Warm-up as you log in

Write the pseudo code for breadth first search and depth first search
- Iterative version, not recursive
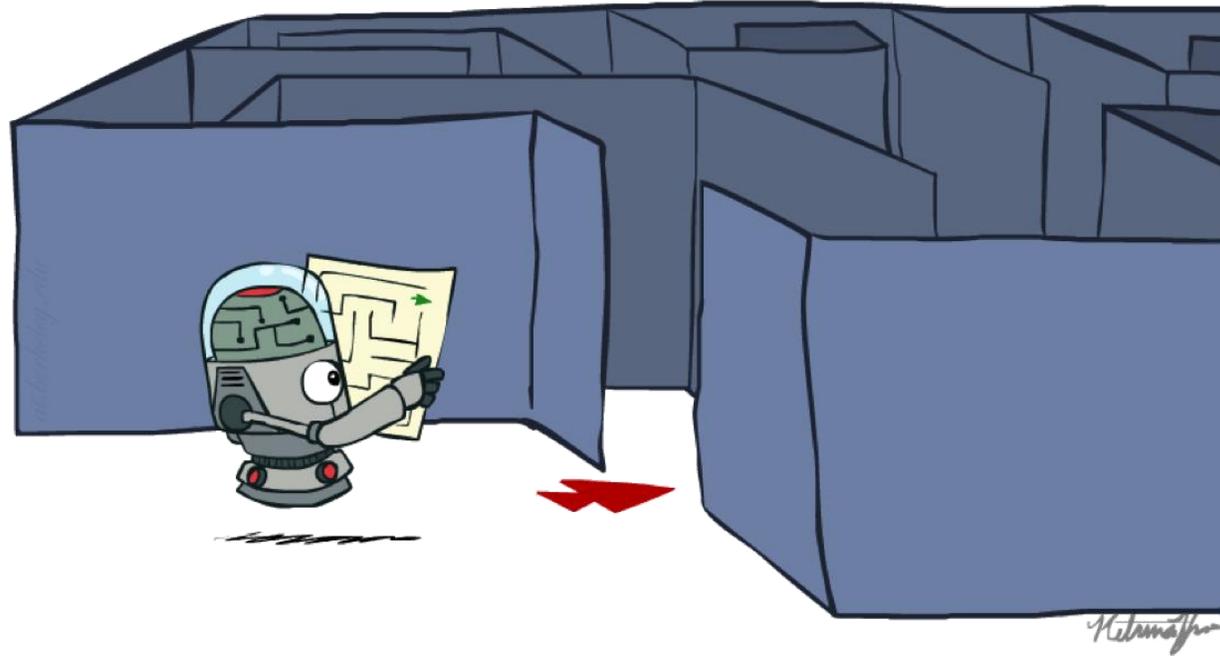
```
class TreeNode
      TreeNode[] children()
      boolean isGoal()


BFS(TreeNode start)…
DFS(TreeNode start)…
```

AI: Representation and Problem Solving

Agents and Search

Instructor: Pat Virtue

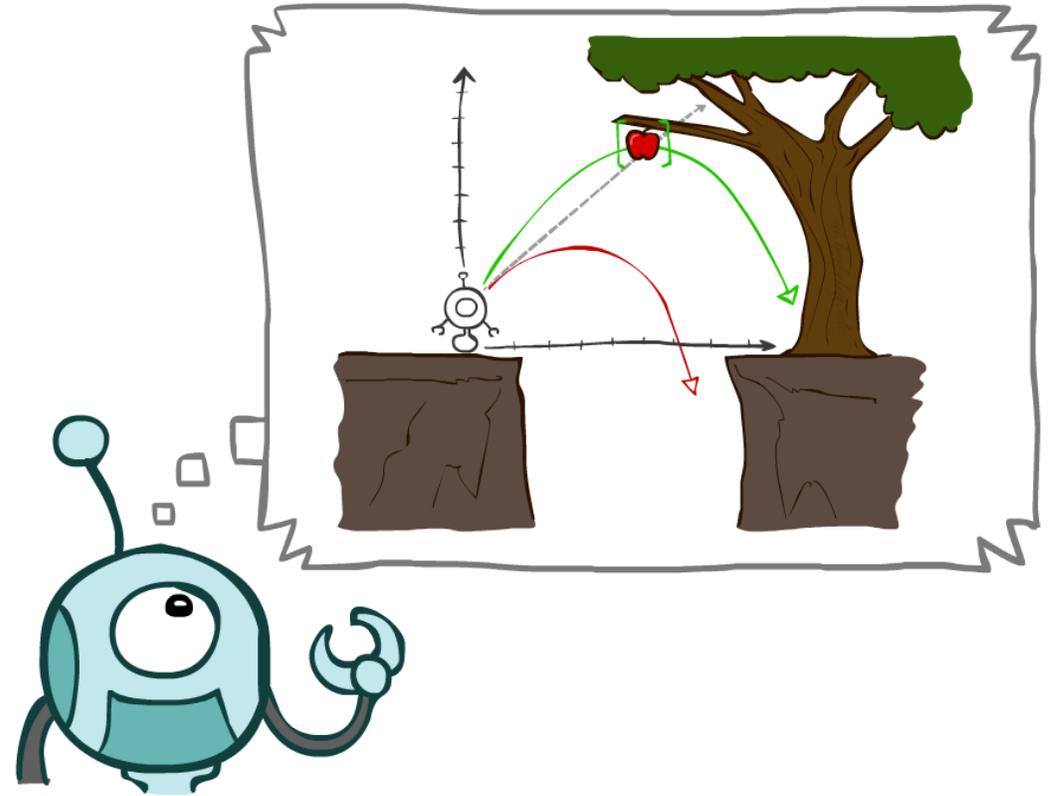Slide credits: CMU AI, http://ai.berkeley.edu

Outline

Agents and Environments

Search Problems
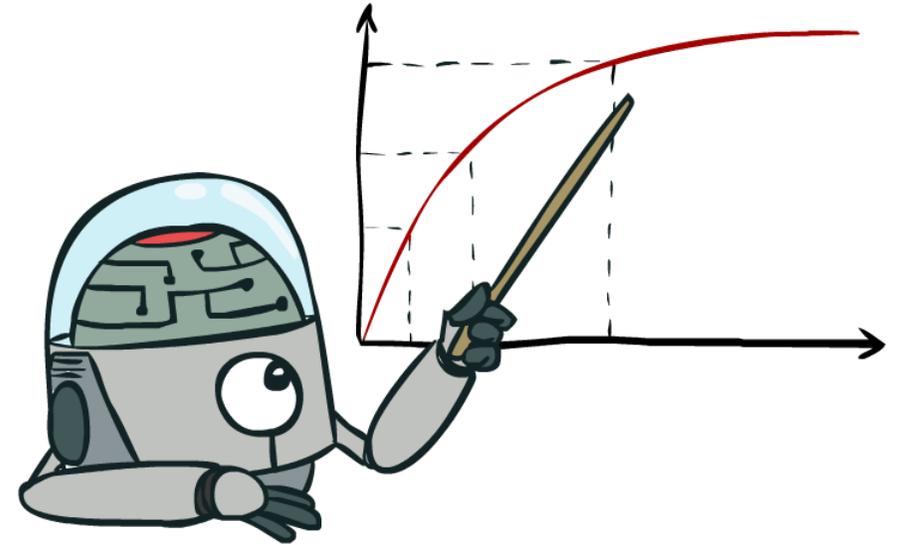
Uninformed Search Methods

- Depth-First Search
- Breadth-First Search
- Uniform-Cost Search

Rationality, contd.

What is rational depends on:

- Performance measure
- Agent's prior knowledge of environment
- Actions available to agent
- Percept sequence to date

Being rational means **maximizing your expected utility**

Rational Agents

Are rational agents *omniscient*?
- No – they are limited by the available percepts

Are rational agents *clairvoyant*?
- No – they may lack knowledge of the environment dynamics

Do rational agents *explore* and *learn*?
- Yes – in unknown environments these are essential

So rational agents are not necessarily successful, but they are *autonomous* (i.e., transcend initial program)

Task Environment - PEAS

Performance measure

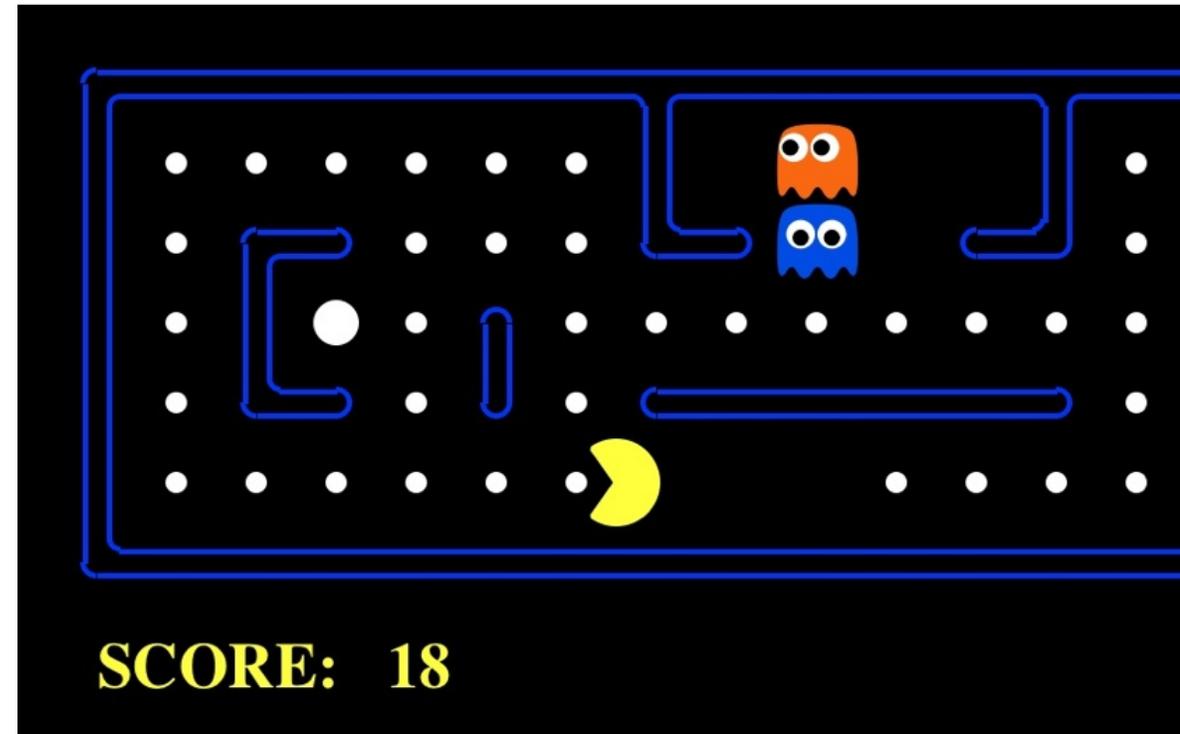- -1 per step; +10 food; +500 win; -500 die; +200 hit scared ghost

Environment

- Pacman dynamics (incl ghost behavior)

Actuators

- North, South, East, West, (Stop)

Sensors

- Entire state is visible

PEAS: Automated Taxi

Performance measure
- Income, happy customer, vehicle costs, fines, insurance premiums

Environment
- US streets, other drivers, customers

Actuators
- Steering, brake, gas, display/speaker

Sensors
- Camera, radar, accelerometer, engine sensors, microphone

Image: http://nypost.com/2014/06/21/how-google-might-put-taxi-drivers-out-of-business/

Environment Types

	Pacman	Taxi
Fully or partially observable		
Single agent or multi-agent		
Deterministic or stochastic		
Static or dynamic		
Discrete or continuous		

Reflex Agents

Reflex agents:

- Choose action based on current percept (and maybe memory)
- May have memory or a model of the world's current state
- Do not consider the future consequences of their actions
- Consider how the world IS

Can a reflex agent be rational?
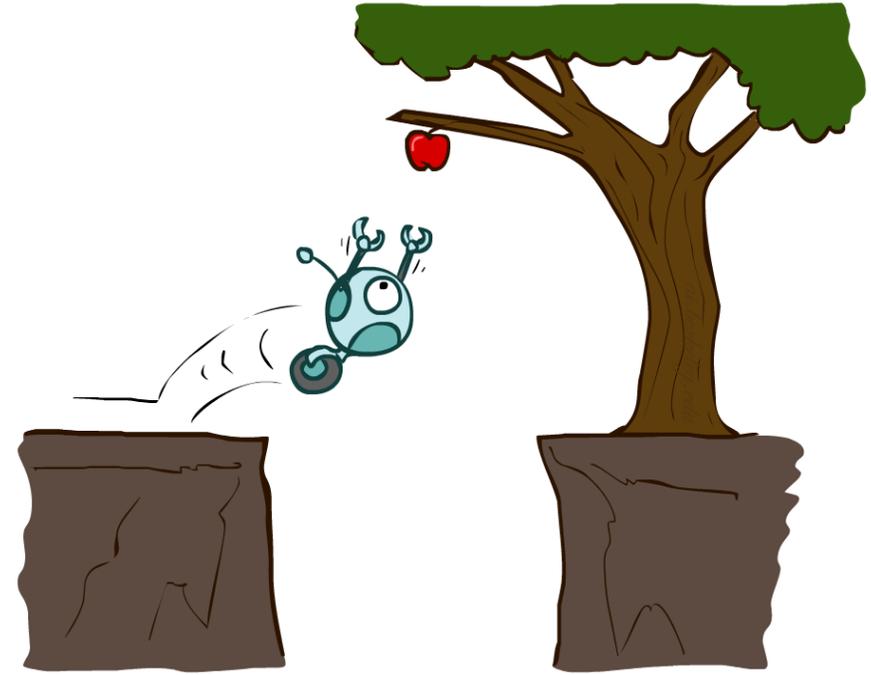
[Demo: reflex optimal (L2D1)]
[Demo: reflex optimal (L2D2)]

Agents that Plan Ahead

Planning agents:

- Decisions based on **_predicted consequences_** of actions
- Must have a **_transition model_**: how the world evolves in response to actions
- Must formulate a goal
- Consider how the world WOULD BE

Spectrum of deliberativeness:

- Generate complete, optimal plan offline, then execute
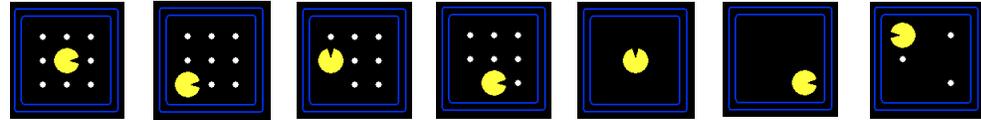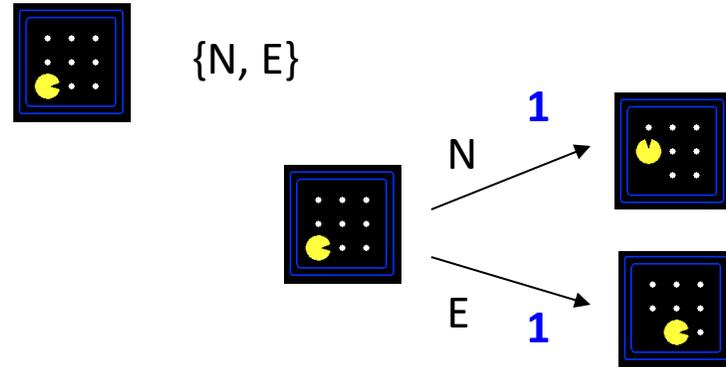- Generate a simple, greedy plan, start executing, replan when something goes wrong
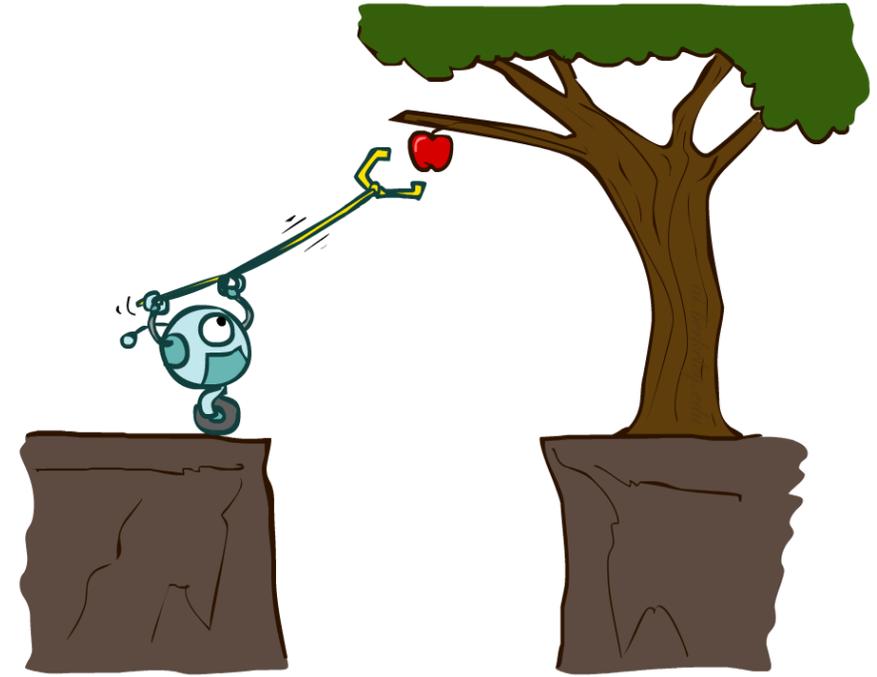
Search Problems

Search Problems

A search problem consists of:

- A state space

- For each state, a set
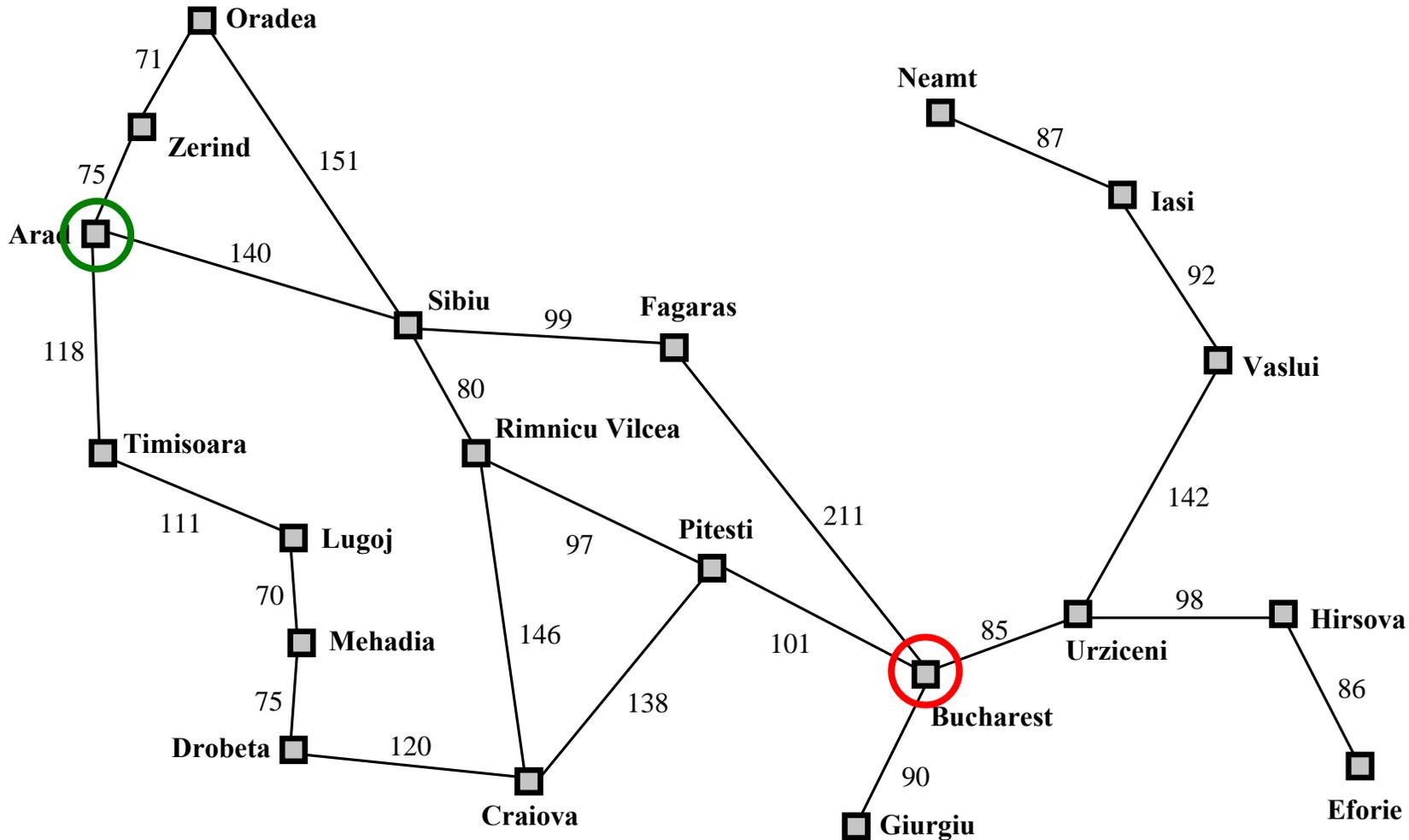 Actions(s) of allowable actions {N, E}

- A transition model Result(s,a)

- A step cost function c(s,a,s')

- A start state and a goal test

A solution is a sequence of actions (a plan) which transforms the start state to a goal state

Search Problems Are Models

Example: Travelling in Romania

State space:
- Cities

Actions:
- Go to adjacent city

Transition model
- Result(A, Go(B)) = B

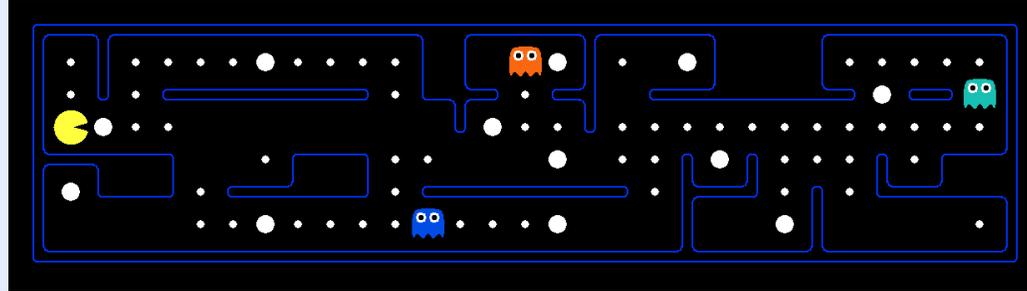Step cost
- Distance along road link

Start state:
- Arad

Goal test:
- Is state == Bucharest?

Solution?

What's in a State Space?

The real world state includes every last detail of the environment

A search state abstracts away details not needed to solve the problem

- Problem: Pathing
  - State representation: (x,y) location
  - Actions: NSEW
  - Transition model: update location
  - Goal test: is (x,y)=END

- Problem: Eat-All-Dots
  - State representation: {(x,y), dot booleans}
  - Actions: NSEW
  - Transition model: update location and possibly a dot boolean
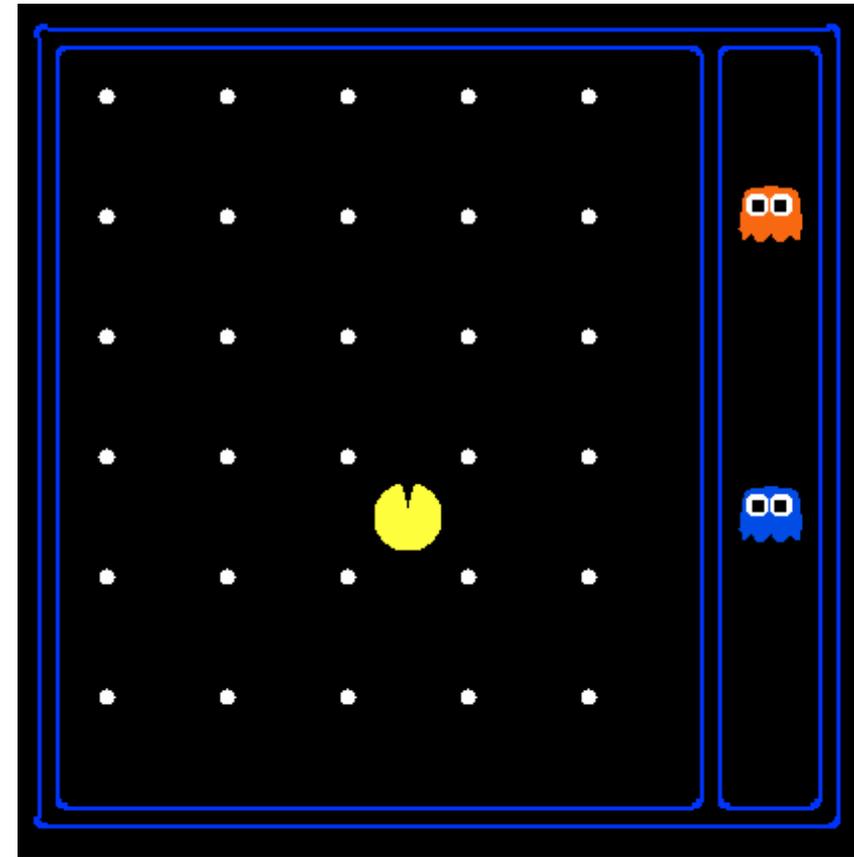 - Goal test: dots all false

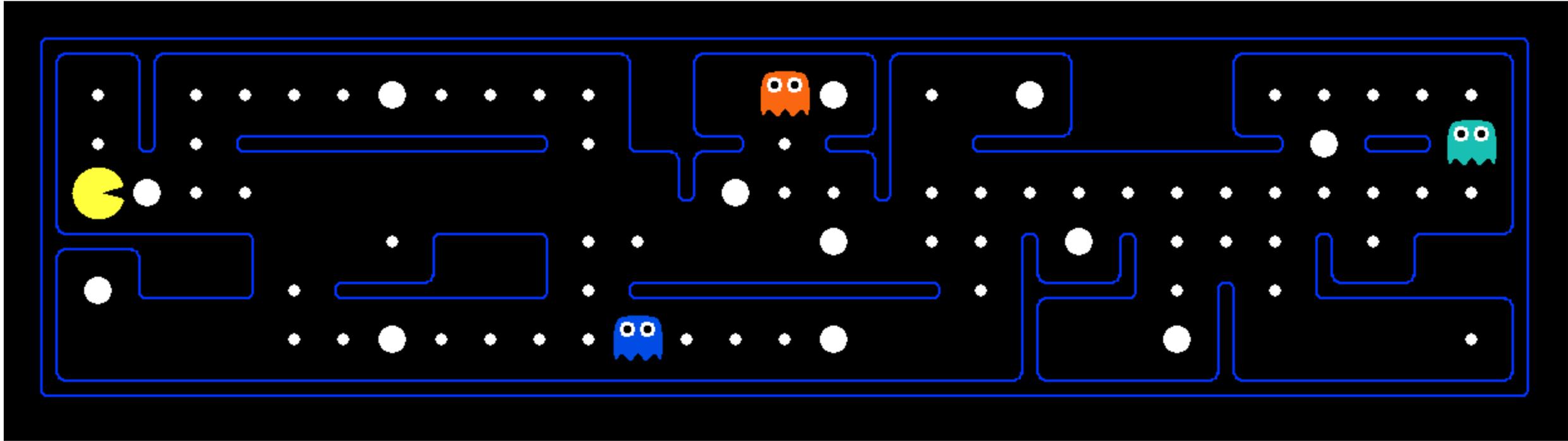# State Space Sizes?

World state:

- Agent positions: 120
- Food count: 30
- Ghost positions: 12
- Agent facing: NSEW

How many

- World states?
  $120 \times (2^{30}) \times (12^2) \times 4$
- States for pathing?
  120
- States for eat-all-dots?
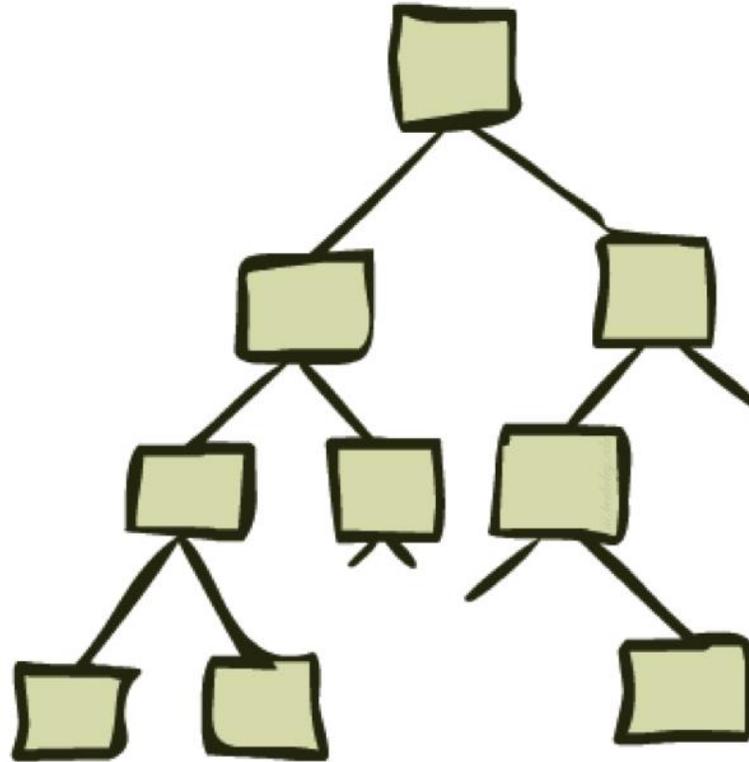 $120 \times (2^{30})$

Safe Passage

Problem: eat all dots while keeping the ghosts perma-scared

What does the state representation have to specify?

- (agent position, dot booleans, power pellet booleans, remaining scared time)
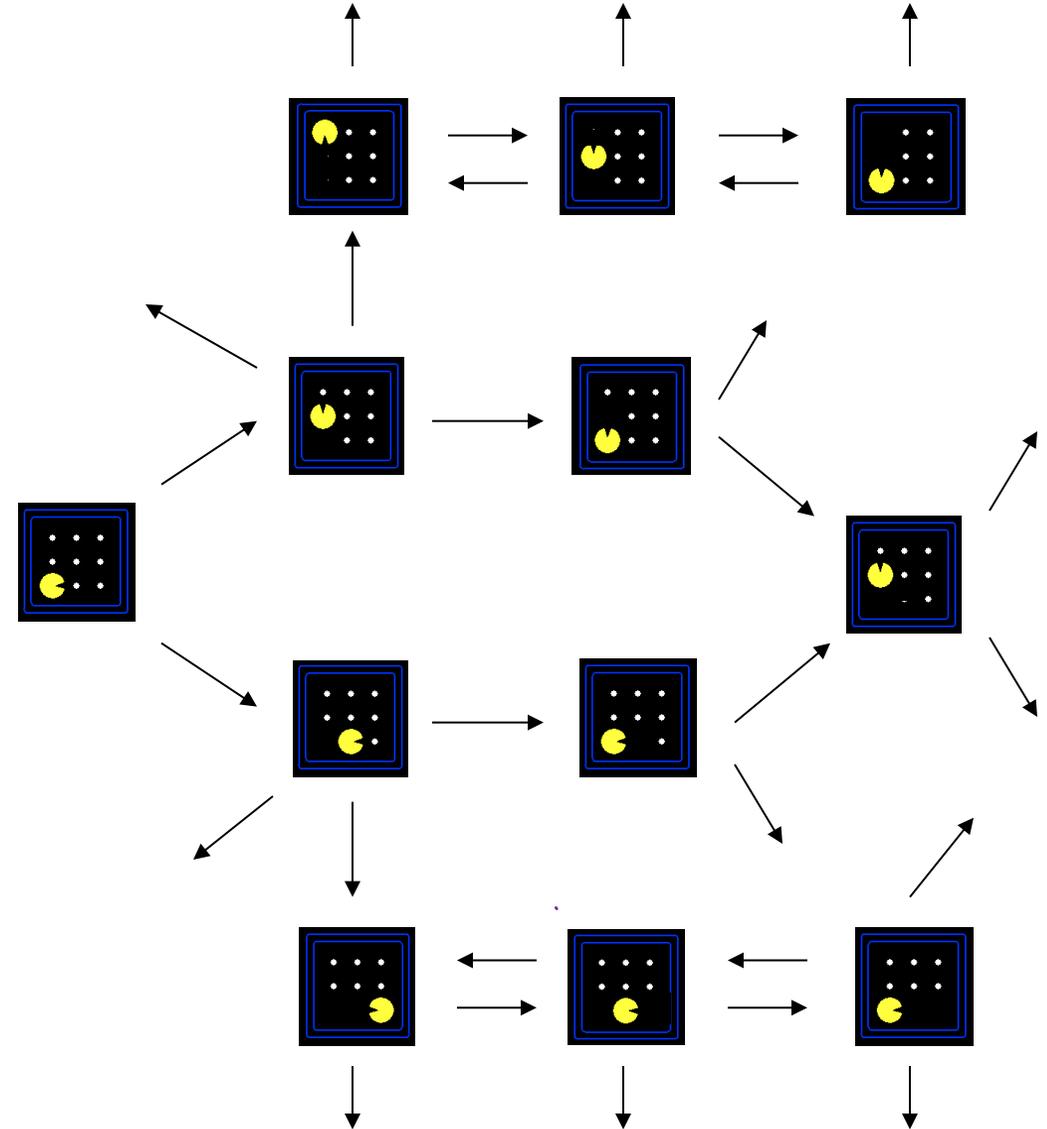
State Space Graphs and Search Trees

State Space Graphs

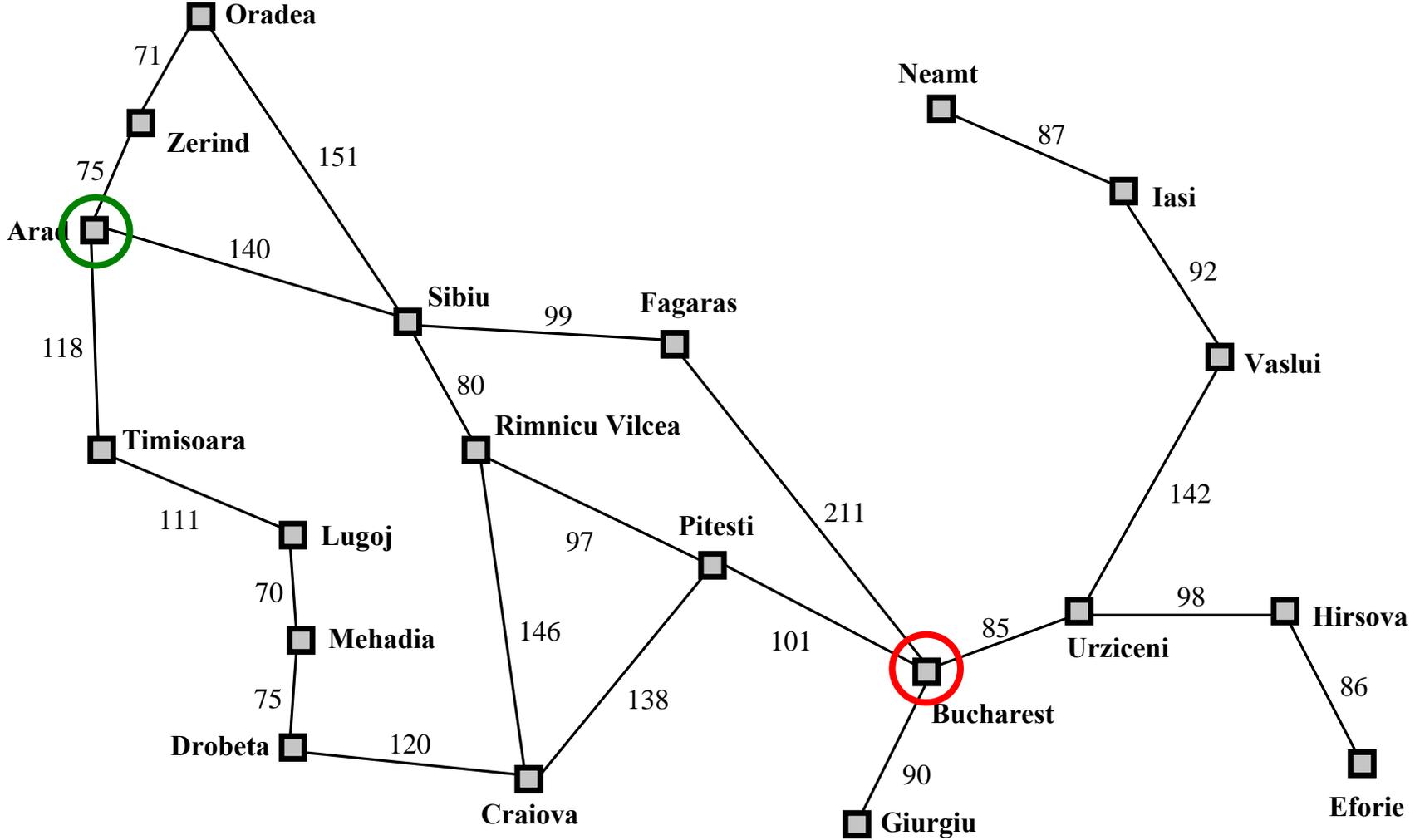State space graph: A mathematical representation of a search problem

- Nodes are (abstracted) world configurations
- Arcs represent transitions resulting from actions
- The goal test is a set of goal nodes (maybe only one)

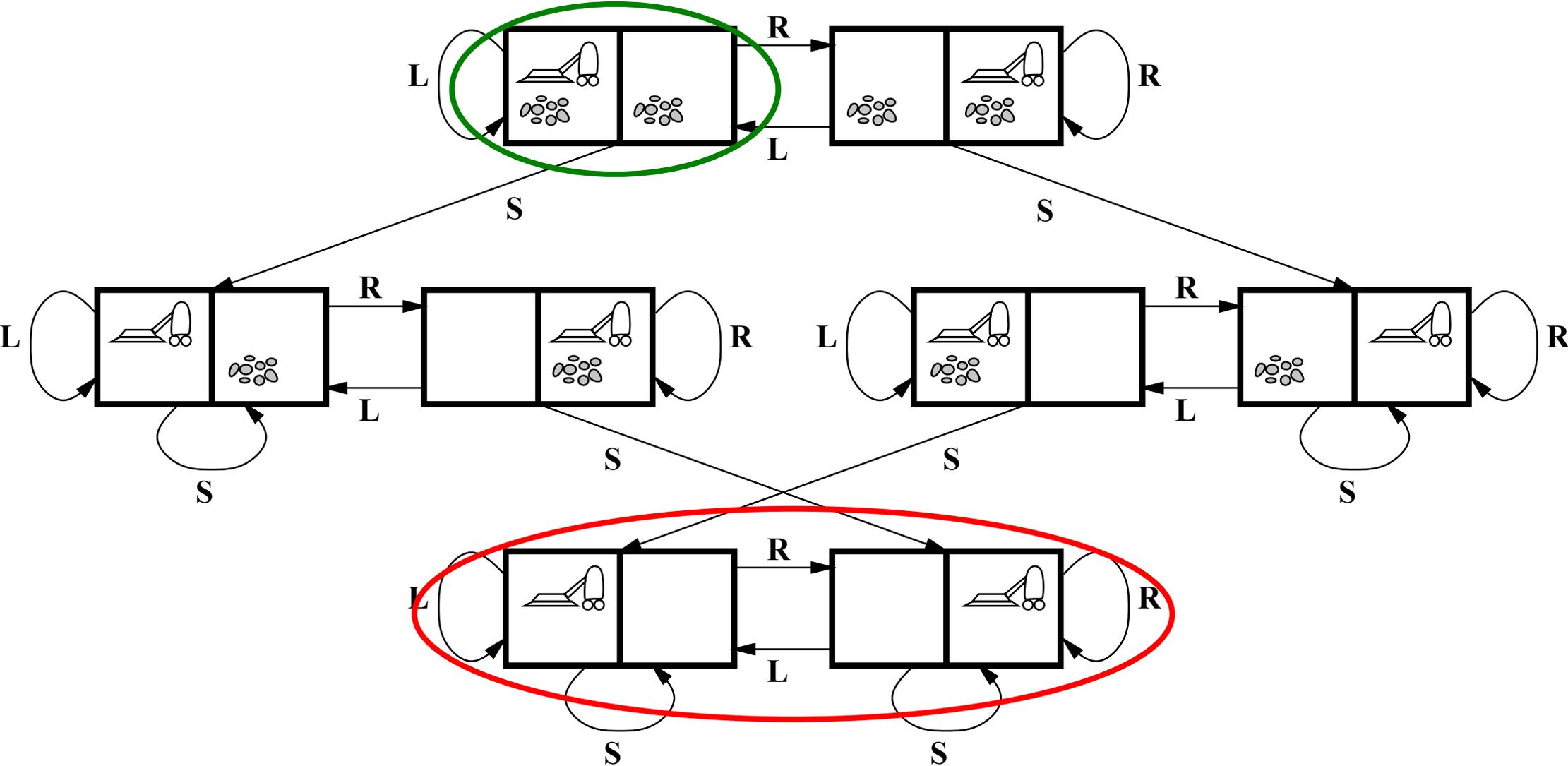In a state space graph, each state occurs only once!

We can rarely build this full graph in memory (it's too big), but it's a useful idea
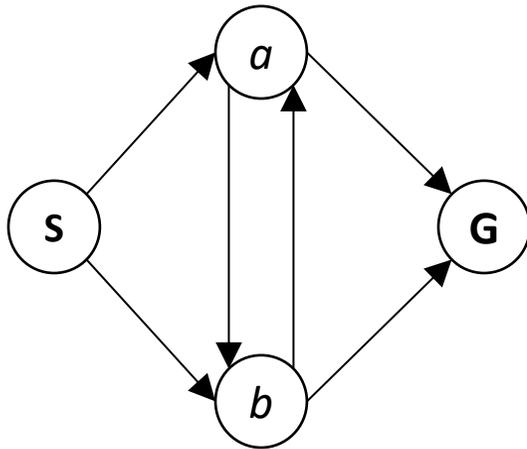
More Examples

More Examples

State Space Graphs vs. Search Trees

We build a search tree by traversing various paths in a state space graph, beginning from a specific start state.

State space graph

Resulting search tree

Important: Lots of repeated structure in the search tree!
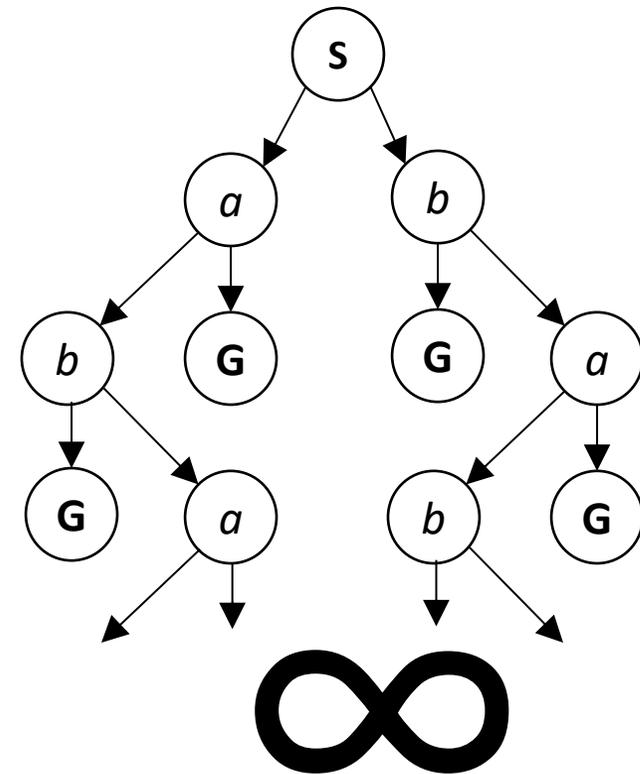
State Space Graphs vs. Search Trees
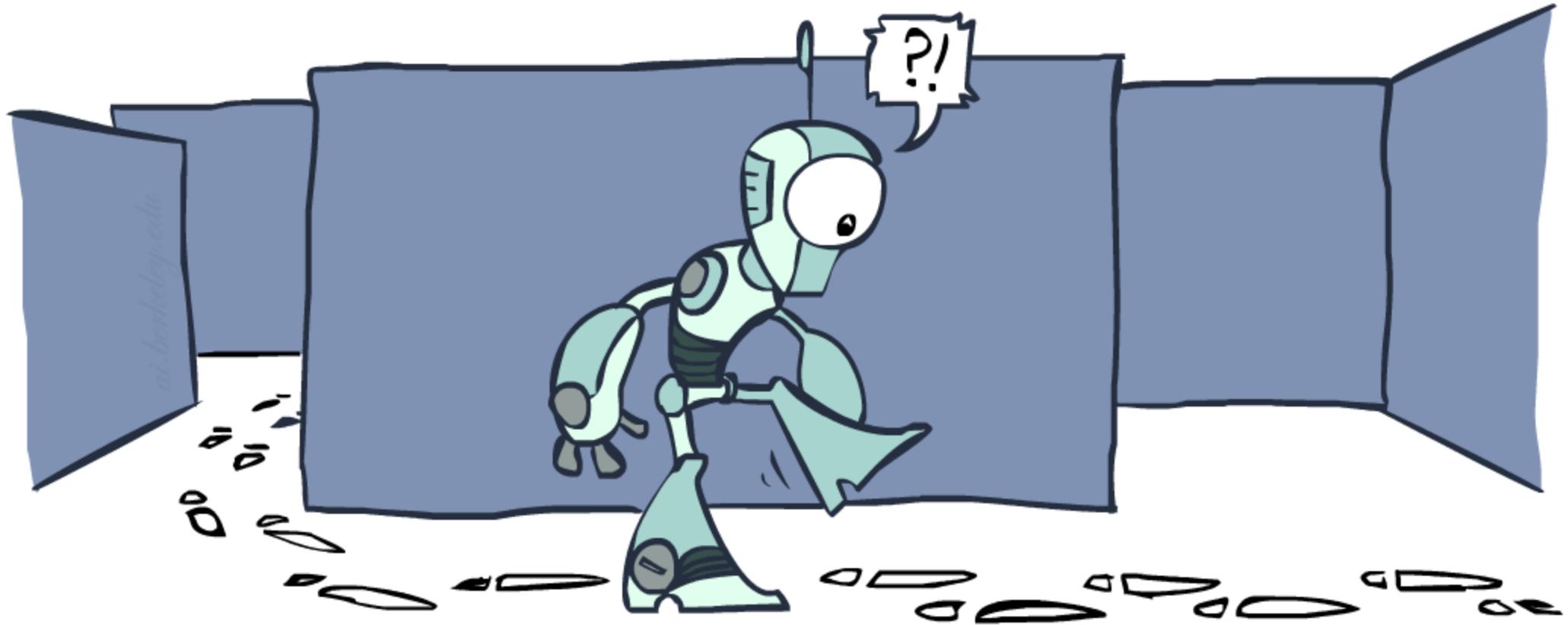
Consider this 4-state graph:

How big is its search tree (from S)?

Important: Lots of repeated structure in the search tree!

Tree Search vs Graph Search

function TREE_SEARCH(problem) returns a solution, or failure

    initialize the frontier as a specific work list (stack, queue, priority queue)

    add initial state of problem to frontier

    loop do

        if the frontier is empty then

            return failure

        choose a node and remove it from the frontier

        if the node contains a goal state then

            return the corresponding solution

        for each resulting child from node

            add child to the frontier

function GRAPH_SEARCH(problem) returns a solution, or failure
 initialize the explored set to be empty
 initialize the frontier as a specific work list (stack, queue, priority queue)
 add initial state of problem to frontier
 loop do
  if the frontier is empty then
   return failure
  choose a node and remove it from the frontier
  if the node contains a goal state then
   return the corresponding solution
  add the node state to the explored set
  for each resulting child from node
   if the child state is not already in the frontier or explored set then
    add child to the frontier

Depth-First (Tree) Search

*Strategy: expand a
deepest node first*

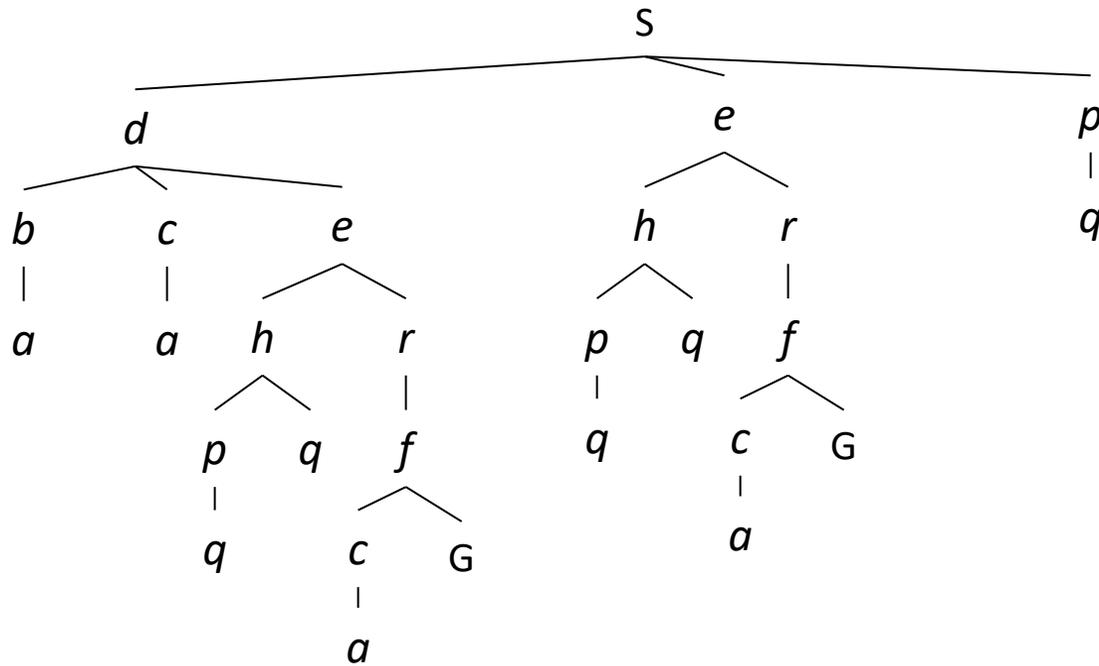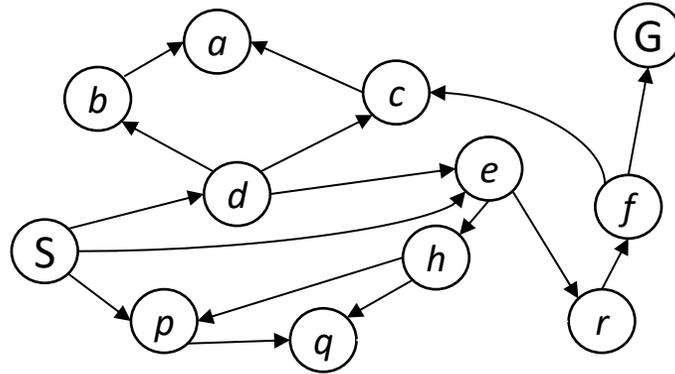*Implementation:*
Frontier is a LIFO stack

Depth-First (Graph) Search

Strategy: expand a
deepest node first

Implementation:
Frontier is a LIFO stack

Explored set prevents
loops and repeated work

Poll 1

function GRAPH-SEARCH(problem) returns a solution, or failure

    initialize the explored set to be empty

    initialize the frontier as a specific work list (stack, queue, priority queue)

    add initial state of problem to frontier

    loop do

        if the frontier is empty then

            return failure

        choose a node and remove it from the frontier

        if the node contains a goal state then

            return the corresponding solution

    add the node state to the explored set
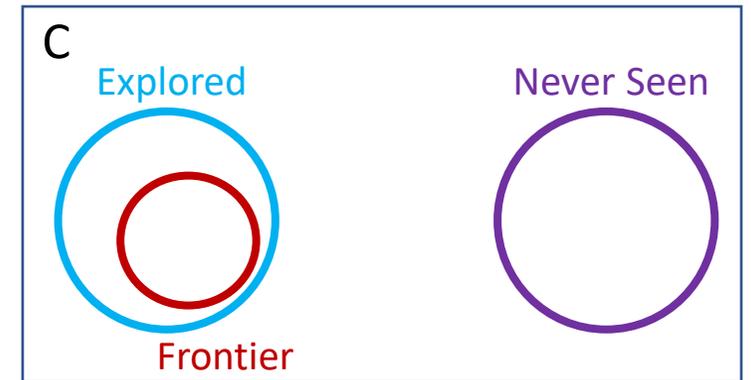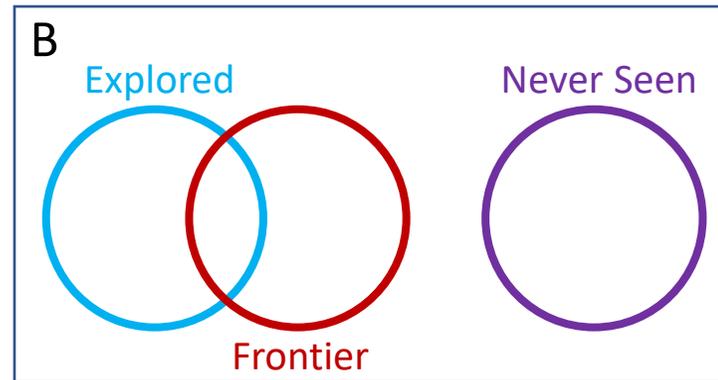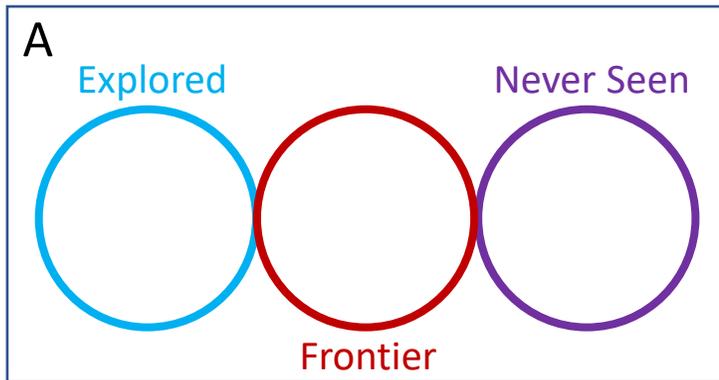
    for each resulting child from node

        if the child state is not already in the frontier or explored set then

            add child to the frontier

Poll 1

What is the relationship between these sets of states after each loop iteration in GRAPH_SEARCH?

(Loop invariants!!!)

Graph Search

This graph search algorithm overlays a tree on a graph

The frontier states separate the explored states from never seen states

Images: AIMA, Figure 3.8, 3.9

A Note on Implementation

Nodes have

state, parent, action, path-cost

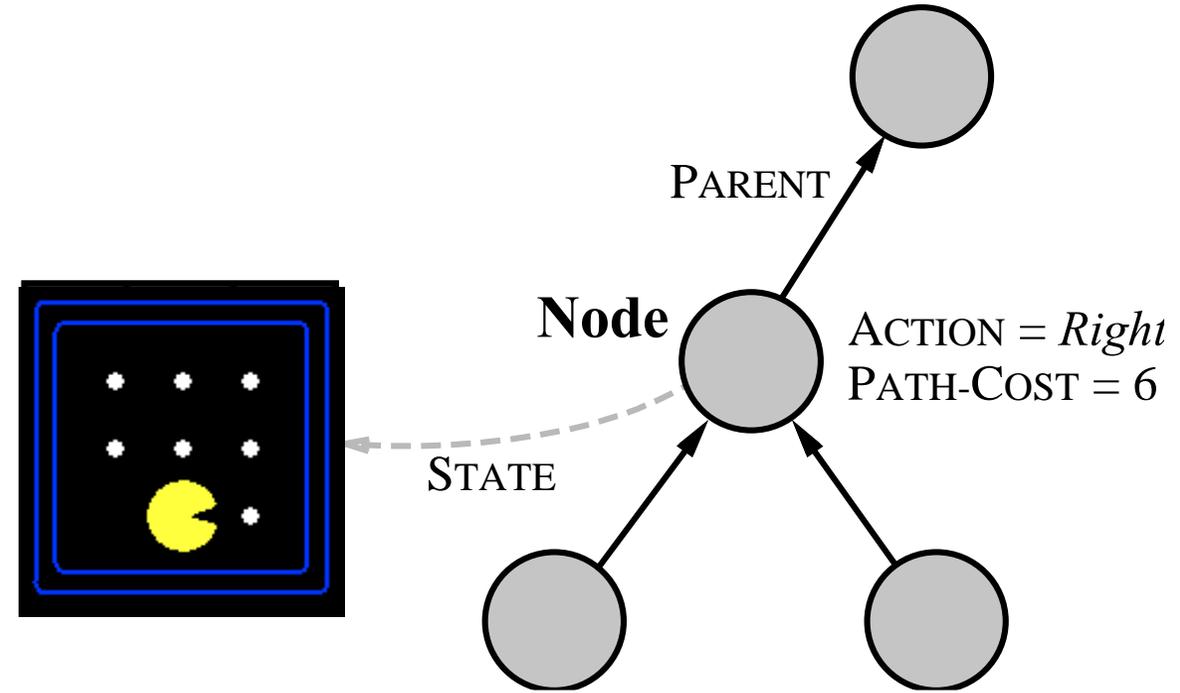**Node**, ACTION = *Right*, PATH-COST = 6, PARENT, STATE

A child of parent_node by action *a* has:

state   =   result(parent_node.state,*a*)
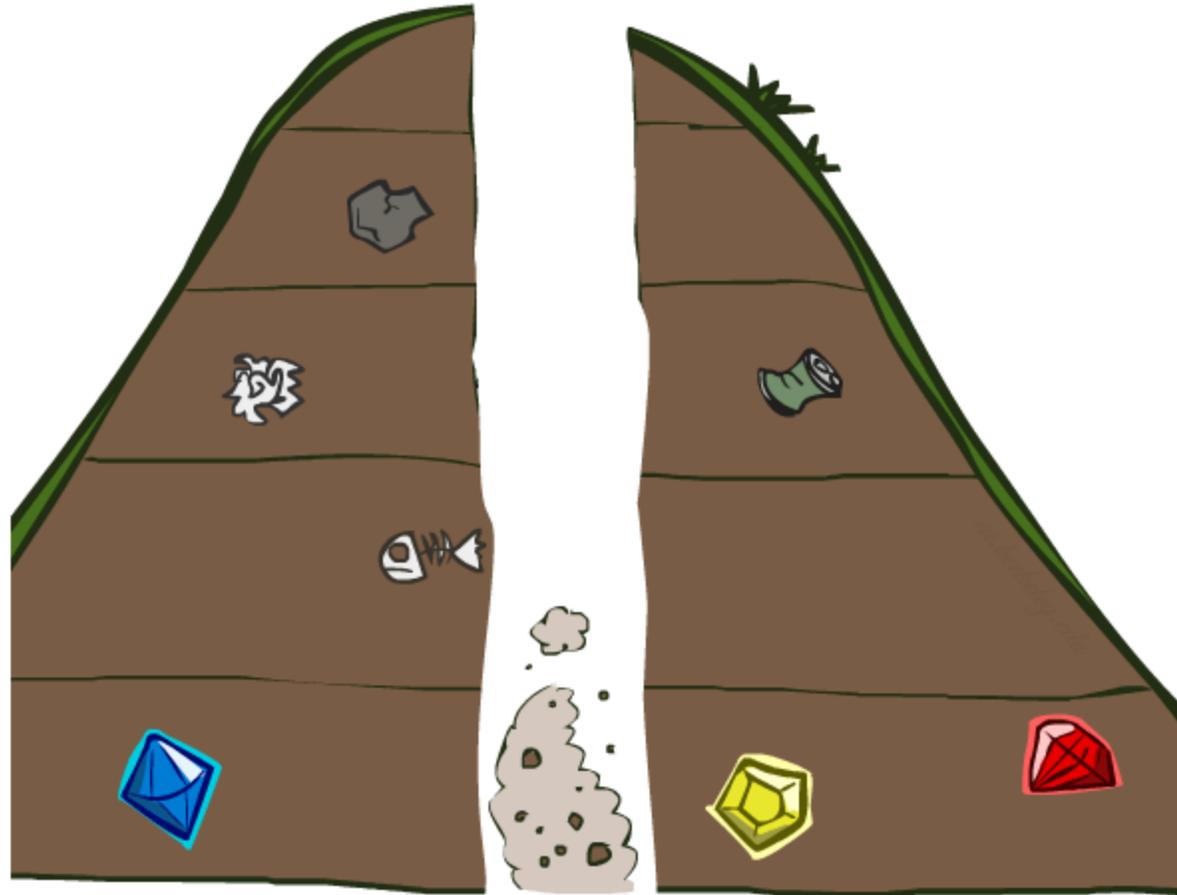
parent   =   parent_node

action   =   *a*

path-cost =   parent_node.path_cost +
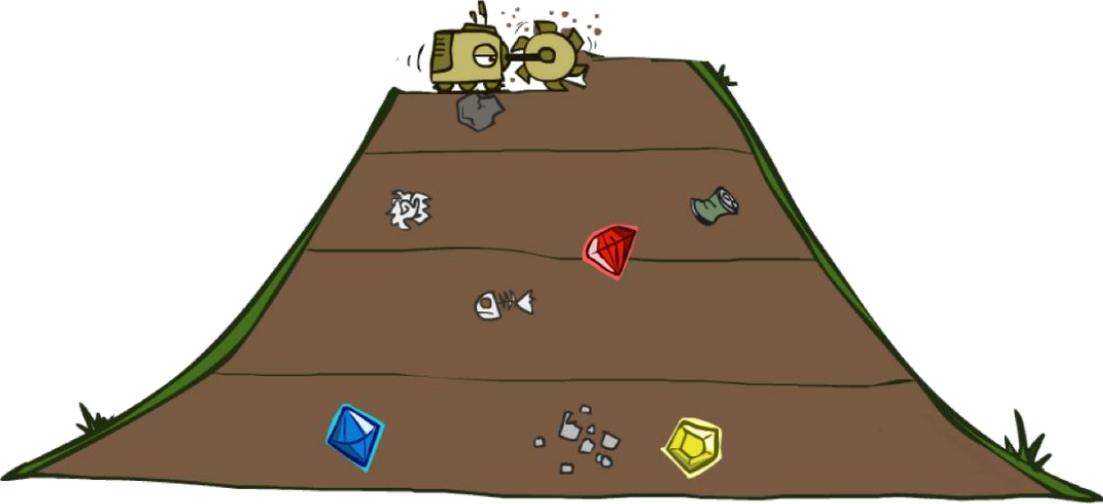   step_cost(parent_ node.state, *a*, self.state)

Extract solution by tracing back parent pointers, collecting actions
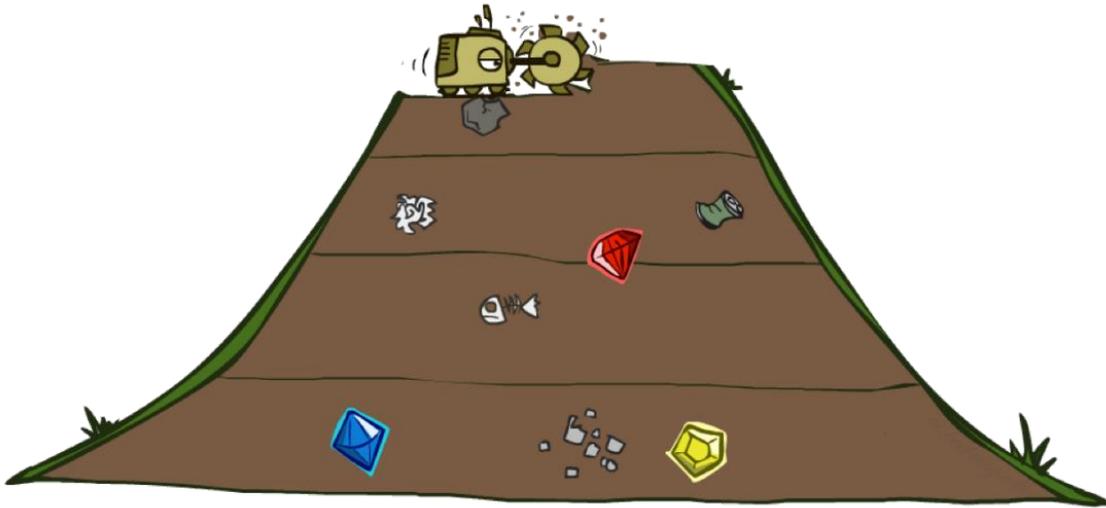
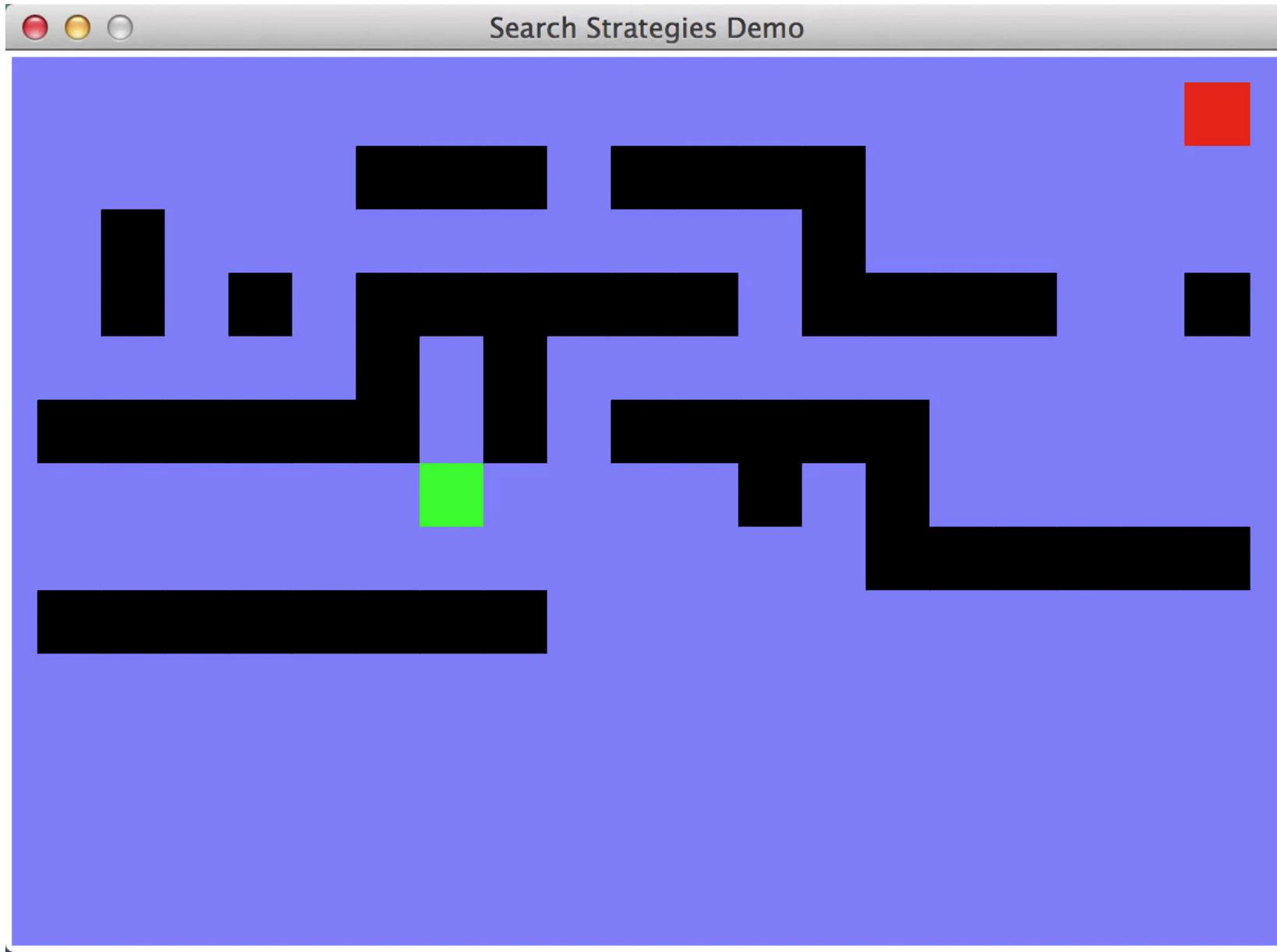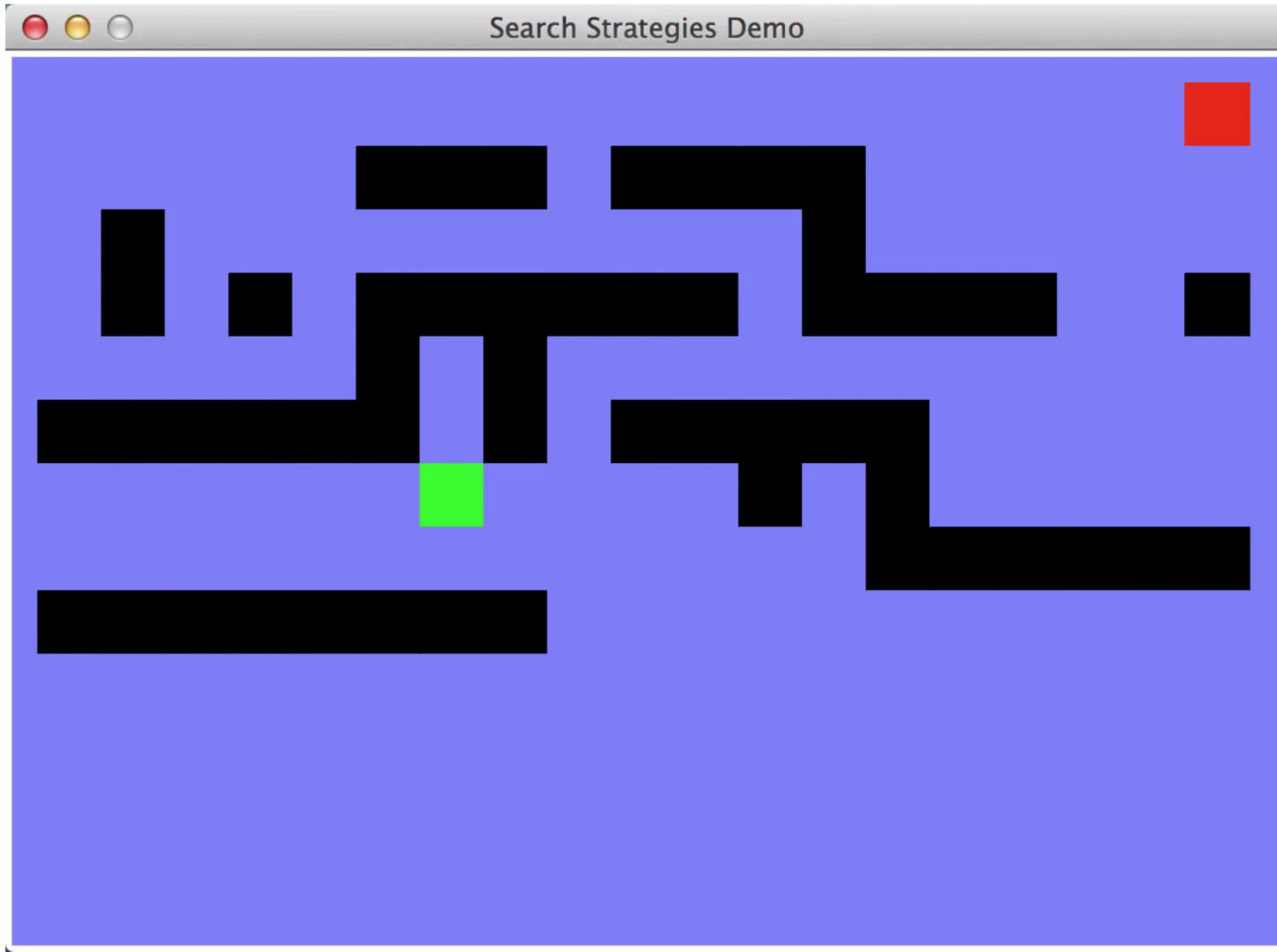# Search Algorithm Properties

BFS vs DFS

BFS vs DFS

Is the following demo using BFS or DFS

[Demo: dfs/bfs maze water (L2D6)]

Video of Demo Maze Water DFS/BFS (part 1)

Video of Demo Maze Water DFS/BFS (part 2)

BFS vs DFS

When will BFS outperform DFS?

When will DFS outperform BFS?

Search Algorithm Properties

Complete: Guaranteed to find a solution if one exists?

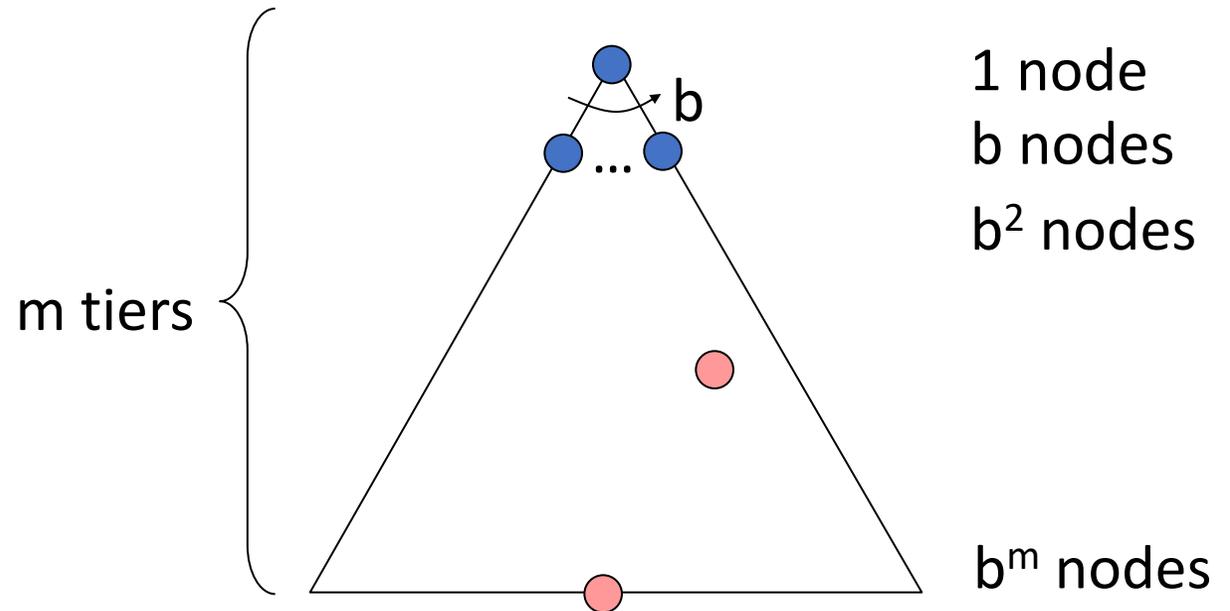Optimal: Guaranteed to find the least cost path?

Time complexity?

Space complexity?

Cartoon of search tree:
- b is the branching factor
- m is the maximum depth
- solutions at various depths

Number of nodes in entire tree?
- $1 + b + b^2 + \ldots b^m = O(b^m)$

m tiers

1 node
b nodes
b^2 nodes

b^m nodes

Search Algorithm Properties
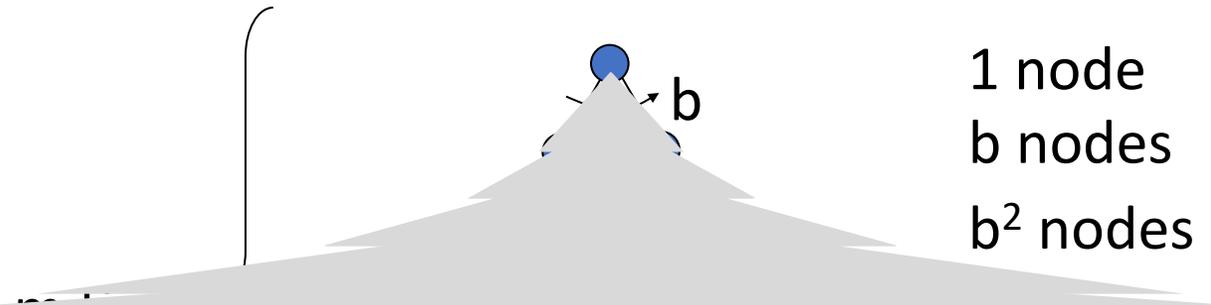
Complete: Guaranteed to find a solution if one exists?

Optimal: Guaranteed to find the least cost path?

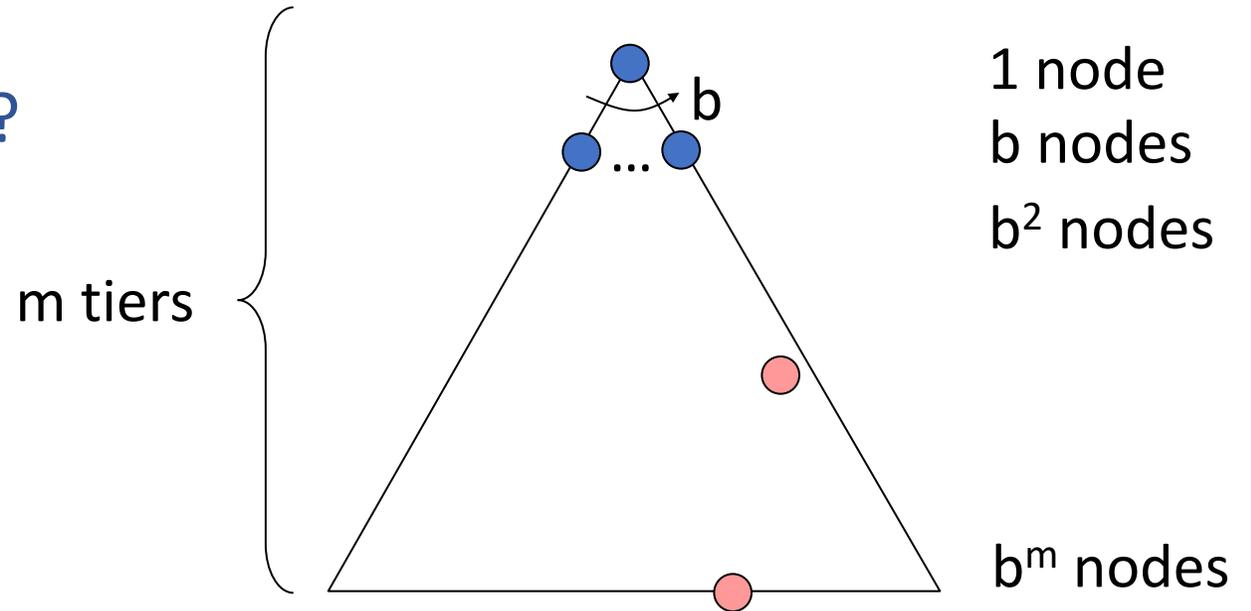Time complexity?

Space complexity?

Cartoon of search tree:
- b is the branching factor

1 node

b nodes

b^2 nodes

Poll 2

Are these the properties for BFS or DFS?

- Takes $O(b^m)$ time

- Uses $O(bm)$ space on frontier

- Complete with graph search

- Not optimal unless all goals are in the same level (and the same step cost everywhere)

m tiers

1 node
b nodes
b^2 nodes

b^m nodes

b
...

Depth-First Search (DFS) Properties

What nodes does DFS expand?

- Some left prefix of the tree.
- Could process the whole tree!
- If m is finite, takes time $O(b^m)$
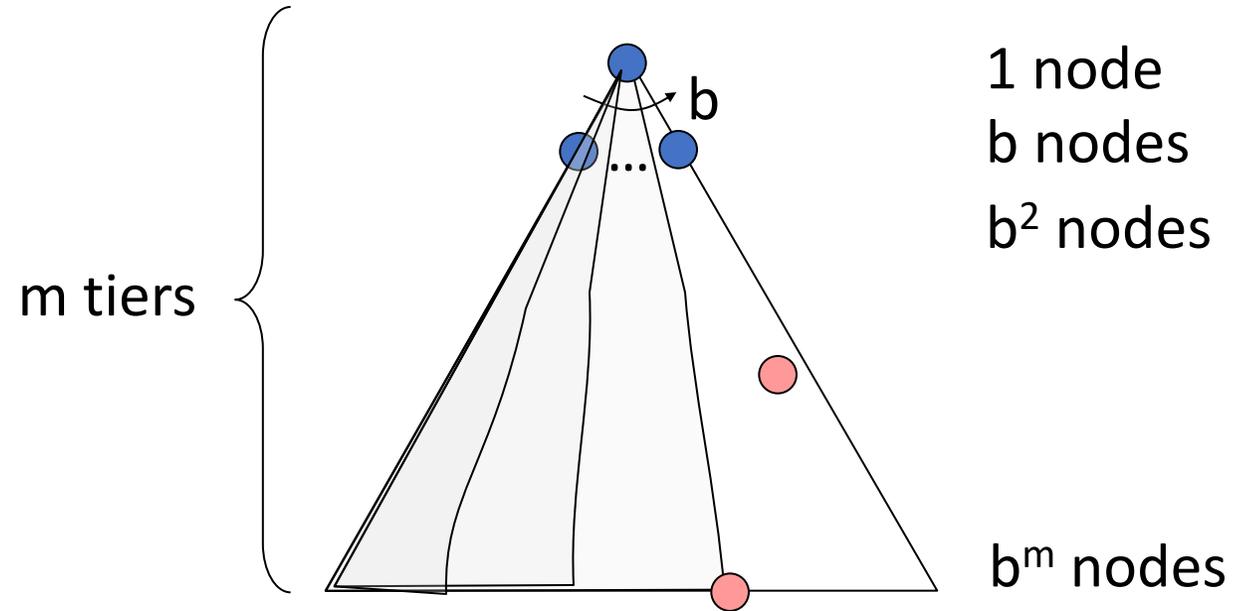
How much space does the frontier take?

- Only has siblings on path to root, so $O(bm)$

Is it complete?

- m could be infinite, so only if we prevent cycles (graph search)

Is it optimal?

- No, it finds the "leftmost" solution, regardless of depth or cost

m tiers

b

1 node

b nodes

b^2 nodes

b^m nodes

Breadth-First Search (BFS) Properties

What nodes does BFS expand?

- Processes all nodes above shallowest solution
- Let depth of shallowest solution be s
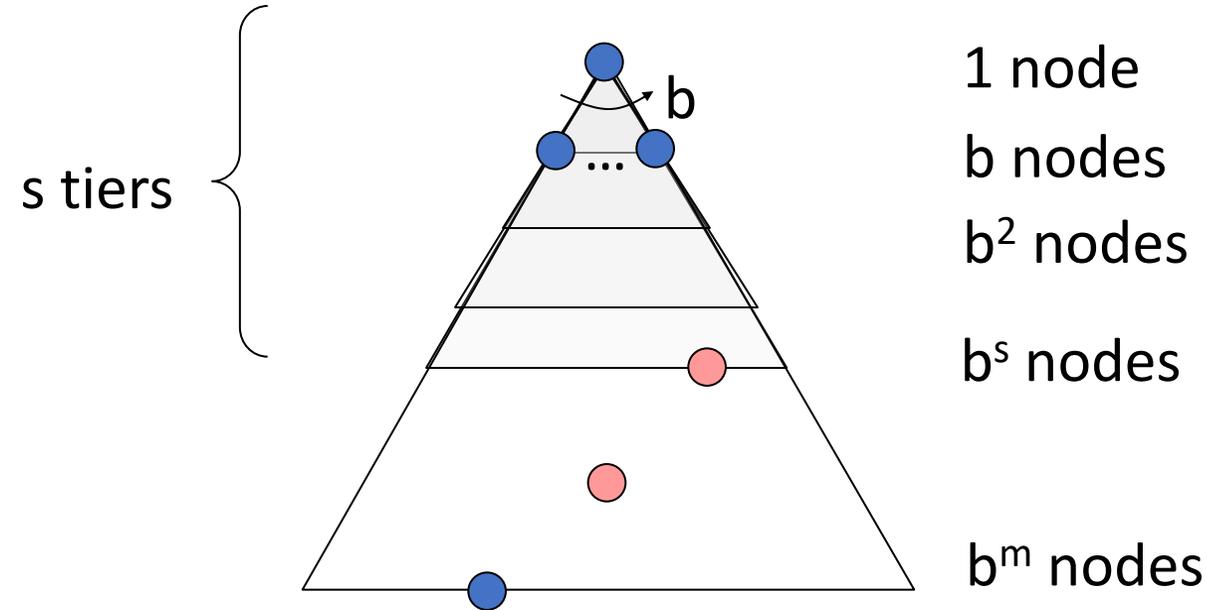- Search takes time $O(b^s)$

How much space does the frontier take?

- Has roughly the last tier, so $O(b^s)$

Is it complete?

- s must be finite if a solution exists, so yes!

Is it optimal?

- Only if costs are all the same (more on costs later)

s tiers

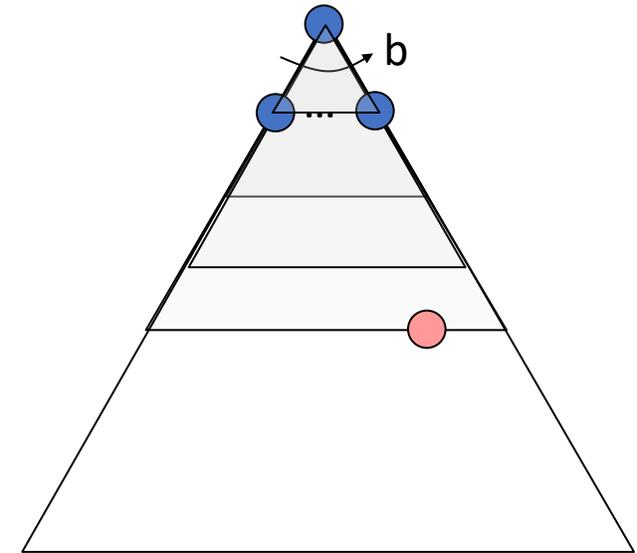1 node

b nodes

b^2 nodes

b^s nodes

b^m nodes

b

Iterative Deepening

Idea: get DFS's space advantage with BFS's time / shallow-solution advantages
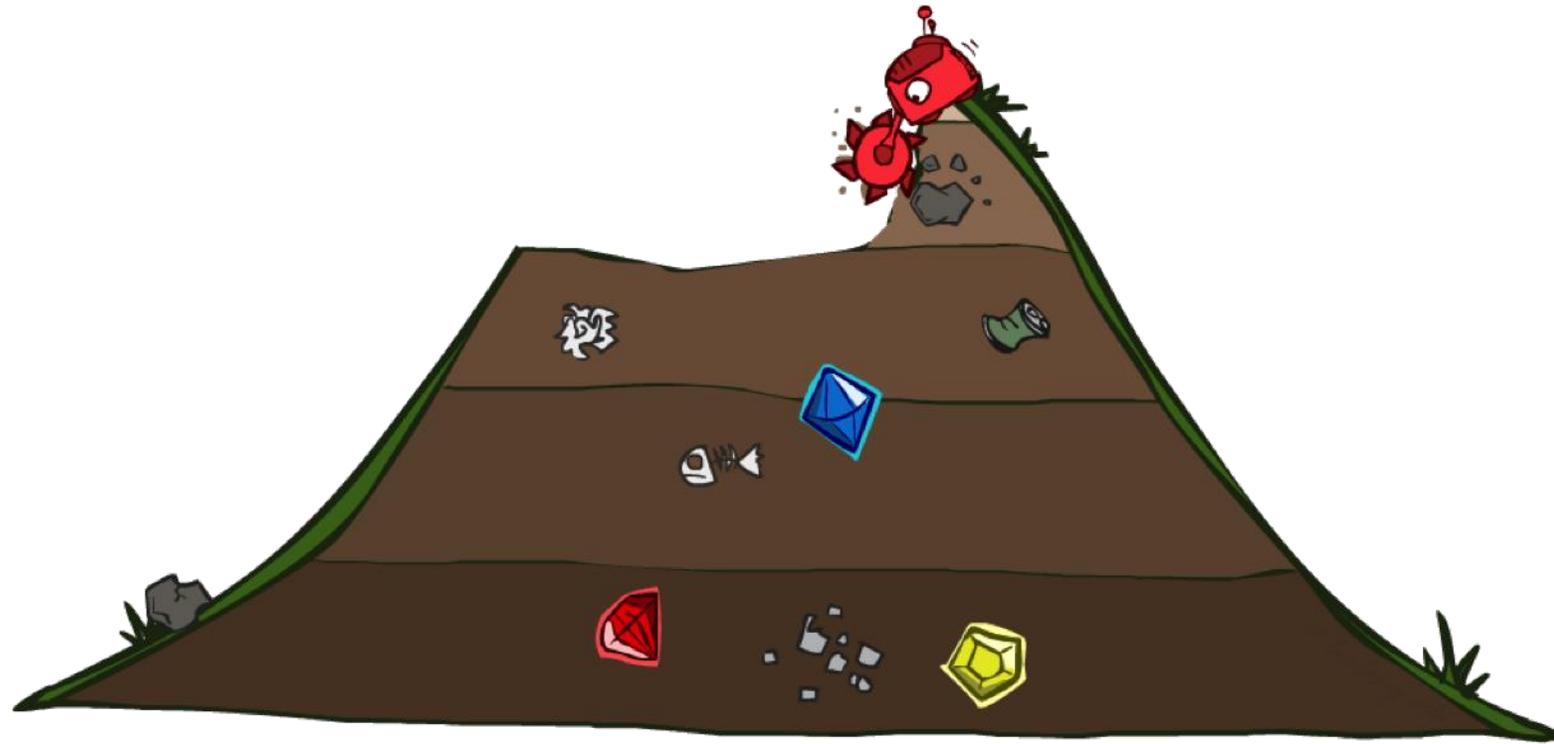
- Run a DFS with depth limit 1. If no solution…
- Run a DFS with depth limit 2. If no solution…
- Run a DFS with depth limit 3. …..
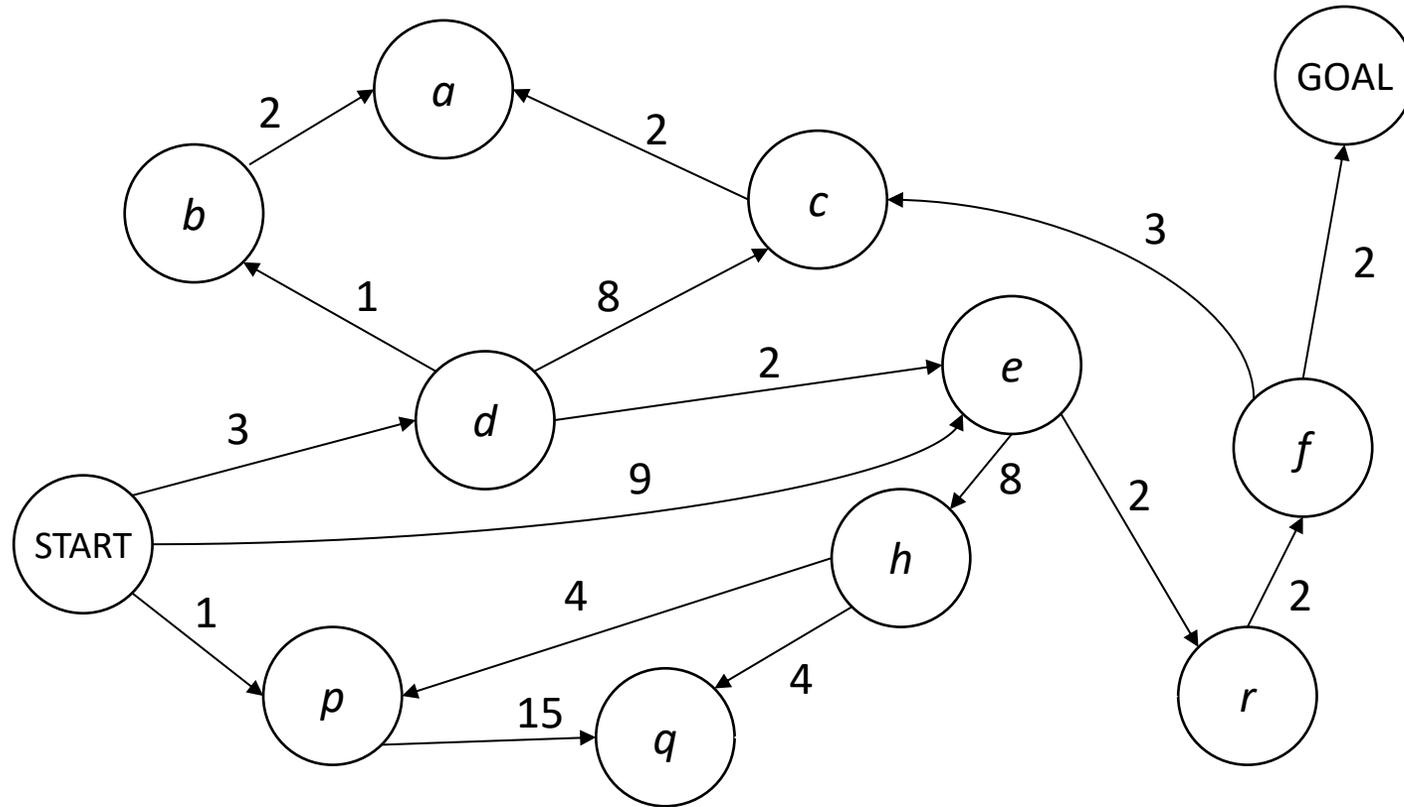
Isn't that wastefully redundant?

- Generally most work happens in the lowest level searched, so not so bad!

Uniform Cost Search
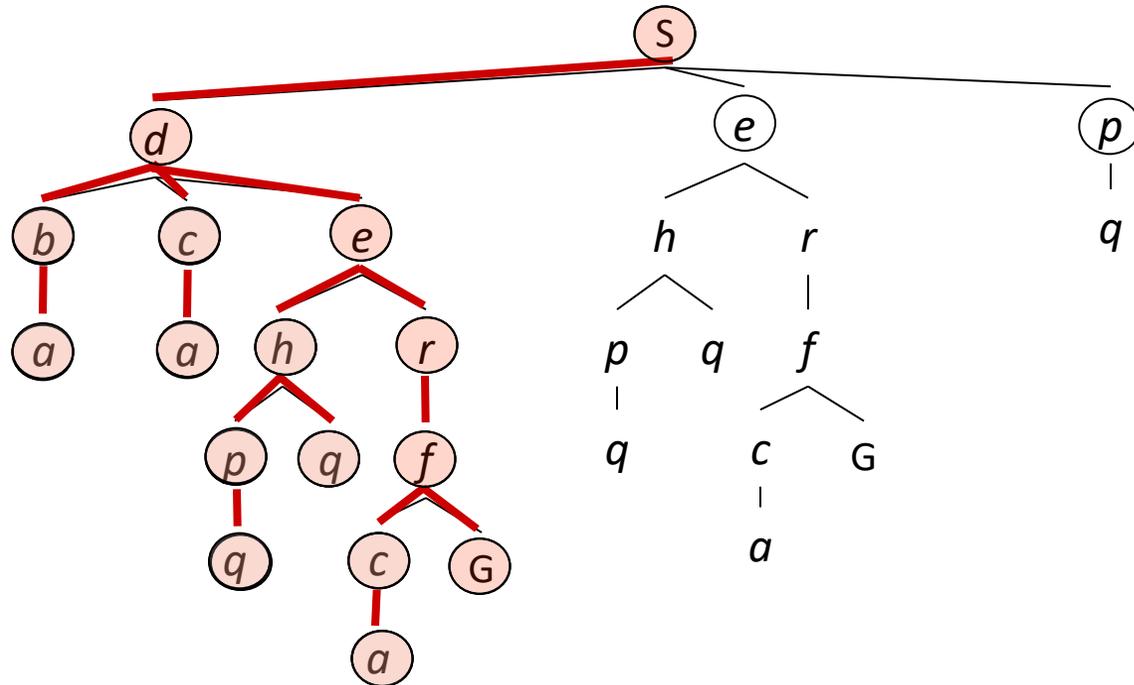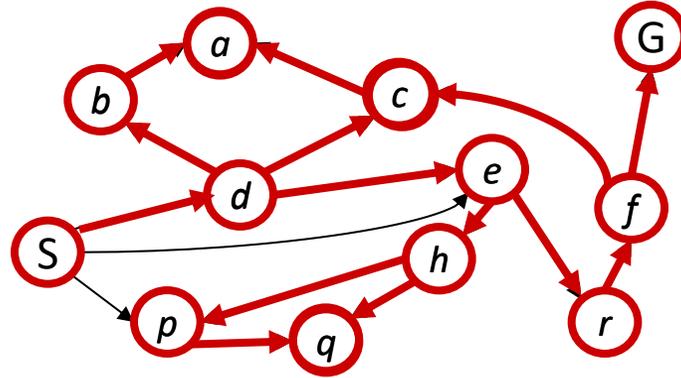
Finding a Least-Cost Path

Depth-First (Tree) Search

Strategy: expand a deepest node first
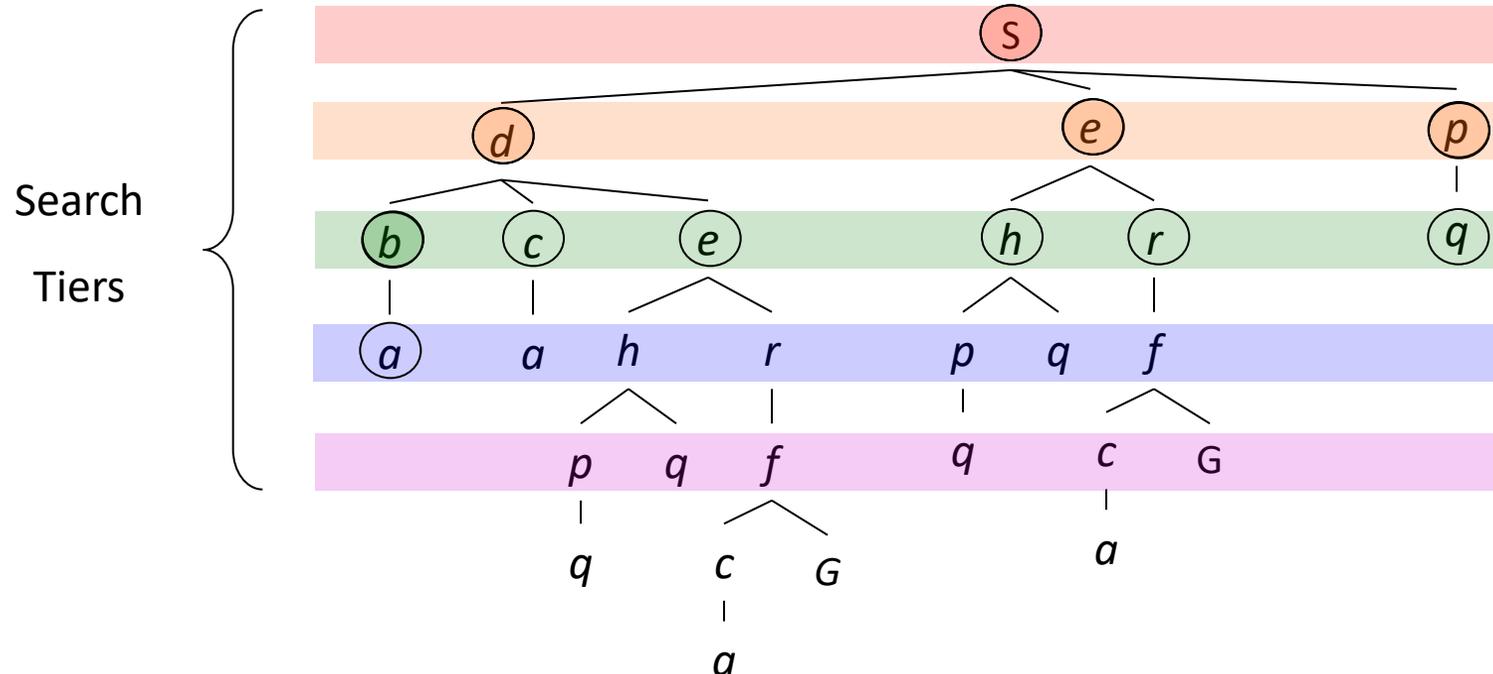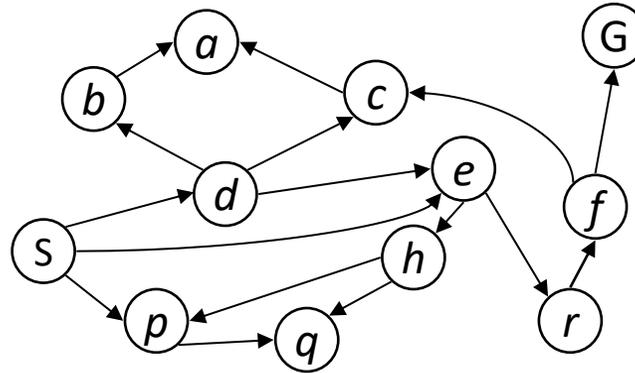
Implementation:
Frontier is a LIFO stack

Breadth-First (Tree) Search

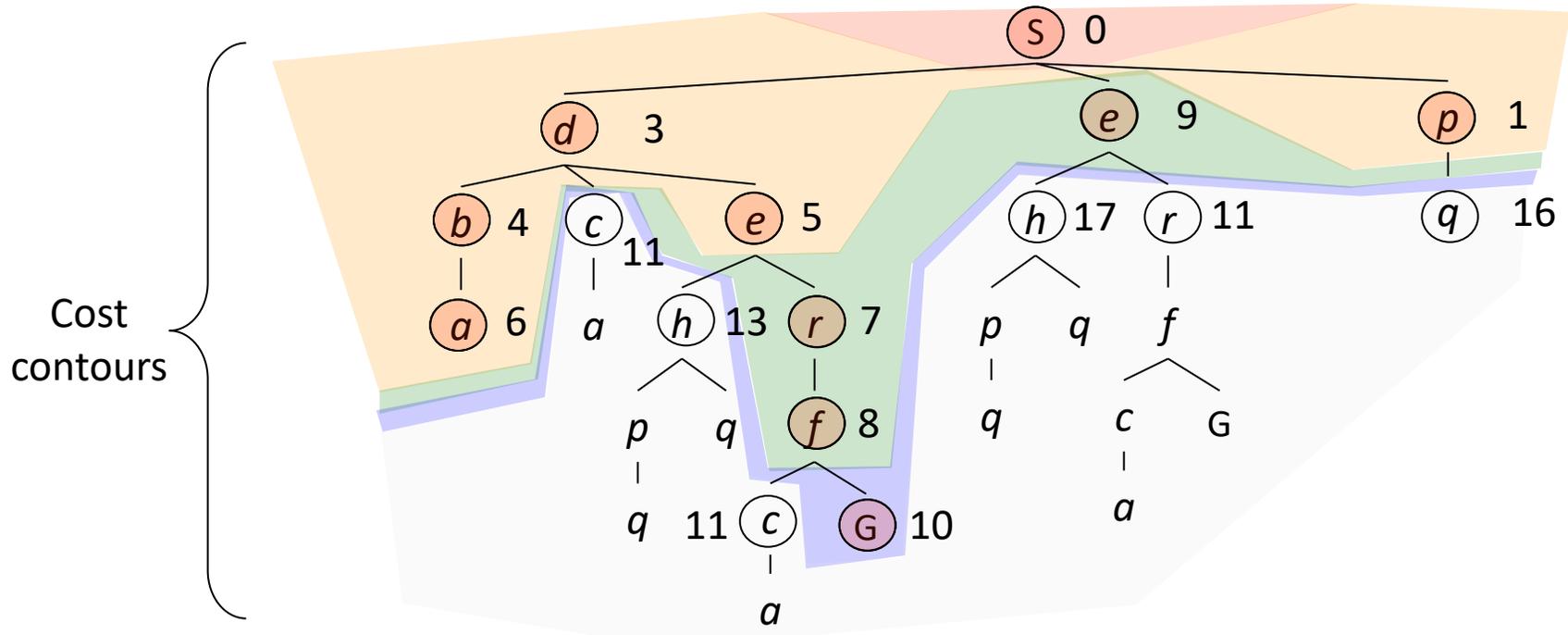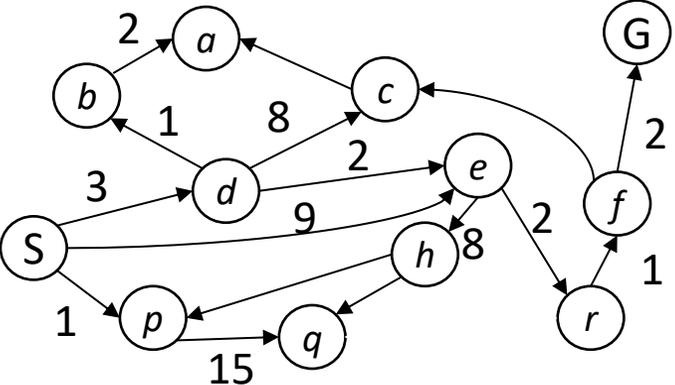*Strategy: expand a shallowest node first*

Implementation:
Frontier is a FIFO queue

Search Tiers

Uniform Cost (Tree) Search

Strategy: expand a cheapest node first:

Frontier is a priority queue (priority: cumulative cost)

Cost contours

function GRAPH_SEARCH(problem) returns a solution, or failure
    initialize the explored set to be empty
    initialize the frontier as a specific work list (stack, queue, priority queue)
    add initial state of problem to frontier
    loop do
        if the frontier is empty then
            return failure
        choose a node and remove it from the frontier
        if the node contains a goal state then
            return the corresponding solution
        add the node state to the explored set
        for each resulting child from node
            if the child state is not already in the frontier or explored set then
                add child to the frontier

function UNIFORM-COST-SEARCH(problem) returns a solution, or failure
    initialize the explored set to be empty
    initialize the frontier as a **priority queue using node path_cost as the priority**
    add initial state of problem to frontier **with path_cost = 0**
    loop do
        if the frontier is empty then
            return failure
        choose a node and remove it from the frontier
        if the node contains a goal state then
            return the corresponding solution
        add the node state to the explored set
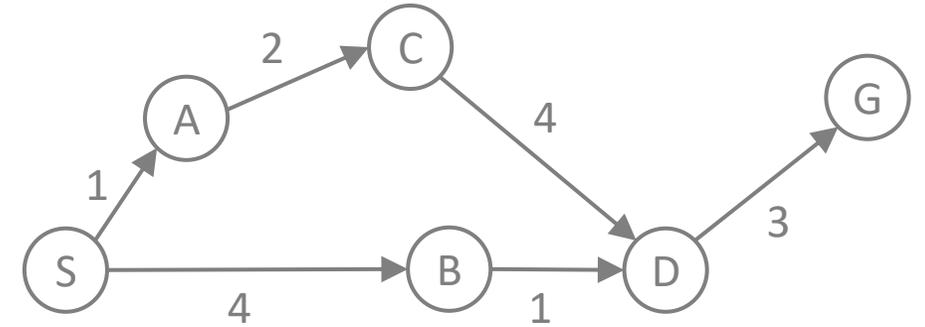   for each resulting child from node
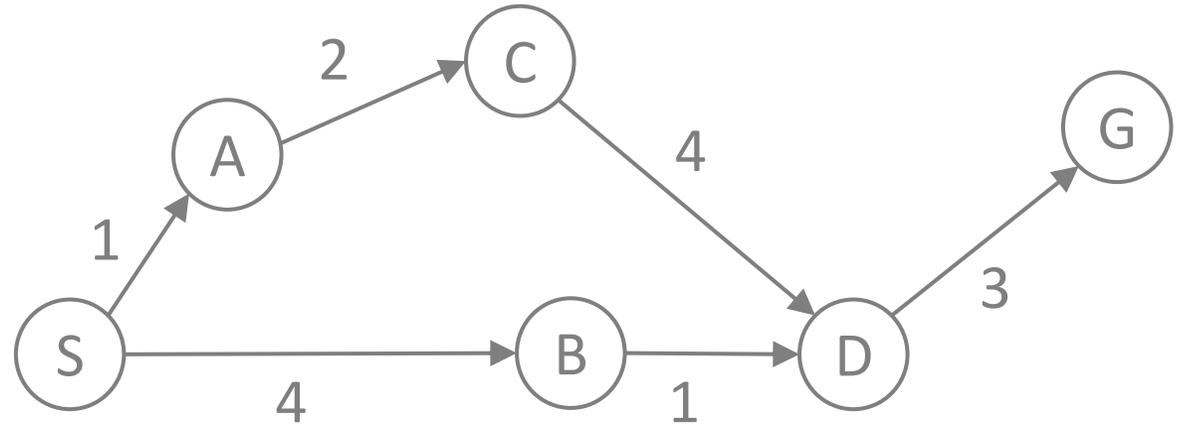   if the child state is not already in the frontier or explored set then
                add child to the frontier
            else if the child is already in the frontier with higher path_cost then
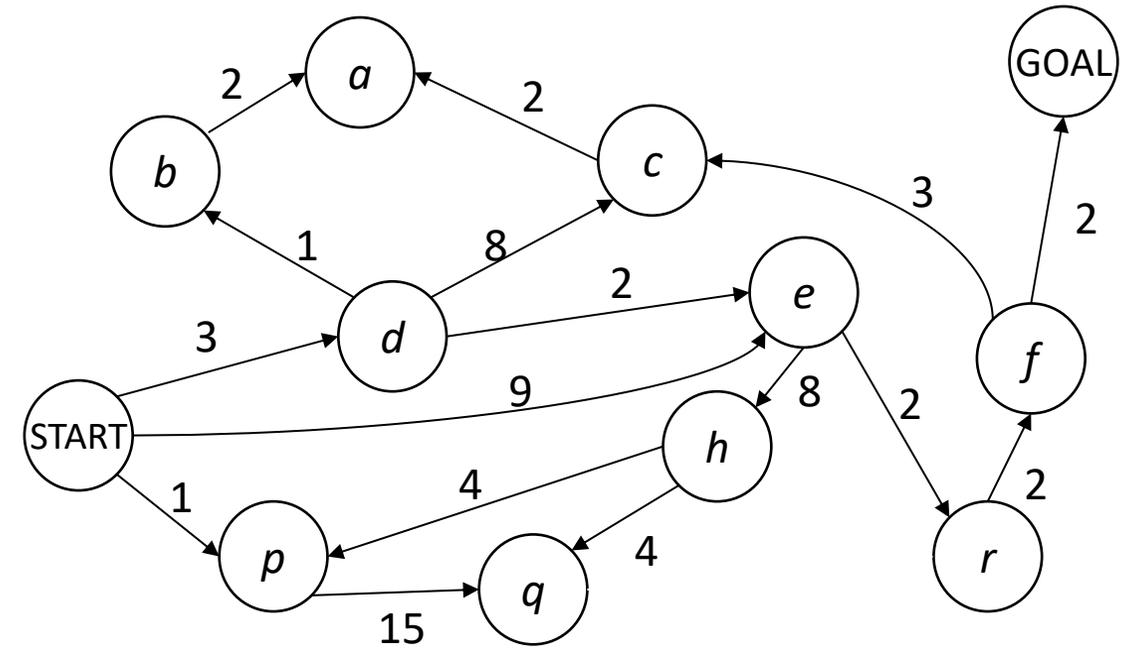   **replace that frontier node with child**

Walk-through UCS

UCS: Another Example

Uniform Cost Search (UCS) Properties

What nodes does UCS expand?

- Processes all nodes with cost less than cheapest solution!
- If that solution costs C^* and arcs cost at least ε, then the "effective depth" is roughly C^*/ε
- Takes time $O(b^{C^*/\varepsilon})$ (exponential in effective depth)
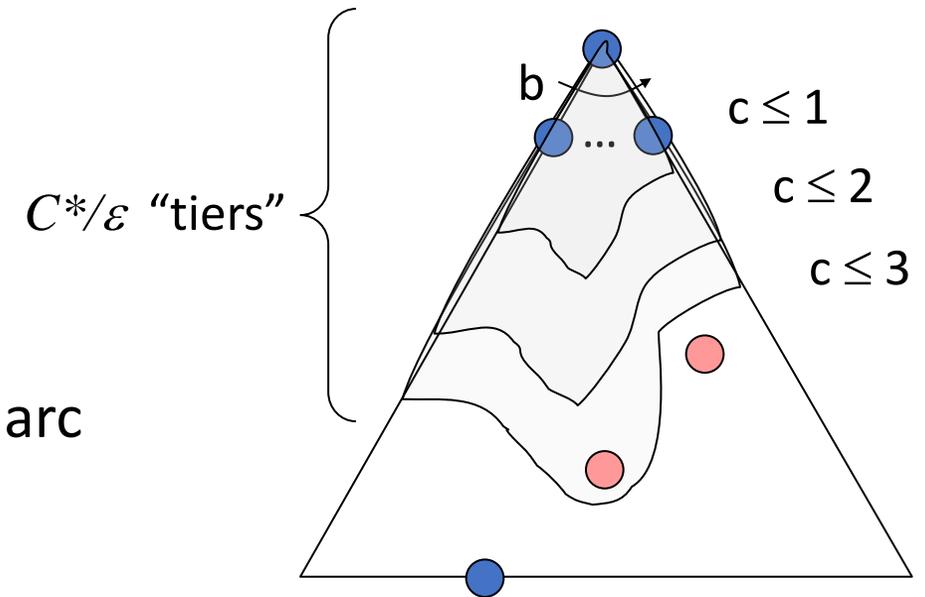
How much space does the frontier take?

- Has roughly the last tier, so $O(b^{C^*/\varepsilon})$

C^*/ε "tiers"

b

$c \leq 1$

$c \leq 2$

$c \leq 3$

Is it complete?

- Assuming best solution has a finite cost and minimum arc cost is positive, yes!

Is it optimal?

- Yes! (Proof next lecture via A*)

Uniform Cost Issues

Remember:
- UCS explores increasing cost contours

The good:
- UCS is complete and optimal!

The bad:
- Explores options in every "direction"
- No information about goal location

We'll fix that!