15-744: Computer Networking

L-14 Network Topology

Sensor Networks

- Structural generators
- Power laws
- HOT graphs
- Graph generators
- Assigned reading
  - On Power-Law Relationships of the Internet Topology
  - A First Principles Approach to Understanding the Internet's Router-level Topology

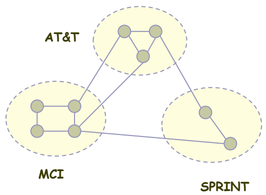
Outline

- Motivation/Background
- Power Laws
- Optimization Models
- Graph Generation

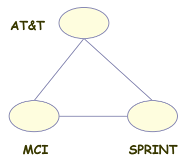
Why study topology?

- Correctness of network protocols typically independent of topology
- Performance of networks critically dependent on topology
  - e.g., convergence of route information
- Internet impossible to replicate
- Modeling of topology needed to generate test topologies

Internet topologies



Router level



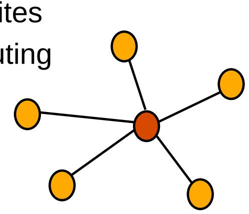
Autonomous System (AS) level

More on topologies..

- Router level topologies reflect physical connectivity between nodes
  - Inferred from tools like *traceroute* or well known public measurement projects like Mercator and Skitter
- AS graph reflects a peering relationship between two providers/clients
  - Inferred from inter-domain routers that run BGP and publlic projects like Oregon Route Views
- Inferring both is difficult, and often inaccurate

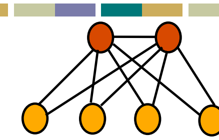
Hub-and-Spoke Topology

- Single hub node
  - Common in enterprise networks
  - Main location and satellite sites
  - Simple design and trivial routing
- Problems
  - Single point of failure
  - Bandwidth limitations
  - High delay between sites
  - Costs to backhaul to hub

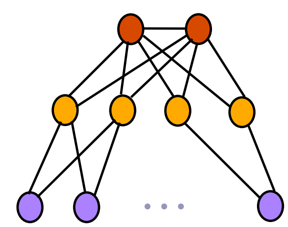


Simple Alternatives to Hub-and-Spoke

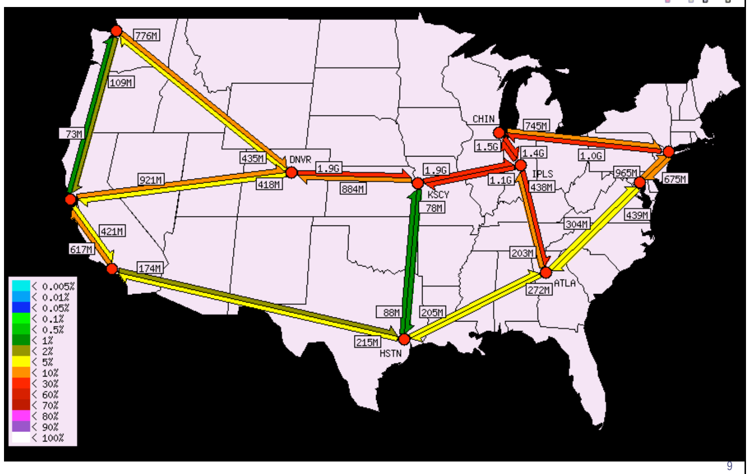
- Dual hub-and-spoke
  - Higher reliability
  - Higher cost
  - Good building block



- Levels of hierarchy
  - Reduce backhaul cost
  - Aggregate the bandwidth
  - Shorter site-to-site delay



Abilene Internet2 Backbone



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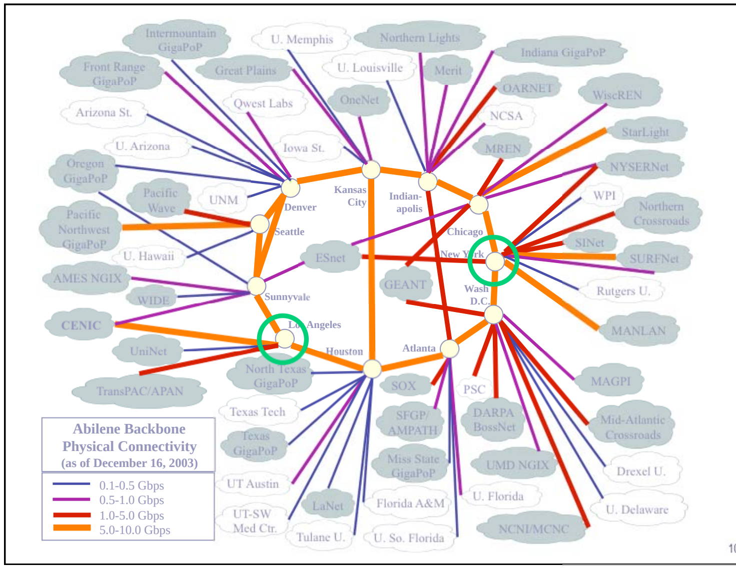

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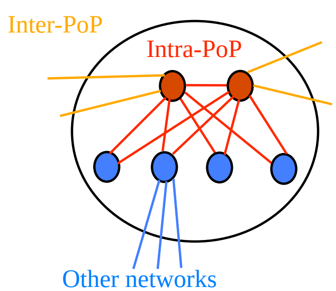
Points-of-Presence (PoPs)

- Inter-PoP links
  - Long distances
  - High bandwidth
- Intra-PoP links
  - Short cables between racks or floors
  - Aggregated bandwidth
- Links to other networks
  - Wide range of media and bandwidth



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Deciding Where to Locate Nodes and Links

- Placing Points-of-Presence (PoPs)
  - Large population of potential customers
  - Other providers or exchange points
  - Cost and availability of real-estate
  - Mostly in major metropolitan areas
- Placing links between PoPs
  - Already fiber in the ground
  - Needed to limit propagation delay
  - Needed to handle the traffic load

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Trends in Topology Modeling

Observation / **Modeling Approach**

- Long-range links are expensive — Random graph (Waxman88)
- Real networks are not random, but have obvious hierarchy — Structural models (GT-ITM Calvert/Zegura, 1996)
- Internet topologies exhibit power law degree distributions (Faloutsos et al., 1999) — Degree-based models replicate power-law degree sequences
- Physical networks have hard technological (and economic) constraints. — Optimization-driven models topologies consistent with design tradeoffs of network engineers

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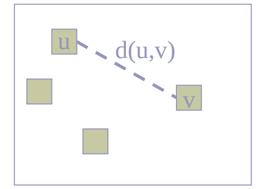
Waxman model (Waxman 1988)

- Router level model
- Nodes placed at random in 2-d space with dimension L
- Probability of edge (u,v):
  - ae^{-d/(bL)}, where d is Euclidean distance (u,v), a and b are constants
- Models locality



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Real world topologies

- Real networks exhibit
  - Hierarchical structure
  - Specialized nodes (transit, stub..)
  - Connectivity requirements
  - Redundancy
- Characteristics incorporated into the Georgia Tech Internetwork Topology Models (GT-ITM) simulator (E. Zegura, K.Calvert and M.J. Donahoo, 1995)

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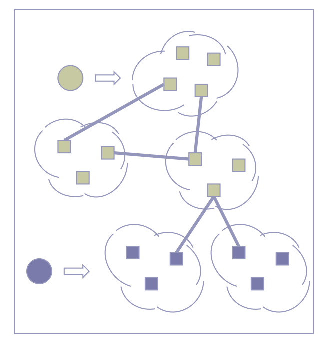
Transit-stub model (Zegura 1997)

- Router level model
- Transit domains
  - placed in 2-d space
  - populated with routers
  - connected to each other
- Stub domains
  - placed in 2-d space
  - populated with routers
  - connected to transit domains
- Models hierarchy



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So…are we done?

- No!
- In 1999, Faloutsos, Faloutsos and Faloutsos published a paper, demonstrating power law relationships in Internet graphs
- Specifically, the node degree distribution exhibited power laws

That Changed Everything…..

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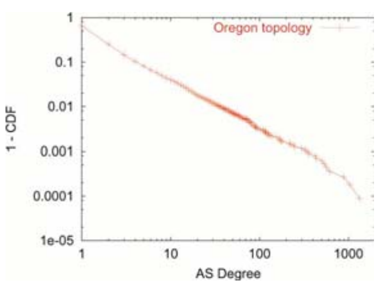
Power laws in AS level topology



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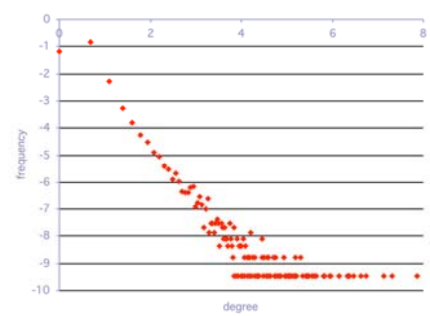
Power Laws

- Faloutsos[3] (Sigcomm'99)
  - frequency vs. degree



topology from BGP tables of 18 routers

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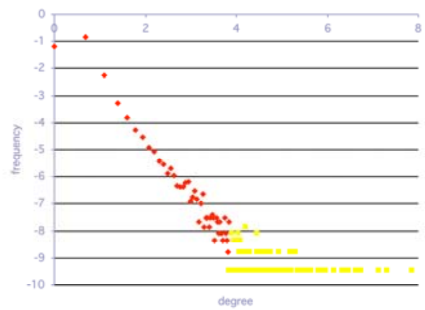

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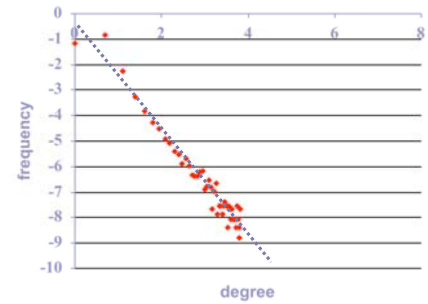

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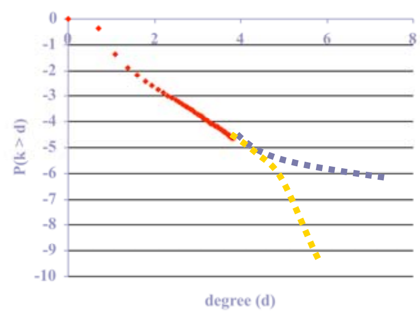
Power Laws

- Faloutsos
  - frequency vs. degree
  - empirical ccdf $P(d>x) \sim x^{-a}$



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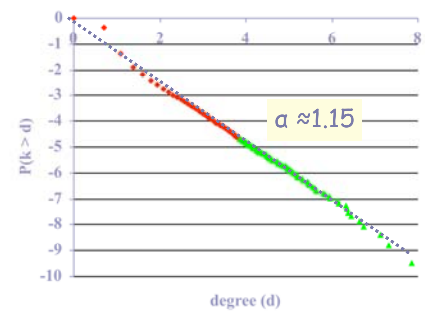

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GT-ITM abandoned..

- GT-ITM did not give power law degree graphs
- New topology generators and explanation for power law degrees were sought
- Focus of generators to match degree distribution of observed graph

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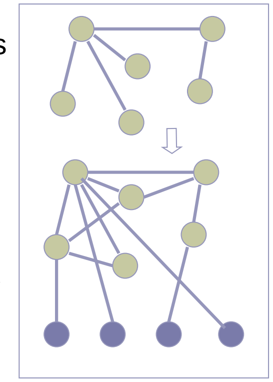
Inet (Jin 2000)

- Generate degree sequence
- Build spanning tree over nodes with degree larger than 1, using preferential connectivity
  - randomly select node u not in tree
  - join u to existing node v with probability d(v)/Σd(w)
- Connect degree 1 nodes using preferential connectivity
- Add remaining edges using preferential connectivity



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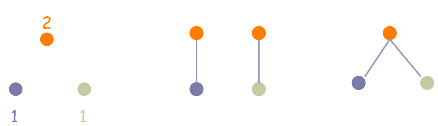
Power law random graph (PLRG)

- Operations
  - assign degrees to nodes drawn from power law distribution
  - create kv copies of node v; kv degree of v.
  - randomly match nodes in pool
  - aggregate edges



may be disconnected, contain multiple edges, self-loops

- contains unique giant component for right choice of parameters

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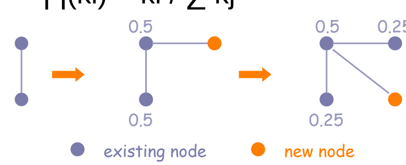
Barabasi model: fixed exponent

- incremental growth
  - initially, m0 nodes
  - step: add new node i with m edges
- linear preferential attachment
  - connect to node i with probability

$$\prod(k_i) = k_i / \sum k_j$$



may contain multi-edges, self-loops

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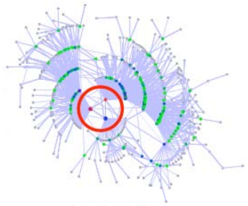
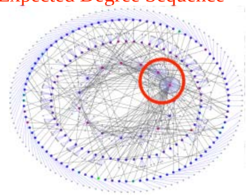
Features of Degree-Based Models

Preferential Attachment



Expected Degree Sequence



- Degree sequence follows a power law (by construction)
- High-degree nodes correspond to highly connected central “hubs”, which are crucial to the system
- Achilles’ heel: robust to random failure, fragile to specific attack

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Does Internet graph have these properties?

- No…(There is no Memphis!)
- Emphasis on degree distribution - structure ignored
- Real Internet very structured
- Evolution of graph is highly constrained

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Problem With Power Law

- ... but they're descriptive models!
- No correct physical explanation, need an understanding of:
  - the driving force behind deployment
  - the driving force behind growth

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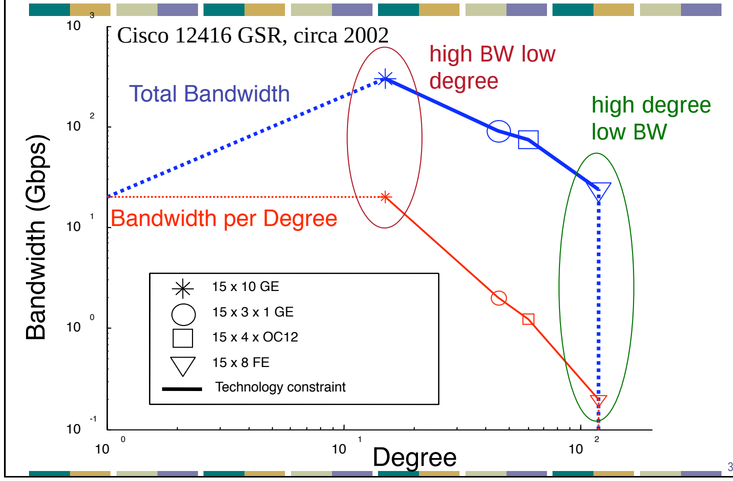
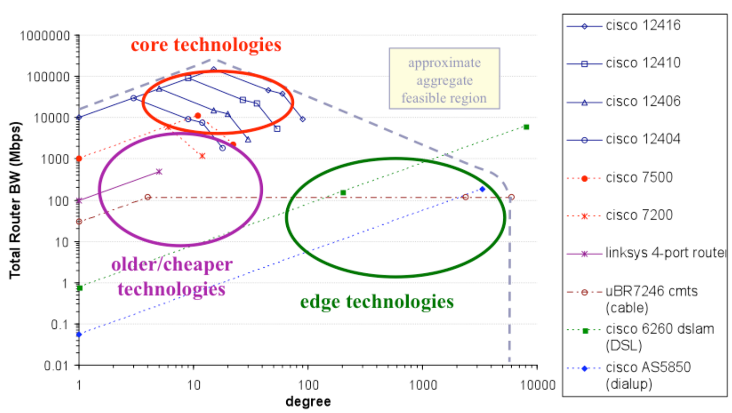
Li et al.

- Consider the explicit design of the Internet
  - Annotated network graphs (capacity, bandwidth)
  - Technological and economic limitations
  - Network performance
- Seek a theory for Internet topology that is explanatory and not merely descriptive.
  - Explain high variability in network connectivity
  - Ability to match large scale statistics (e.g. power laws) is only secondary evidence

Router Technology Constraint

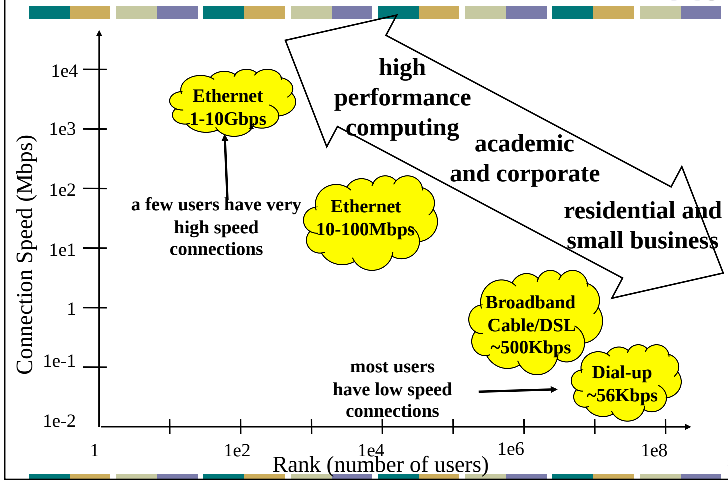


Aggregate Router Feasibility

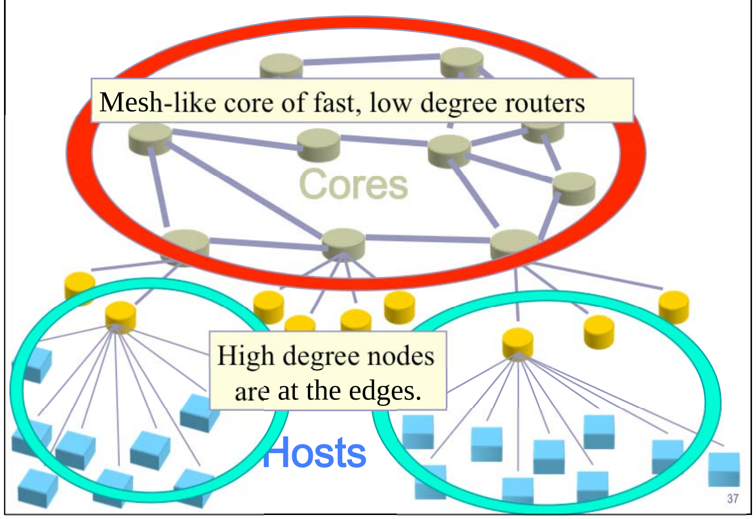


Source: Cisco Product Catalog, June 2002

Variability in End-User Bandwidths



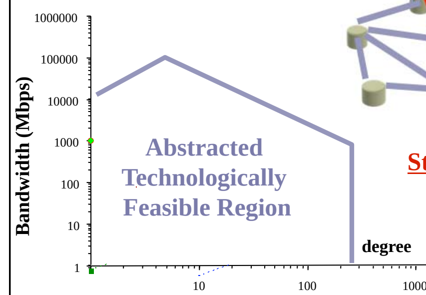
Heuristically Optimal Topology



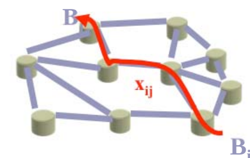
Comparison Metric: Network Performance

Given realistic technology constraints on routers, how well is the network able to carry traffic?

Step 1: Constrain to be feasible



Step 2: Compute traffic demand



$$x_{ij} \propto B_i B_j$$

Step 3: Compute max flow

$$\max_{\alpha} \sum_{i,j} x_{ij} = \max \sum_{i,j} \alpha B_i B_j$$

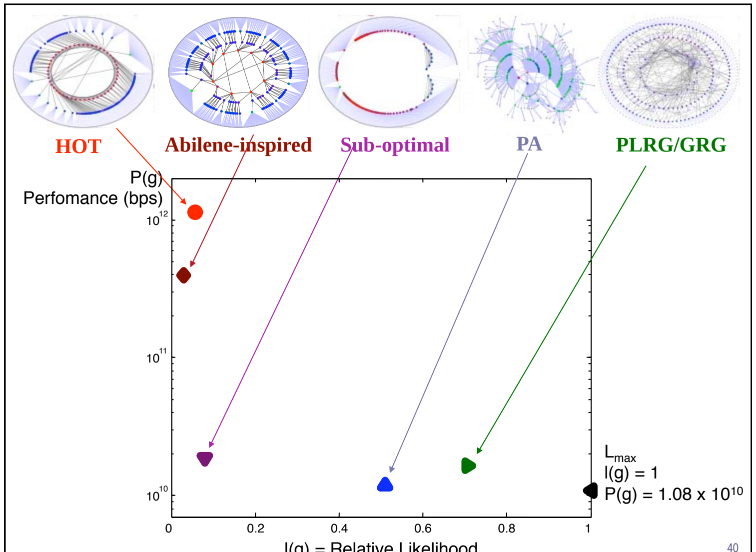
$$s.t. \sum_{i,j:k \in r_{ij}} x_{ij} \le B_k, \forall k$$

Likelihood-Related Metric

Define the metric $L(g) = \sum_{i,j \text{ connected}} d_i d_j$ (d_i = degree of node i)

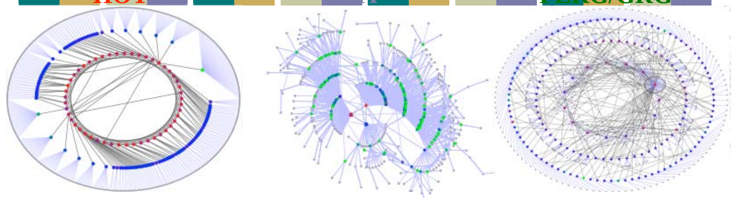
- Easily computed for any graph
- Depends on the structure of the graph, not the generation mechanism
- Measures how "hub-like" the network core is
- For graphs resulting from probabilistic construction (e.g. PLRG/GRG),

  LogLikelihood (LLH) $\propto L(g)$
- Interpretation: How likely is a particular graph (having given node degree distribution) to be constructed?

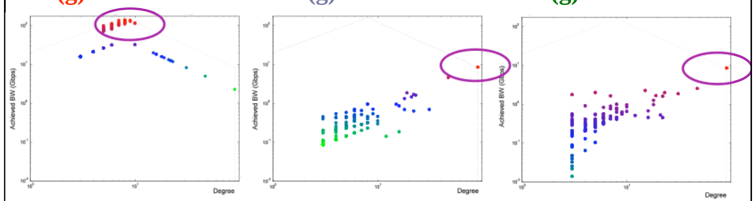


Structure Determines Performance

HOT — PA — PLRG/GRG



$P(g) = 1.13 \times 10^{12}$ — $P(g) = 1.19 \times 10^{10}$ — $P(g) = 1.64 \times 10^{10}$



Summary Network Topology

- Faloutsos[3] [SIGCOMM99] on Internet topology
  - Observed many "power laws" in the Internet structure
    - Router level connections, AS-level connections, neighborhood sizes
  - Power law observation refuted later, Lakhina [INFOCOM00]
- Inspired many degree-based topology generators
  - Compared properties of generated graphs with those of measured graphs to validate generator
  - What is wrong with these topologies? Li et al [SIGCOMM04]
    - Many graphs with similar distribution have different properties
    - Random graph generation models don't have network-intrinsic meaning
    - Should look at fundamental trade-offs to understand topology
      - Technology constraints and economic trade-offs
    - Graphs arising out of such generation better explain topology and its properties, but are unlikely to be generted by random processes!

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Graph Generation

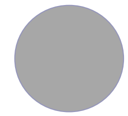
- Many important topology metrics
  - Spectrum
  - Distance distribution
  - Degree distribution
  - Clustering…
- No way to reproduce most of the important metrics
- No guarantee there will not be any other/ new metric found important

dK-series approach

- Look at inter-dependencies among topology characteristics
- See if by reproducing most basic, simple, but not necessarily practically relevant characteristics, we can also reproduce (capture) all other characteristics, including practically important
- Try to find the one(s) defining *all others*

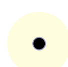
0K

Average degree <*k*>



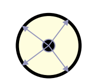
1K

Degree distribution *P(k)*



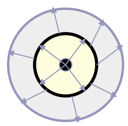
2K

Joint degree distribution $P(k_1,k_2)$

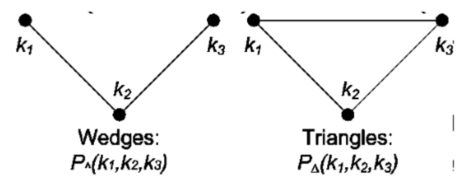


3K

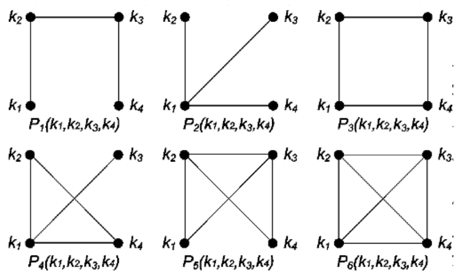
"Joint edge degree" distribution $P(k_1,k_2,k_3)$



3K, more exactly



4K



Definition of *dK*-distributions

dK-distributions are degree correlations within simple connected graphs of size *d*

Nice properties of properties P_d

- **Constructability**: we can construct graphs having properties P_d (*dK*-graphs)
- **Inclusion**: if a graph has property P_d, then it also has all properties P_i, with $i < d$ (*dK*-graphs are also *iK*-graphs)
- **Convergence**: the set of graphs having property P_n consists only of one element, *G* itself (*dK*-graphs converge to *G*)

Rewiring