
A New Boosting Algorithm Using Input-Dependent Regularizer

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Abstract

AdaBoost has proved to be an effective method to improve the performance of base classifiers both theoretically and empirically. However, previous studies have shown that AdaBoost might suffer from the overfitting problem, especially for noisy data. In addition, most current work on boosting assumes that the combination weights are fixed constants and therefore does not take particular input patterns into consideration. In this paper, we present a new boosting algorithm, “WeightBoost”, which tries to solve these two problems by introducing an input-dependent regularization factor to the combination weight. Similarly to AdaBoost, we derive a learning procedure for WeightBoost, which is guaranteed to minimize training errors. Empirical studies on eight different UCI data sets and one text categorization data set show that WeightBoost almost always achieves a considerably better classification accuracy than AdaBoost. Furthermore, experiments on data with artificially controlled noise indicate that the WeightBoost is more robust to noise than AdaBoost.

1. Introduction

As a generally effective algorithm to create a “strong” classifier out of a weak classifier, boosting has gained popularity recently. Boosting works by repeatedly running the weak classifier on various training examples sampled from the original training pool, and combining the base classifiers produced by the weak learner into a single composite classifier. AdaBoost has been theoretically proved and empirically shown to be an effective method to improve the classification accuracy. Through the particular weight updating procedure,

AdaBoost is able to focus on those data points that have been misclassified in previous training iterations and therefore minimizes the training errors.

Since AdaBoost is a greedy algorithm and intentionally focuses on the minimization of training errors, there have been many studies on the issues of overfitting for AdaBoost (Quinlan, 1996; Grove & Schuurmans, 1998; Ratsch et al., 1998). The general conclusion from early studies appears to be that in practice AdaBoost seldom overfits the training data; namely, even though the AdaBoost algorithm greedily minimizes the training errors via gradient descent, the testing error usually goes down accordingly. Recent studies have implied that this phenomena might be related to the fact that the greedy search procedure used in AdaBoost is able to implicitly maximize the classification margin (Onoda et al., 1998; Friedman et al., 1998). However, other studies (Opitz & Macline, 1999; Jiang, 2000; Ratsch et al., 2000; Grove & Schuurmans, 1998; Dietterich, 2000) have shown that AdaBoost might have the problem of overfitting, particularly when the data are noisy.

In fact, noise in the data can be introduced by two factors, either the mislabelled data or the limitation of the hypothesis space of the base classifier. When noise level is high, there could be some data patterns that are difficult for the classifiers to capture. Therefore, the boosting algorithm is forced to focus on those noisy data patterns and thereby distort the optimal decision boundary. As a result, the decision boundary will only be suitable for those difficult data patterns and not necessarily general enough for other data. The overfitting problem can also be analyzed from the viewpoint of generalized error bound (Ratsch et al., 2000). As discussed in (Ratsch et al., 2000), the margin maximized by AdaBoost is actually a “hard margin”, namely the smallest margin of those noisy data patterns. As a consequence, the margin of the

other data points may decrease significantly when we maximize the “hard margin” and thus force the generalized error bound (Schapire, 1999) to increase.

In order to deal with the overfitting problems in Adaboost, several strategies have been proposed, such as smoothing (Schapire & Singer, 1998), Gentle Boost (J. Friedman & Tibshirani, 1998), BrownBoost (Freund, 2001), Weight Decay (Ratsch et al., 1998) and regularized AdaBoost (Ratsch et al., 2000). The main ideas of these methods can be summarized into two groups: one is changing the cost function such as introducing regularization factors into the cost function; the other is introducing a soft margin. The problem of overfitting for AdaBoost may be related to the exponential cost function, which makes the weights of the noisy data grow exponentially and leads to the overemphasis of those data patterns. The solution to this issue can be, either to introduce a different cost function, such as a logistic regression function in (Friedman et al., 1998), or to regularize the exponential cost function with a penalty term such as the weight decay method used in (Ratsch et al., 1998), or to introduce a different weighting function, such as BrownBoost (Freund, 2001). A more general solution is to replace the “hard margin” in AdaBoost with a “soft margin”. Similar to the strategy used in support vector machine (SVM) algorithm (Cortes & Vapnik, 1995), the boosting algorithm with a soft margin is able to allow a larger margin at the expenses of some misclassification errors. This idea leads to works such as the regularized boosting algorithms using both linear programming and quadratic programming (Ratsch et al., 1999).

However, there is another problem with AdaBoost that has been overlooked in previous studies. The Adaboost algorithm employs a linear combination strategy, that is, combining different base classifiers with a set of constants. As illustrated in previous studies, one advantage of the ensemble approach over a single model is that, an ensemble approach allows each sub-model to cover a different aspect of the data set. By combining them together, we are able to explain the whole data set thoroughly. Therefore, in order to take full strength of each submodel, a good combination strategy should be able to examine the input pattern and invoke the sub-models that are only appropriate for the input pattern. For example, in the Hierarchical Mixture Expert model (Jordan & Jacobs, 1994), the sub-models are organized into a tree structure, with leaf nodes acting as experts and internal nodes as “gates”. Those internal nodes examine the patterns of the input data and route them to the most appropriate leaf nodes for classification. Therefore,

for linear combination models, it seems more desirable to have those weighting factors dependent on the input patterns, namely given larger values if the associated submodel is appropriate for the input pattern and smaller value otherwise. Unfortunately, previous work on additive models for boosting almost all assumes the combination weights as fixed constants, and therefore is not able to take the input patterns into account.

In order to solve the two problems pointed out above, i.e. overfitting and constant combination weights for all input examples, we propose a new boosting algorithm that combines the base classifiers using a set of input-dependent weighting factors. This new approach is able to alleviate the second problem because by those input-dependent weight factors, we are able to force each submodel to focus on what it is good at. Meanwhile, we can show that those input-dependent factors can also alleviate the overfitting problem substantially. The reason is summarized as follows: in the common practice of boosting, a set of “weak” classifiers are combined with fixed constants. Therefore, for noisy data patterns, the error will accumulate through the sum and the weights of distribution will grow exponentially. In our work, we intentionally set the weighting factors of “weak classifiers” to be inverse to the previously accumulated weights, therefore we are able to significantly discount the weights of noisy data and alleviate the problem of overfitting.

The rest of the paper is arranged as follows: in Section 2 we discuss the related work on other boosting algorithms. The full description of our algorithm is presented in Section 3. The empirical study of our new algorithm versus the AdaBoost algorithm is described in Section 4. Finally, we draw conclusions and discuss future work.

2. Related Work

Since the AdaBoost algorithm is a greedy algorithm and intentionally focuses on minimizing the training errors, there have been many studies on the issue of overfitting for AdaBoost algorithm. However, most of the modification algorithms are unsuccessful either due to the high computational cost or lack of strong empirical results of improvement. One of the most successful algorithms is the Weight Decay method.

The basic idea of Weight Decay method can be described as follows: in analogy to weight decay in neural network, Ratsch et al. define $\zeta_i^t = (\sum_{t=1}^t \alpha_t h_t(x_i))^2$, where the inner sum ζ_i^t is the cumulative weight of the pattern in the previous iterations. Similar to the Support Vector Machines (Vapnik, 1995), they add ζ_i^t into

the cost function as the “slack variables”. The new cost function becomes:

$$\epsilon^t = \frac{1}{N} \left(\sum_{i=1}^N e^{\text{sign}(-H(x_i)y_i) - C\zeta_i^t} \right),$$

where C is a constant. Using this error function, we can control the tradeoff between the weights of training examples, that is, it will not change much for easy classifiable data points, but will change a lot for difficult patterns. Weight Decay method has proved to achieve some improvement over the AdaBoost algorithm.

3. Description of Algorithm

3.1. Brief Review of AdaBoost Algorithm

In order to introduce our new boosting algorithm, we will first visit the proof of AdaBoost briefly, which has direct impact on the derivation of the new algorithm. The particular derivation that we shown basically follows the paper by Friedman et al (Friedman et al., 1998).

In Adaboost, we construct a new classifier $H(x)$ by the linear combination of the base classifier $h(x)$, i.e.

$$H(x) = \sum_{t=1}^T \alpha_t h_t(x) = H_{T-1}(x) + \alpha_T h_T(x) \quad (1)$$

where α_t is the linear combination coefficients for the t_{th} basic classifier $h_t(x)$, and $H_{T-1}(x)$ is defined as $\sum_{t=1}^{T-1} \alpha_t h_t(x)$.

In order to obtain the optimal base classifiers $\{h_T(x)\}$ and linear combination coefficients $\{\alpha_T\}$, we need to minimize the training error. For binary classification problems, assume that the value of class label takes either 1 or -1, and the training error for the classifier $H(x)$ can be written as $err = \sum_{i=1}^N \text{sign}(-H(x_i)y_i)/N$. For the simplicity of computation, people usually use the exponential cost function as the objective function, namely $\sum_{i=1}^N e^{-H(x_i)y_i}/N$. Apparently, the exponential cost function upper bounds the training error err .

To minimize the exponential cost function, we use the inductive form for $H(x)$ in *eq1* and rewrite the upper bound function for the training error as:

$$\begin{aligned} err &\leq \frac{1}{N} \sum_{i=1}^N e^{-H_T(x_i)y_i} \\ &= \frac{1}{N} \sum_{i=1}^N \{e^{-H_{T-1}(x_i)y_i} e^{\alpha_T} I(h_T(x_i), y_i) \\ &\quad + e^{-H_{T-1}(x_i)y_i} e^{-\alpha_T} I(-h_T(x_i), y_i)\}, \end{aligned}$$

where function I is defined as:

$$I(x_1, x_2) = \begin{cases} 1 & \text{if } x_1 = x_2 \\ 0 & \text{if } x_1 \neq x_2 \end{cases}.$$

By setting the derivative of the equation above with respect to α_T to be zero, we have the expression as follows:

$$\alpha_T = \frac{1}{2} \ln \left(\frac{\sum_{i=1}^N e^{-H_{T-1}(x_i)y_i} I(h_T(x_i), y_i)}{\sum_{i=1}^N e^{-H_{T-1}(x_i)y_i} I(-h_T(x_i), y_i)} \right)$$

Meanwhile, to minimize *eq1*, the classifier $h_T(x)$ needs to be optimized with respect to the following data distribution:

$$W_i^T = \frac{e^{-H_{T-1}(x_i)y_i}}{\sum_{j=1}^N e^{-H_{T-1}(x_j)y_j}}. \quad (2)$$

With the expression of data distribution W_i^T , the linear combination coefficient α_T can be rewritten as

$$\alpha_T = \frac{1}{2} \ln \left(\frac{\sum_{i=1}^N W_i^T I(h_T(x_i), y_i)}{\sum_{i=1}^N W_i^T I(-h_T(x_i), y_i)} \right) = \frac{1}{2} \ln \left(\frac{1 - \epsilon^T}{\epsilon^T} \right) \quad (3)$$

where ϵ^T stands for the weighted error rate under the weight distribution W^t for the base classifier $h_T(x)$ in iteration T .

In summary, the minimization of training error is accomplished through this stepwise optimization. In each iteration, we train a new base classifier according to the data distribution in *eq2*, and combine it with previous classifiers using the weight described in *eq3*.

3.2. New Boosting Algorithm: WeightBoost

The overfitting problem of AdaBoost can be implied by the weight updating function in *eq2*. For each iteration, the weight for the i th data point is proportional to the function $e^{-H_{T-1}(x_i)y_i}$. As we can see, $H_{T-1}(x)$ is a linear combination of all the base classifiers obtained from iteration 1 to iteration $T-1$. If there are some noisy data patterns that are difficult to be classified correctly by the base classifier, the value of $-H_{T-1}(x_i)y_i$ for those data points will accumulate linearly and thus the corresponding weights can grow exponentially. Therefore, the particular sampling procedure within the AdaBoost algorithm will overemphasize the noisy training data points and may lead to a complex decision boundary that is not well generalized. In this subsection, we present a new boosting algorithm, which combine base classifiers using input-dependent weighting factors instead of fixed coefficients. We will first discuss a special form of this idea since it is a more intuitive way to solve overfitting problems and then develop a more general form.

Since the overfitting problem is caused by the accumulation of errors within the function $H_{T-1}(x)$, one way to avoid this is to modify the expression form for $H_{T-1}(x)$. Instead of multiplying each base classifier with a simple constant α_t , we can make the combination coefficients to be input dependent, i.e.

$$H_T(x) = \sum_{t=1}^T \alpha_t e^{-|\beta H_{t-1}(x)|} h_t(x). \quad (4)$$

Compared with *eq1*, the above expression replaces the weighting constant α_t with $\alpha_t e^{-|\beta H_{t-1}(x)|}$. More interestingly, it can be shown easily that, under the condition that the weighting coefficients α_t is bounded by some fixed constant α_{max} , the value of $H_T(x)$ in *eq 4* will increase at most by the logarithmic degree with respect to the number of iteration T . More specifically, we have $H_T(x)$ bounded by the following expression:

$$H_T(x) \leq \frac{1}{\beta} \ln(\beta \alpha_{max} e^{\beta \alpha_{max}} (T-1) + e^{\beta H_1(x)})$$

(detailed proof can be found in our later paper). Therefore, the weight of each data pattern will grow at most polynomial with the number of iterations and as a result, the problem of overemphasizing noisy data patterns in AdaBoost can be alleviated substantially.

As pointed out before, another problem with AdaBoost algorithm is that, by combining the base classifiers with fixed constants, the opinion of each classifier will always be weighted with the same number no matter what input patterns are. According to AdaBoost, each base classifier $h_t(x)$ is trained intentionally on the data patterns that are either misclassified or weakly classified by previous classifiers $H_{t-1}(x)$. Therefore, every base classifier $h_t(x)$ should be appropriate only for a subset of input patterns. However, in the prediction phase, the opinion of the base classifier $h_t(x)$ will always be weighted by the same number α_t no matter what the test examples are. On the contrary, in the new form of $H_T(x)$ in *eq 4*, the introduction of the “instance dependent factor” $e^{-|\beta H_{t-1}(x)|}$ in the combination coefficients offers us a way to make tradeoff between the opinion of the base classifier $h_t(x)$ and that of the previously built meta-classifier $H_{t-1}(x)$. The value of $H_{t-1}(x)$ indicates its confidence on classifying the instance x , so the factor $e^{-|\beta H_{t-1}(x)|}$ can be interpreted as to consider the opinion of $h_t(x)$ seriously only when previous classifiers $H_{t-1}(x)$ is not confident about its decision. In this way, the introduction of “input-dependent factor” makes the base classifier $h_t(x)$ to be consistent between the training phase and the prediction phase, namely $h_t(x)$ is used for prediction on the particular type of input patterns that it has been trained on.

The factor β within the “input-dependent factor” $e^{-|\beta H_{t-1}(x)|}$ is used to control to what extent the opinion of $H_{t-1}(x)$ should be considered seriously. When β is set to be zero, the combination coefficient goes back to the simple form α_t and the combination form (in *eq4*) simply becomes *eq1*. In this sense, AdaBoost can be treated as a special case of *eq4*. When β goes to infinity, the effect of the base classifier $h_t(x)$ is almost ignored and only the opinion of $H_{T-1}(x)$ is dominant.

Next, we need to obtain a learning procedure that is able to minimize the exponential cost function with the new combination form for $H_T(x)$. Following similar procedures for deriving AdaBoost algorithm as we did in previous subsection, we can get:

$$\begin{aligned} H_T(x) &= \sum_{i=1}^{T-1} \alpha_i e^{-|\beta H_{i-1}(x)|} h_i(x) + \alpha_T e^{-|\beta H_{T-1}(x)|} h_T(x) \\ &= H_{T-1}(x) + \alpha_T e^{-|\beta H_{T-1}(x)|} h_T(x) \end{aligned}$$

With this new inductive form for $H_T(x)$, we will have the upper bound function for the training error as

$$\begin{aligned} err &\leq \frac{1}{N} \sum_{i=1}^N e^{-H_T(x_i) y_i} \\ &= \frac{1}{N} \sum_{i=1}^N e^{-H_{T-1}(x_i) y_i} e^{-\alpha_T e^{-|\beta H_{T-1}(x_i)|} h_T(x_i) y_i} \\ &= \frac{1}{N} \sum_{i=1}^N \{ e^{-H_{T-1}(x_i) y_i} e^{-\alpha_T e^{-|\beta H_{T-1}(x_i)|}} I(h_T(x_i), y_i) \\ &\quad + e^{-H_{T-1}(x_i) y_i} e^{\alpha_T e^{-|\beta H_{T-1}(x_i)|}} I(-h_T(x_i), y_i) \}. \end{aligned} \quad (5)$$

Since $e^{-|\beta H_{T-1}(x)|}$ is between 0 and 1, we can have $\exp(\alpha_T e^{-|\beta H_{T-1}(x)|})$ up bounded by the following expression:

$$\exp(\alpha_T e^{-|\beta H_{T-1}(x)|}) \leq 1 + (e^{\alpha_T} - 1) e^{-|\beta H_{T-1}(x)|}.$$

Similarly,

$$\exp(-\alpha_T e^{-|\beta H_{T-1}(x)|}) \leq 1 + (e^{-\alpha_T} - 1) e^{-|\beta H_{T-1}(x)|}.$$

Then, *eq5* can be rewritten as:

$$\begin{aligned} err &\leq \frac{1}{N} \sum_{i=1}^N \{ e^{-H_{T-1}(x_i) y_i} e^{-\alpha_T e^{-|\beta H_{T-1}(x_i)|}} I(h_T(x_i), y_i) \\ &\quad + e^{-H_{T-1}(x_i) y_i} e^{\alpha_T e^{-|\beta H_{T-1}(x_i)|}} I(-h_T(x_i), y_i) \} \\ &\leq \frac{1}{N} \sum_{i=1}^N \{ e^{-H_{T-1}(x_i) y_i} e^{-\alpha_T} e^{-|\beta H_{T-1}(x_i)|} I(h_T(x_i), y_i) \\ &\quad + e^{-H_{T-1}(x_i) y_i} e^{\alpha_T} e^{-|\beta H_{T-1}(x_i)|} I(-h_T(x_i), y_i) \} \\ &\quad + \frac{1}{N} \sum_{i=1}^N e^{-H_{T-1}(x_i) y_i} (1 - e^{-|\beta H_{T-1}(x_i)|}). \end{aligned}$$

(6)

Similar to the derivation stated in previous subsection, we set the derivative of $eq6$ with respect to α_T to be zero, which leads to the expression form for α_T as:

$$\alpha_T = \frac{1}{2} \ln \left(\frac{\sum_{i=1}^N e^{-H_{T-1}(x_i)y_i} e^{-|\beta H_{T-1}(x_i)|} I(h_T(x_i), y_i)}{\sum_{i=1}^N e^{-H_{T-1}(x_i)y_i} e^{-|\beta H_{T-1}(x_i)|} I(-h_T(x_i), y_i)} \right)$$

By defining the updating functions W_i^T as

$$W_i^T = \frac{e^{-H_{T-1}(x_i)y_i - |\beta H_{T-1}(x_i)|}}{\sum_{j=1}^N e^{-H_{T-1}(x_j)y_j - |\beta H_{T-1}(x_j)|}}, \quad (7)$$

we will get the exact same expression for α_T as in $eq3$, i.e.

$$\alpha_T = \frac{1}{2} \ln \left(\frac{\sum_{i=1}^N W_i^T I(h_T(x_i), y_i)}{\sum_{i=1}^N W_i^T I(-h_T(x_i), y_i)} \right) = \frac{1}{2} \ln \left(\frac{1 - \epsilon^T}{\epsilon^T} \right), \quad (8)$$

where ϵ^T stands for the weighted error for the classifier $h_T(x)$ in the T_{th} training iteration.

In summary, the procedures for WeightBoost algorithm is similar to that of AdaBoost. For each training iteration, we update the weight of each data point using $eq7$, then train a new base classifier with the weighted training data and finally combine the new base classifier with the previous ones with the weight expressed in $eq8$.

Compared with AdaBoost algorithm, the only difference is the weight updating function, which is defined in $eq7$. In the original AdaBoost algorithm, the weight for instance x_i is proportional to $e^{(-H_{T-1}(x_i)y_i)}$, and therefore only instances that are misclassified by the previously obtained classifier $H_{T-1}(x_i)$ will be emphasized in the next round of training. As indicated in $eq7$, in the new boosting algorithm, the weight for instance x_i is proportional to $e^{-H_{T-1}(x_i)y_i - |\beta H_{T-1}(x_i)|}$. With this additional term $|\beta H_{T-1}(x_i)|$ within the exponential function, not only the data points misclassified by classifier $H_{T-1}(x)$, but also the data points close to the decision boundary of classifier H_{T-1} will be emphasized in the next training round. Therefore, the modified weight updating function in $eq7$ is able to achieve the tradeoff between the goal of minimizing the training errors and the goal of maximizing the classification margin. This is similar to the concept of minimizing classification risk in Support Vector Machine (SVM) (Cortes & Vapnik, 1995; Vapnik, 1995) and regularized boosting algorithm (Ratsch et al., 2000). Furthermore, by adjusting the constant β , we are able to control the balance between two different goals.

3.3. More General Solution

In $eq4$, we restrict ourselves to the specific combination form by using term $e^{-|H_{T-1}(x_i)|}$ as the "input-dependent regularizer". In fact, the derivation of the learning algorithm in previous section is applicable to any regularization function as long as it is bounded between 0 and some fixed non-negative constant. Let $f(x)$ stand for the chosen regularizer. Then $H_T(x)$ is written as:

$$H_T(x) = \sum_{t=1}^T \alpha_t f(x) h_t(x). \quad (9)$$

Assume that the value of function $f(x)$ is between 0 and f_{max} , by defining $\alpha'_t = \alpha f_{max}$ and $g(x) = f(x)/f_{max}$, we have $H_T(x)$ rewritten as:

$$H_T(x) = \sum_{t=1}^T \alpha'_t g(x) h_t(x). \quad (10)$$

Since the function $g(x)$ is bound between 0 and 1, which is same as $e^{-|\beta H_T(x)|}$, all the results derived in previous section will be correct for function $g(x)$. Thus, for regularization function $f(x)$, the updating function becomes

$$W_i^T = \frac{e^{-H_{T-1}(x_i)y_i} f(x_i)/f_{max}}{\sum_{j=1}^N e^{-H_{T-1}(x_j)y_j} f(x_j)/f_{max}} \quad (11)$$

and the weighting coefficient α_T is

$$\alpha_T = \frac{f_{max}}{2} \ln \left(\frac{1 - \epsilon^T}{\epsilon^T} \right). \quad (12)$$

One problem with simply using $e^{-|\beta H_{T-1}(x_j)|}$ as the "input-dependent regularizer" is that, the value of this function may become too small if the value of $|\beta H_{T-1}(x_j)|$ is large. This may discount the opinion of the base classifier $h_T(x)$ too much. One solution would be replacing the function $e^{-|\beta H_{T-1}(x_j)|}$ with $e^{-|\beta H_{T-1}(x_j)|}/C_T$. In our experiments, we set C_T as the normalization factor, which is $\sum_i e^{-|\beta H_{T-1}(x_j)|}/0.1N$.

3.4. Comparison to the Weight Decay Method

The weight updating function in $eq7$ is somewhat similar to the one obtained via the weight decay method. However, there are two significant differences between these two methods:

1) Instead of modifying the objective function, we modify the combination form by introducing an input-dependent regularizer for each weighting coefficient.

Therefore, unlike the weight decay method, where the regularization is achieved by introducing a penalty term in the objective function, the regularization of WeightBoost is realized by the input-dependent regularizer.

2) Similar to other boosting algorithms, the weight decay method combines different base classifiers with a set of input independent weights. In WeightBoost algorithm, the weighting coefficients depend on the input patterns, which has the advantage of being able to direct testing instances to the appropriate base classifiers according to their input patterns.

4. Empirical Validation

As discussed before, there are two problems that our algorithm tries to solve: overfitting and constant weight combination. In previous section, we have discussed how WeightBoost can tackle these two problems theoretically. Next we will examine empirically whether our algorithm performs better than others.

Table 1. Description of Data sets

Collection Name	Instances Num	Attributes Num
Ionosphere	351	341
German	1000	20
Pima Indians Diabetes	768	8
Breast Cancer	268	9
wdbc	198	30
wdbc	569	30
Contraceptive	1473	10
Spambase	4601	58

4.1. Standard Evaluation

In this subsection, we examine the general effectiveness of WeightBoost algorithm by comparing it with AdaBoost and the Weight Decay method. Eight data sets from the UCI repository (Blake & Merz, 1998) and a benchmark of text categorization evaluation – the ApteMod version of Reuters-21578 corpus are used as testbeds. All of UCI data sets are binary classification problems and the detailed information is listed in Table 1. Reuters-21578 corpus consists of a training set of 7,769 documents and a test set of 3,019 documents with 90 categories each of which has at least one occurrence in both sets. The number of categories per document is 1.3 on average. In order to deal with the multiple classes, we decompose the multiple-class classification into a set of binary classification problems using the standard *one-against-all* approach.

The base classifier we used in our experiment is decision tree C4.5(Quinlan, 1993), which is commonly used

for evaluating boosting algorithm in previous studies(Schapire, 1999; Quinlan, 1996). For all UCI data sets, we set the maximum training iteration to be 100 as Freund did in their experiments(Freund & Schapire, 1996) and reported the results via averaged 10-fold cross validation. The parameter β in WeightBoost algorithm is set to be 0.5 for all the data sets.

Table 2. Classification errors for the WeightBoost, AdaBoost and Weight Decay

Collection Name	C4.5	AdaBoost	Weight Decay	ϵ -Boost	Weight Boost
Ionosphere	9.1%	6.8%	5.7%	6.8%	6.2%
German	26.9%	26.3%	26.7%	24.7%	24.7%
Pima-Indians-Diabetes	25.2%	24.7%	25.1%	23.9%	22.6%
Breast Cancer	5.4%	4.5%	3.7%	3.2%	3.3%
wdbc	28.8%	26.3%	21.1%	21.1%	19.9%
wdbc	6.1%	3.5%	3.0%	3.7%	3.0%
Contraceptive	31.5%	31%	29.8%	30.4%	27.6%
Spambase	7.2%	5.8%	4.9%	4.5%	4.2%

The error rate of the new boosting algorithm, AdaBoost and Weight Decay method on the eight UCI collections are listed in Table 2. From the table, we can see: first, WeightBoost is able to achieve lower classification errors than AdaBoost on all of the eight data sets and than Weight Decay on six out of eight. Secondly, for data sets such as “German”, “Pima-indian-diabetes” and “Contraceptive”, the classification errors of AdaBoost and Weight Decay are almost identical to the baseline results while our new boosting algorithm is able to lower the error rate significantly. To further see if the improvements come from the input dependent regularizer or simply due to the regularization on the value of $H(x)$, we compare the WeightBoost to the ϵ -Boost, which is introduced by Friedman (Friedman et al., 1998). In this method, each weak classifier is given with a small weights and therefore the value of the combined classifier will usually not very large. The fourth column of Table 1 shows the results of ϵ -Boost. Again, the proposed boosting algorithm outperforms the ϵ -Boost in seven out of eight data sets. Based on the above observations, the introduction of input-dependent regularizer does help improve the effectiveness of the boosting algorithm.

To further demonstrate the effectiveness of WeightBoost, we test our method and AdaBoost on Reuters-21578 corpus, a benchmark in recent text categorization evaluations. We pre-processed the documents, including down-casing, tokenization, removal of punctuation and stop words, stemming, and the supervised

feature selection using χ^2 -max criterion, i.e. the maximum of χ^2 over the 90 categories by cross-validation and the resulting vocabulary is 2,000. Document vectors based on these feature sets were computed using the SMART *lbc* version of TF-IDF term weighting. This gives term t in document d a weight of:

$$w_d(t) = (1 + \log_2 n(t, d)) \times \log_2(|\mathcal{D}|/n(t)), \quad (13)$$

where $n(t)$ is the number of documents that contain t . For the evaluation metric, we used a common effectiveness measure, F_1 , defined to be: $F_1 = \frac{2rp}{r+p}$, where p refers to the precision and r represents recall. We tune the number of training iteration and reported the best results (the corresponding iteration is 25 and 10 respectively for WeightBoost and AdaBoost).

Table 4.1 shows the results of C4.5, AdaBoost and WeightBoost on the ten most common categories of the Reuters corpus in terms of F_1 measurement and improvement over the baseline. It can be seen from the results that WeightBoost outperforms AdaBoost in seven out of the ten most common categories. For some categories, such as “crude” and “wheat”, WeightBoost got impressive improvement over the baseline even though AdaBoost tends to overfit for those cases.

Table 3. Classification Results of AdaBoost and WeightBoost on Reuters21578 corpus

Category	C4.5	AdaBoost		WeightBoost	
	F1	F1	Impro	F1	Impro
Trade	.5897	.6634	12.5%	.6949	17.8%
Grain	.9030	.8814	-2.4%	.8966	-0.7%
Crude	.8223	.8204	-0.2%	.8587	4.4%
Corn	.8740	.8926	2.1%	.9091	4.0%
Ship	.7283	.7853	7.8%	.7273	-0.1%
Wheat	.8800	.8767	-0.4%	.9128	3.7%
Acq	.8915	.9344	4.8%	.9243	3.7%
Interest	.6224	.6747	8.4%	.6352	2.1%
Money-fx	.6477	.6805	5.1%	.7041	8.7%
Earn	.9564	.9698	1.4%	.9707	1.5%

4.2. Robustness to Noise

In this subsection, we study the robustness of our new boosting algorithm by introducing noise to the data. Generally speaking, there are many kinds of noise in the real application. For our experiments, we choose the labelling noise as the main focus since it can be controlled easily. We randomly select part of training examples and change their label to the opposite ones while leaving the other examples the same as before. In this way, we got UCI data sets with 10%, 20% and 30% noise and did the same experiments as the one in previous subsection.

Fig 1 show the comparison results of AdaBoost and WeightBoost on the eight UCI data sets with 10% noise. From the results we can see that AdaBoost algorithm did suffer from overfitting on some of the data sets, such as “German”, “Breast-cancer” and “Contraceptive”, while WeightBoost consistently achieved improvement on all of the eight data sets. In addition, our new algorithm demonstrates great robustness to noise. For example, in “wdpc” data set, WeightBoost got almost the same results for data with 10% noise (3.5% in Table 4.1) compared with the results without noise (3.1% in Table 2). Table 4.1 lists detailed results with different percentage of noise and we can observe similar patterns as discussed above.

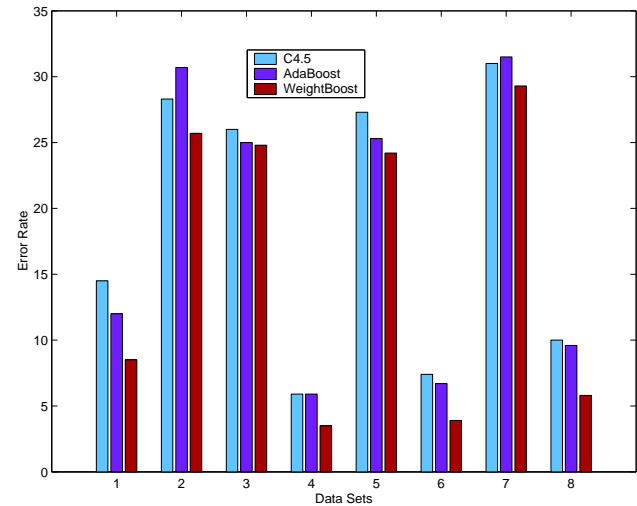


Figure 1. Classification Errors with 10% Noise

5. Conclusion and Future Work

In this paper, we presented a new boosting algorithm with a different combination form from most previous works on boosting. By introducing an “input-dependent regularizer”, we managed to route the testing examples to the appropriate base classifiers and at the same time solve overfitting problems. Furthermore, with the parameter β , we are able to balance the goal of minimizing training errors and the goal of maximizing margin. The new algorithm is able to outperform the AdaBoost algorithm on almost eight different UCI data sets and a text categorization data set. Furthermore, we demonstrate that the new algorithm is much more robust to the label noise than AdaBoost.

Future work involves in doing experiments with different “input-dependent regularizers”. Since the exponential function may drop too rapidly, “slower” functions such as the inverse of polynomials could be better

Table 4. Classification Errors of AdaBoost and WeightBoost on UCI data sets with Introducing Noise (WB = Weight-Boost)

	10% Noise			20% Noise			30% Noise		
	C4.5	AdaBoost	WB	C4.5	AdaBoost	WB	C4.5	AdaBoost	WB
Ionosphere	14.50%	12.00%	8.50%	17.70%	16.80%	11.10%	26.50%	24.20%	19.90%
German	28.30%	30.70%	25.70%	35.10%	32.90%	30.50%	42.80%	40.20%	35.80%
Pima	26.00%	25.00%	24.80%	27.80%	26.00%	24.90%	31.30%	30.00%	26.20%
Breast-cancer	5.90%	5.90%	3.50%	5.90%	5.90%	4.10%	10.30%	10.80%	4.70%
wdbc	27.30%	25.30%	24.20%	35.40%	38.00%	27.30%	31.30%	38.60%	34.10%
wdbc	7.40%	6.70%	3.90%	7.00%	7.00%	5.30%	14.20%	14.20%	7.70%
Contraceptive	31.00%	31.50%	29.30%	33.90%	33.90%	30.30%	36.20%	39.70%	34.50%
Spambase	10.00%	9.60%	5.80%	11.10%	11.10%	7.00%	13.30%	13.30%	8.90%

candidates. Moreover, more investigation is needed to discover how to automatically determine the value of β , which plays an important role in balancing the goal of minimizing the training error and that of maximizing margin.

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