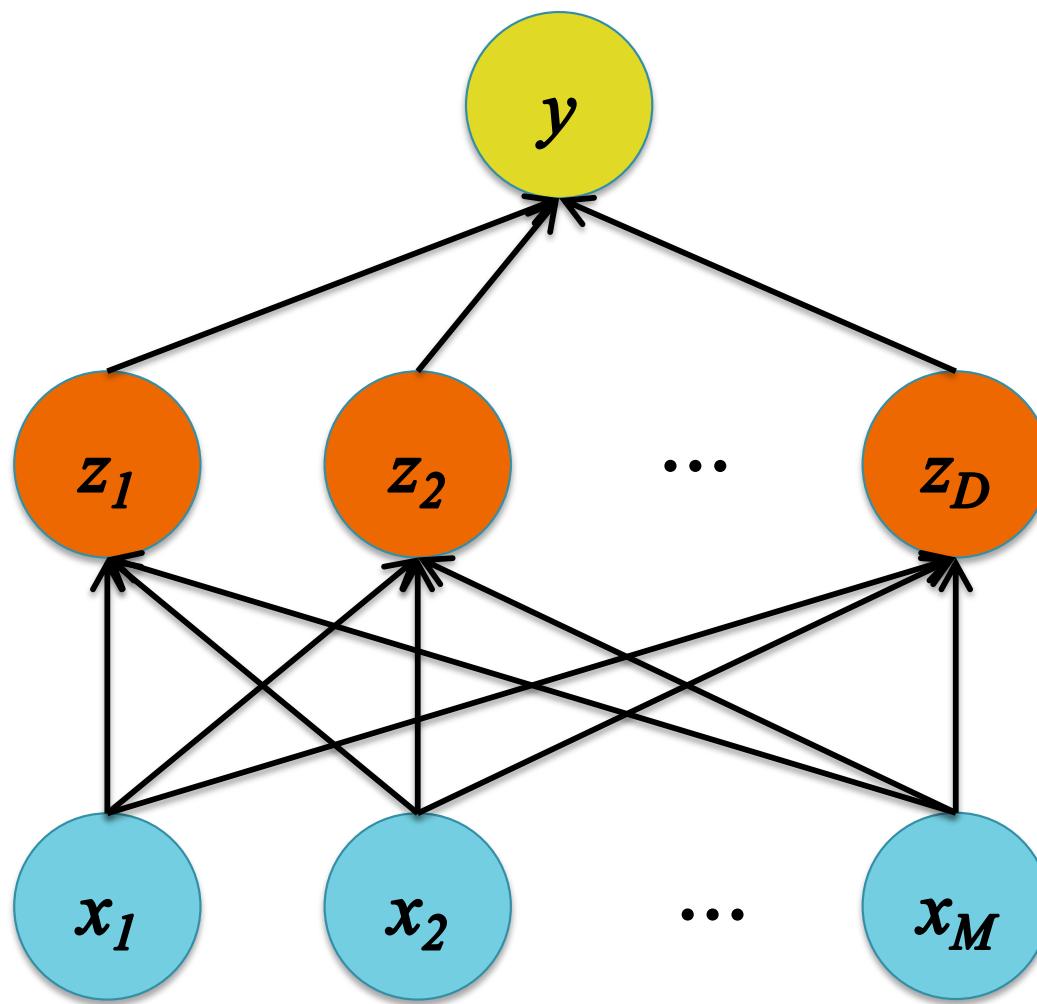
# Building a Neural Net

Q: How many hidden units,  $D$ , should we use?

Output

Hidden Layer

Input



The hidden units could learn to be...

- a selection of the most useful features
- nonlinear combinations of the features
- a lower dimensional projection of the features
- a higher dimensional projection of the features
- a copy of the input features
- a mix of the above

D < M

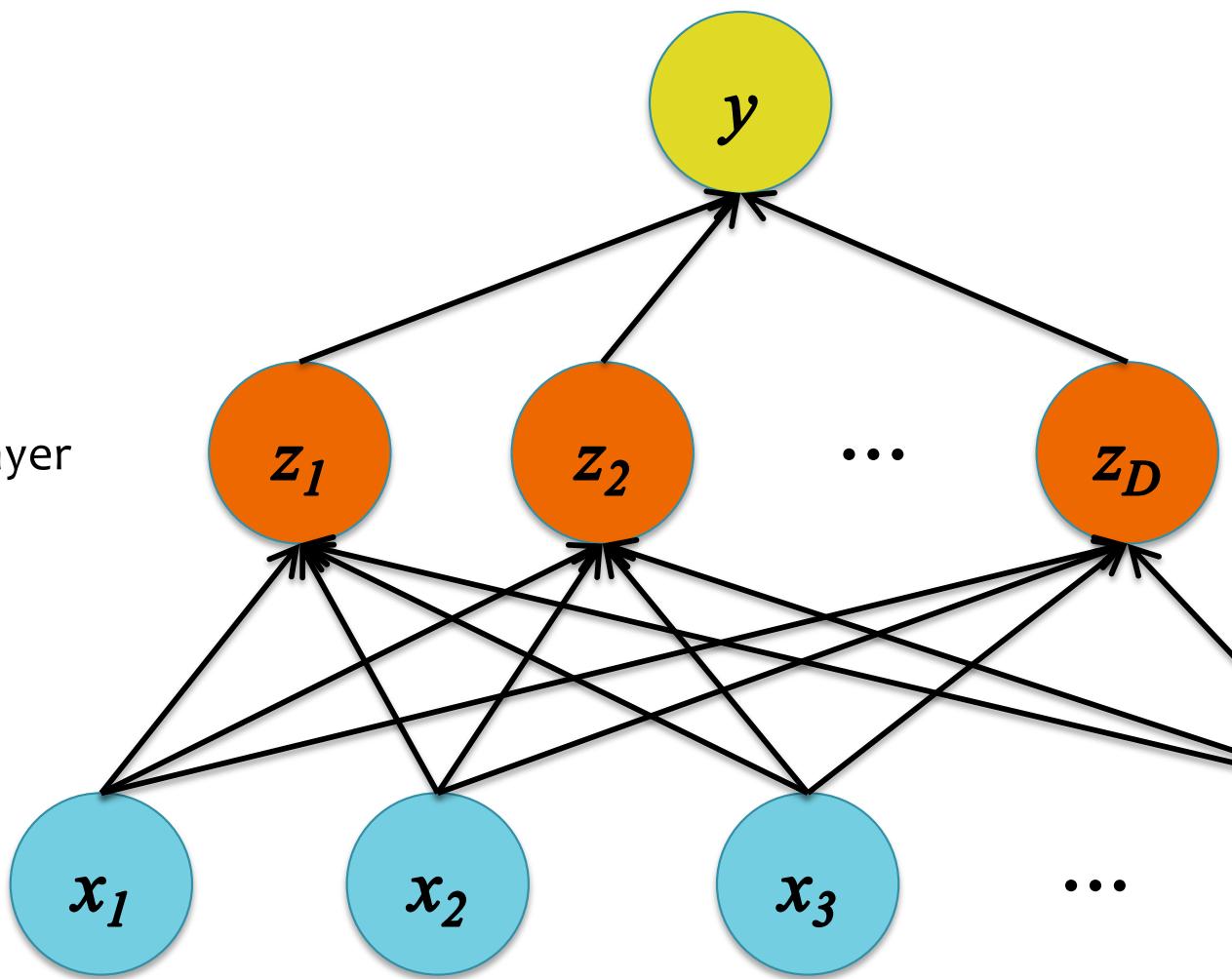
# Building a Neural Net

Q: How many hidden units, D, should we use?

Output

Hidden Layer

Input



The hidden units could learn to be...

- a selection of the most useful features
- nonlinear combinations of the features
- a lower dimensional projection of the features
- a higher dimensional projection of the features
- a copy of the input features
- a mix of the above

D > M

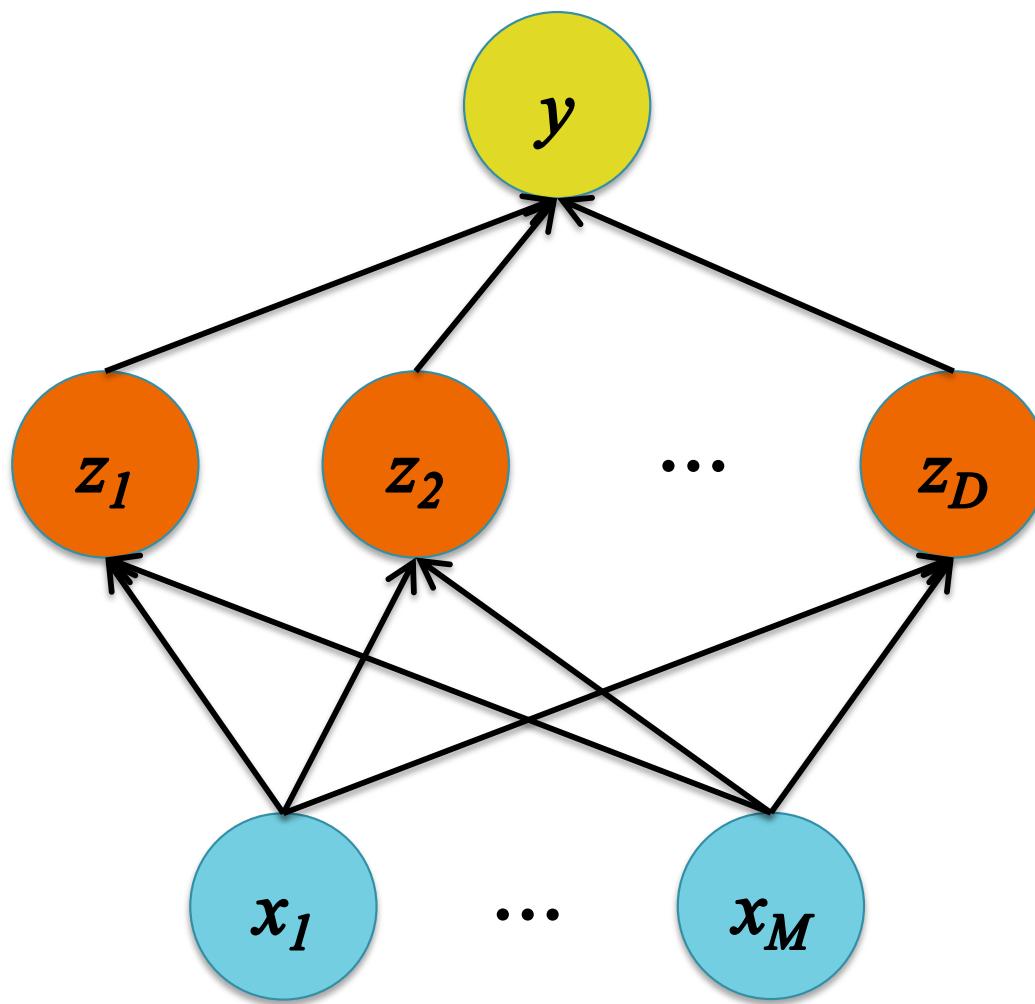
# Building a Neural Net

Q: How many hidden units,  $D$ , should we use?

Output

Hidden Layer

Input



The hidden units could learn to be...

- a selection of the most useful features
- nonlinear combinations of the features
- a lower dimensional projection of the features
- a higher dimensional projection of the features
- a copy of the input features
- a mix of the above

$D \geq M$

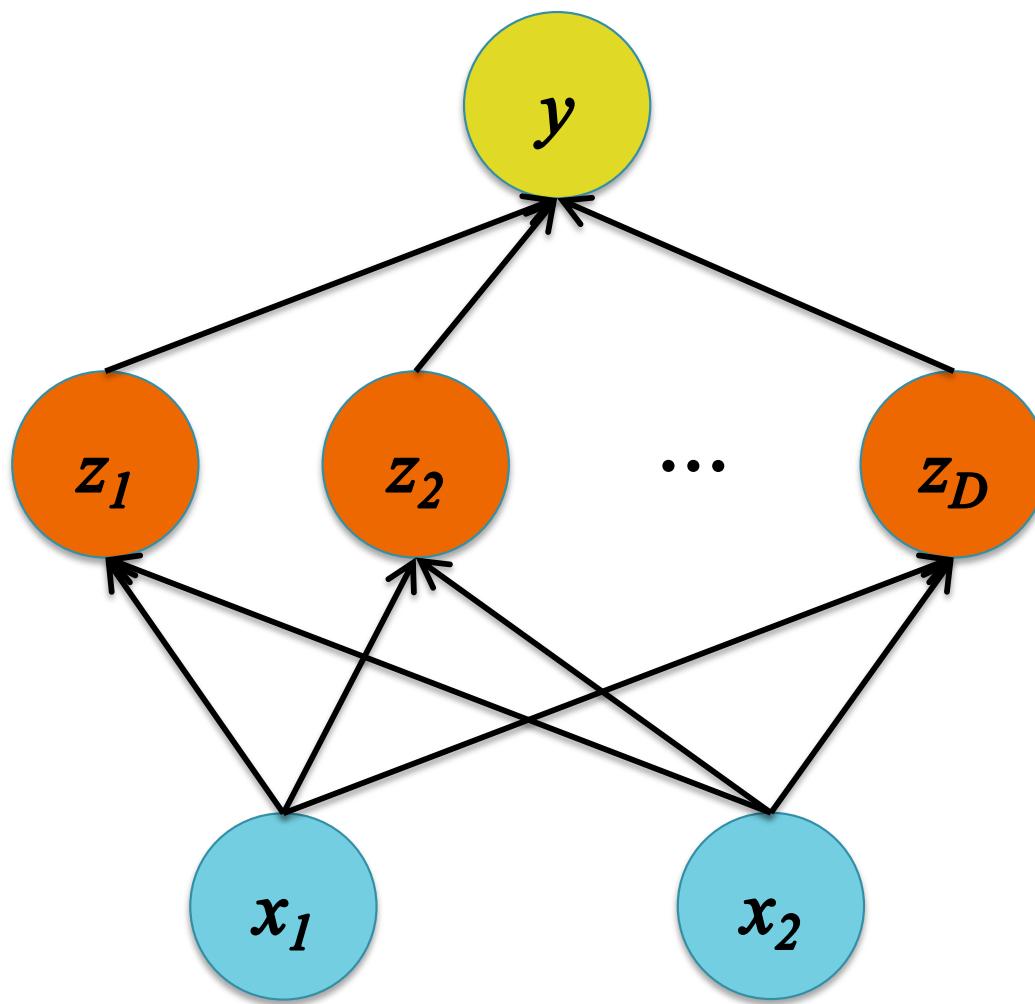
# Building a Neural Net

In the following examples, we have two input features,  $M=2$ , and we vary the number of hidden units,  $D$ .

Output

Hidden Layer

Input



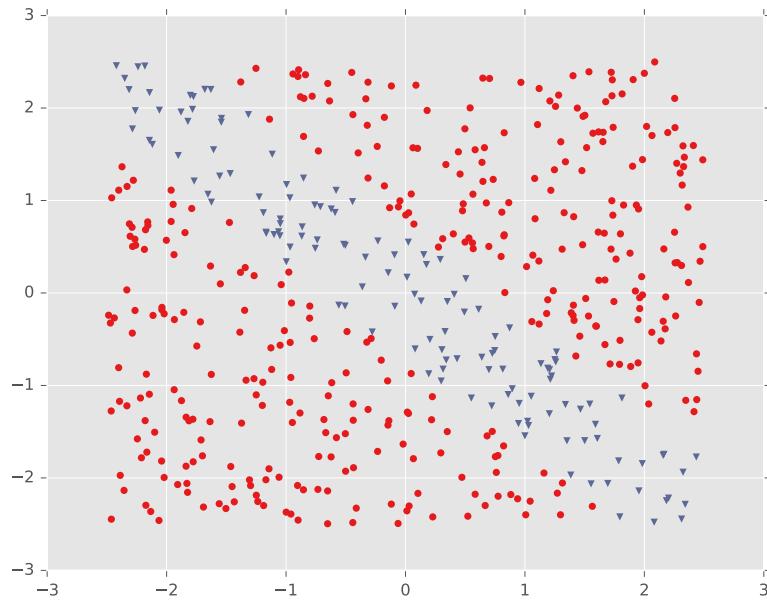
The hidden units could learn to be...

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- a lower dimensional projection of the features
- a higher dimensional projection of the features
- a copy of the input features
- a mix of the above

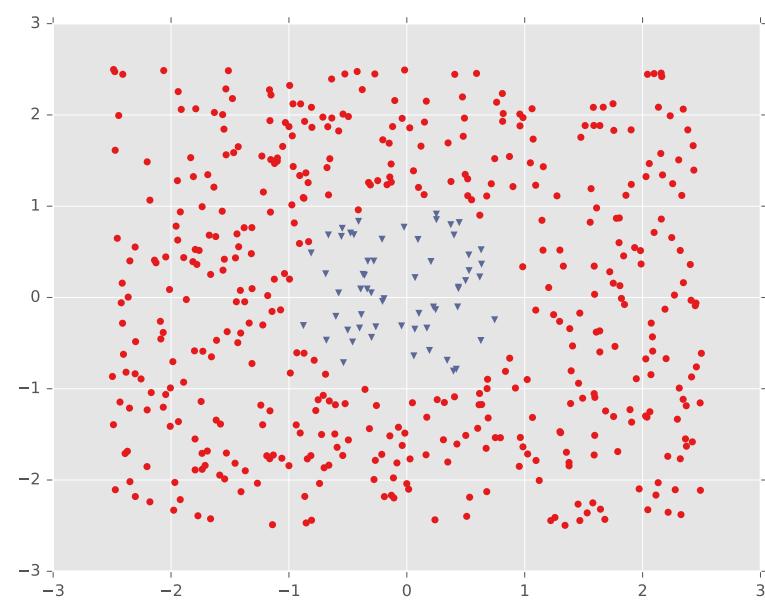
Examples 1 and 2

## **DECISION BOUNDARY EXAMPLES**

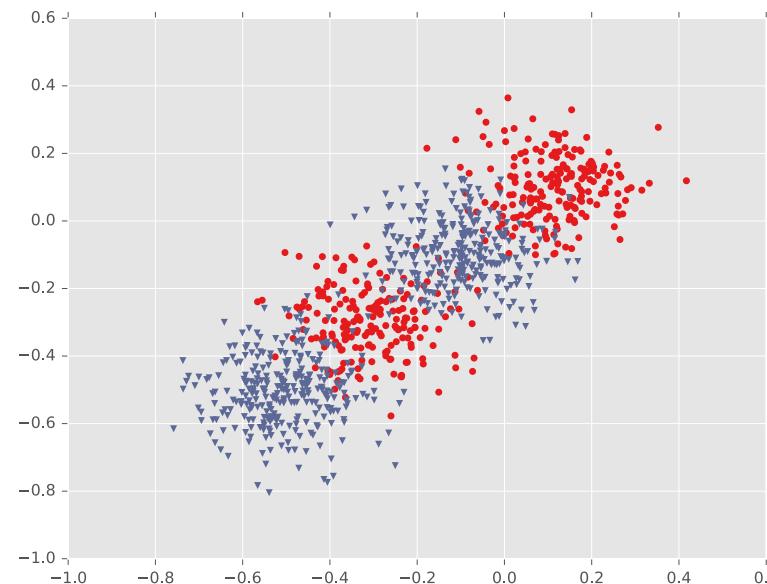
## Example #1: Diagonal Band



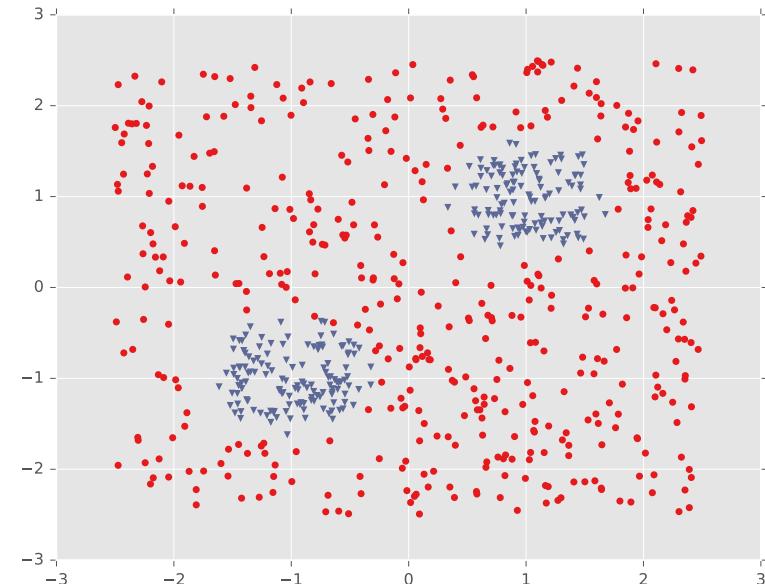
## Example #2: One Pocket



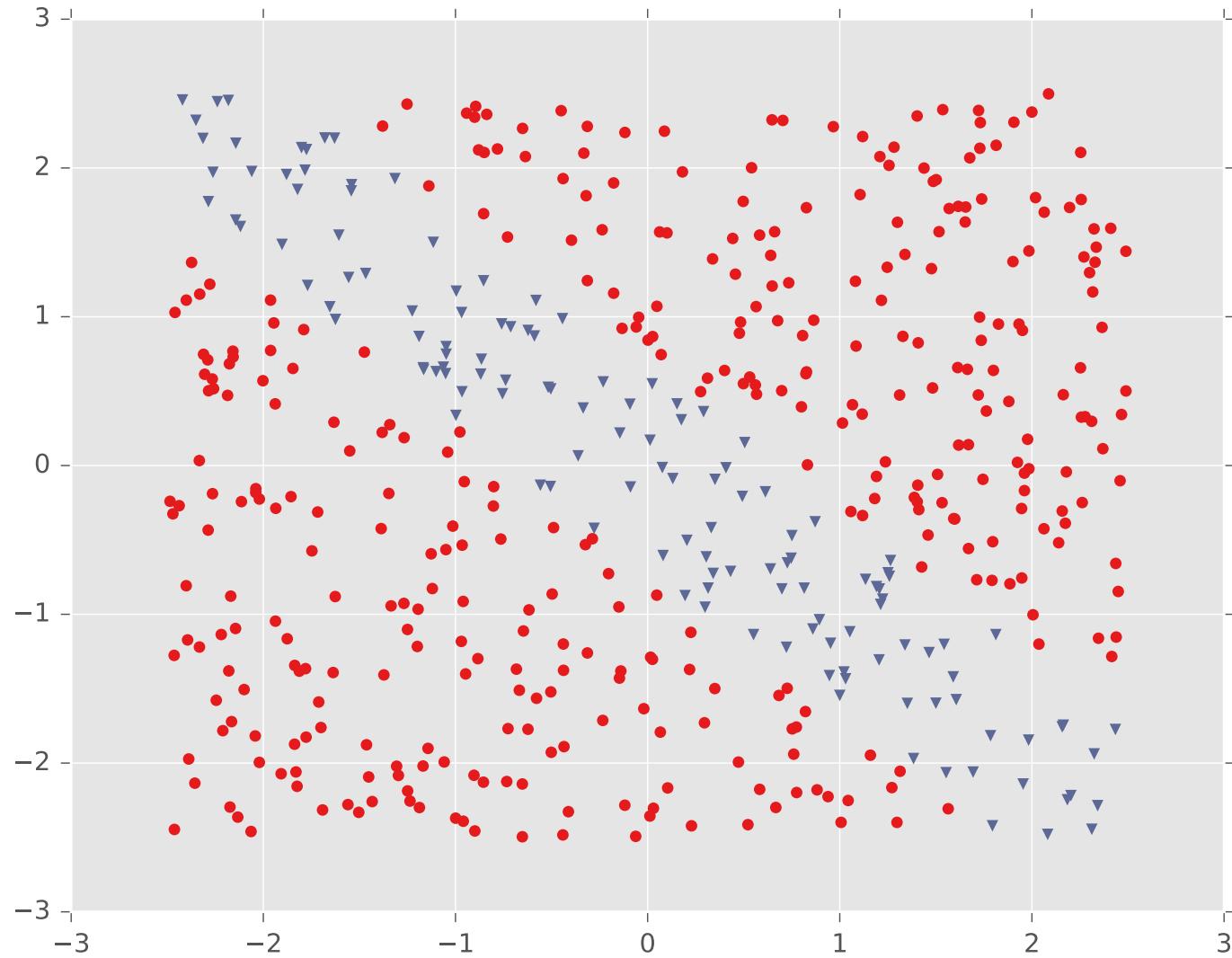
## Example #3: Four Gaussians



## Example #4: Two Pockets

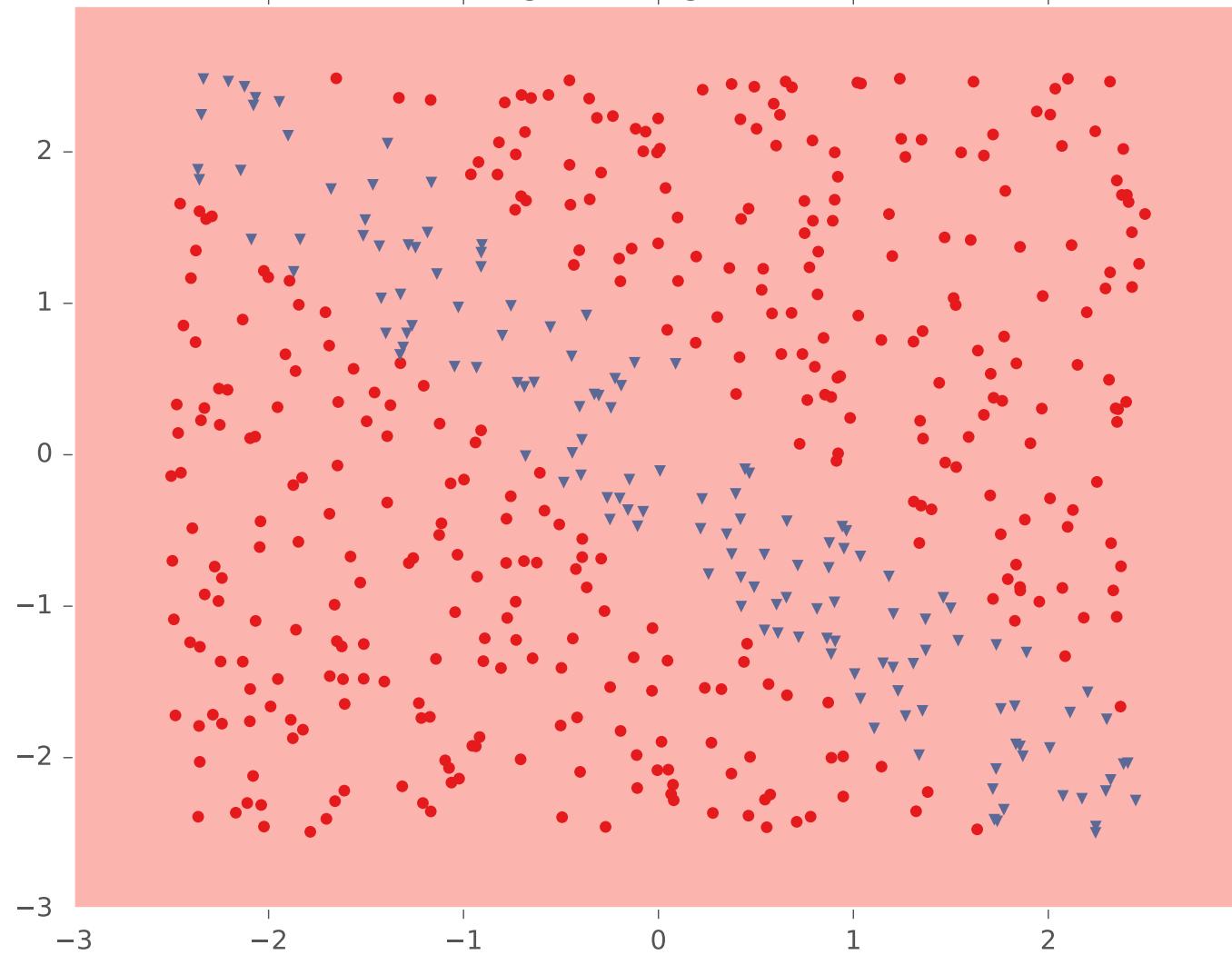


# Example #1: Diagonal Band



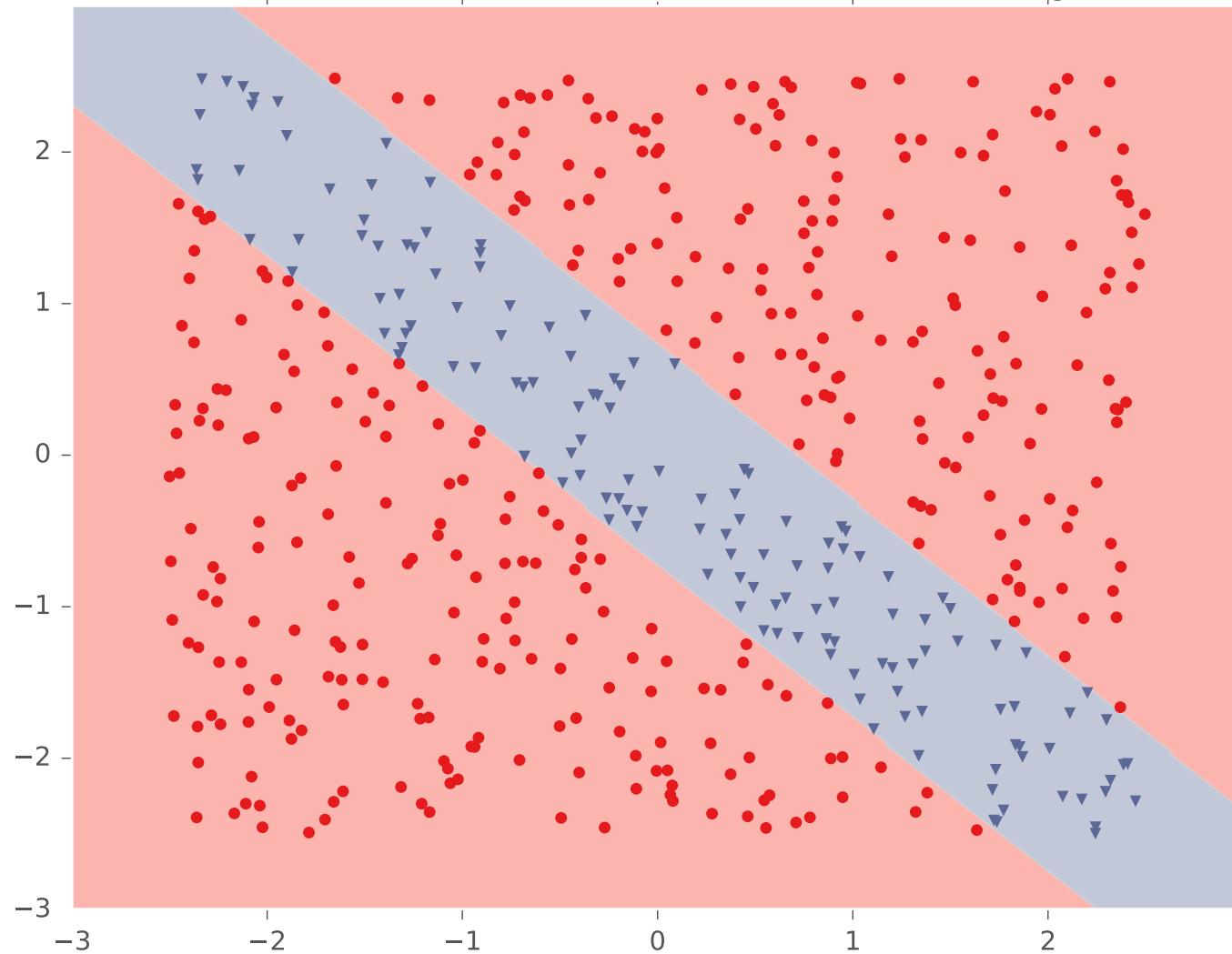
# Example #1: Diagonal Band

Logistic Regression



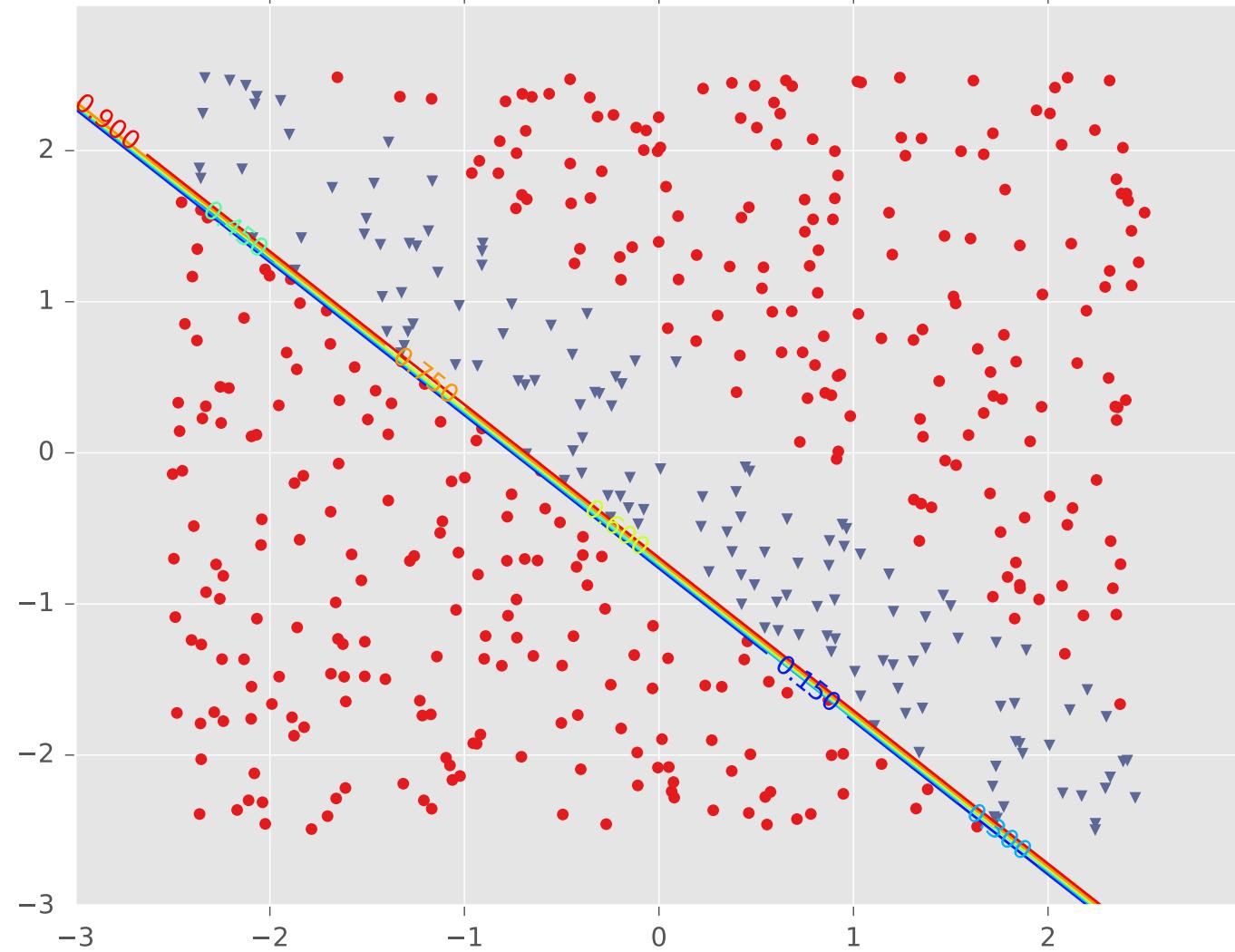
# Example #1: Diagonal Band

Tuned Neural Network (hidden=2, activation=logistic)



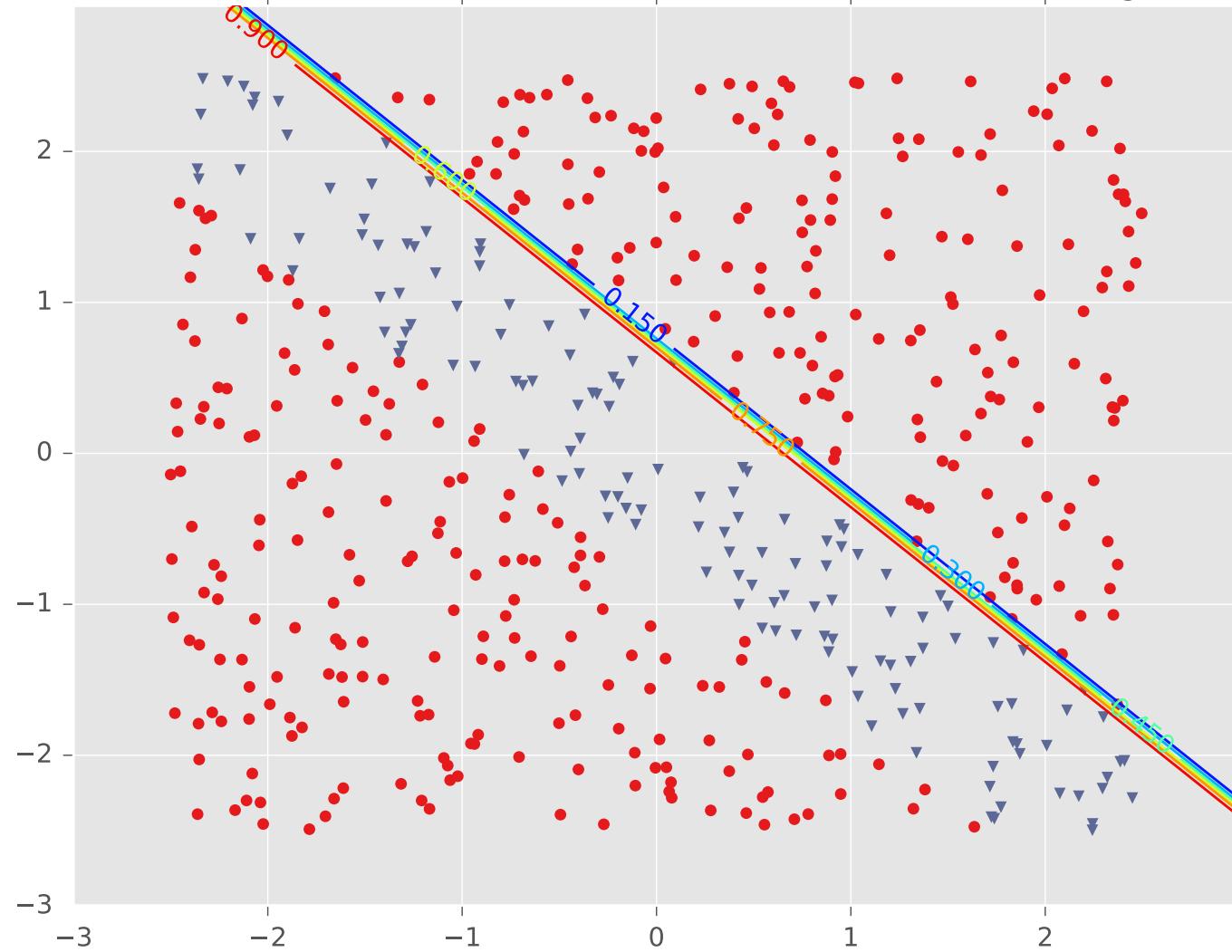
# Example #1: Diagonal Band

LR1 for Tuned Neural Network (hidden=2, activation=logistic)



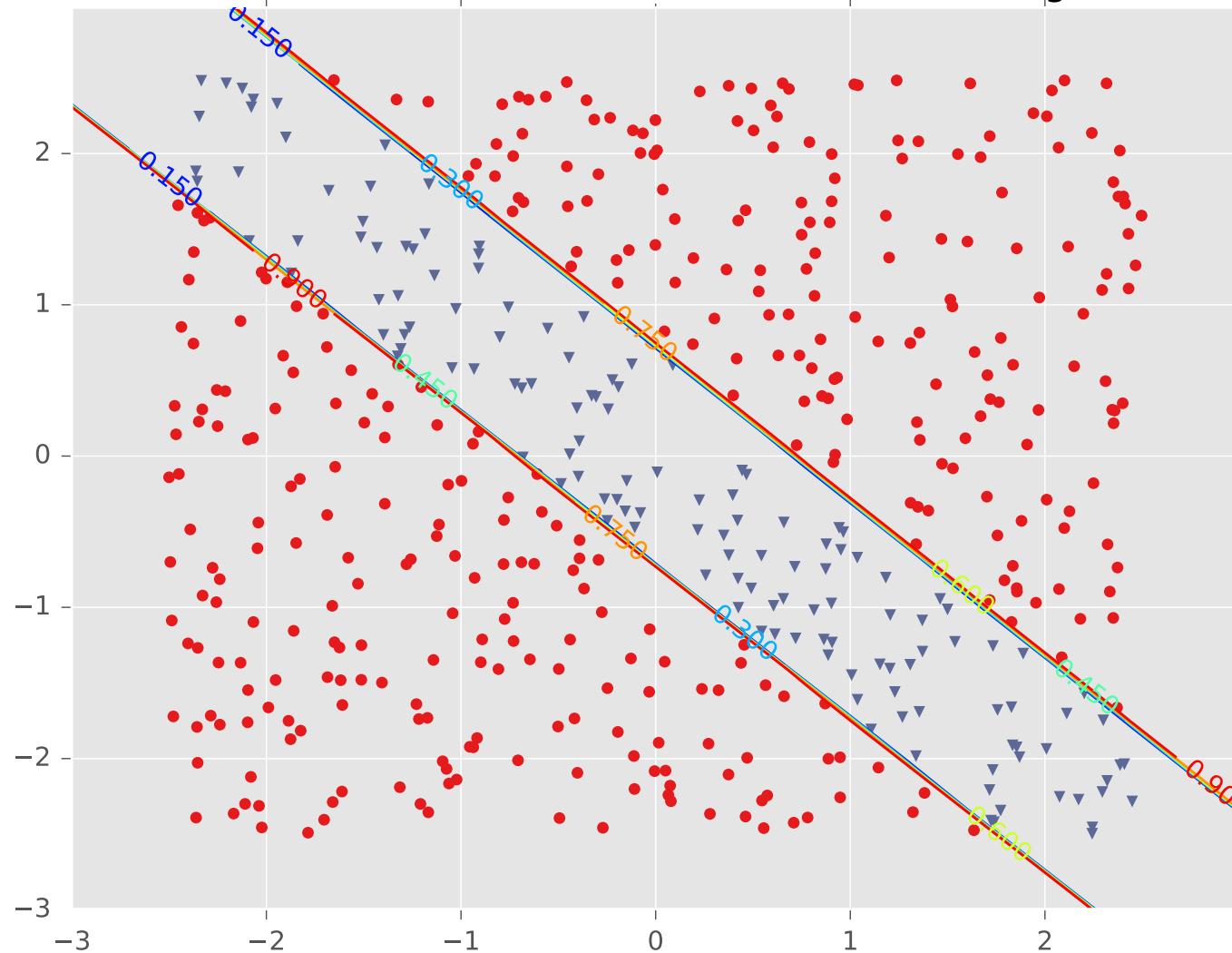
# Example #1: Diagonal Band

LR2 for Tuned Neural Network (hidden=2, activation=logistic)

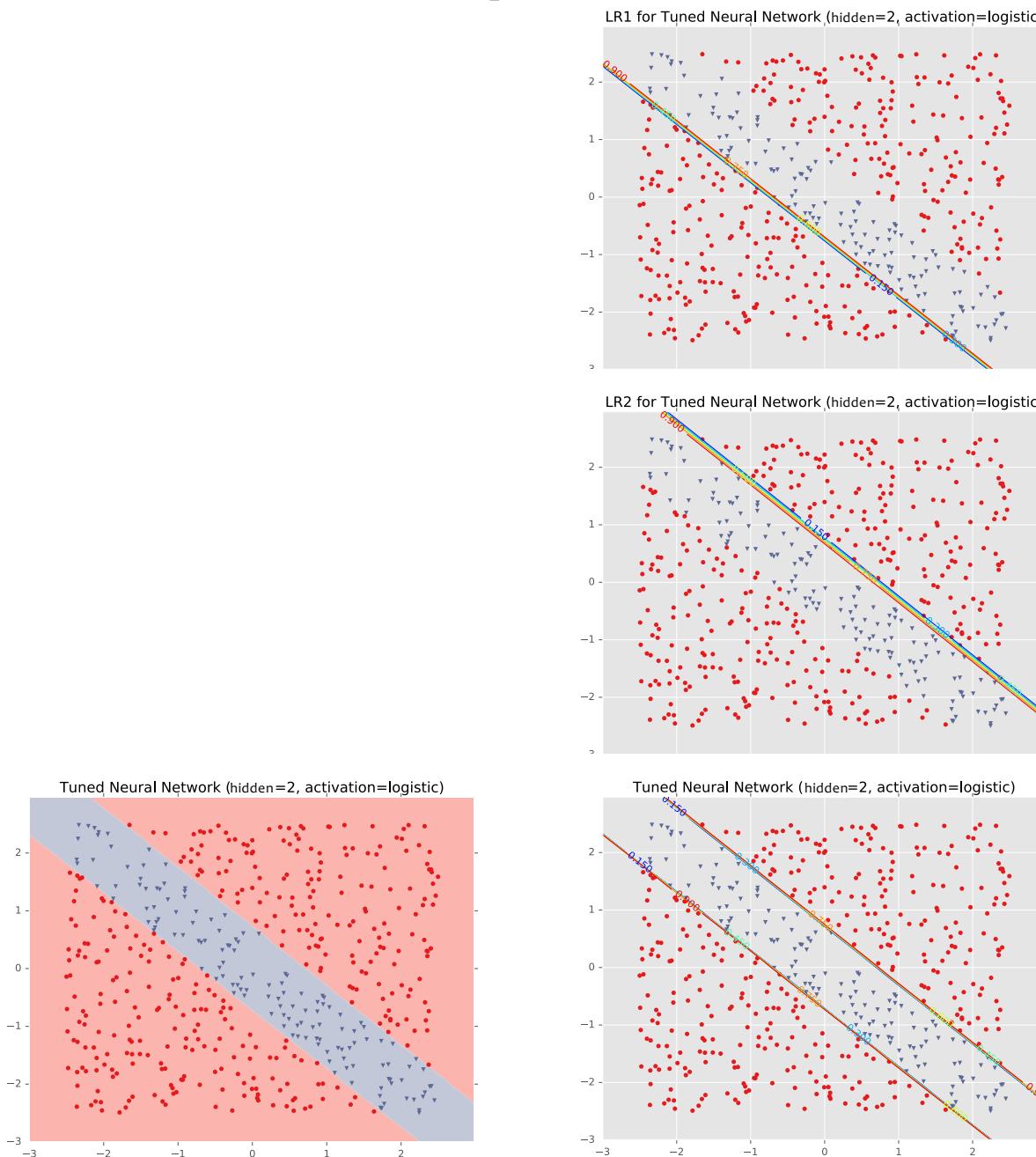


# Example #1: Diagonal Band

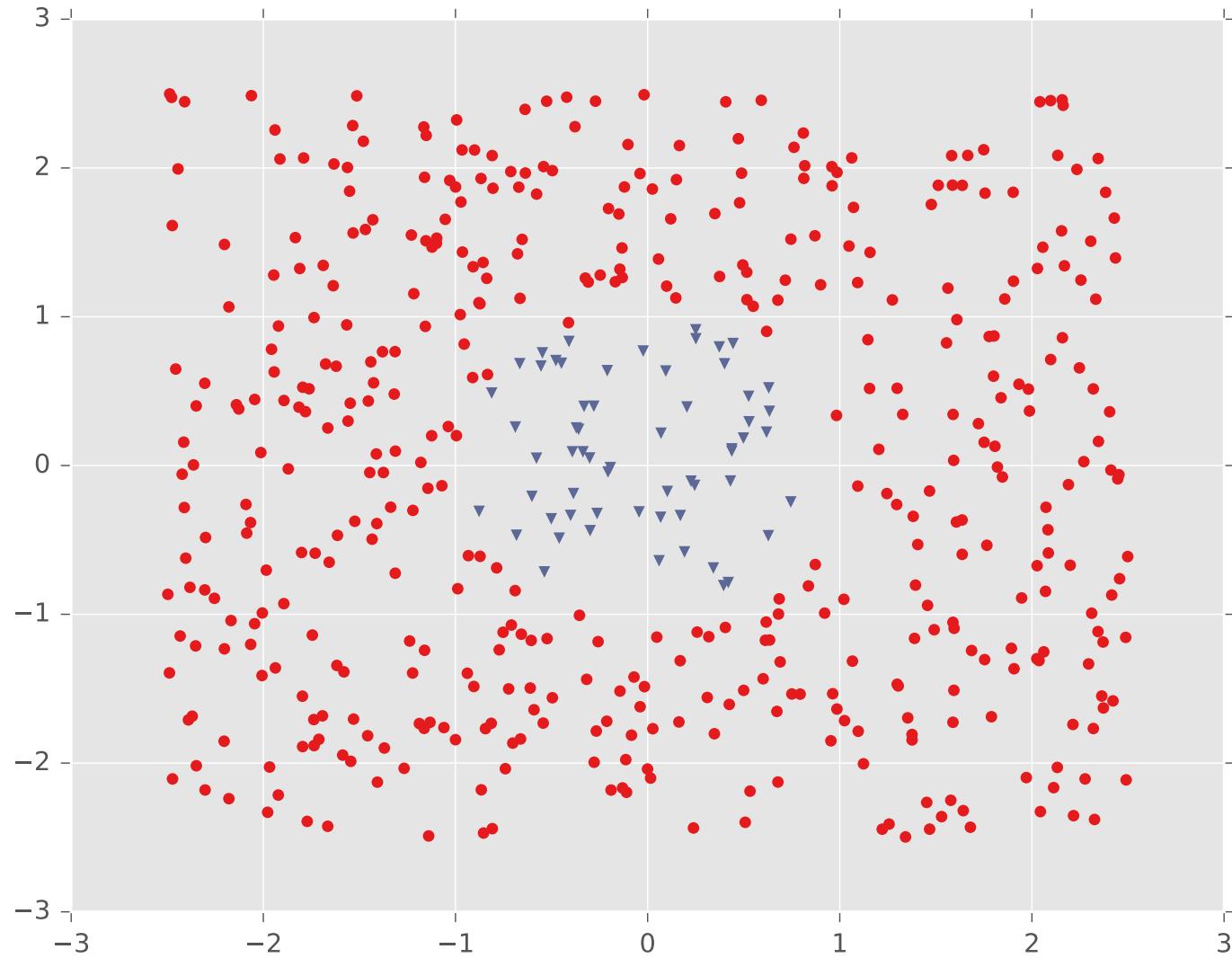
Tuned Neural Network (hidden=2, activation=logistic)



# Example #1: Diagonal Band

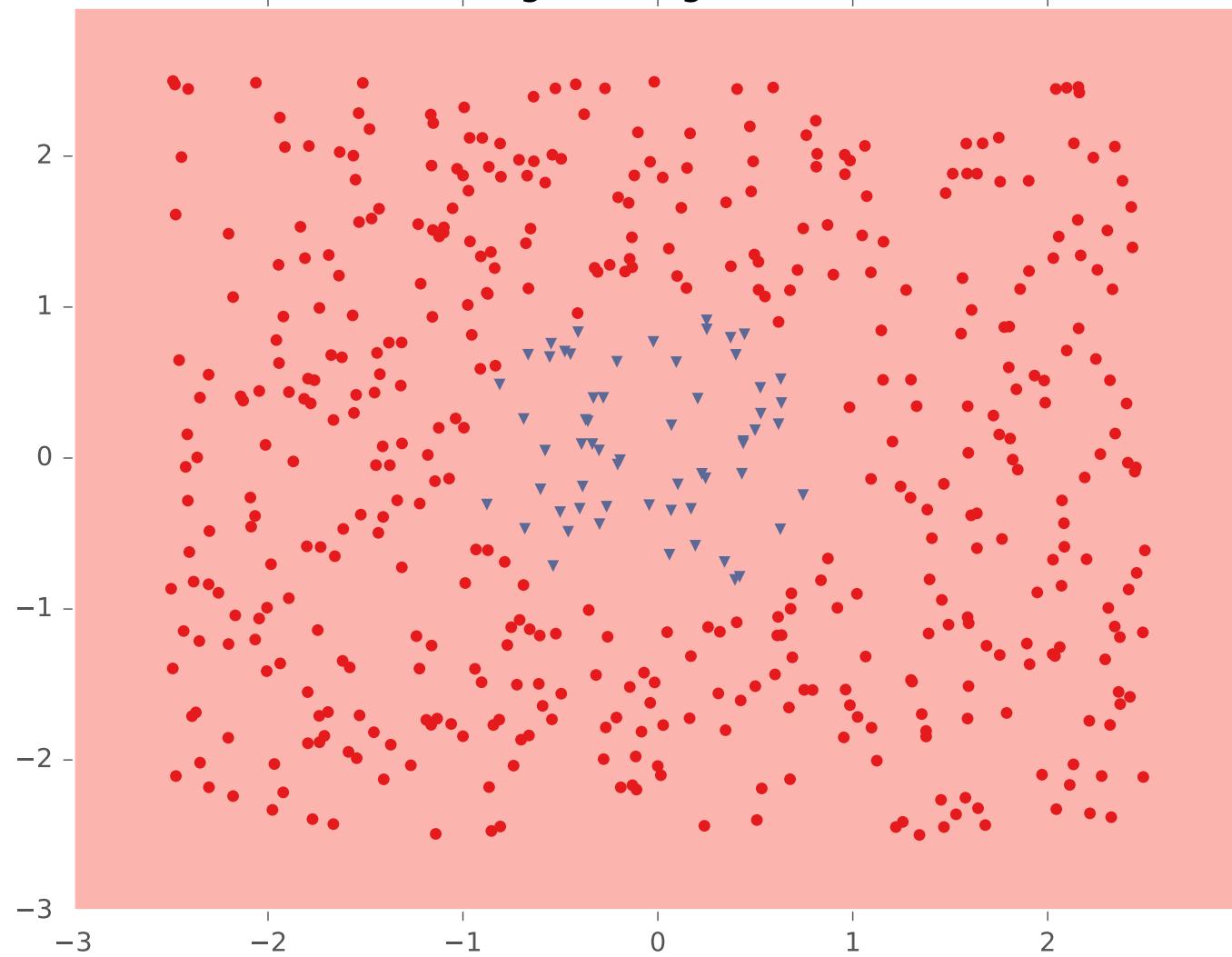


# Example #2: One Pocket



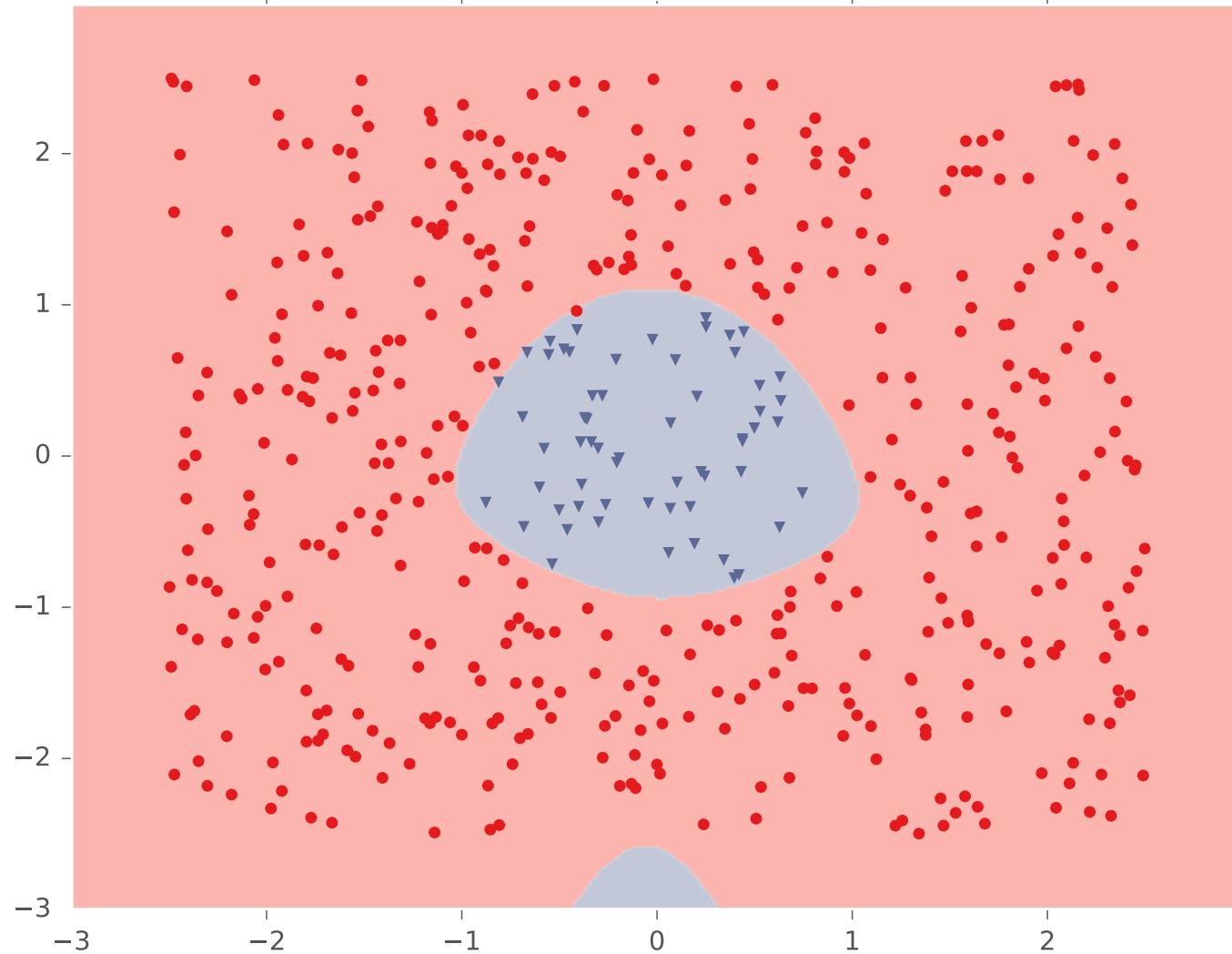
# Example #2: One Pocket

Logistic Regression



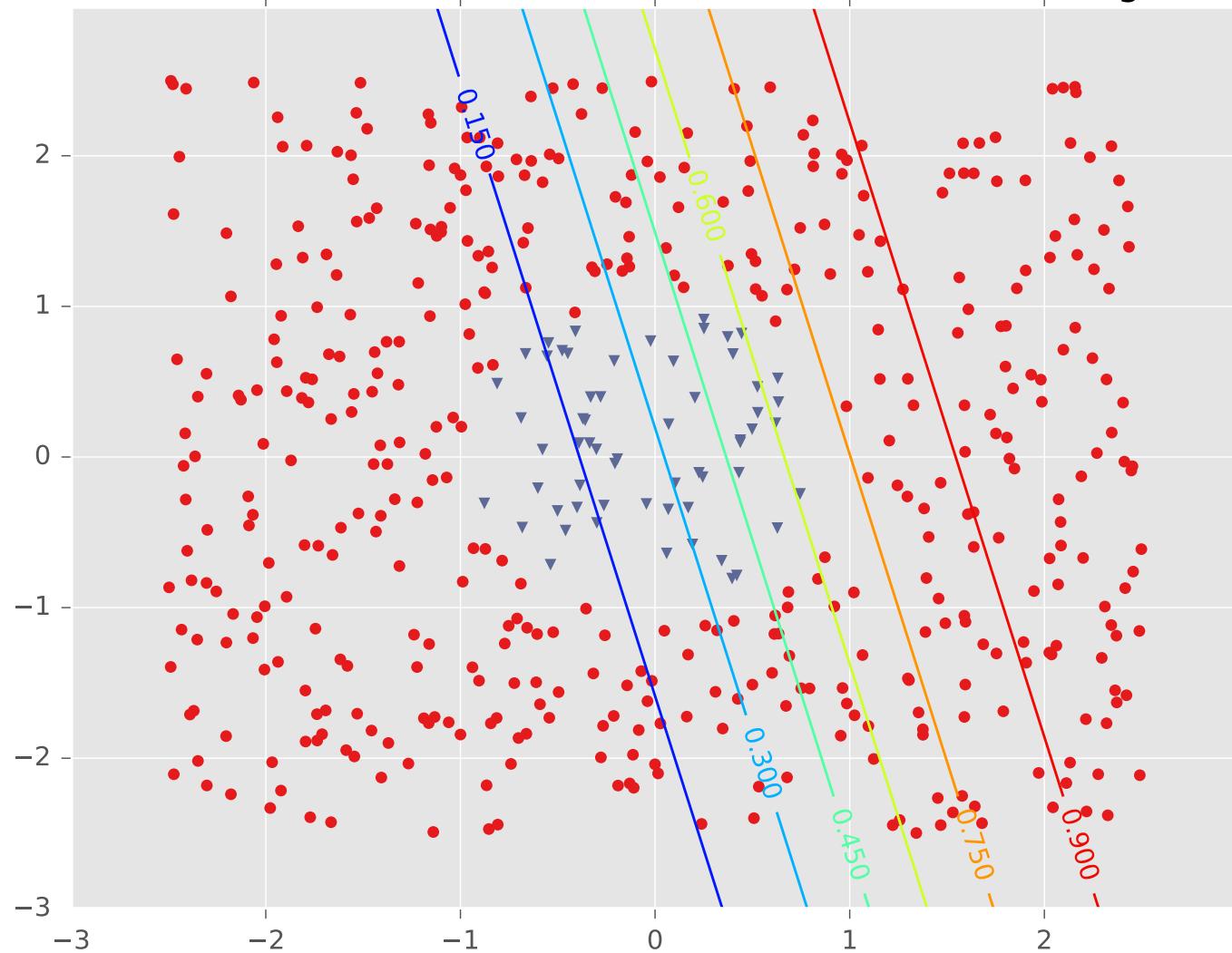
# Example #2: One Pocket

Tuned Neural Network (hidden=3, activation=logistic)



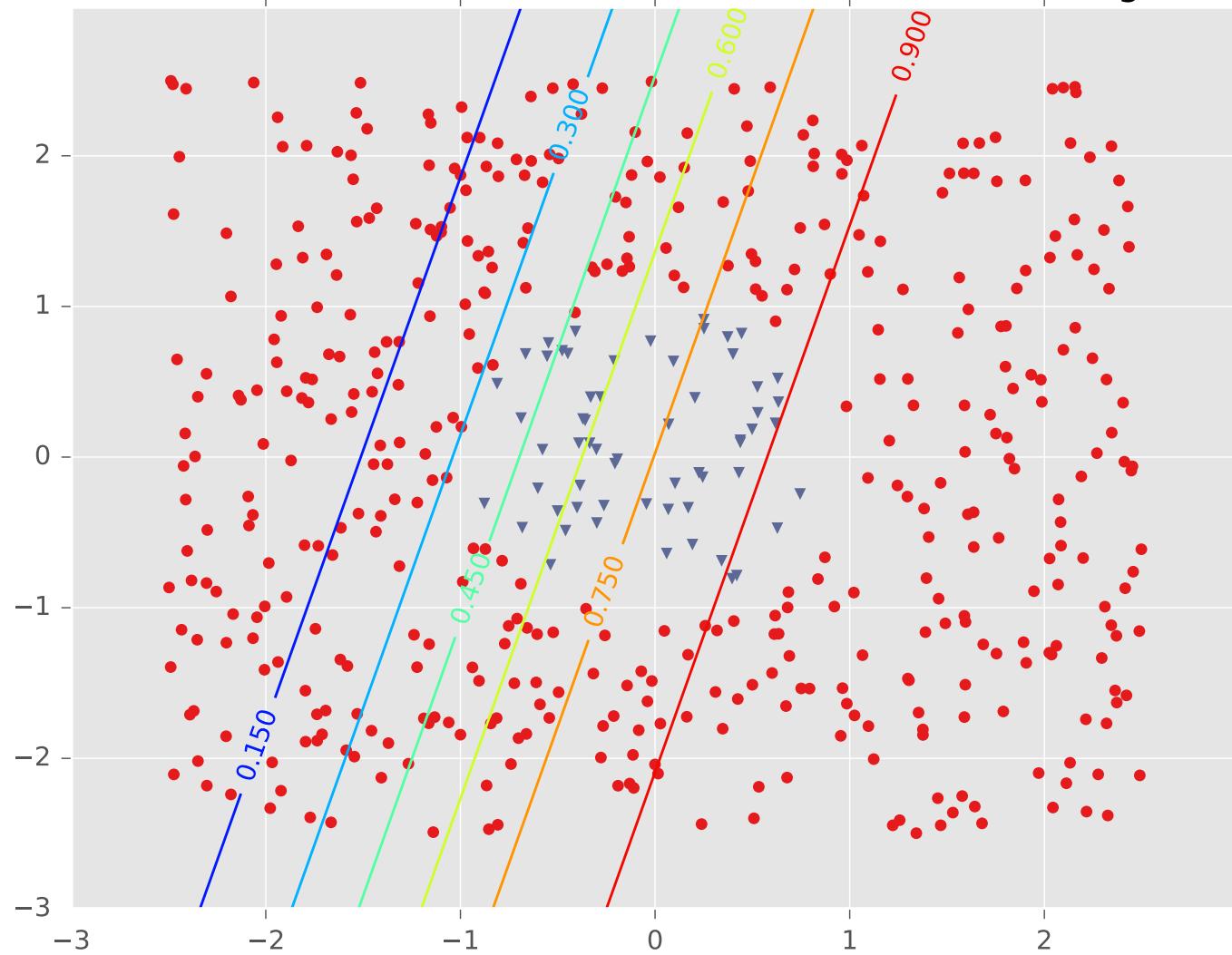
# Example #2: One Pocket

LR1 for Tuned Neural Network (hidden=3, activation=logistic)



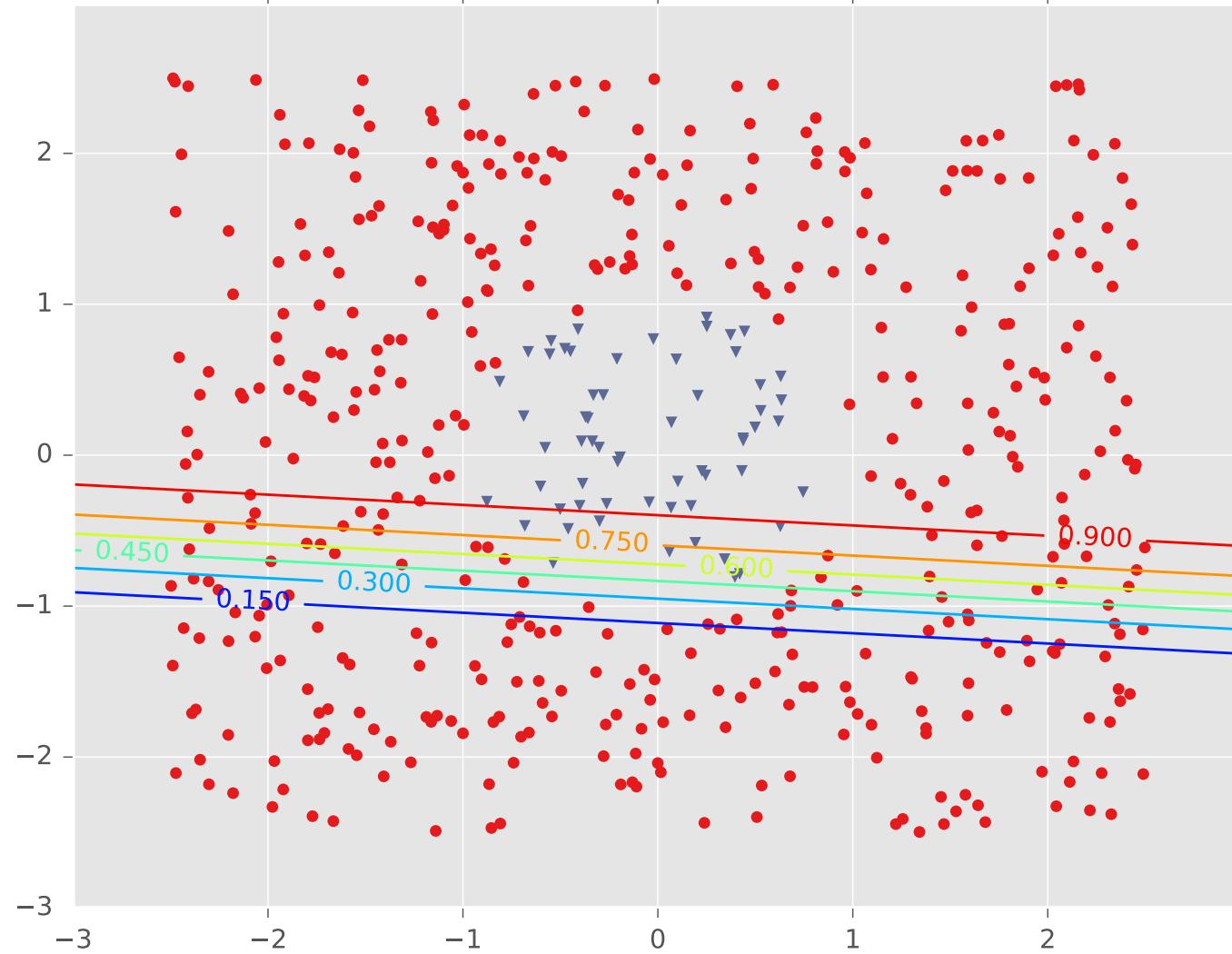
# Example #2: One Pocket

LR2 for Tuned Neural Network (hidden=3, activation=logistic)



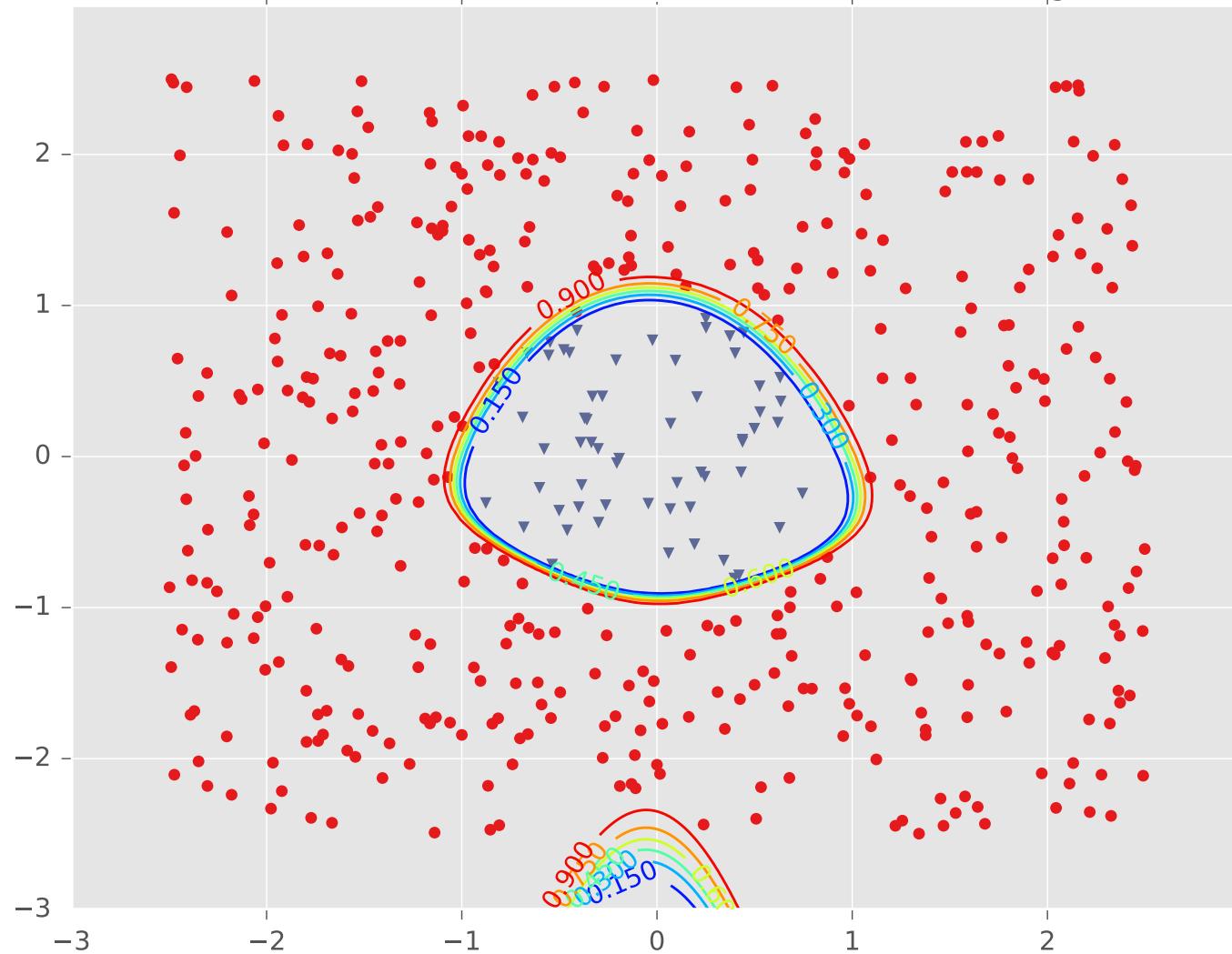
# Example #2: One Pocket

LR3 for Tuned Neural Network (hidden=3, activation=logistic)

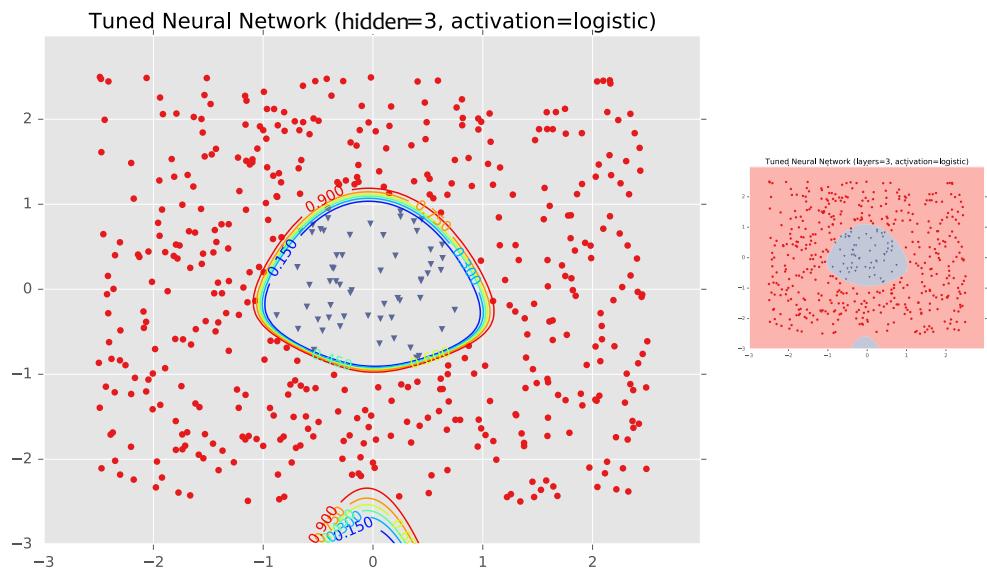
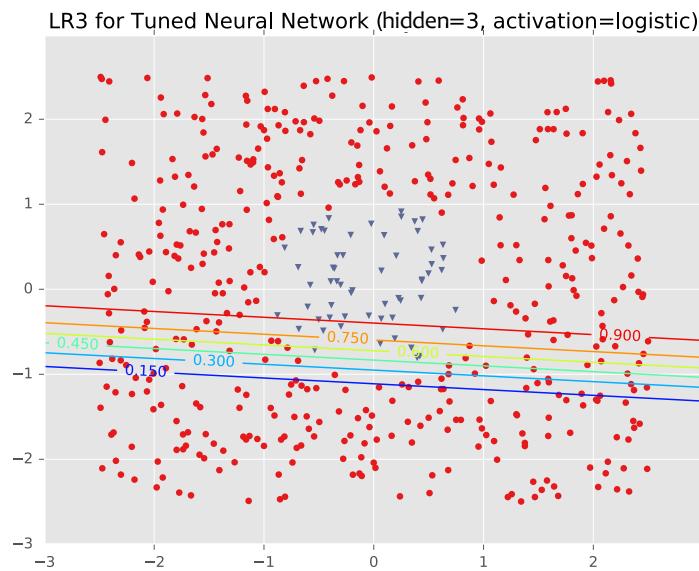
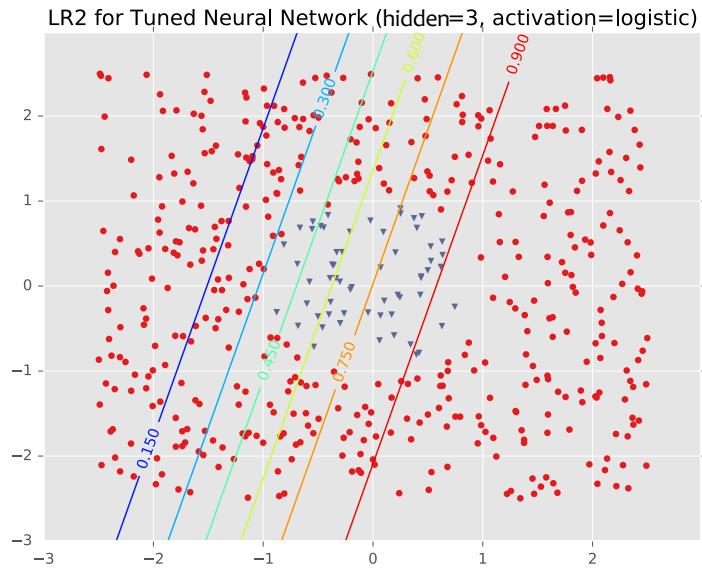
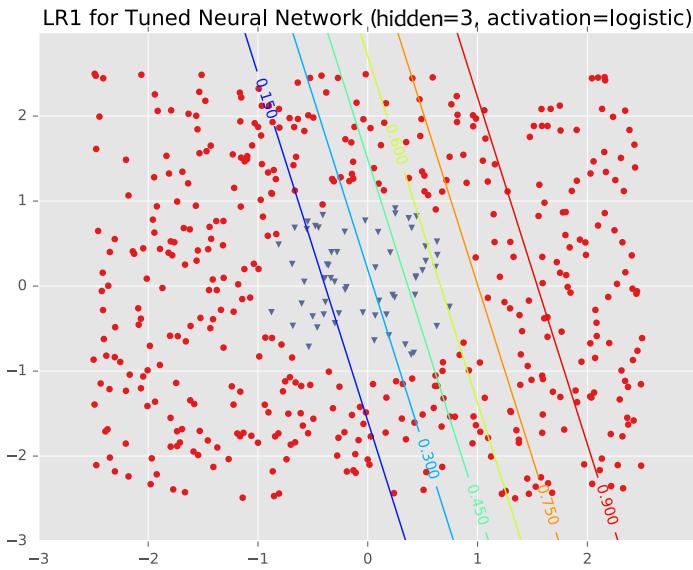


# Example #2: One Pocket

Tuned Neural Network (hidden=3, activation=logistic)



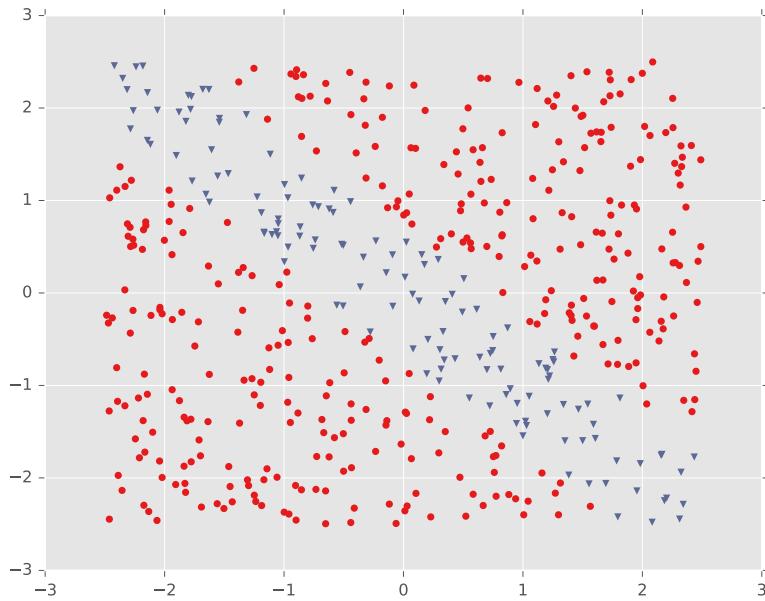
# Example #2: One Pocket



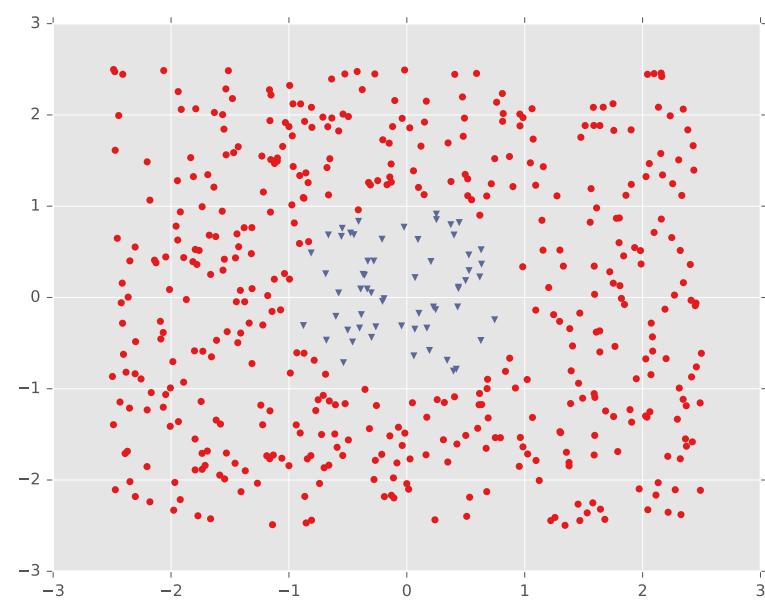
Examples 3 and 4

## **DECISION BOUNDARY EXAMPLES**

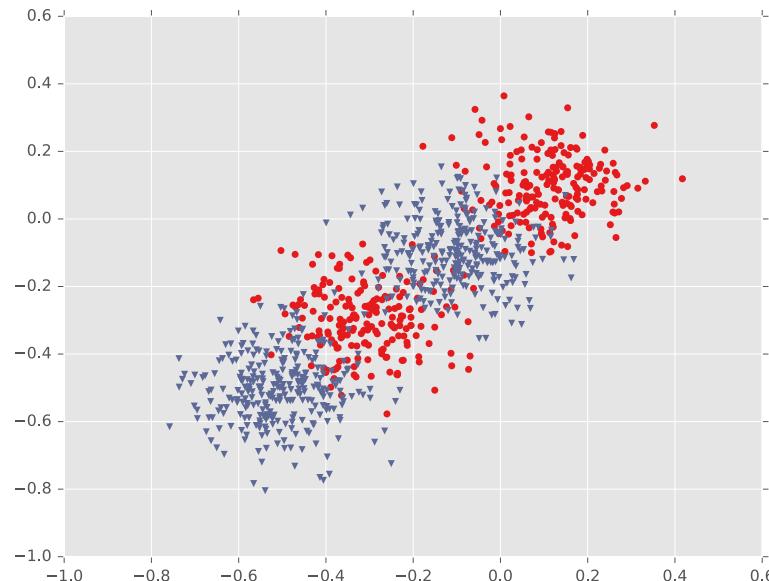
## Example #1: Diagonal Band



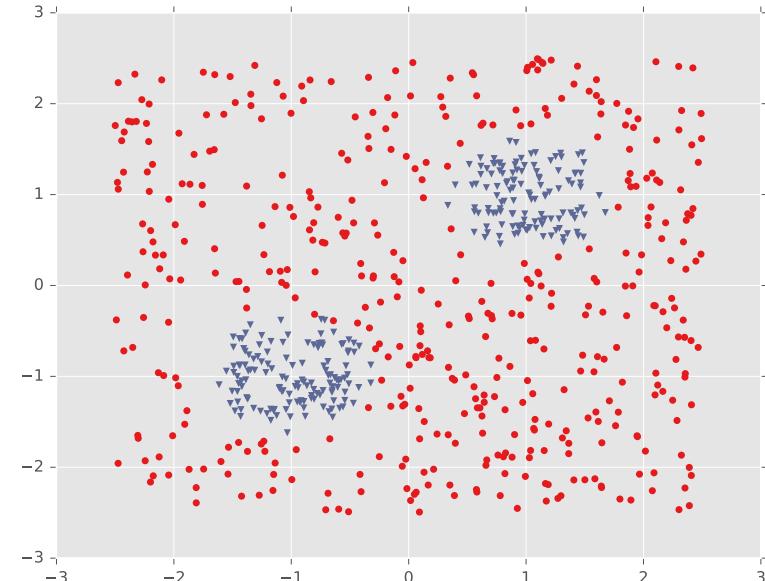
## Example #2: One Pocket



## Example #3: Four Gaussians



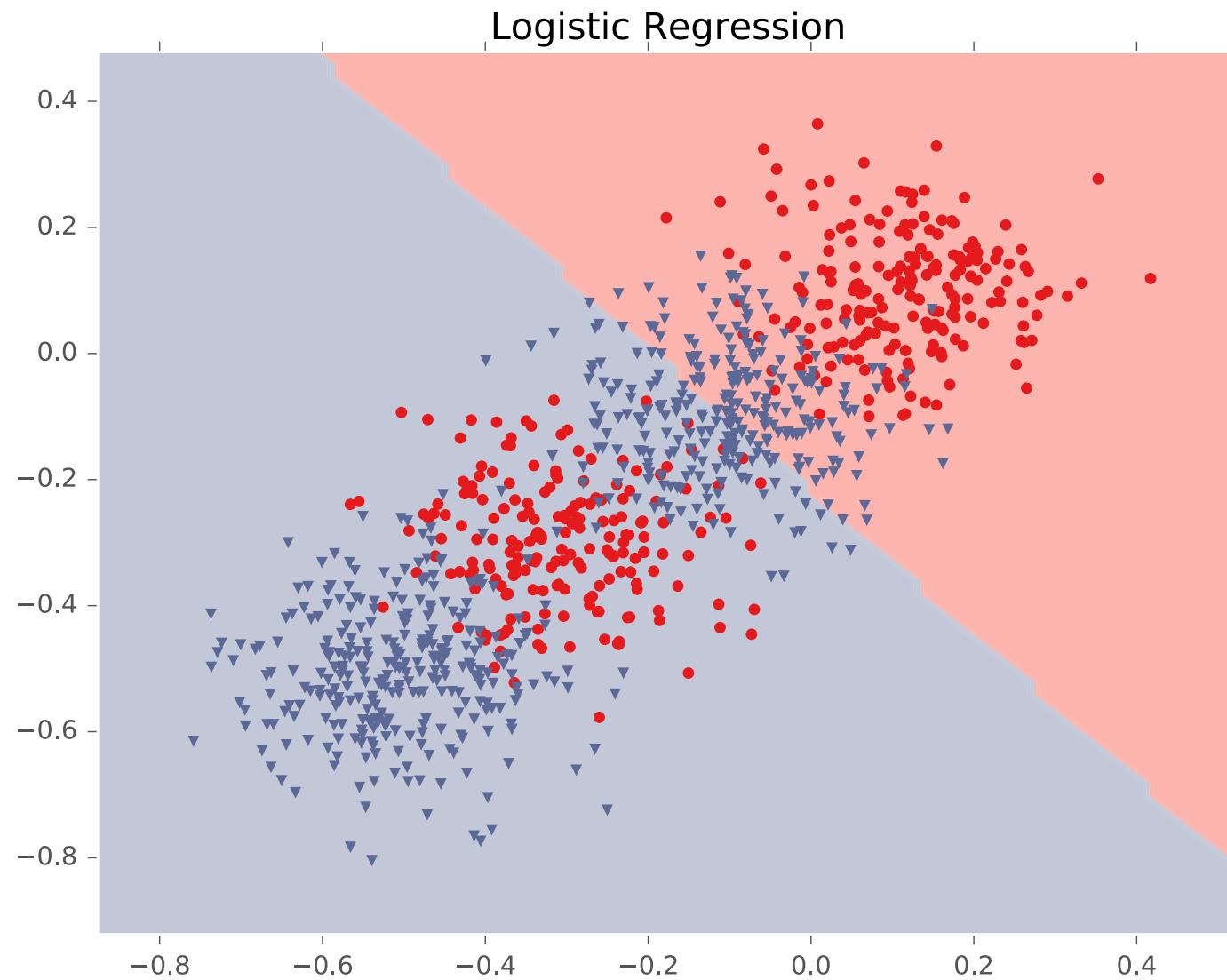
## Example #4: Two Pockets



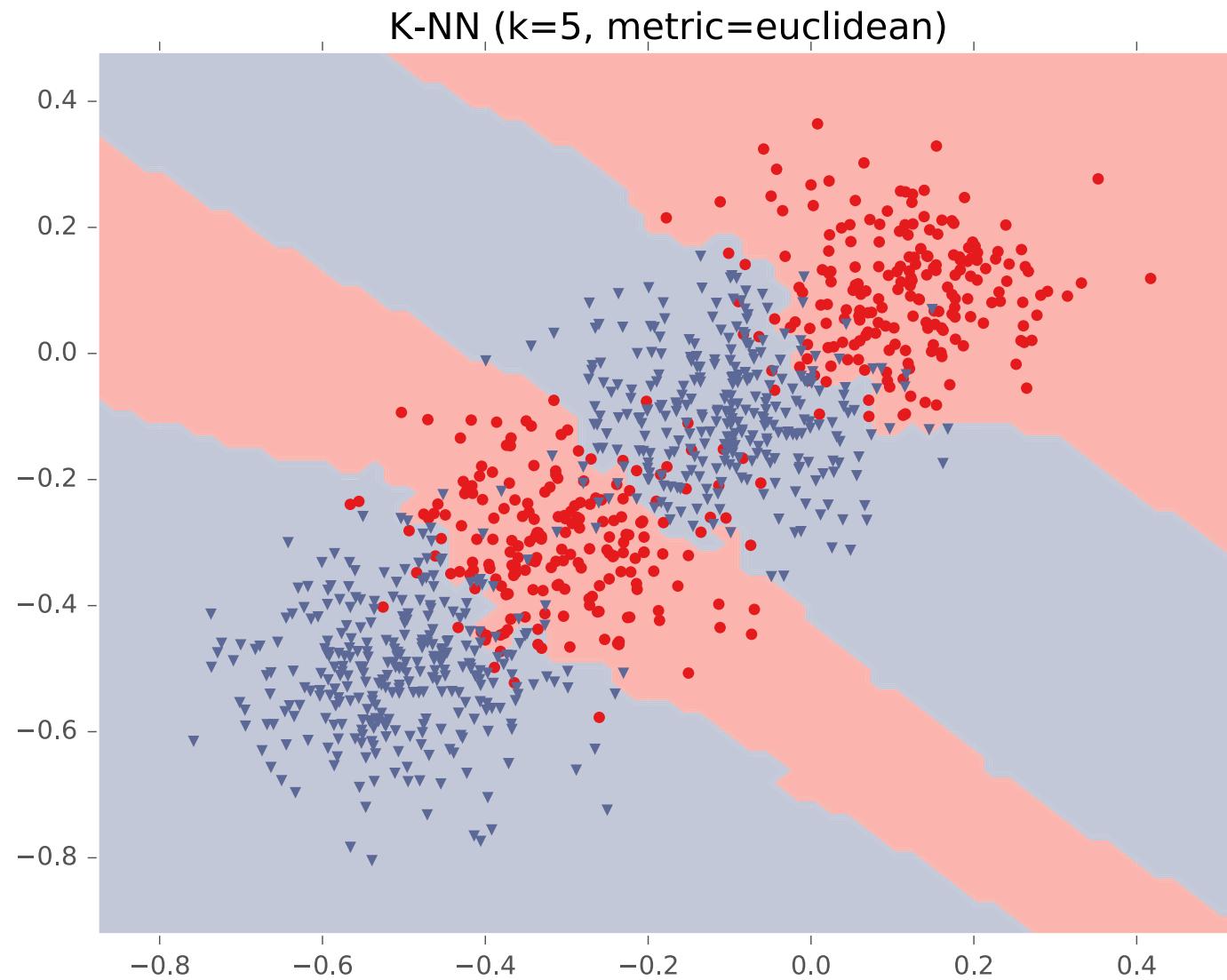
# Example #3: Four Gaussians



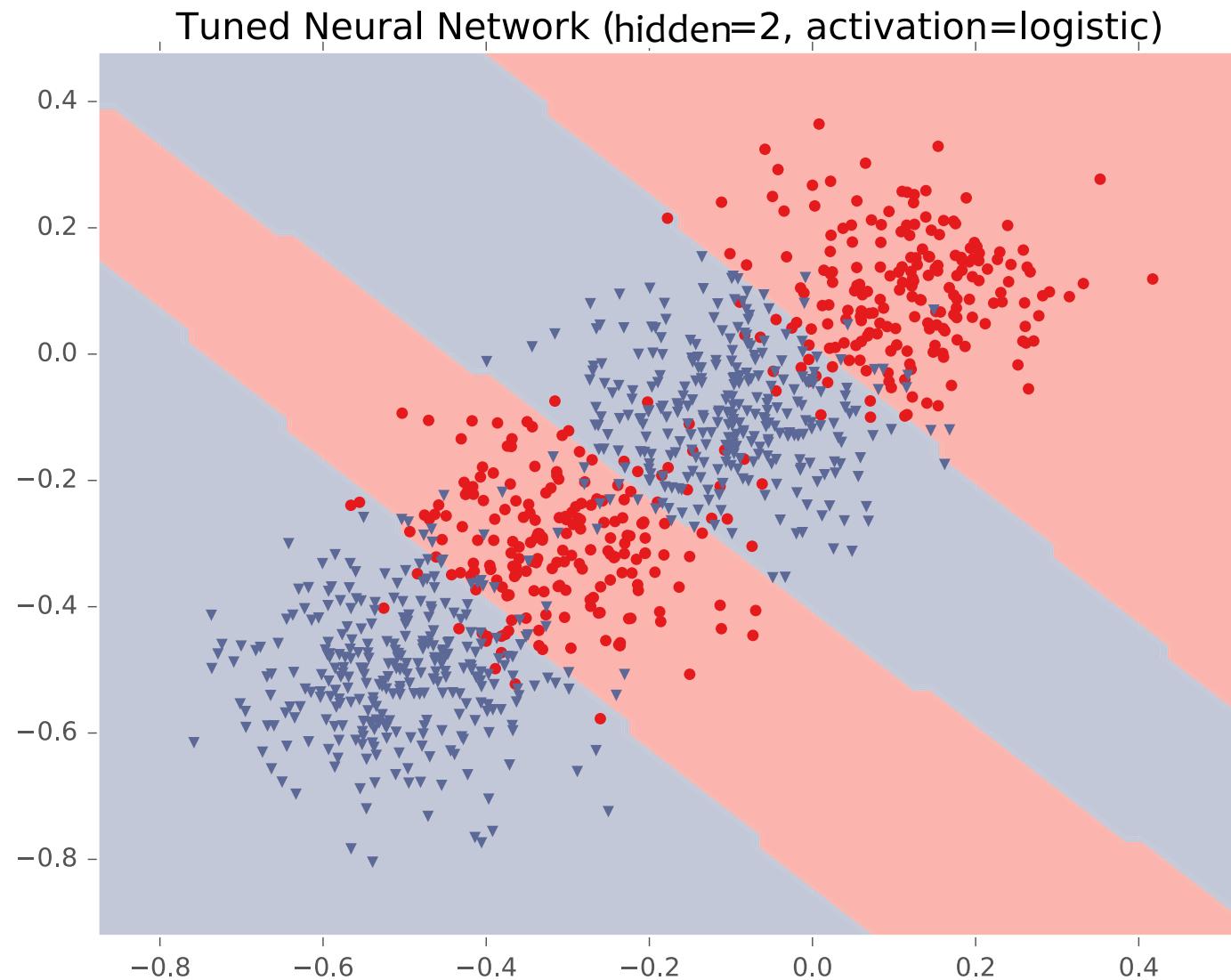
# Example #3: Four Gaussians



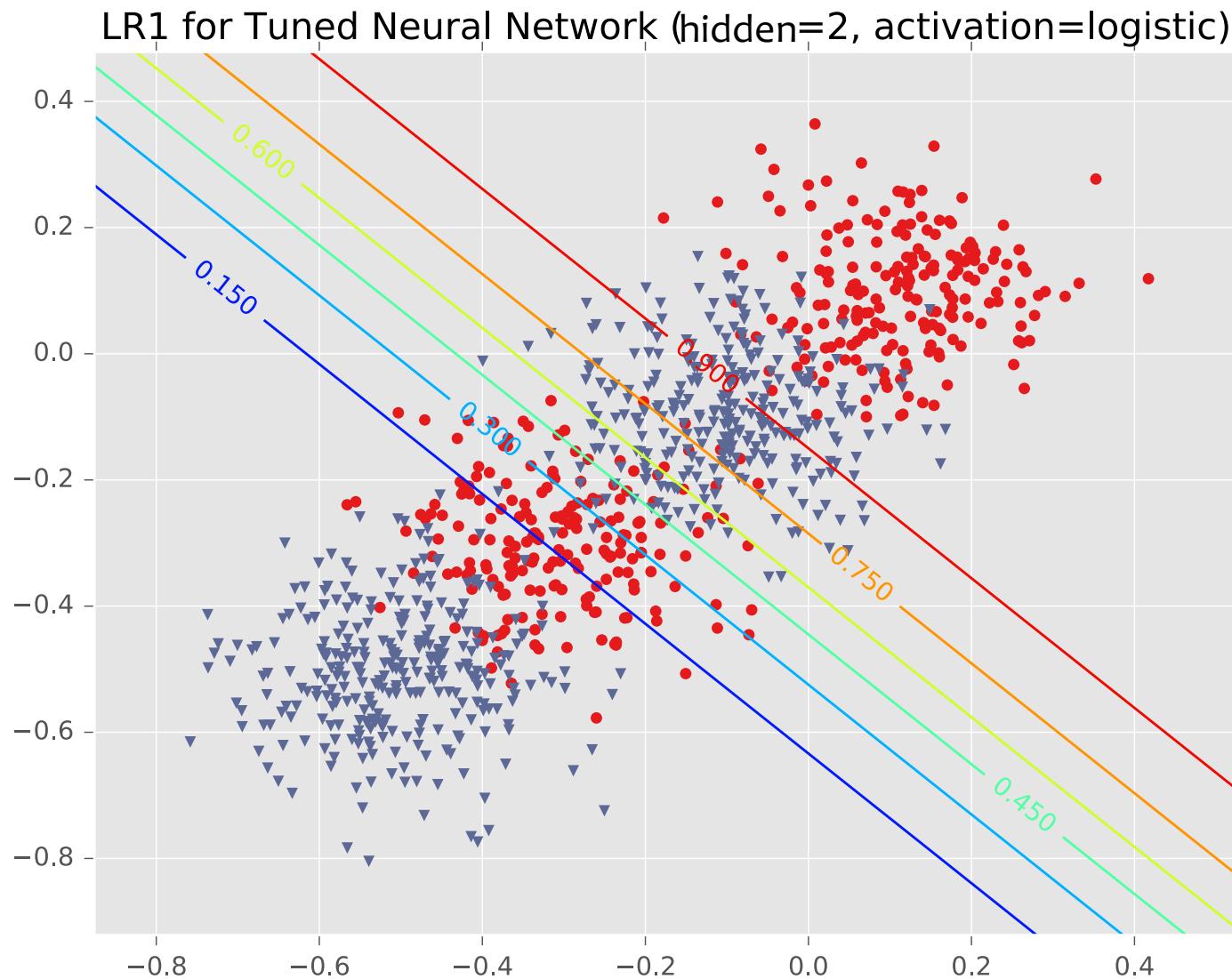
# Example #3: Four Gaussians



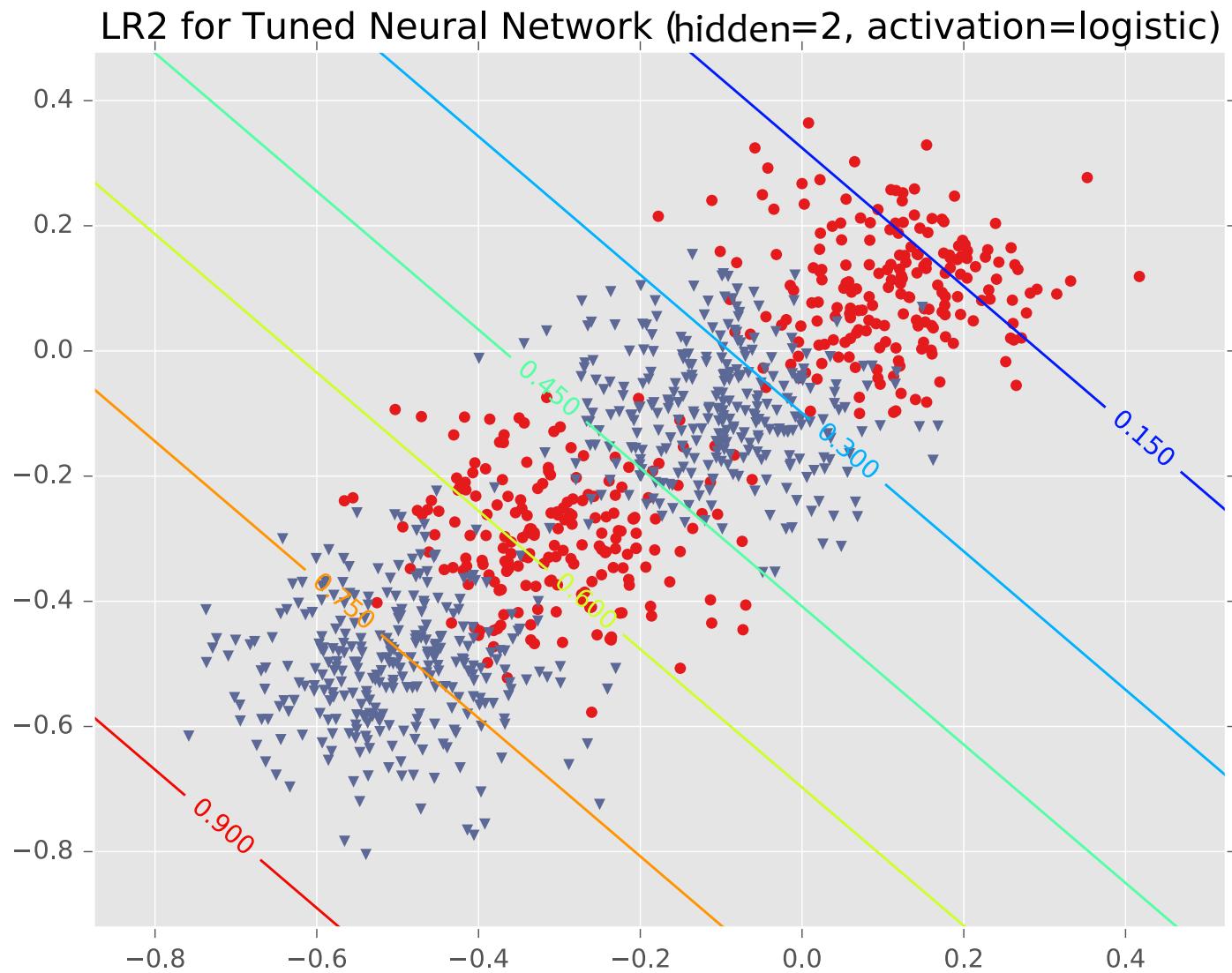
# Example #3: Four Gaussians



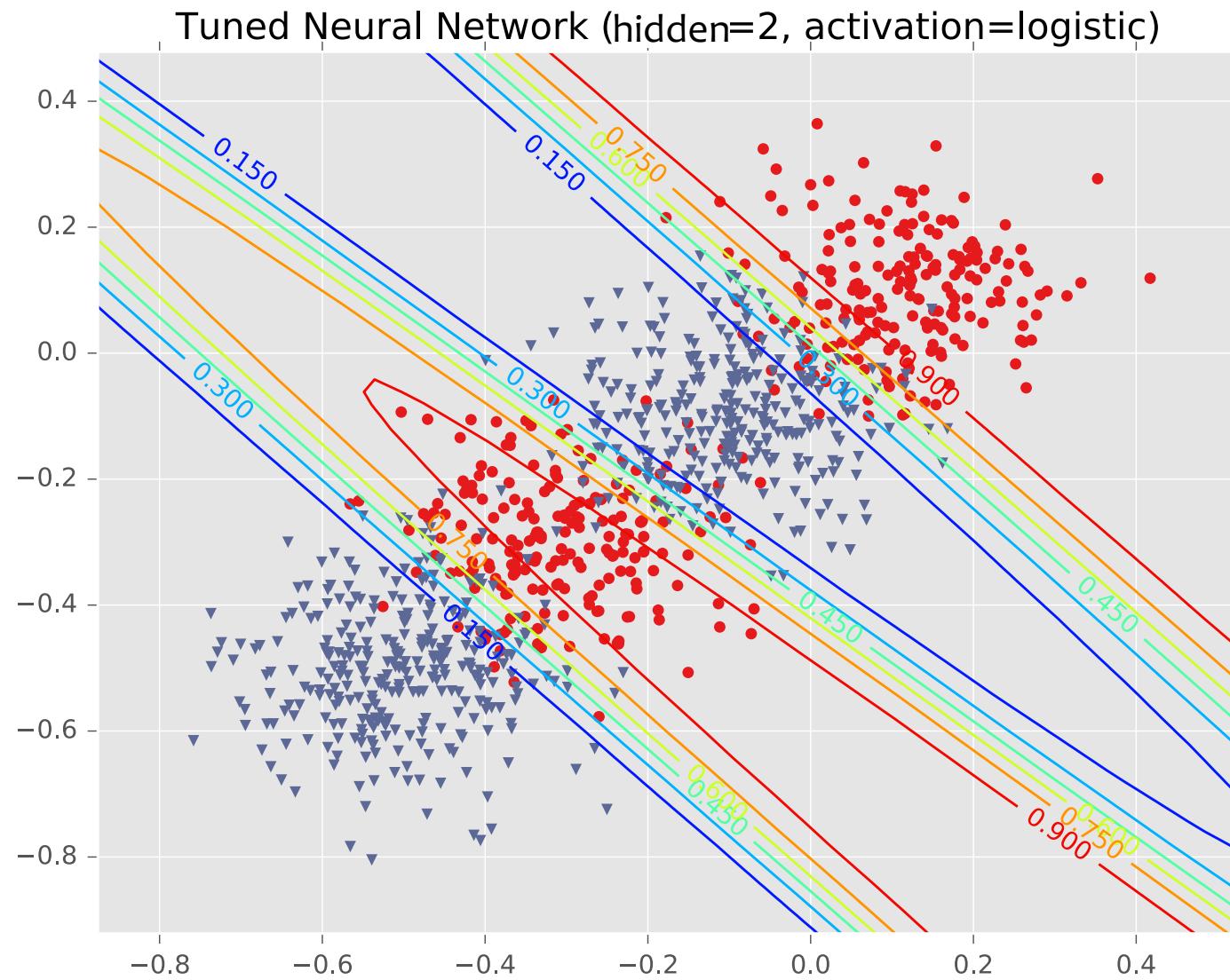
# Example #3: Four Gaussians



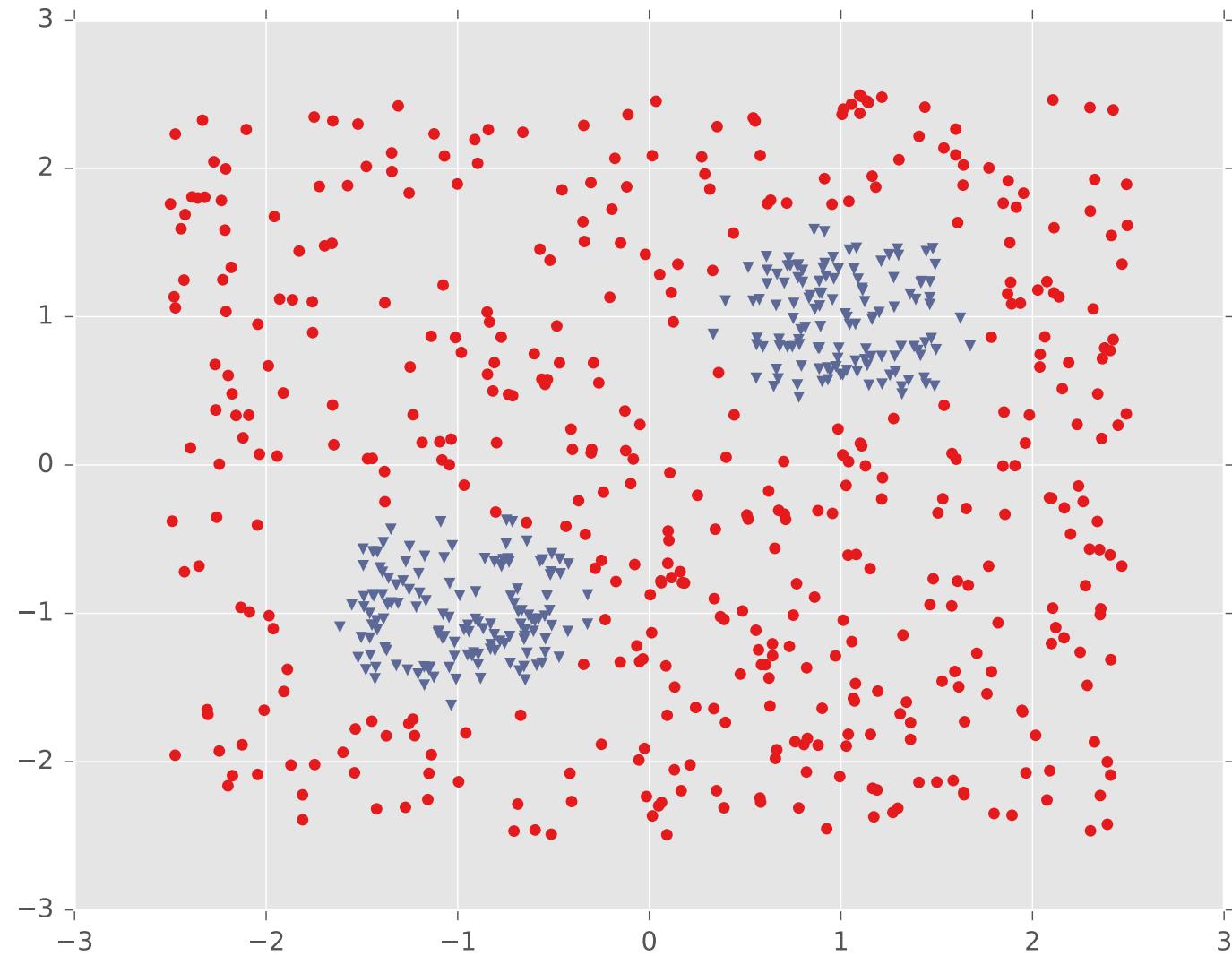
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# Example #3: Four Gaussians

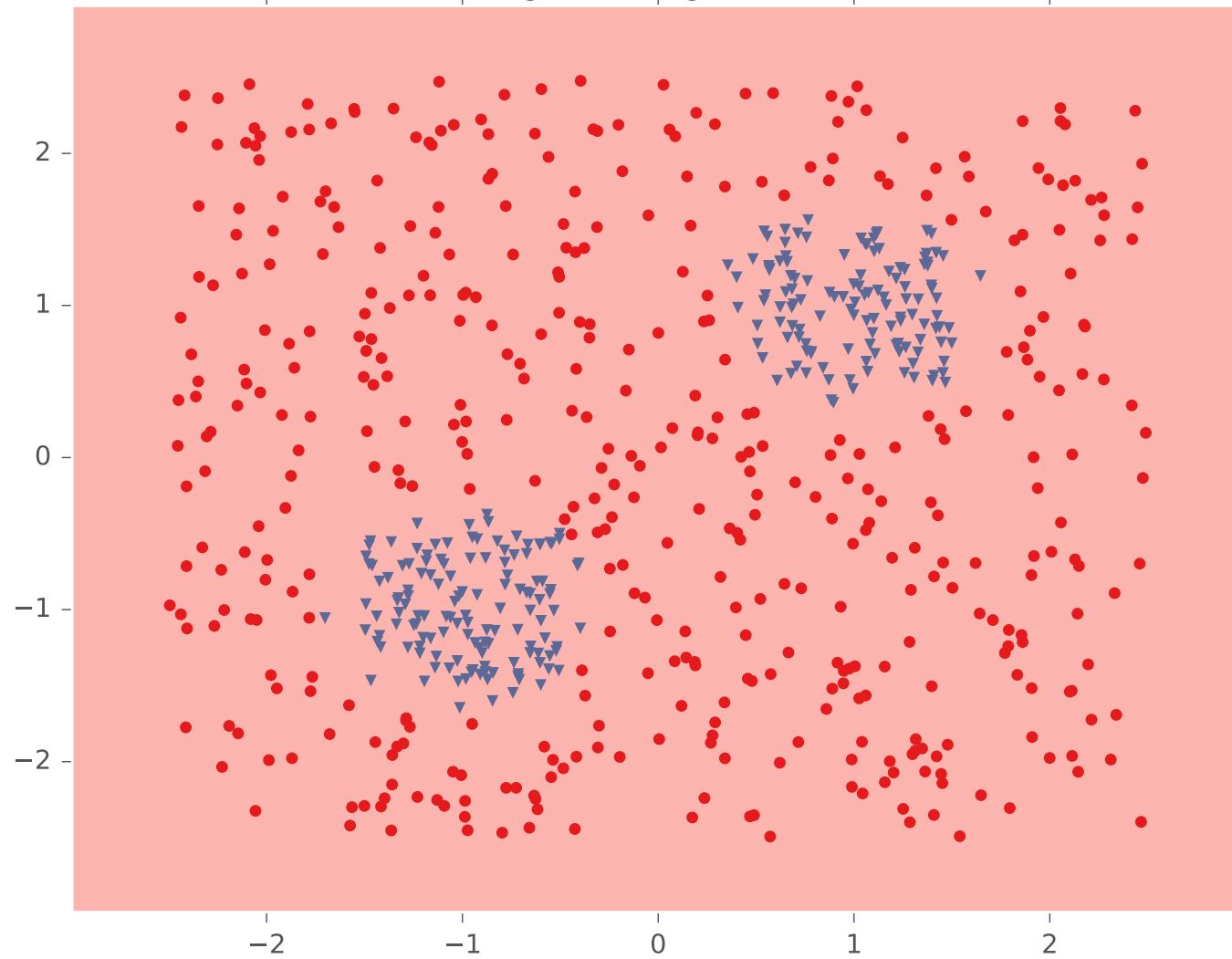


# Example #4: Two Pockets



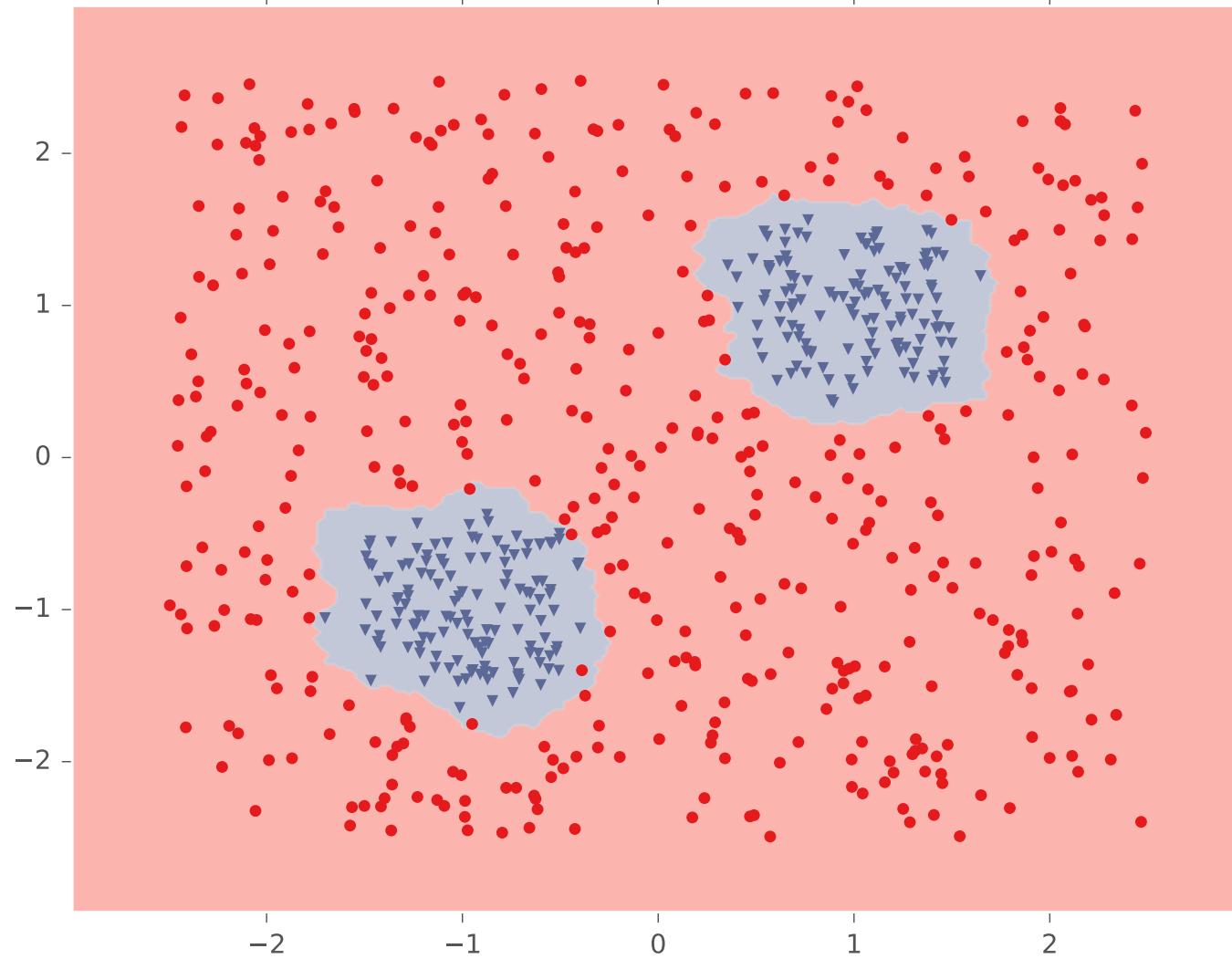
# Example #4: Two Pockets

Logistic Regression



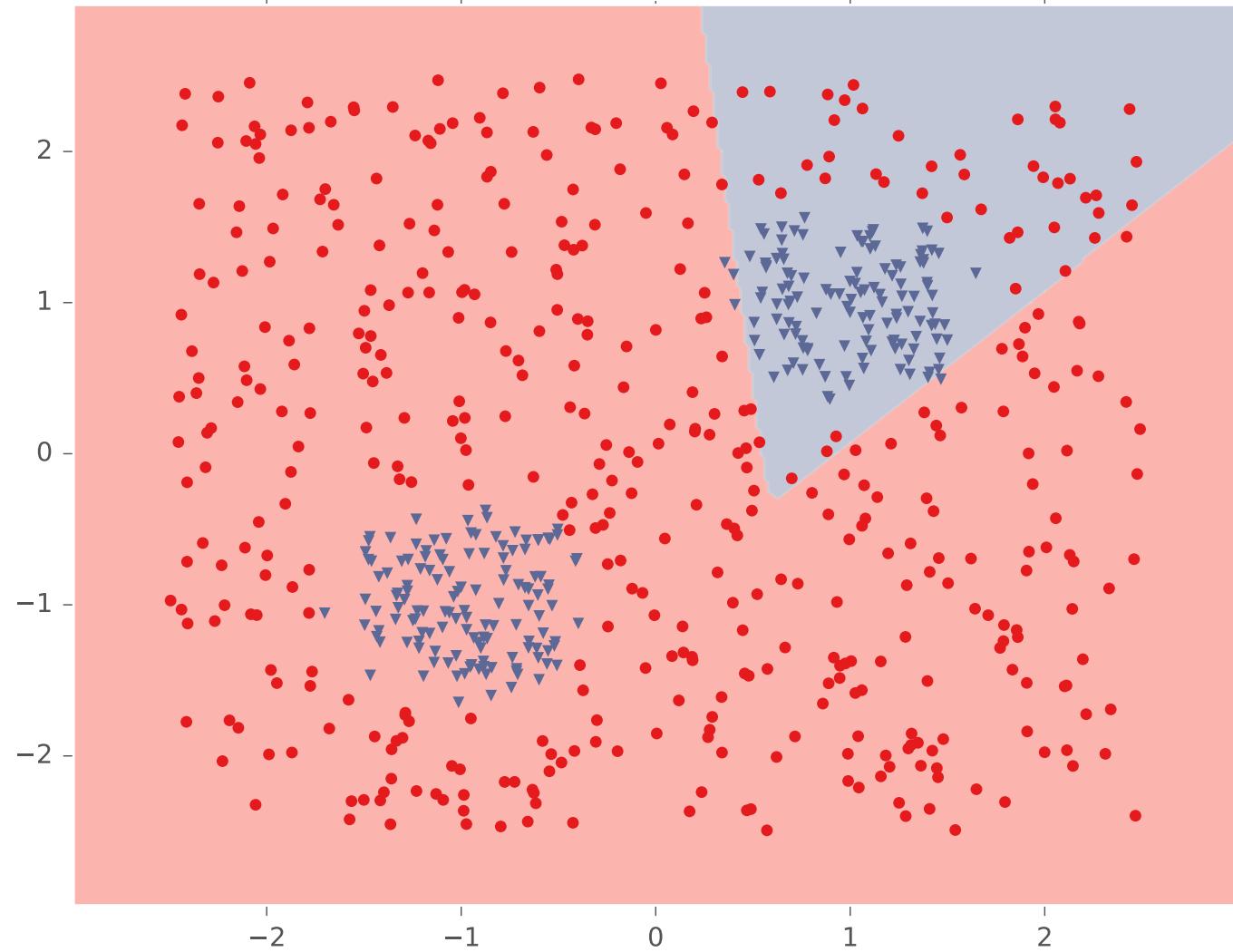
# Example #4: Two Pockets

K-NN (k=5, metric=euclidean)



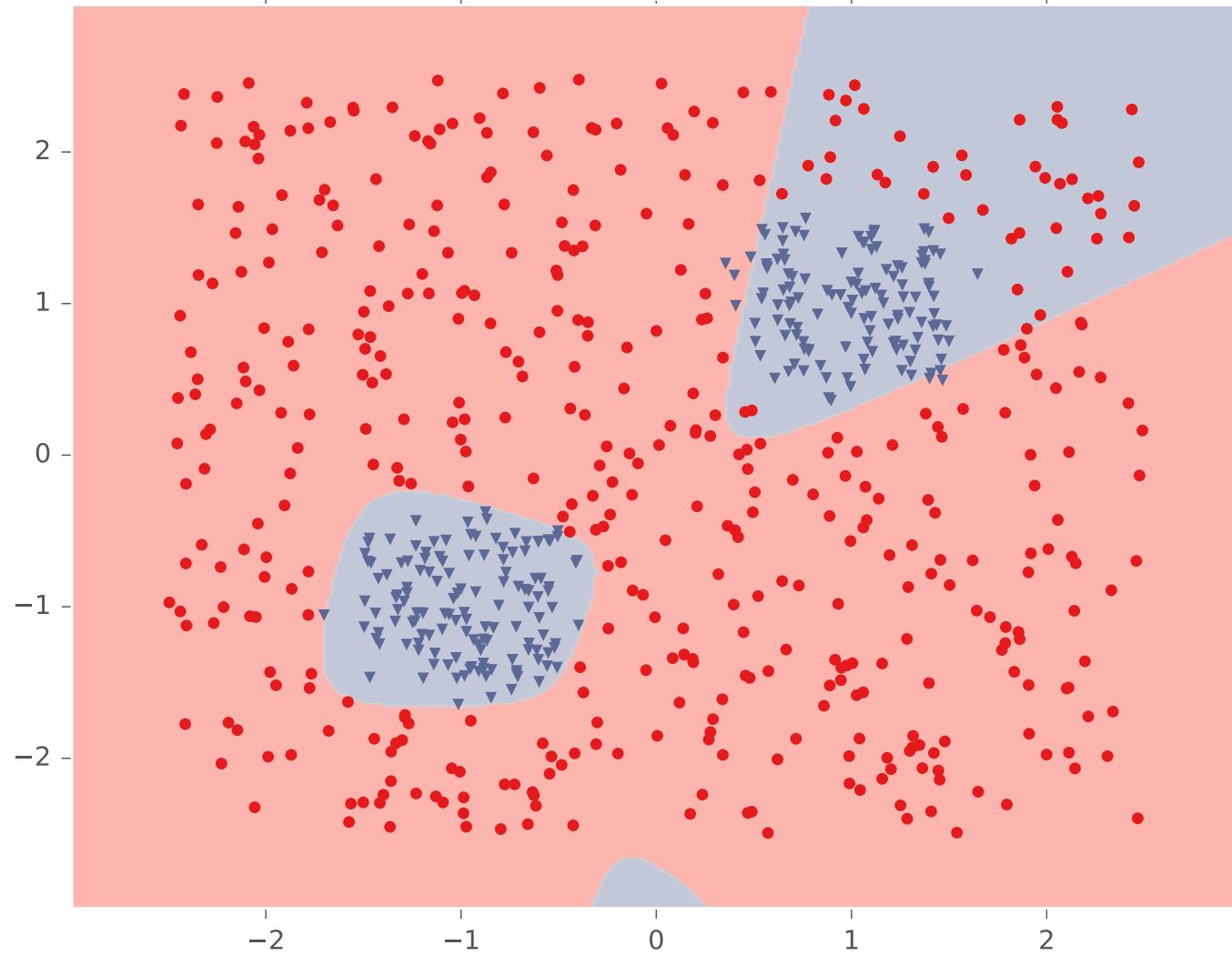
# Example #4: Two Pockets

Tuned Neural Network (hidden=2, activation=logistic)



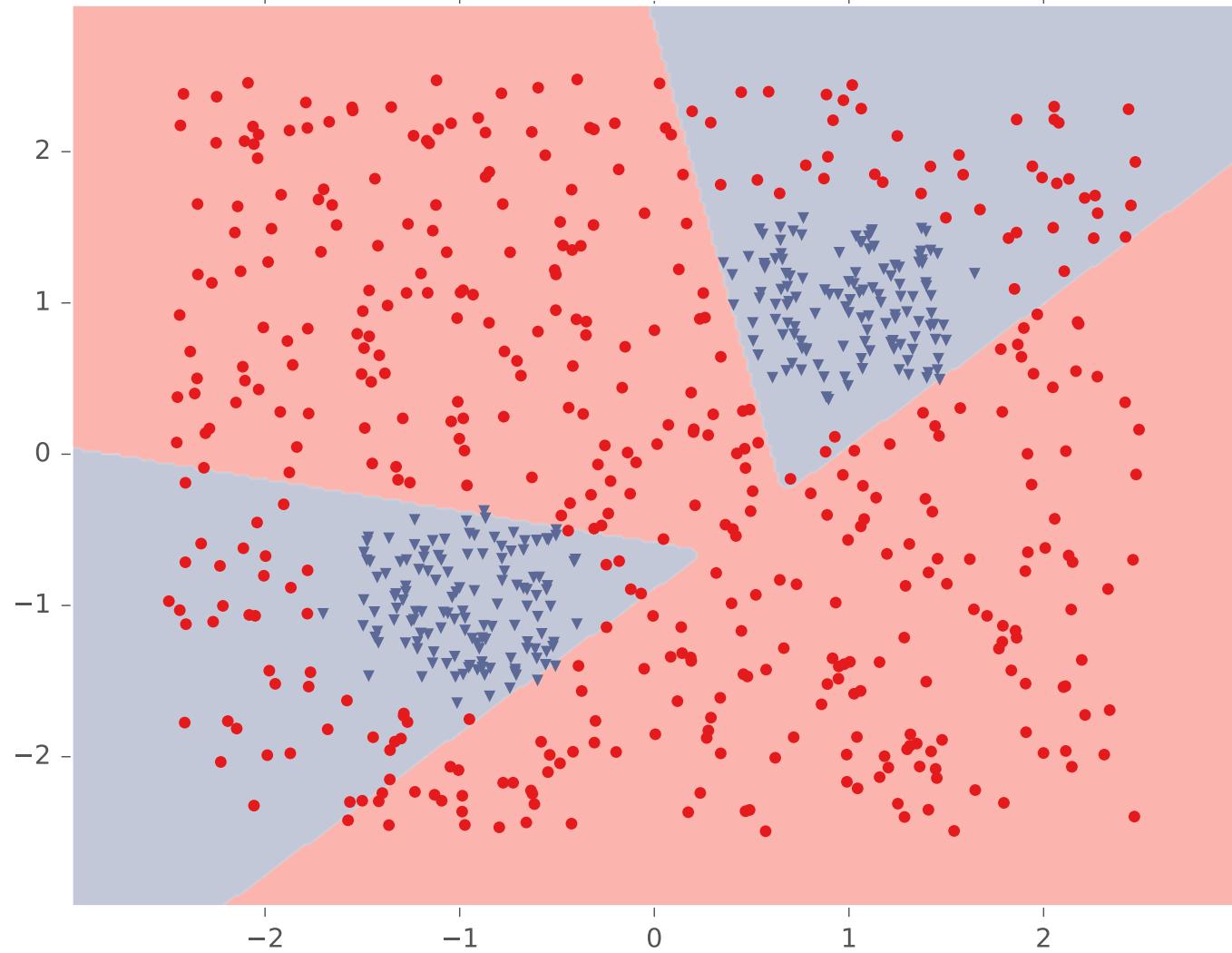
# Example #4: Two Pockets

Tuned Neural Network (hidden=3, activation=logistic)



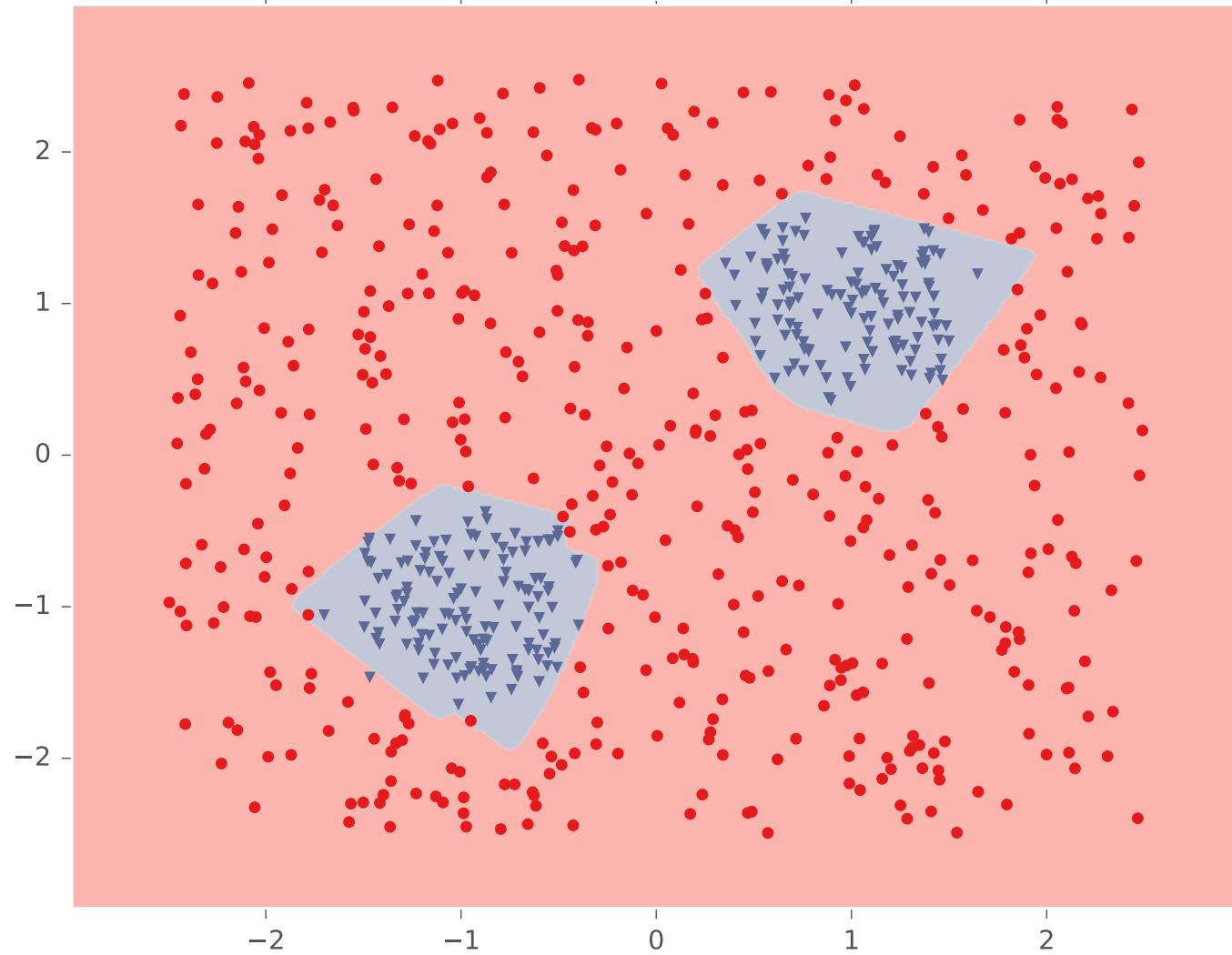
# Example #4: Two Pockets

Tuned Neural Network (hidden=4, activation=logistic)



# Example #4: Two Pockets

Tuned Neural Network (hidden=10, activation=logistic)



# **BUILDING DEEPER NETWORKS**

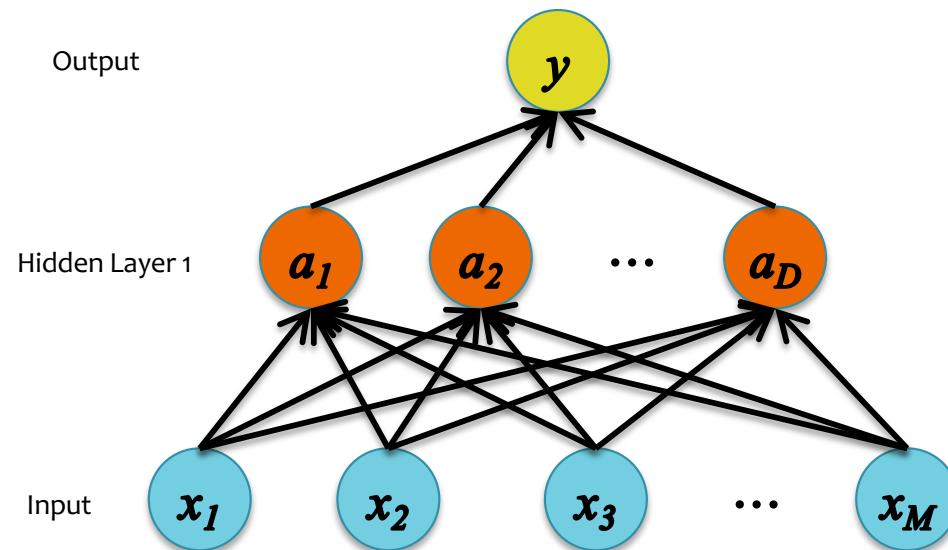
# Neural Networks

## Whiteboard

- Example: Neural Network w/2 Hidden Layers
- Example: Feed Forward Neural Network  
(matrix form)

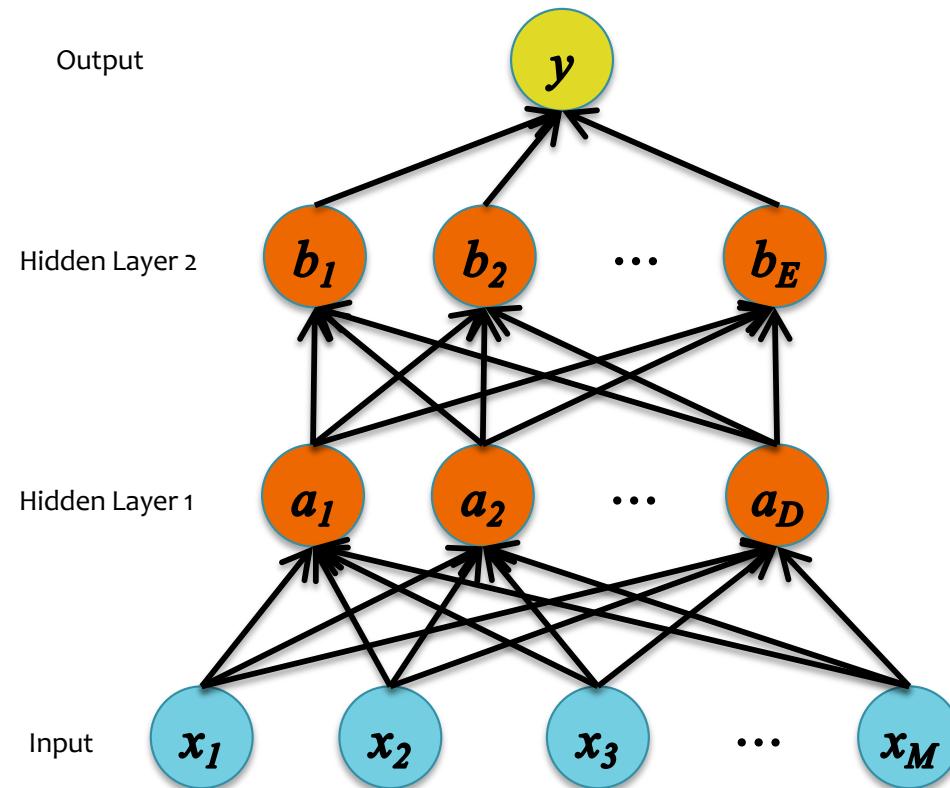
# Deeper Networks

Q: How many *layers* should we use?



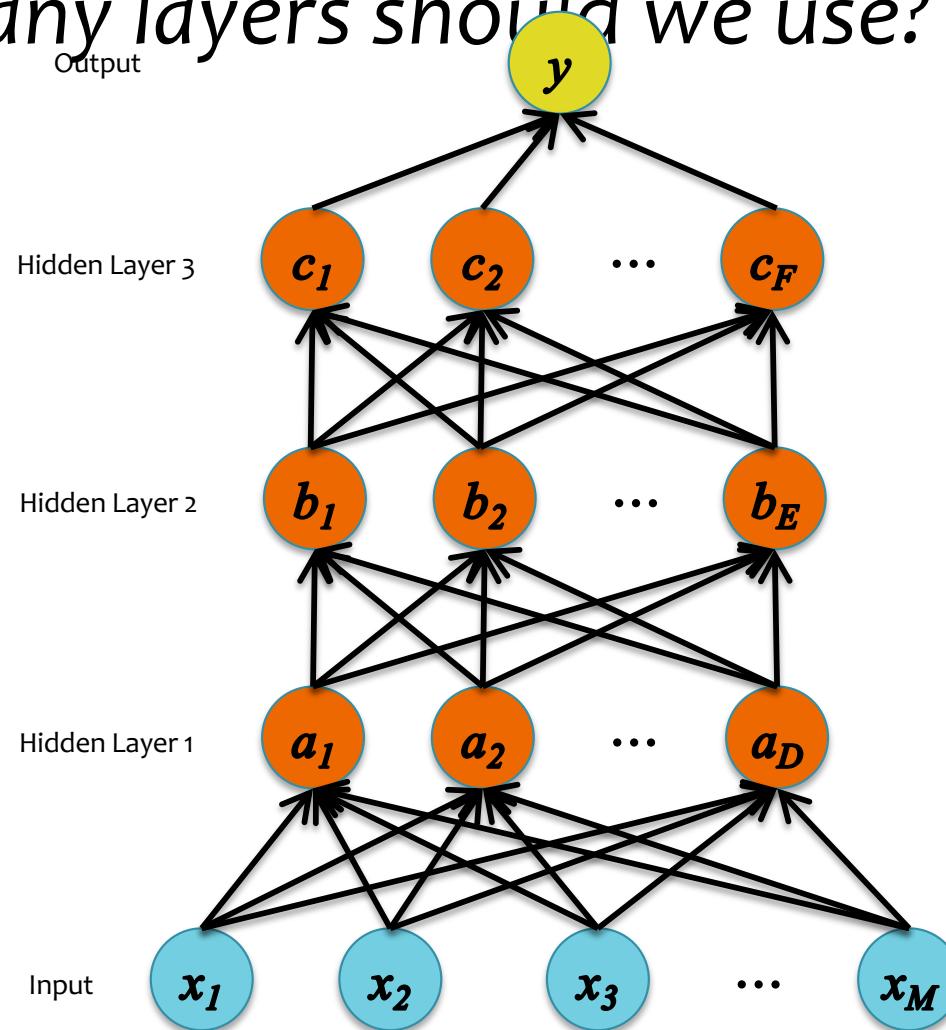
# Deeper Networks

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# Deeper Networks

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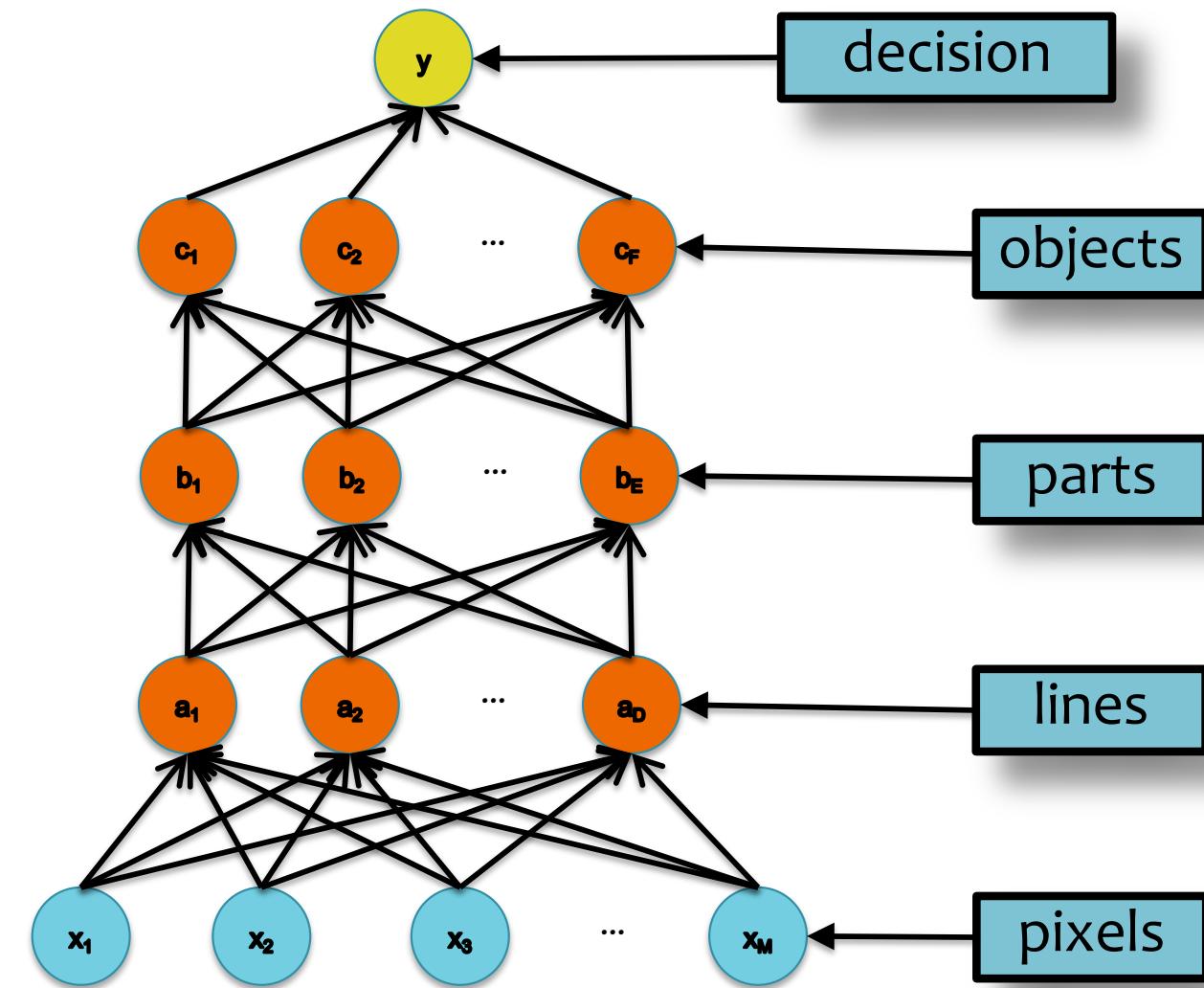
# Deeper Networks

Q: How many layers should we use?

- **Theoretical answer:**
  - A neural network with 1 hidden layer is a **universal function approximator**
  - Cybenko (1989): For any continuous function  $g(\mathbf{x})$ , there exists a 1-hidden-layer neural net  $h_\theta(\mathbf{x})$  s.t.  $|h_\theta(\mathbf{x}) - g(\mathbf{x})| < \epsilon$  for all  $\mathbf{x}$ , assuming sigmoid activation functions
- **Empirical answer:**
  - Before 2006: “Deep networks (e.g. 3 or more hidden layers) are too hard to train”
  - After 2006: “Deep networks are easier to train than shallow networks (e.g. 2 or fewer layers) for many problems”

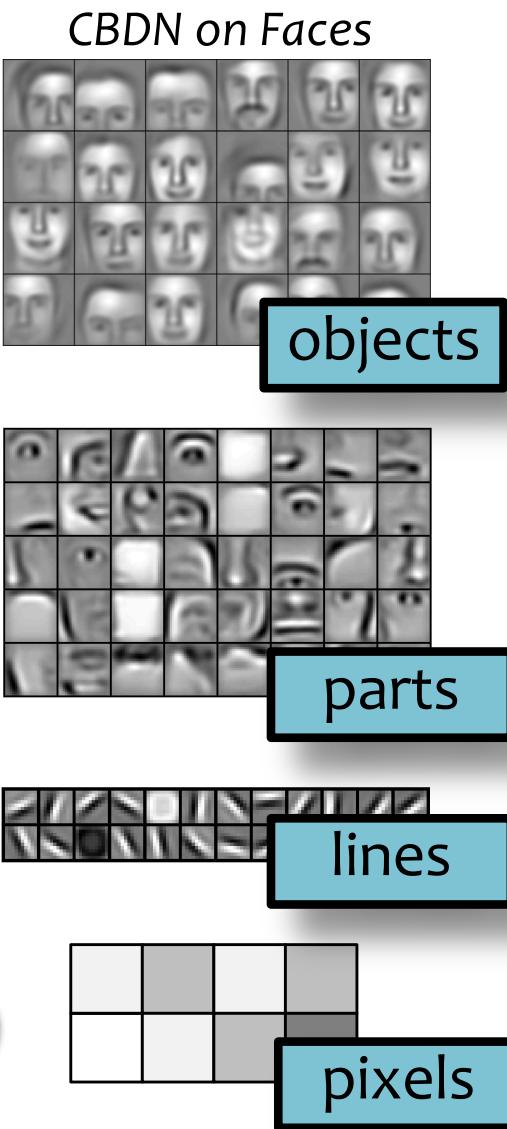
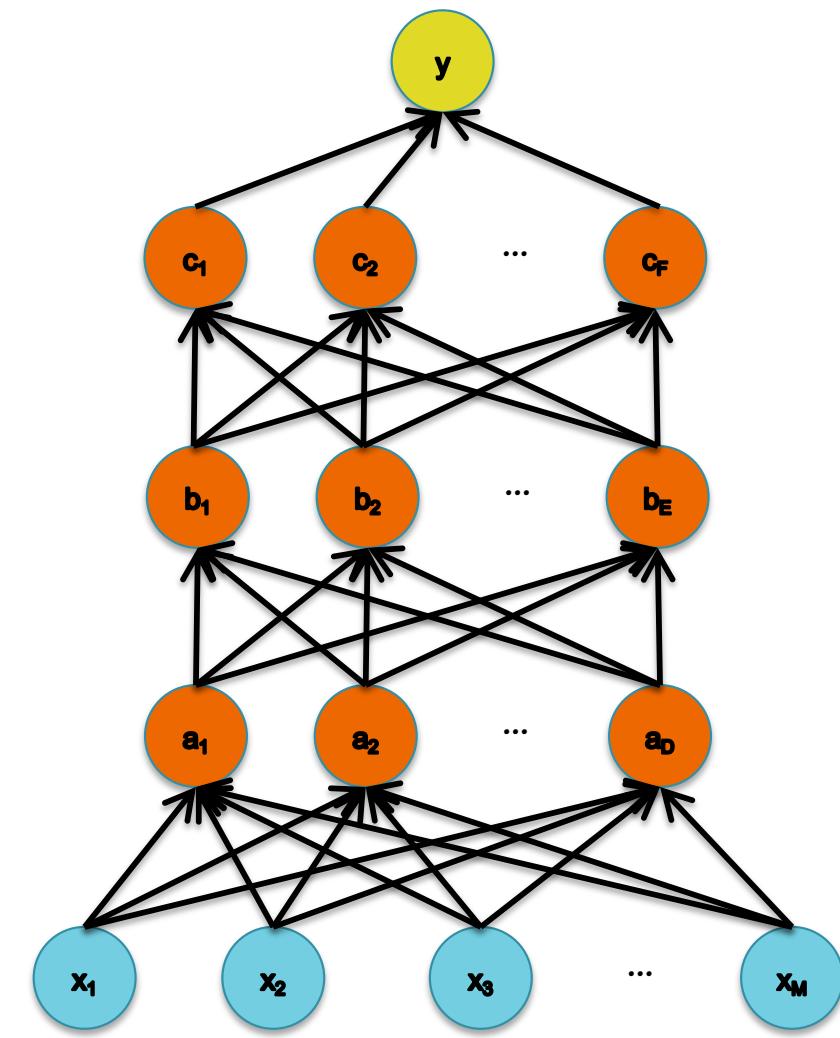
Big caveat: You need to know and use the right tricks.

# Feature Learning



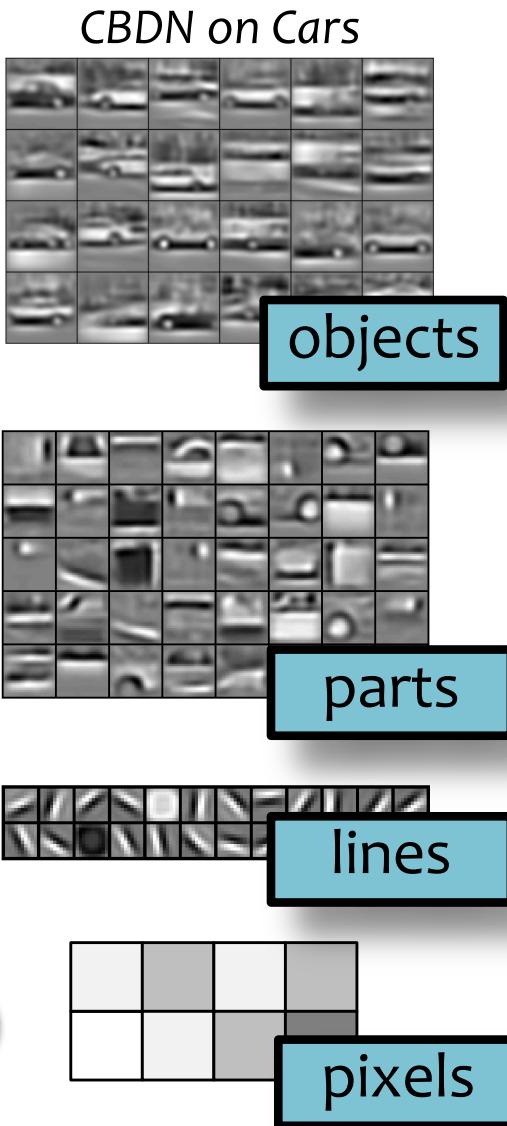
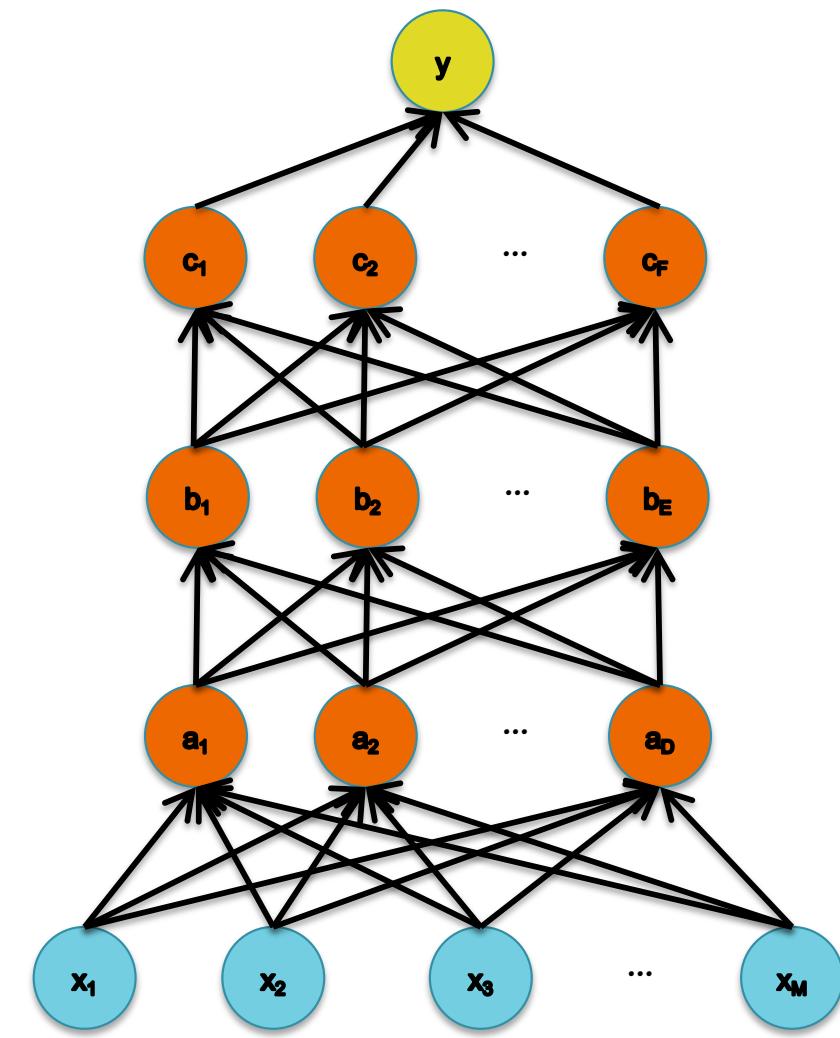
- **Traditional feature engineering:** build up levels of abstraction by hand
- **Deep networks** (e.g. convolution networks): learn the increasingly higher levels of abstraction from data
  - each layer is a learned feature representation
  - sophistication increases in higher layers

# Feature Learning



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# Feature Learning



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