

**Modern Organ Exchanges:  
Designs, Algorithms, and Opportunities**

**OR**

**AI Making Life-and-Death Decisions about Humans**

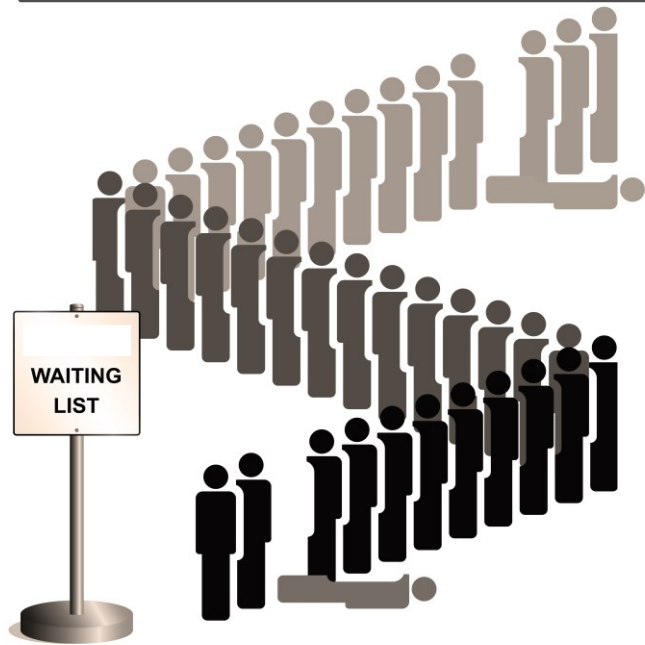
**OR**

**Longest-Running Application of AI for Good?**

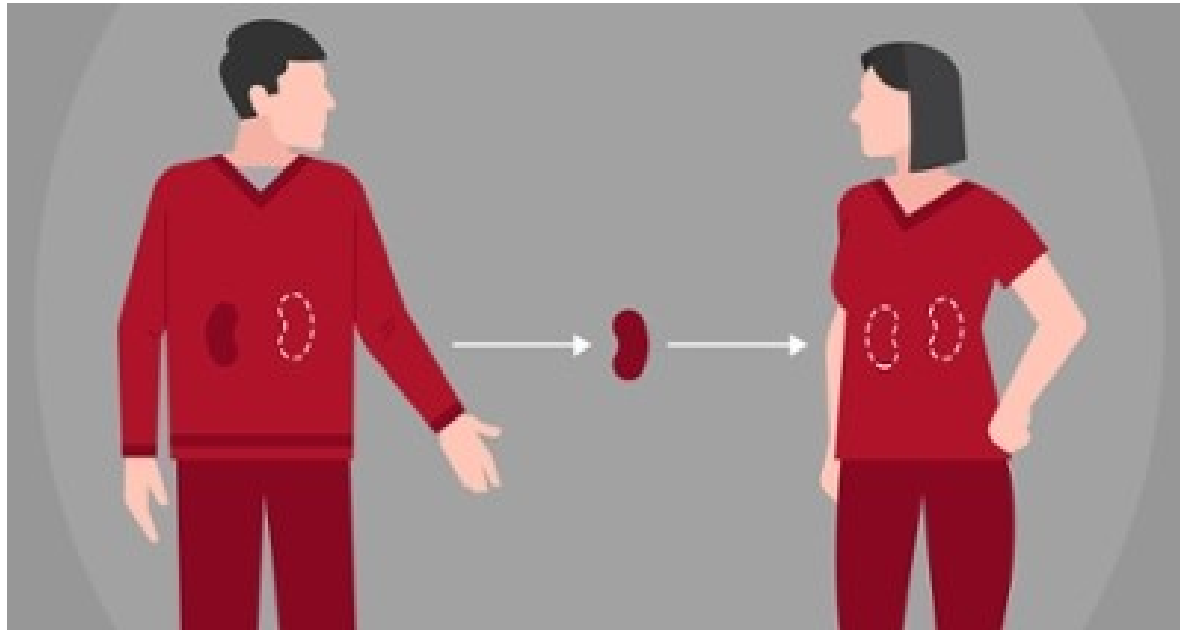
Tuomas Sandholm

**90,000+**

Waiting for a kidney  
in the U.S.



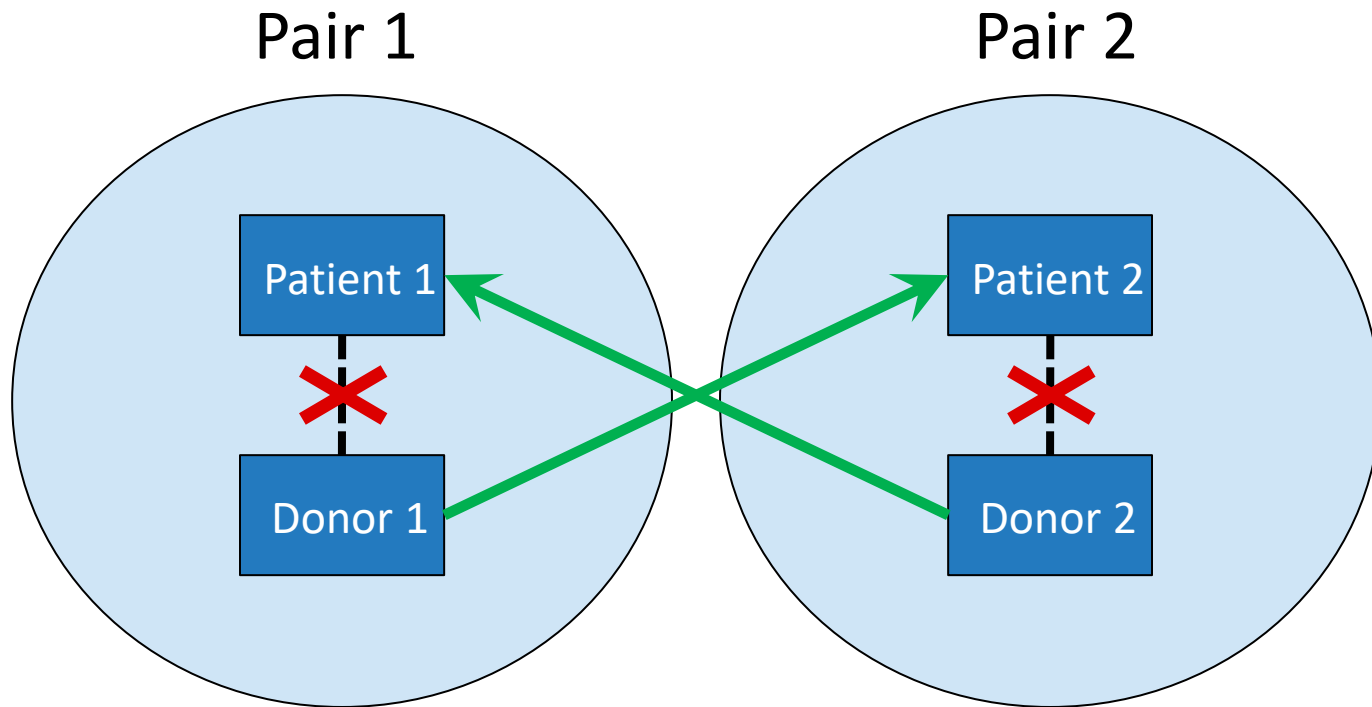
# Live donation

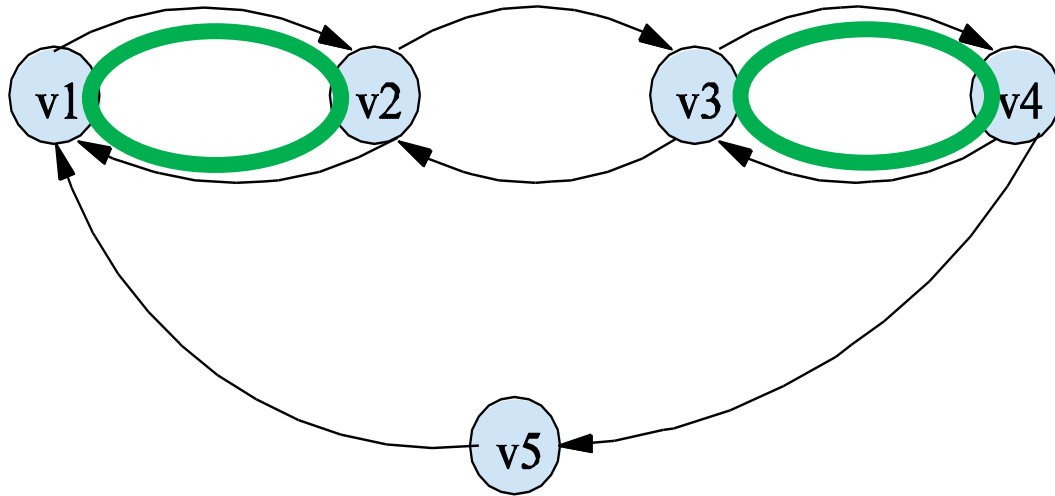


# Kidney exchange

Idea introduced in 1986 [Rapaport]

First exchange (NEPKE) started 2003-04 [Roth, Sönmez, Ünver, ...]





**Objective of the batch problem:**

Maximum weight *combination* of short disjoint cycles

# Other barter-exchange markets

- Holiday Homes: Intervac
- Books: Read It Swap It
- General used goods:  
Netcyclers / swap.com
- National Odd Shoe Exchange
- Room exchange (e.g. dorm rooms)
- Nurse shift exchange



# Cap on cycle length

- Why a cap?
  - Transplants in a cycle must occur simultaneously
  - Cycle may fail
- Cap is typically 3

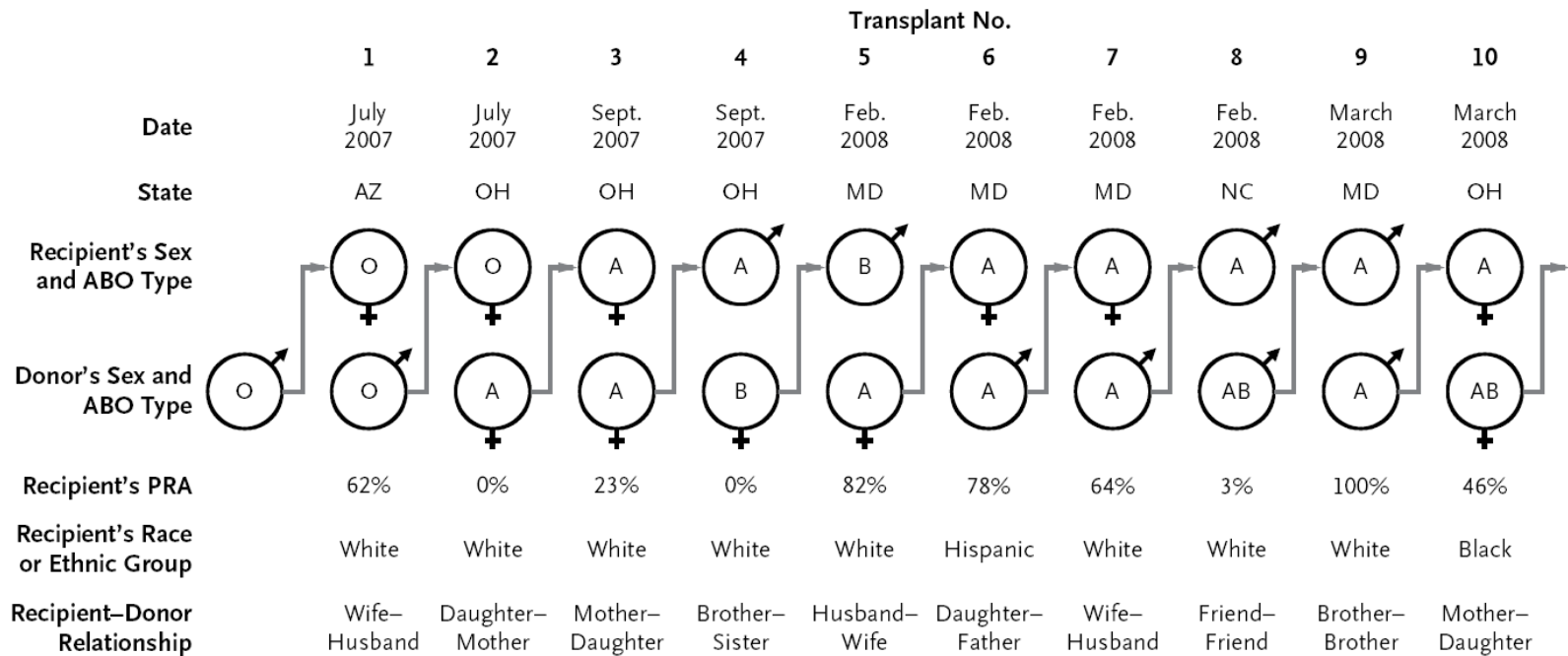
**What if ?**



# Never-ending altruist-donor (NEAD) chains

[With Rees *et al.* *New England Journal of Medicine* 2009]

- First NEAD chain, generated by our algorithm:



- NEAD chains have become the main modality of kidney exchange worldwide: >10,000 transplants

# 30-chain *[New York Times 2/18/2012]*



[National Kidney Registry]

# Kidney exchanges use designs, algorithms, and software from my CMU lab



UNITED NETWORK FOR ORGAN SHARING

- Technology selected in 2008
  - Licensed to UNOS for free
  - National exchange went live in 2010
  - Now includes 80% of the transplant centers in the US
  - Match run every week
  - Only US organ exchange that is fully algorithmically run
- 
- Previously:
    - Alliance for Paired Donation
    - Paired Donation Network

# Solving the batch problem

- NP-complete (even without chains) [Abraham, Blum, Sandholm, EC-07]
- Novel branch-and-price algorithm enabled nationwide scaling [Abraham, Blum, Sandholm, EC-07]
- ...
- Fastest current algorithm: [Dickerson, Manlove, Plaut, Sandholm, Trimble, EC-16]
  - $x_{ij} \rightarrow x_{ijk}$
  - uses the extra constraints:

**“if an edge is used at position k+1 in chain, there must be an appropriate edge used at position k in that chain”**

# “Position-indexed” compact formulation for within-batch chain caps

[Dickerson, Manlove, Plaut, Sandholm & Trimble, EC-16]

$$\max \sum_{(i,j) \in A} \sum_{k \in \mathcal{K}(i,j)} w_{ij} y_{ijk} + \sum_{c \in \mathcal{C}} w_c z_c \quad (3a)$$

$$\text{s.t.} \quad \sum_{j:(j,i) \in A} \sum_{k \in \mathcal{K}(j,i)} y_{jik} + \sum_{c \in \mathcal{C}: i \text{ appears in } c} z_c \leq 1 \quad i \in P \quad (3b)$$

$$\sum_{j:(i,j) \in A} y_{ij1} \leq 1 \quad i \in N \quad (3c)$$

$$\sum_{\substack{j:(j,i) \in A \\ k \in \mathcal{K}(j,i)}} y_{jik} \geq \sum_{j:(i,j) \in A} y_{i,j,k+1} \quad \forall i \in P, \\ k \in \{1, \dots, K-1\} \quad (3d)$$

$$y_{ijk} \in \{0, 1\} \quad (i, j) \in A, k \in \mathcal{K}(i, j) \quad (3e)$$

$$z_c \in \{0, 1\} \quad c \in \mathcal{C} \quad (3f)$$

3a: max weight of edges in chains + weight of cycles

3b: each pair is in at most one chain or cycle

3c: each NDD has at most one used out-edge

**3d: if an edge is used at position k+1 in chain, there must be an appropriate edge used at position k in that chain**

**Additional functionality for modern kidney exchanges supported by our algorithm and our later enhancements**

# Multiple willing donors per patient

- All their edges included in input graph
- Solver automatically uses at most one of the donors

# Incorporating compatible pairs

- Why?
  - Patient can get a better kidney
  - Others get more/better matches
- Our algorithm supports this
  - Could preprocess so patient can't get worse kidney than her compatible donor brings



# Weights on edges

- Algorithm supports weights on edges (thus also on nodes)
- Weights can represent, e.g.,
  - Degrees of compatibility
  - Projected life years (potentially quality-adjusted)
  - Travel distance
  - Wait time
  - Transplanting children
  - Transplanting sensitized, hard-to-match patients

# Side constraints

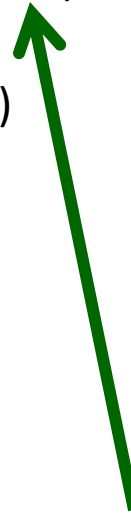
- Algorithm supports certain kinds of side constraints, e.g.,
  - Center A does not want to be in cycles longer than 2
  - Patient x does not want to be in a cycle longer than 2
  - Center B does not want to participate in altruistic donor chains of length greater than 3
  - ...

# Fielded kidney exchanges

- NEPKE (started 2003-04, now closed)
- United Network for Organ Sharing (UNOS)
- Alliance for Paired Donation
- Paired Donation Network (now closed)
- National Kidney Registry
- San Antonio
- Mayo Clinic
- St. Barnabas Compassionate Share
- Netherlands
- UK
- Canada
- Australia
- Portugal
- Israel
- Sweden
- ...



~600 transplants  
in US per year,  
mainly via NEAD  
chains



Only US one that uses  
purely algorithmic matching

# **Failure-aware kidney exchange**

[Dickerson, Procaccia & Sandholm,  
EC-13, Management Science 2019]

# Failure-aware kidney exchange

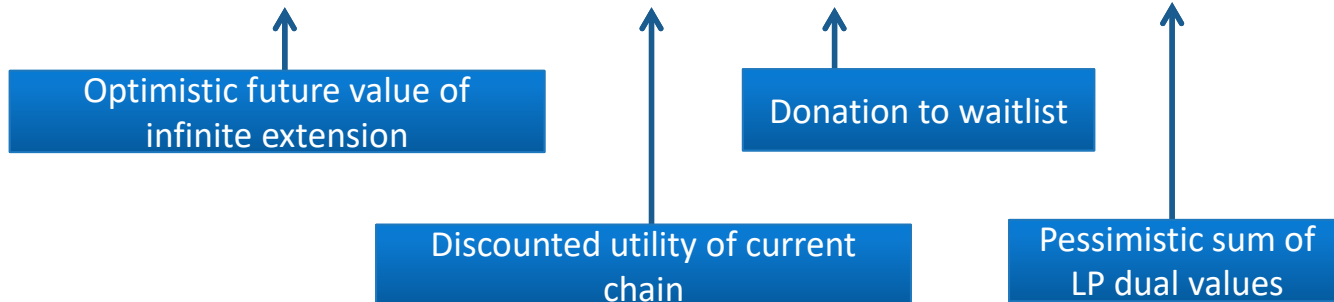
[Dickerson, Procaccia & Sandholm, EC-13, Management Science 2019]

- Only 7-12% of planned transplants go into execution
- We propose to find a solution that has maximum *expected* weight
  - Each edge has a weight and a success probability
  - Can't just multiply weight and probability
- We needed to develop a different optimal algorithm
  - Based on branch-and-price

# Algorithm changes for probabilistic setting

- Use chain extension in pricing problem
  - **Theorem.** Don't need to extend a chain by any #steps if optimistic infinite extension has negative value:

$$\left( \frac{q_{max}}{1 - q_{max}} \prod_{i=0}^{k-1} q_i \right) + u(c) + \ell - \left( d_{min} + \sum_{i=0}^k d_i \right) \leq 0$$



- Ordering heuristics for cycle and chain generation
- Upper bound now hard
  - **Theorem.** Discounted clearing NP-complete (even with no chains or cycle length cap)
  - So, we use looser bound: solve with  $w'_e = (1 - p_{fail}) w_e$
- Lower bound still easy
  - **Theorem.** Discounted clearing with 2-cycles polytime

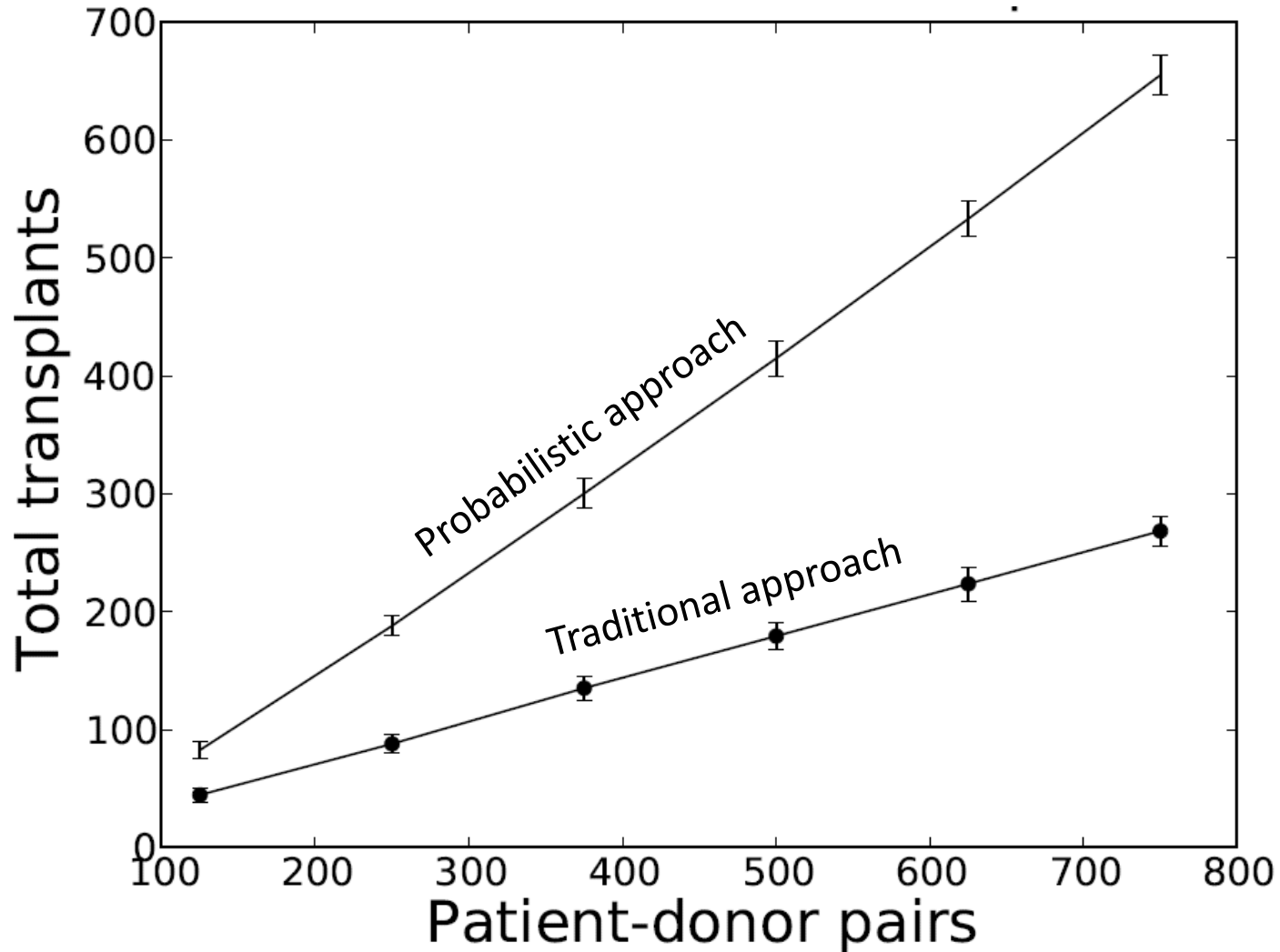
# Scalability experiment

Time limit 1 hour; 8GB RAM; Saidman *et al.* generator;  $p_{\text{fail}} = 0.7$ ;  $\#\text{altruists} = 0.1 * \#\text{pairs}$

$ V $	CPLEX (Discounted)		Ours (Discounted)	
	Cleared	Time (cleared)	Cleared	Time (cleared)
10	127 / 128	0.044	128 / 128	0.027
25	125 / 128	0.045	128 / 128	0.023
50	105 / 128	0.123	128 / 128	0.046
75	91 / 128	0.180	126 / 128	0.072
100	1 / 128	1.406	121 / 128	0.075
150	0 / 128	–	114 / 128	0.078
200	0 / 128	–	113 / 128	0.135
250	0 / 128	–	94 / 128	0.090
500	0 / 128	–	107 / 128	0.264
700	0 / 128	–	115 / 128	1.071
900	0 / 128	–	38 / 128	2.789
1000	0 / 128	–	0 / 128	–

# Dynamic experiment with failures

24 weeks; Bimodal failure probability; #altruists = 0.1 \* #pairs

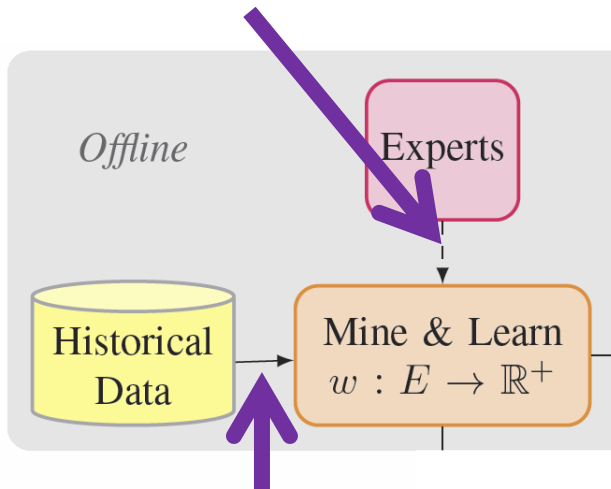




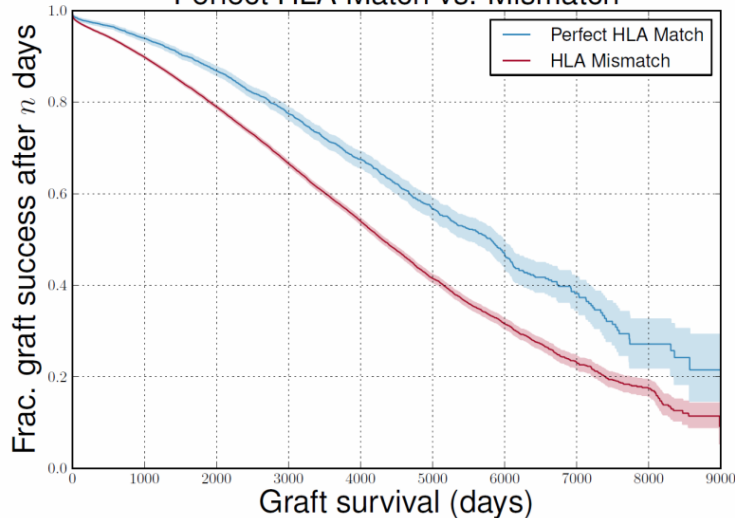
# **FutureMatch:** Combining human value judgments, ML, and integer programming for automatically generating the best policy for large-scale dynamic problems

[Dickerson & S., AAI-15]

Experiments with 3 objectives: max-graft-survival, max-cardinality, max- $\beta$ -weighted-cardinality



Perfect HLA Match vs. Mismatch



E.g., for  $\beta=2$ , improves over myopic in both #transplants and #sensitized transplants

# Preference elicitation from multiple experts

- To extract the value system from the multiple expert stakeholders, I designed a careful questionnaire with questions comparing small-case solutions
- Experts are reluctant to answer, and even ask

# Edge testing

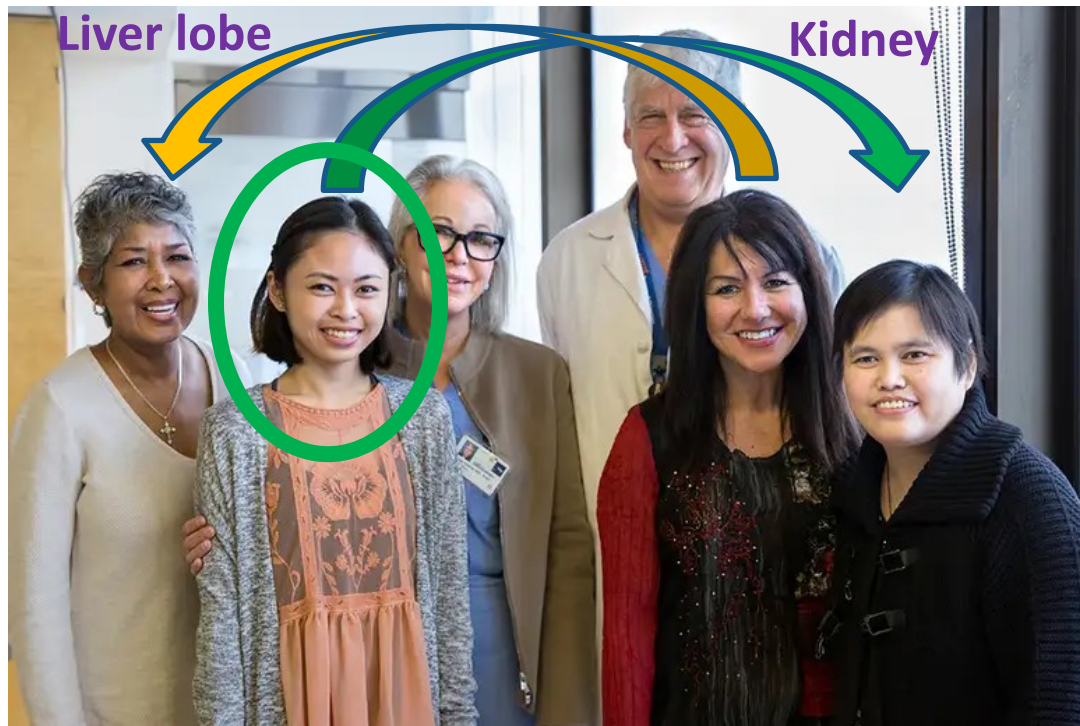
- Algorithms for better edge testing policies
  - Blum, Dickerson, Haghtalab, Procaccia & Sandholm  
EC-15, Operations Research 2019
  - McElfresh, Curry, Sandholm & Dickerson  
NeurIPS-20
- Ongoing pilot with UNOS for prioritizing queries in UNOS's donor pre-select tool

# Transplant centers hide pairs and NDDs from exchange(s)

- Why do centers do this?
  - Logistical benefit
  - Money
- What fraction of locally matchable pairs/NDDs do centers hide?
  - A: 100% [Stewart, Leishman, Sleeman, Monstello, Lunsford, Maghirang, Sandholm, Gentry, Formica, Friedewald, Andreoni. 2013. American Transplant Congress]
- No mechanism design solution possible in static setting  
[Roth, Sönmez, Ünver (2007a); Ashlagi, Fischer, Kash, Procaccia, GEB-13; Ashlagi & Roth (2014)]
- Incentive-compatible, efficient, long-term-IR credit mechanism  
[Hajaj, Dickerson, Hassidim, Sandholm, Sarne, AAI-15]
  - Matching favors centers that reveal more than their expected number of pairs/NDDs, and disfavors those who reveal fewer than that
  - Supports chains and long cycles
  - Assumes pairs and NDDs last for only one matching period

# Liver lobe and cross-organ exchanges

- Invented liver lobe and cross-organ exchange [Sandholm, UMass DLS-10]
- Merging kidney and liver lobe exchanges produces a large benefit in theory and simulation [Dickerson & Sandholm, JAIR-17]
- Fielding has started in the small, with manual matching, as it started with kidneys
  - A few liver lobe swaps per year in the US
  - First liver lobe - kidney swap took place in 2019



# Our ongoing research on organ exchange

- Better algorithms that handle the dynamic problem with arrivals & departures
- Better edge testing policies
- Matching cadence: Race to bottom among exchanges [Das, Dickerson, Li, Sandholm, AMMA-15]
  - Why allow multiple kidney exchanges in a country?
- Better incentive schemes for transplant centers to reveal pairs
- Multi-donor kidney exchange
  - Current practice allows multiple donors listed, only one used
  - Our new approaches allow multiple donors to be used in various ways [Sandholm, Farina, Dickerson, Leishman, Stewart, Formica, Thiessen, Kulkarni ATC-17; Farina, Dickerson, Sandholm IJCAI-17, AGT-17]
- “Operation frames” [Farina, Dickerson, Sandholm IJCAI-17, AGT-17]
- Other organs
  - Liver & cross-organ exchange [Dickerson & Sandholm, GREEN-COPLAS-13, AAAI-14, JAIR-17]
  - Lung “components” [Ergin, Sönmez, Ünver, draft 2014-15; Tang et al. 2015]
- International exchanges

# Some more of my future research on organ donation

