Exercise: Perceptron Classification

Data

$$\mathcal{D} = \left\{ \begin{pmatrix} x_1^{(i)}, x_2^{(i)}, y^{(i)} \end{pmatrix} \right\}_{i=1}^{N} \\
= \left\{ (2, 2, 1), (2, 0, 1), (2, -2, 1), (-2, -3, -1), (-2, 0, -1), (-2, 3, -1) \right\}$$

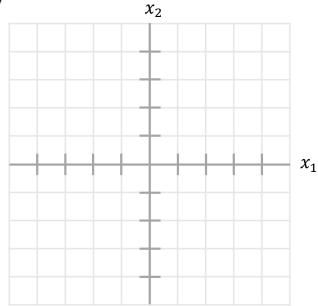
Model

$$\hat{y} = h(\mathbf{x}) = sign(\mathbf{w}^T \mathbf{x} + b)$$

with parameters

$$w_1 = -1$$
, $w_2 = 2$, $b = 0$

- 1) Plot the data in \mathbb{R}^2 with two different shapes for y=1 and y=-1
- 2) Draw the decision boundary (all the points (x_1, x_2) where $\hat{y} = 0$)
- 3) Draw the vector w



- 4) How many mistakes (errors) were made with this model on this dataset?
- 5) What is the classification error rate for this model on this dataset?
- 6) What is the classification accuracy for this model on this dataset?
- 7) Fill in the confusion matrix below with the count of points in each category.

	$\hat{y} = 1$	$\hat{y} = -1$
y = 1	TP:	FN:
y = -1	FP:	TN:

TP: True positive

TN: True negative

FP: False positive FN: False negative