

# Coded Computational Imaging: Light Fields and Applications

Ankit Mohan  
MIT Media Lab

# Schedule

Introduction	Srinivasa, 10 mins
Assorted Pixels	Srinivasa, 20 mins
Coding and Modulation in Cameras	Amit, 45 mins
Break	10 min
Light Fields and Applications	Ankit, 60 mins
Break	10 min
Computational Illumination	Srinivasa, 45 mins
Future Trends	Amit, 15 mins
Discussion	

# Light Field Basics

# The Plenoptic Function



Figure by Leonard McMillan

Q: What is the set of all things that we can ever see?

A: The Plenoptic Function [Adelson & Bergen]

Let's start with a stationary person and try to parameterize everything that she can see



# Grayscale Snapshot



$$P(\theta, \phi)$$

is intensity of light

- Seen from a single view point
- At a single time
- Averaged over the wavelengths of the visible spectrum

# Color Snapshot



Figure by Leonard McMillan

$$P(\theta, \phi, \lambda)$$

is intensity of light

- Seen from a single view point
- At a single time
- As a function of wavelength

# A Movie



Figure by Leonard McMillan

$$P(\theta, \phi, \lambda, t)$$

is intensity of light

- Seen from a single view point
- Over time
- As a function of wavelength



# A Holographic Movie

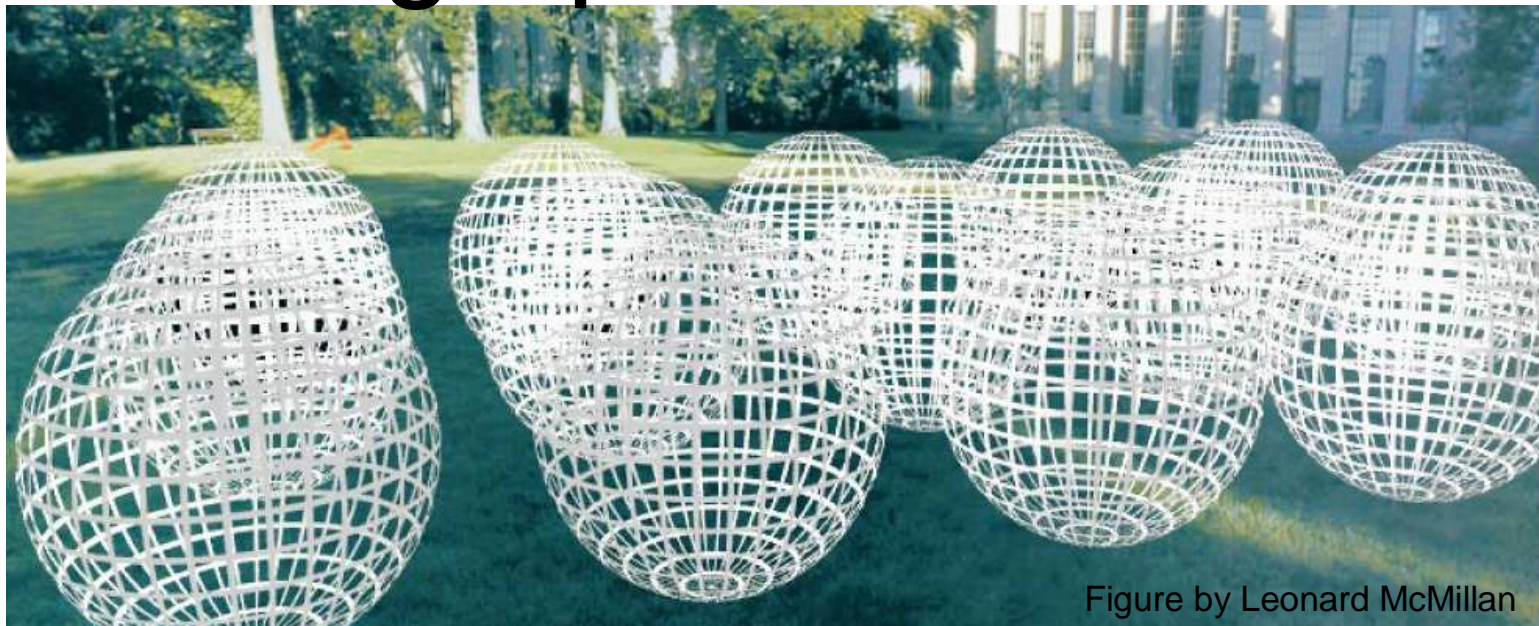


Figure by Leonard McMillan

$$P(\theta, \phi, \lambda, t, V_X, V_Y, V_Z)$$

is intensity of light

- seen from ANY viewpoint
- over time
- as a function of wavelength

# The Plenoptic Function

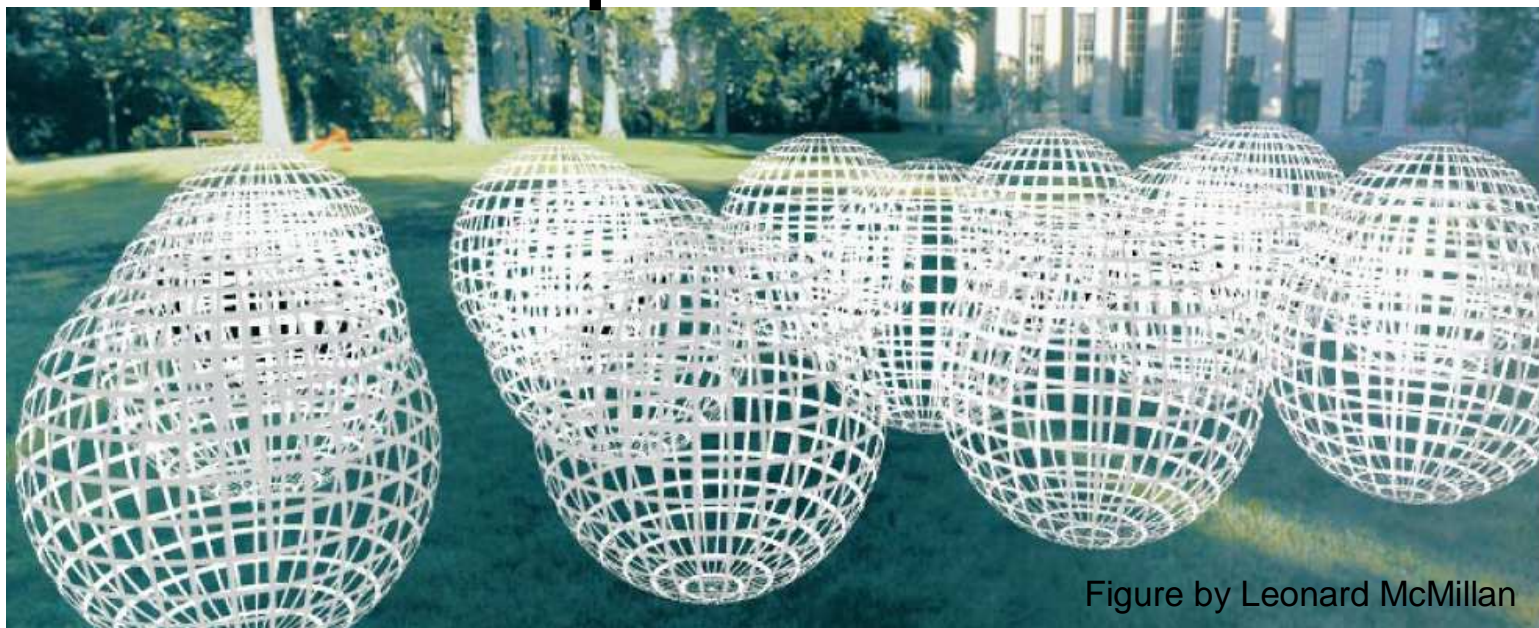


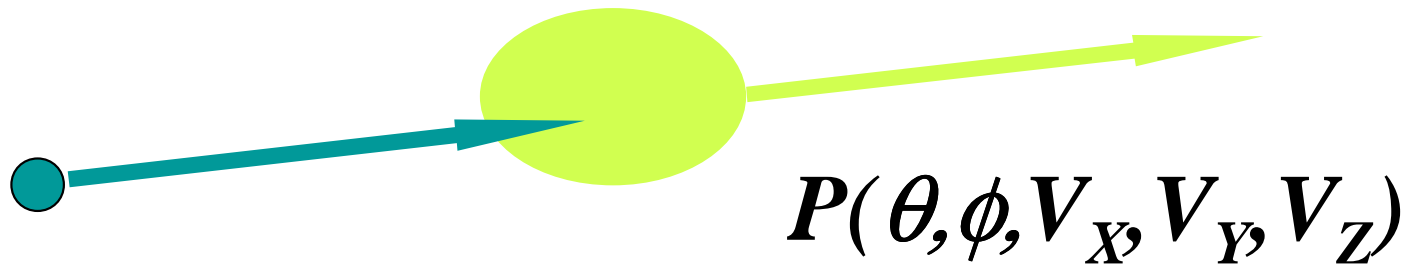
Figure by Leonard McMillan

$$P(\theta, \phi, \lambda, t, V_X, V_Y, V_Z)$$

Can reconstruct every possible view, at every moment, from every position, at every wavelength

# Ray of Light

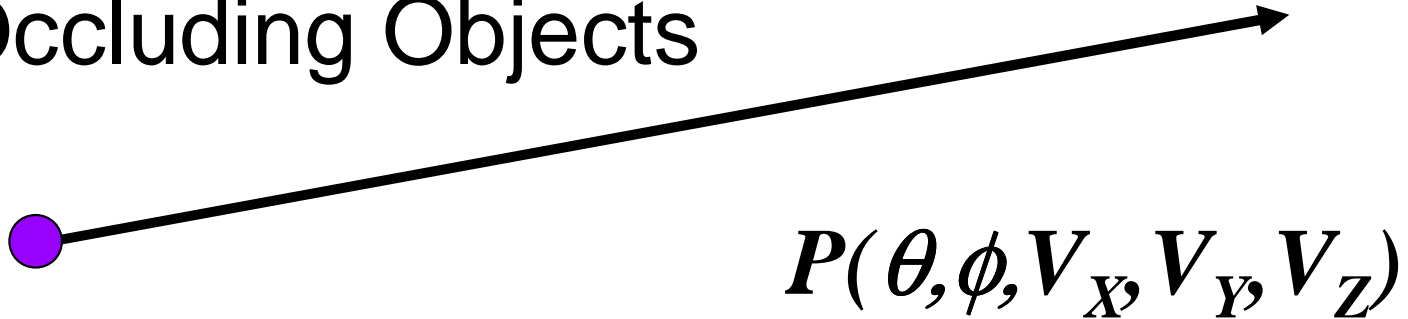
- Let's ignore time and color:



- 5D
  - 3D position
  - 2D direction

# Ray of Light in Free Space

- No Occluding Objects

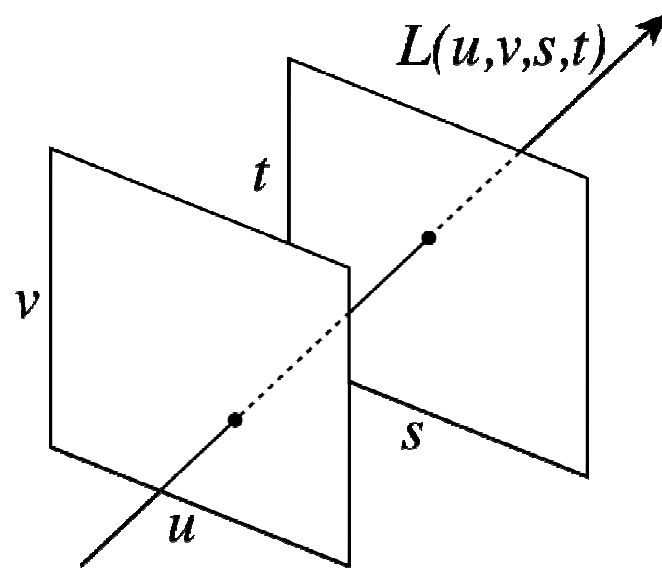


- 4D
  - 2D position
  - 2D direction

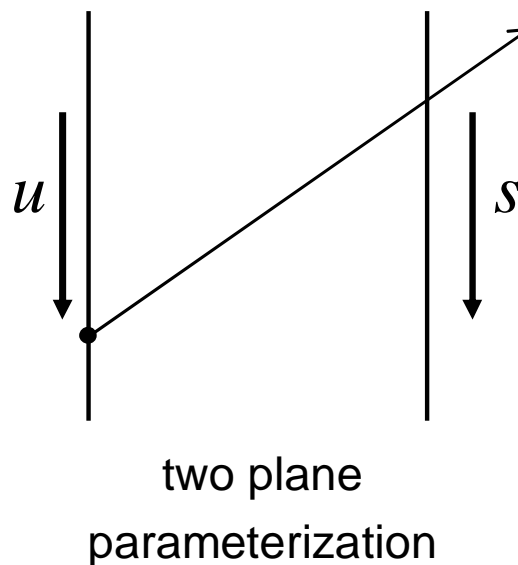
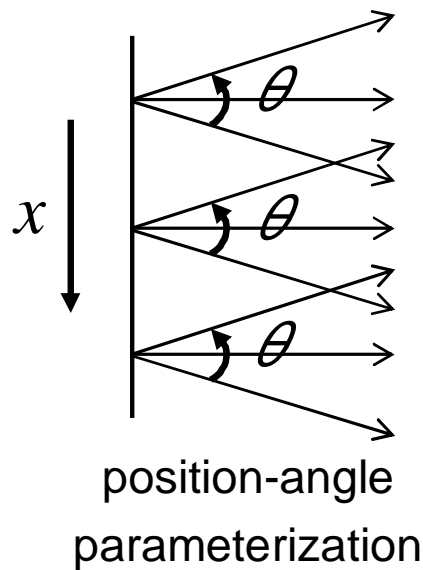
# Light Field [Levoy & Hanrahan 1996]

*Radiance as a function of position and direction*

- 4D in 3D free space ( $u, v, s, t$ )

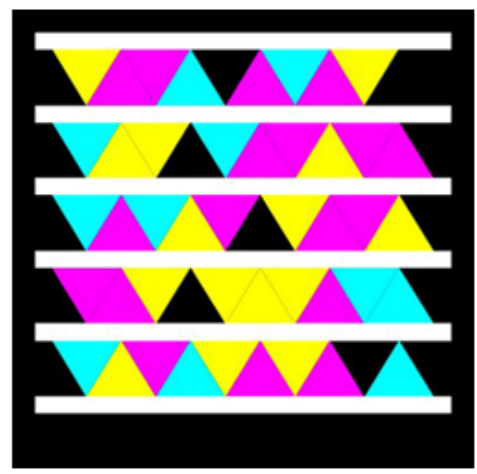


- 2D in flatland ( $u, v, s, t$ )





# Light Field Generation





# visible light barcodes

space



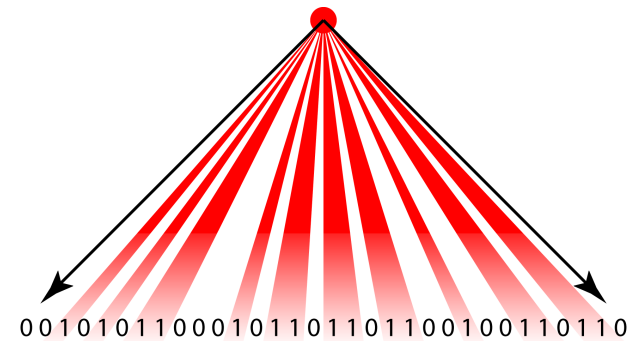
[UPC Code, QR Code, Data Matrix Code, Shot Code, Microsoft Tag, ...]

time



[IR remote, Sony ID CAM]

angle

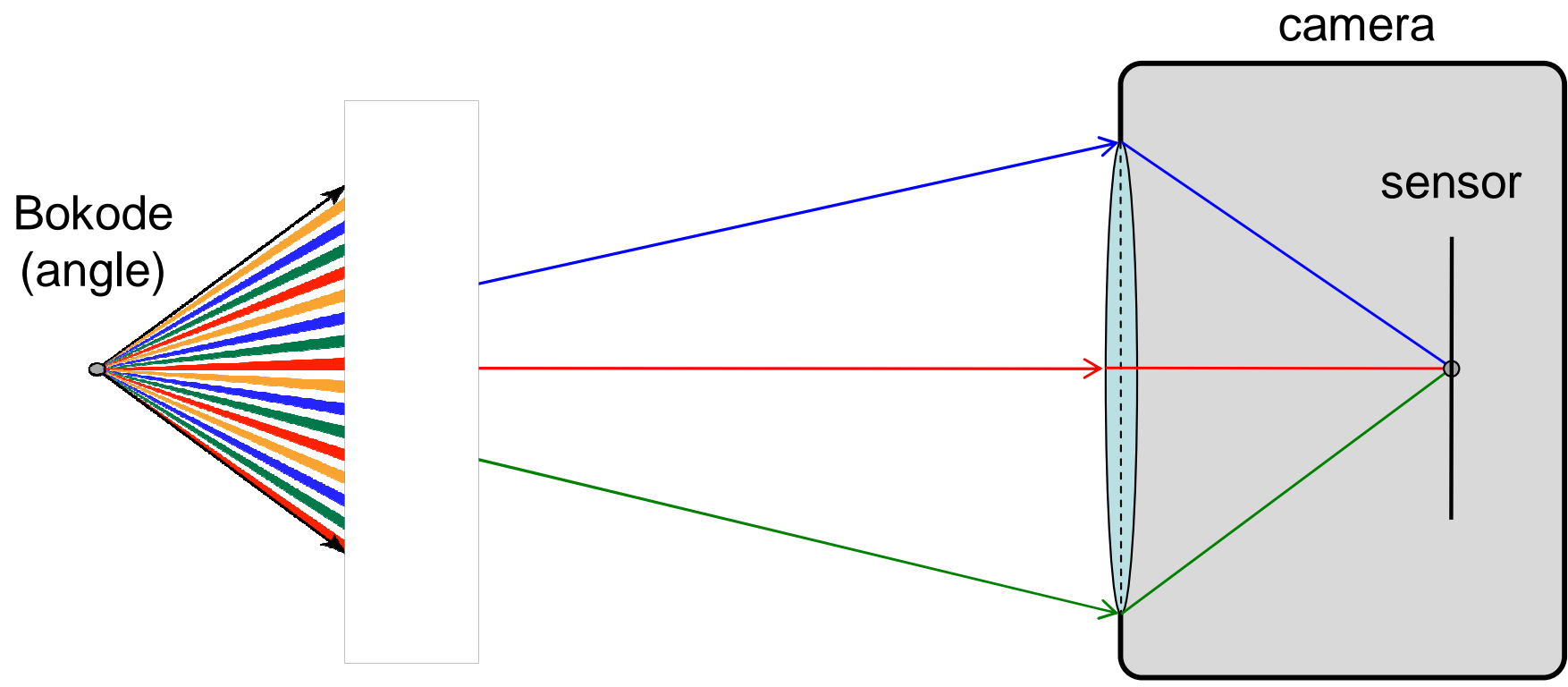


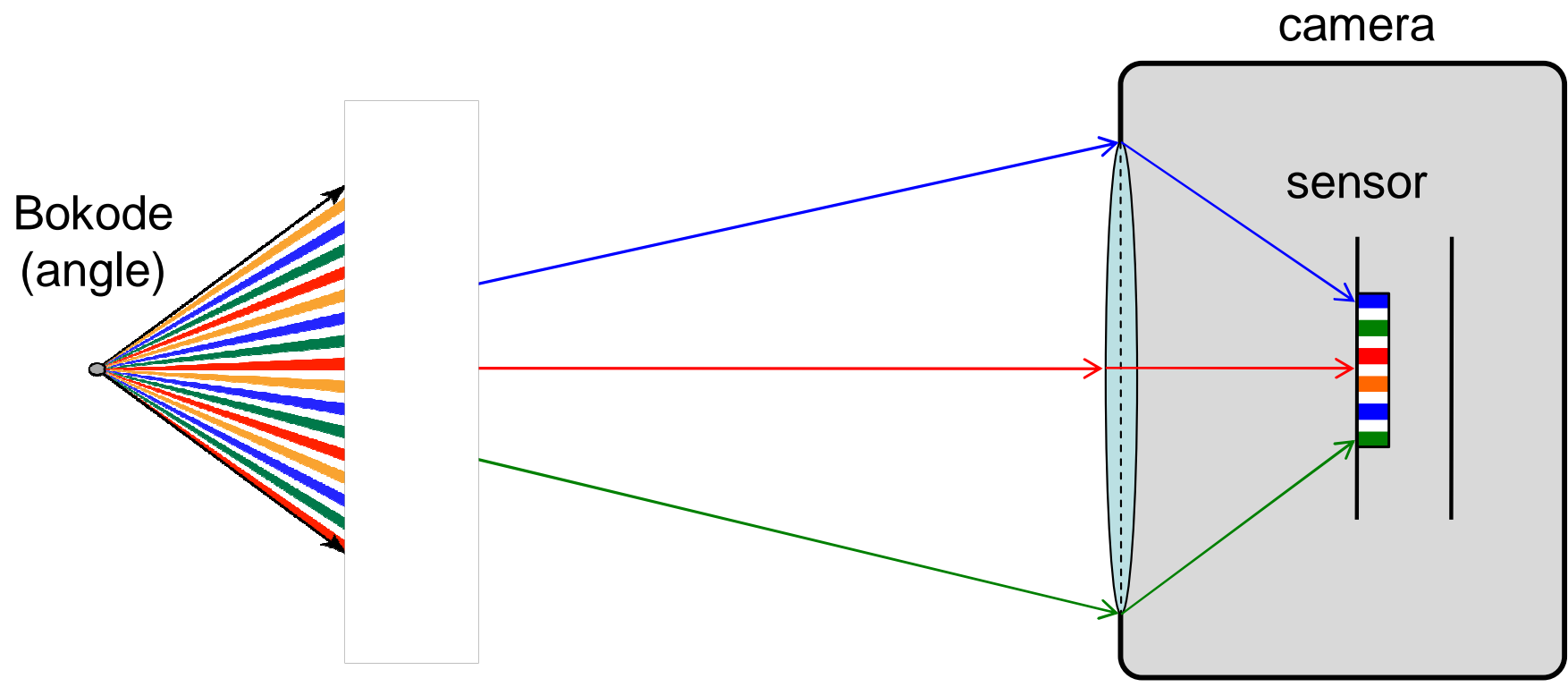
+

standard camera  
focused at infinity

**Bokode**

*“Bokode: Imperceptible Visual Tags for Camera Based Interaction from a Distance”*, Ankit Mohan, Grace Woo, Shinsaku Hiura, Quinn Smithwick and Ramesh Raskar, in **SIGGRAPH 2009**.

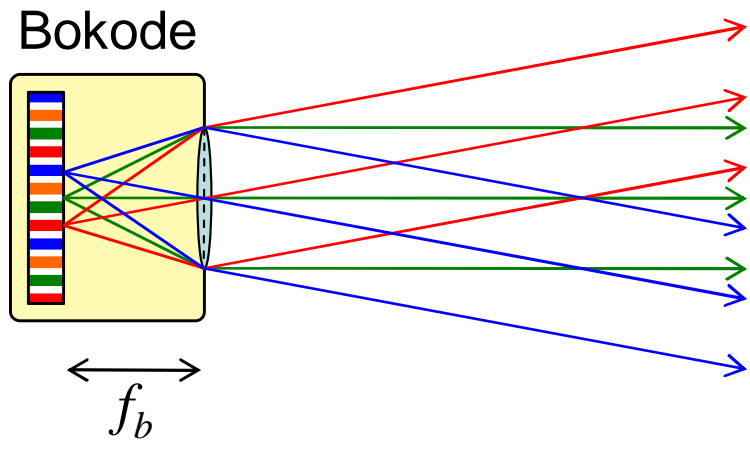




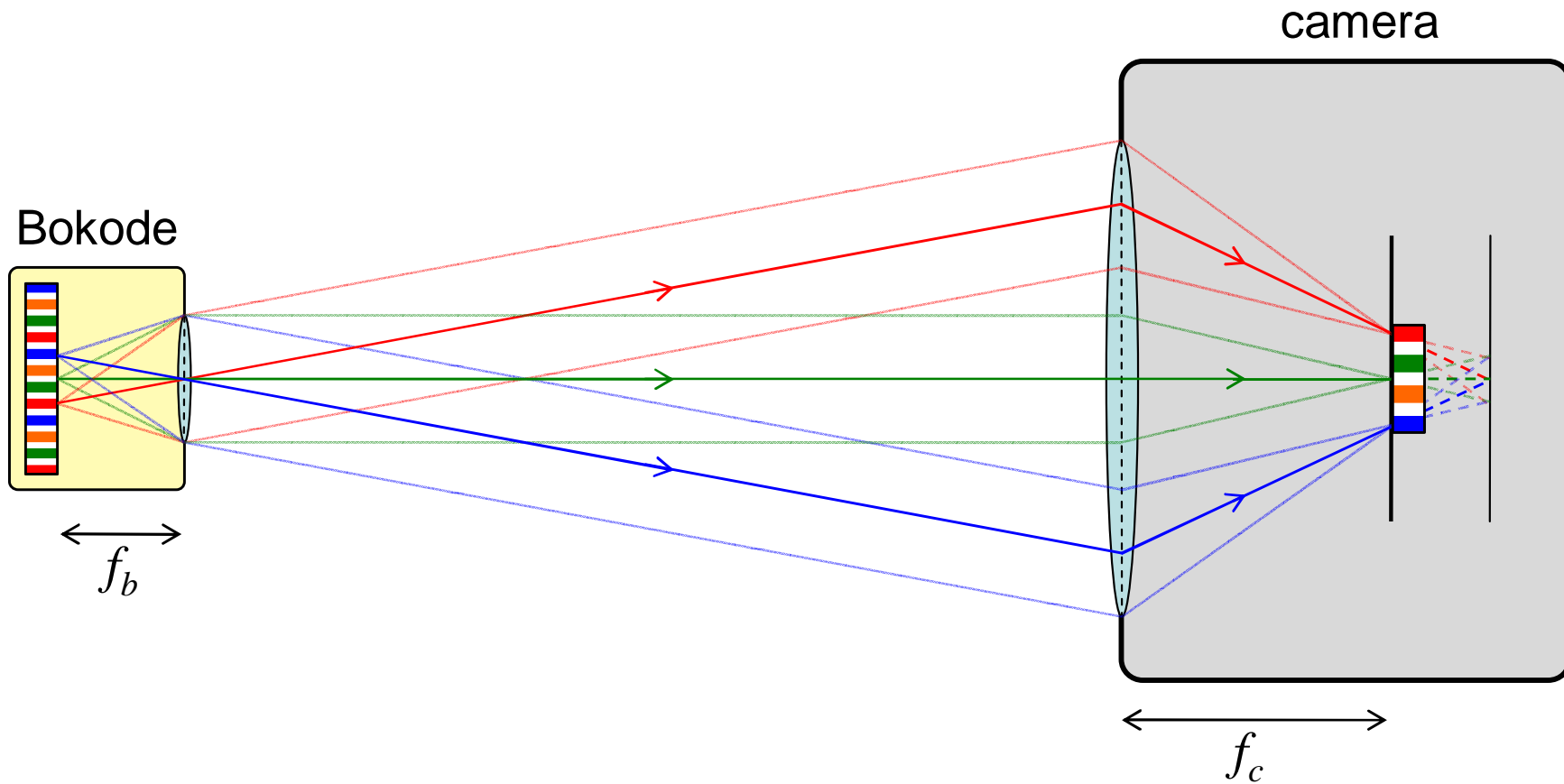
“ahh... circle of confusion → circle of information”

- Kurt Akeley

# generate directionally encoded information

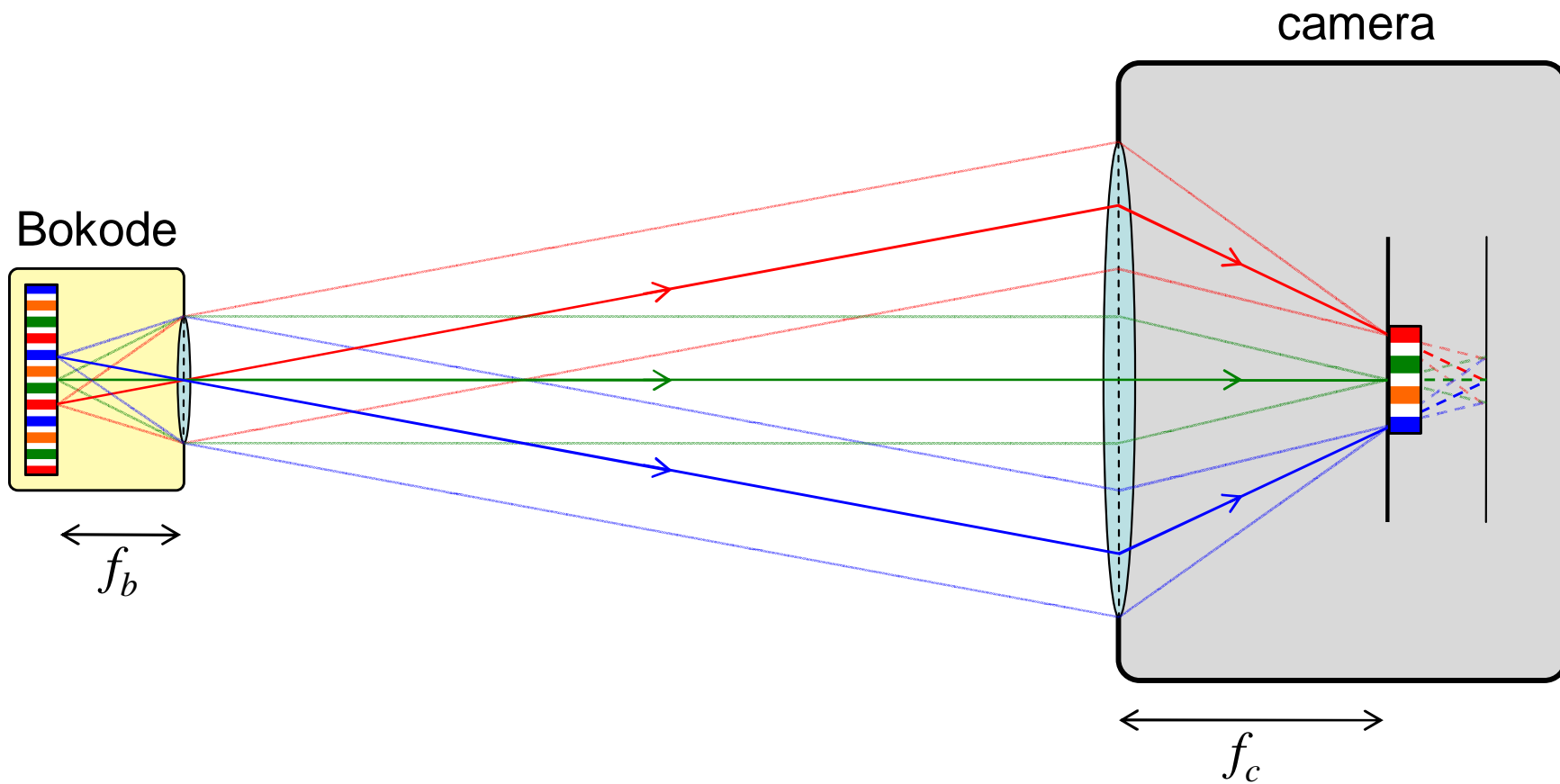


# capture directionally encoded information

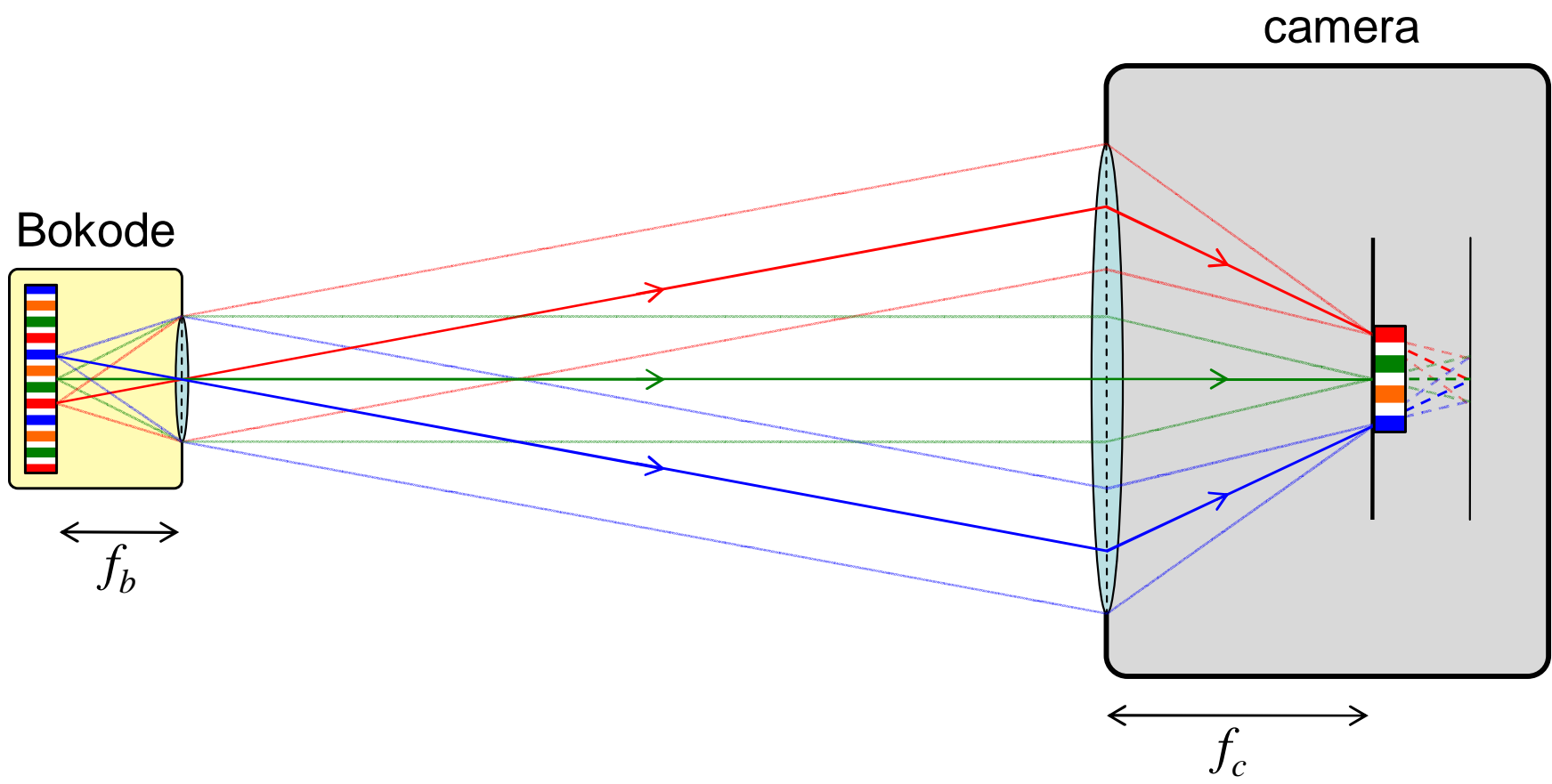
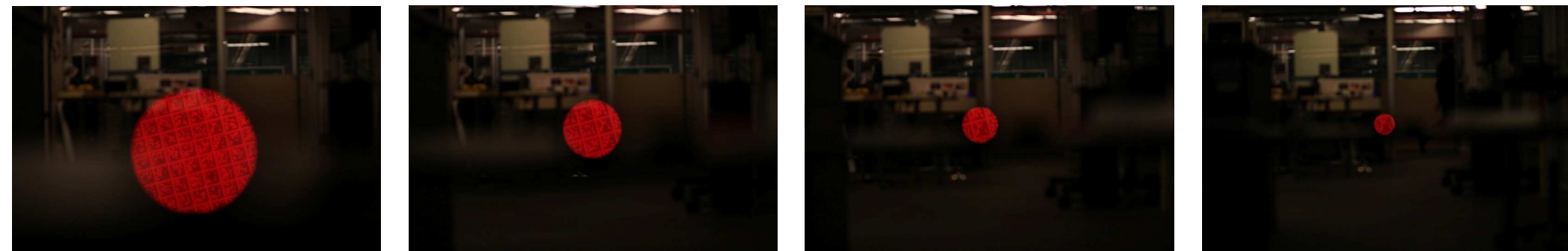




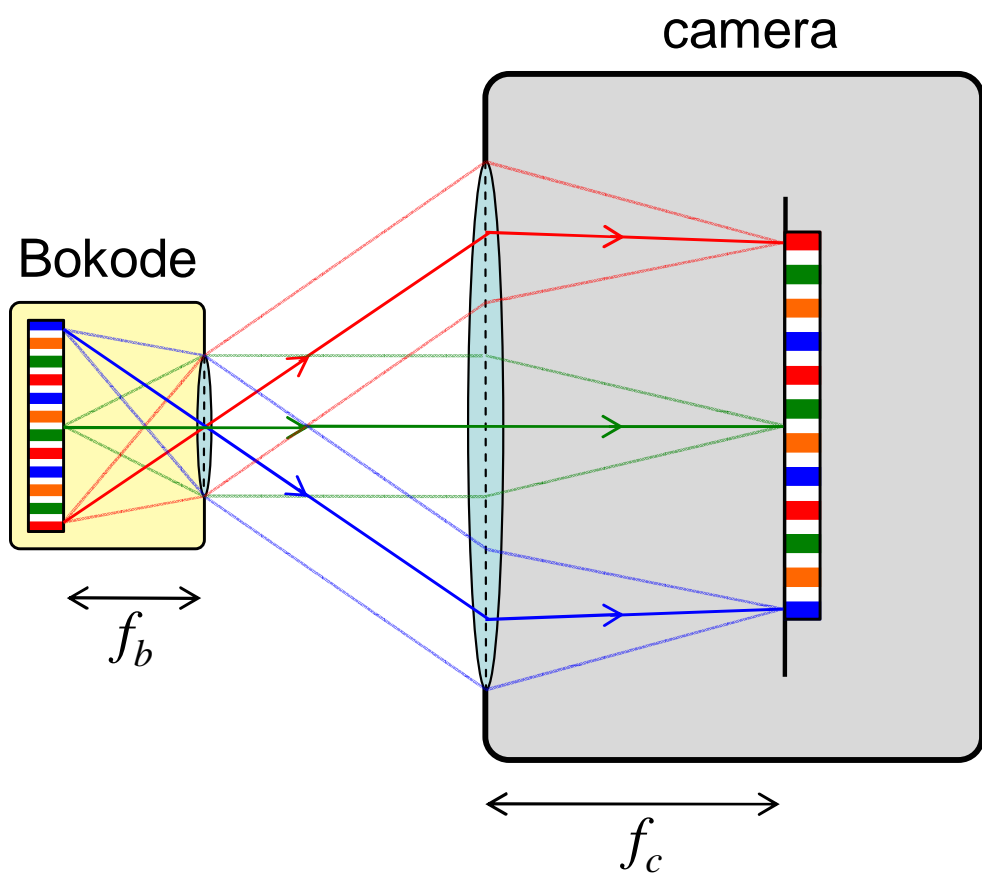
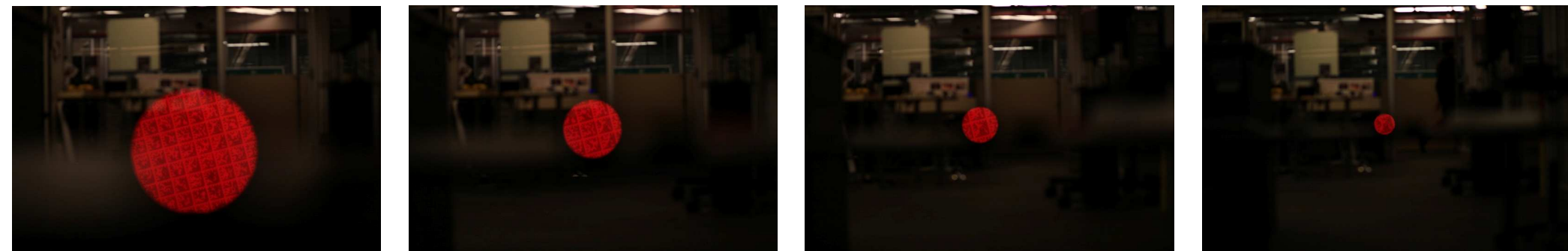
# infinity-corrected microscope



magnification =  $f_c/f_b$  (microscope);  
focus always at infinity

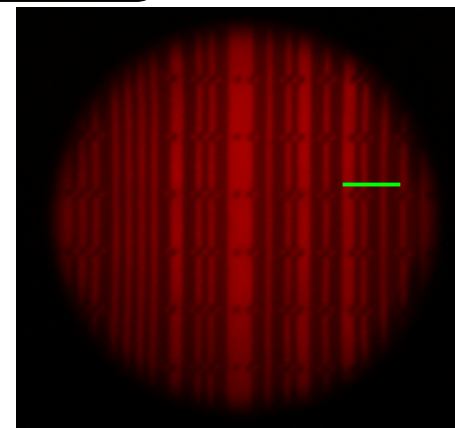
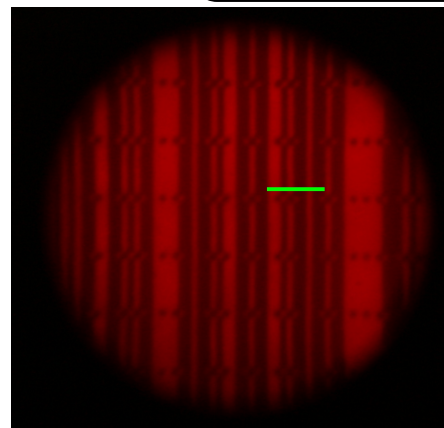
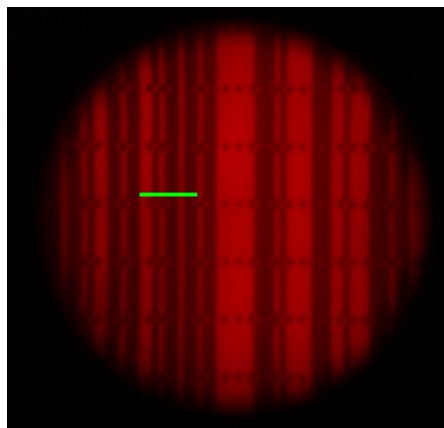
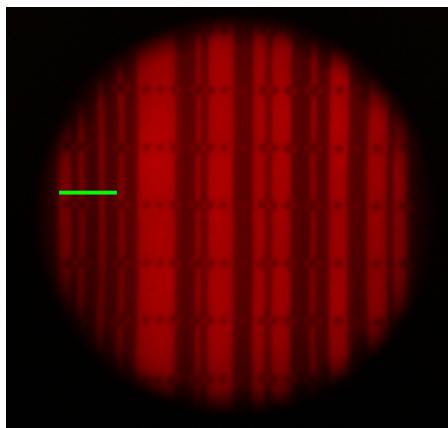
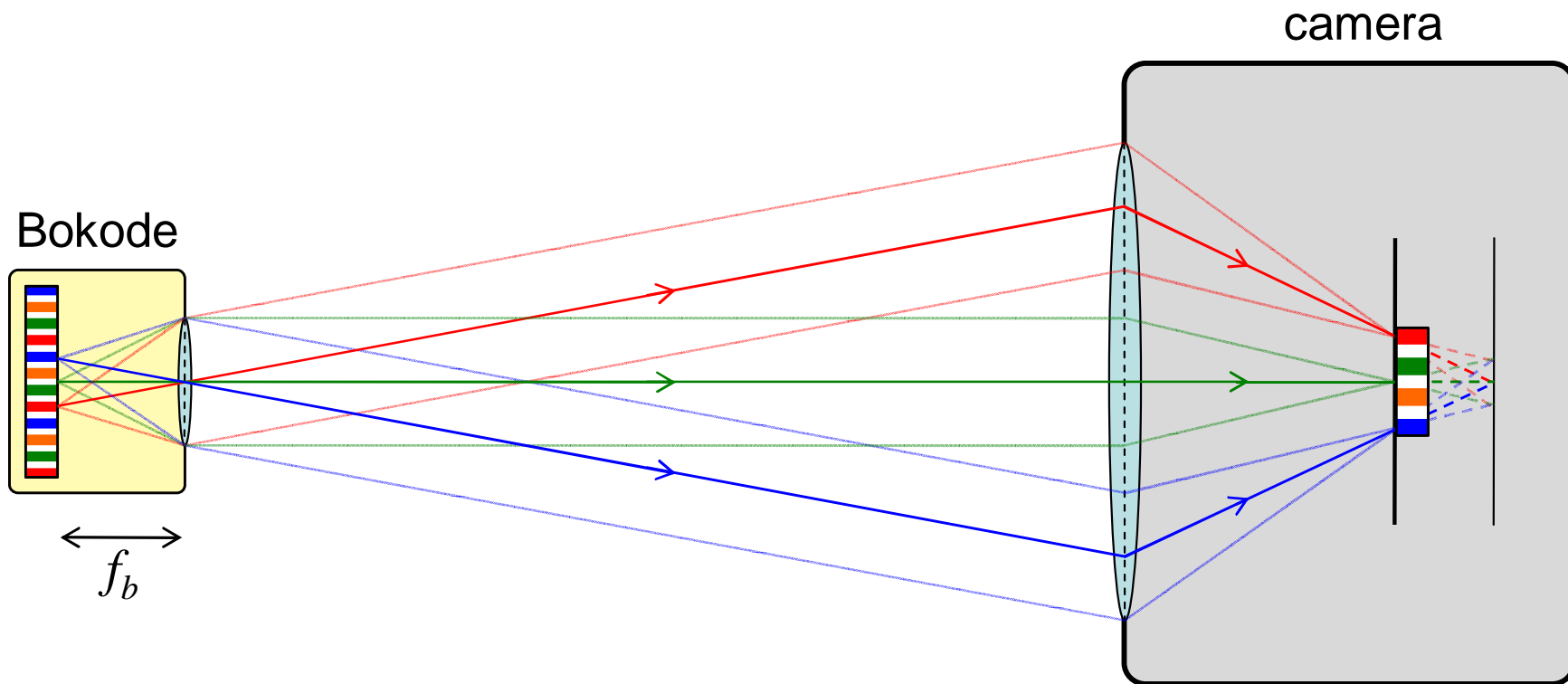


less distance  $\rightarrow$  more of Bokode imaged

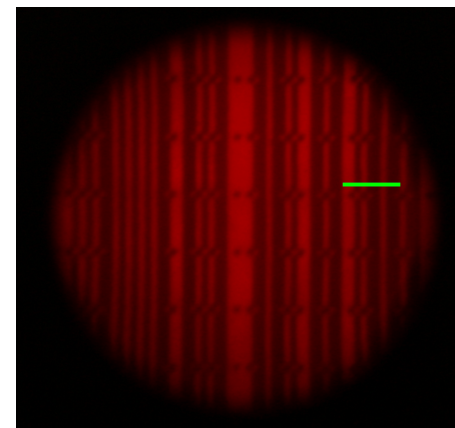
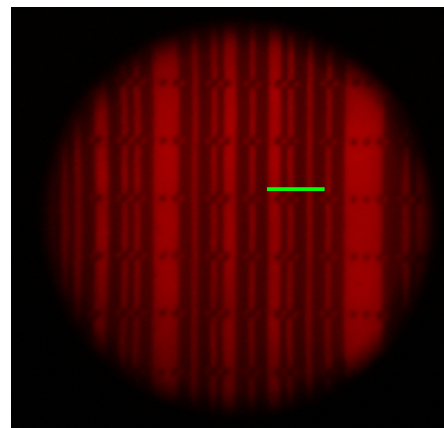
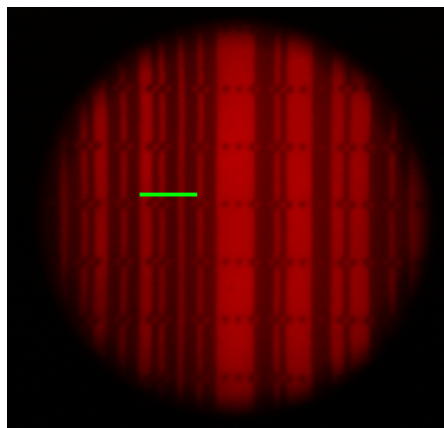
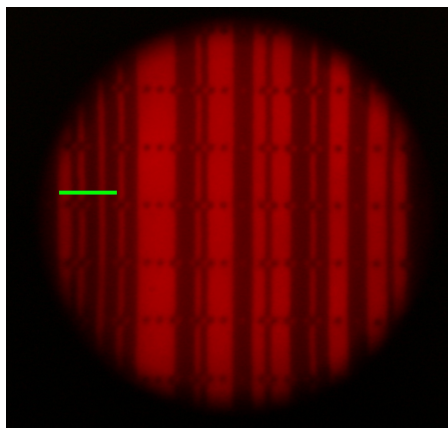
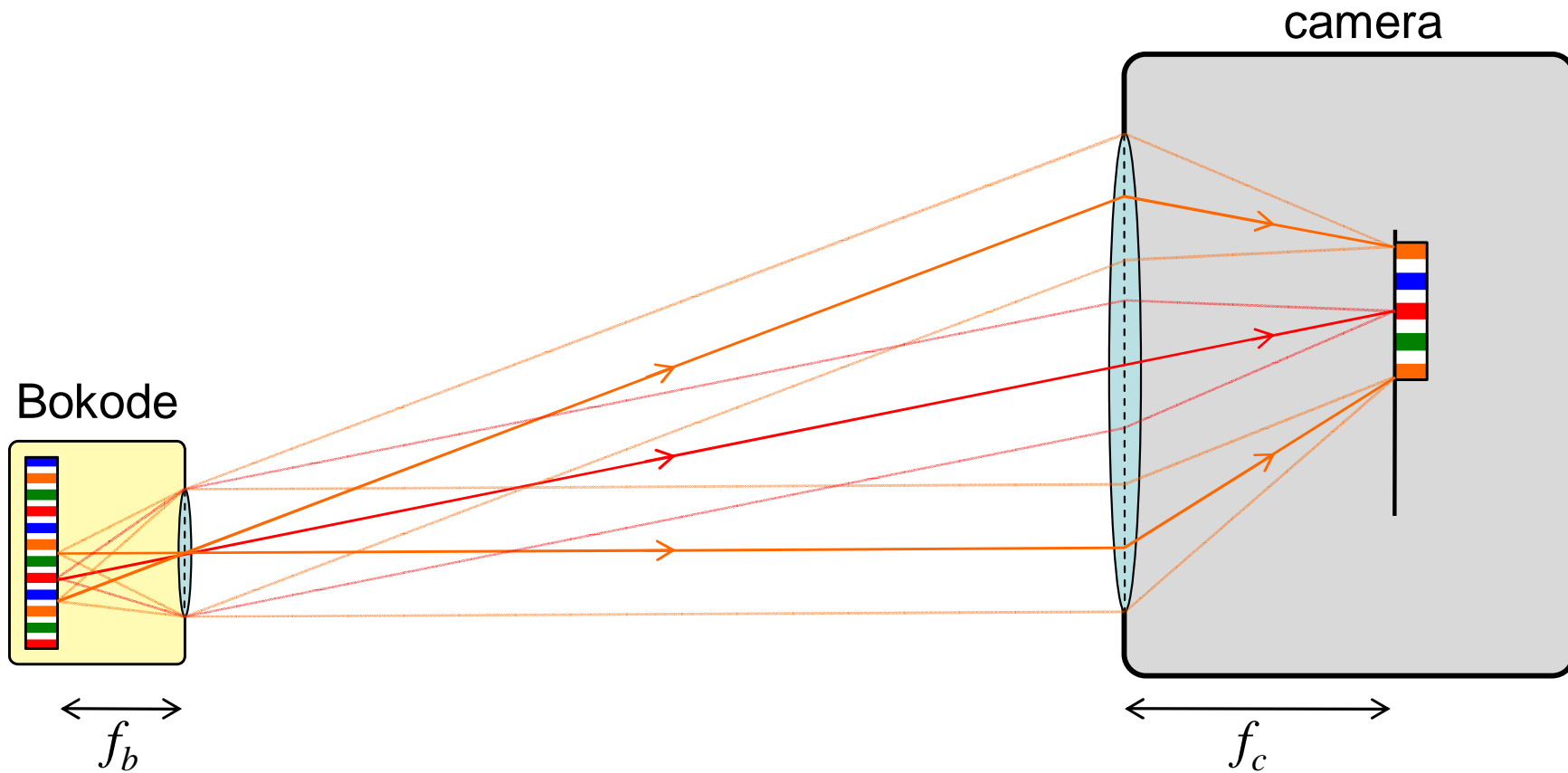


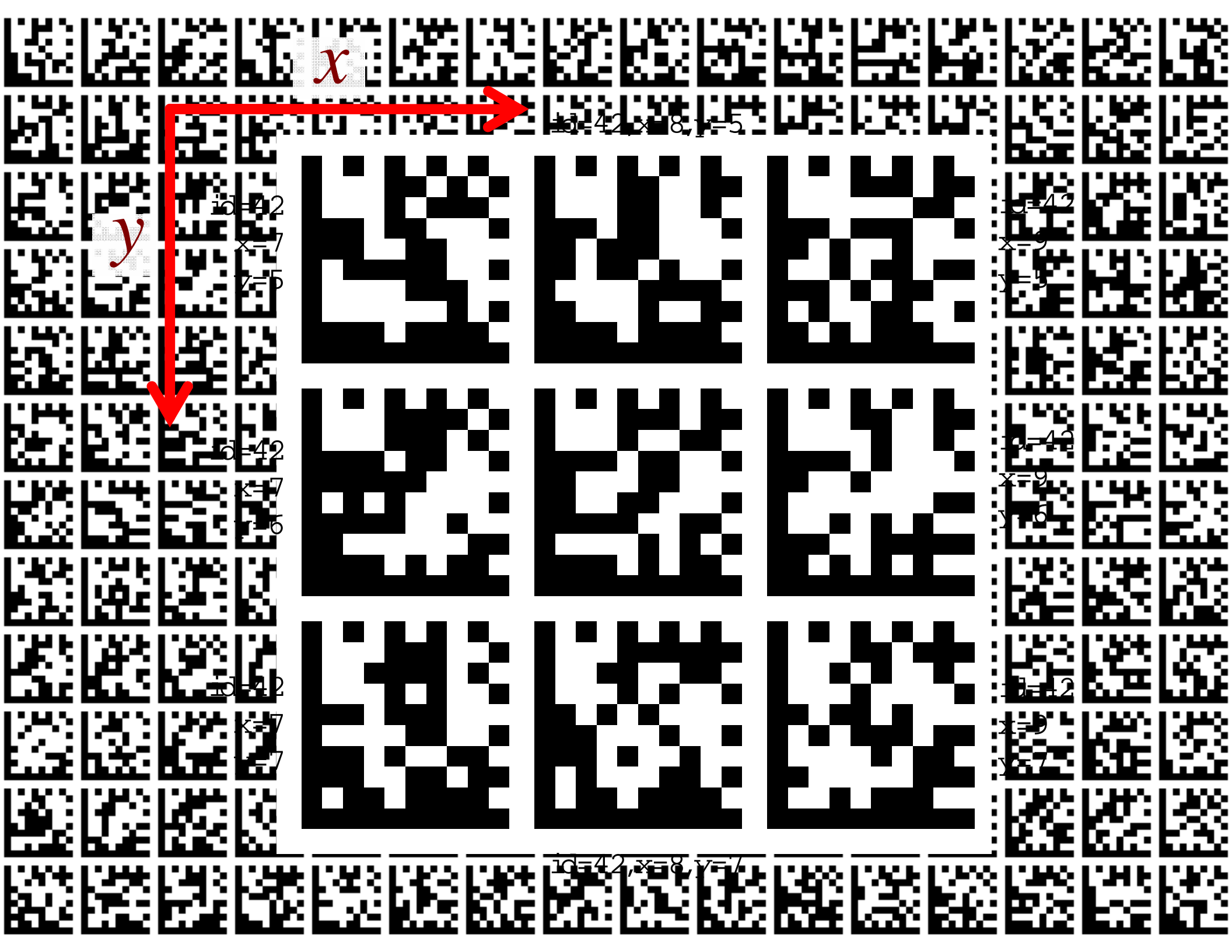
less distance  $\rightarrow$  more of Bokode imaged

# Bokode image depends on camera angle



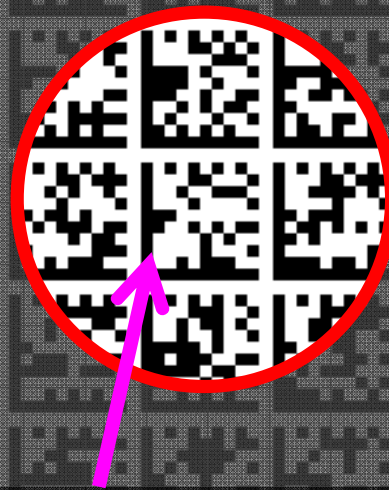
# Bokode image depends on camera angle





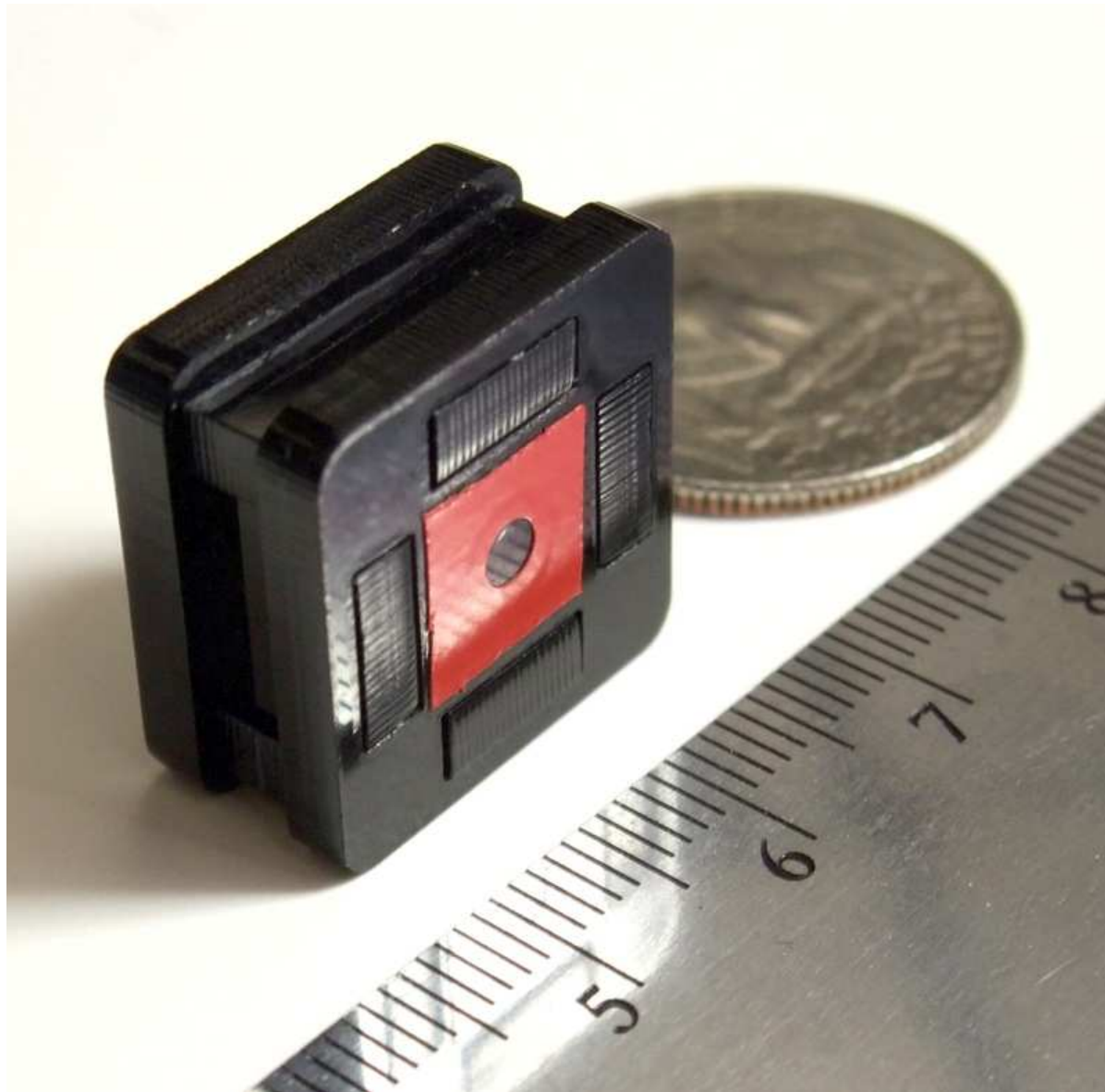


# *digital angle* from Bokode



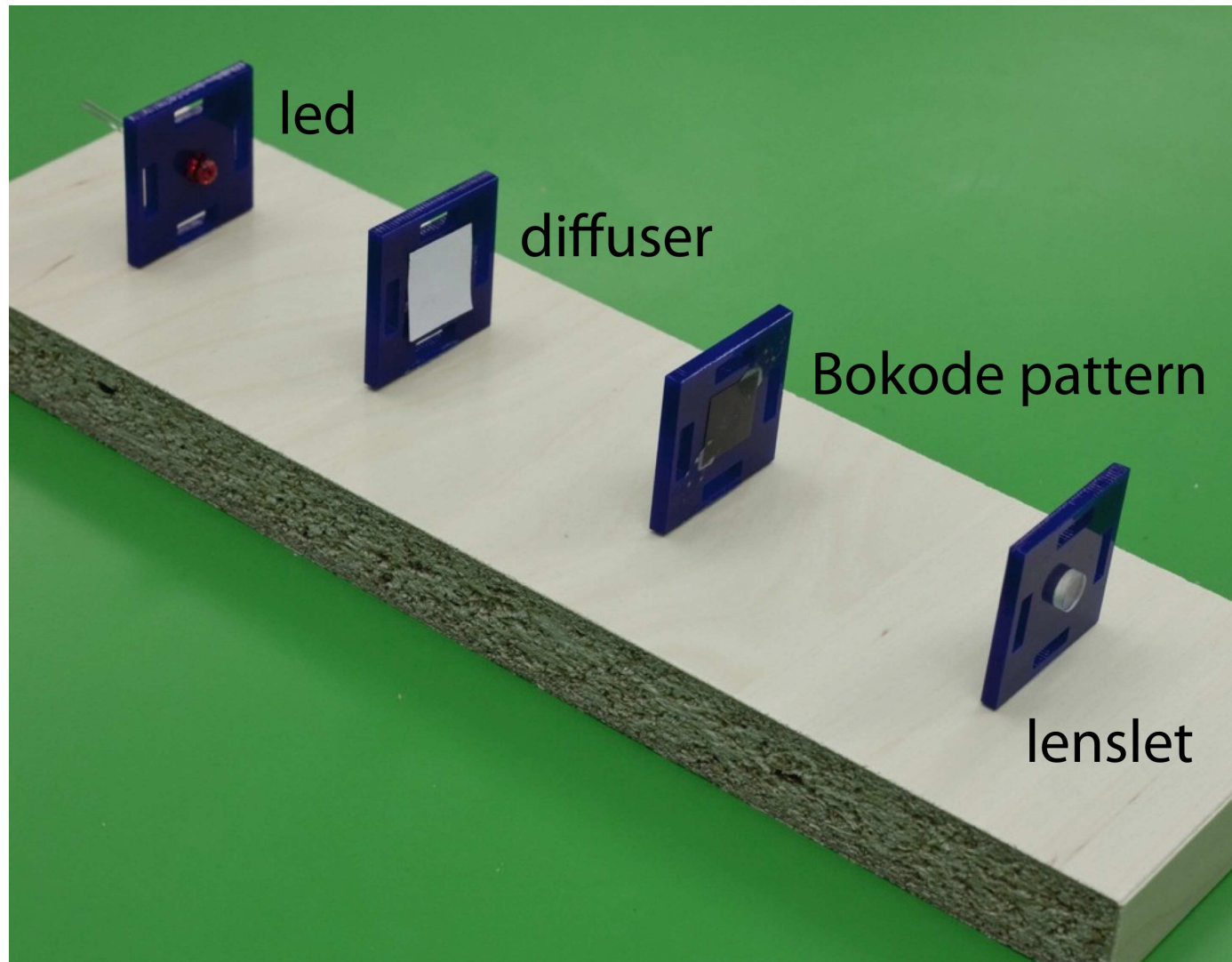
id = (42, 10, 7)

# prototype – assembled





# prototype – exploded



**led:** 120° view angle, 1350mcd

**pattern:** 15 $\mu$ m resolution

**lenslet:**  $f=8\text{mm}$ ,  $\Phi=3\text{mm}$

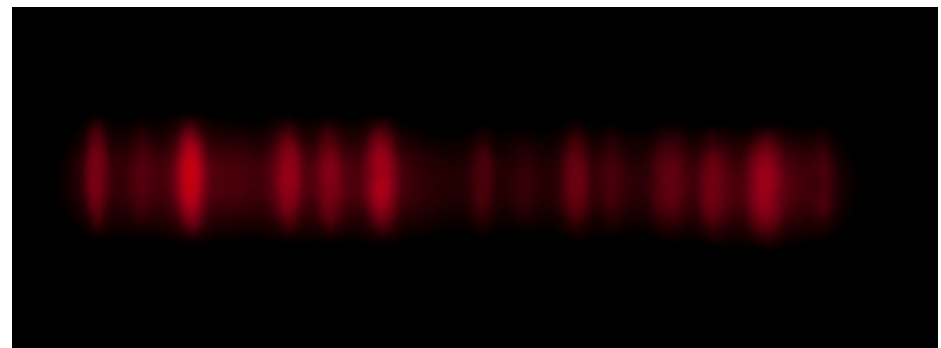
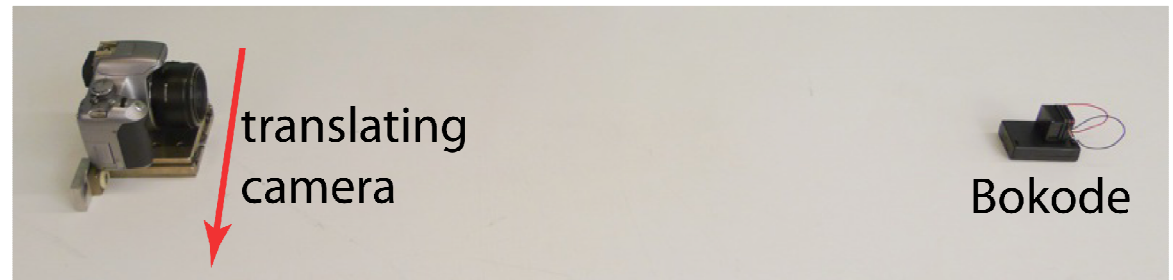
**cost:** ~\$5

# capturing Bokodes

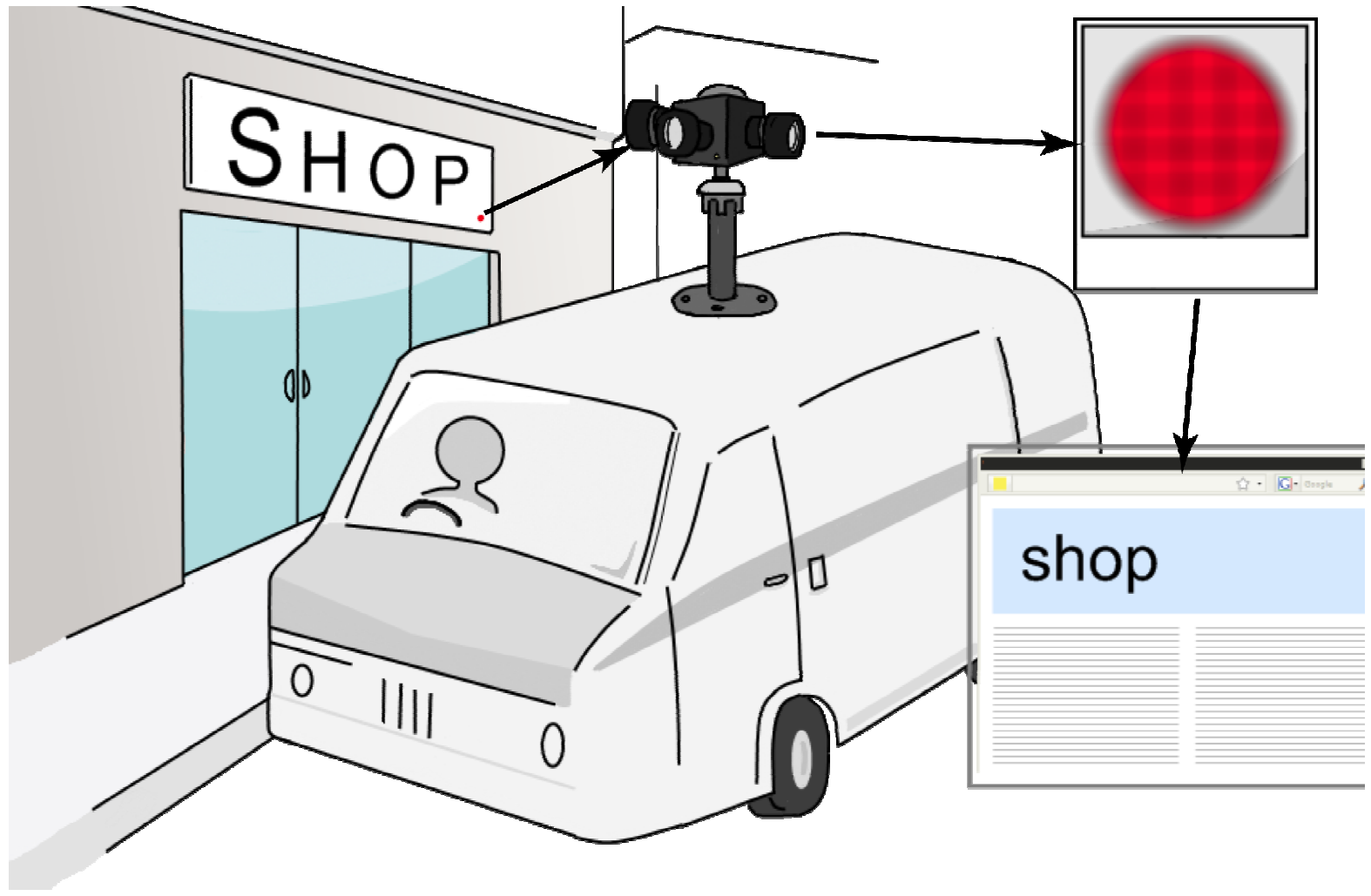
focus blur  
(85mm f/1.8;  
infinity focus)



motion blur  
(50mm f/8;  
~2cm motion)

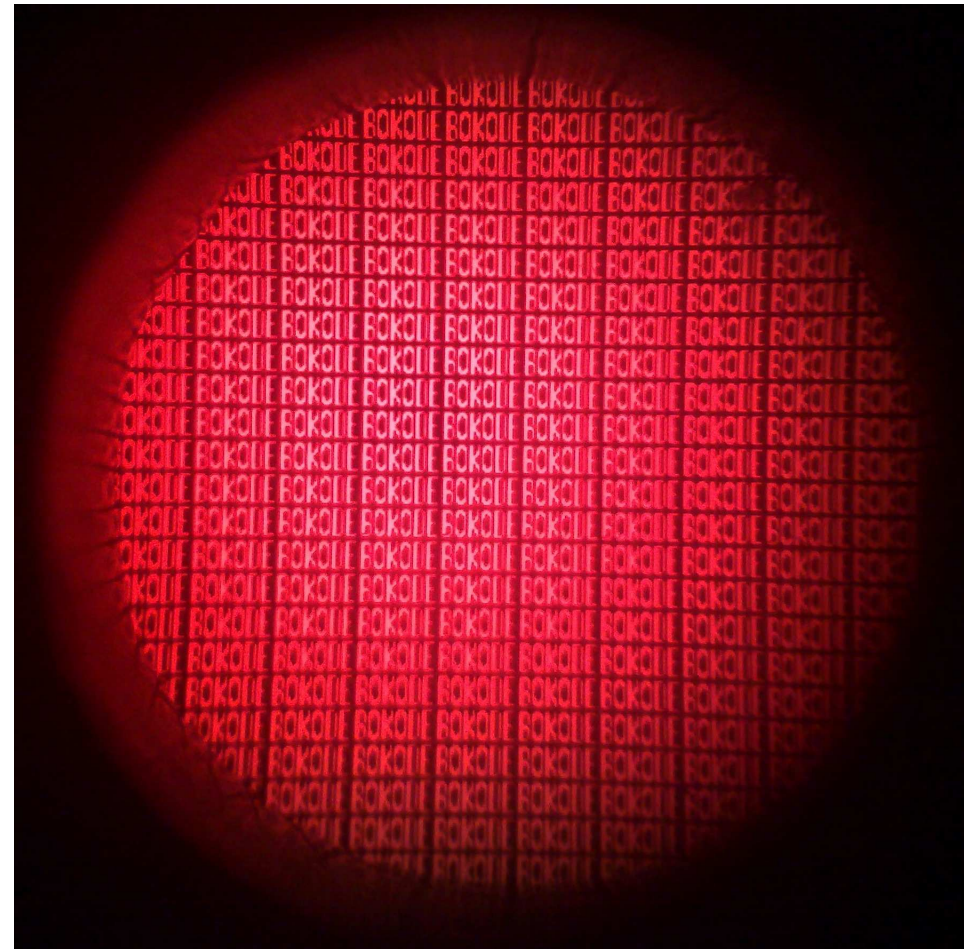


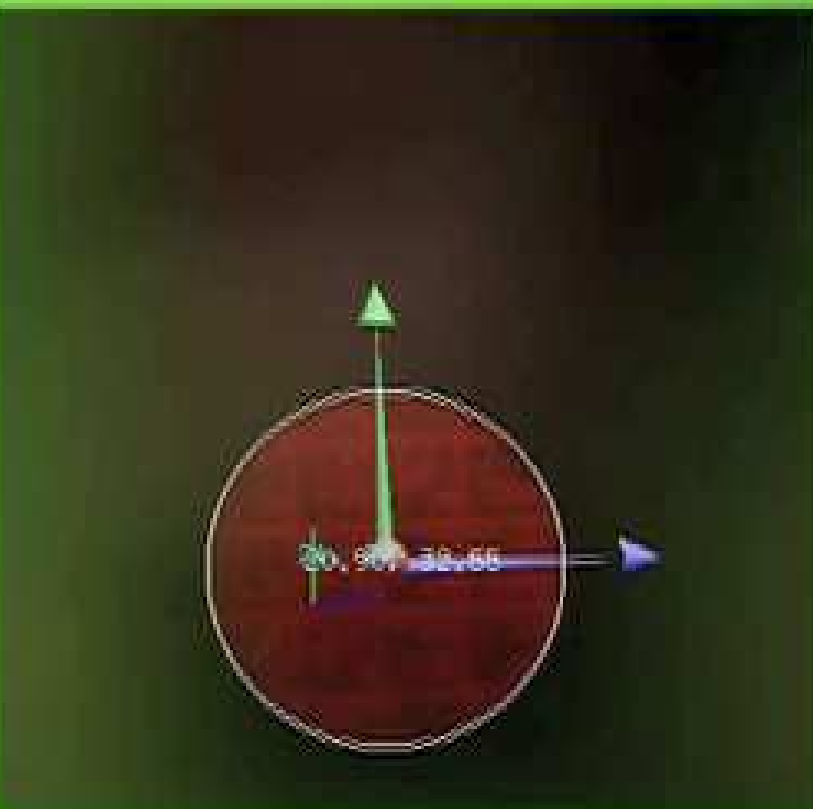
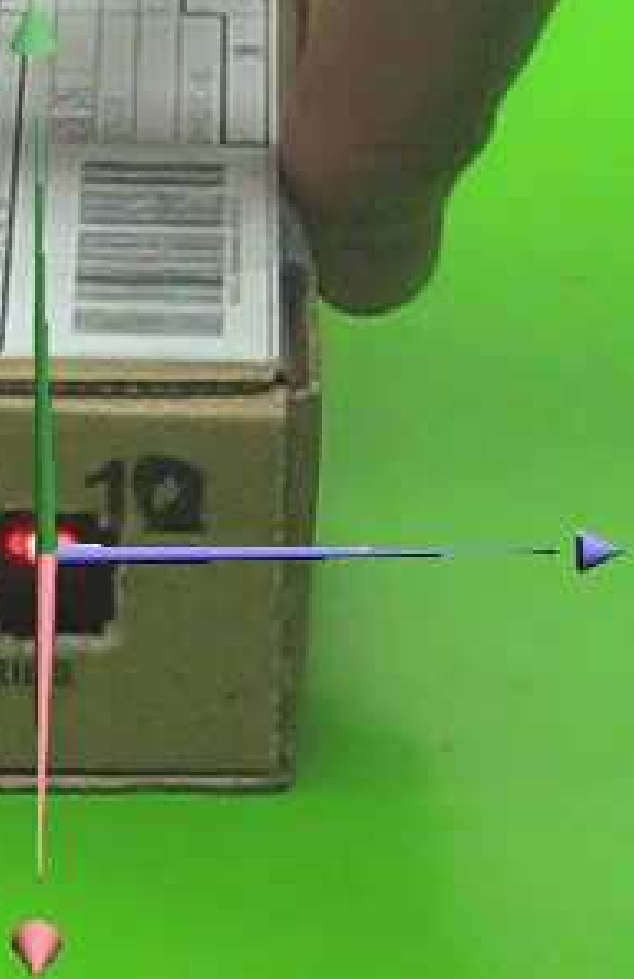
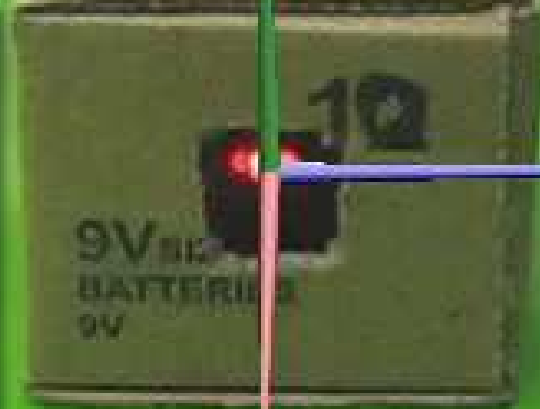
# street-view tagging



# capturing Bokodes

cell-phone camera  
close to the Bokode  
(10,000+ bytes of data)







# traditional AR markers



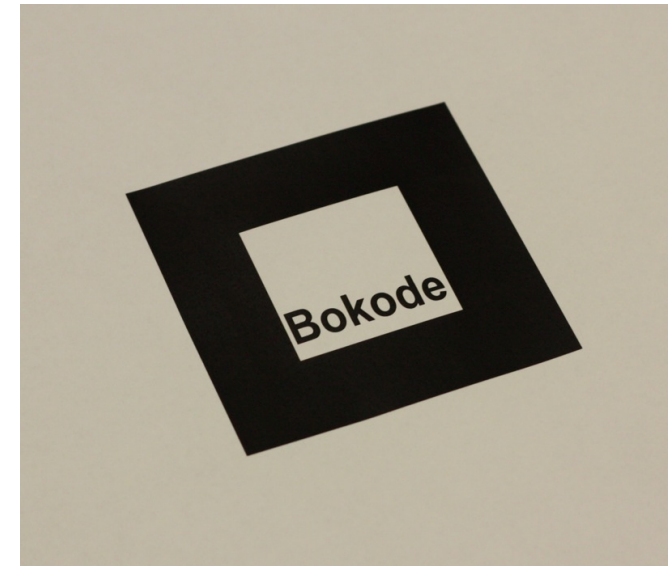
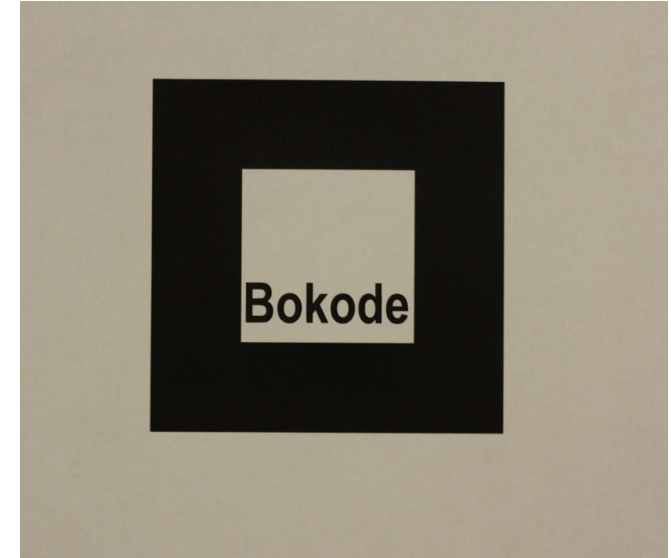
## ARToolKit

[Kato and Billinghurst 1999]



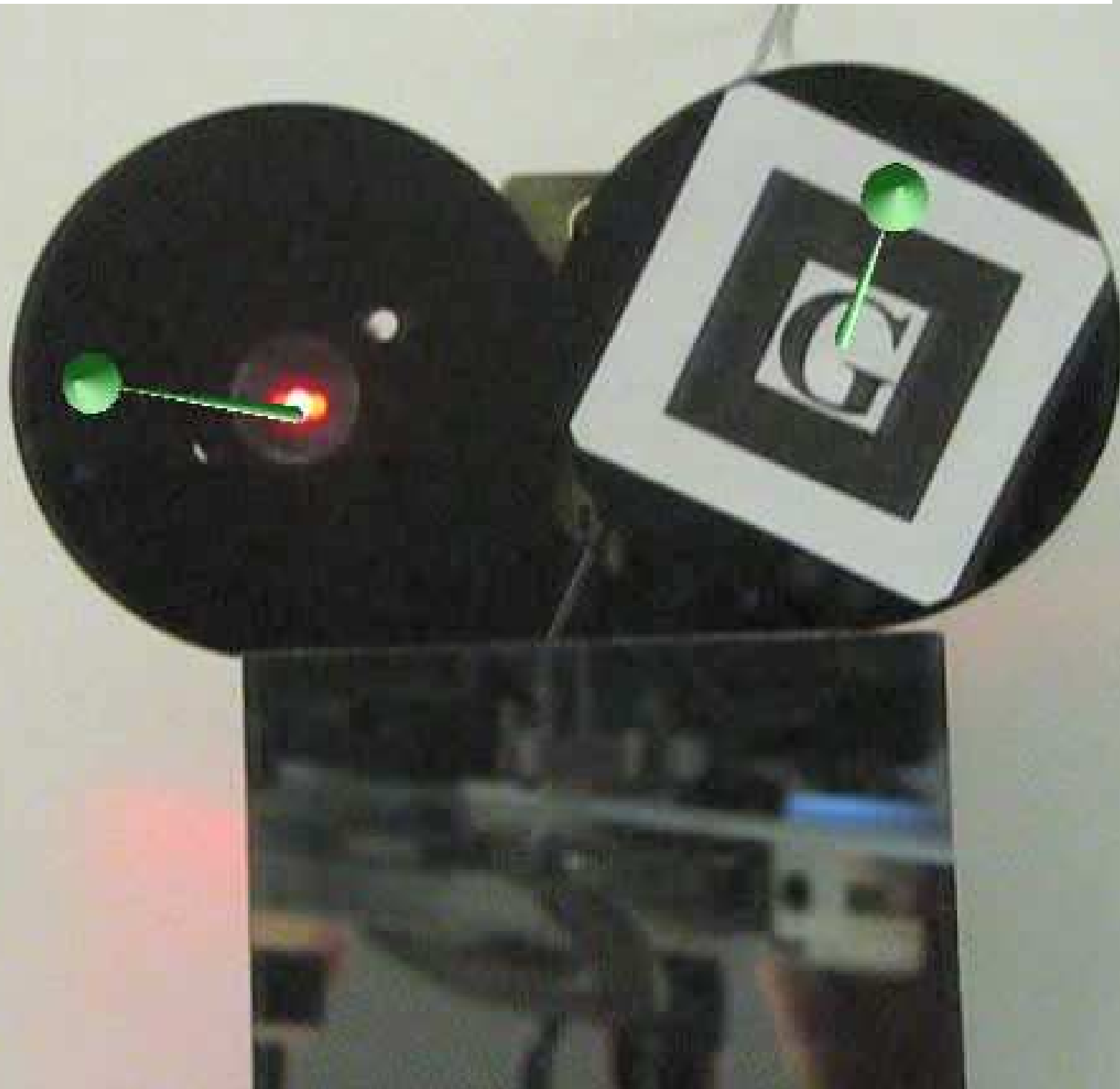
## ARTag

[Fiala 2005]



skew of marker

# angle estimation robustness





# wide field of view Bokode via Krill eye

compound superposition optics

*“Krill-eye: Superposition Compound Eye for Wide-Angle Imaging via GRIN Lenses”*, Shinsaku Hiura, **Ankit Mohan**, Ramesh Raskar, in **OMNIVIS 2009**.



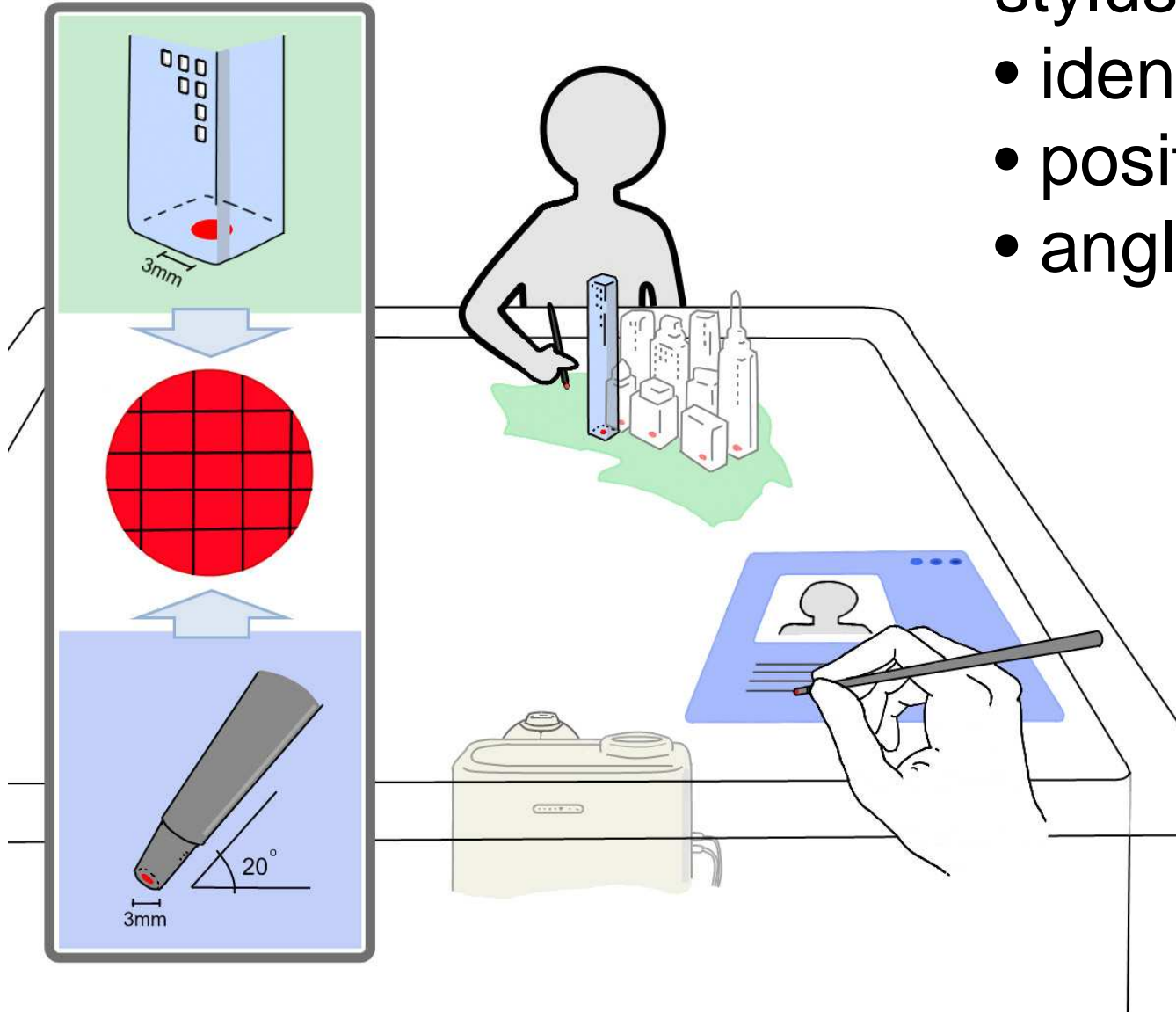


	<b>barcode</b>	<b>RFID</b>	<b>Bokode</b>
<b>encoding</b>	spatial	rf modulation	angular
<b>decoder</b>	<b>camera</b>	<b>dedicated reader</b>	<b>camera</b>
<b>geometry</b>	<b>no</b>	<b>no</b>	<b>yes</b>
<b>physical size</b>	<b>~ cm</b>	~ cm	<b>~ mm</b>
<b>cost</b>	<b>~ free</b>	<b>~ \$0.05</b>	<b>~ \$0.05</b> (currently \$5)
<b>range</b>	<b>~ cm</b>	~ cm	<b>~ m</b> (with large aperture lens)
<b>line of sight</b>	yes	no	yes

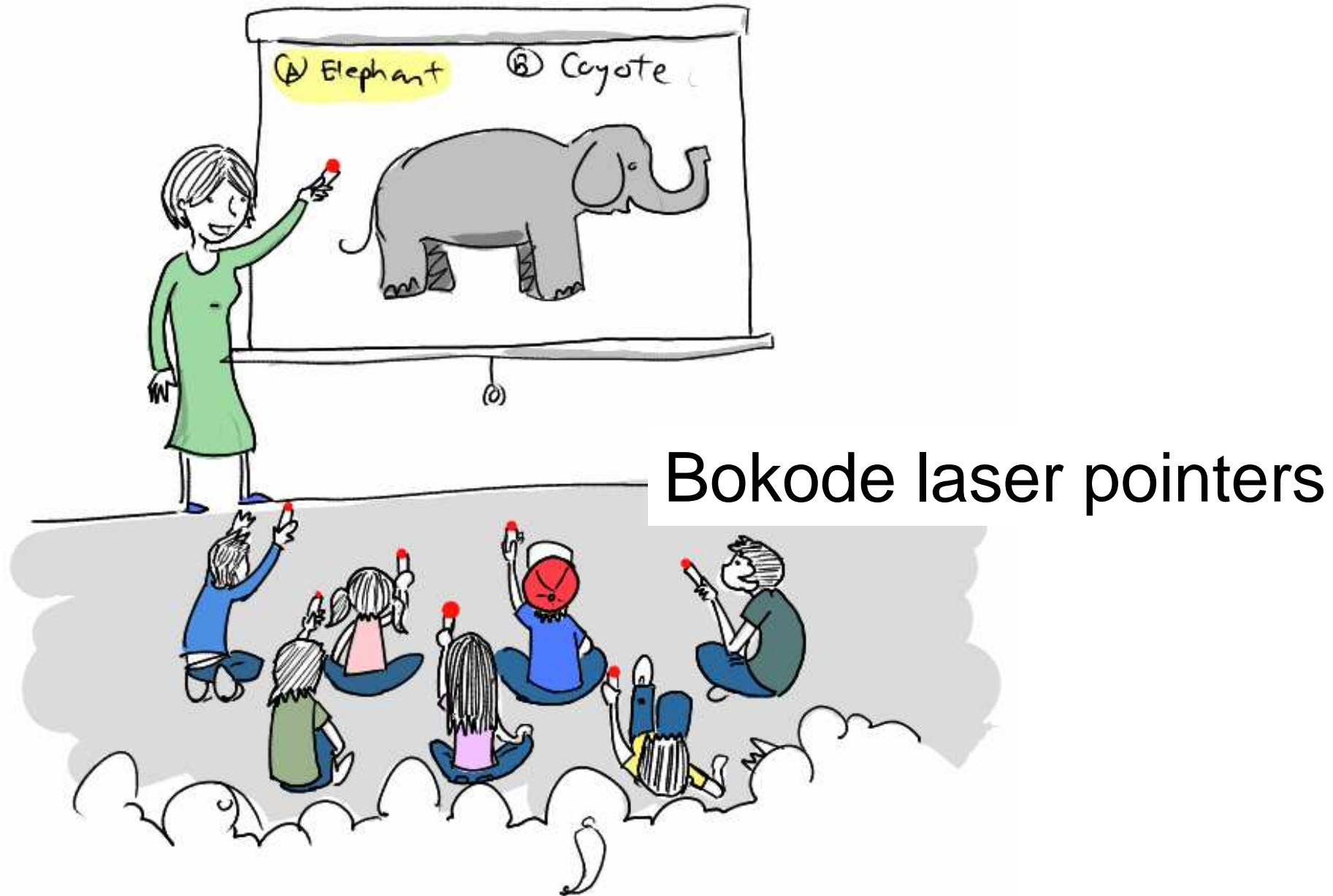
# tabletop/surface interaction

stylus based interaction

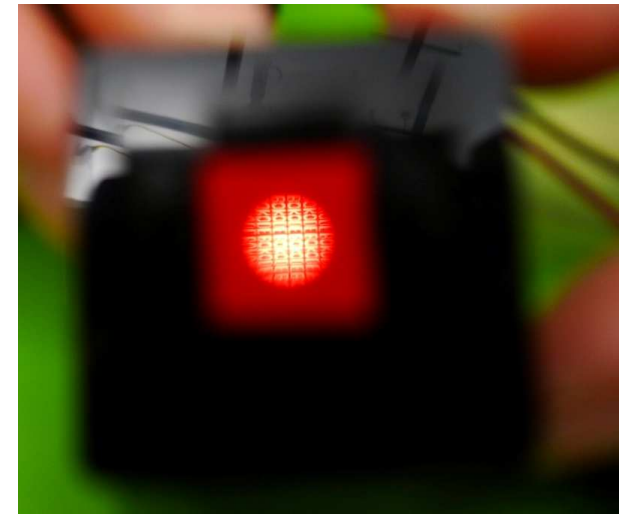
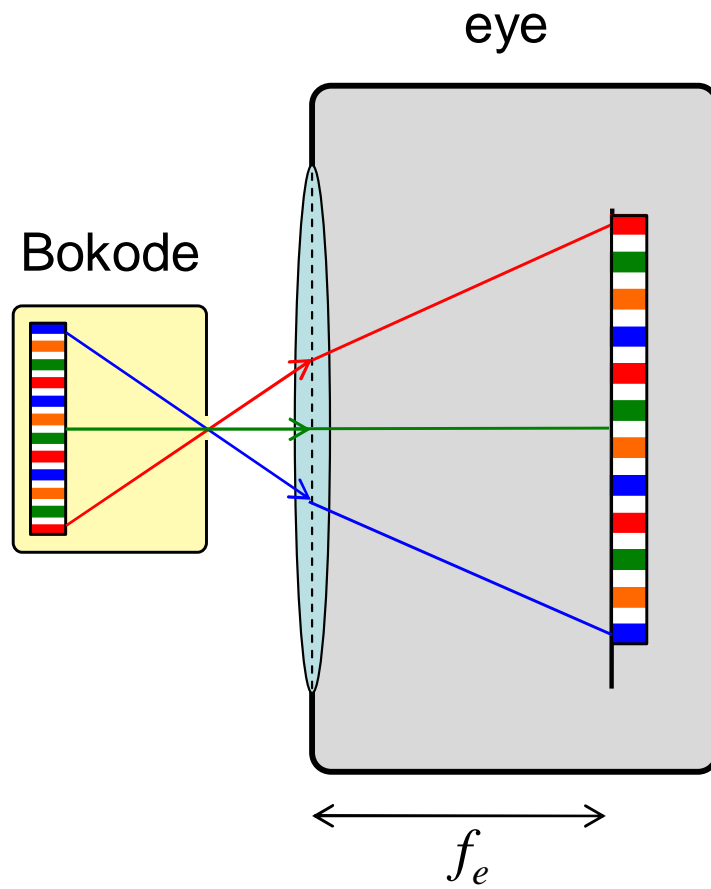
- identity
- position
- angle



# multi-user interaction

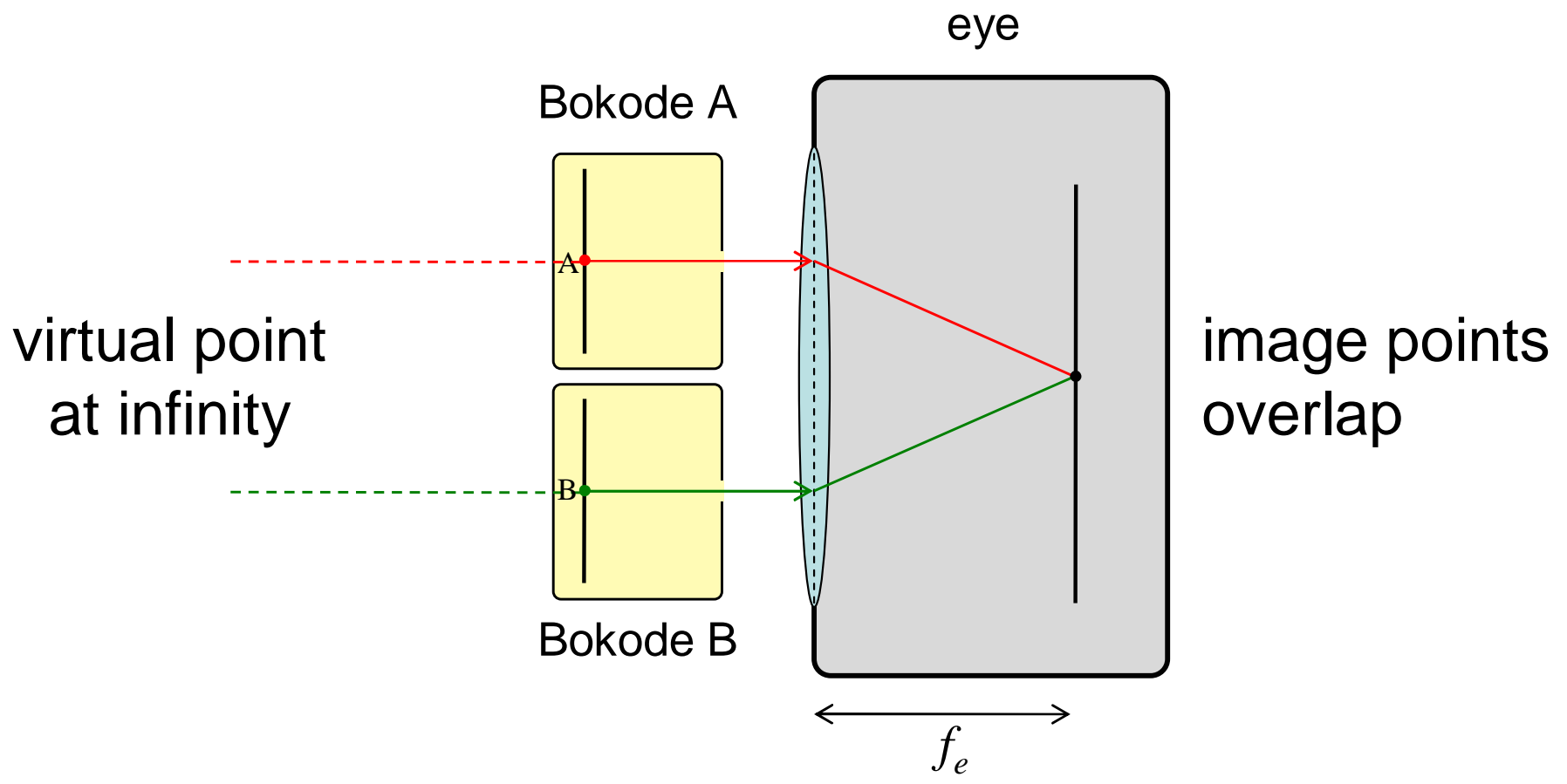


# Bokode next to the eye



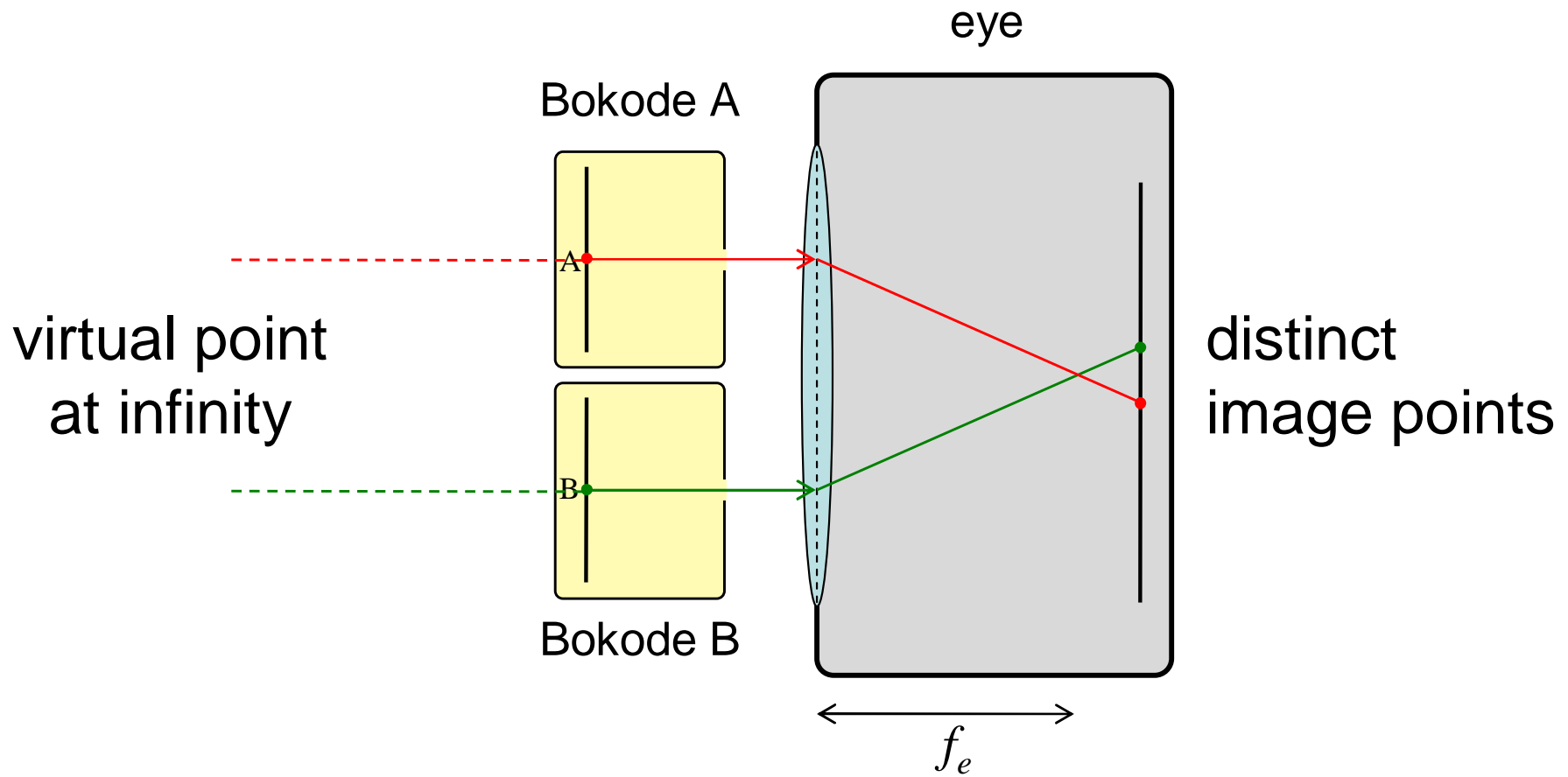


# relaxed perfect eye focused at infinity



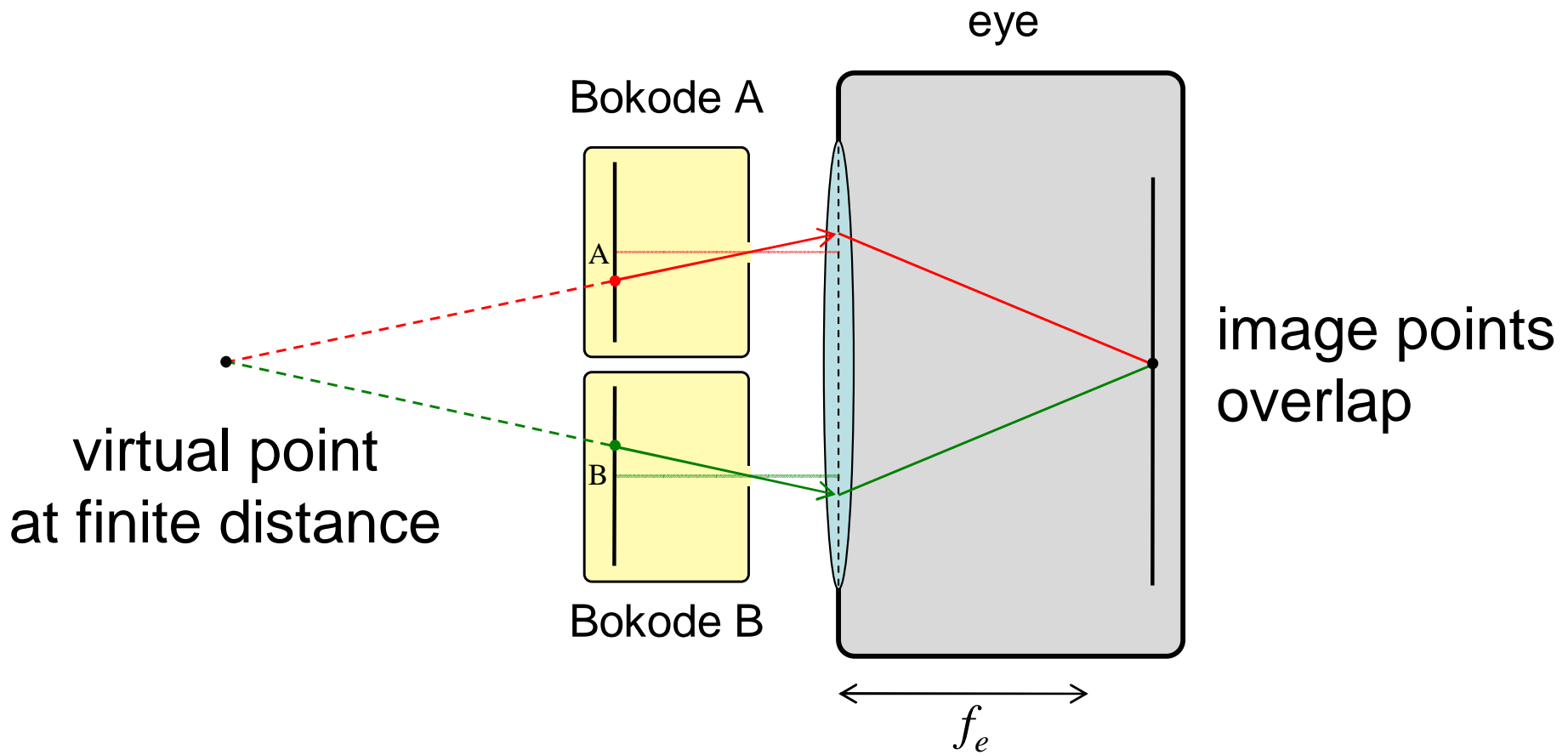


# relaxed eye with *myopia*



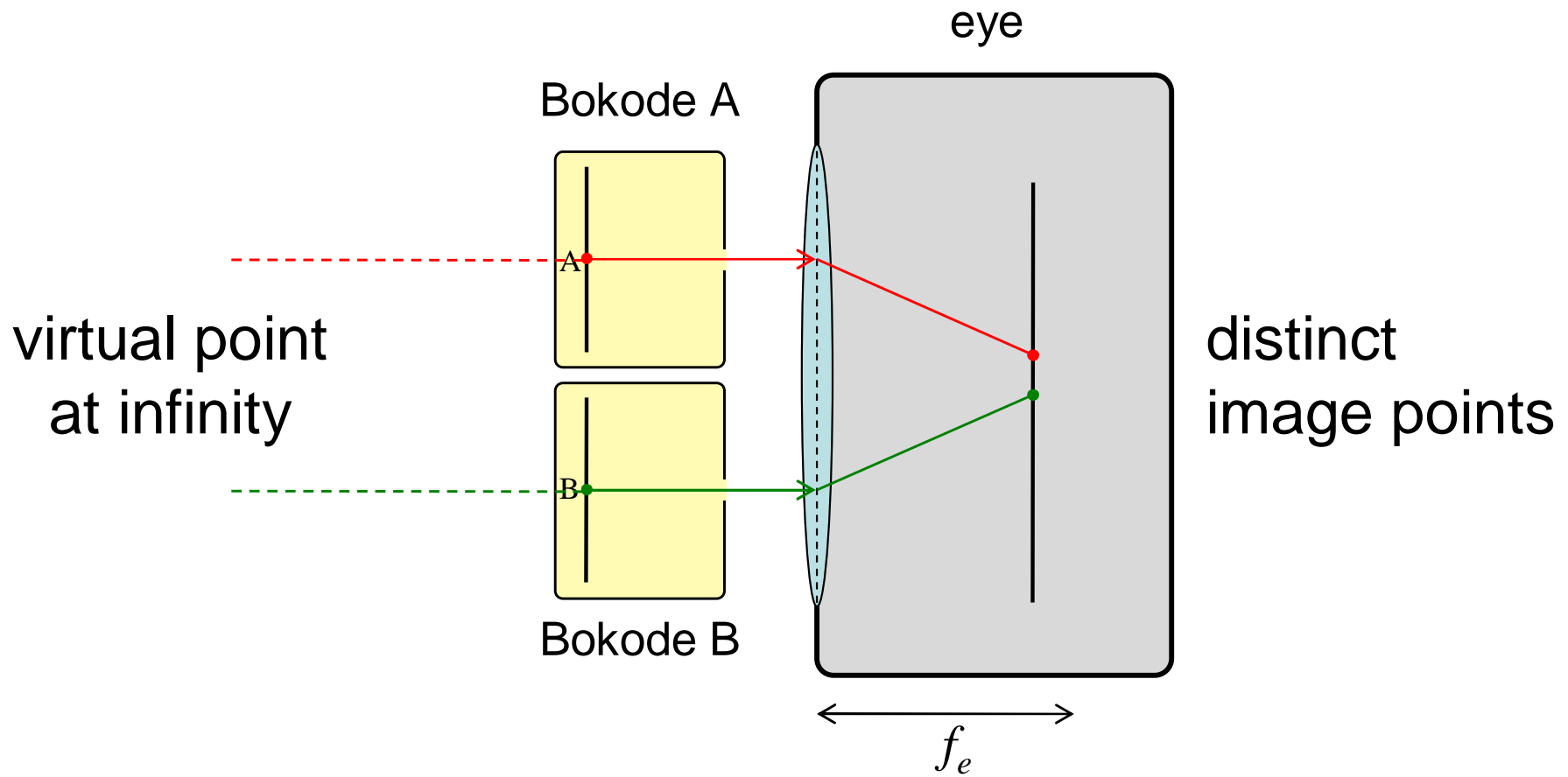
eye unable to focus at infinity

# relaxed eye with *myopia*

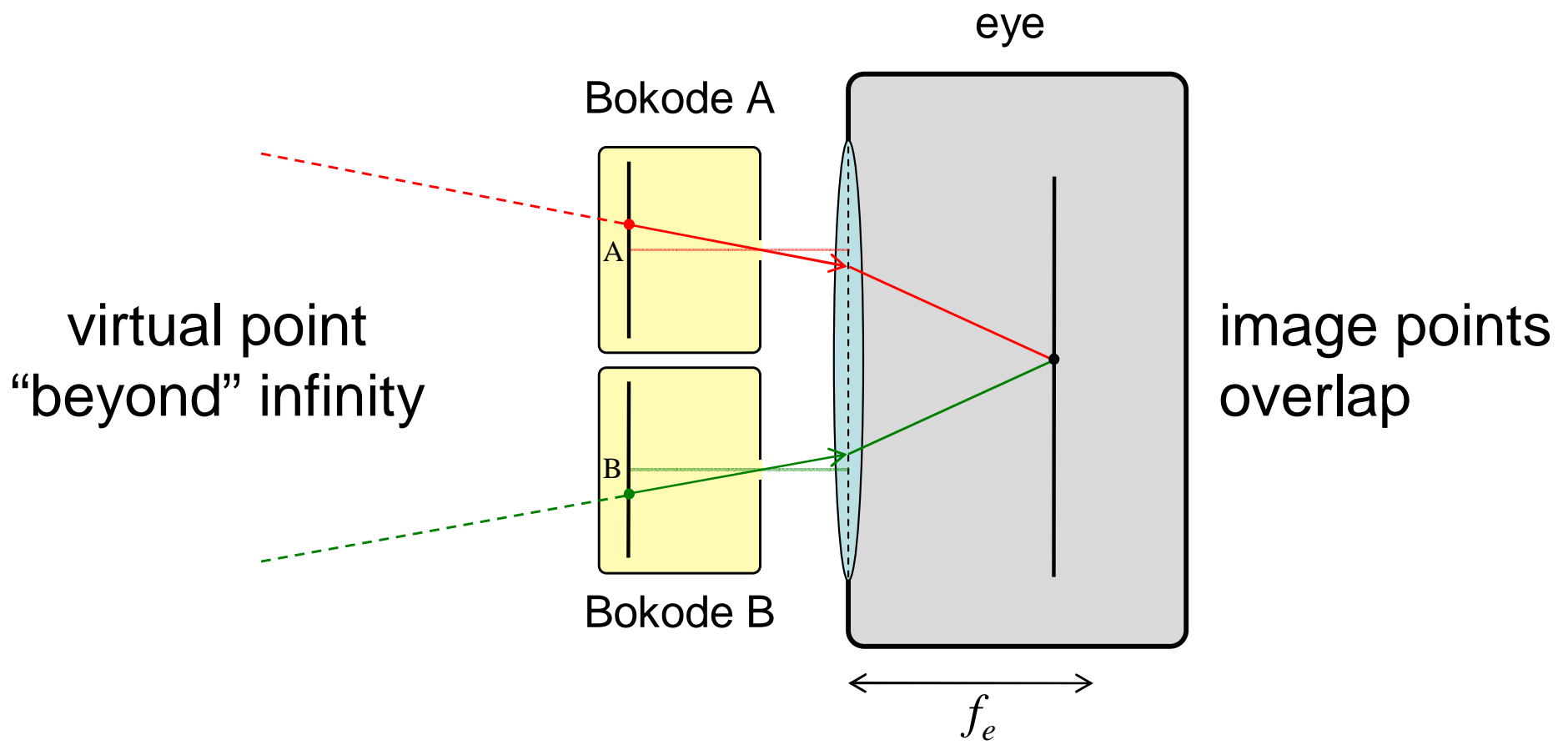


move points **towards** each other

# relaxed eye with *hyperopia*

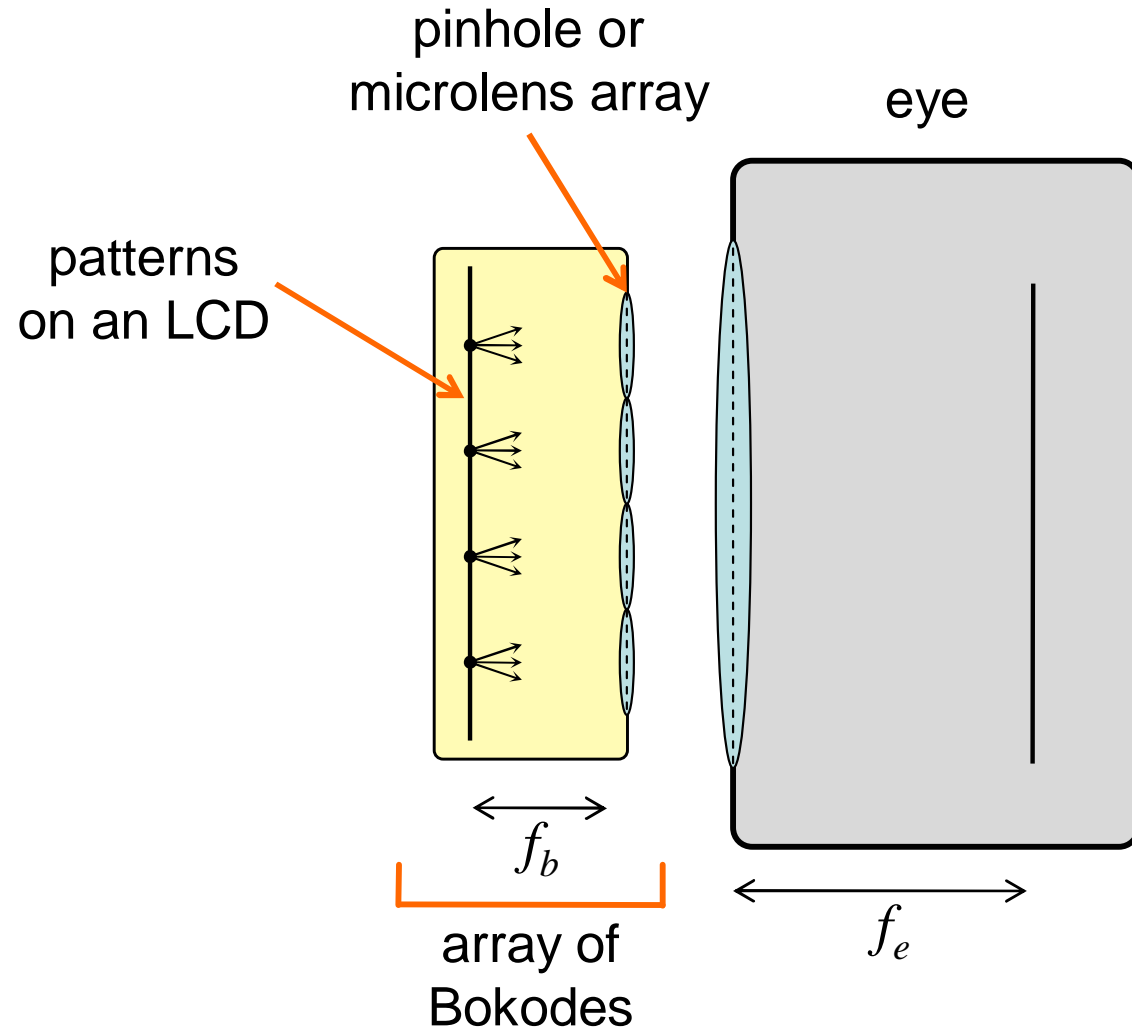


# eye with *hyperopia*

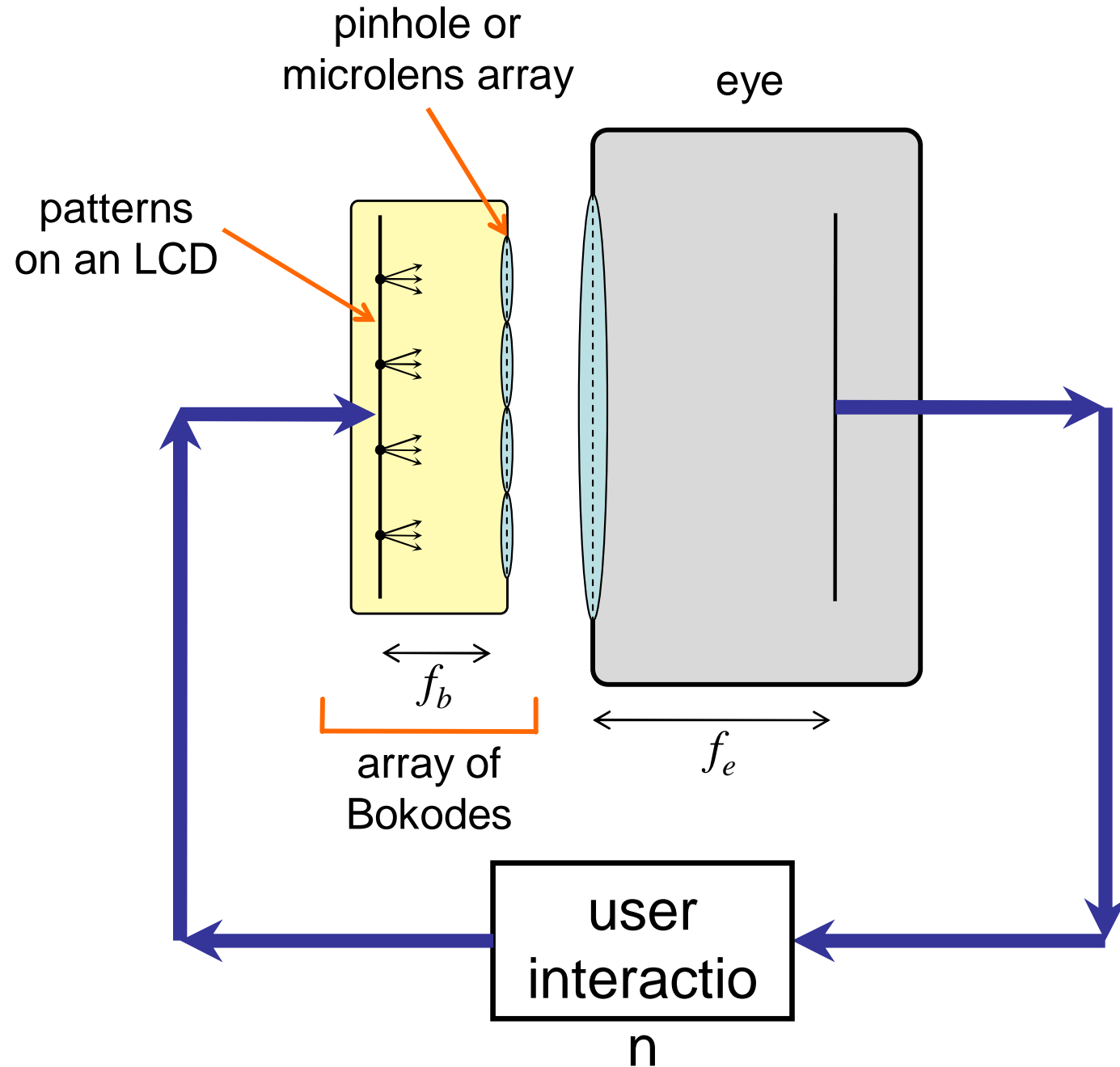


move points **away** from each other

# NETRA: interactively measure prescription

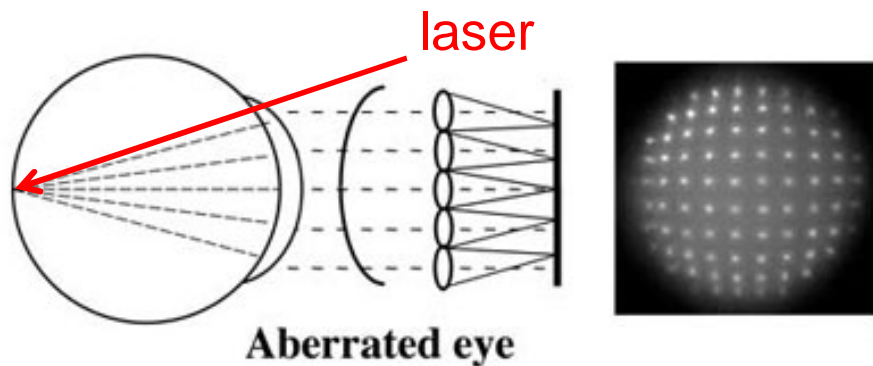
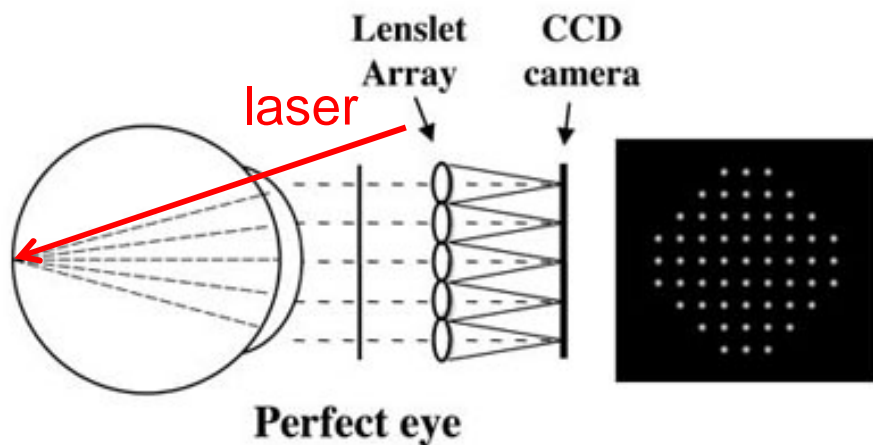


# NETRA: interactively measure prescription





# Shack-Hartmann wave-front sensor

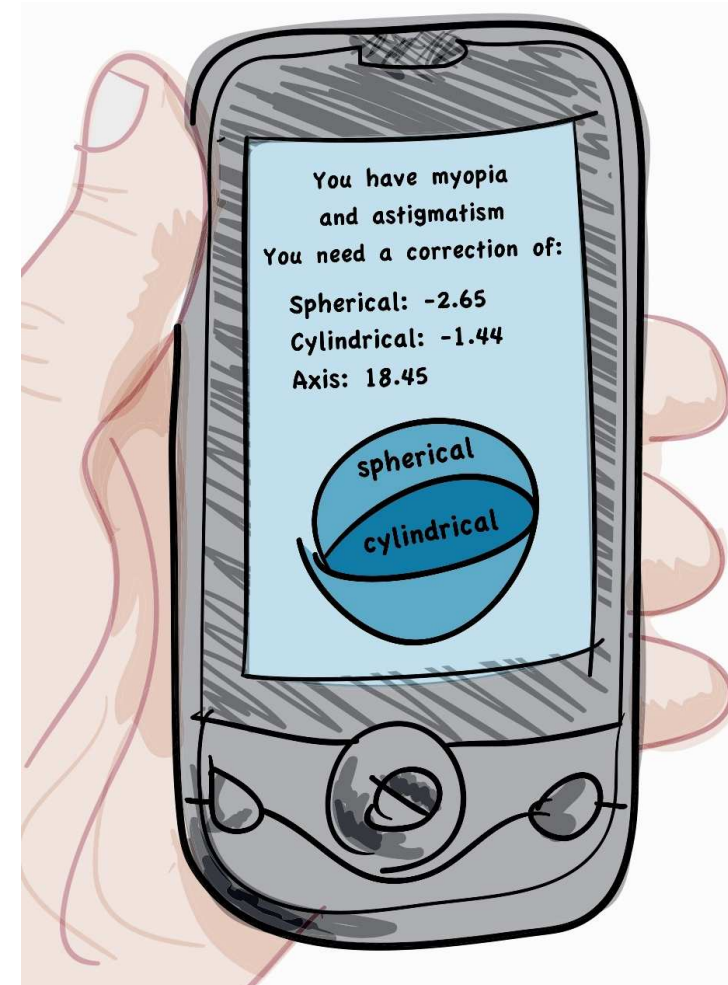
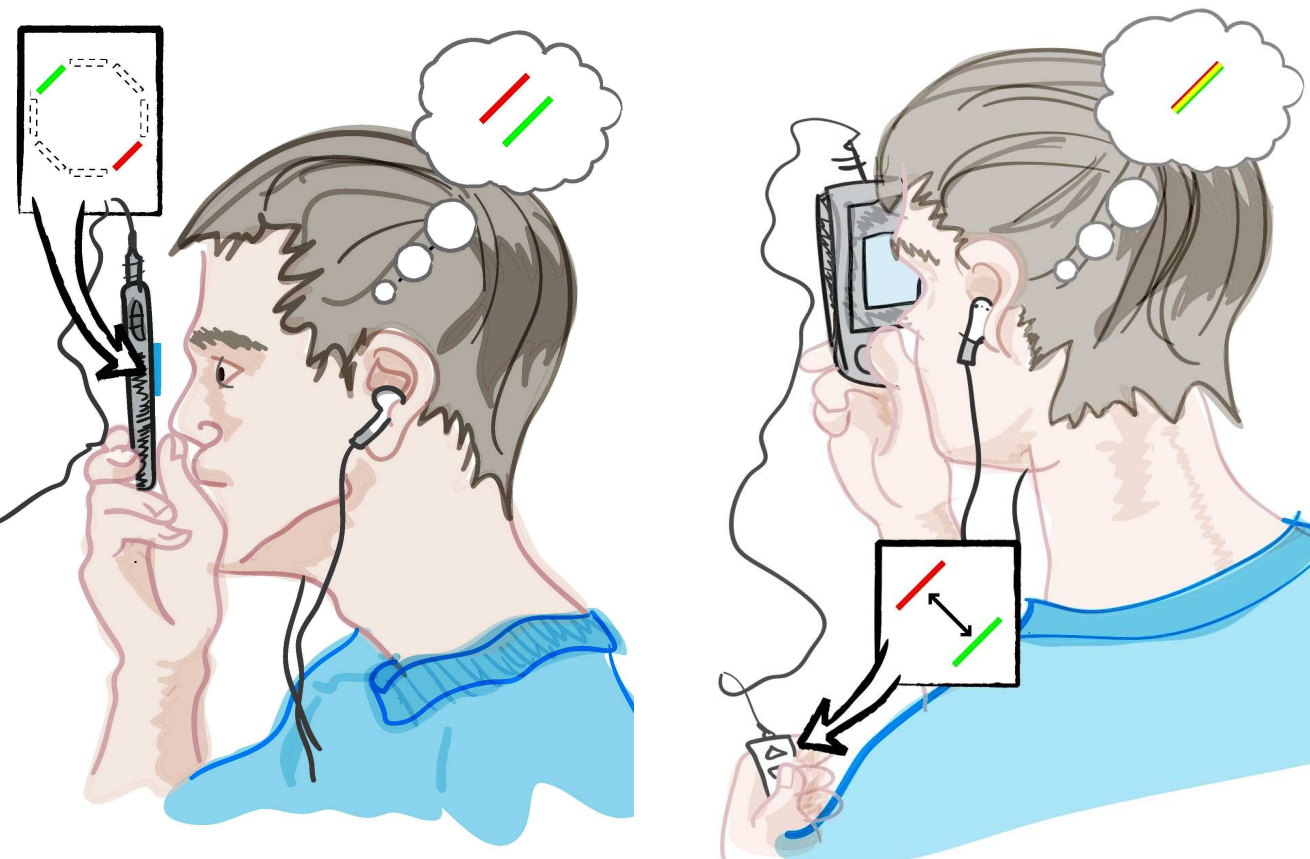


wavefront aberrometer



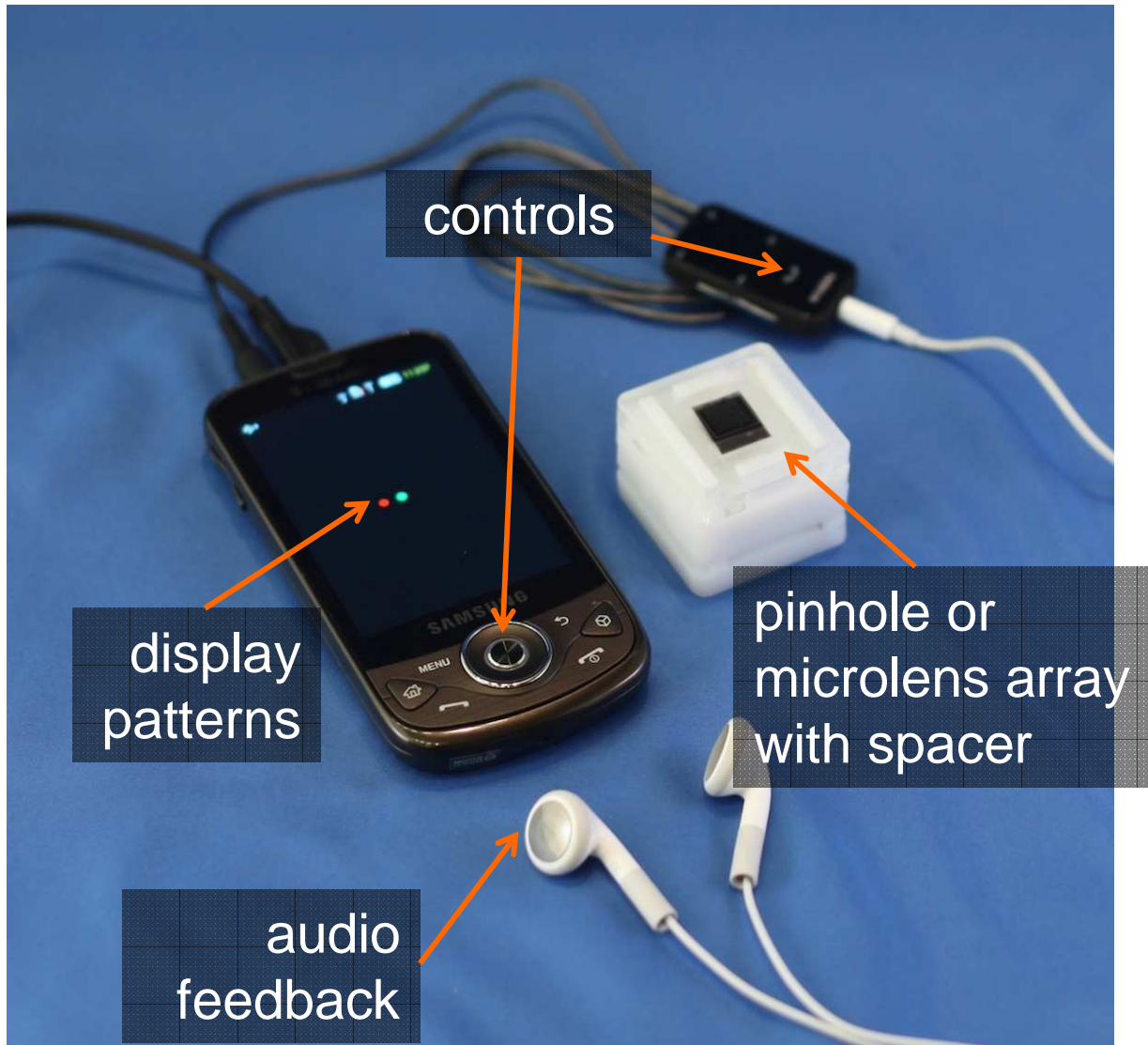
expensive; requires trained professionals

# interactive self-evaluation of eye's refractive error



*“NETRA: Interactive Display for Estimating Refractive Errors and Focal Range”*, Vitor Pamplona, Ankit Mohan, Manuel Oliveira, and Ramesh Raskar, in **SIGGRAPH 2010**.

# cell phone prototype



**lcd:** 180dpi

**pinhole:**  $a=3\text{mm}$ ,  
 $\Phi \sim 100\mu\text{m}$

**lenslet:**  $f=20\text{mm}$ ,  
 $a=3\text{mm}$

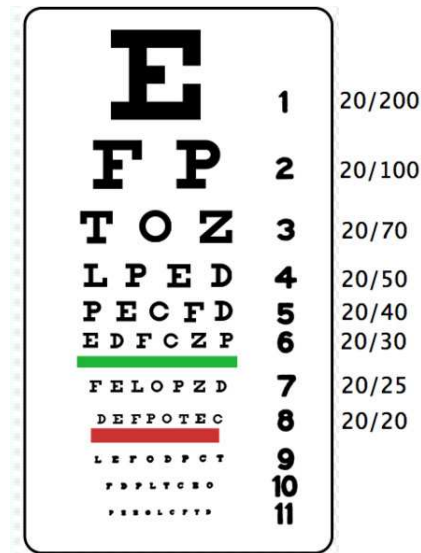
**resolution:** 0.71D

**cost:** ~\$2 (pinhole)





VS



Snellen chart



trial lenses

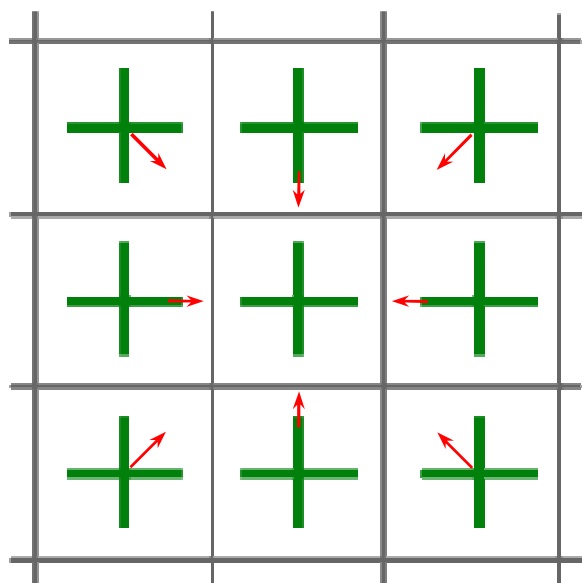


phoropter

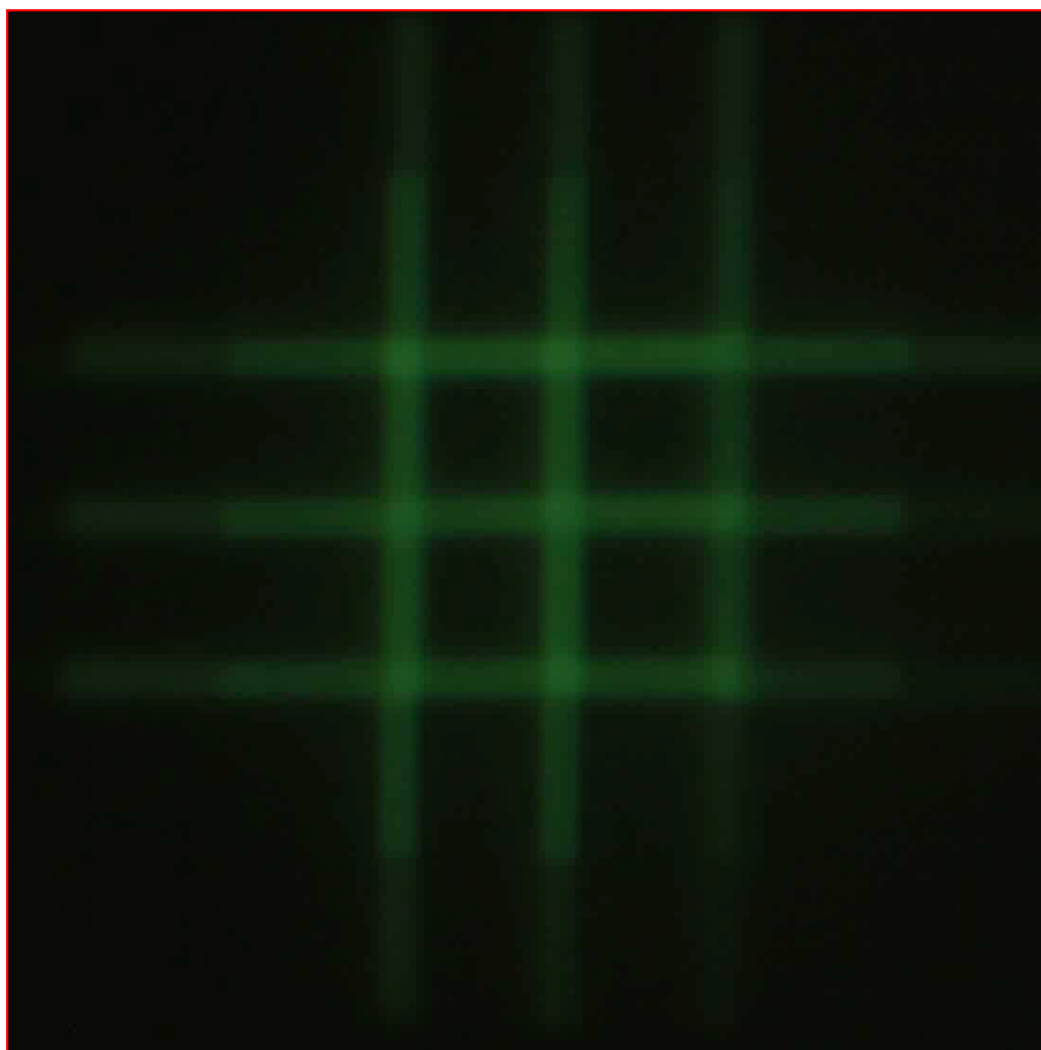
### NETRA

- smaller, less bulky, easier to carry
- little no training required
- avoids cycloplegic eye drops
- allows self-evaluation
- cheaper (if phone already exists)

# interaction session with camera



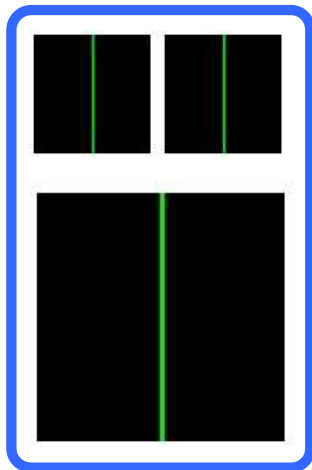
displayed  
patterns



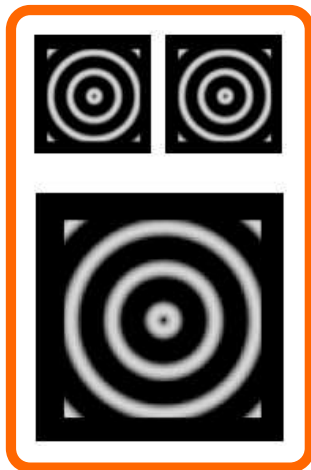
camera/subject view

# patterns

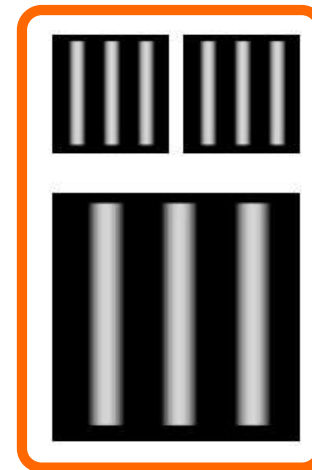
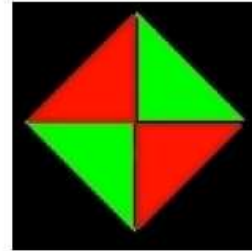
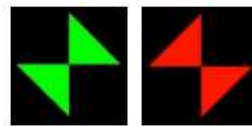
displayed



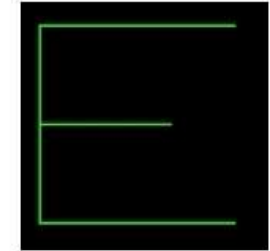
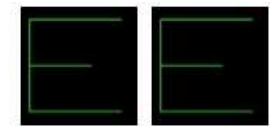
alignment



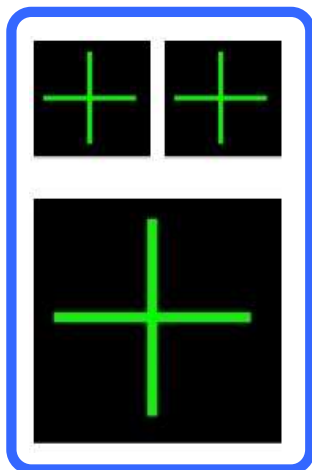
accommodation



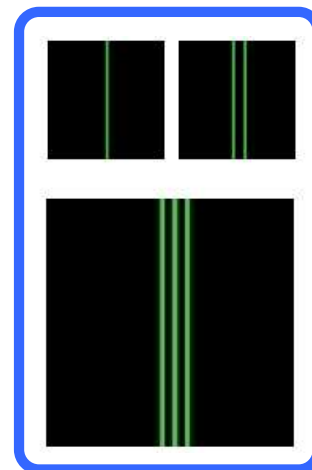
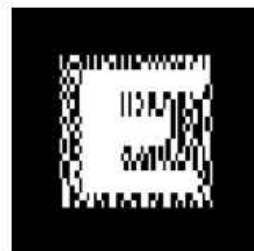
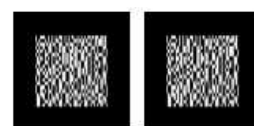
accommodation



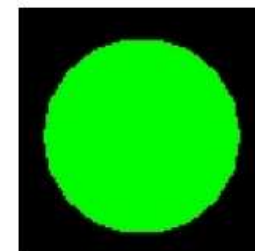
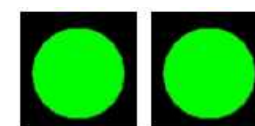
displayed



alignment

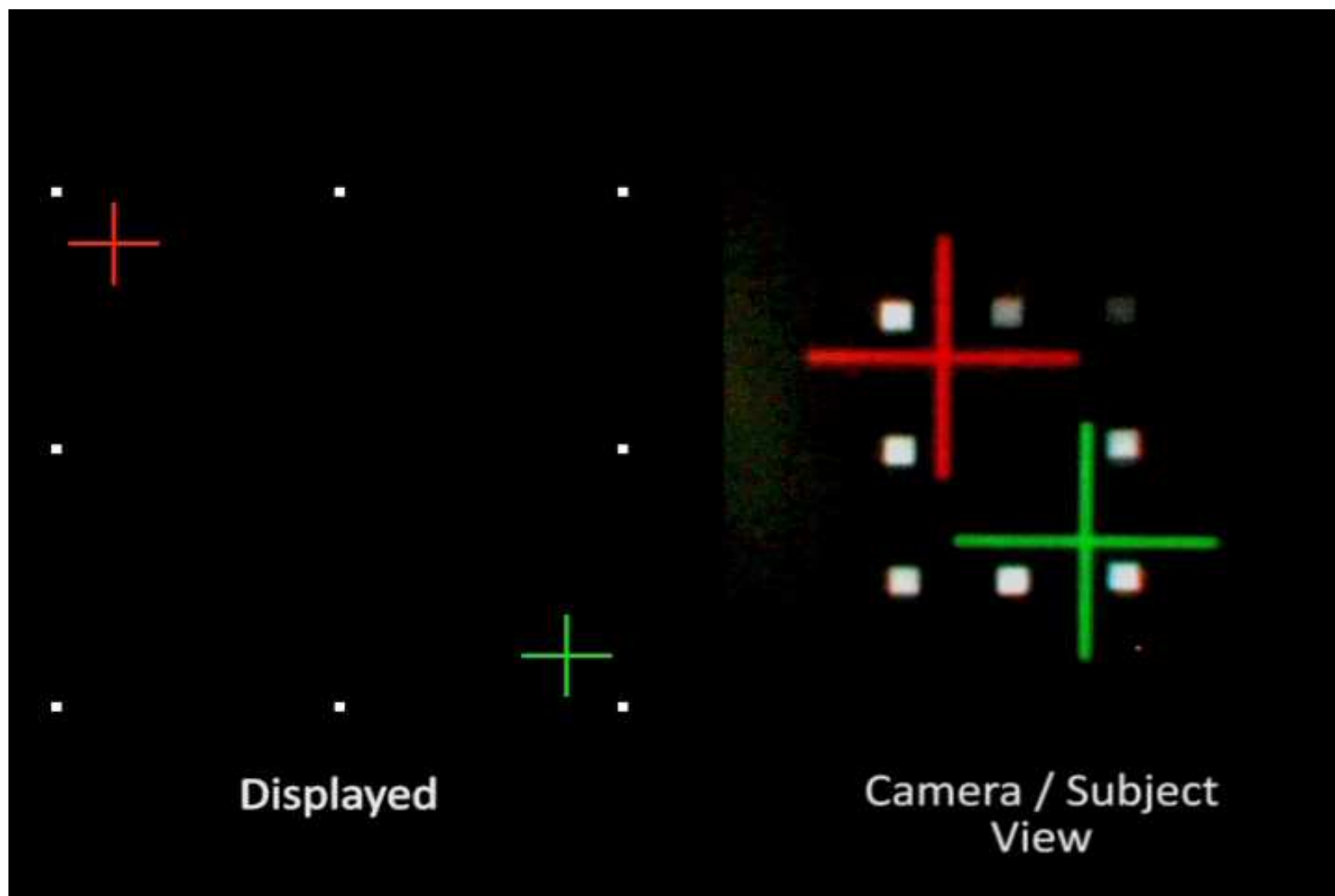


alignment



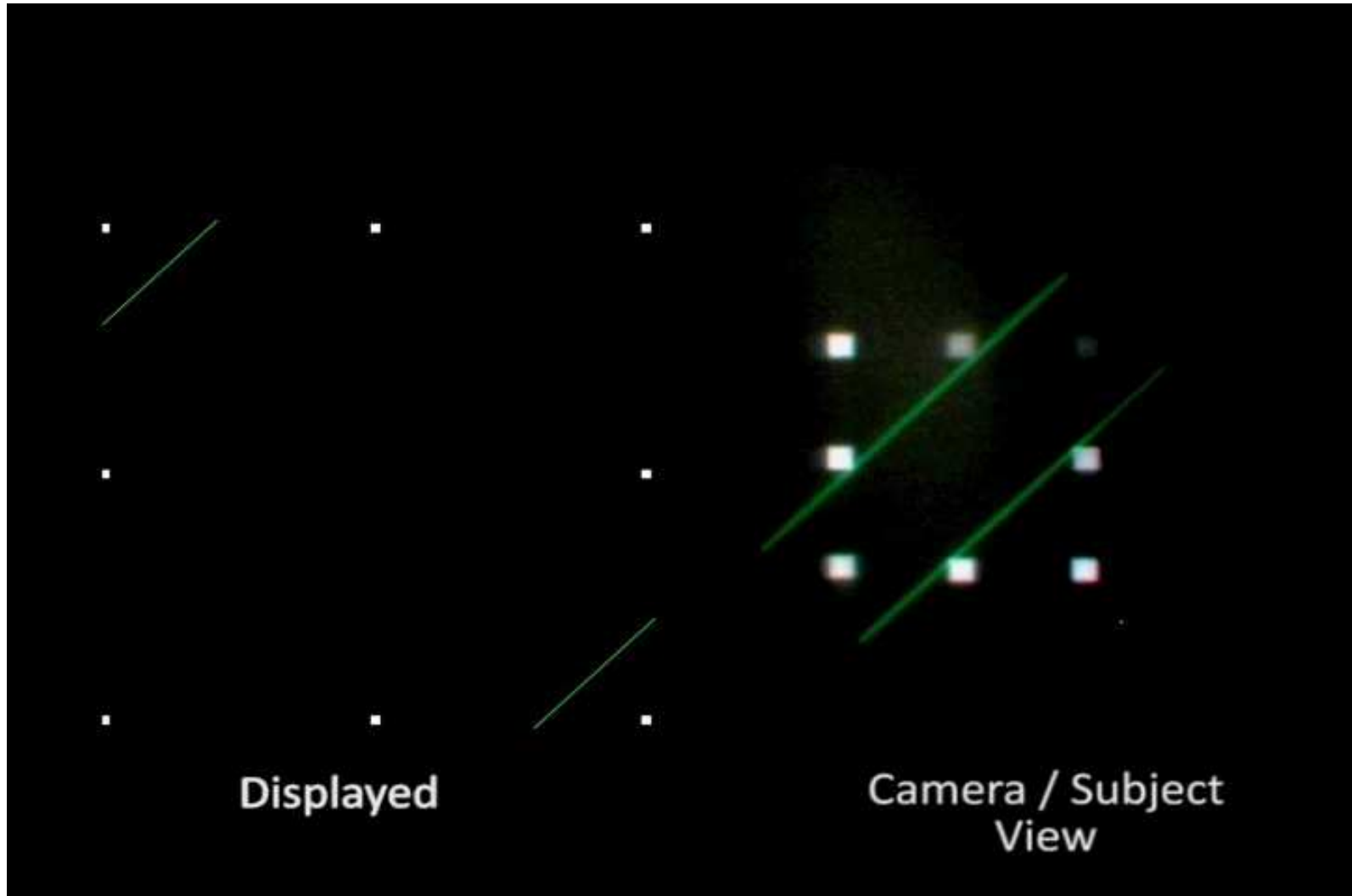


# astigmatism: radially non-symmetric error



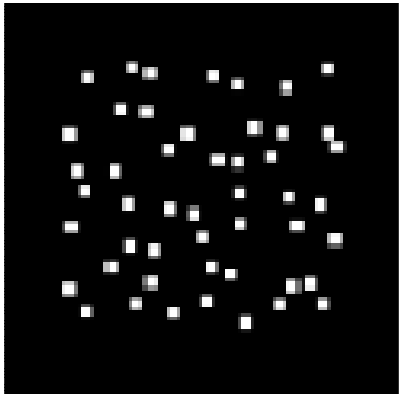
cross or points may never meet with a 1d search

# astigmatism

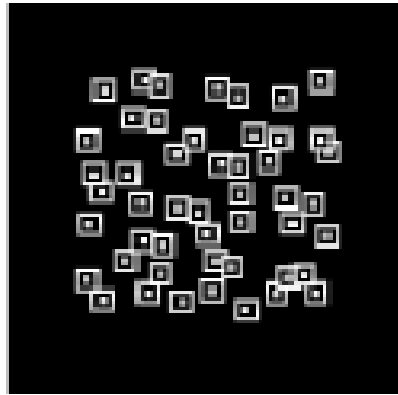


**lines** reduce the problem to a 1d search

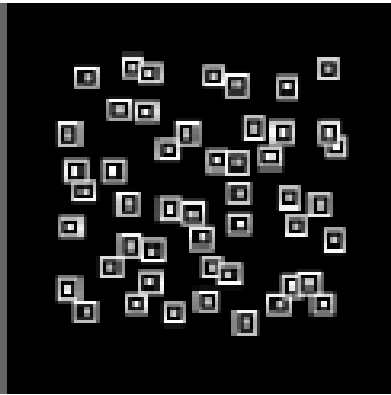
# jittered pinholes – reduce crosstalk



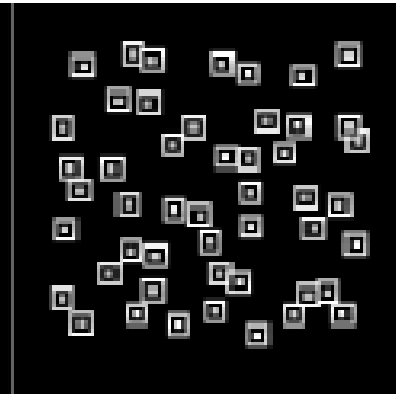
jittered  
pinholes



-5D

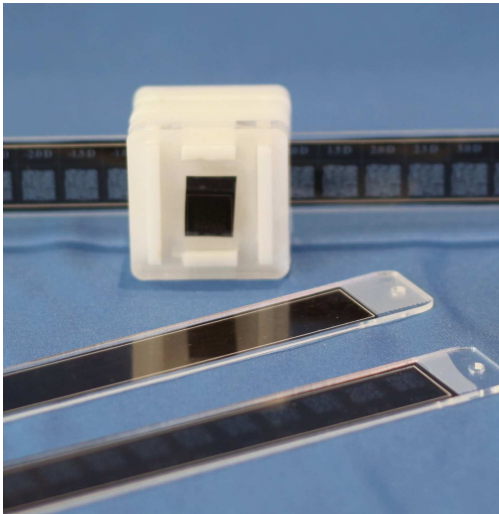


0D

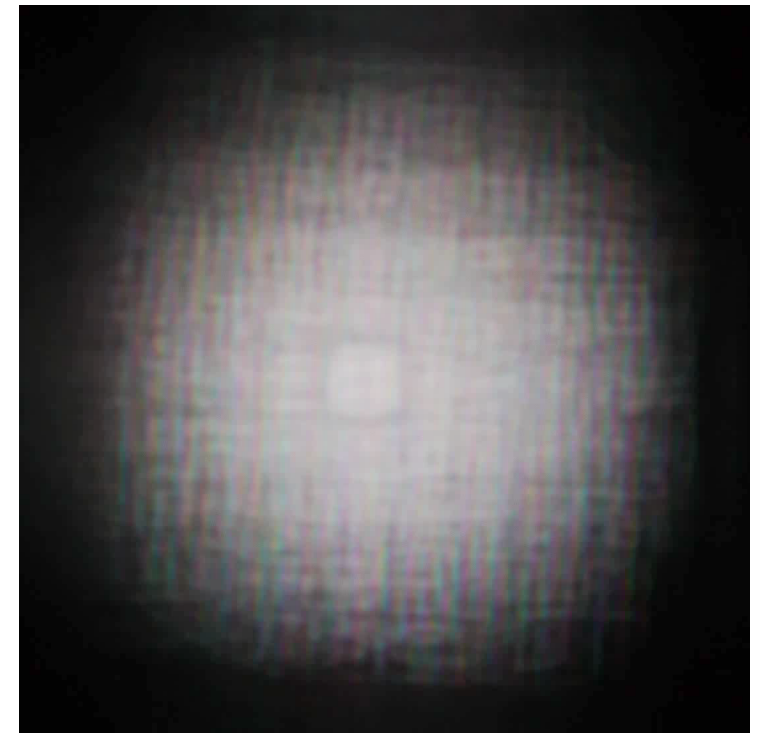
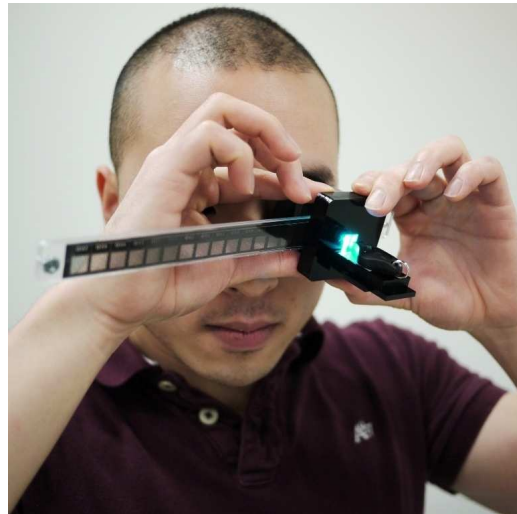


+5D

display patterns

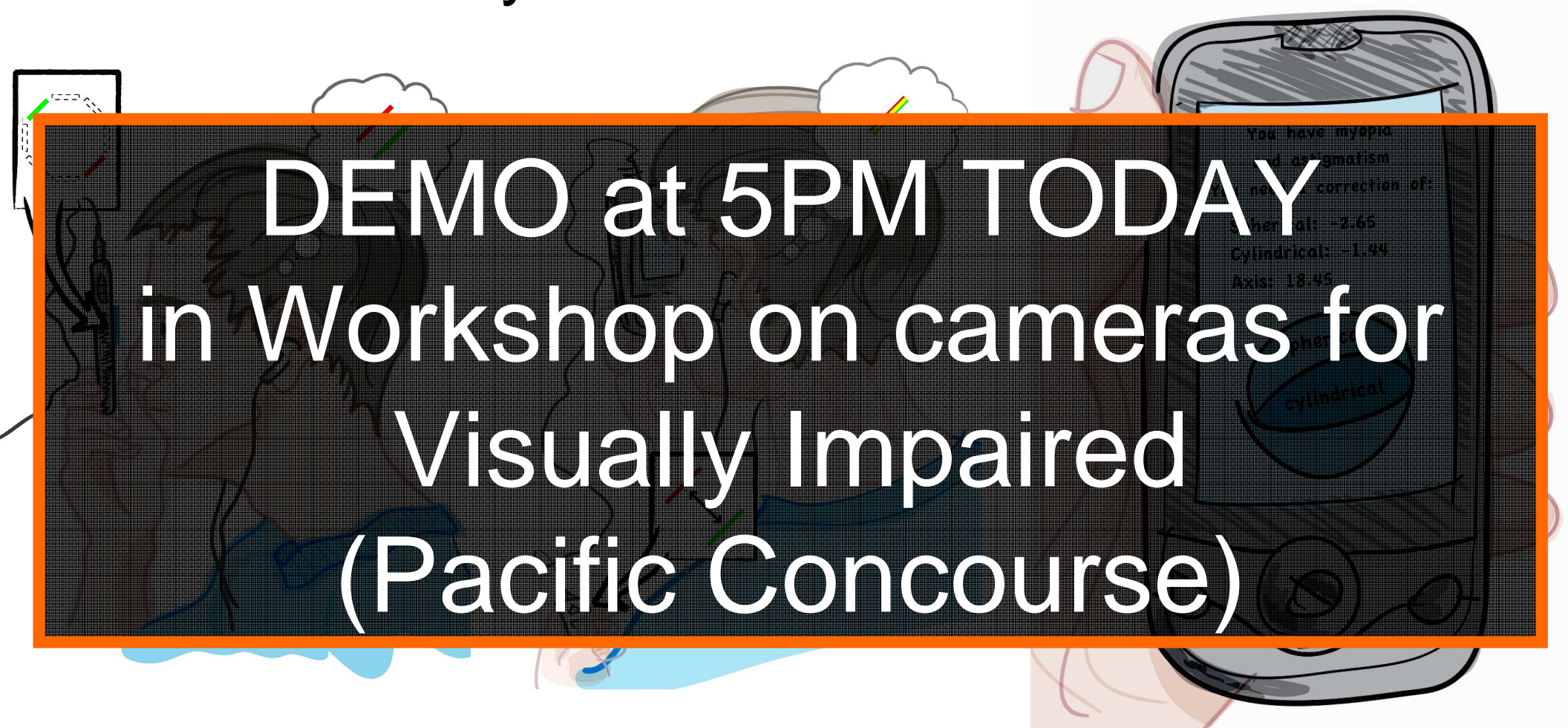


viewmaster inspired prototype



+3D to -5D with accommodation

# interactive self-evaluation of eye's refractive error



**DEMO at 5PM TODAY**  
in Workshop on cameras for  
Visually Impaired  
(Pacific Concourse)

*“NETRA: Interactive Display for Estimating Refractive Errors and Focal Range”*, Vitor Pamplona, Ankit Mohan, Manuel Oliveira, and Ramesh Raskar, in **SIGGRAPH 2010**.

# Light Field Capture



# Camera Arrays [Wilburn 2005]



*“High Performance Imaging Using Large Camera Arrays”,  
Bennett Wilburn, Neel Joshi, Vaibhav Vaish, Eino-Ville Talvala,  
Emilio Antunez, Adam Barth, Andrew Adams, Mark Horowitz,  
Marc Levoy, in **SIGGRAPH 2005**.*



# Synthetic aperture photography



Camera array is far away from these bushes, yet it sees...

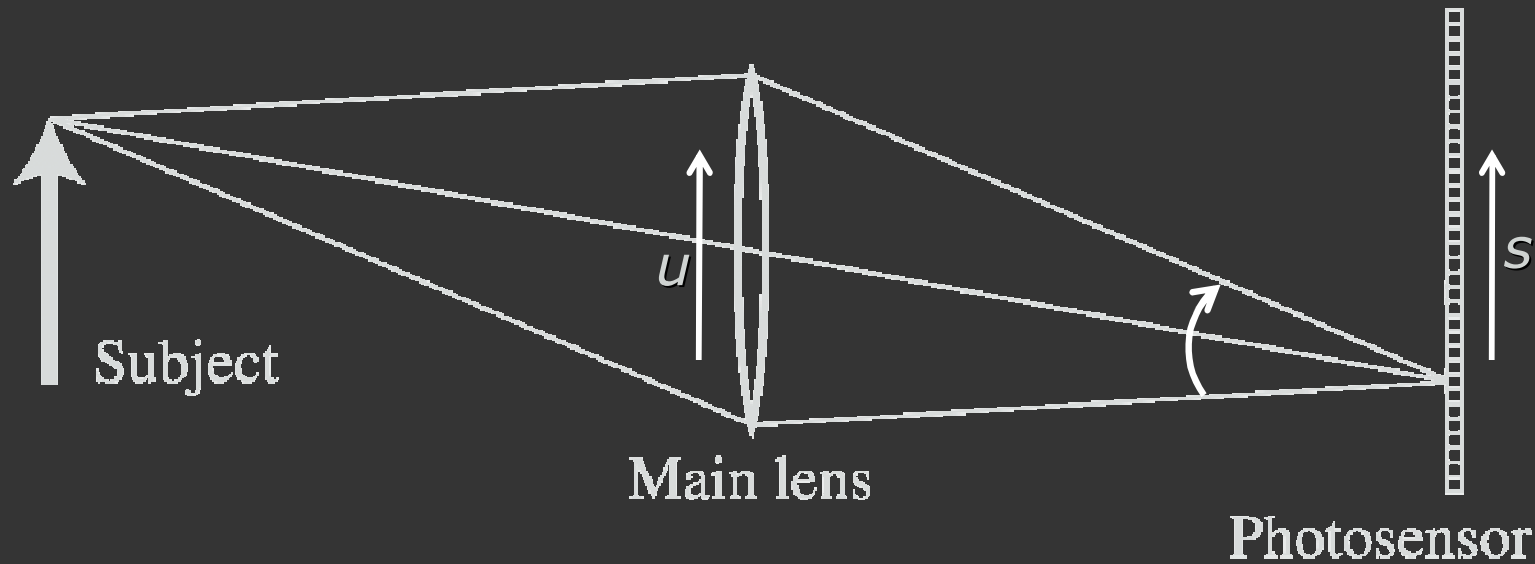


# Focus Adjustment: Sum of Bundles

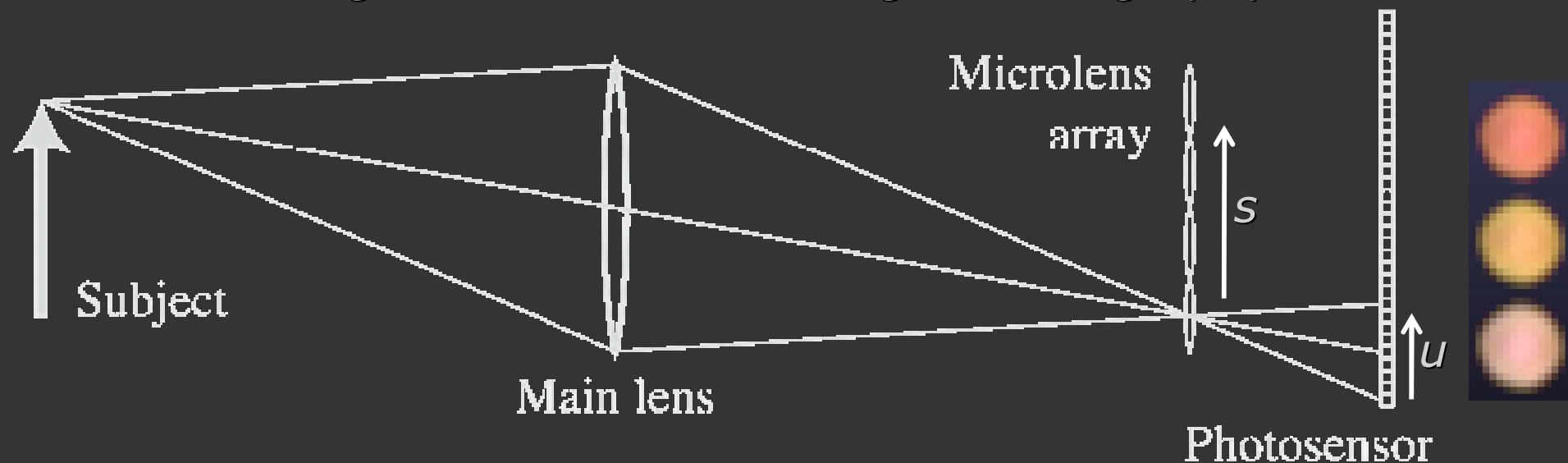
[Vaish et al. 2004]



# Light Field Inside a Camera



Lenslet-based Light Field camera / Integral Photography



[Lippman 1908, Adelson and Wang, 1992, Ng et al. 2005]

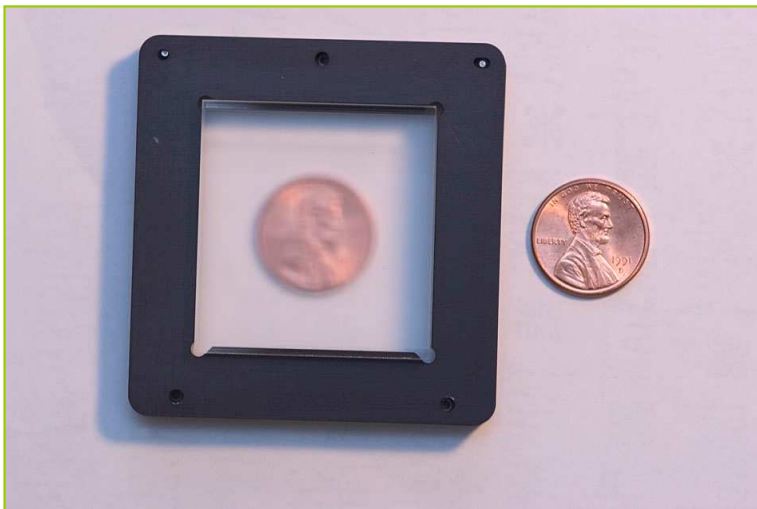
# Stanford Plenoptic Camera [Ng et al 2005]



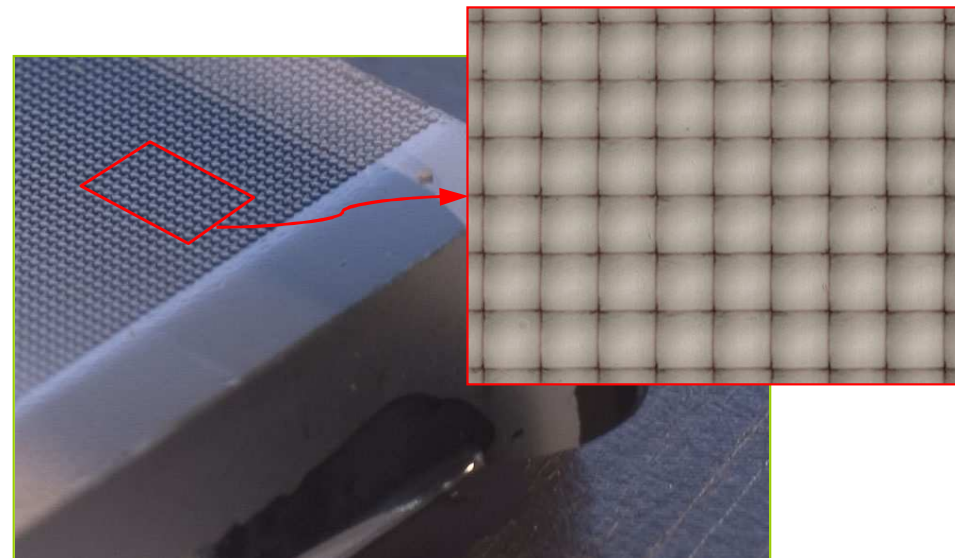
Contax medium format camera



Kodak 16-megapixel sensor



Adaptive Optics microlens array



125  $\mu$  square-sided microlenses

$$4000 \times 4000 \text{ pixels} \div 292 \times 292 \text{ lenses} = 14 \times 14 \text{ pixels per lens}$$



# Captured Image Behind Microlens



Slide from Ren Ng and Marc Levoy

# Digital Refocusing [Ng et al 2005]



*“Light Field Photography with a Hand-Held Plenoptic Camera”*, Ren Ng, Marc Levoy, Mathieu Bredif, Gene Duval, Mark Horowitz, Pat Hanrahan, in **Stanford Tech Report 2005**.

# Extended Depth of Field

Light field  
↓  
focal stack  
↓  
extended DOF



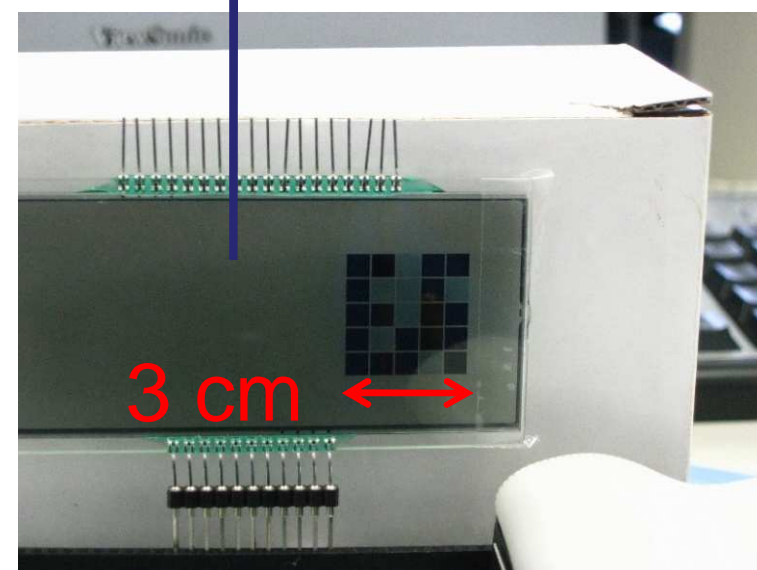


# Light Field Capture with a Programmable Aperture



Nikon D70

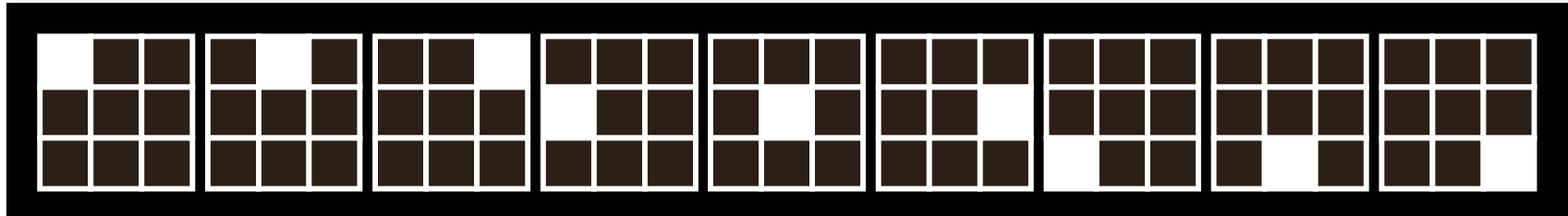
Liquid crystal array



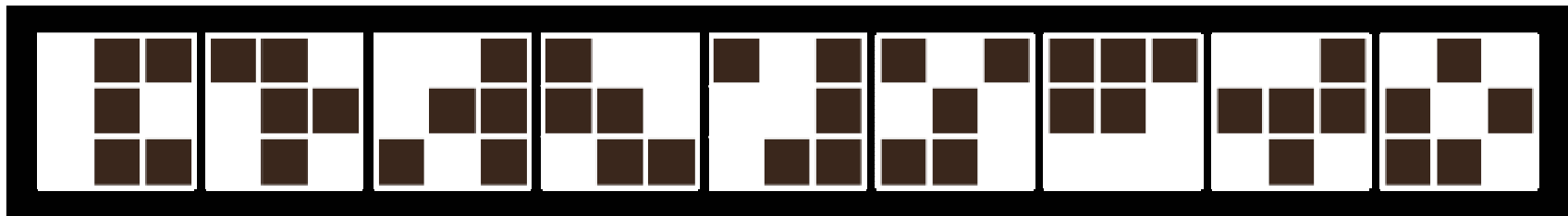
*“Programmable Aperture Photography: Multiplexed Light Field Acquisition”*, Chia-Kai Liang, Tai-Hsu Lin, Bing-Yi Wong, Chi Liu, Homer Chen, in **SIGGRAPH 2008**.



# Multiplexing to improve SNR



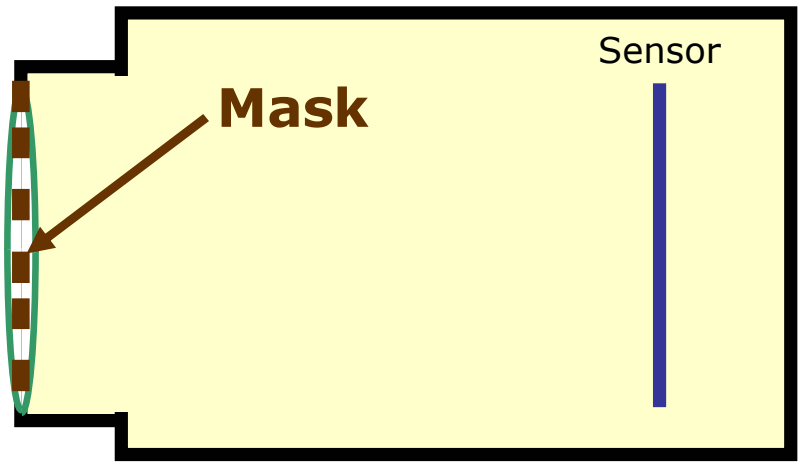
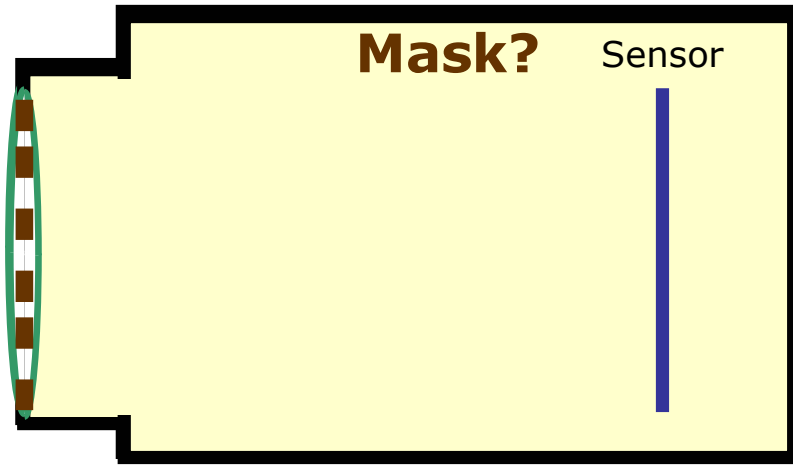
9 aperture patterns for capturing a light field with 3x3 angular resolution



9 multiplexed aperture patterns

- $O(M)$  SNR improvement
  - Comparable to previous single-shot light field cameras
- SNR is a function of
  - $W$  (aperture patterns)
  - The camera noise characteristics

Can we capture the Light-Field  
using a static mask?



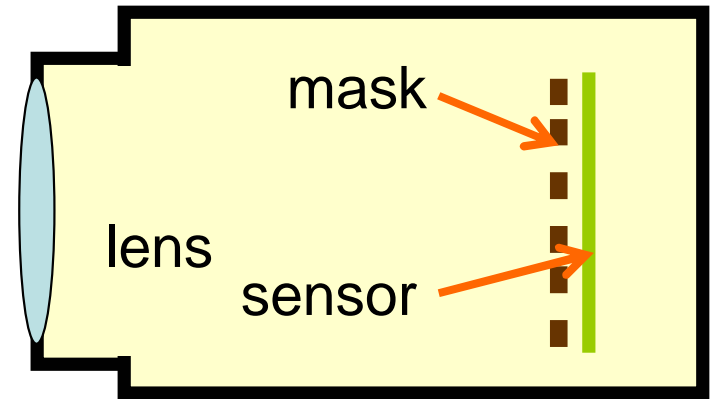
Full Resolution Digital Refocusing:

Coded Aperture Camera

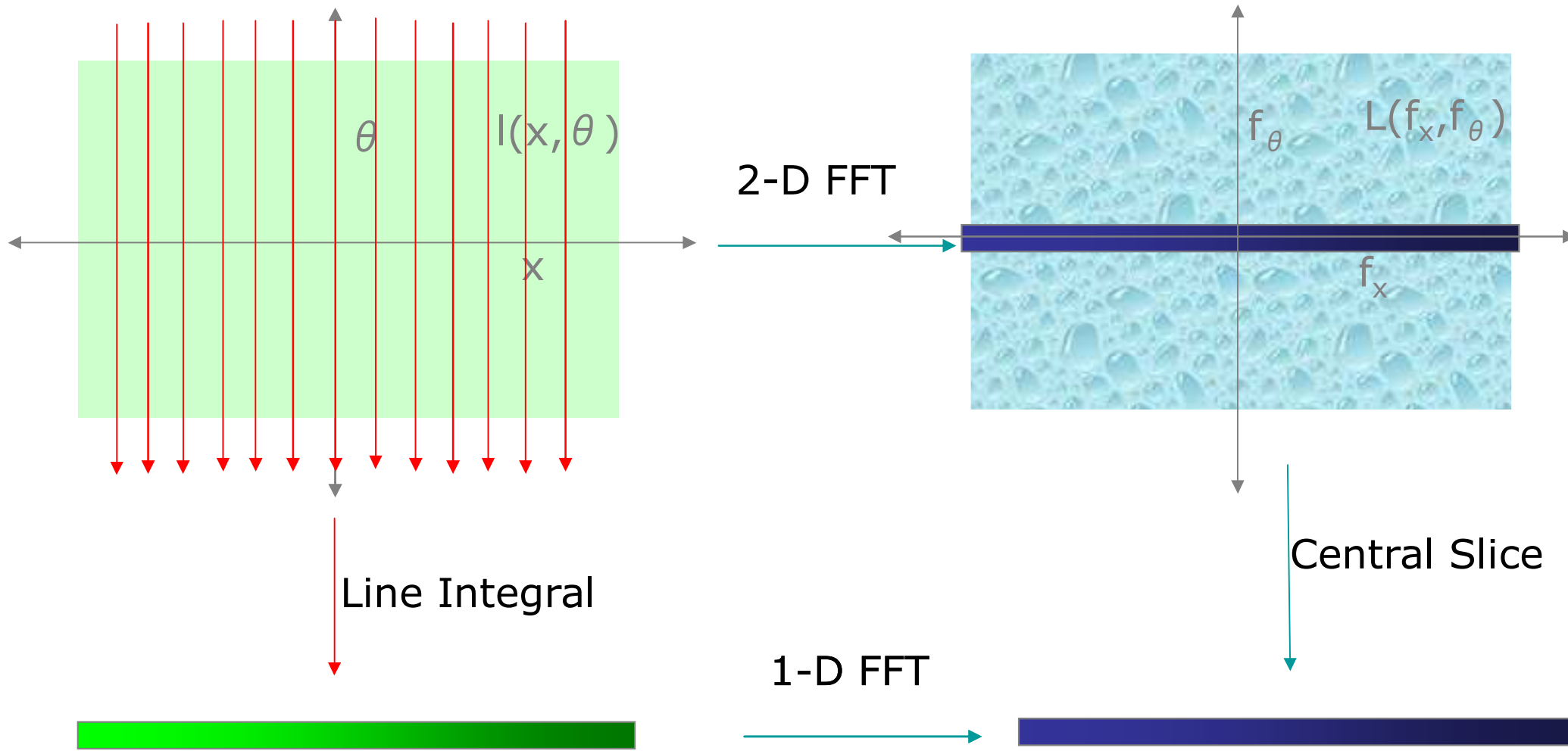
4D Light Field from 2D Photo:

Heterodyne Light Field Camera

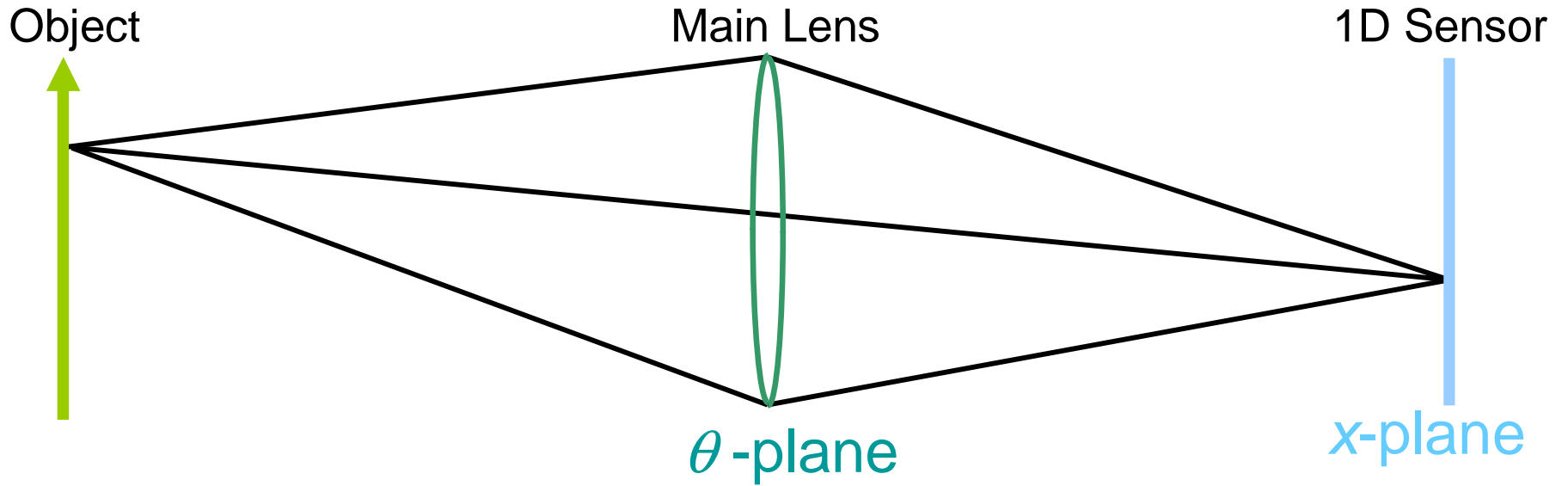
# mask based light-field camera



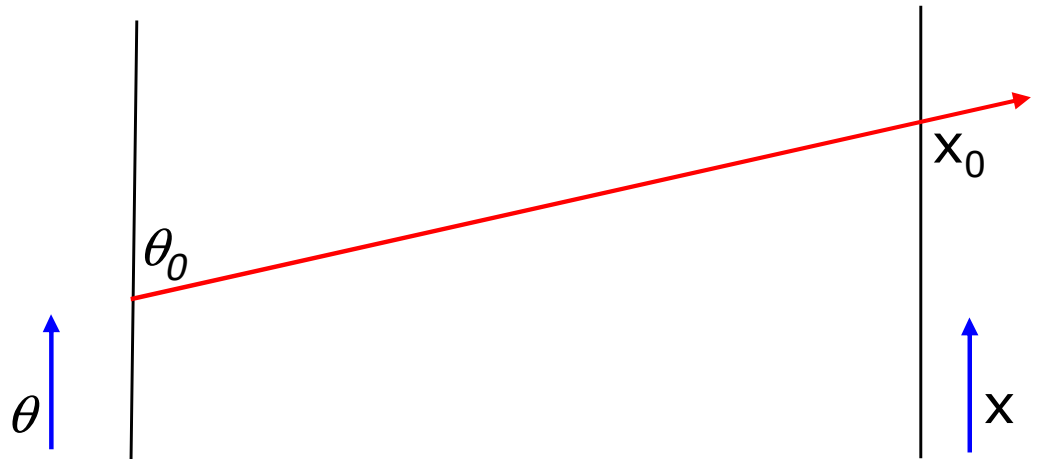
# Fourier Slice Theorem



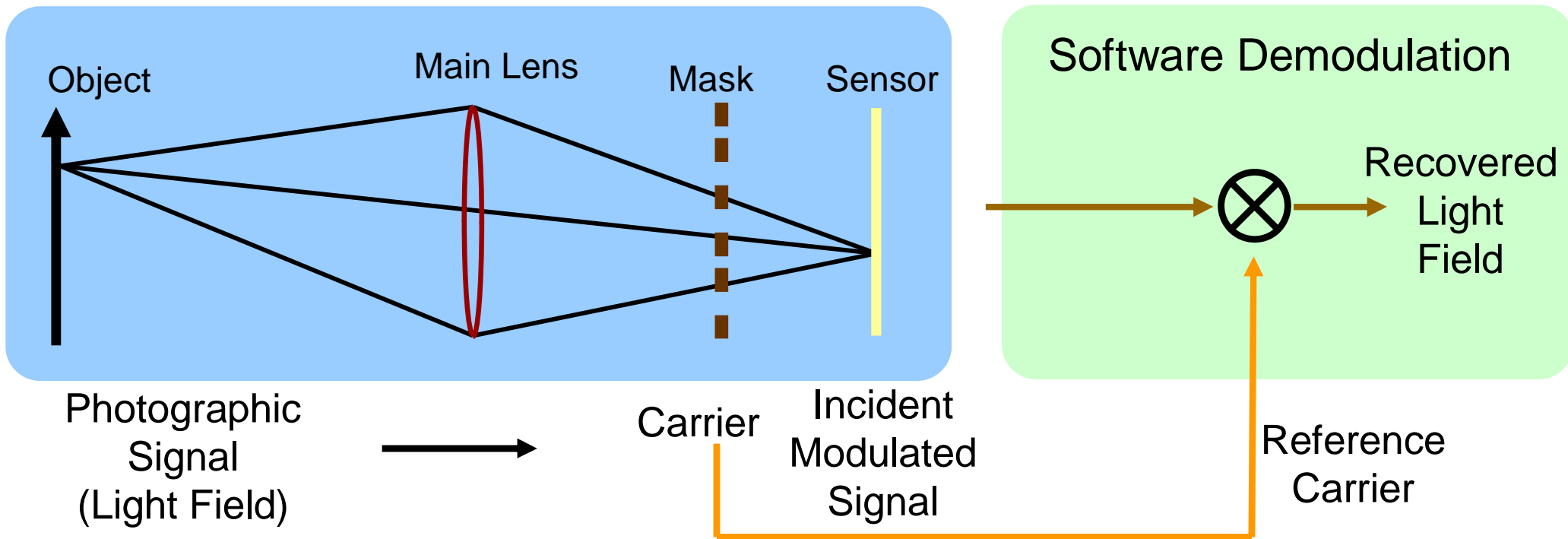
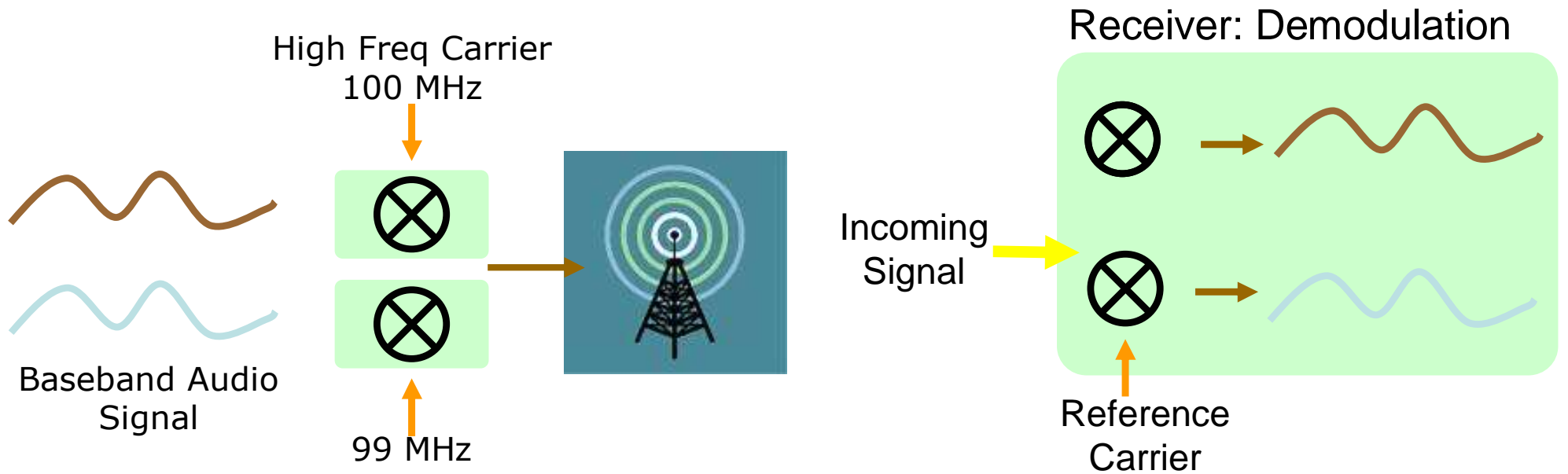
# Two-Plane Parameterization of Light Field



Levoy and Hanrahan 1996  
Gortler *et al.* 1996

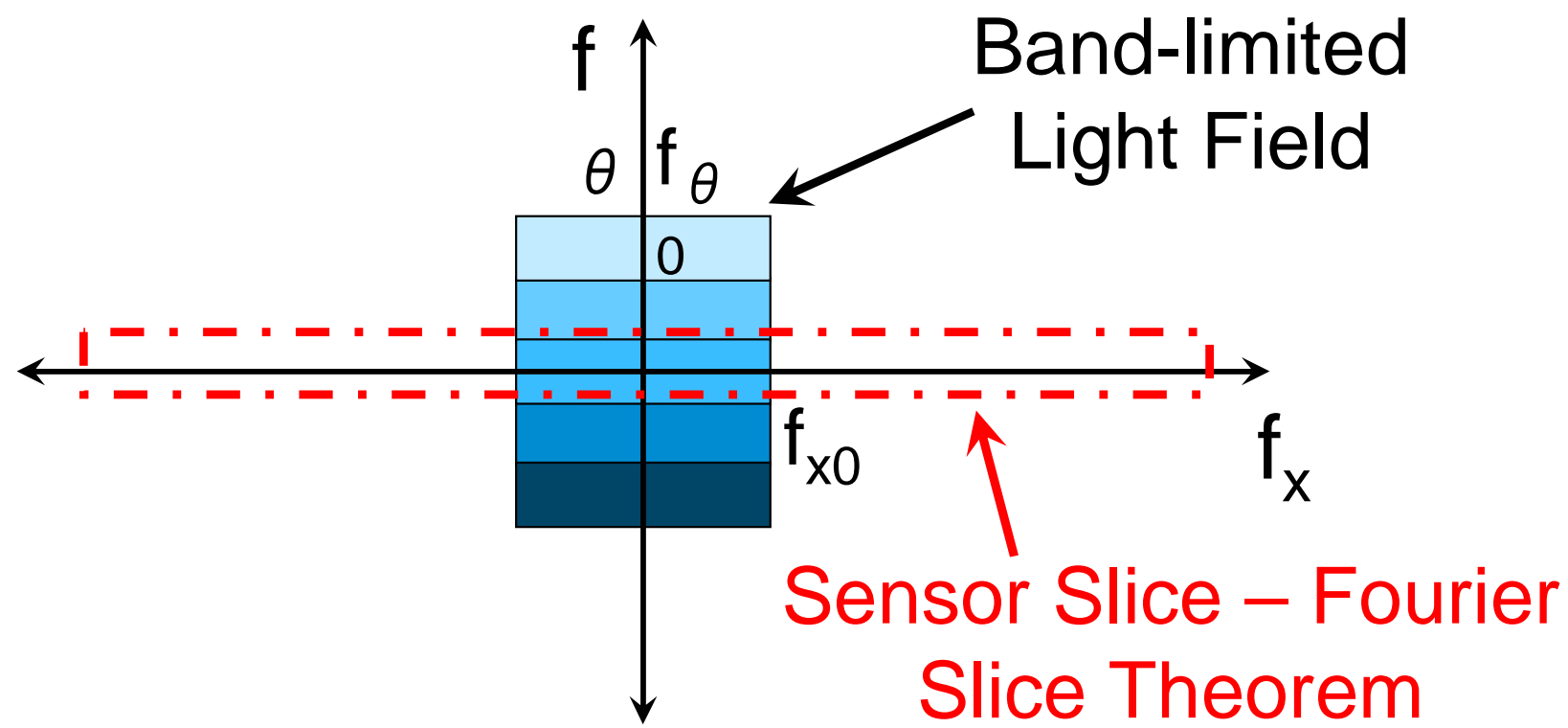


# Optical Heterodyning



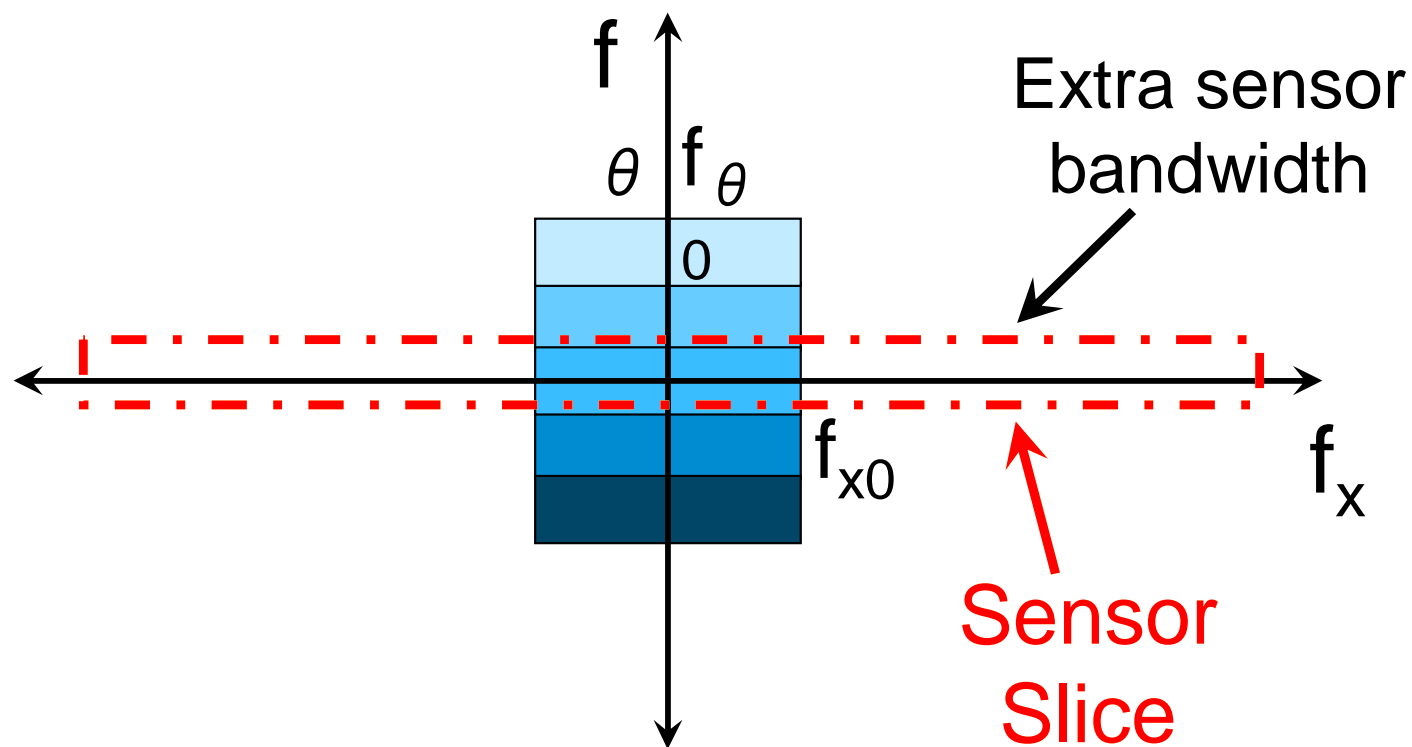


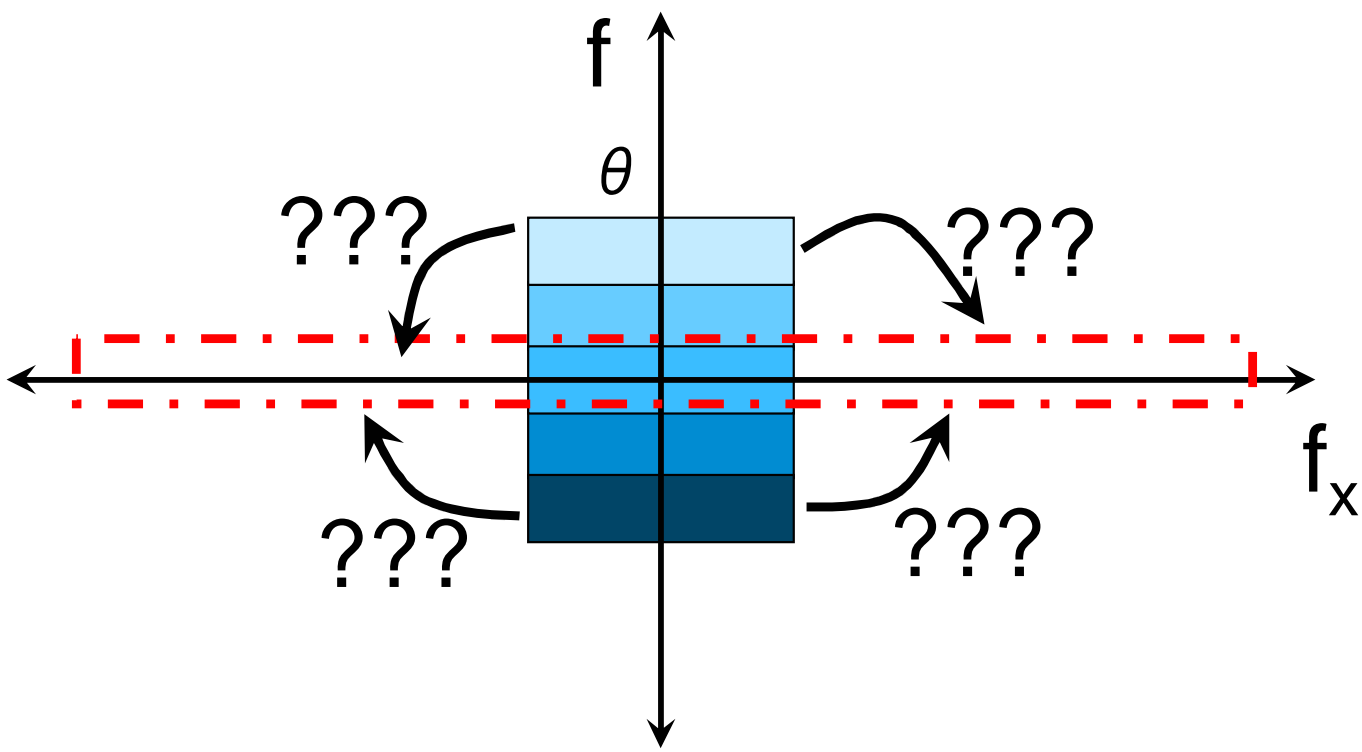
# How to Capture 2D Light Field with 1D Sensor ?



## Fourier Light Field Space

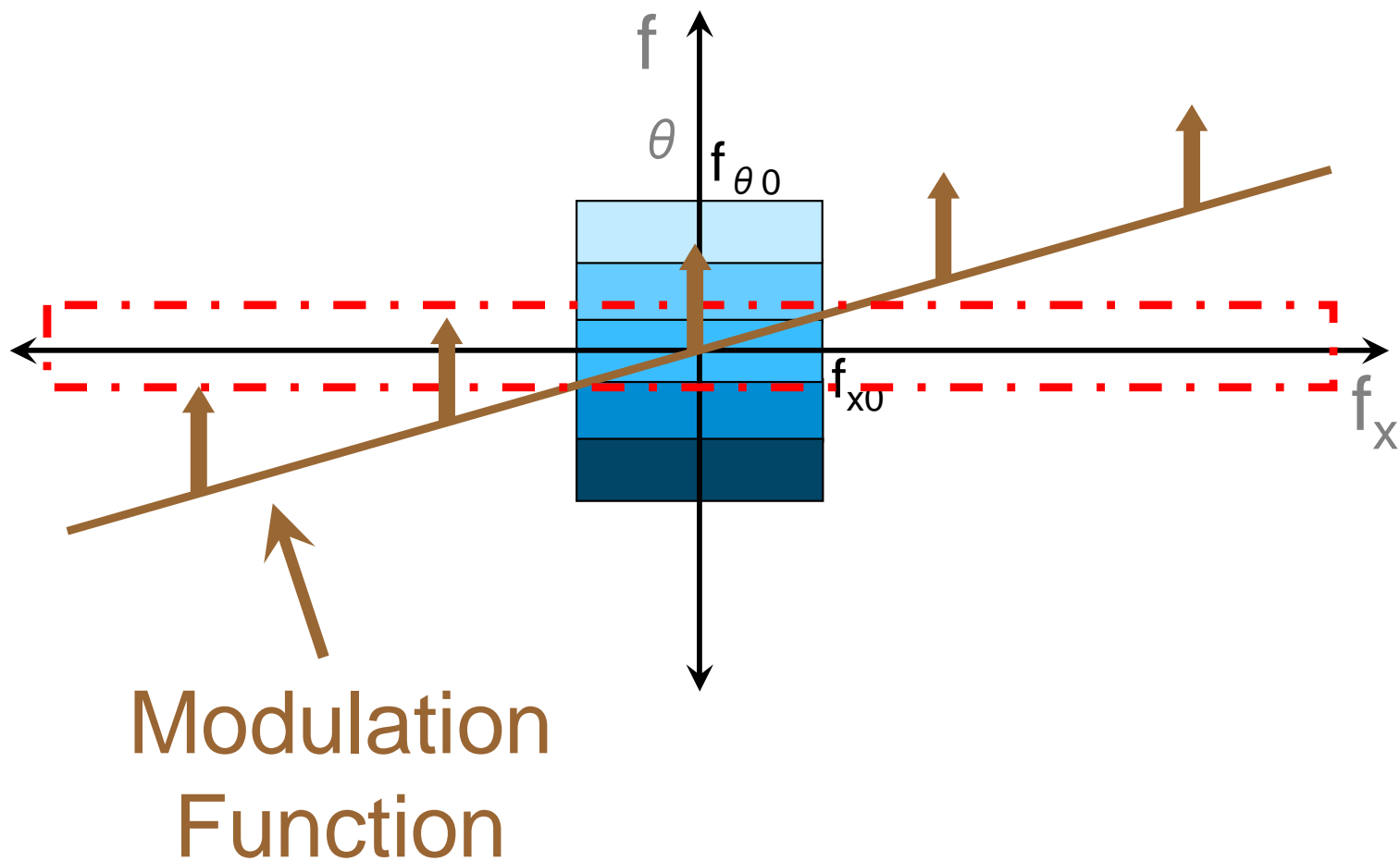
Extra sensor bandwidth cannot capture extra *dimension* of the light field



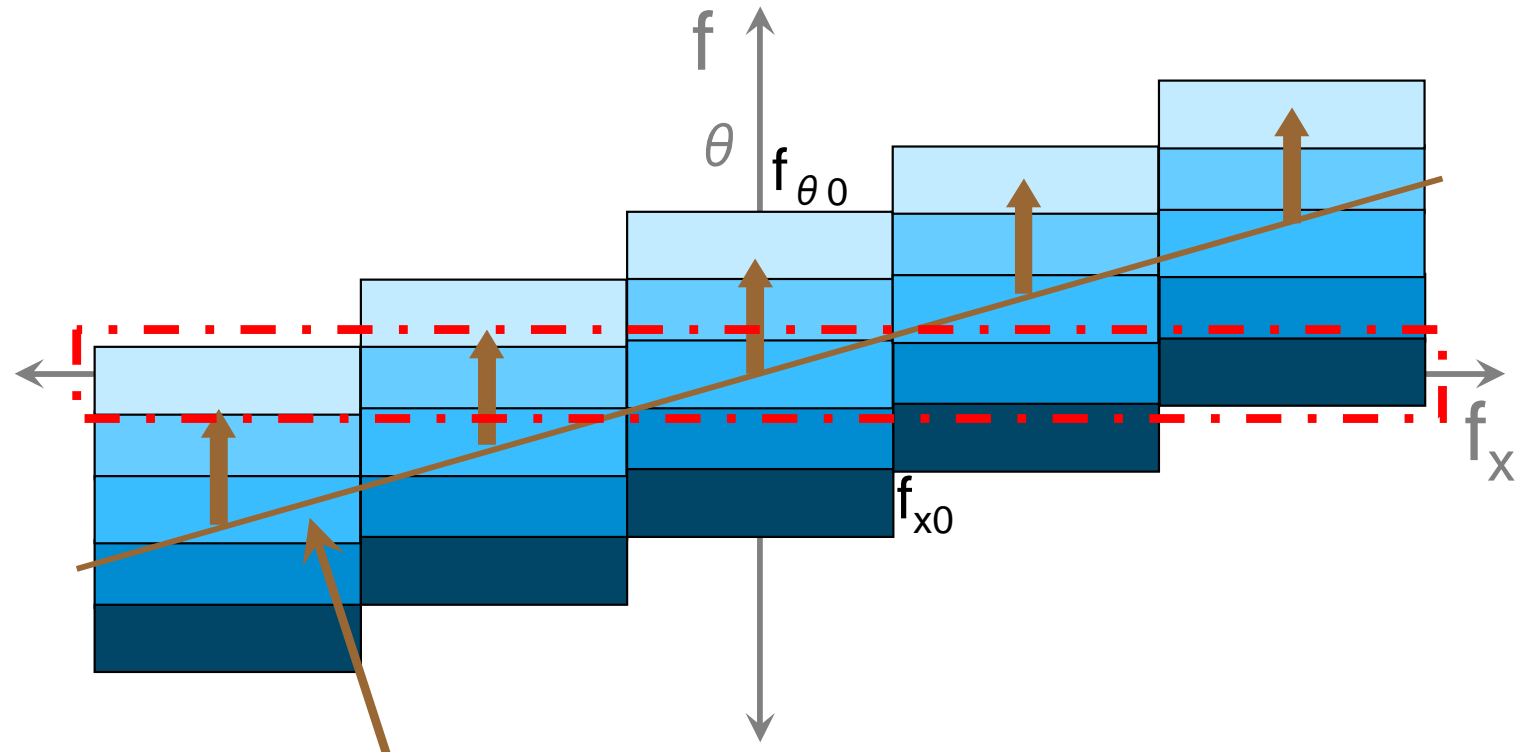


# Solution: Modulation Theorem

Make spectral copies of light field



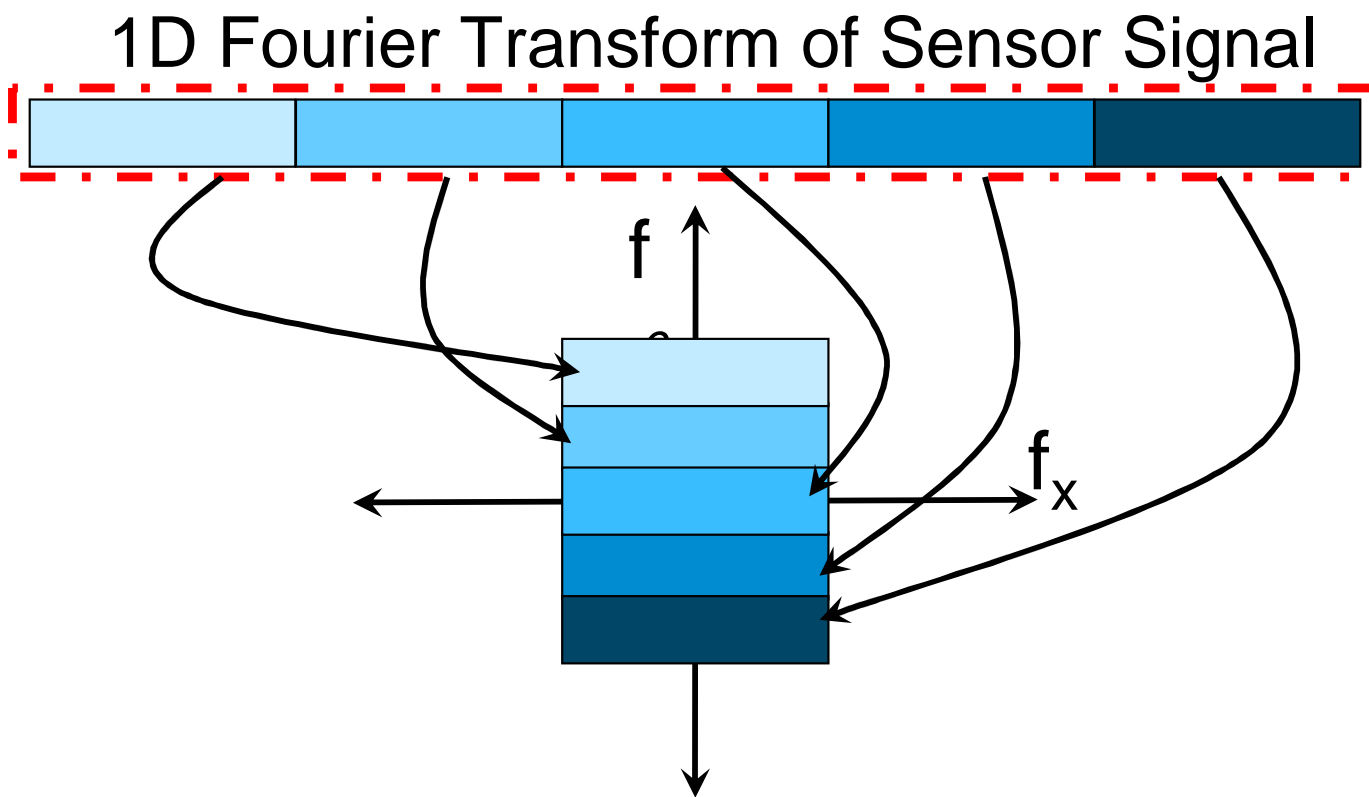
# Sensor Slice captures entire Light Field



Modulation  
Function

**Modulated Light Field**

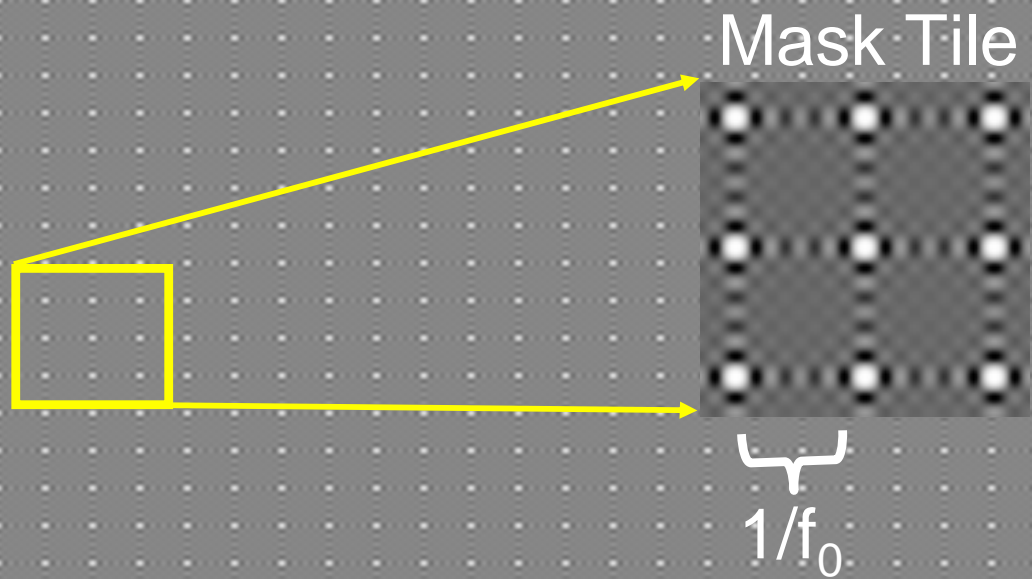
# Demodulation to recover Light Field



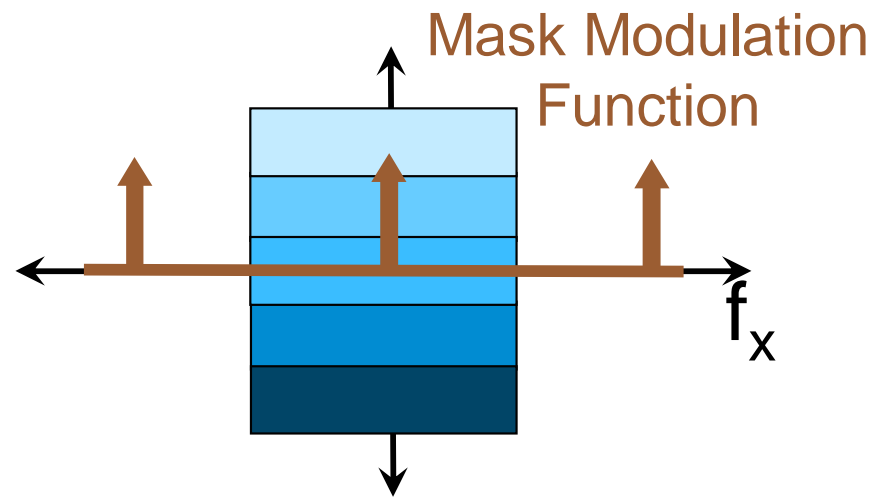
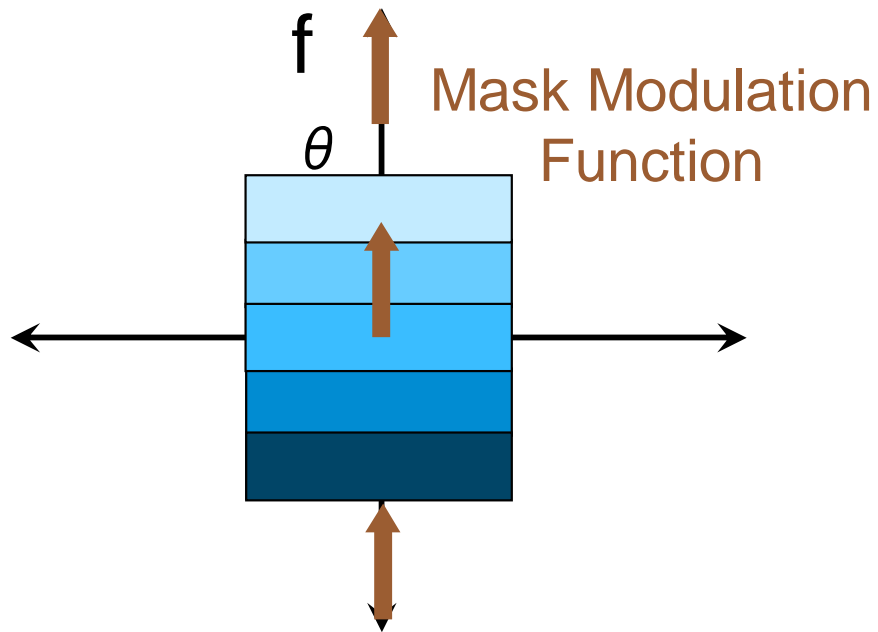
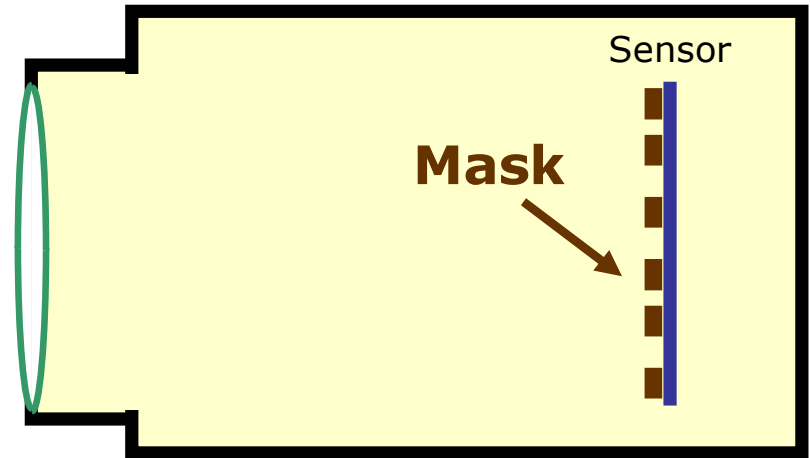
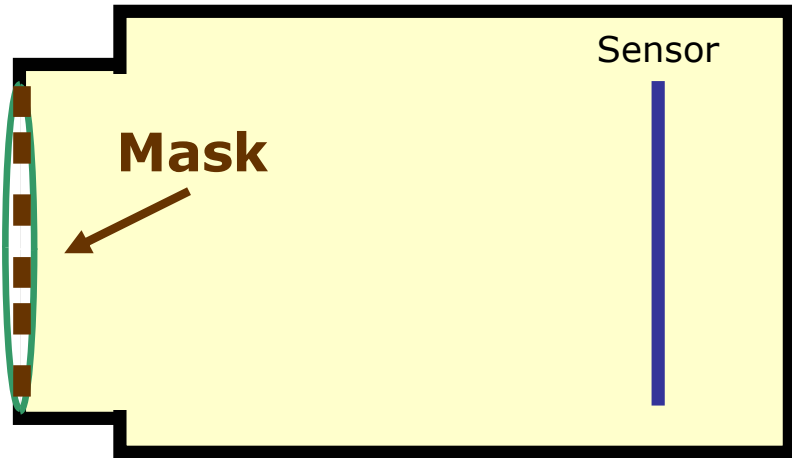
*Rearrange* 1D Fourier Transform into 2D



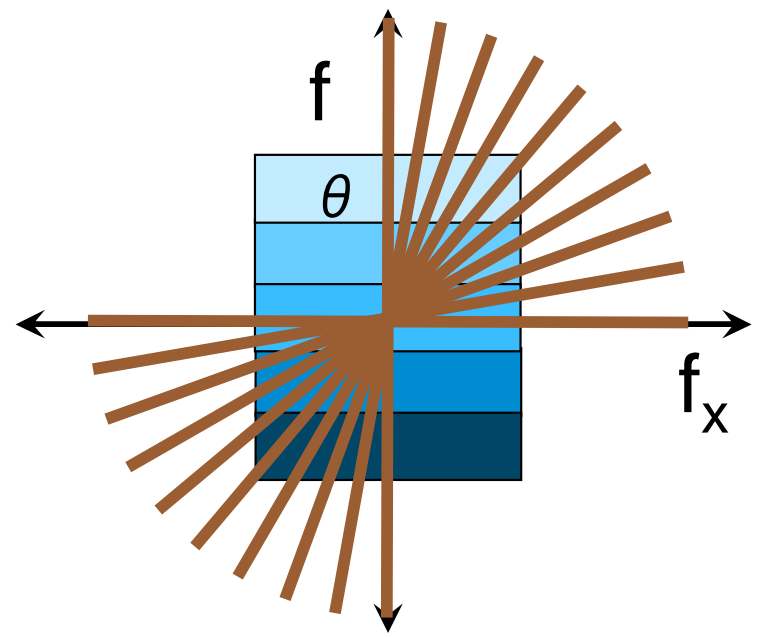
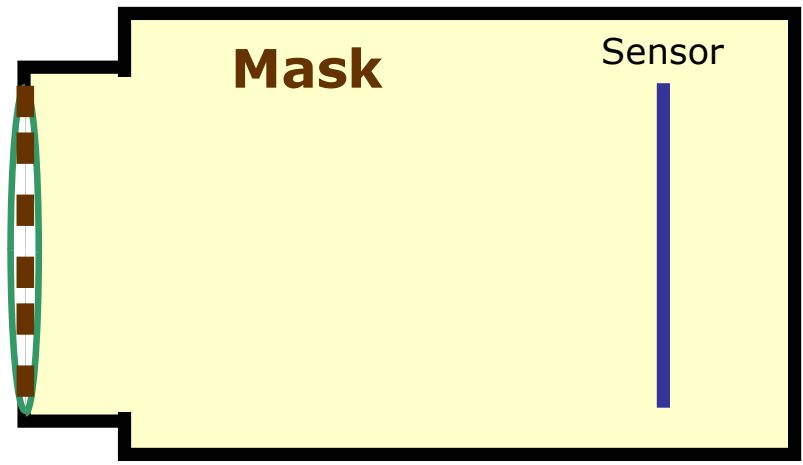
# Narrowband Cosine Mask Used



# Where to place the Mask?

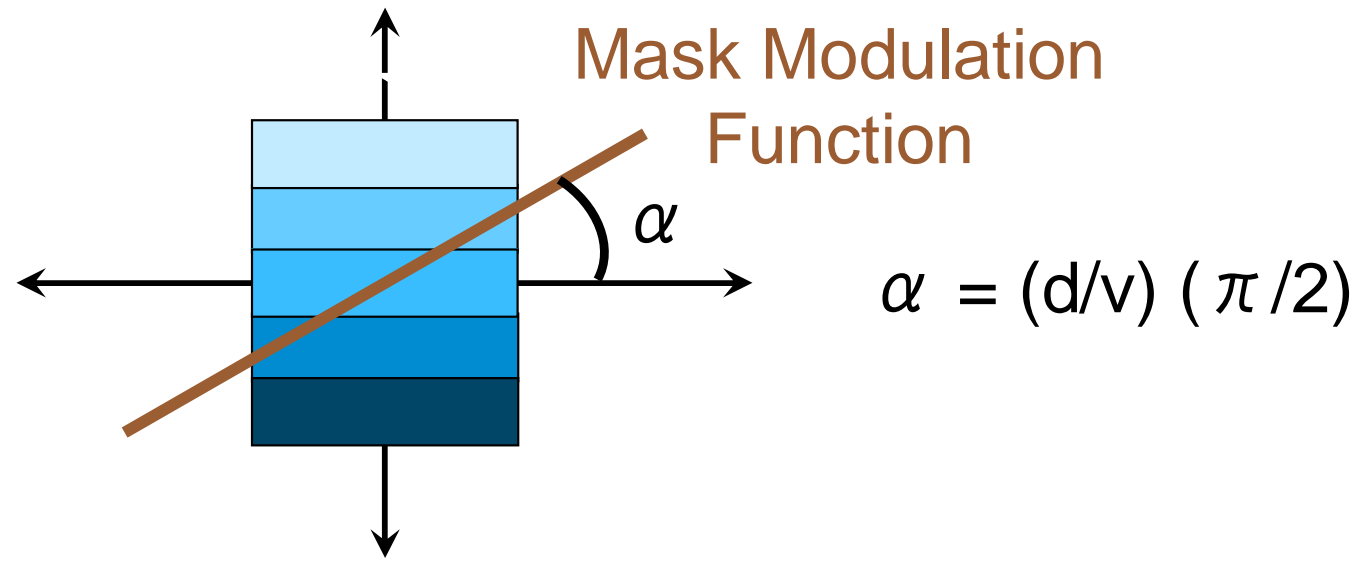
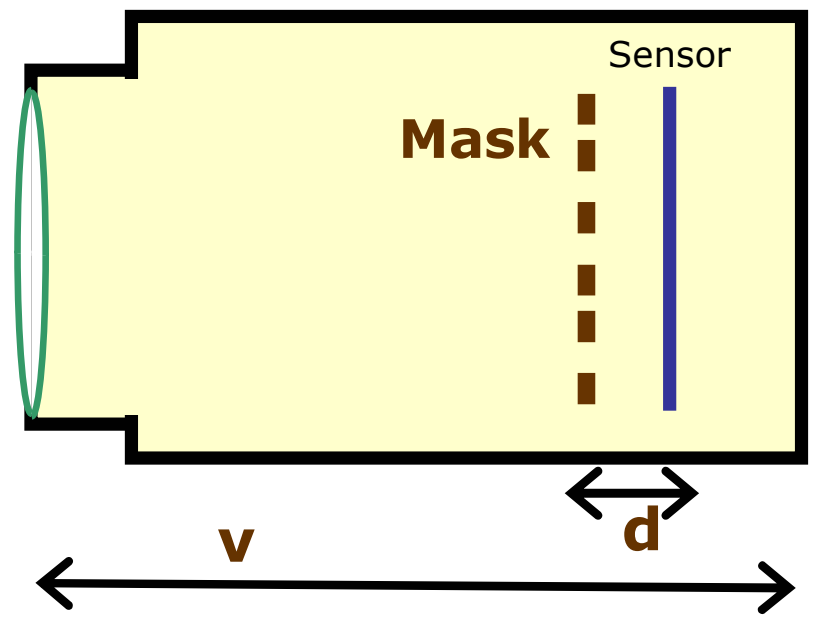


# Where to place the Mask?



Mask  
Modulation  
Function

# Where to place the Mask?





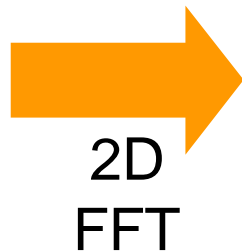
# Captured 2D Photo



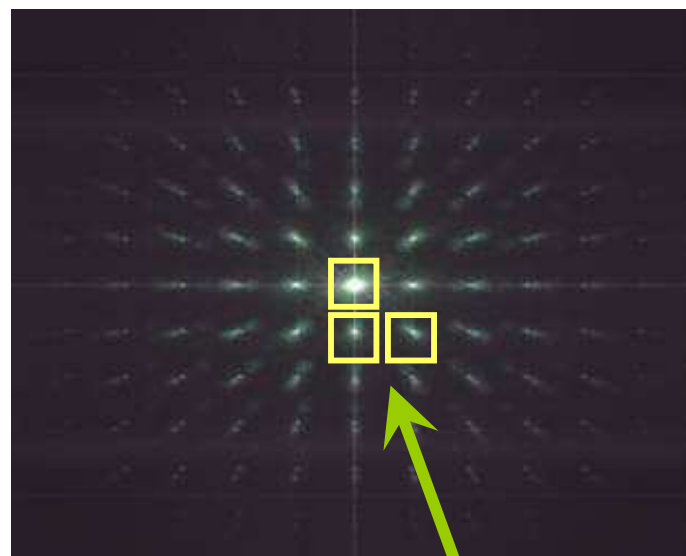
Encoding due to  
Cosine Mask

# Computing 4D Light Field

2D Sensor Photo, 1800\*1800



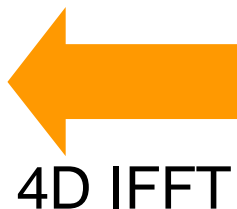
2D Fourier Transform, 1800\*1800



9\*9=81 spectral copies



Rearrange 2D tiles into 4D planes  
200\*200\*9\*9



4D Light Field

200\*200\*9\*9



# 4d light-field capture results

Captured Photo



Refocusing

Changing Views



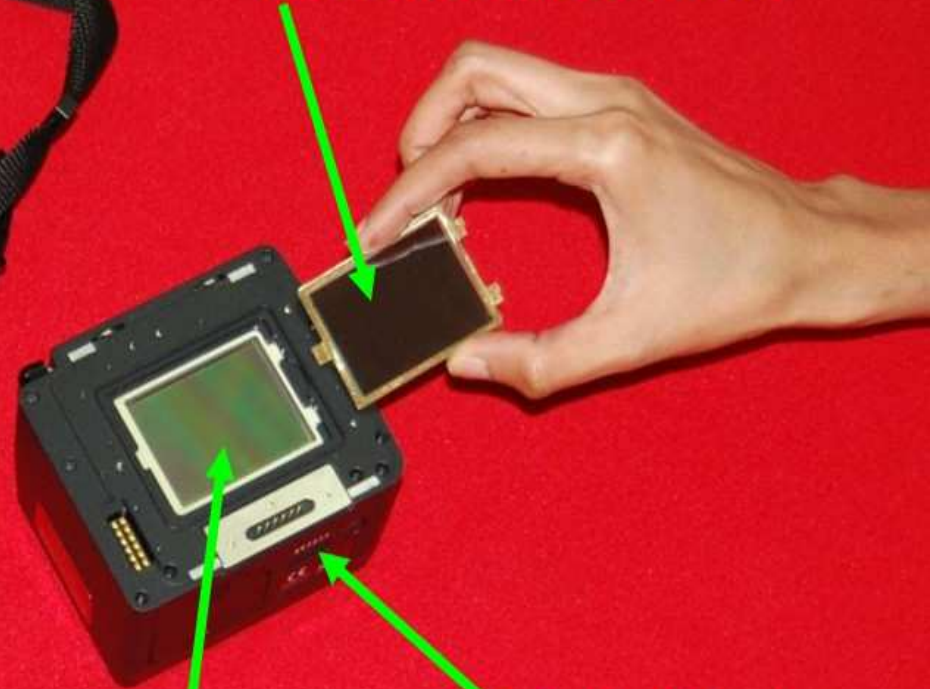
*“Dappled Photography: Mask Enhanced Cameras for Heterodyned Light Fields and Coded Aperture Refocusing”*, Ashok Veeraraghavan, Ramesh Raskar, Amit Agrawal, Ankit Mohan, and Jack Tumblin, in **SIGGRAPH 2007**.

*“Non-refractive modulators for encoding and capturing scene appearance and depth”*, Ashok Veeraraghavan, Ramesh Raskar, Amit Agrawal, Ankit Mohan, and Jack Tumblin, in **IEEE CVPR 2008**.



Camera Body

Mask is placed under a glass sheet and slid over the bare sensor.



Bare Sensor

Digital Back

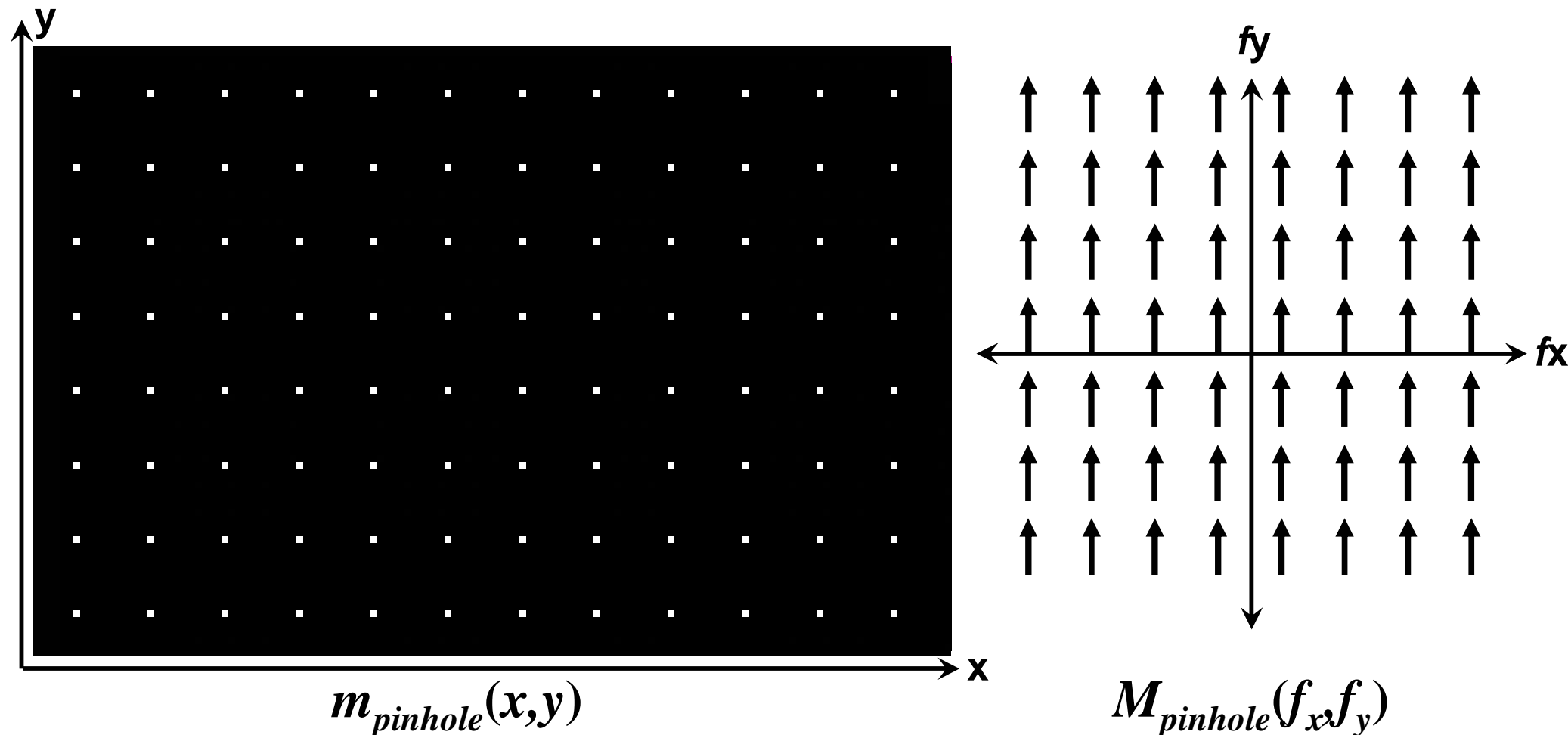


210 mm Lens



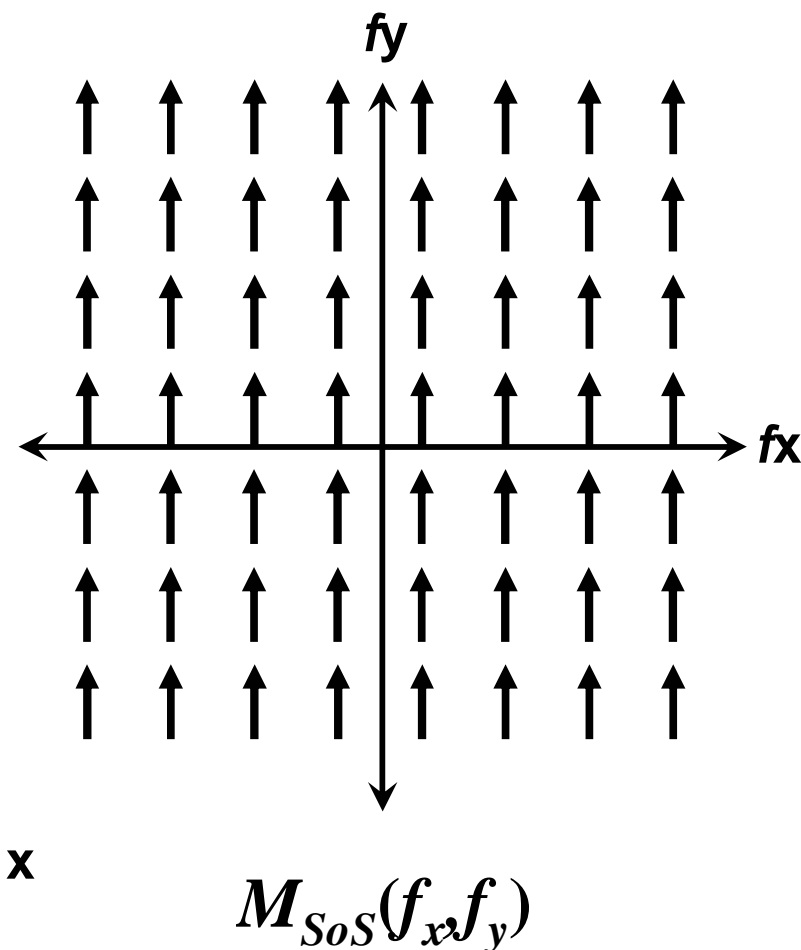
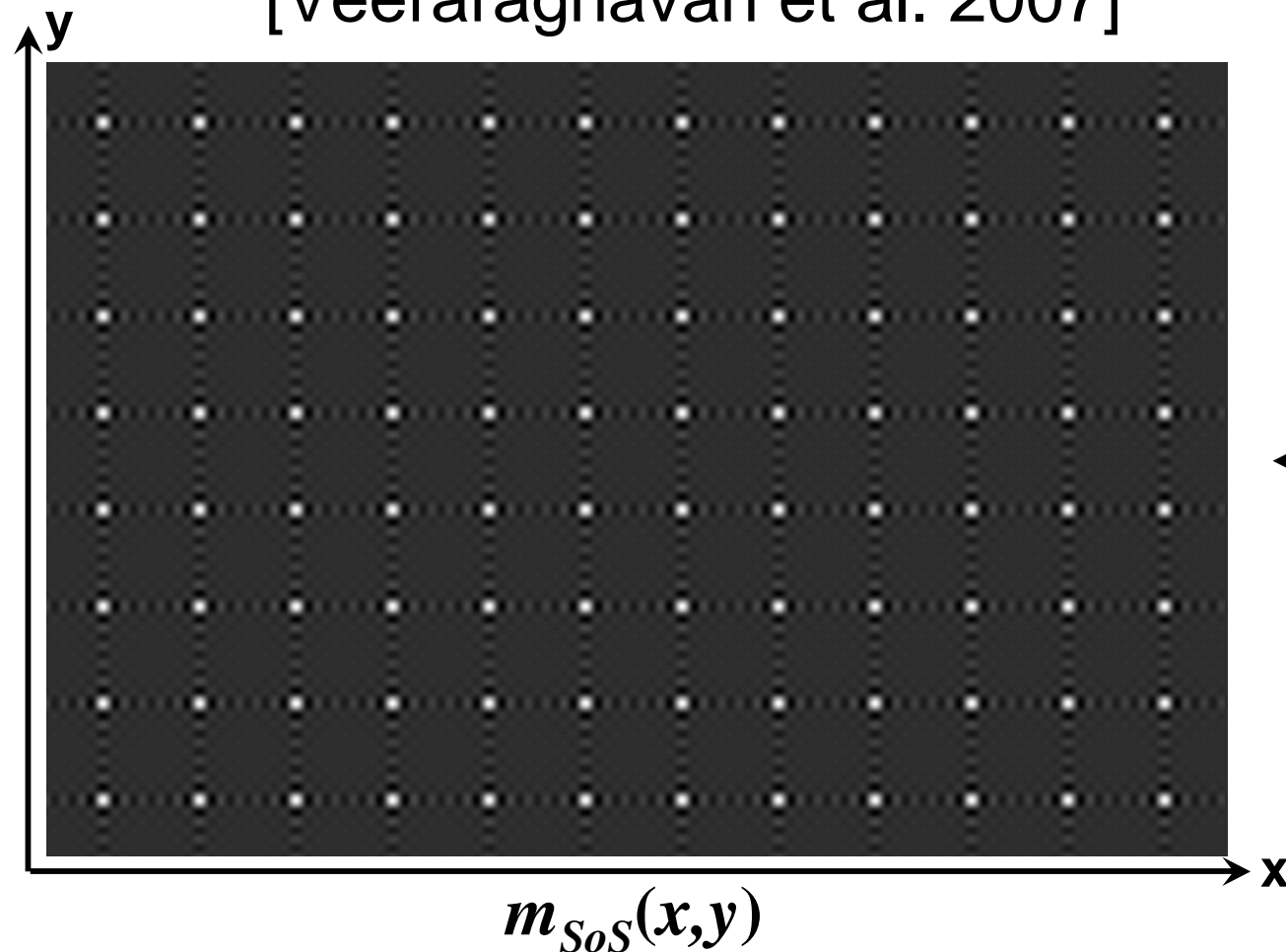
# Which Heterodyne Mask to Use?

- **Conditions for heterodyne light field detection**
  - Mask spectrum must be a (windowed) 2D impulse train
  - Can be achieved (approximately) with a **pinhole array**



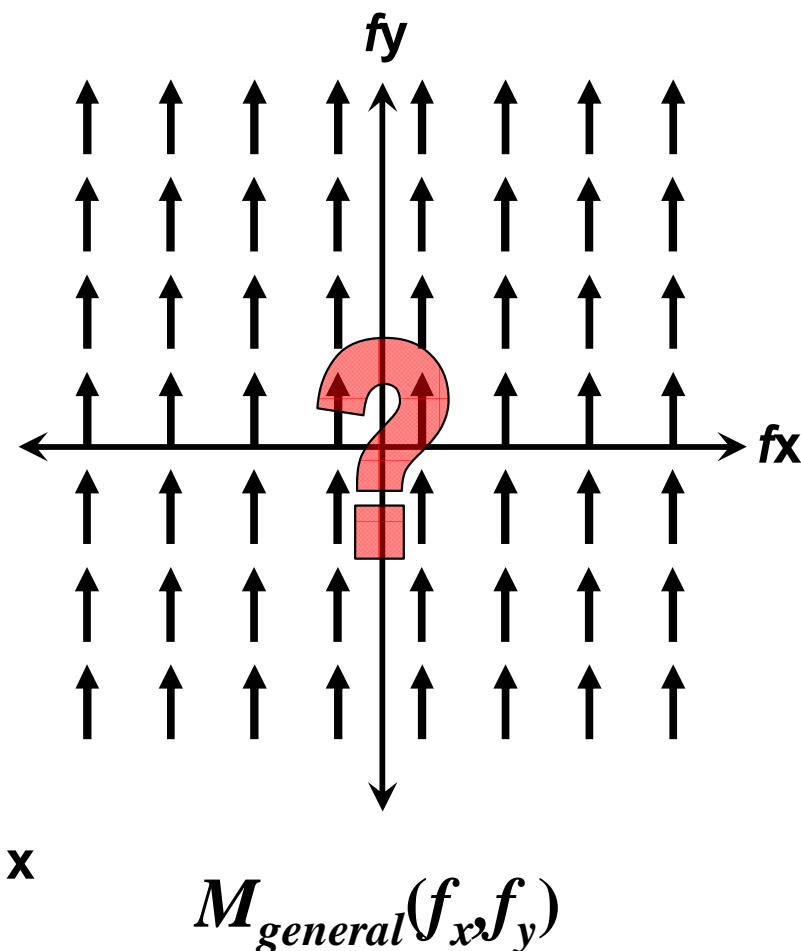
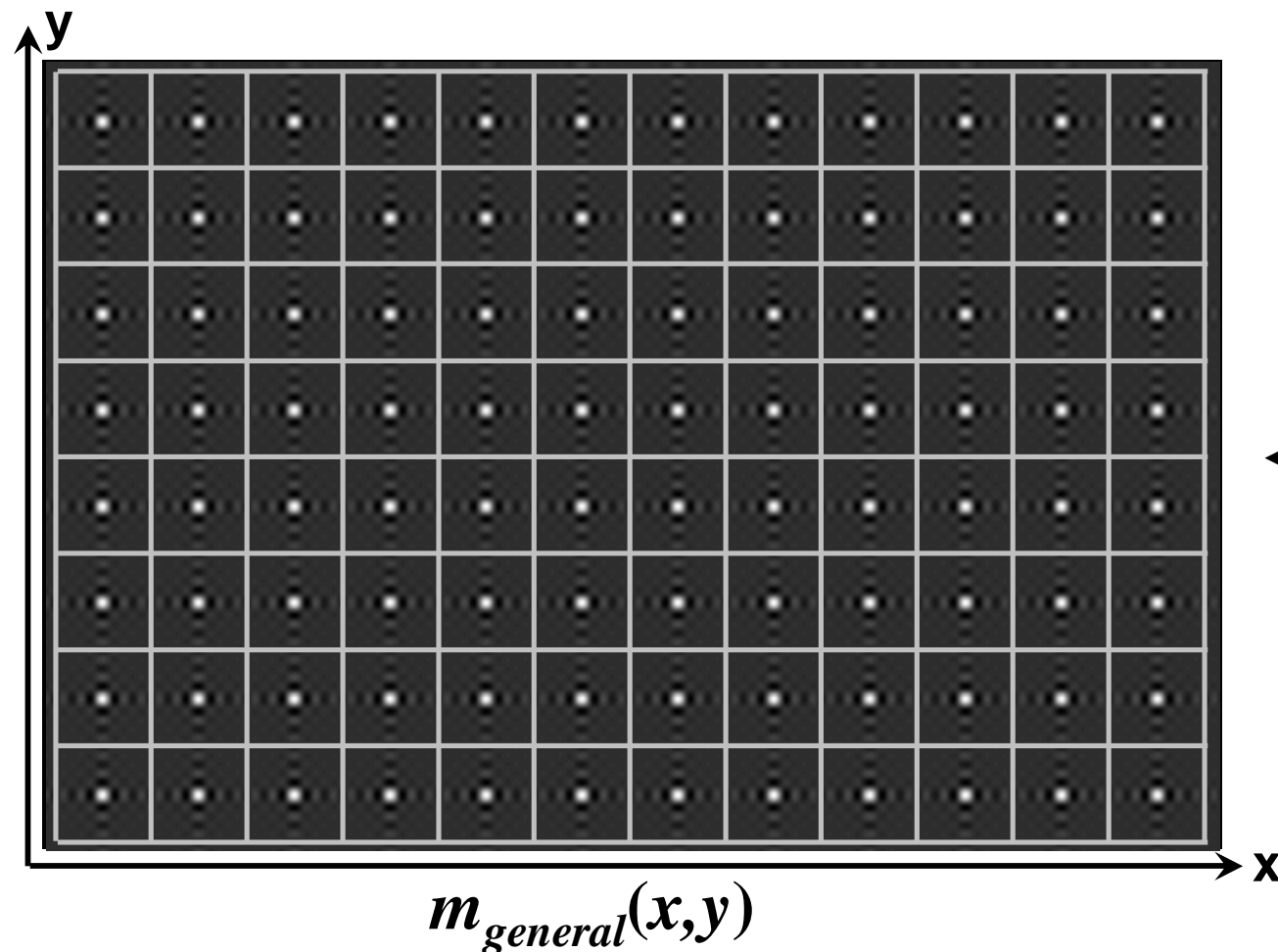
# Which Heterodyne Mask to Use?

- **Conditions for heterodyne light field detection**
  - Mask spectrum must be a (windowed) 2D impulse train
  - Can be achieved exactly by **Sum-of-Sinusoids (SoS)** [Veeraraghavan et al. 2007]



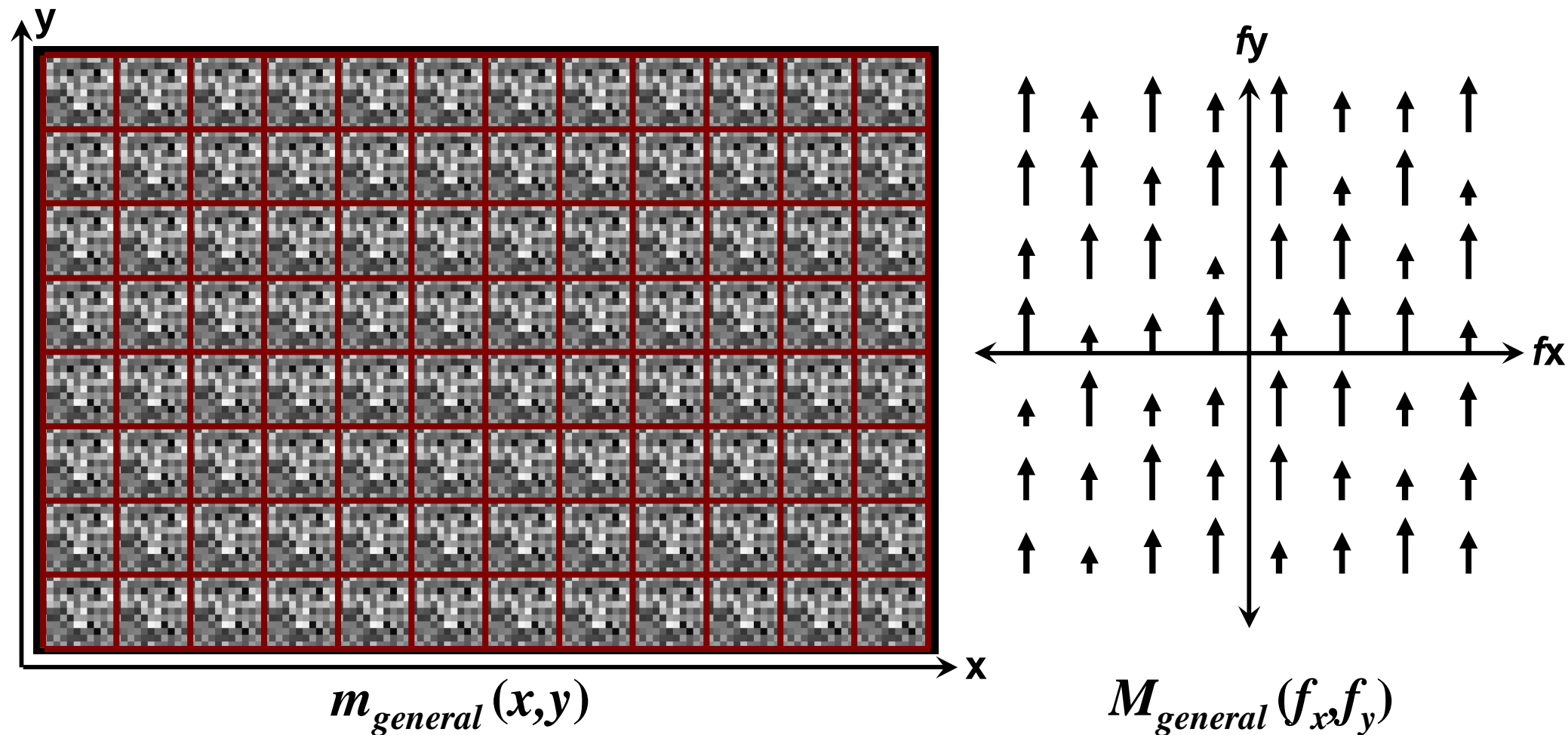
# Which Heterodyne Mask to Use?

- **Conditions for heterodyne light field detection**
  - Both pinhole array and SoS are *periodic* functions
  - What other tiles lead to impulse trains?



# General Tiled-broadband Masks

- **Conditions for heterodyne light field detection**
  - (Almost) any 2D tile can be used (tiling  $\rightarrow$  impulse train)
  - Amplitude of impulses given by Fourier series of tile



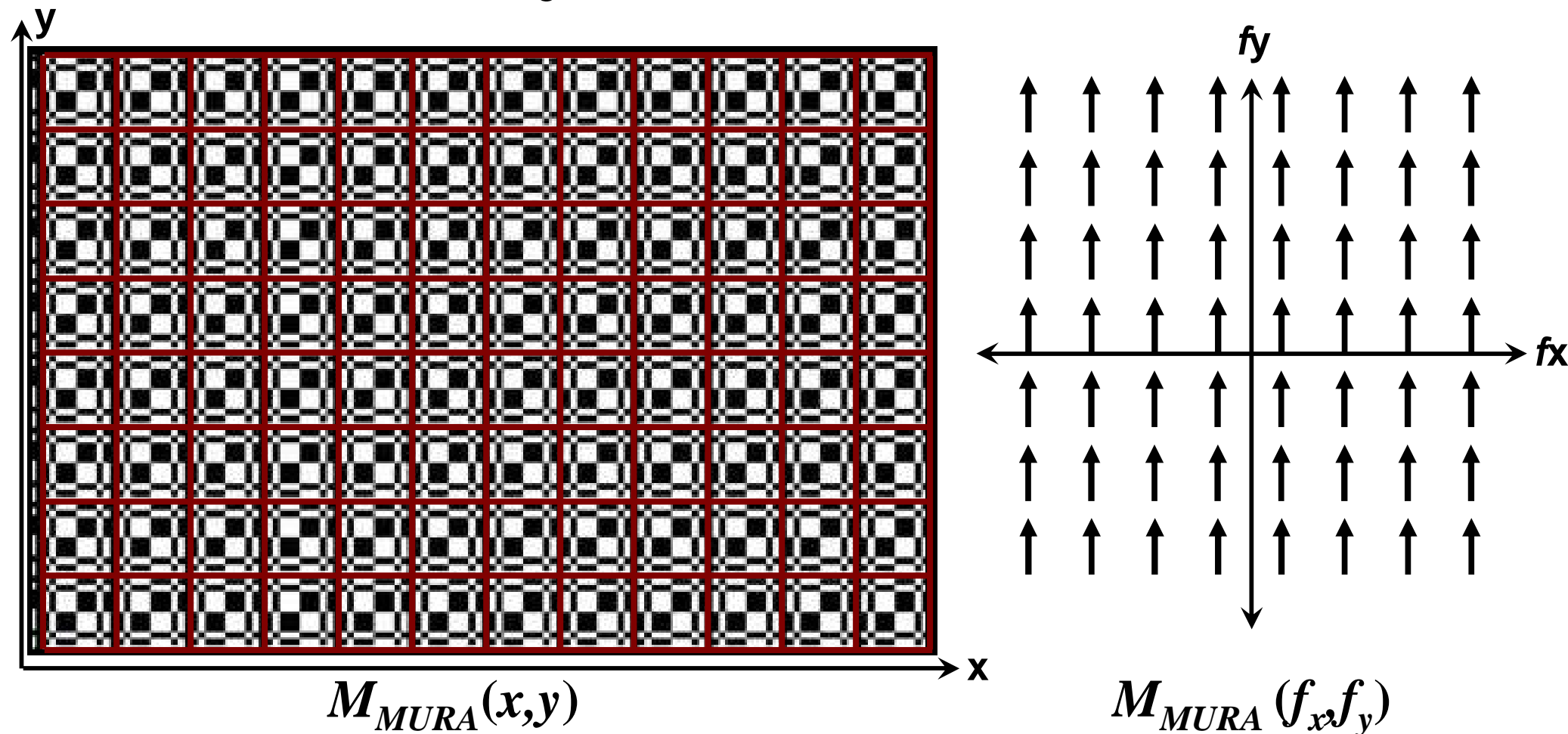


# Specific Choice: Tiled-MURA

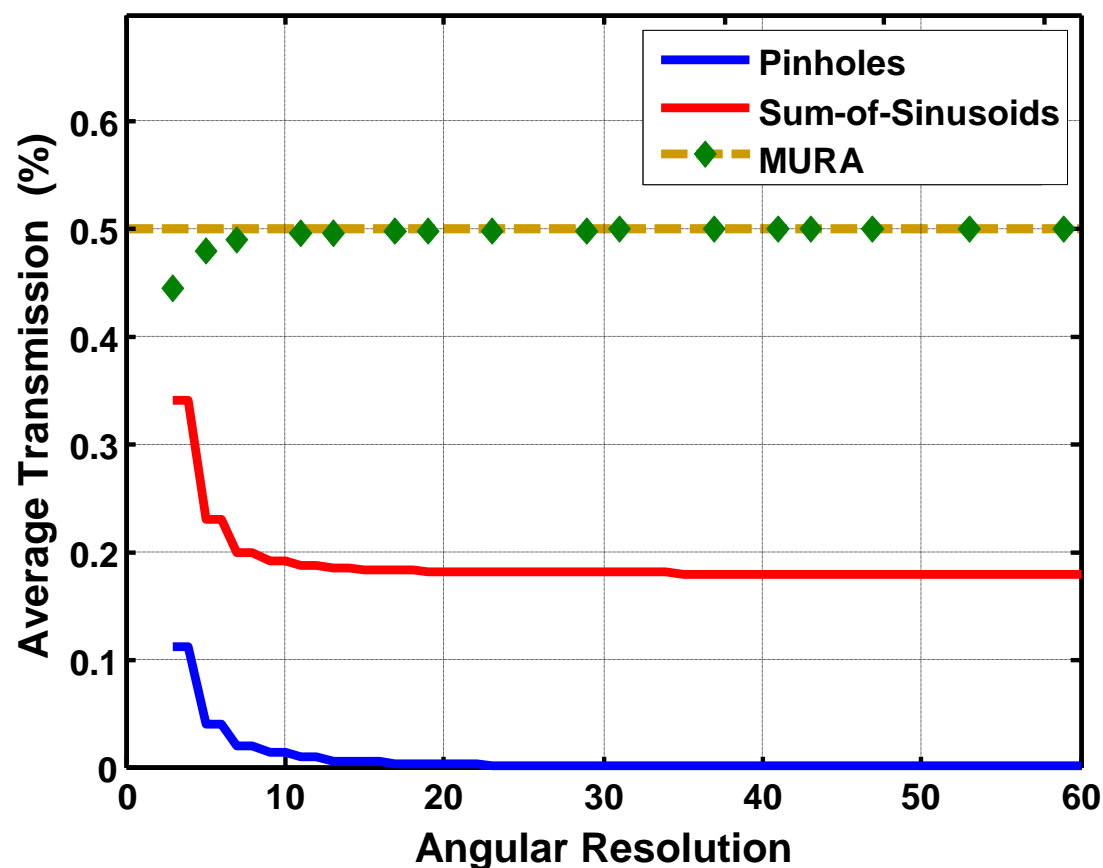
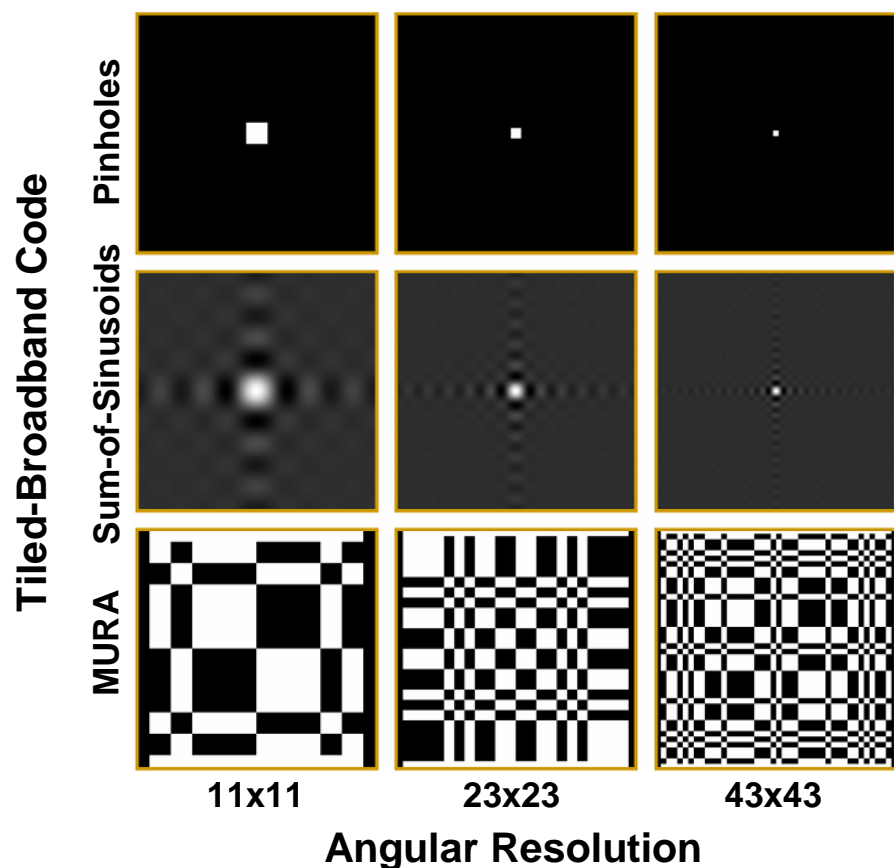
- Conditions for optimal heterodyne light field detection

## Modified Uniformly Redundant Array (MURA)

“Shield Fields: Modeling and Capturing 3D Occluders”, Douglas Lanman, Ramesh Raskar, Amit Agrawal, Gabriel Taubin, in **SIGGRAPH Asia 2008**.



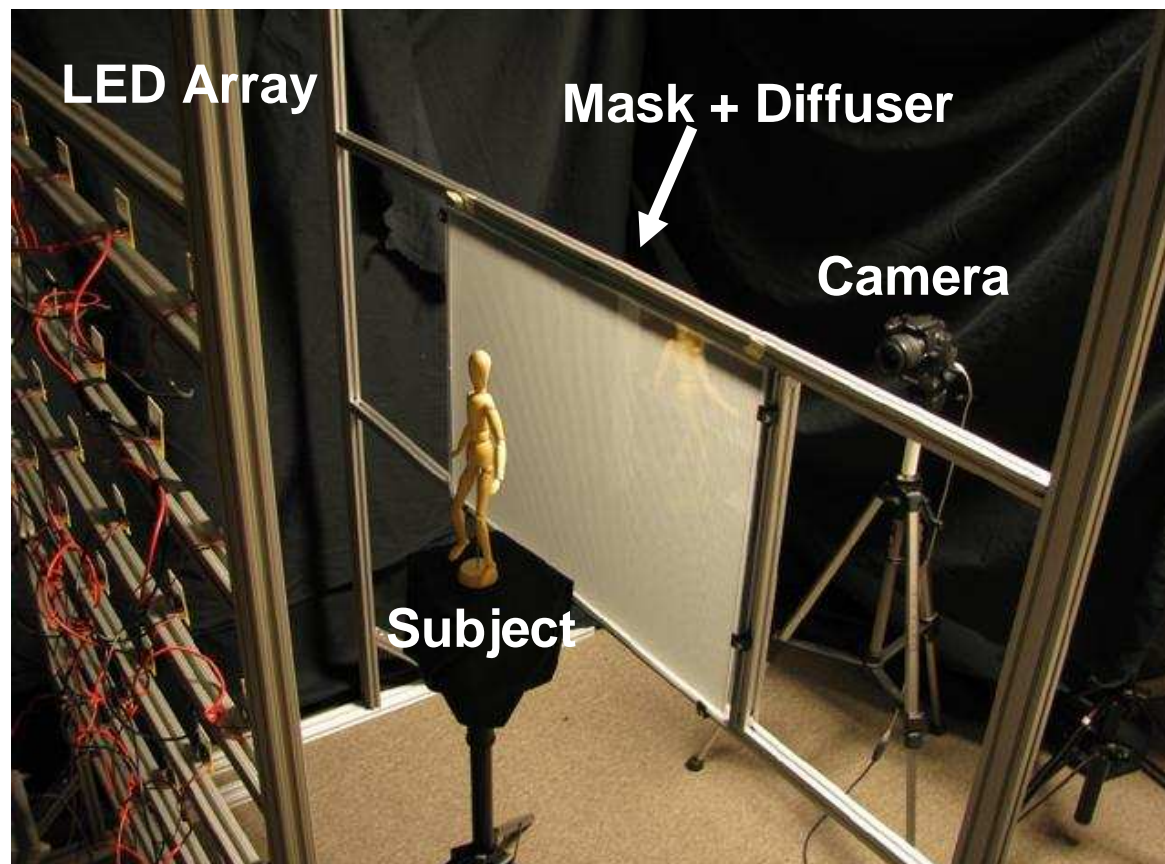
# Benefits of New Heterodyne Codes



## • Benefits and Limitations

- Sum-of-Sinusoids converges to  $\approx 18\%$  transmission
- Tiled-MURA near 50% (but only for prime-lengths)
- Binary vs. continuous-tone process (quantization)

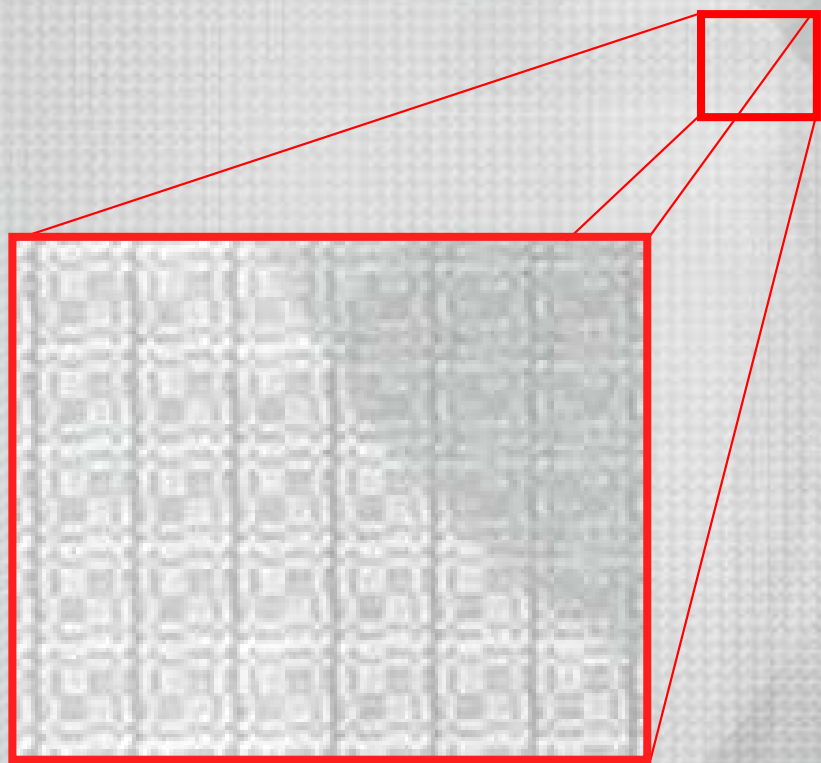
# Prototype Implementation



- **Components**

- 8.0 megapixel Canon EOS Digital Rebel XT
- 6x6 array of Philips Luxeon Rebel LEDs [1.2x1.2 m]
- 5,080 DPI mask and a paper vellum diffuser [75x55 cm]

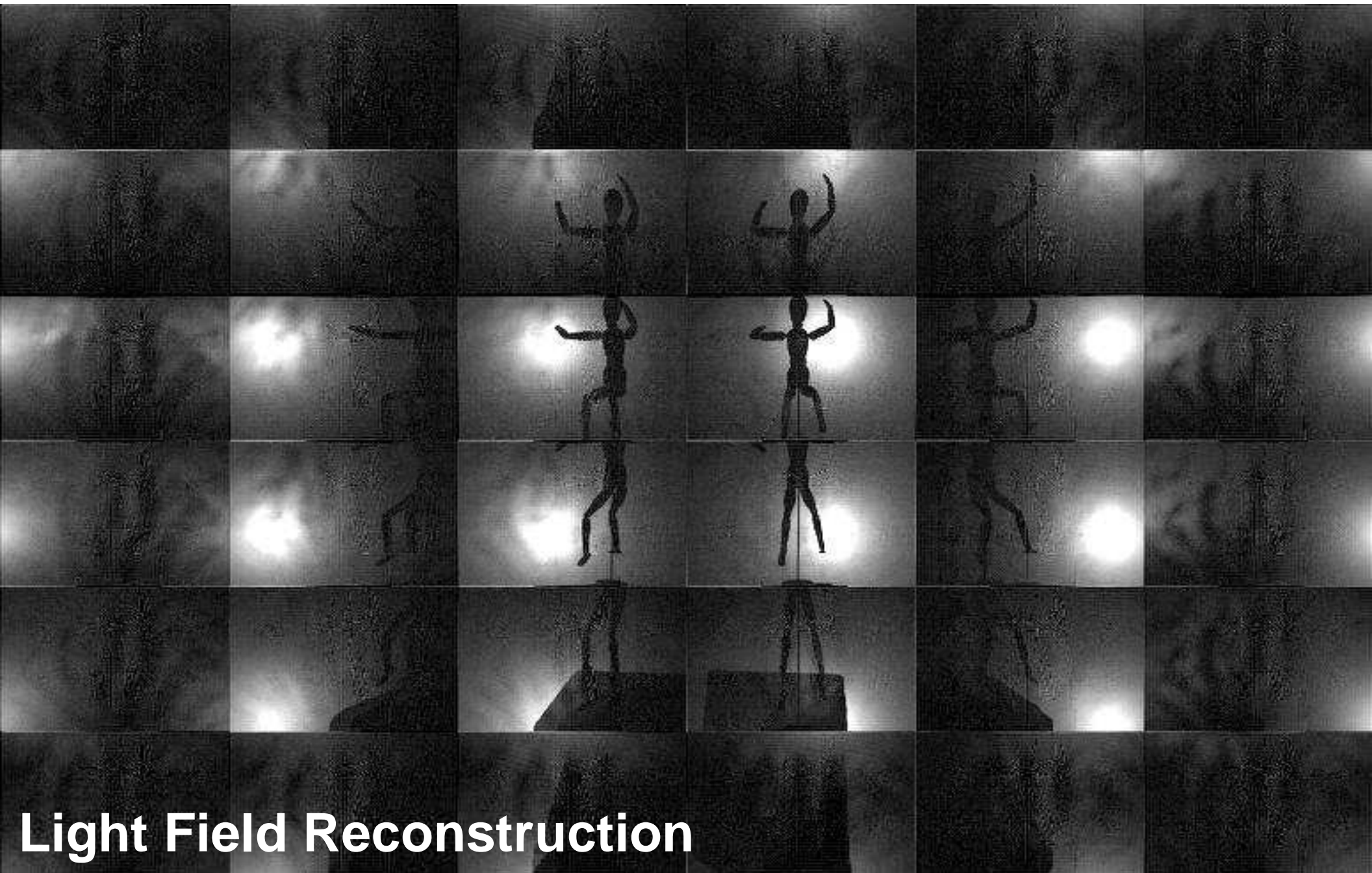
# Tiled-MURA Results: Sensor Image



**High-Resolution Sensor Image (0.25 sec. Exposure)**



# Tiled-MURA Results: Shadowgrams



**Light Field Reconstruction**

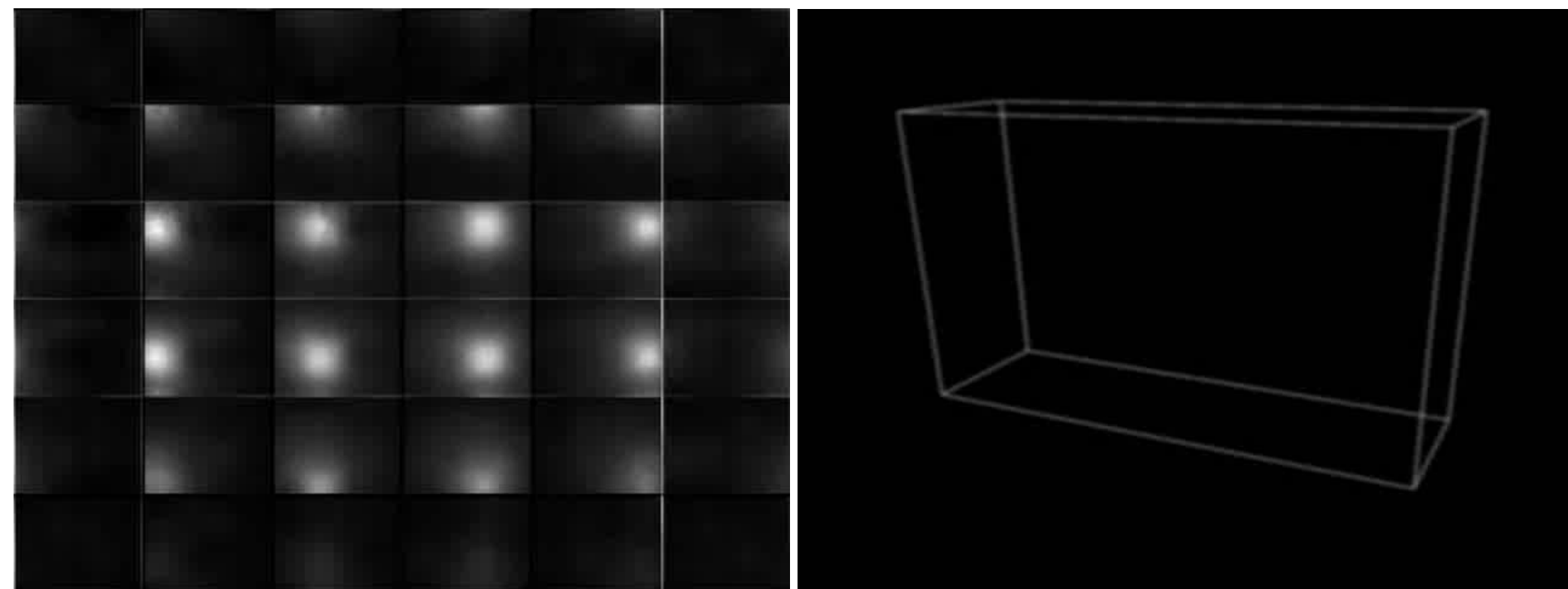
# Reconstruction



**Visual Hull Reconstruction**



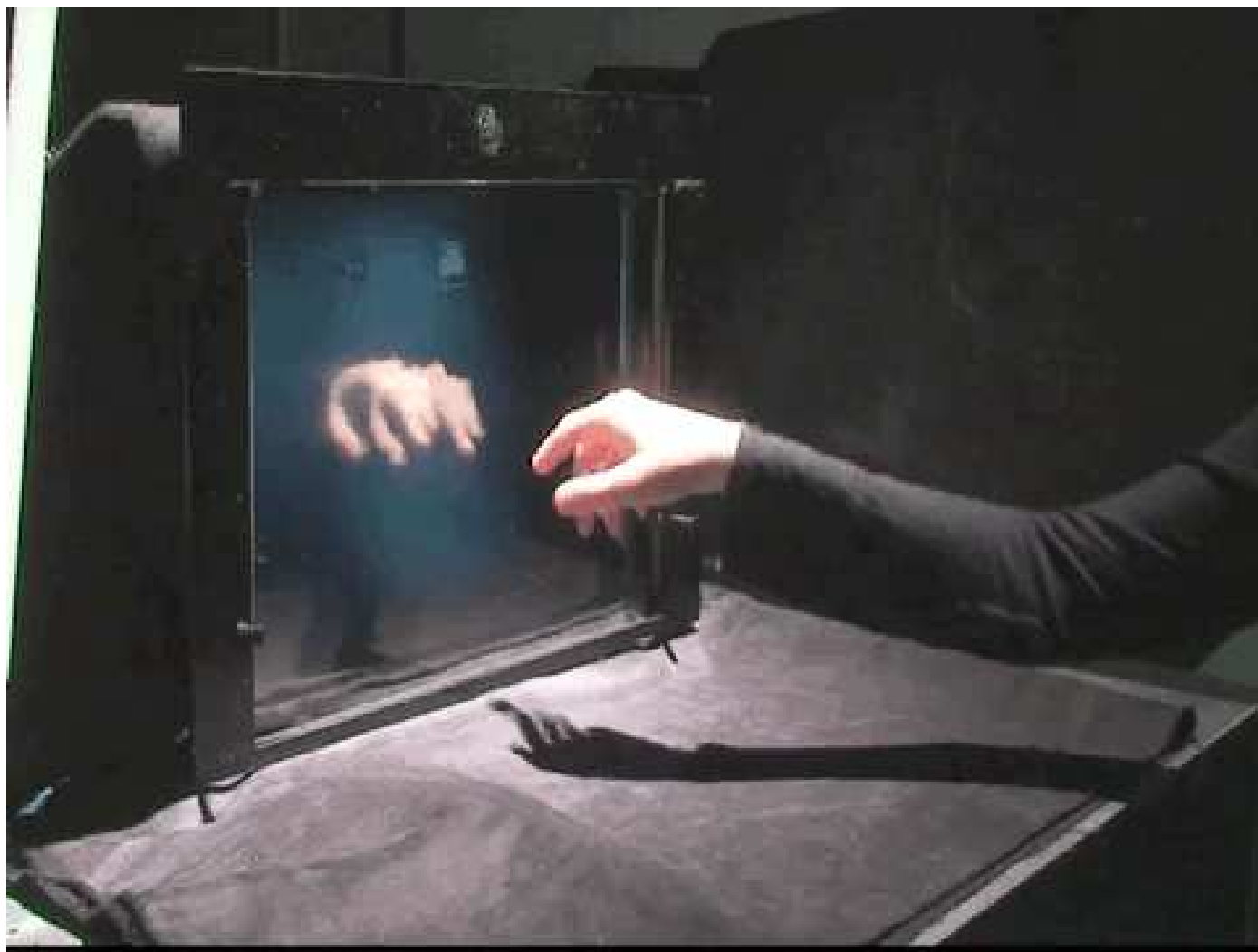
# Tiled-MURA Results: Dynamic Scene



- **Components and Limitations**

- 1600x1200 15 fps Point Grey Grasshopper camera
- 6x6 array of Philips Luxeon Rebel LEDs [1.2x1.2 m]
- 5,080 DPI mask and a paper vellum diffuser [75x55 cm]
- Individual shadowgrams **only 75x50 pixels**

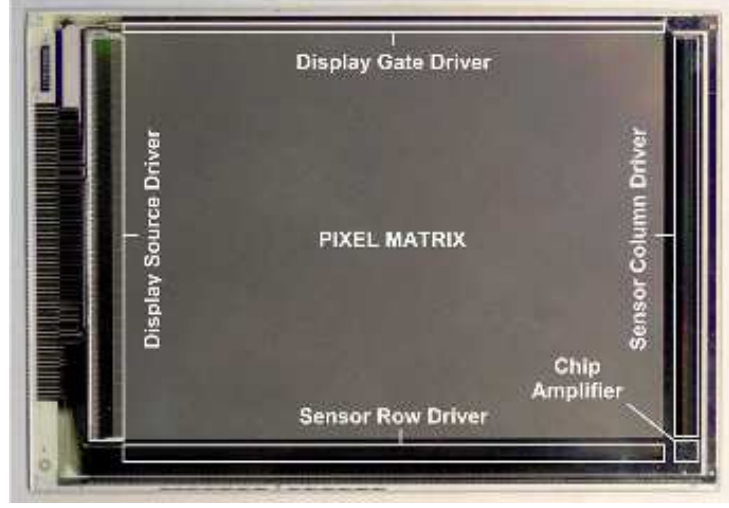
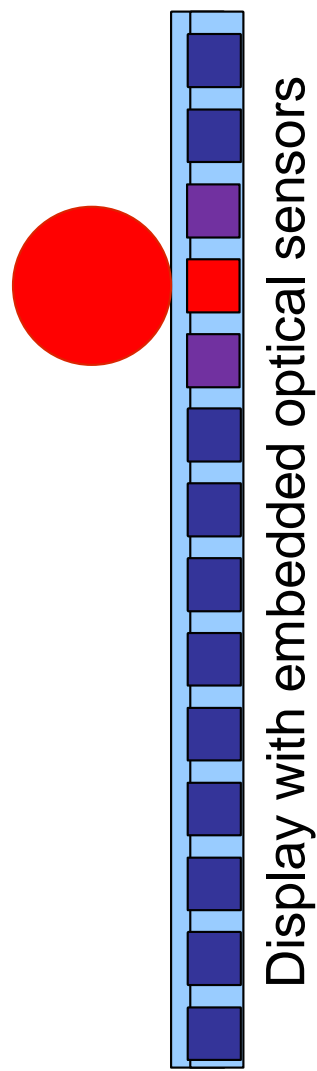
# Bi-Di Screen: Light Field capture with a flat display for **User Interaction**



*“BiDi Screen: A Thin, Depth-Sensing LCD for 3D Interaction using Light Fields”, Matthew Hirsch, Douglas Lanman, Henry Holtzman, Ramesh Raskar, in **SIGGRAPH Asia 2009**.*

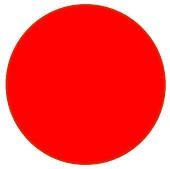
# BiDi Screen

Sharp Microelectronics Optical Multi-touch Prototype

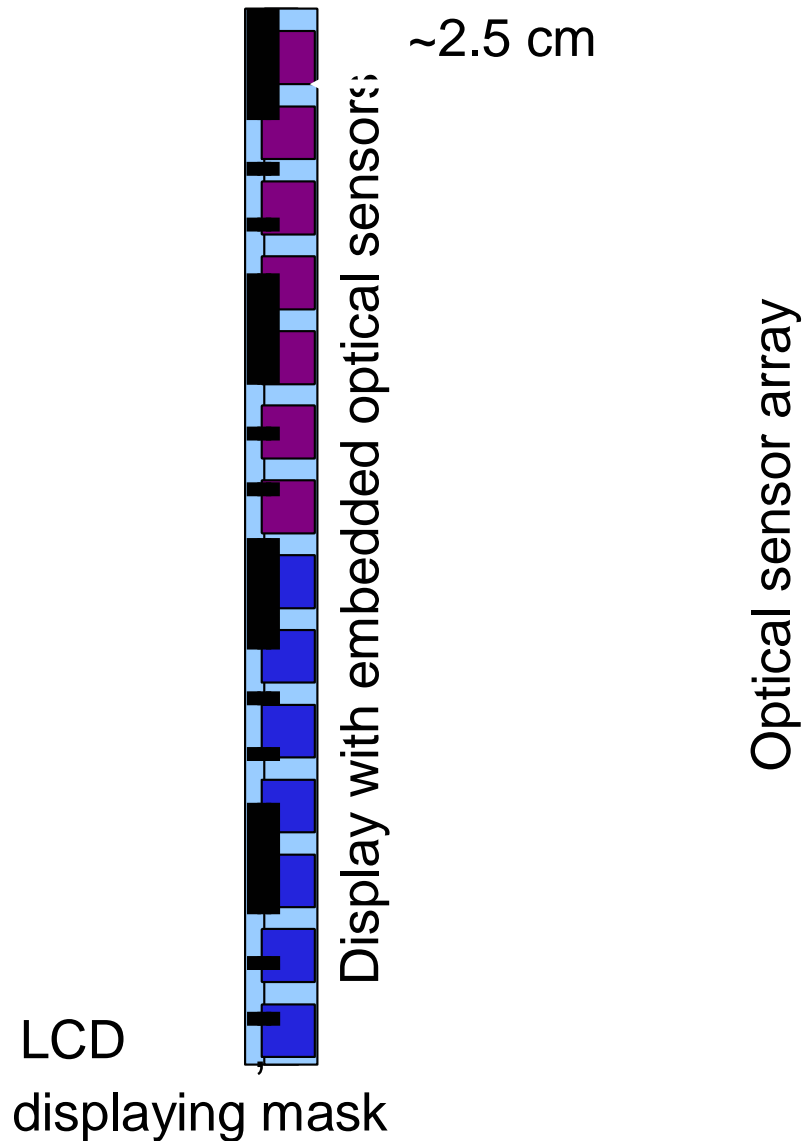


# BiDi Screen: Design Overview

~50 cm



~2.5 cm

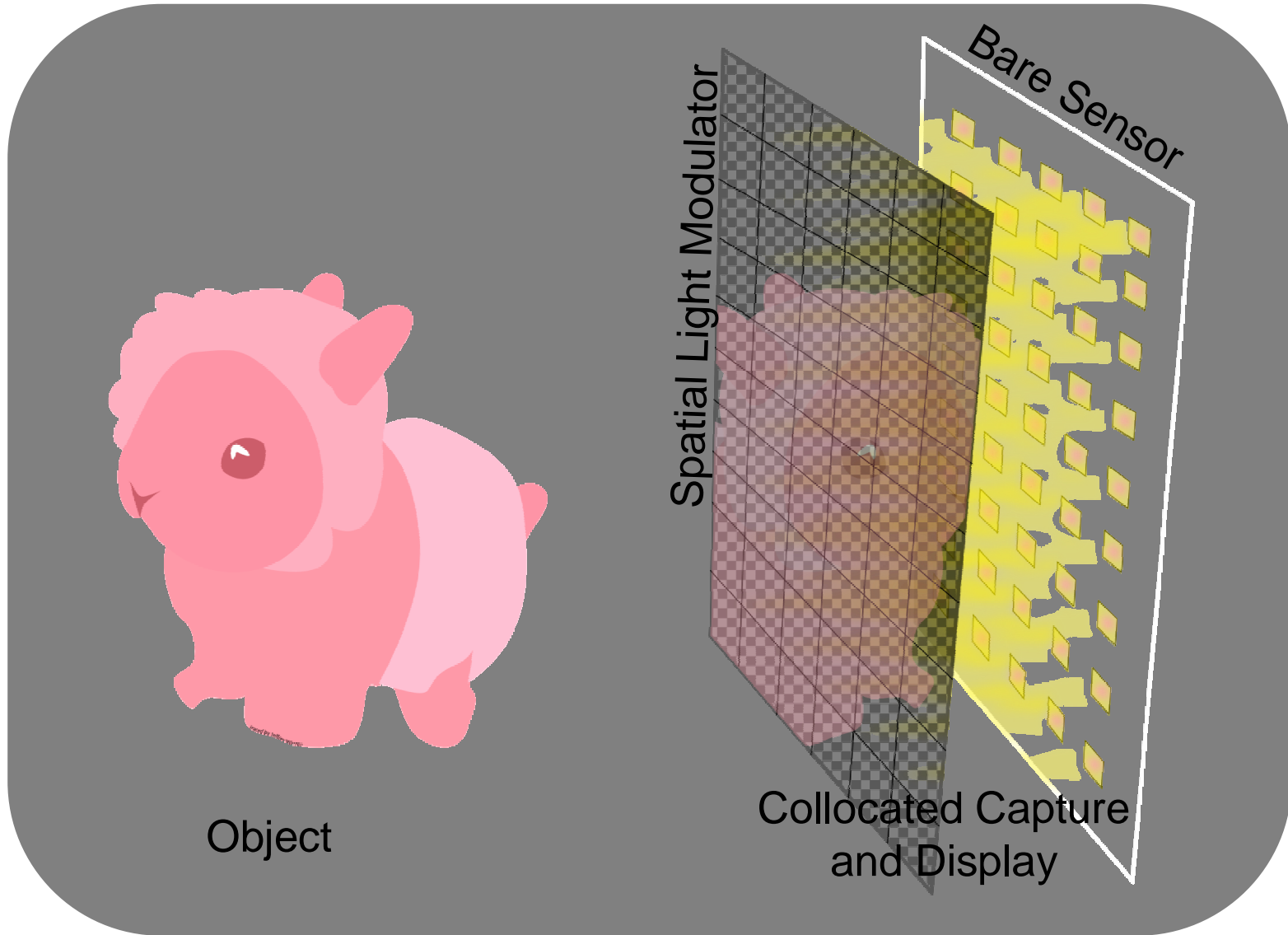


LCD  
displaying mask

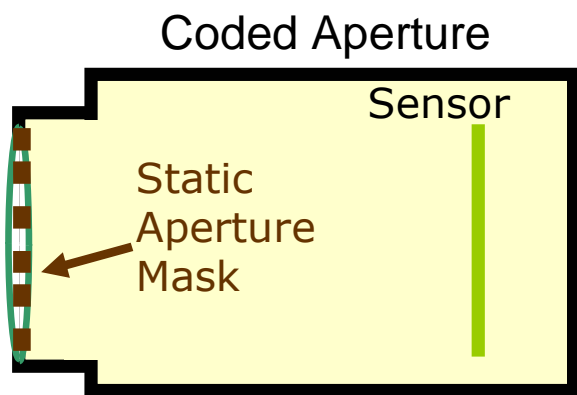
Display with embedded optical sensors

Optical sensor array

# BiDi Screen: Design Vision

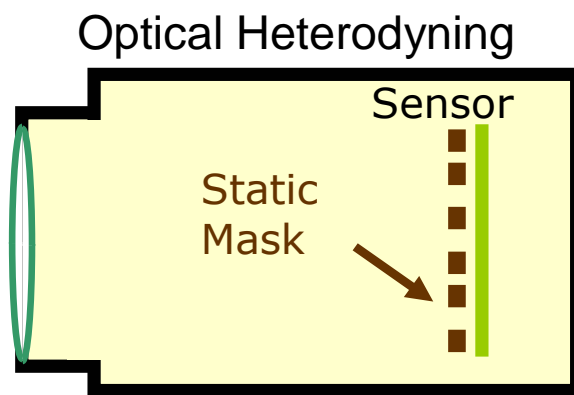


# Reinterpretable Imaging



Veeraraghavan et al.  
SIGGRAPH 2007

Digital  
Refocusing

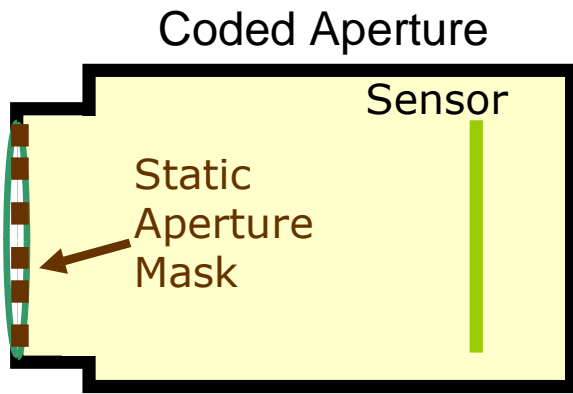


Veeraraghavan et al.  
SIGGRAPH 2007

Light Field  
Capture

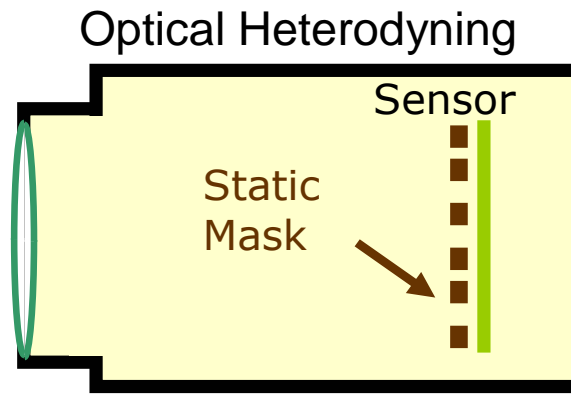


# Reinterpretable Imager



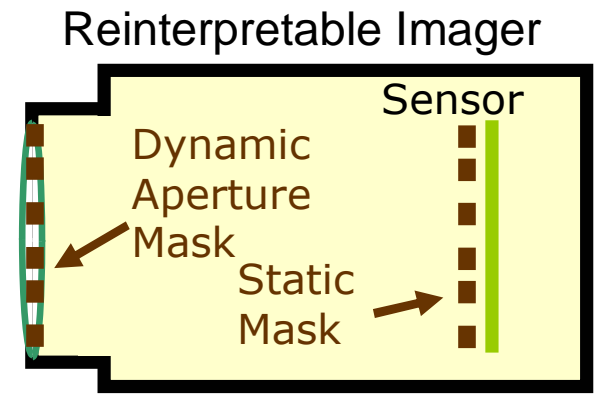
Veeraraghavan et al.  
SIGGRAPH 2007

Digital  
Refocusing



Veeraraghavan et al.  
SIGGRAPH 2007

Light Field  
Capture

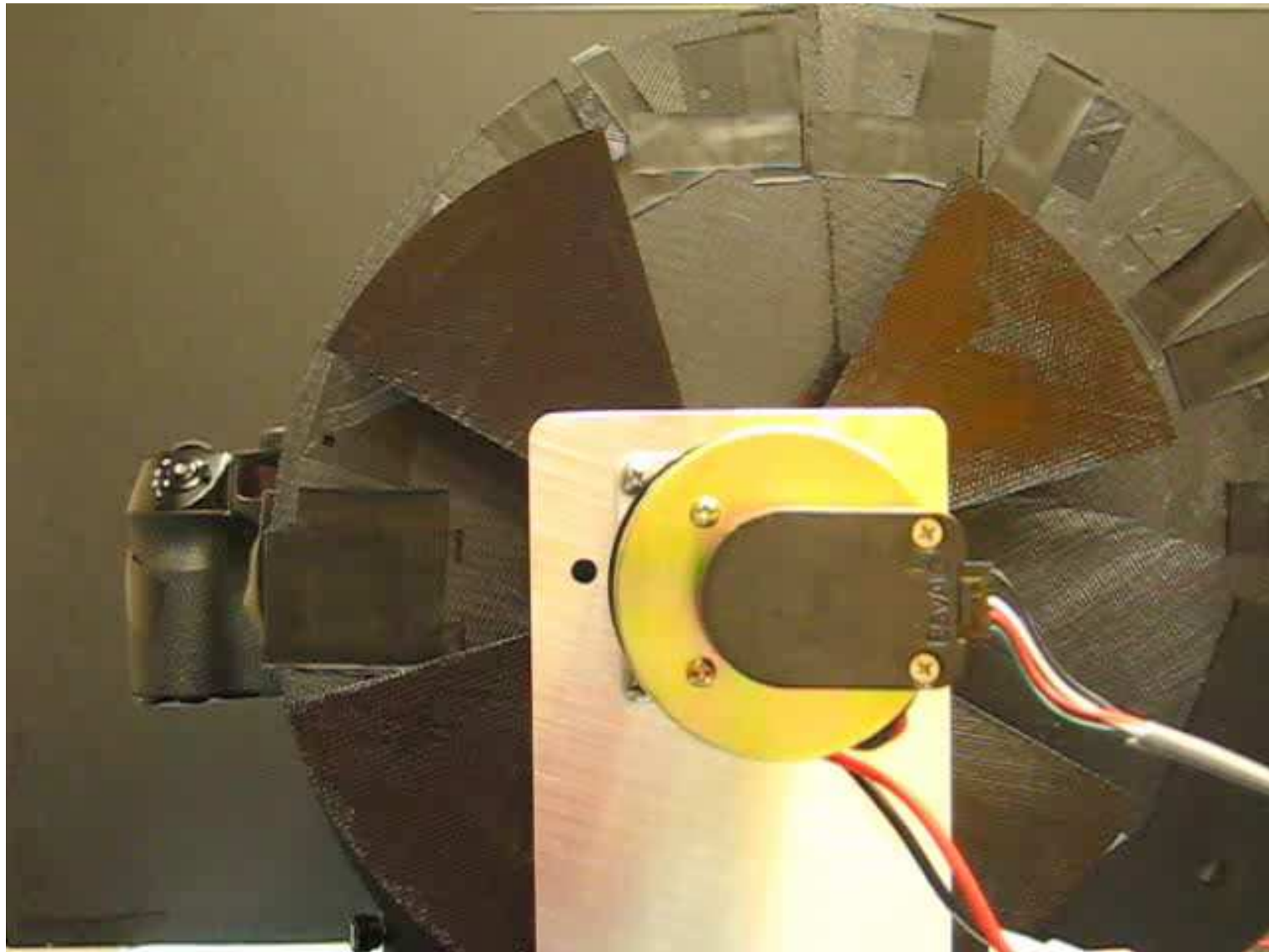


Agrawal et al.  
Eurographics 2009

Post-Capture  
Resolution Control

*“Reinterpretable Imager: Towards Variable Post-Capture Space, Angle and Time Resolution in Photography”*, Amit Agrawal, Ashok Veeraraghavan, Ramesh Raskar, in **Eurographics 2010**.

# Temporally changing mask in Aperture



Captured 2D Photo



Static Scene Parts

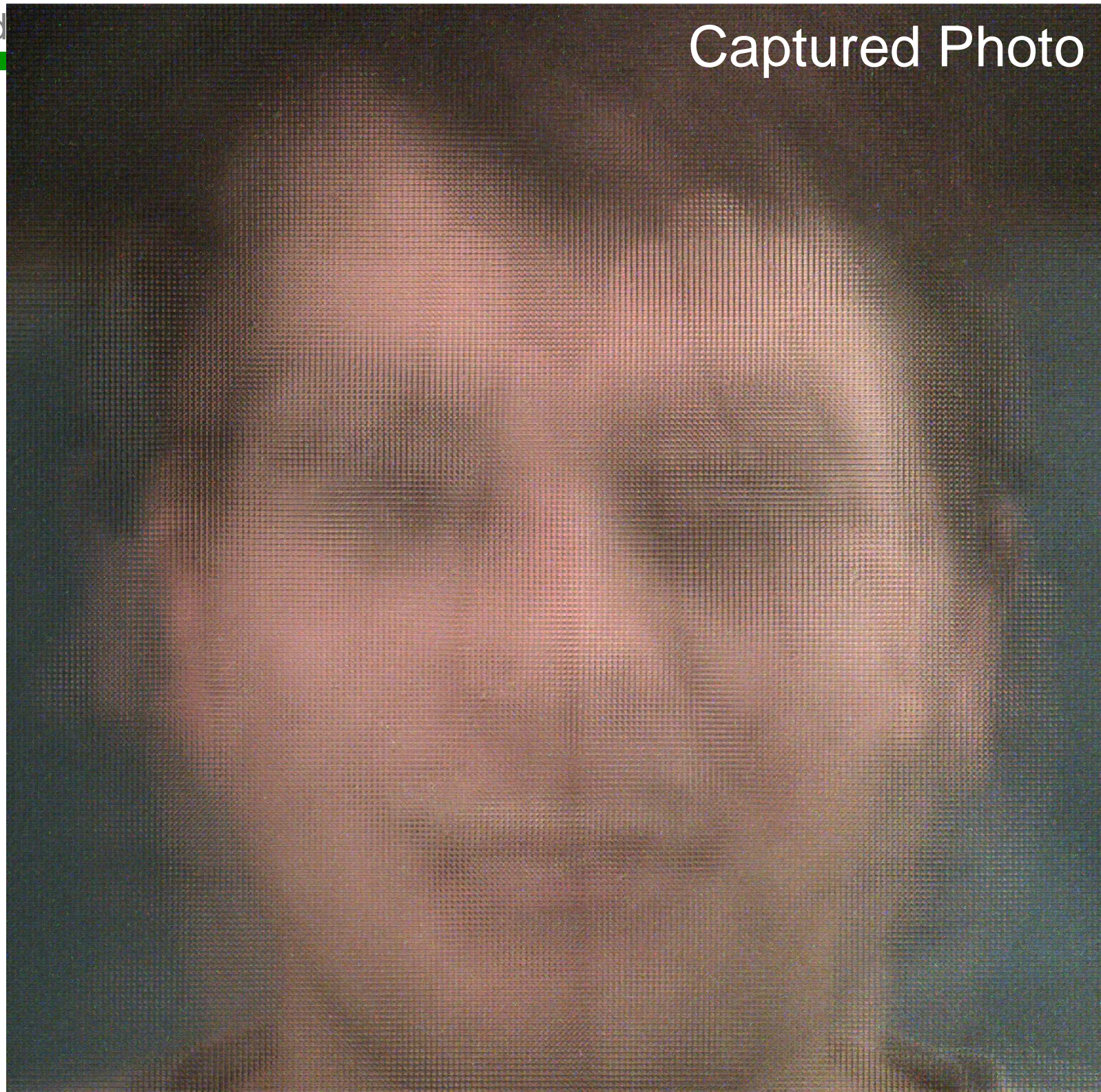
In-Focus	Out of Focus
High Resolution 2D Image	4D Light Field

Dynamic Scene Parts

In-Focus	Out of Focus
Video	1D Parallax + Motion



# Captured Photo







Video from Single-Shot (Temporal Frames)



Reconstructed Sub-Aperture Views (3 by 3 Light Field)



Time



Time



For Rotating Doll

Angle



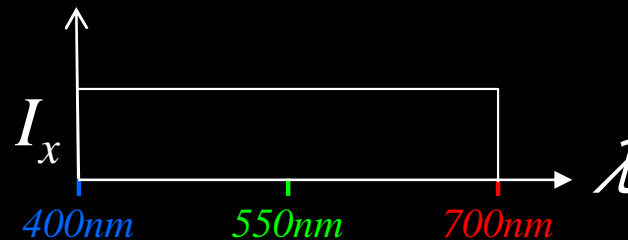
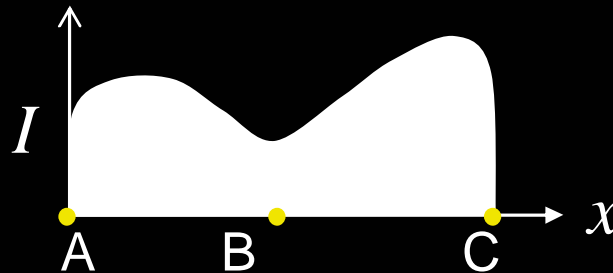
Angle



For Static Scene Parts

# Light Field Modulation

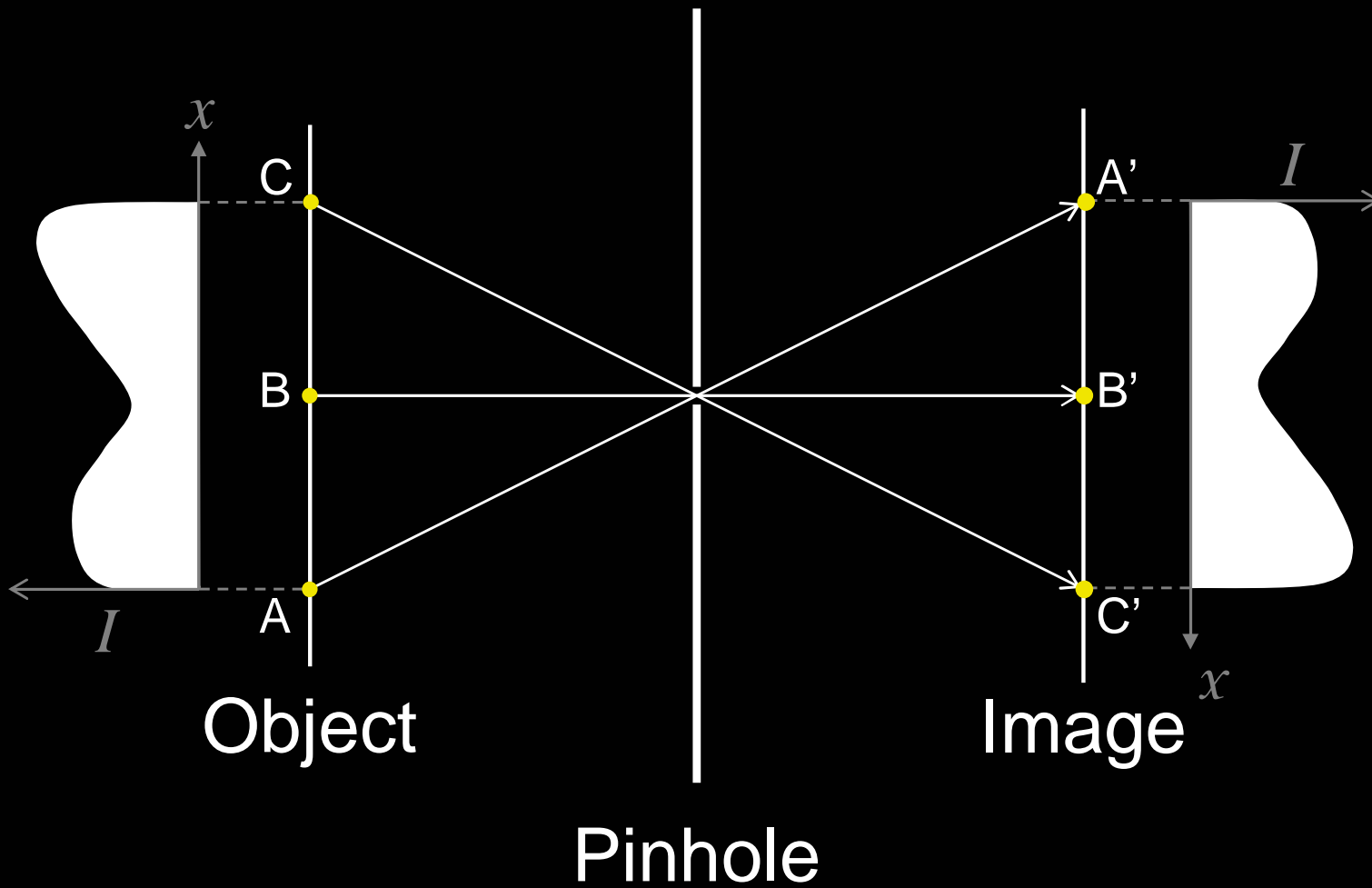
# Agile Spectrum Imaging



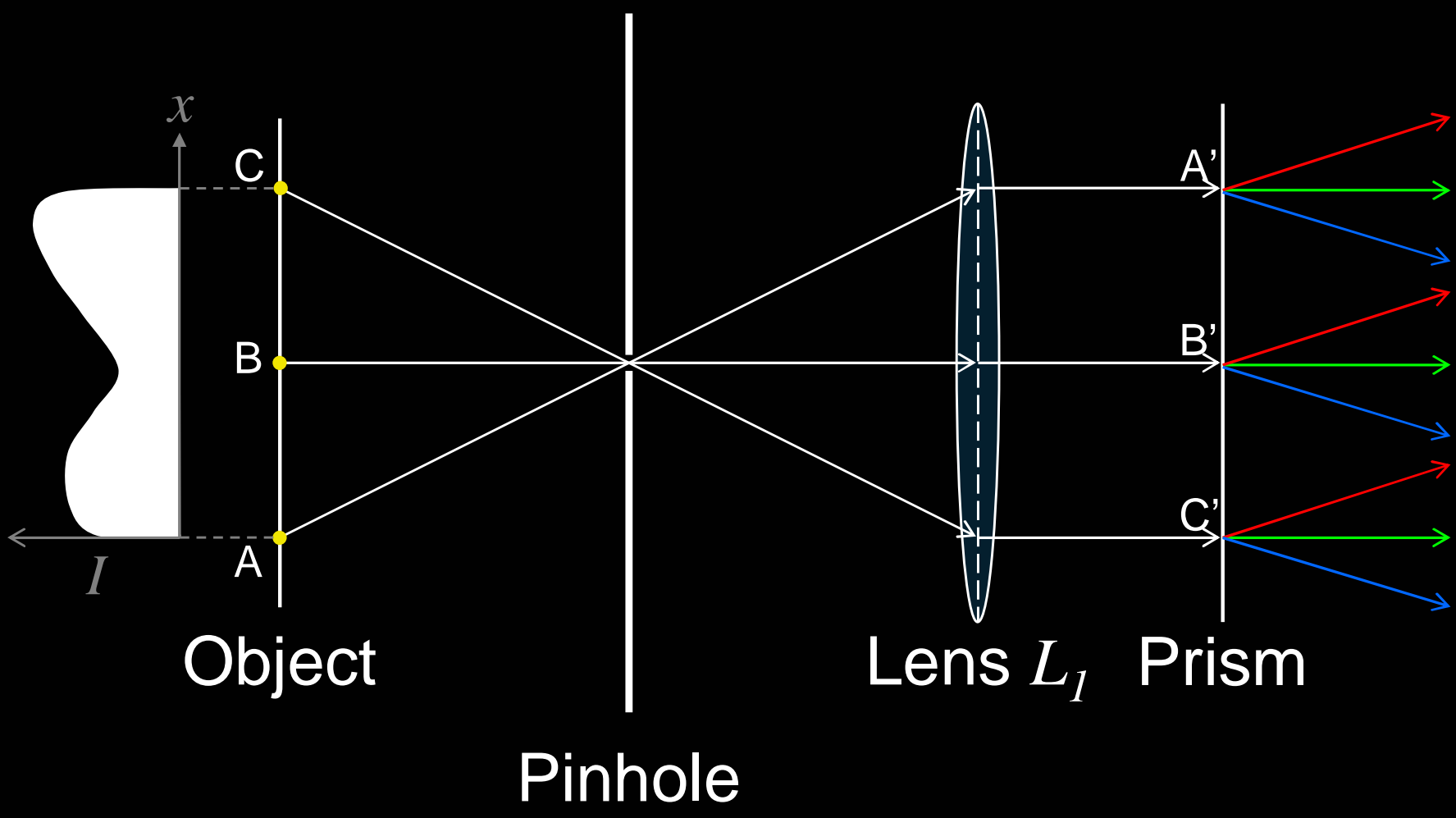
## Arbitrary *white* 1D signal

*“Agile Spectrum Imaging: Programmable Wavelength Modulation for Cameras and Projectors”*, Ankit Mohan, Ramesh Raskar and Jack Tumblin, in **Eurographics 2008**.

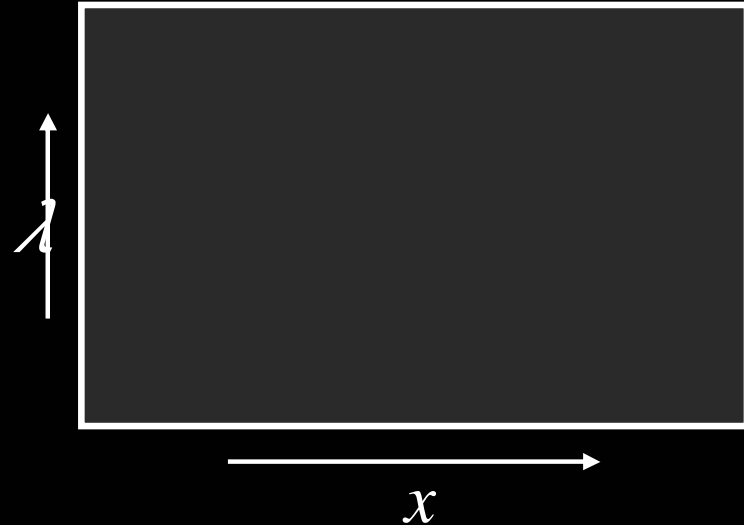
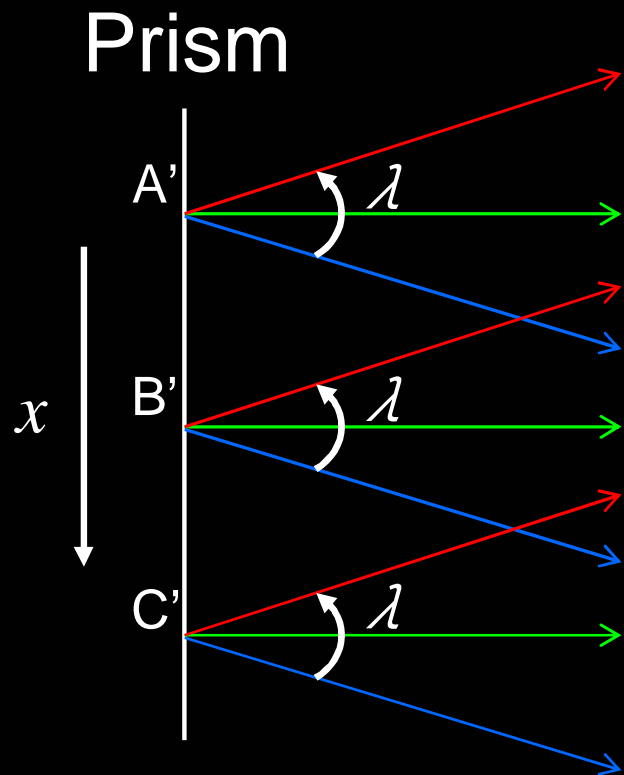
# Pinhole Camera

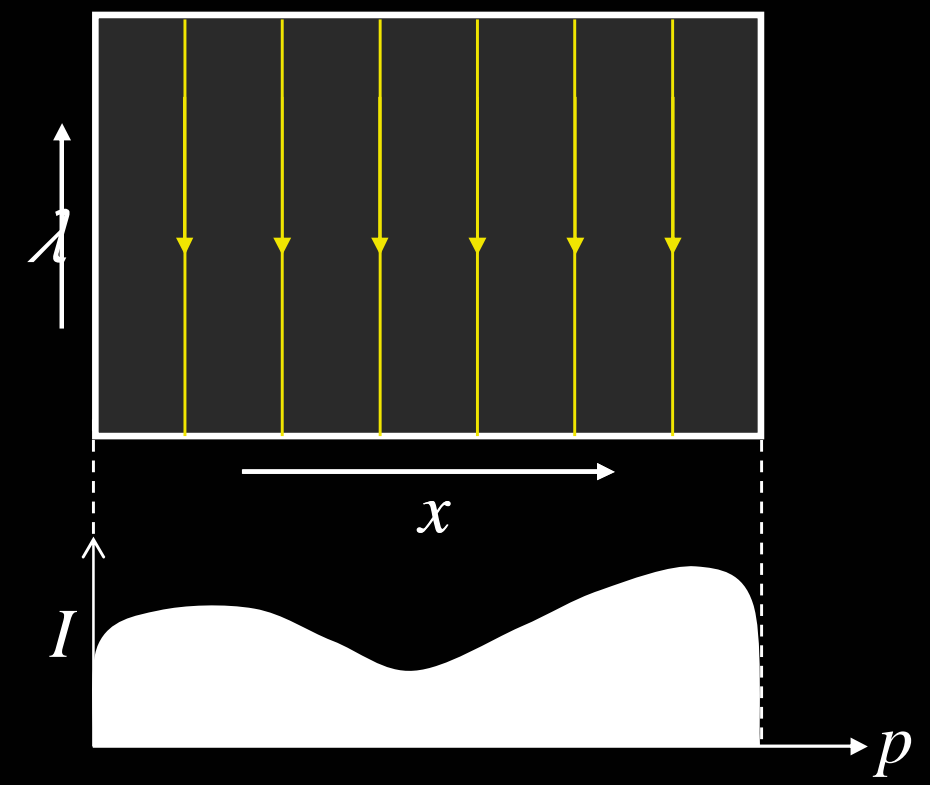
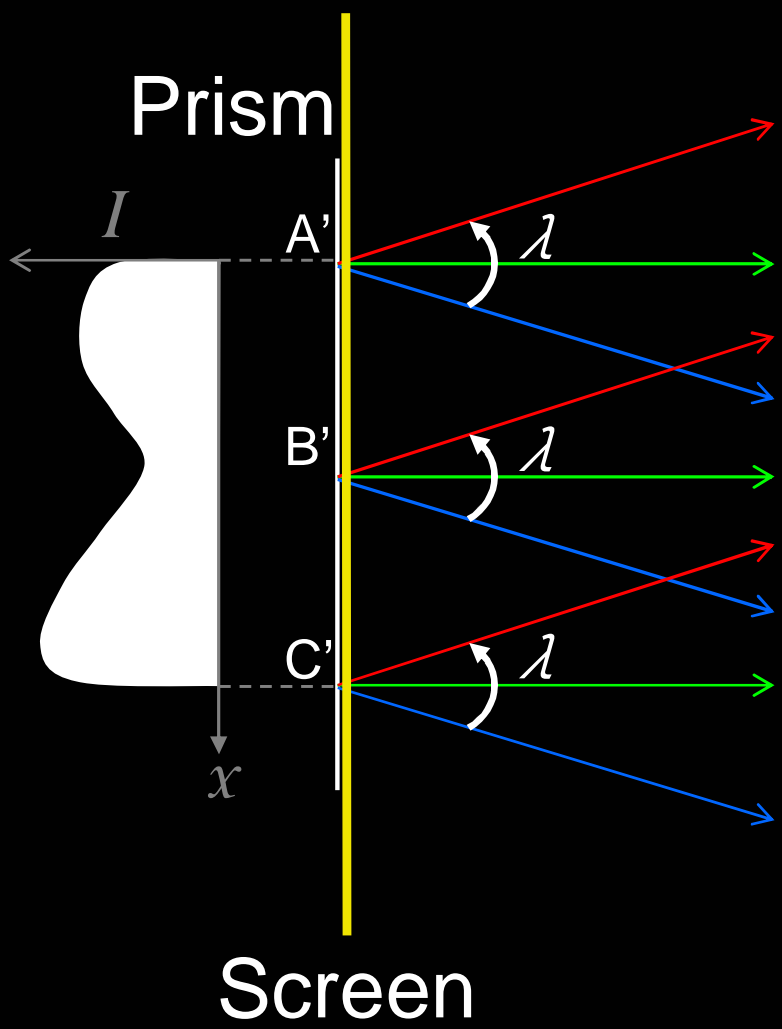




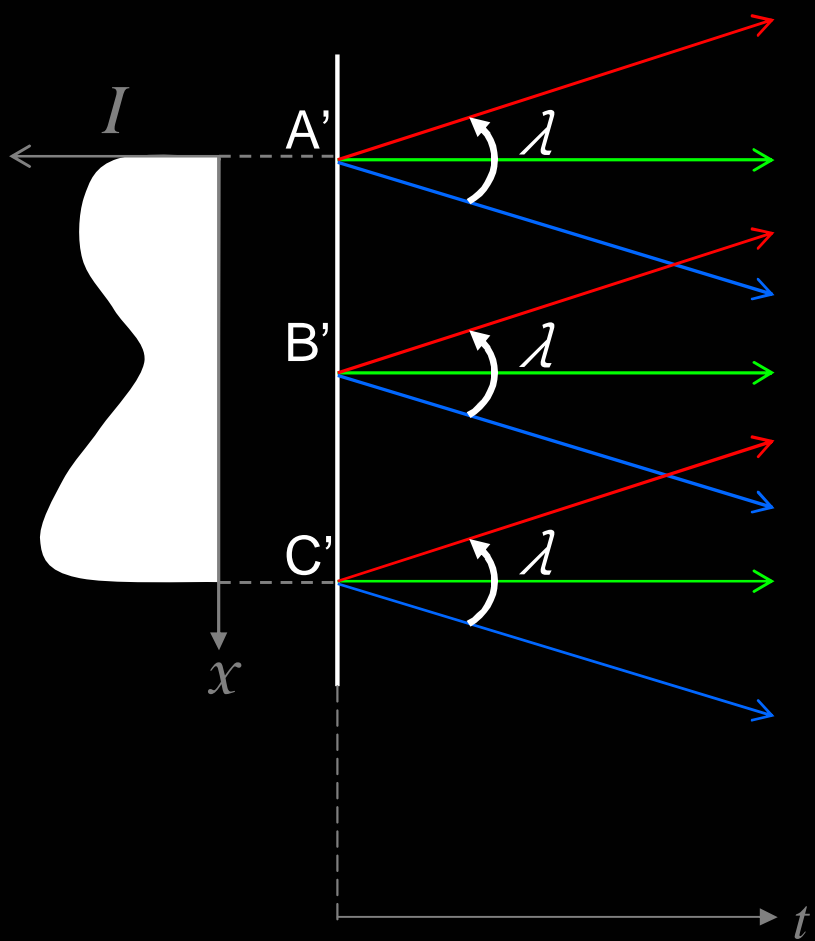


# Spectral Light-Field

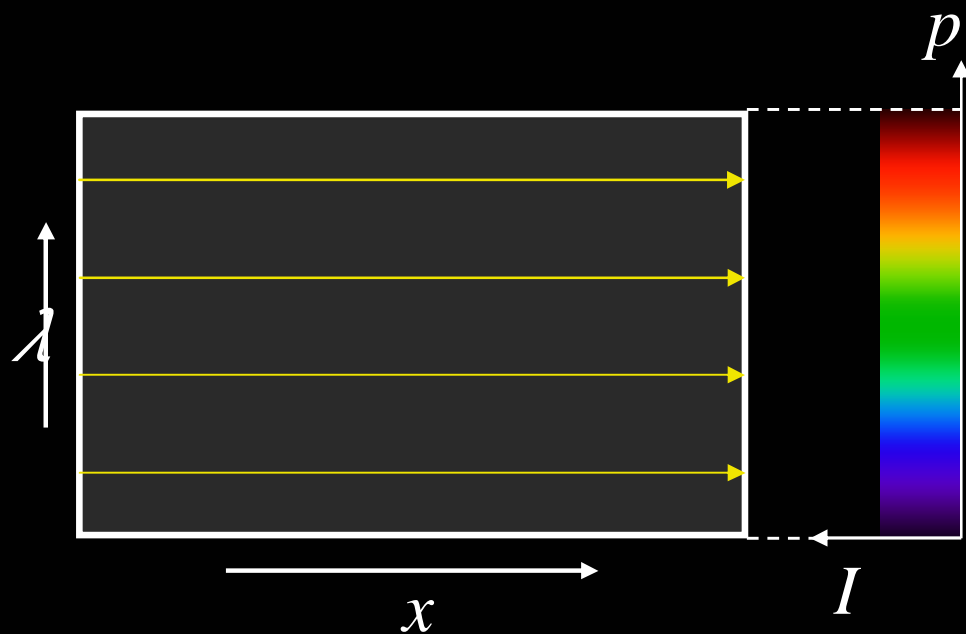


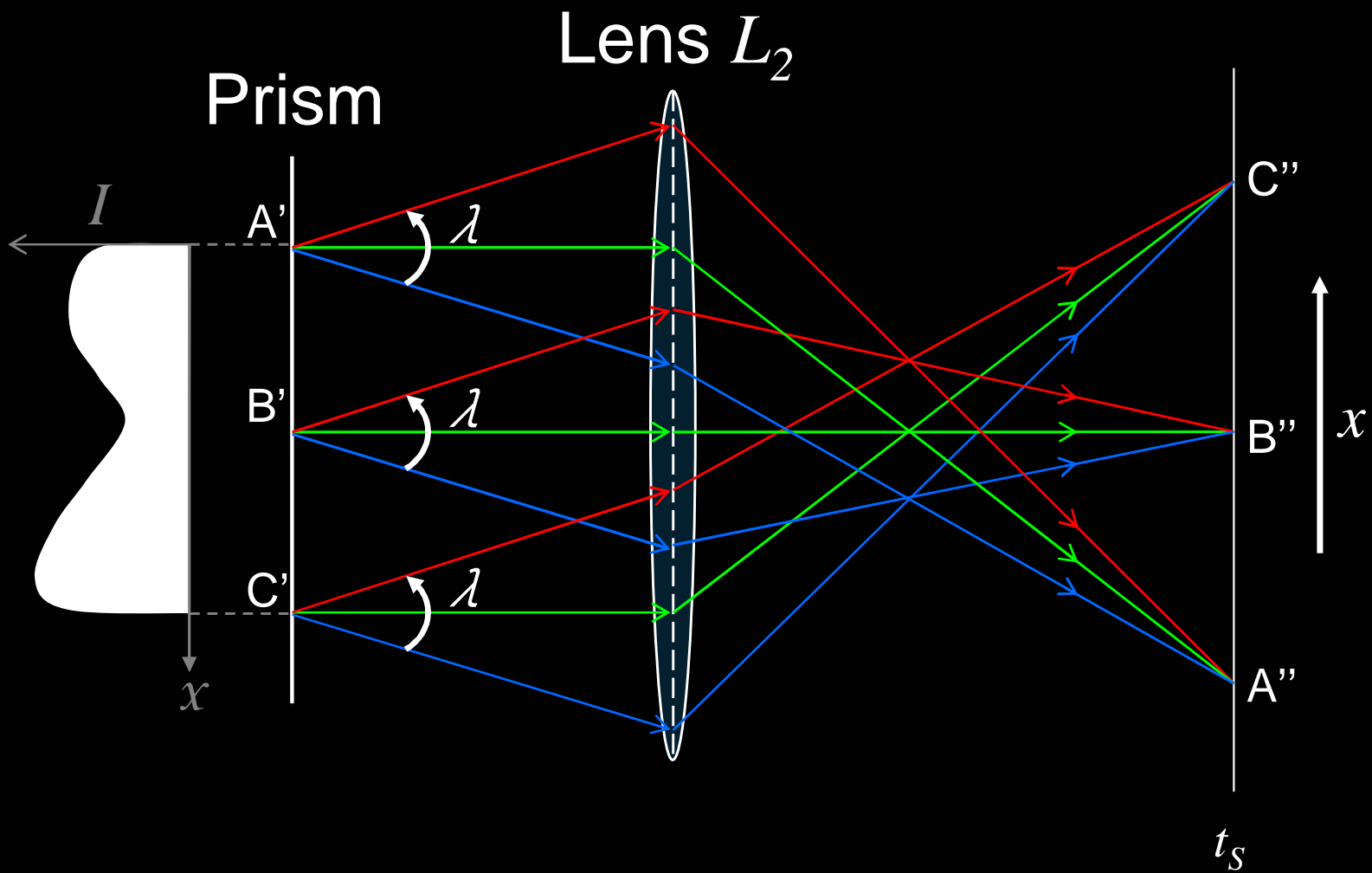


# Prism

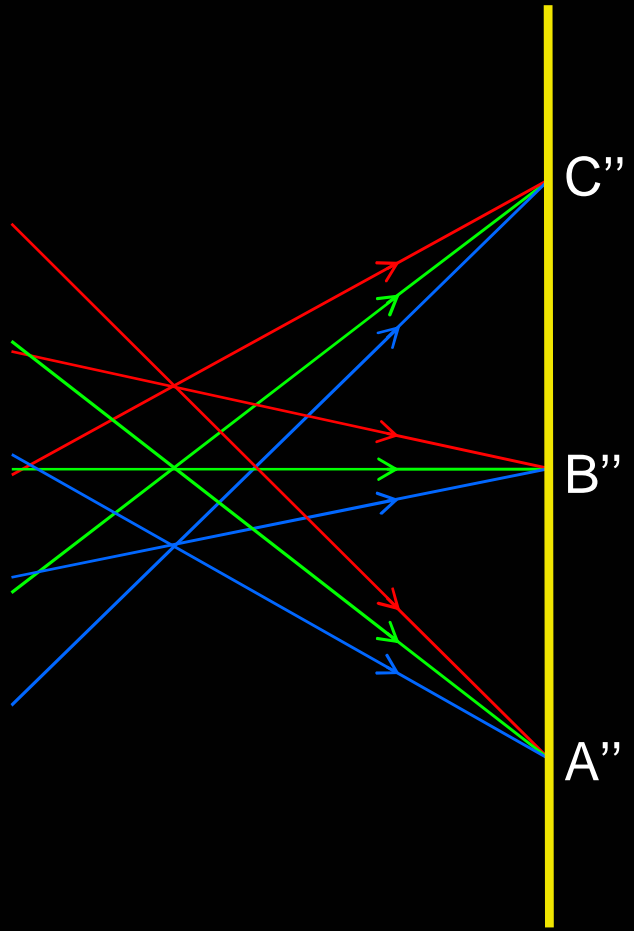


$$t = \infty$$

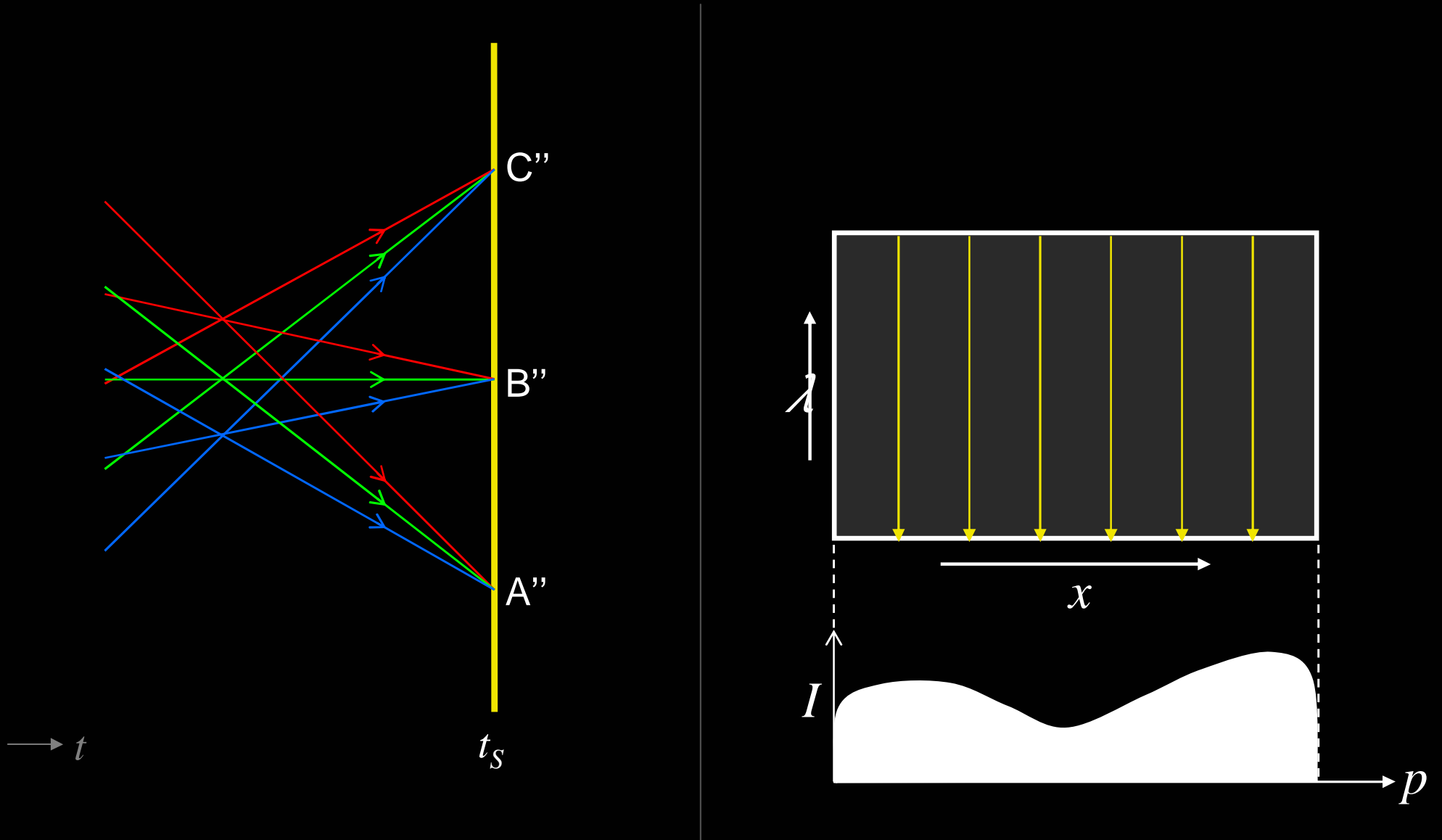




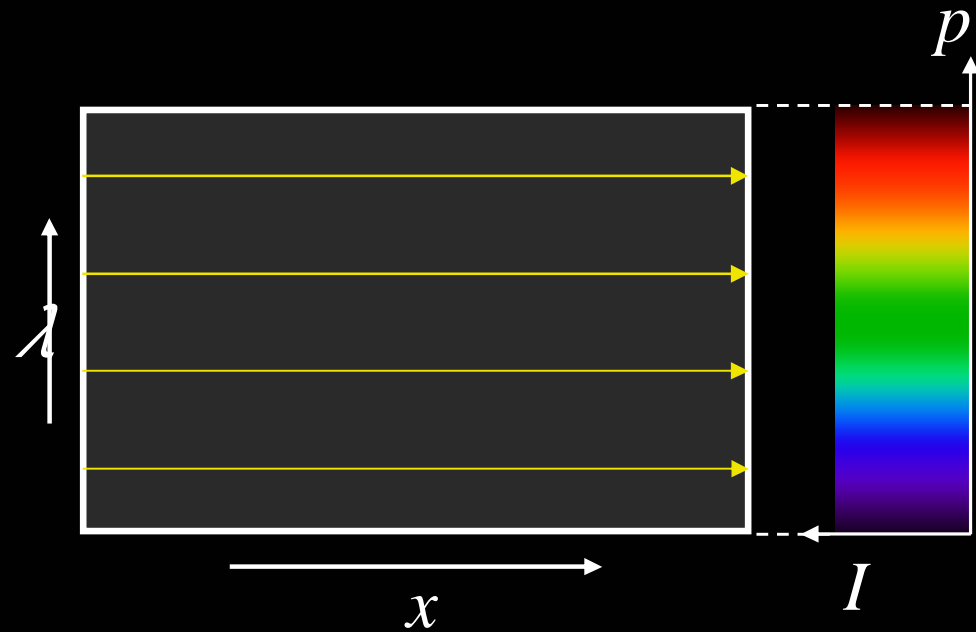
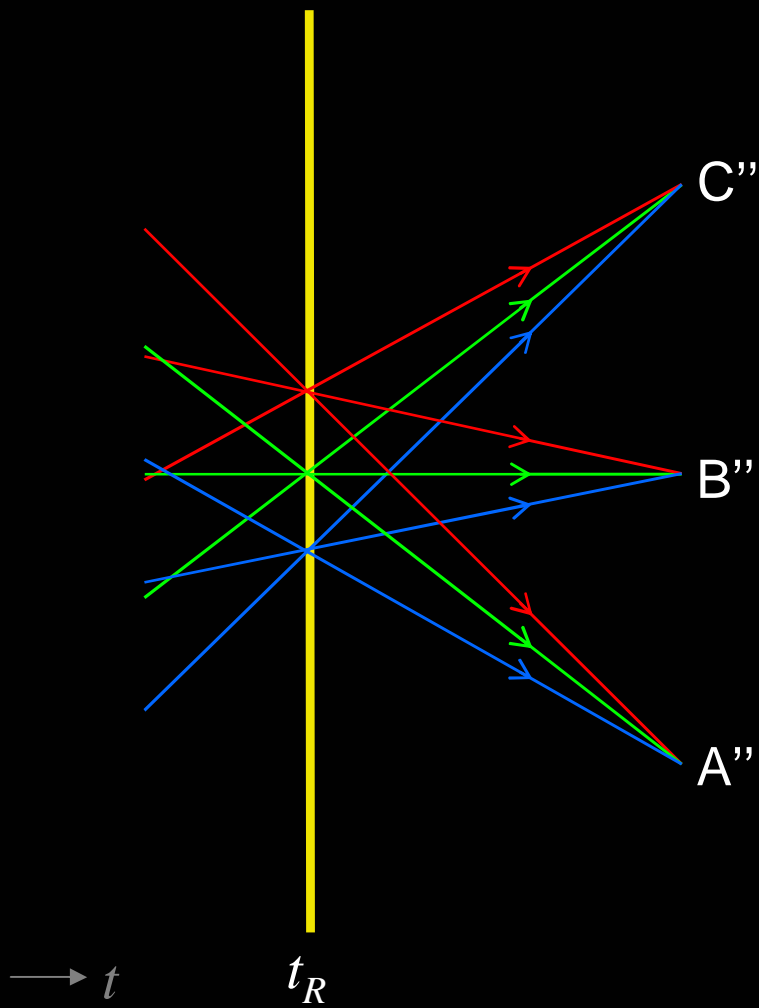




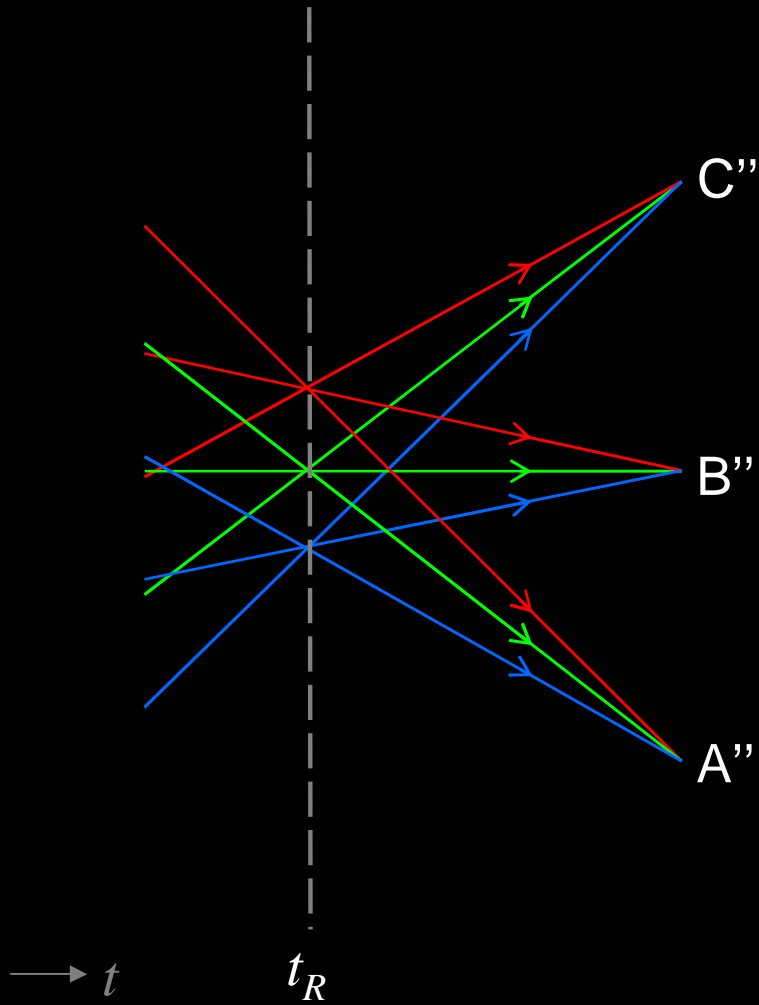
# Sensor plane ( $t=t_s$ )



# Rainbow plane ( $t=t_R$ )



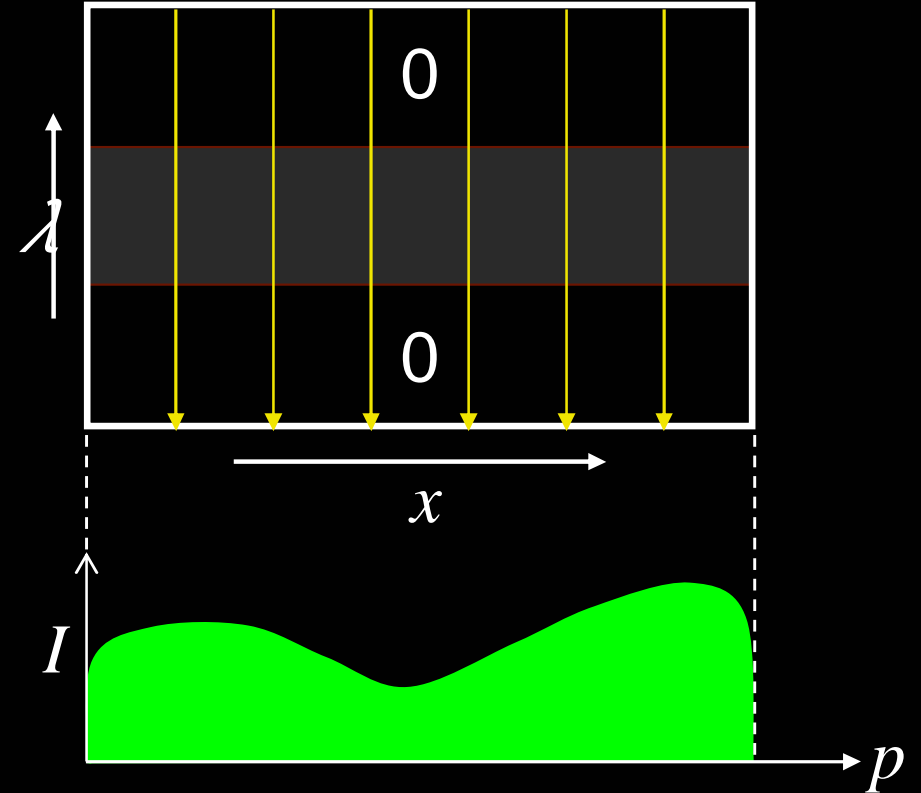
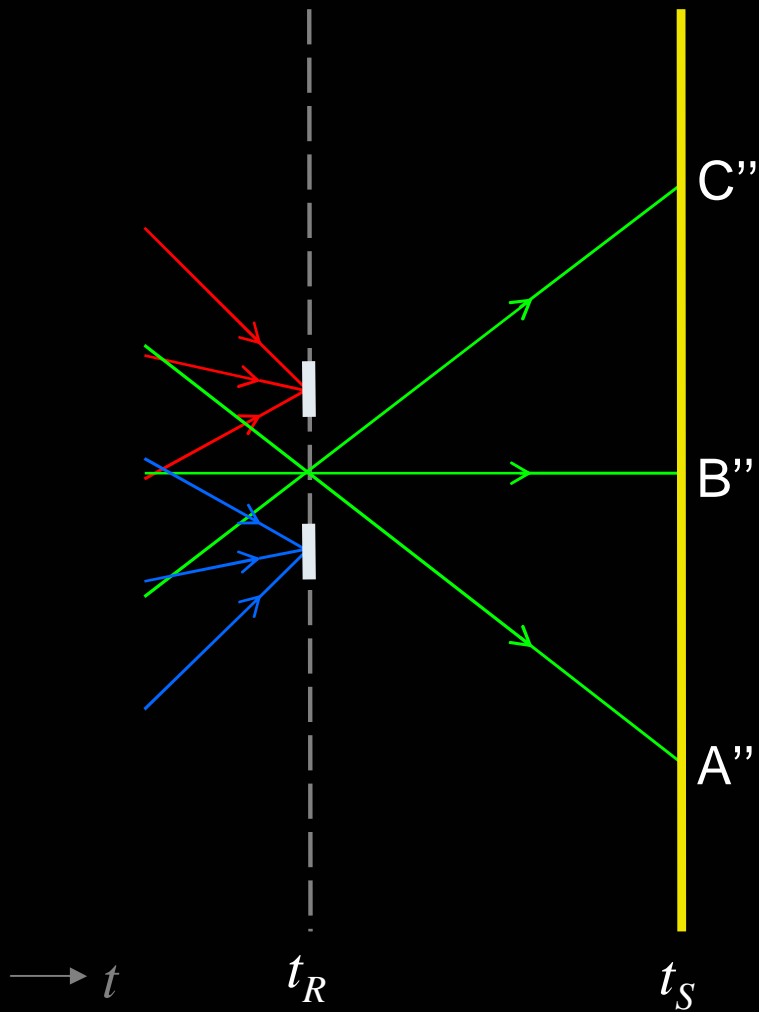
# Rainbow plane ( $t=t_R$ )



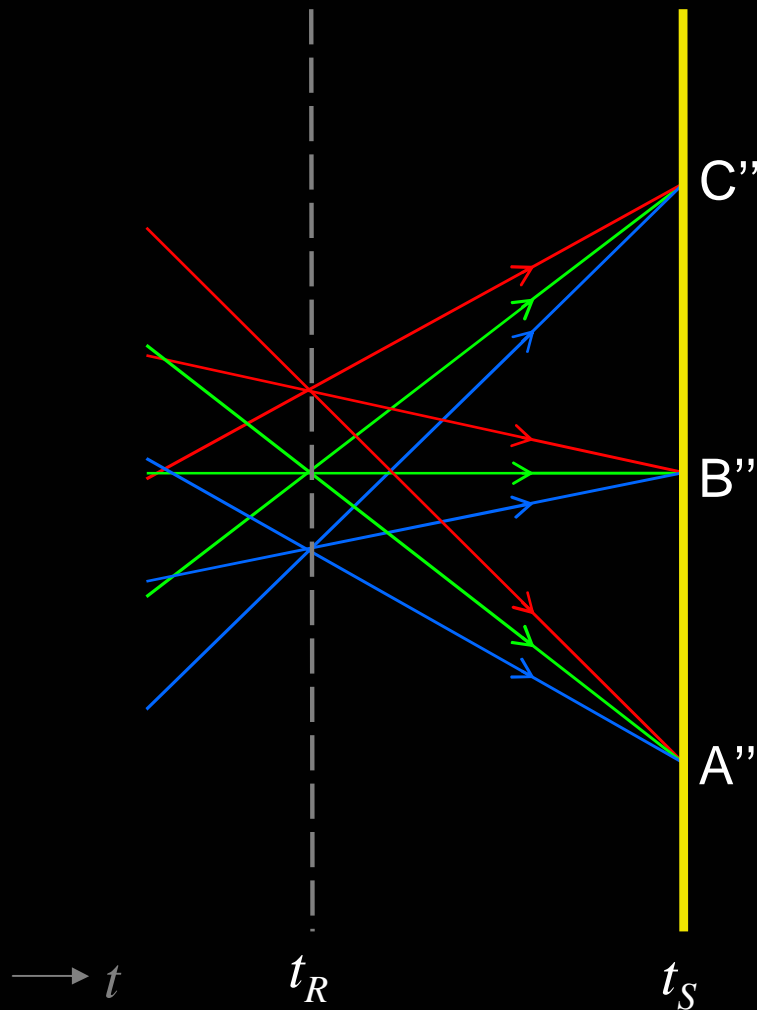
$\lambda \leftrightarrow$

position

# Mask in the Rainbow plane

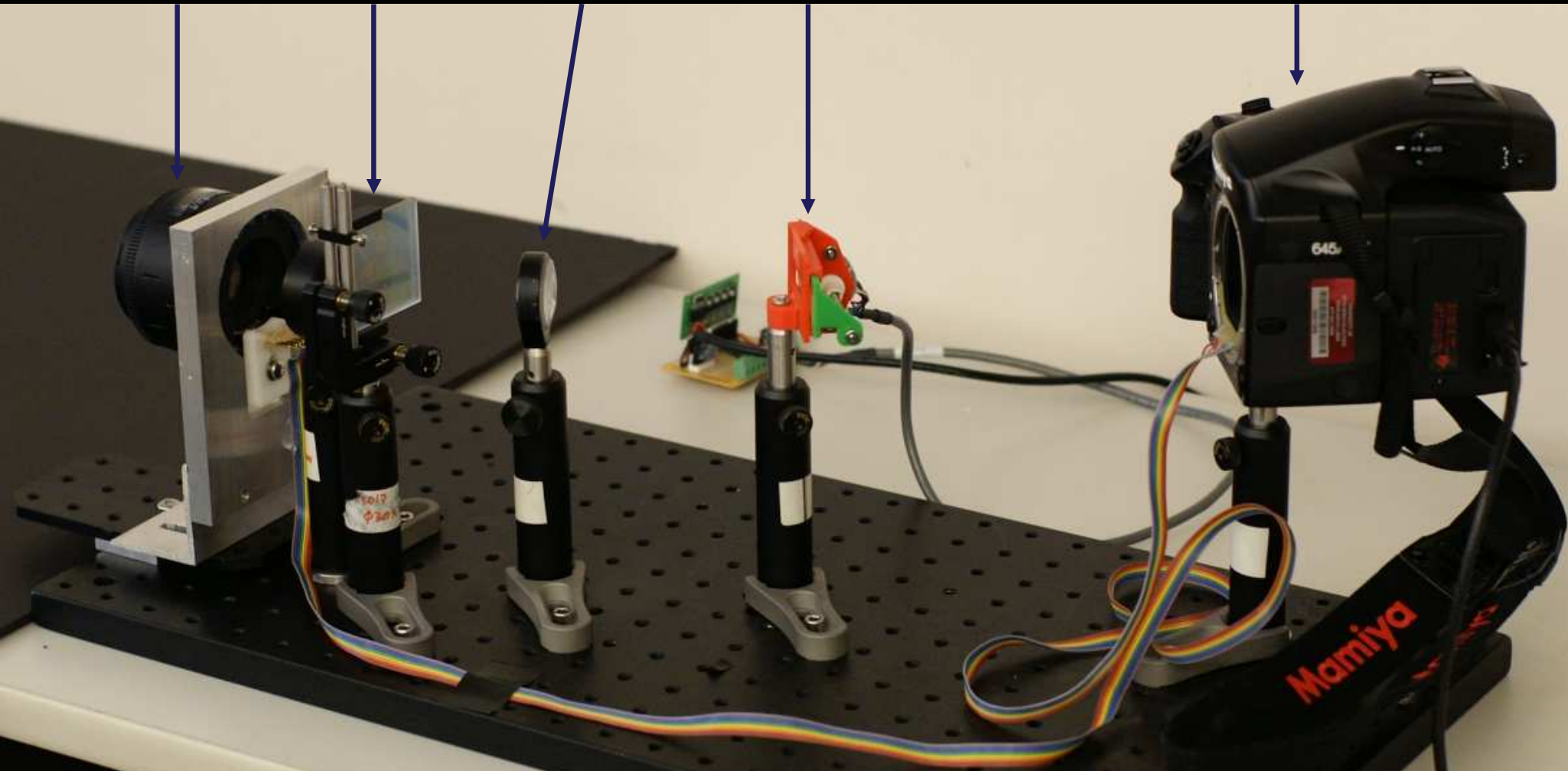
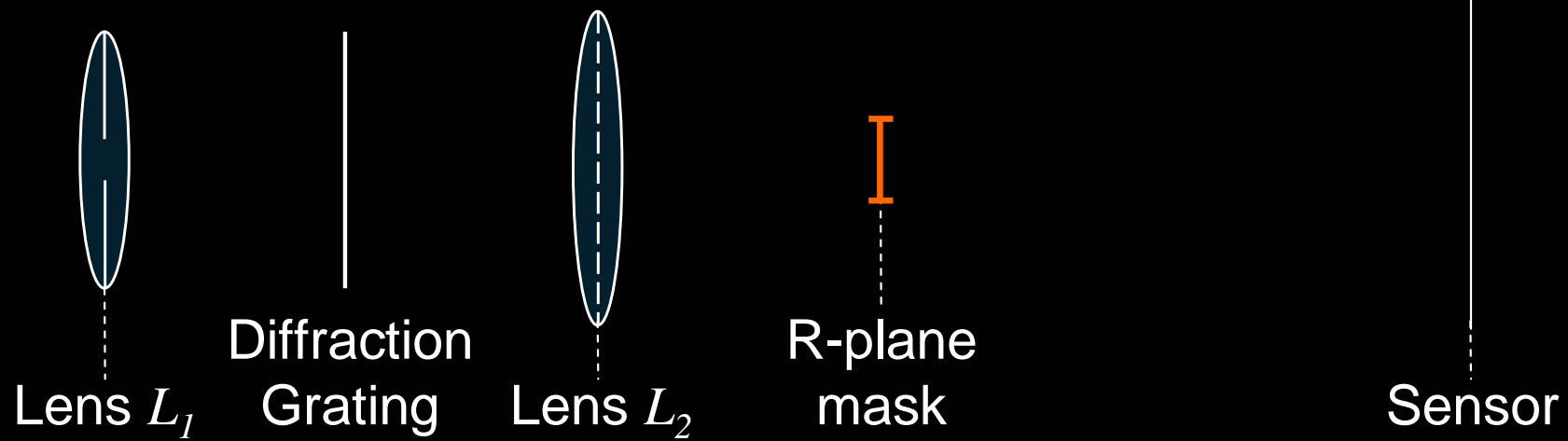


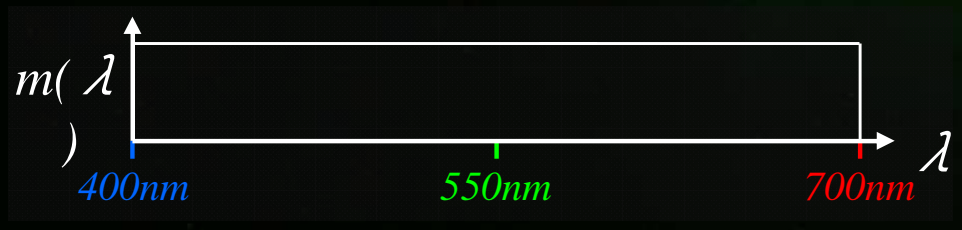
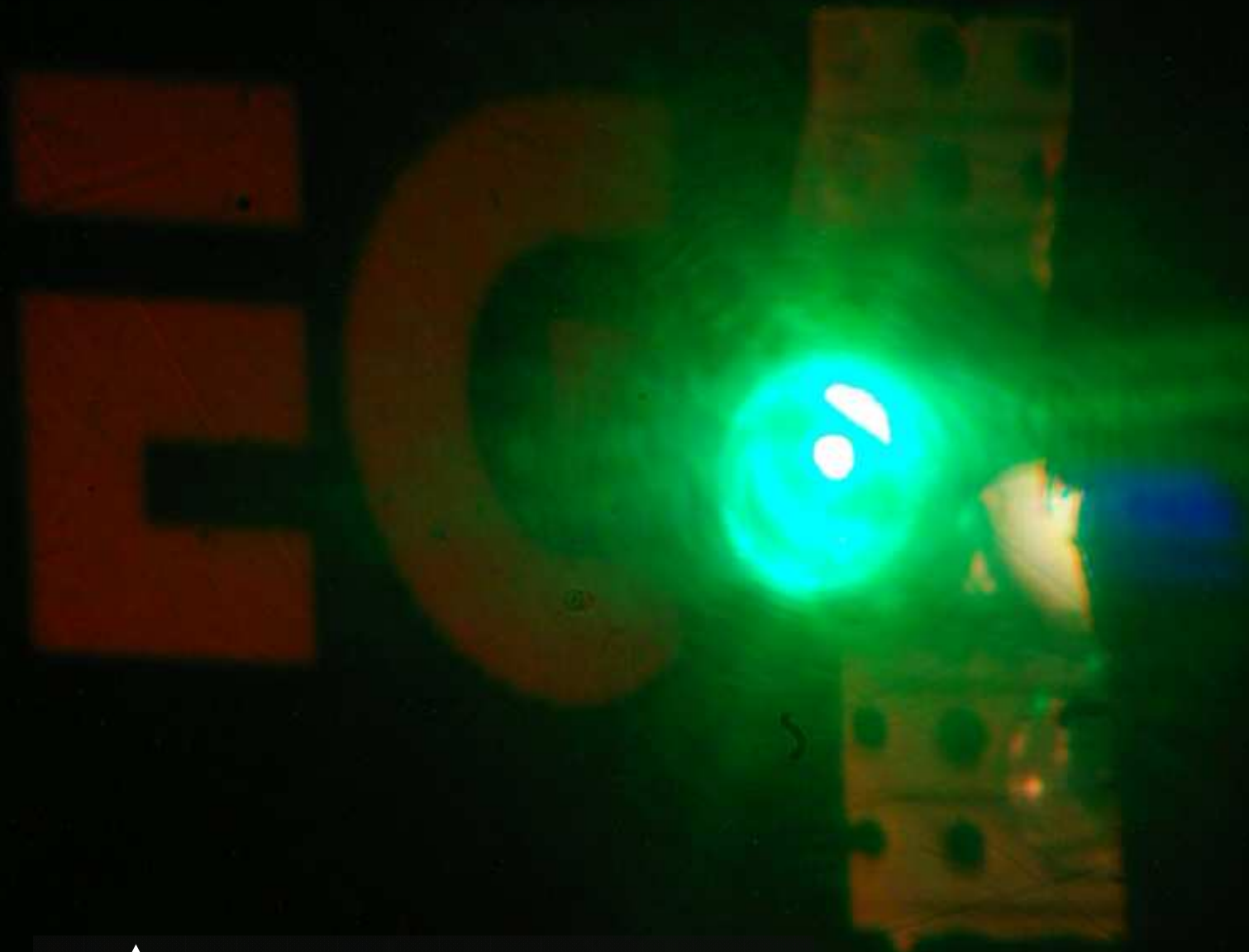
# Rainbow plane ( $t=t_R$ )

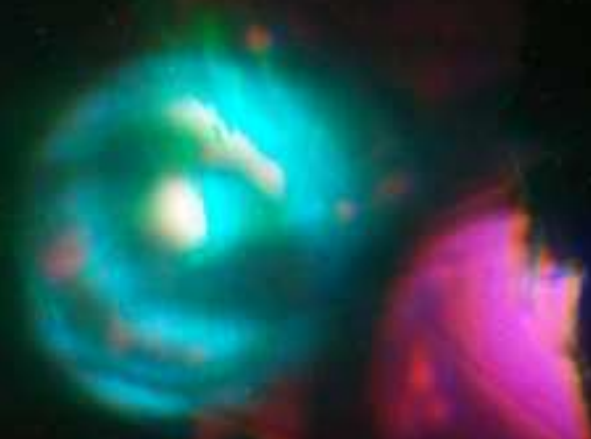
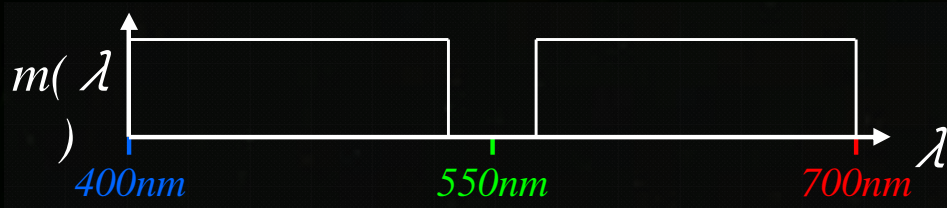


Control the *spectral sensitivity* of the sensor by placing an appropriate *grayscale masks* in the R-plane.

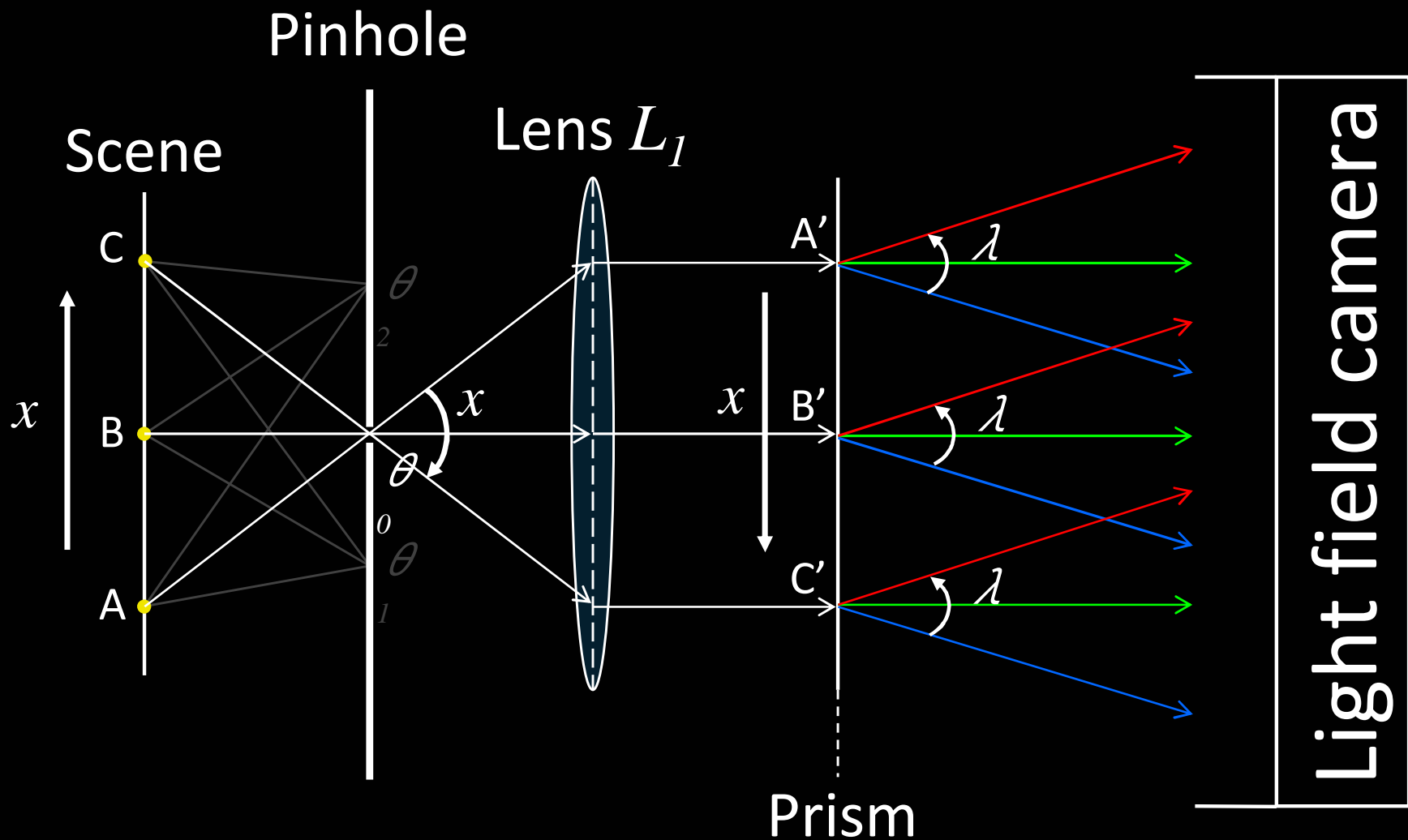




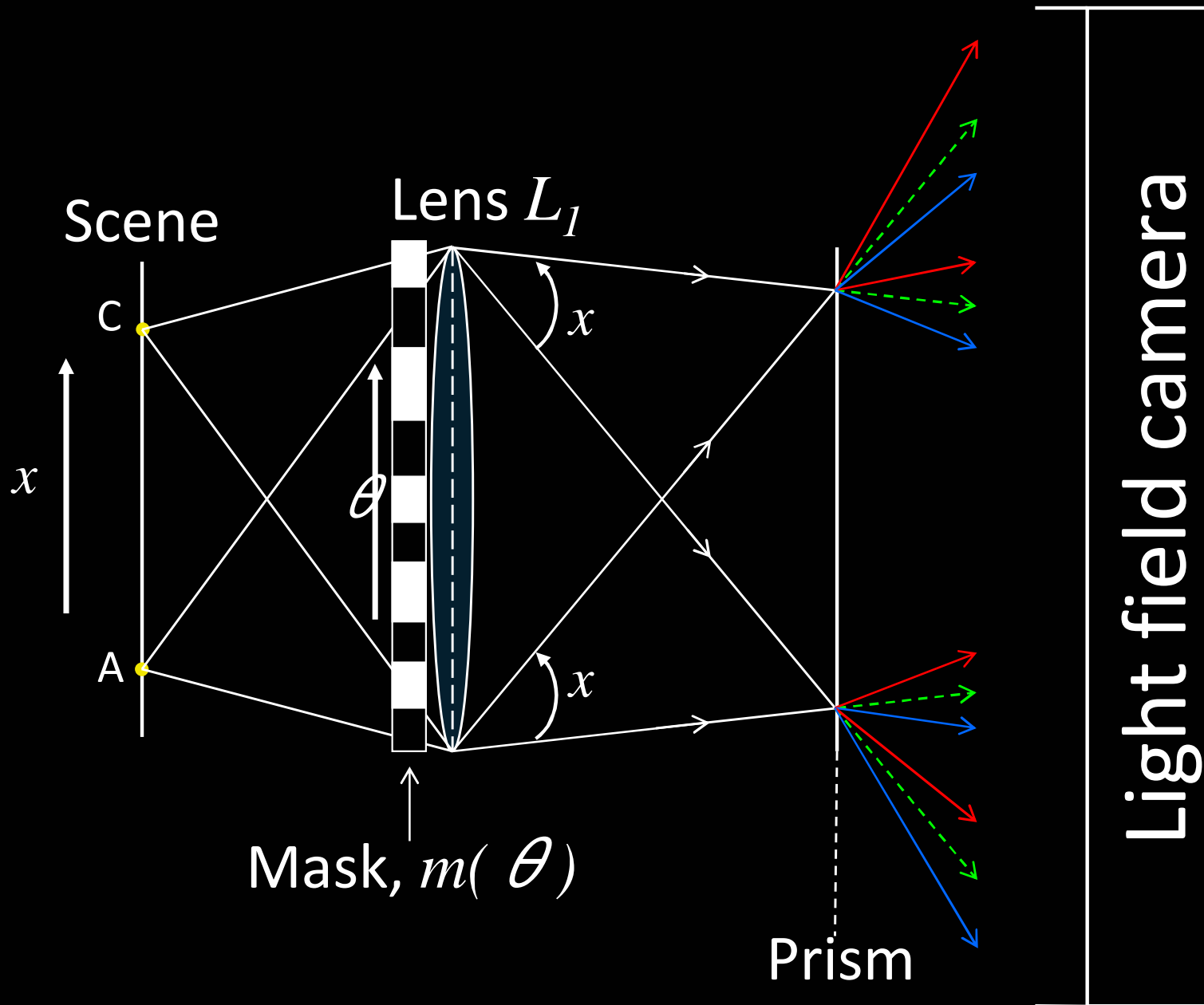




# Pinhole multi-spectral camera



# Mask based multi-spectral camera



# Glare separation camera

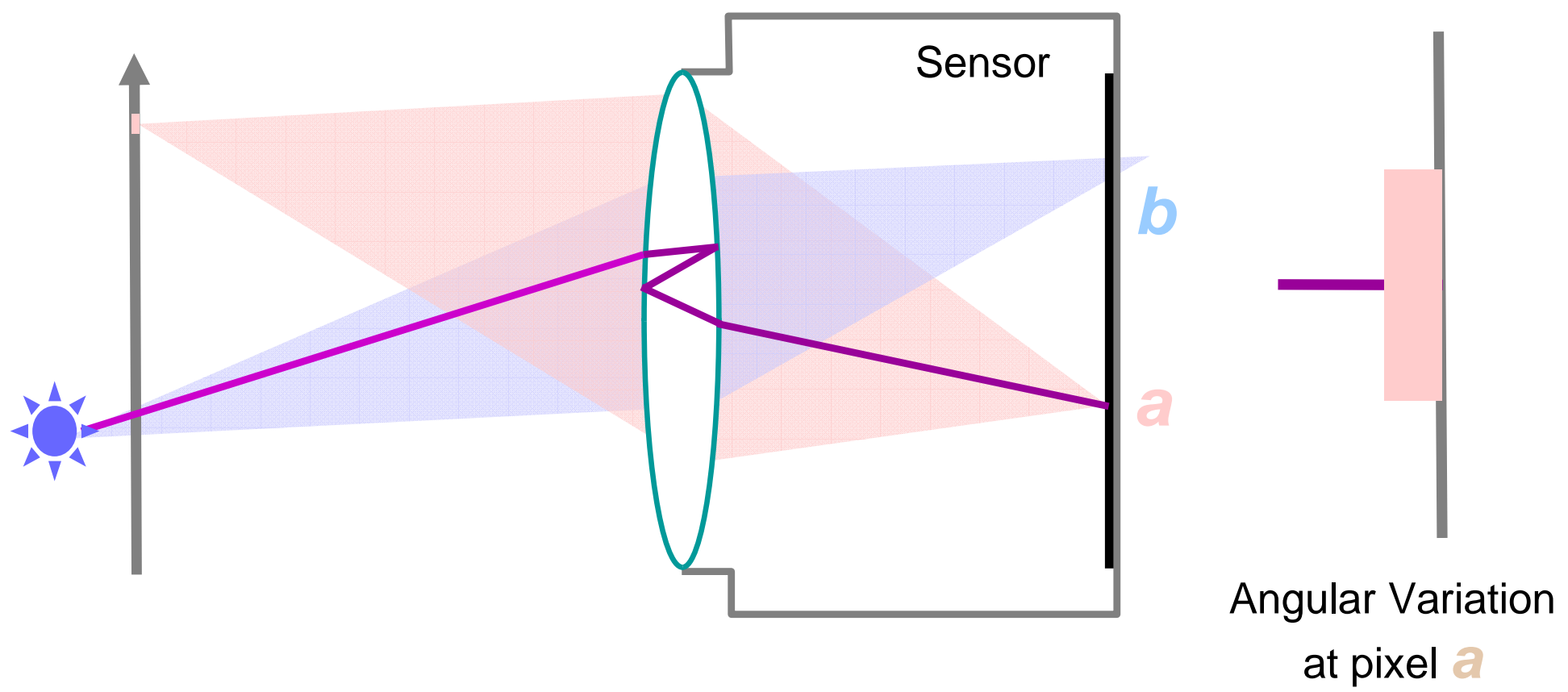


*“Glare Aware Photography: 4D Ray Sampling for Reducing Glare Effects of Camera Lenses”*, Ramesh Raskar, Amit Agrawal, Cyrus Wilson and Ashok Veeraraghavan, in **SIGGRAPH 2008**.



# Effects of Glare on Image

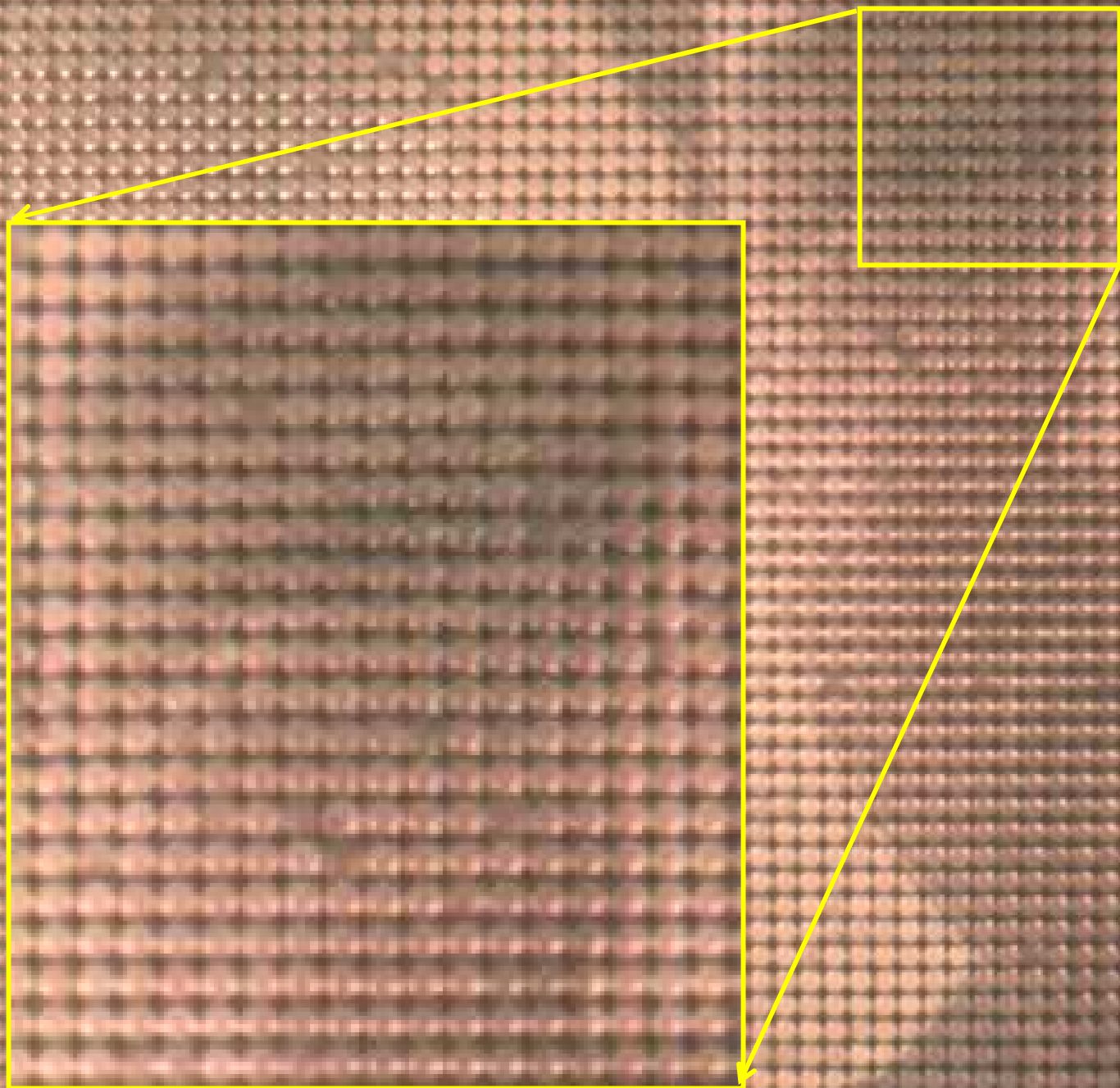
- Hard to model, Low Frequency in 2D
- But reflection glare is **outlier in 4D ray-space**
- Glare coherence to recover full resolution











# Reducing Glare



Conventional Photo



After removing outliers  
Glare Reduced Image

# Enhancing Glare



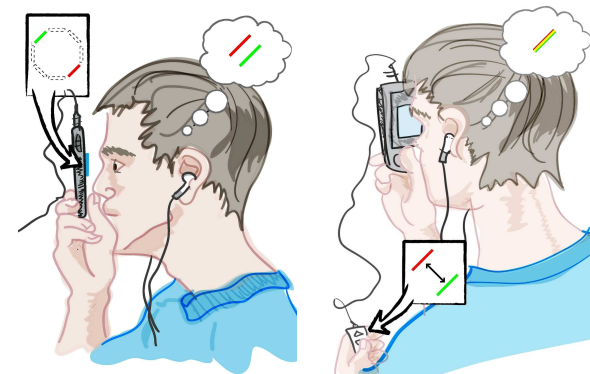
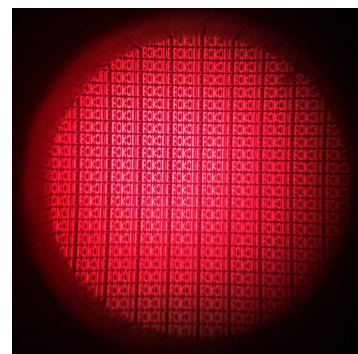
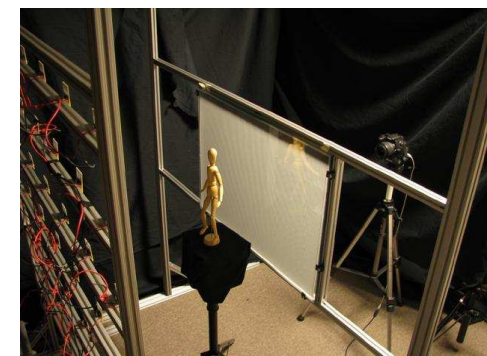
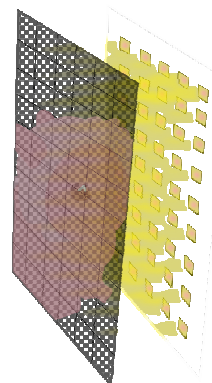
Conventional Photo



Glare Enhanced Image

# Conclusions

- Light Field Capture
  - Heterodyne Camera
  - Shield Fields
  - BiDi Screen
  - Reinterpretable Imager
- Light Field Modulation
  - Spectral Light Fields
  - Glare Camera
- Light Field Generation
  - Bokode
  - NETRA







## Post-doc Position at MIT Camera Culture group

**Start Date:** Immediately

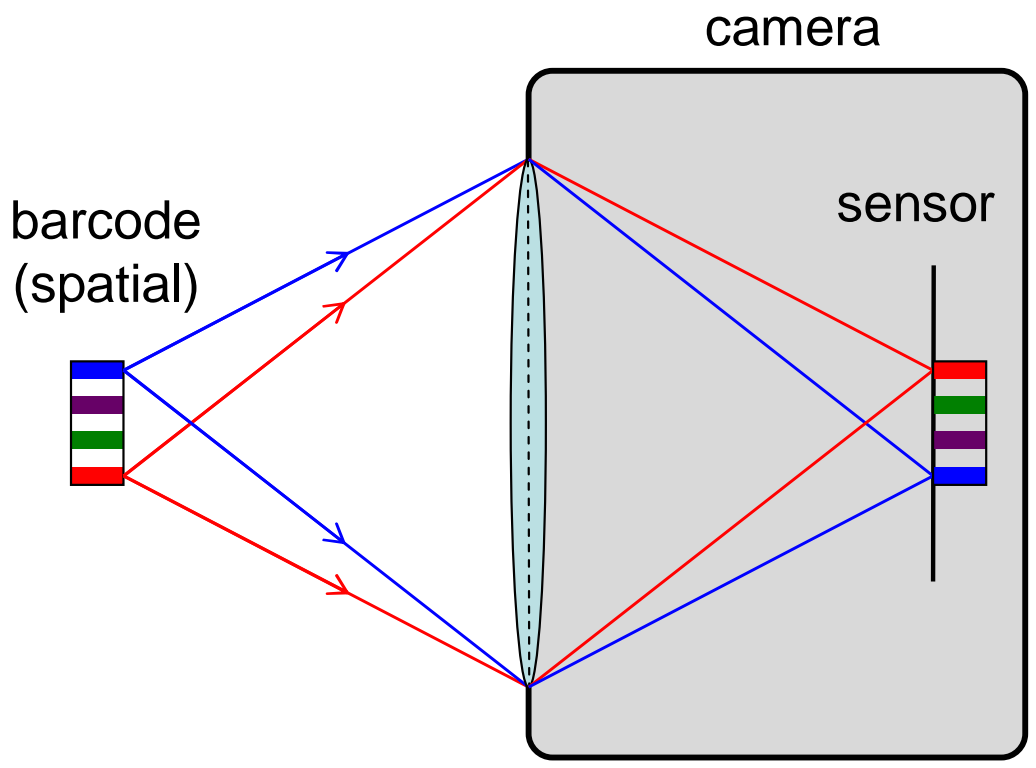
**Duration:** 1-2 years

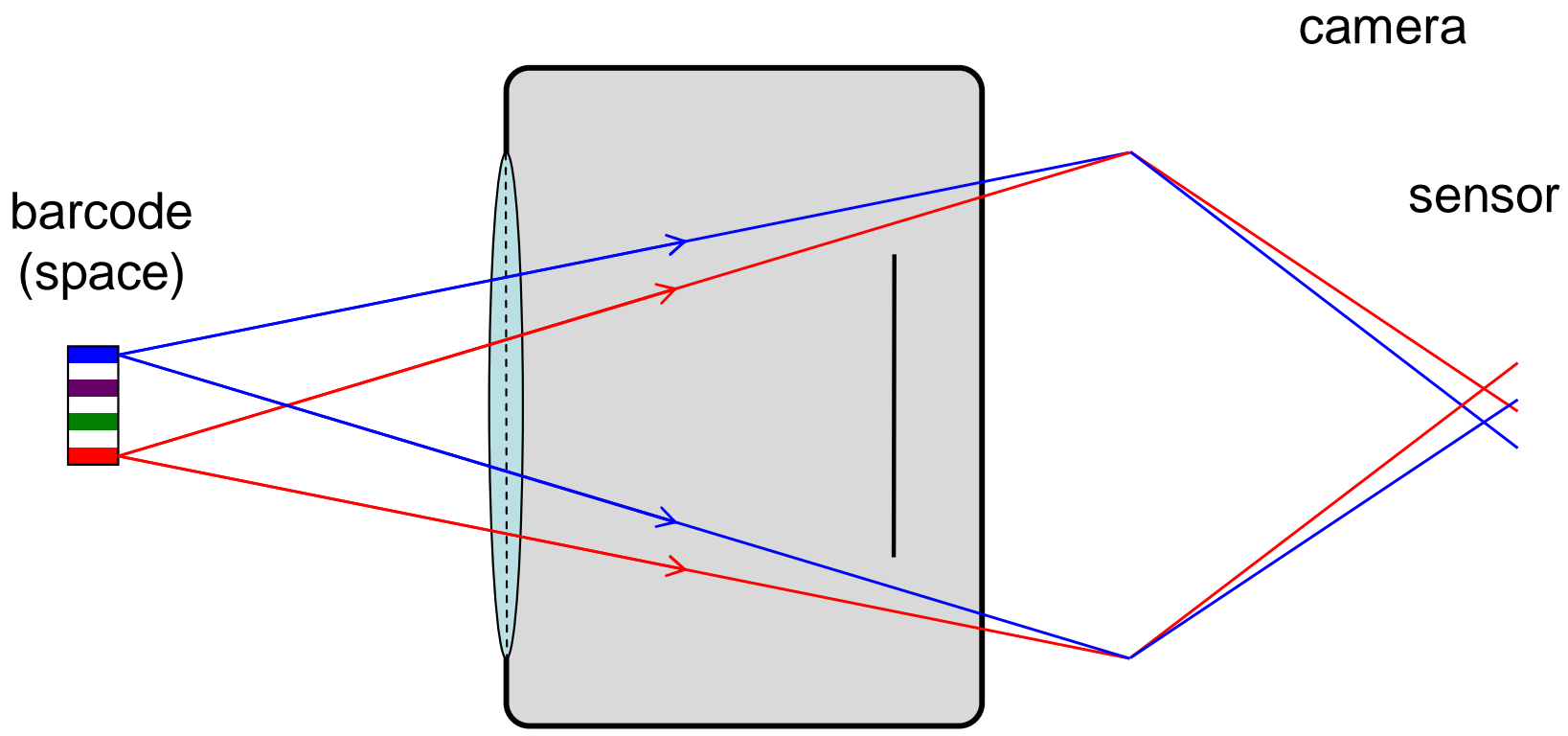
We are seeking a talented and highly motivated Postdoctoral Fellow with a strong background in computer graphics, vision, HCI and/or applied optics.

Camera Culture Group conducts multi-disciplinary research in computational imaging, modern optics, sensors, illumination, actuators, probes and software processing. This work ranges from creating novel feature-revealing computational cameras and new lightweight medical imaging mechanisms, to facilitating positive social impact via the next billion personalized cameras.

Please refer to the group webpage for instructions on how to apply.  
<http://cameraculture.media.mit.edu/join>

**\*Keywords:** Computational photography and imaging, Displays, Signal processing, Applied optics, Computer graphics and vision, Medical Imaging, Thermal and ultrasound sensing, Electronic hardware, Art, Online photo collections, Internet Vision, Visual social computing.





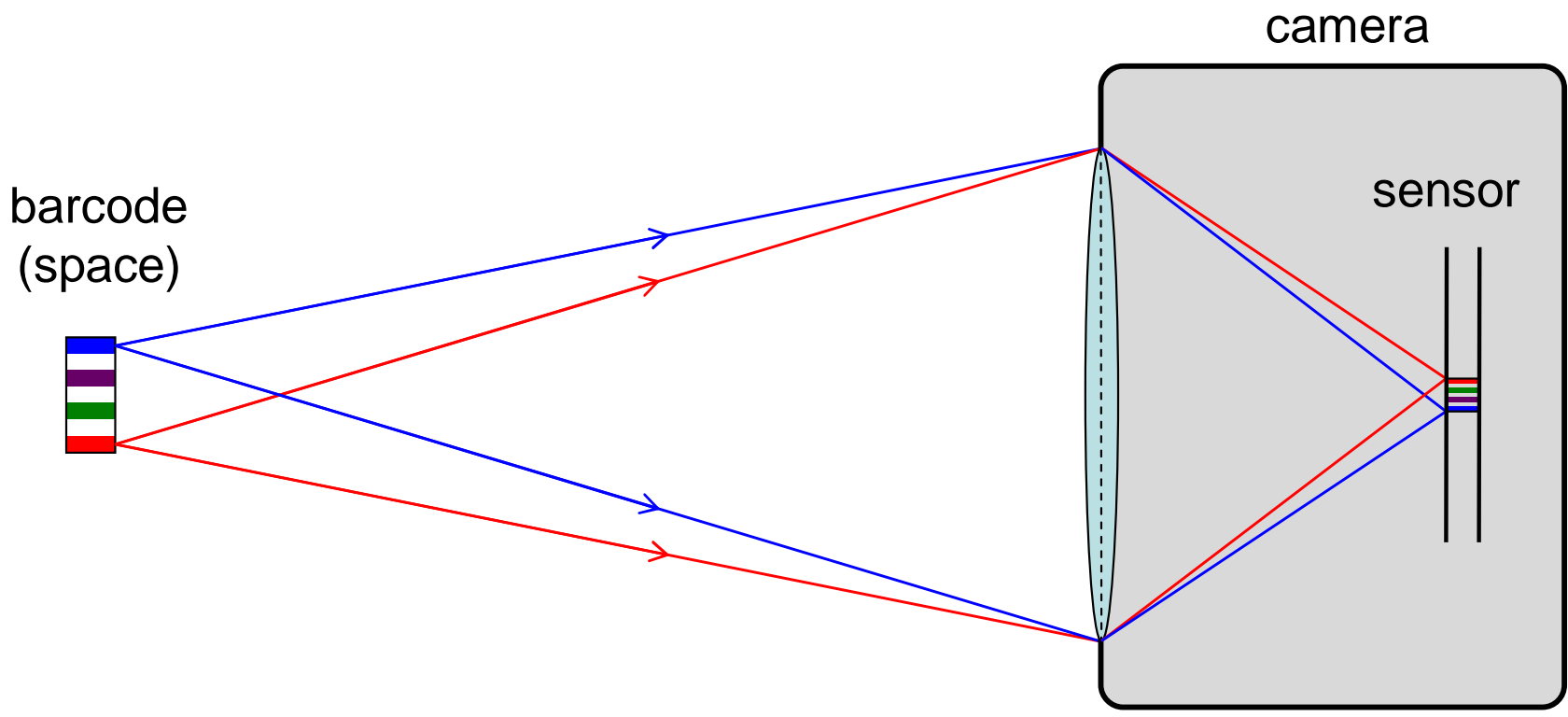
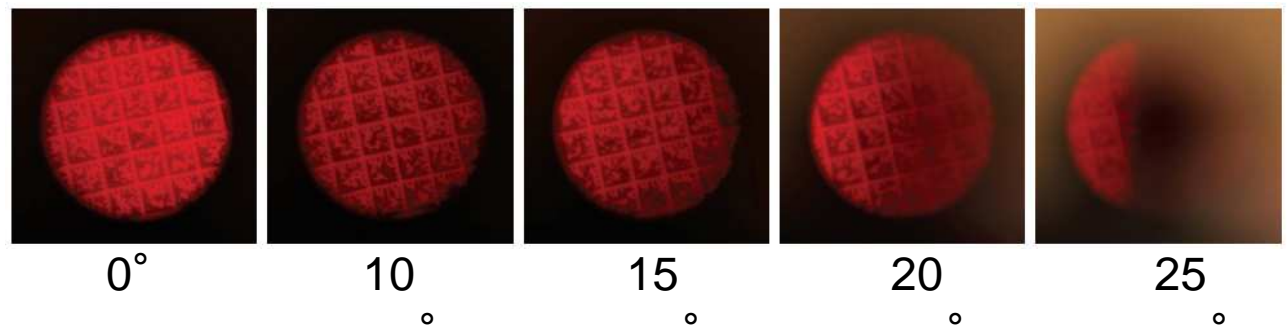
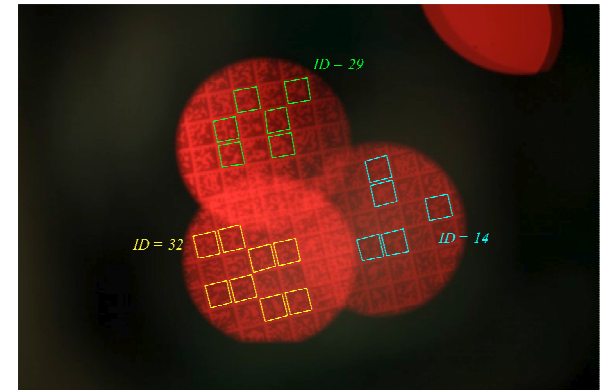


image much smaller;  
refocus if distance changes

# limitations

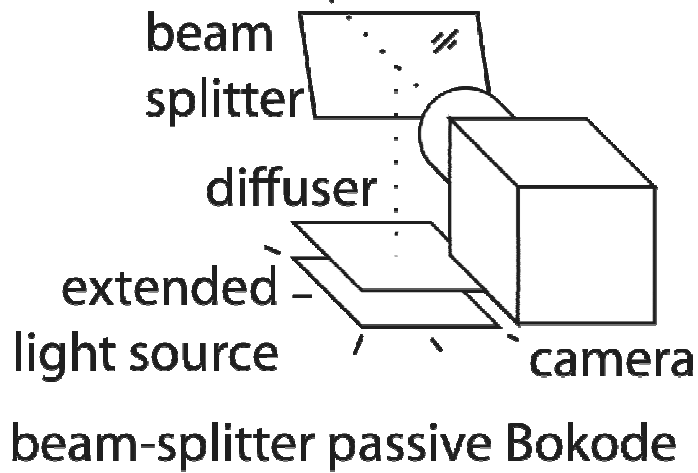
- overlapping Bokodes
- auto-exposure / motion blur
- angular range ( $\pm 20^\circ$ )



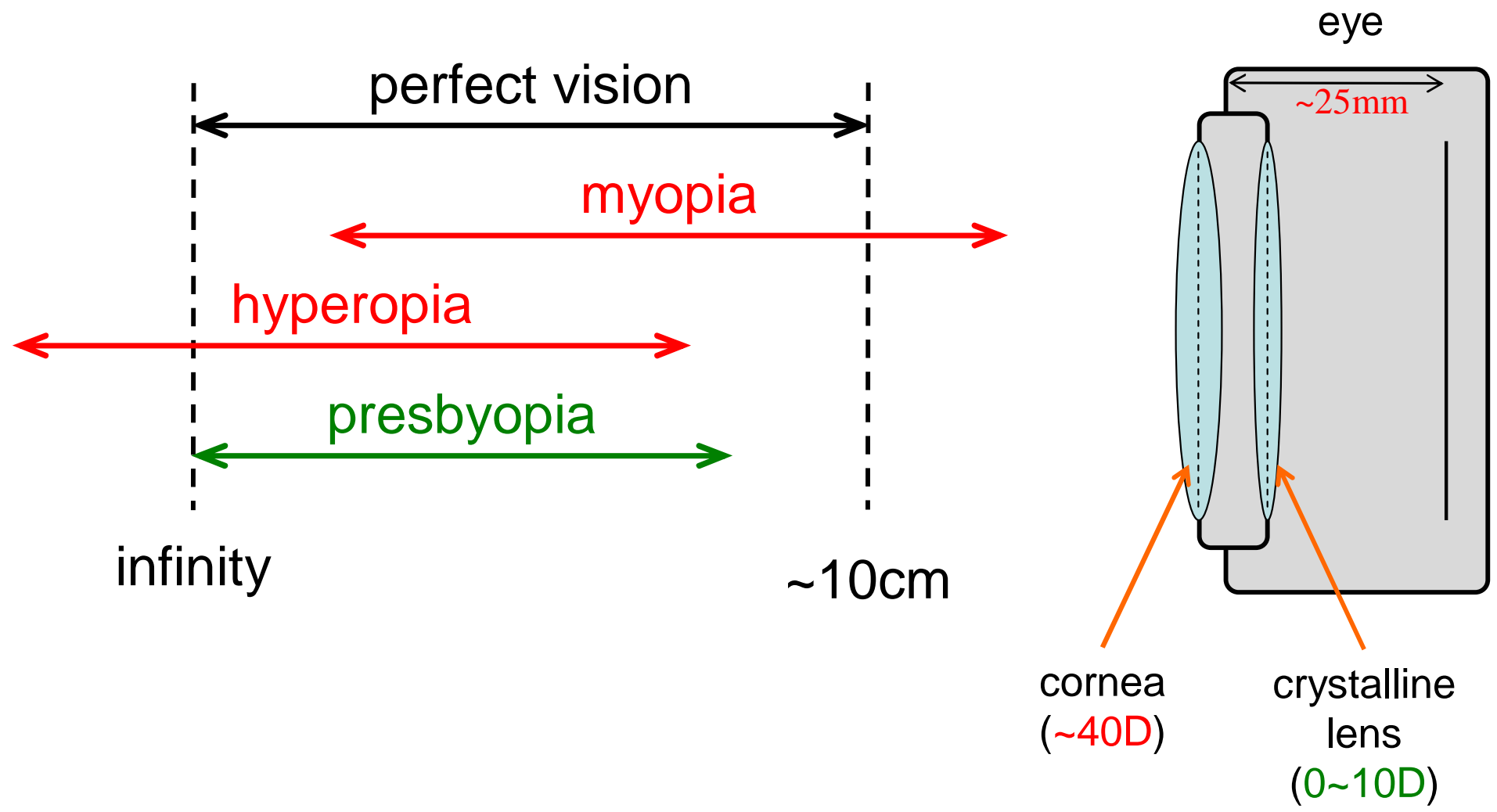
- thickness  $\rightarrow$  holographic Bokode



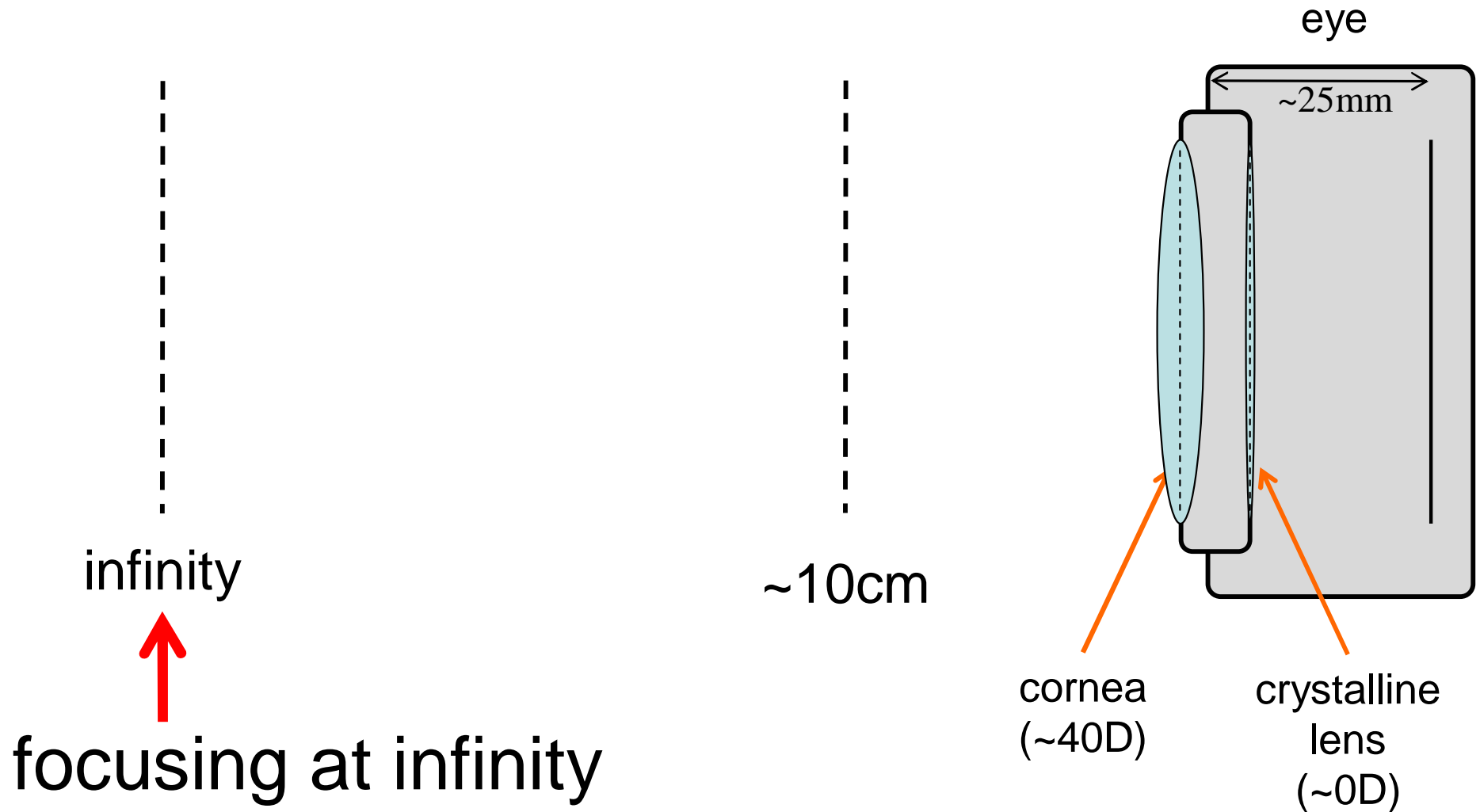
# retro-reflector for passive Bokode



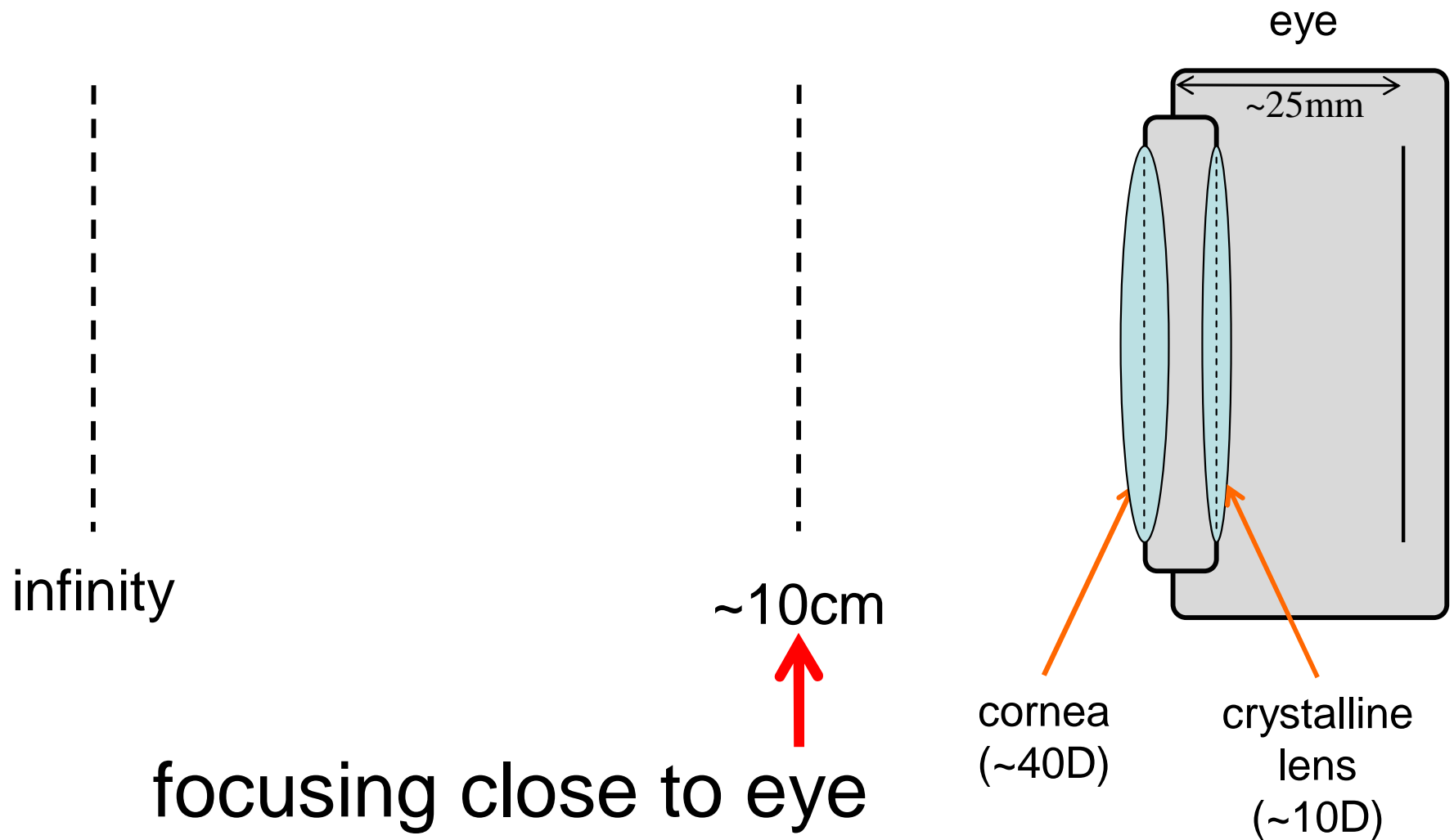
# focusing range and refractive errors



# accommodation



# accommodation



# Impact / PerfectSight



MIT IDEAS award to deploy in Mwanda, Malawi



So that all may see  
L V Prasad Eye Institute

sending 4 prototypes over the summer



local testing

