# Mining Billion-node Graphs: Patterns, Generators and Tools

# Christos Faloutsos CMU

## **Thanks!**

- Andy Yoo
- Tina Eliassi-Rad
- Brian Gallagher
- Keith Henderson
- Irene Massiat









## **Our goal:**

Open source system for mining huge graphs:

PEGASUS project (PEta GrAph mining System)

• www.cs.cmu.edu/~pegasus

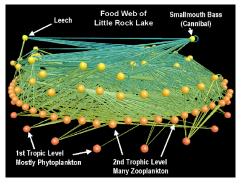


• code and papers

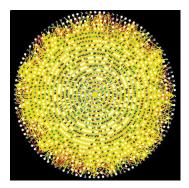
## Outline

- Introduction Motivation
  - Problem#1: Patterns in graphs
  - Problem#2: Tools
  - Problem#3: Scalability
  - Conclusions

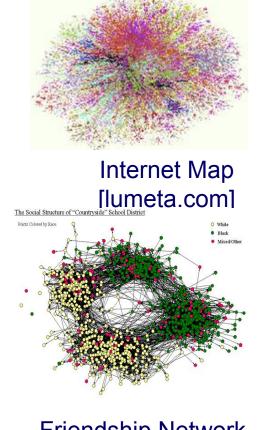
## **Graphs - why should we care?**



Food Web [Martinez '91]



Protein Interactions [genomebiology.com]

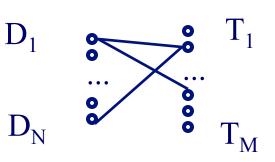


Friendship Network [Moody '01]

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# **Graphs - why should we care?**

• IR: bi-partite graphs (doc-terms)



• web: hyper-text graph

• ... and more:

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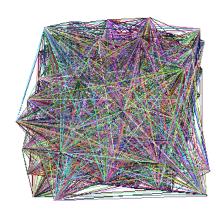
# **Graphs - why should we care?**

- network of companies & board-of-directors members
- 'viral' marketing
- web-log ('blog') news propagation
- computer network security: email/IP traffic and anomaly detection

## Outline

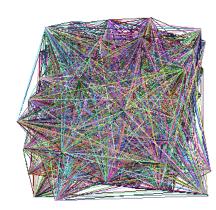
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  - Static graphs
  - Weighted graphs
  - Time evolving graphs
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# Problem #1 - network and graph mining



- How does the Internet look like?
- How does FaceBook look like?
- What is 'normal'/'abnormal'?
- which patterns/laws hold?

# Problem #1 - network and graph mining

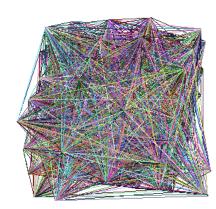


• How does the Internet look like?

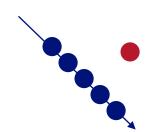
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- What is 'normal'/'abnormal'?
- which patterns/laws hold?
  - To spot anomalies (rarities), we have to discover patterns

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# Problem #1 - network and graph mining



- How does the Internet look like?
- How does FaceBook look like?
- What is 'normal'/'abnormal'?
- which patterns/laws hold?
  - To spot anomalies (rarities), we have to discover patterns
  - Large datasets reveal patterns/anomalies that may be invisible otherwise...



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# **Graph mining**

• Are real graphs random?

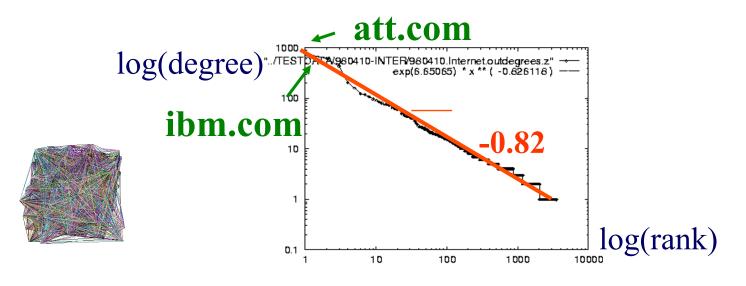
# Laws and patterns

- Are real graphs random?
- A: NO!!
  - Diameter
  - in- and out- degree distributions
  - other (surprising) patterns
- So, let's look at the data

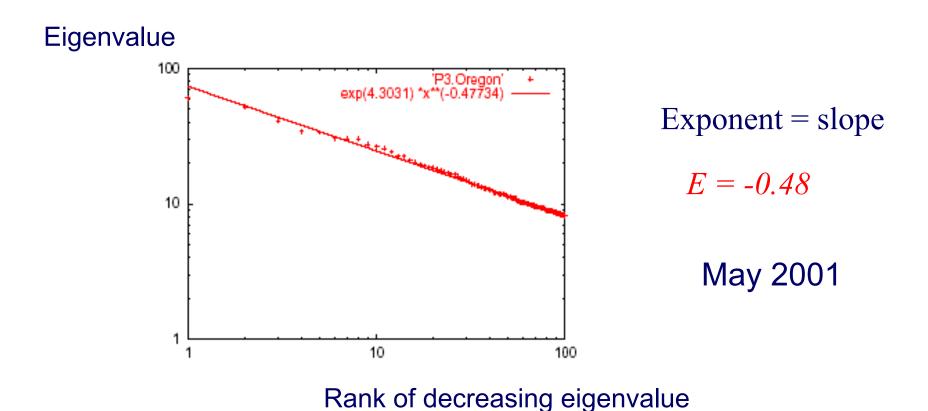
## **Solution# S.1**

• Power law in the degree distribution [SIGCOMM99]

internet domains



# Solution# S.2: Eigen Exponent E



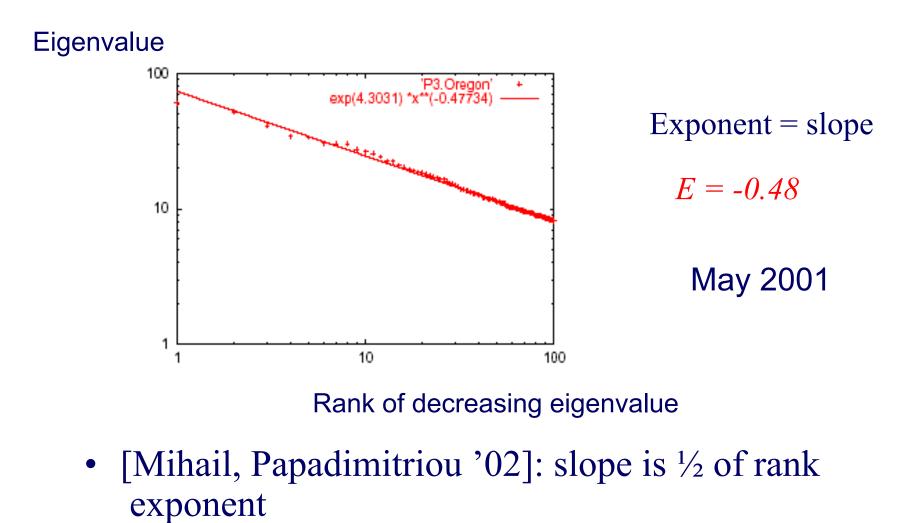
• A2: power law in the eigenvalues of the adjacency matrix

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# Solution# S.2: Eigen Exponent E



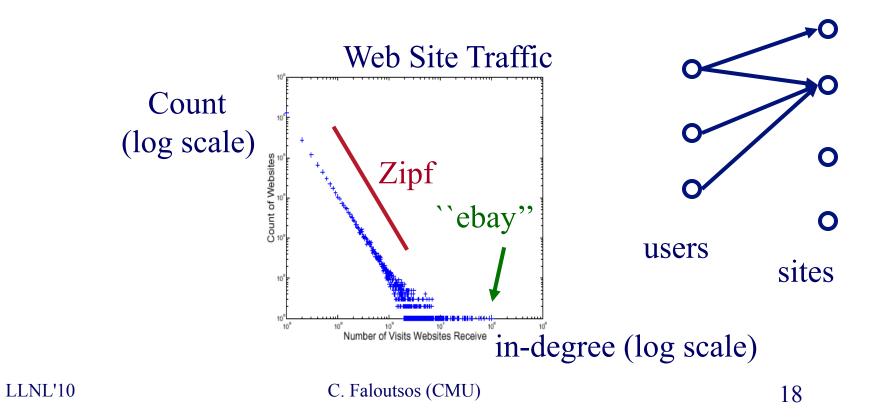
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## **But:**

#### How about graphs from other domains?

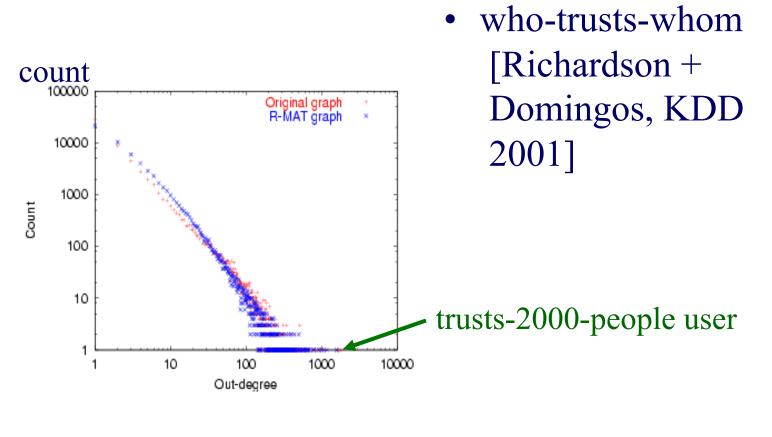
## More power laws:

• web hit counts [w/ A. Montgomery]



0

## epinions.com



#### (out) degree

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## And numerous more

- # of sexual contacts
- Income [Pareto] –'80-20 distribution'
- Duration of downloads [Bestavros+]
- Duration of UNIX jobs ('mice and elephants')
- Size of files of a user
- . .
- 'Black swans'

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- Problem#1: Patterns in graphs
  - Static graphs
    - degree, diameter, eigen,
    - triangles
    - cliques
  - Weighted graphs
  - Time evolving graphs
- Problem#2: Tools

# Solution# S.3: Triangle 'Laws'

• Real social networks have a lot of triangles

# Solution# S.3: Triangle 'Laws'

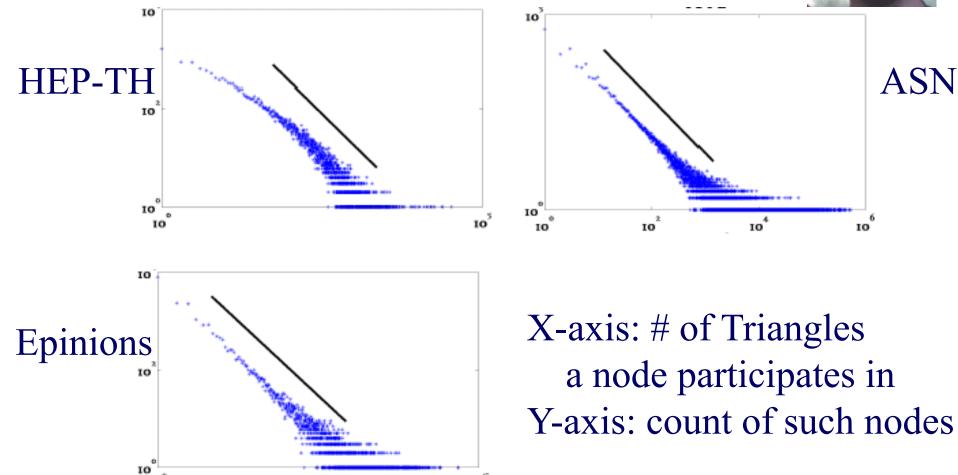
- Real social networks have a lot of triangles

   Friends of friends are friends
- Any patterns?

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## Triangle Law: #S.3 [Tsourakakis ICDM 2008]





10<sup>5</sup> )s (CMU)

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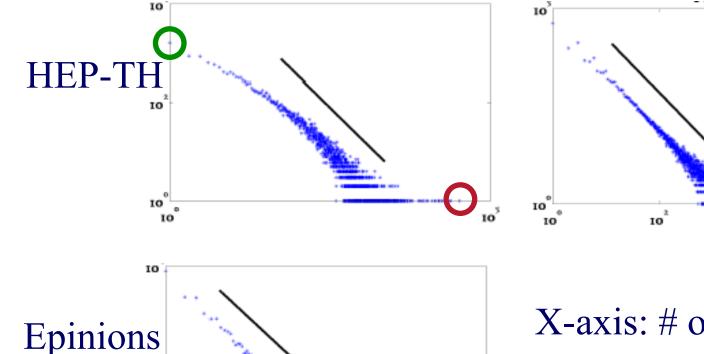
## Triangle Law: #S.3 [Tsourakakis ICDM 2008]



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**ASN** 

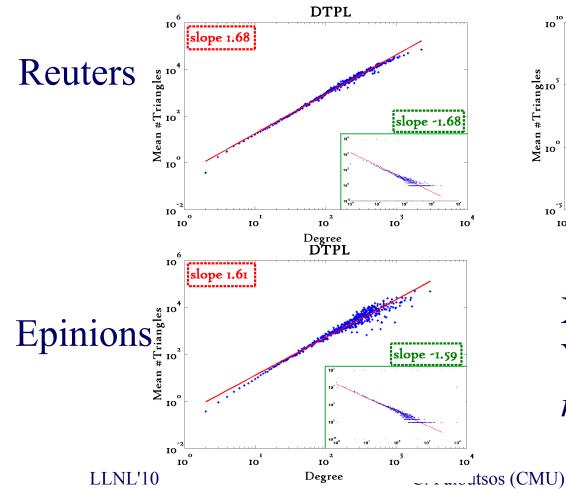


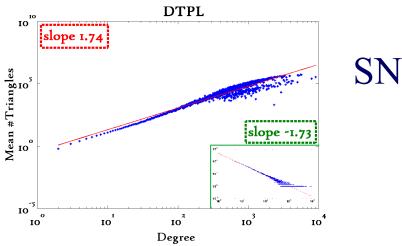
X-axis: # of Triangles a node participates in Y-axis: count of such nodes

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## Triangle Law: #S.4 [Tsourakakis ICDM 2008]





X-axis: degree Y-axis: mean # triangles *n* friends ->  $\sim n^{1.6}$  triangles

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## **Triangle Law: Computations** [Tsourakakis ICDM 2008]

But: triangles are expensive to compute (3-way join; several approx. algos) Q: Can we do that quickly?



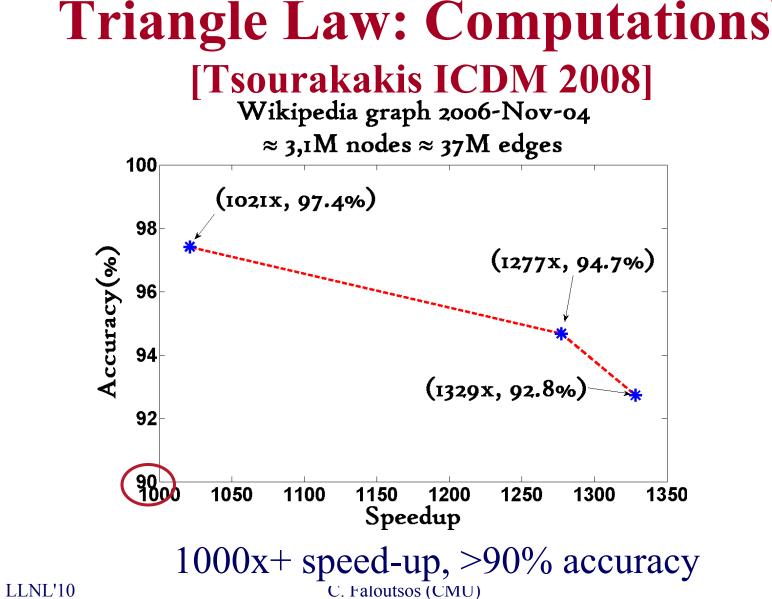
## **Triangle Law: Computations** [Tsourakakis ICDM 2008]

But: triangles are expensive to compute (3-way join; several approx. algos)Q: Can we do that quickly?A: Yes!

### #triangles = 1/6 Sum ( $\lambda_i^3$ ) (and, because of skewness, we only need the top few eigenvalues!

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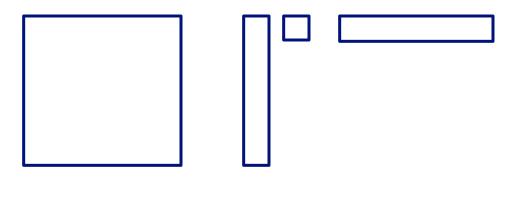
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B. Aditya Prakash, Mukund Seshadri, Ashwin Sridharan, Sridhar Machiraju and Christos Faloutsos: *EigenSpokes: Surprising Patterns and Scalable Community Chipping in Large Graphs*, PAKDD 2010, Hyderabad, India, 21-24 June 2010.

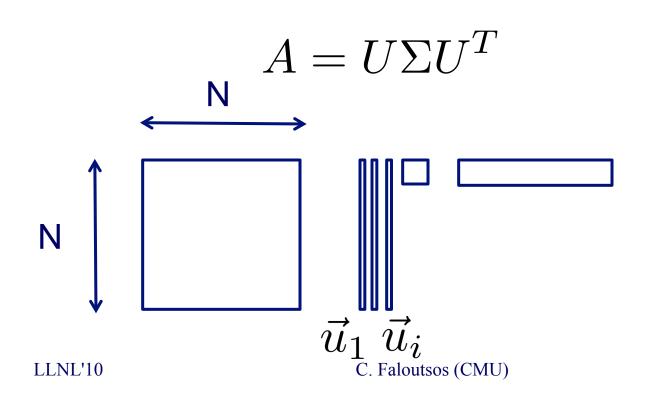
- Eigenvectors of adjacency matrix
  - equivalent to singular vectors (symmetric, undirected graph)

$$A = U\Sigma U^T$$



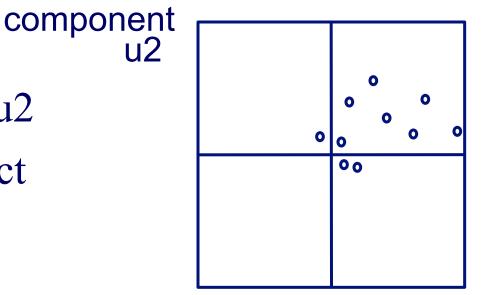


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2<sup>nd</sup> Principal

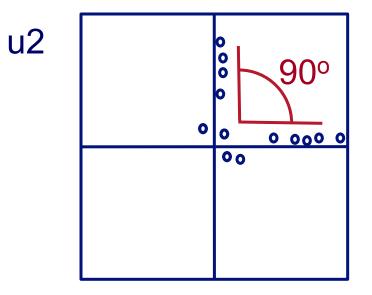
- EE plot:
- Scatter plot of scores of u1 vs u2
- One would expect
  - Many points @ origin
  - A few scattered
     ~randomly



u1 1<sup>st</sup> Principal component

- EE plot:
- Scatter plot of scores of u1 vs u2
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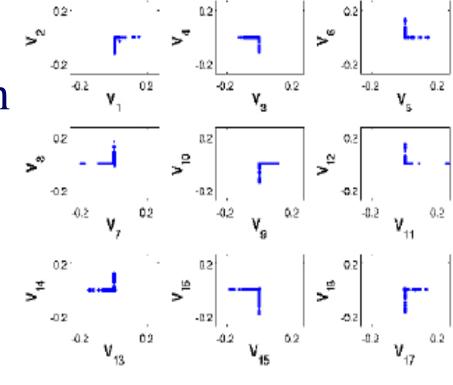


u1

# **EigenSpokes - pervasiveness**

- Present in mobile social graph
  - across time and space

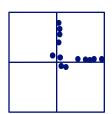


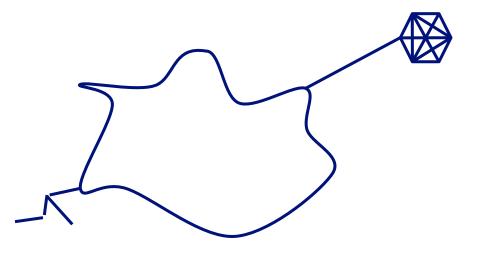


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## **EigenSpokes - explanation**

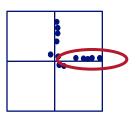
Near-cliques, or near -bipartite-cores, loosely connected

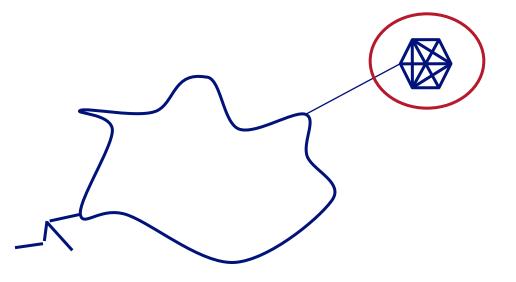




#### **EigenSpokes - explanation**

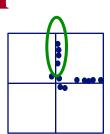
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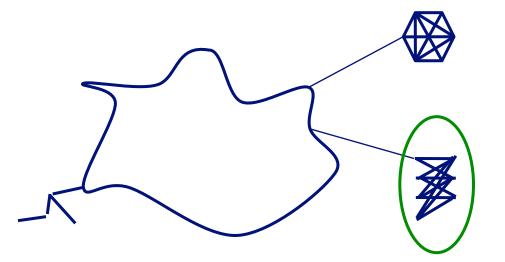




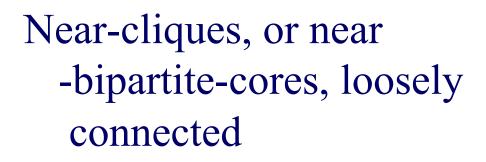
# **EigenSpokes - explanation**

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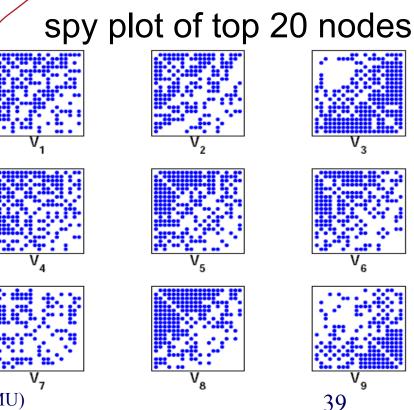


# **EigenSpokes - explanation**



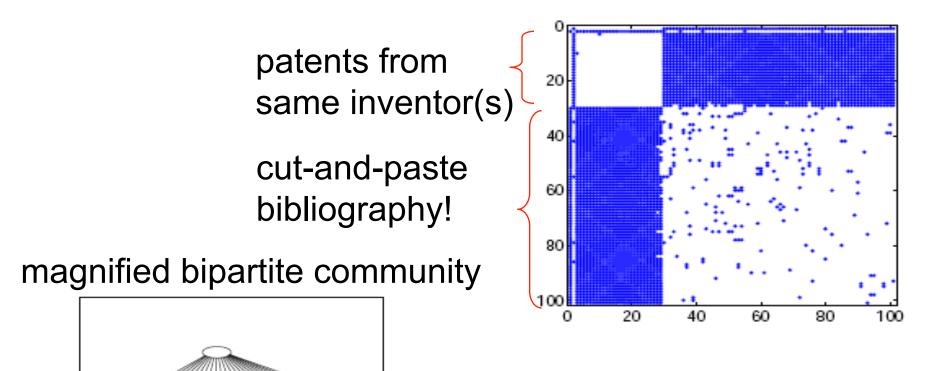
So what?

- Extract nodes with high scores
- high connectivity
- Good "communities"



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#### **Bipartite Communities!**



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  - Time evolving graphs
- Problem#2: Tools

# Observations on weighted graphs?

• A: yes - even more 'laws'!



M. McGlohon, L. Akoglu, and C. Faloutsos Weighted Graphs and Disconnected Components: Patterns and a Generator. SIG-KDD 2008

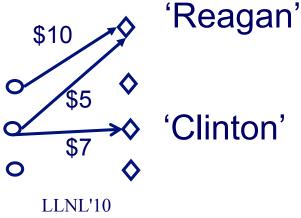
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#### **Observation W.1: Fortification**

Q: How do the weights of nodes relate to degree?

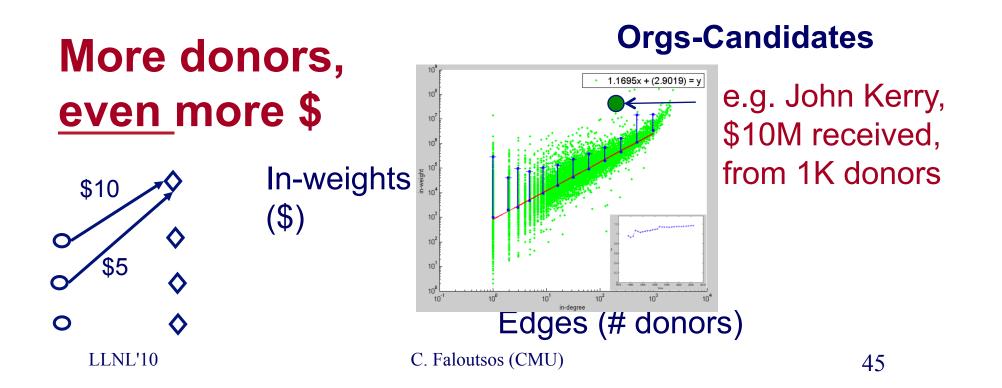
#### **Observation W.1: Fortification**

# More donors, more \$ ?



# **Observation W.1: fortification: Snapshot Power Law**

- Weight: super-linear on in-degree
- exponent 'iw': 1.01 < iw < 1.26



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#### **Problem: Time evolution**

 with Jure Leskovec (CMU -> Stanford)



• and Jon Kleinberg (Cornell – sabb. @ CMU)



# **T.1 Evolution of the Diameter**

- Prior work on Power Law graphs hints at **slowly growing diameter**:
  - diameter  $\sim O(\log N)$
  - diameter  $\sim O(\log \log N)$
- What is happening in real data?

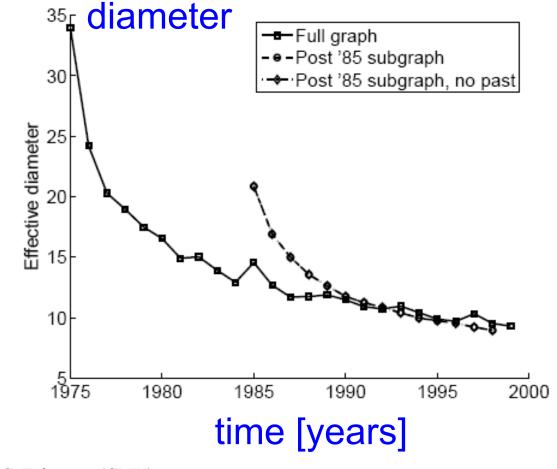
# **T.1 Evolution of the Diameter**

- Prior work on Power Law graphs hints at slowly growing diameter:

  - diameter ~ (ICTN)
    diameter ~ O(ICTN)
- What is happening in real data?
- Diameter shrinks over time

#### T.1 Diameter – "Patents"

- Patent citation network
- 25 years of data
- @1999
  - 2.9 M nodes
  - 16.5 M edges



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# **T.2 Temporal Evolution of the Graphs**

- N(t) ... nodes at time t
- E(t) ... edges at time t
- Suppose that

N(t+1) = 2 \* N(t)

• Q: what is your guess for E(t+1) =? 2 \* E(t)

# **T.2 Temporal Evolution of the Graphs**

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- Suppose that

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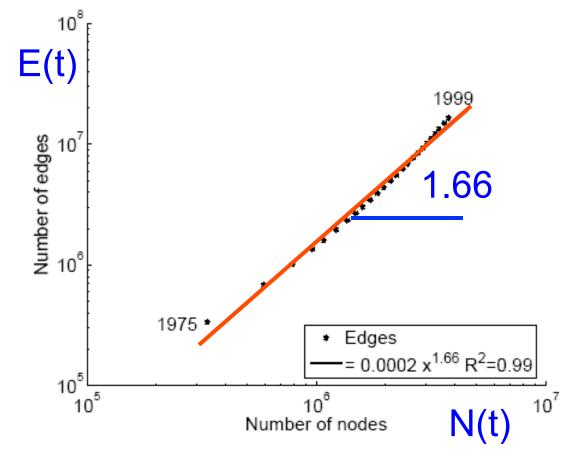
- Q: what is your guess for E(t+1) • E(t)
- A: over-doubled!

– But obeying the ``Densification Power Law''

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# T.2 Densification – Patent Citations

- Citations among patents granted
- @1999
  - 2.9 M nodes
  - 16.5 M edges
- Each year is a datapoint



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#### Outline

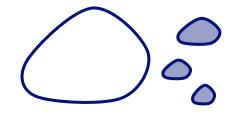
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# More on Time-evolving graphs

M. McGlohon, L. Akoglu, and C. Faloutsos Weighted Graphs and Disconnected Components: Patterns and a Generator. SIG-KDD 2008

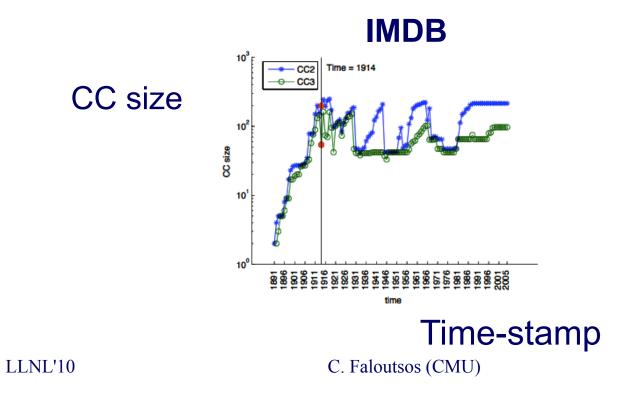
# **Observation T.3: NLCC behavior**

- *Q: How do NLCC's emerge and join with the GCC?*
- (``NLCC'' = non-largest conn. components)
- -Do they continue to grow in size?
- or do they shrink?
- or stabilize?



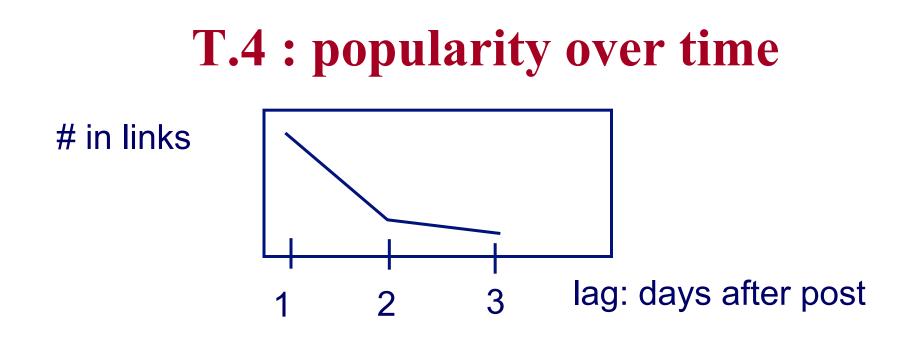
# **Observation T.3: NLCC behavior**

• After the gelling point, the GCC takes off, but NLCC's remain ~constant (actually, oscillate).



#### **Timing for Blogs**

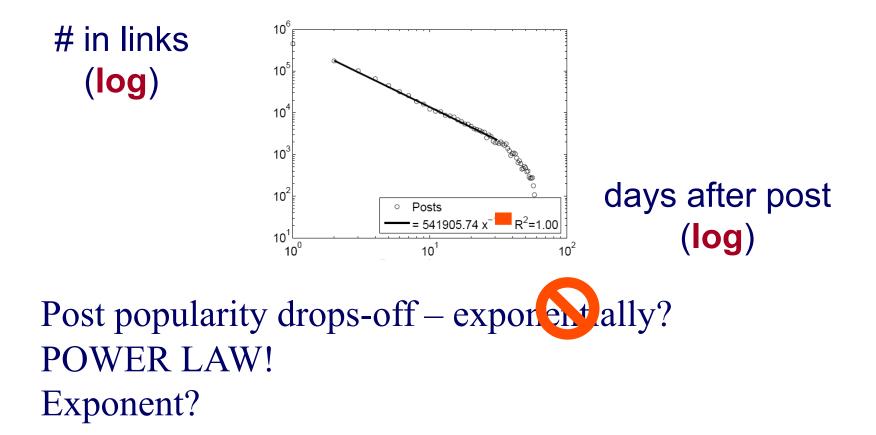
- with Mary McGlohon (CMU)
- Jure Leskovec (CMU->Stanford)
- Natalie Glance (now at Google)
- Mat Hurst (now at MSR)
  [SDM'07]



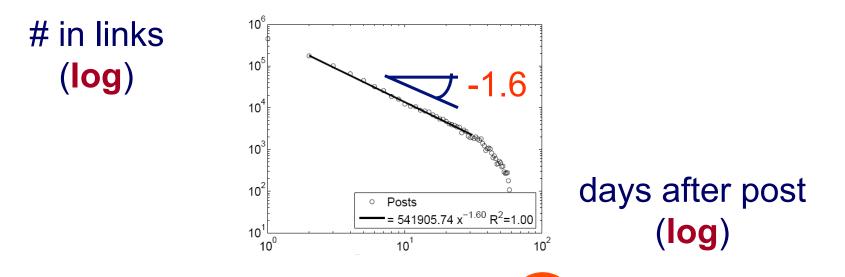
Post popularity drops-off – exponentially? @t + lag

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## **T.4 : popularity over time**

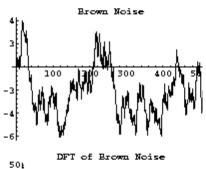


# **T.4 : popularity over time**



Post popularity drops-off – exporent ally? POWER LAW! Exponent? -1.6

- close to -1.5: Barabasi's stack model
- and like the zero-crossings of a random walk C. Faloutsos (CMU)



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- Introduction Motivation
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  - CenterPiece Subgraphs; G-Ray
  - OddBall (anomaly detection)
  - PEGASUS
  - Problem#3: Scalability
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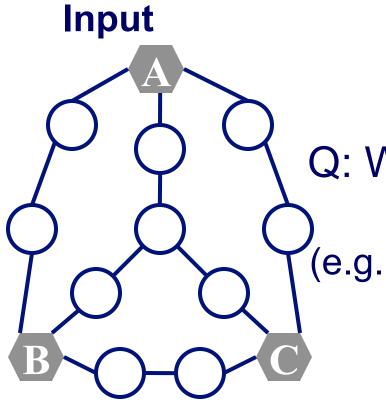
# **CenterPiece Subgraphs**

• Hanghang TONG et al, KDD'06



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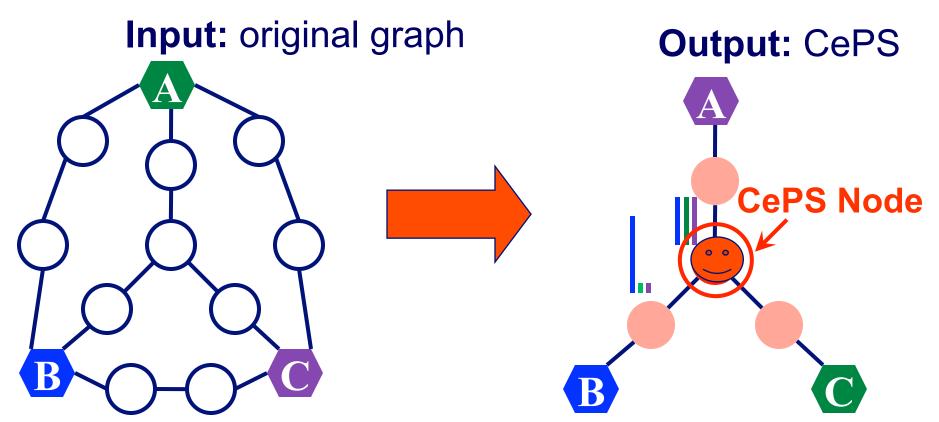
#### Center-Piece Subgraph Discovery [Tong+ KDD 06]



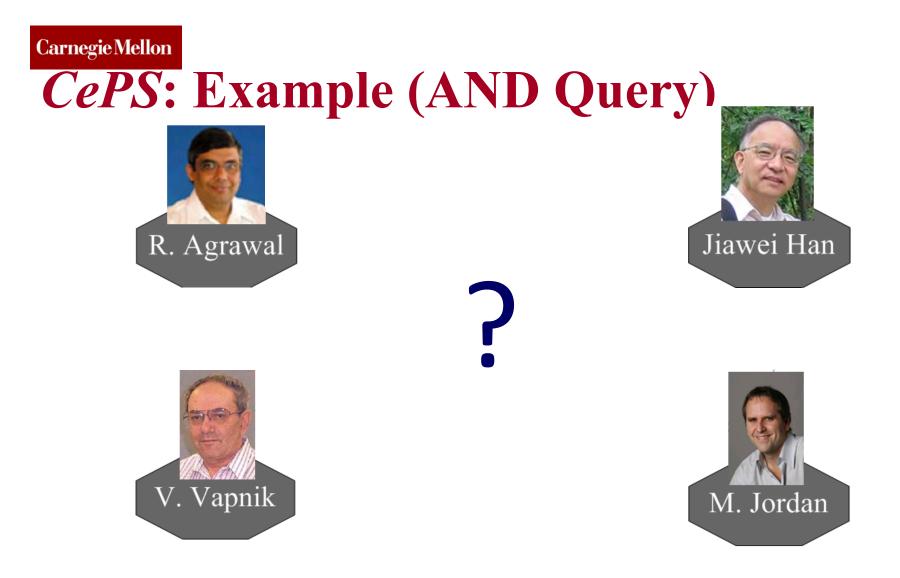
Q: Who is the most central node wrt the black nodes? (e.g., master-mind criminal, common advisor/collaborator, etc)

#### **Original Graph**

#### Center-Piece Subgraph Discovery [Tong+ KDD 06]

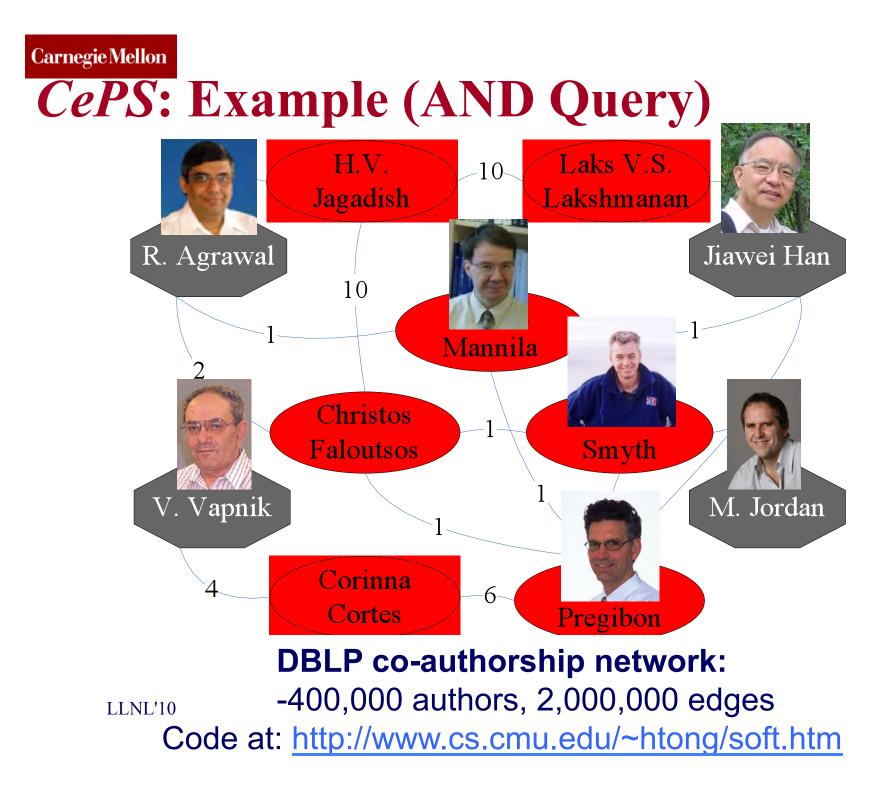


Q: How to find hub for the query nodes?LLNL'10A: Combine proximity scores (RWR)65



#### DBLP co-authorship network:

-400,000 authors, 2,000,000 edges Code at: <u>http://www.cs.cmu.edu/~htong/soft.htm</u>

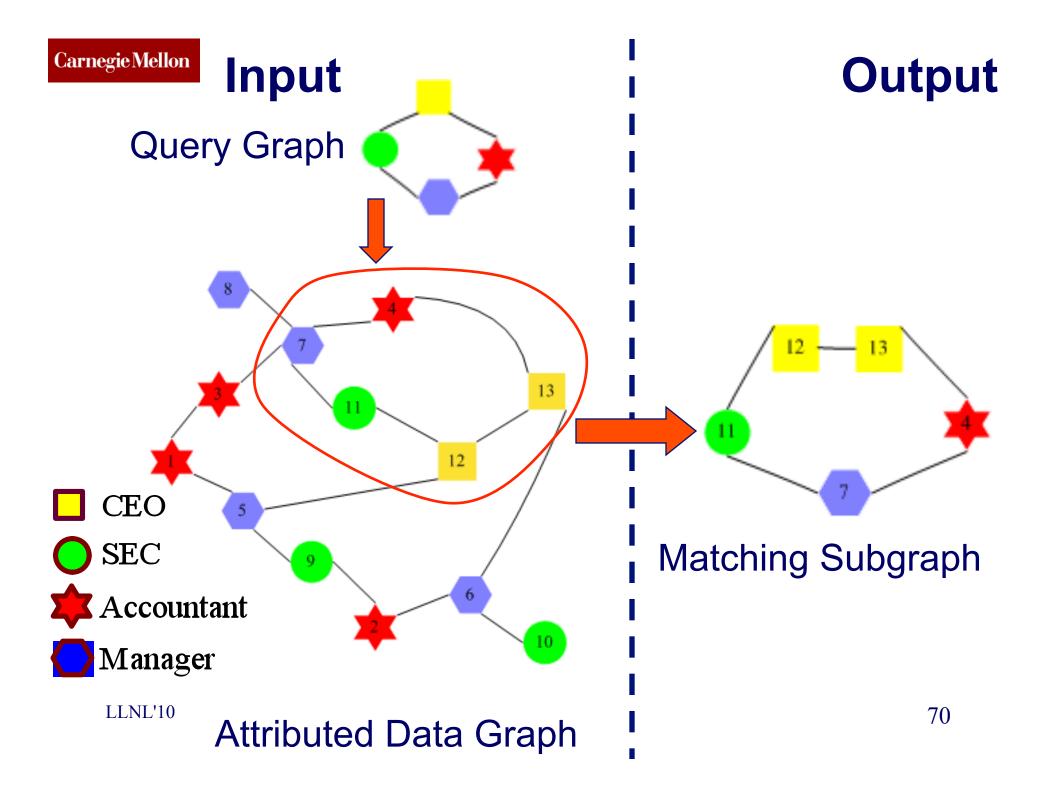


#### Outline

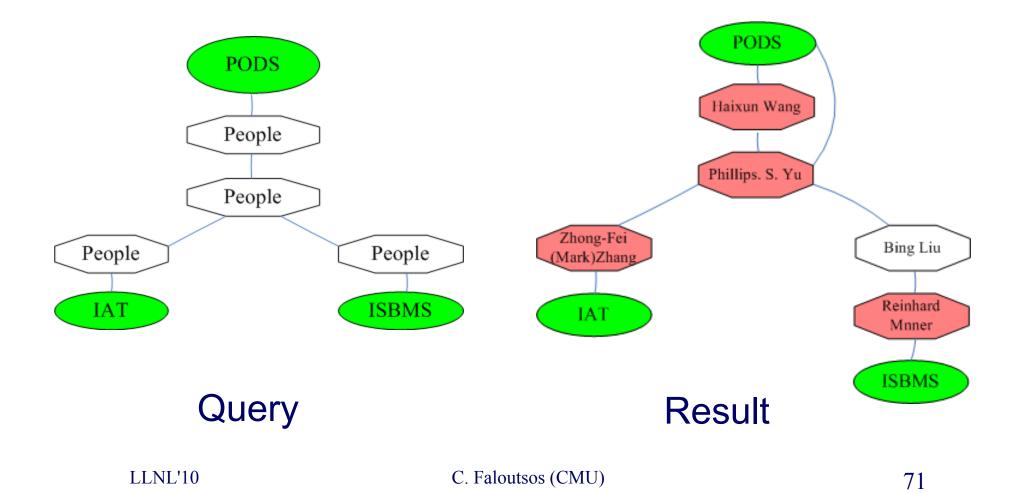
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# **Graph X-Ray: Fast Best-Effort Pattern Matching in Large Attributed Graphs**

Hanghang Tong, Brian Gallagher, Christos Faloutsos, Tina Eliassi-Rad KDD'07



#### **Effectiveness: star-query**



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# OddBall: Spotting Anomalies in Weighted Graphs





Leman Akoglu, Mary McGlohon, Christos Faloutsos

> Carnegie Mellon University School of Computer Science

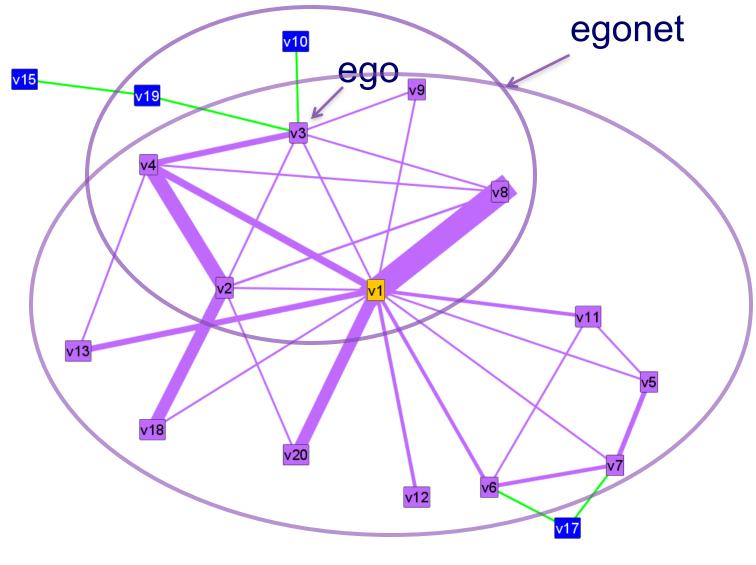
To appear in PAKDD 2010, Hyderabad, India

## Main idea

For each node,

- extract 'ego-net' (=1-step-away neighbors)
- Extract features (#edges, total weight, etc etc)
- Compare with the rest of the population

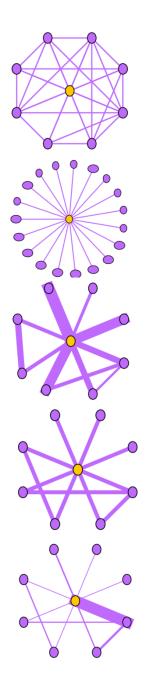
# What is an egonet?



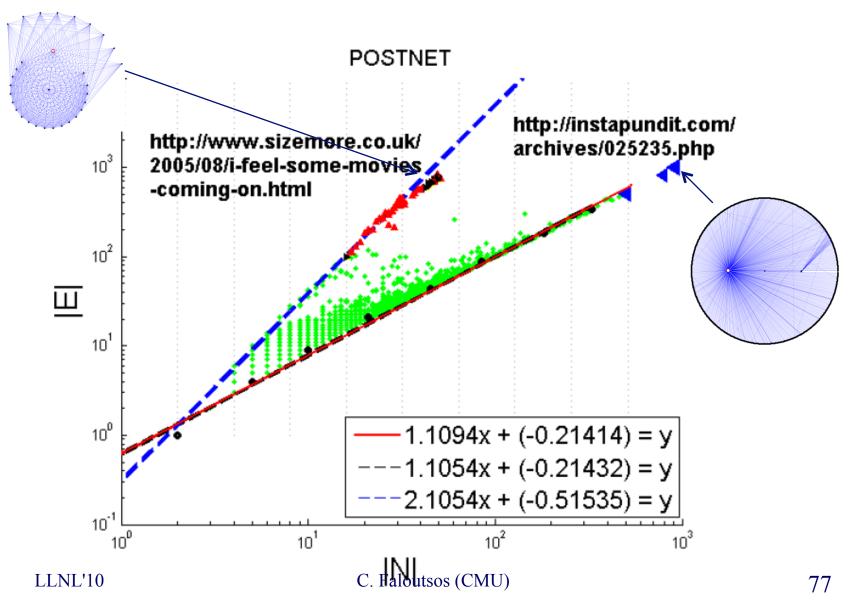
**Carnegie Mellon** 

# **Selected Features**

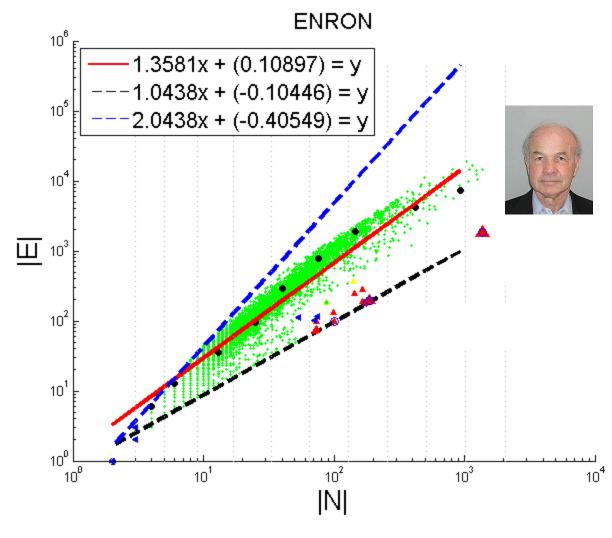
- $N_i$ : number of neighbors (degree) of ego i
- $E_i$ : number of edges in egonet i
- $W_i$ : total weight of egonet *i*
- $\lambda_{w,i}$ : principal eigenvalue of the weighted adjacency matrix of egonet *I*



# **Near-Clique/Star**



# **Near-Clique/Star**



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#### **Outline – Algorithms & results**

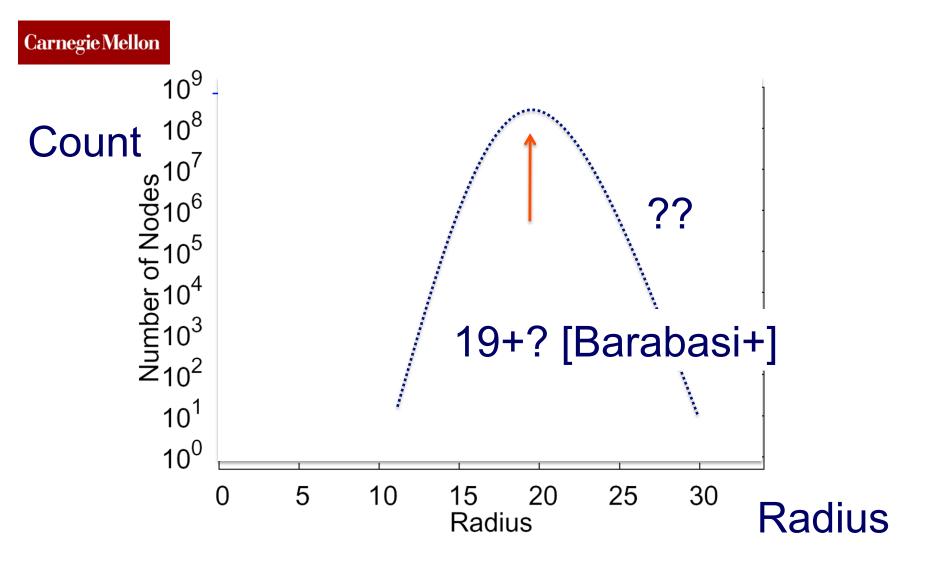
	Centralized	Hadoop /PEGASUS
Degree Distr.	old	old
Pagerank	old	old
Diameter/ANF	old	DONE
Conn. Comp	old	DONE
Triangles	DONE	
Visualization	STARTED	

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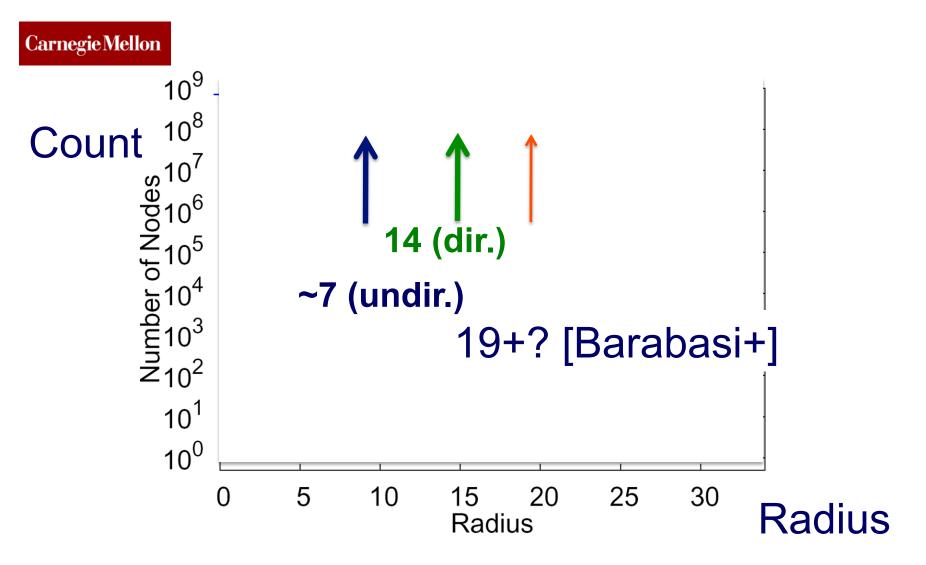
# HADI for diameter estimation

- Radius Plots for Mining Tera-byte Scale Graphs U Kang, Charalampos Tsourakakis, Ana Paula Appel, Christos Faloutsos, Jure Leskovec, SDM'10
- Naively: diameter needs O(N\*\*2) space and up to O(N\*\*3) time – prohibitive (N~1B)
- Our HADI: linear on E (~10B)
  - Near-linear scalability wrt # machines
  - Several optimizations -> 5x faster



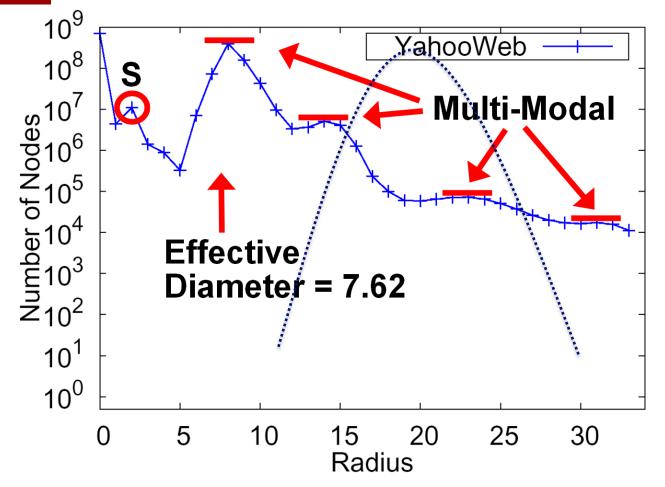
YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

• Largest publicly available graph ever studied.



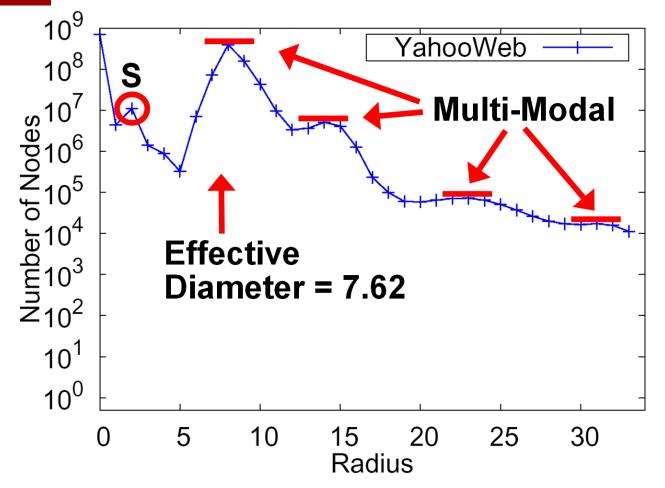
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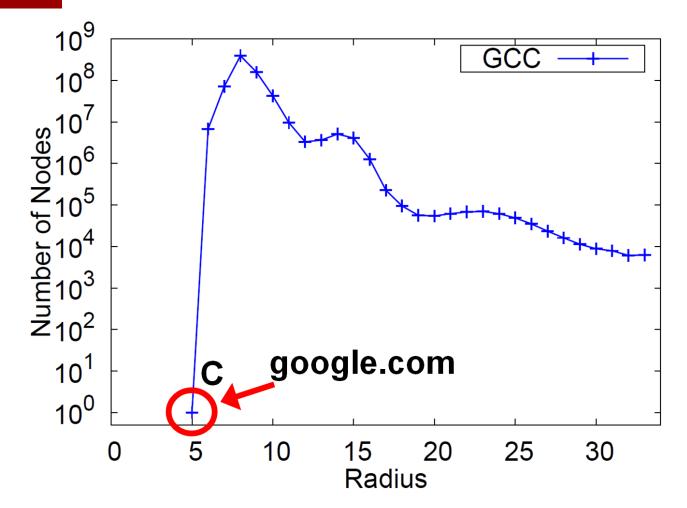
YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

- effective diameter: surprisingly small.
- Multi-modality: probably mixture of cores . C. Faloutsos (CMU)



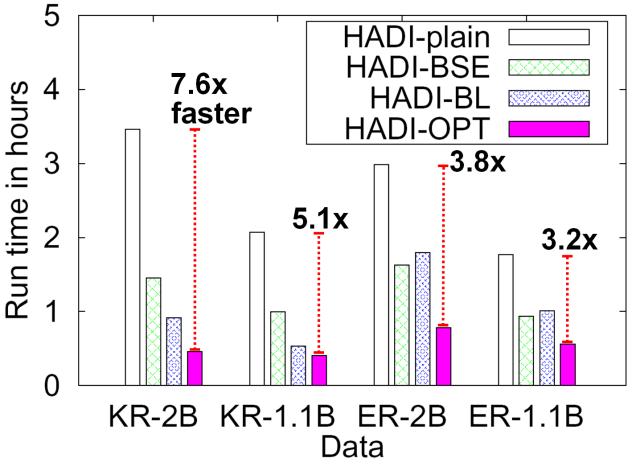
YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

- effective diameter: surprisingly small.
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Radius Plot of GCC of YahooWeb.





Running time - Kronecker and Erdos-Renyi Graphs with billions edges.

#### **Outline – Algorithms & results**

	Centralized	Hadoop /PEGASUS
Degree Distr.	old	old
Pagerank	old	old
Diameter/ANF	old	DONE
Conn. Comp	old	DONE
Triangles	DONE	
Visualization	STARTED	

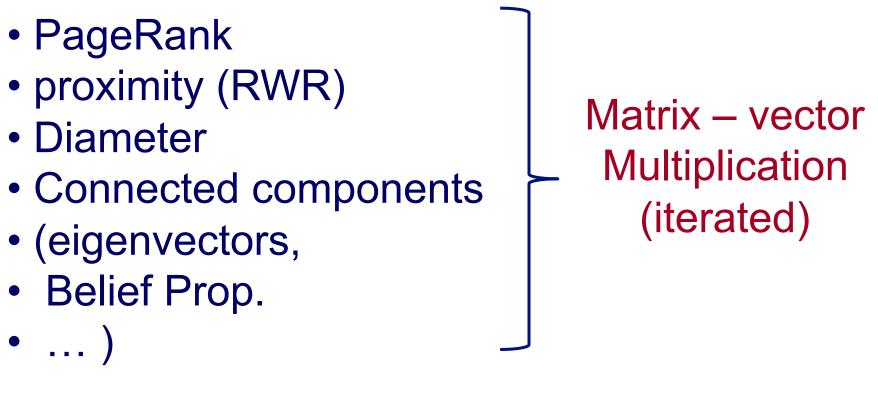
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# **Generalized Iterated Matrix Vector Multiplication (GIMV)**

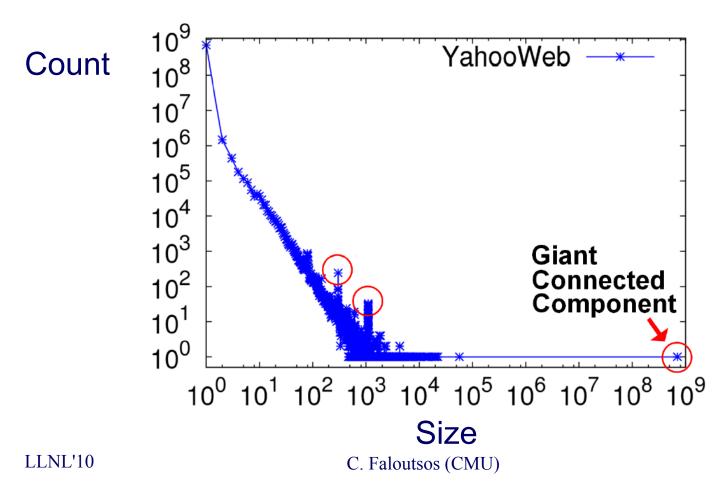
<u>PEGASUS: A Peta-Scale Graph Mining</u> <u>System - Implementation and Observations</u>. U Kang, Charalampos E. Tsourakakis, and Christos Faloutsos. (ICDM) 2009, Miami, Florida, USA. Best Application Paper (runner-up).



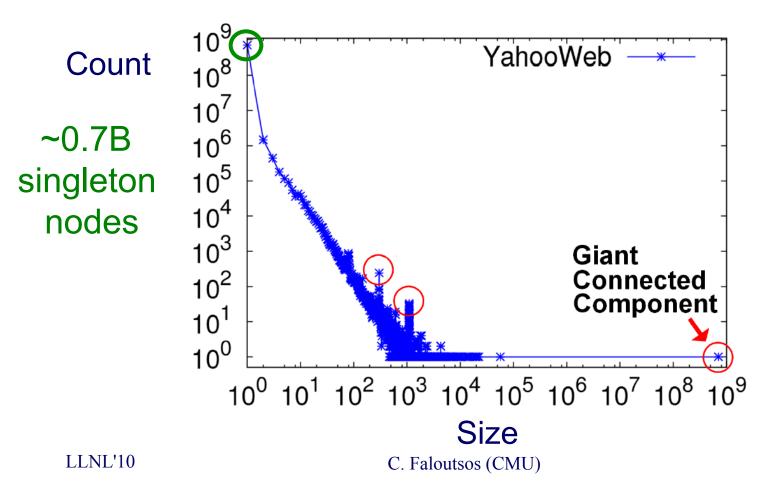
# Generalized Iterated Matrix Vector Multiplication (GIMV)



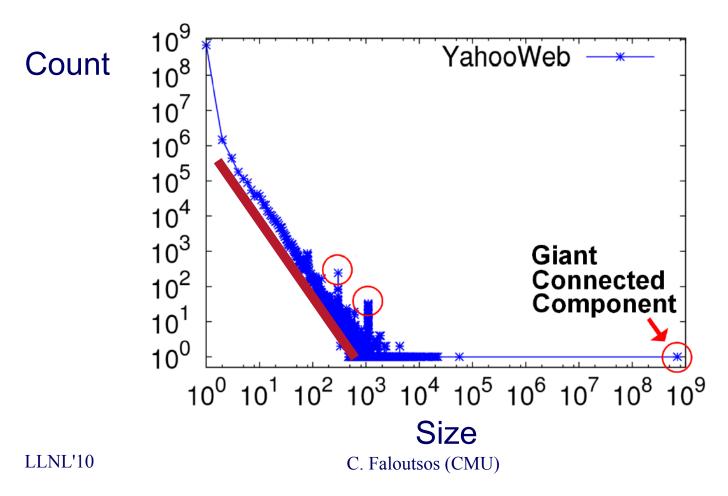
• Connected Components



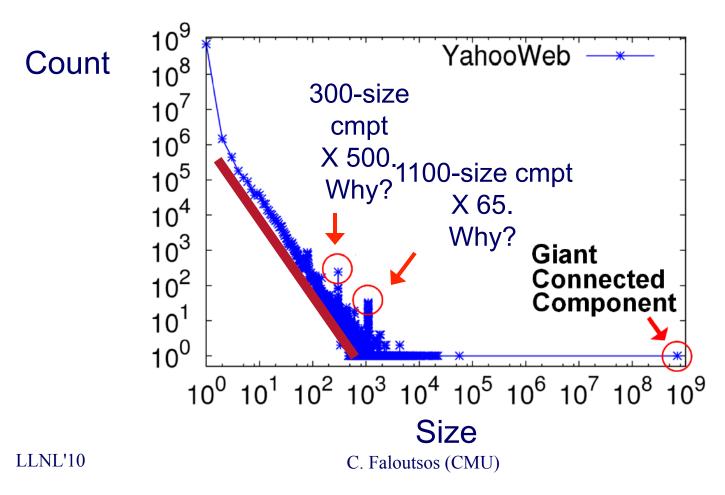
• Connected Components



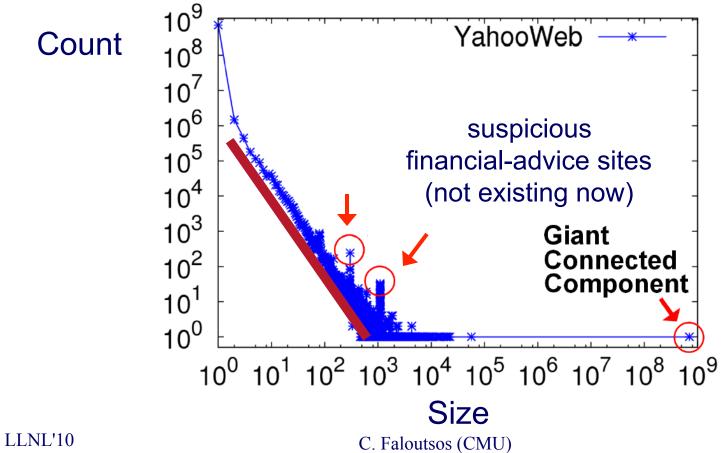
• Connected Components



• Connected Components

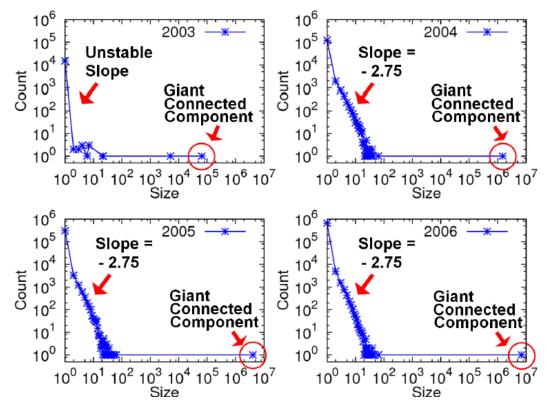


Connected Components



## **GIM-V At Work**

- Connected Components over Time
- LinkedIn: 7.5M nodes and 58M edges



# Stable tail slope after the gelling point

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#### **Outline – Algorithms & results**

	Centralized	Hadoop /PEGASUS
Degree Distr.	old	old
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Diameter/ANF	old	DONE
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Triangles	DONE	
Visualization	STARTED	

# Mentioned alreadyTriangles : Computations[Tsourakakis ICDM 2008]

But: triangles are expensive to compute (3-way join; several approx. algos)Q: Can we do that quickly?A: Yes!

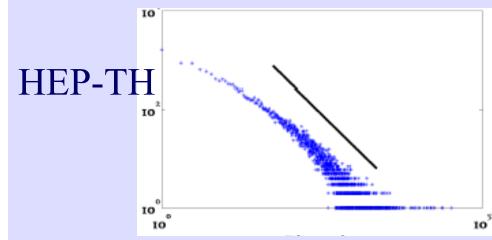


#### #triangles = 1/6 Sum ( $\lambda_i^3$ ) (and, because of skewness, we only need the top few eigenvalues!

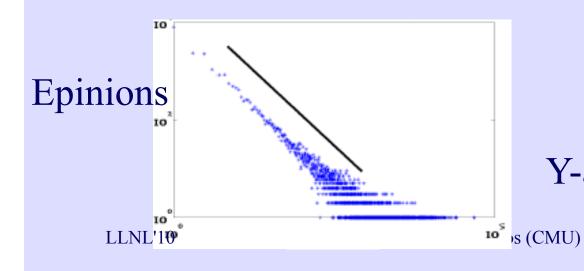
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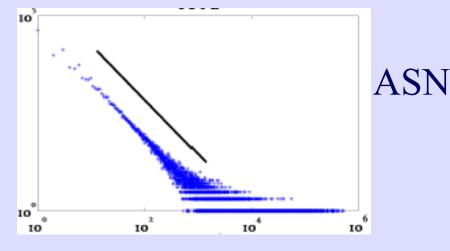
# **Mentioned already**

#### Triangle Law: #1 [Tsourakakis ICDM 2008]



**Carnegie Mellon** 





X-axis: # of Triangles a node participates in Y-axis: count of such nodes

#### **Outline – Algorithms & results**

	Centralized	Hadoop /PEGASUS
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# **Visualization: ShiftR**

 Supporting Ad Hoc Sensemaking: Integrating Cognitive, HCI, and Data Mining Approaches Aniket Kittur, Duen Horng ('Polo') Chau, Christos Faloutsos, Jason I. Hong Sensemaking Workshop at CHI 2009, April 4-5. Boston, MA, USA.

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	C. Taiouisos (CIVIO)	102

#### Outline

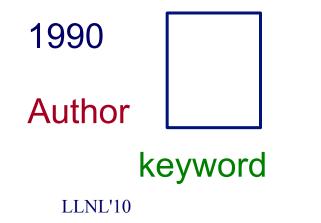
- Introduction Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
- Problem#3: Scalability
- ➡ (additional topics, skipped)
  - Conclusions

### **Other topics - part#1 - tools**

- Community detection how many?
  - Cross-Associations [Chakrabarti +, KDD 2004]
- Time-evolving graphs
  - Tensors [Sun+, KDD'06],
  - [Kolda+ ICDM'05]
  - GraphScope [Sun+, KDD'07]
- Graph compression
  - CUR decomposition [Sun+ SDM'07]

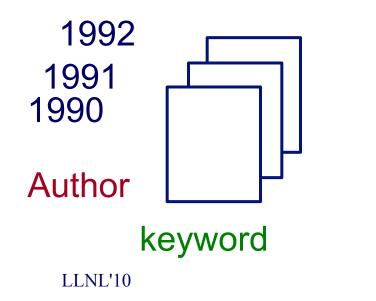
#### Tensors

• Adjacency matrices, stacked (over time, and/or edge-type – 'composite networks')



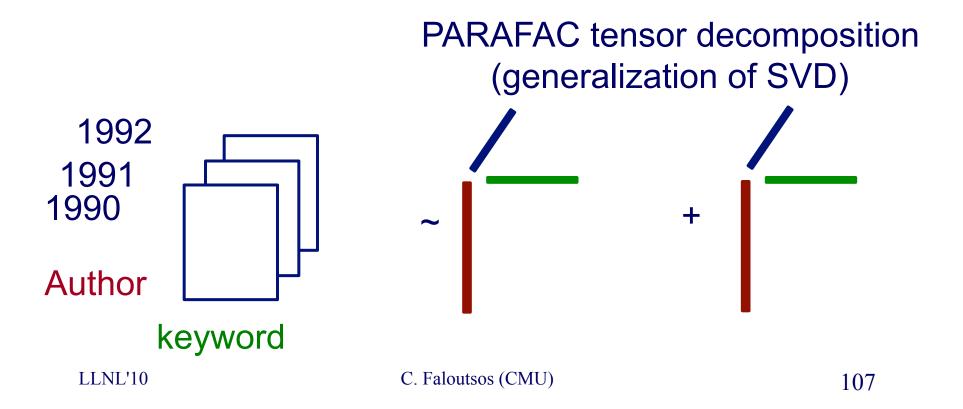
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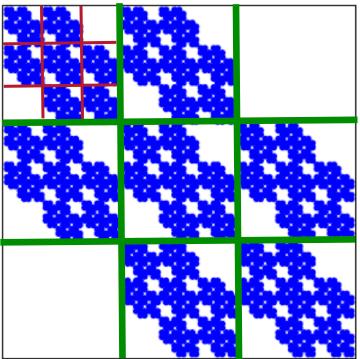


#### **Other topics – part#2 - generators**

- Kronecker [PKDD'05];
- Random Typing [Akoglu+, PKDD'09]

### Kronecker Product – a Graph

• One of most realistic generators, with **provable** properties



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### Other topics - part#3 – virus propagation

• Epidemic threshold for SIS: depends **only** on first eigenvalue of adjacency matrix

 $\lambda_1$ 

- [Chakrabarti+, TISSEC'07]
- Immunization policies [Tong+, under review]
- Drinking water sensor placement [KDD'07]

### More info

#### Tutorial on graph mining: KDD'09 (w/ Gary Miller and C. Tsourakakis) www.cs.cmu.edu/~christos/TALKS/09-KDD-tutorial/

#### Tutorial on tensors: SIGMOD'07 (w/ T. Kolda and J. Sun): www.cs.cmu.edu/~christos/TALKS/SIGMOD-07-tutorial/

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#### Outline

- Introduction Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
- Problem#3: Scalability
- (additional topics, skipped)
- Conclusions

# OVERALL CONCLUSIONS – low level:

- Several new **patterns** (fortification, triangle-laws, conn. components, etc)
- New tools:
  - CenterPiece Subgraphs, G-Ray, anomaly detection (OddBall), EigenSpokes
- Scalability: PEGASUS / hadoop

# OVERALL CONCLUSIONS – high level

- Large datasets may reveal patterns/outliers that would be invisible otherwise
- Terrific opportunities
  - Large datasets, easily(\*) available PLUS
  - s/w and h/w developments
- Promising collaborations between DB/Sys, AI/Stat, sociology, marketing, epidemiology, ++

- Leman Akoglu, Christos Faloutsos: *RTG: A Recursive Realistic Graph Generator Using Random Typing*. ECML/PKDD (1) 2009: 13-28
- Deepayan Chakrabarti, Christos Faloutsos: *Graph mining: Laws, generators, and algorithms*. ACM Comput. Surv. 38(1): (2006)

- Deepayan Chakrabarti, Yang Wang, Chenxi Wang, Jure Leskovec, Christos Faloutsos: *Epidemic thresholds in real networks*. ACM Trans. Inf. Syst. Secur. 10(4): (2008)
- Deepayan Chakrabarti, Jure Leskovec, Christos Faloutsos, Samuel Madden, Carlos Guestrin, Michalis Faloutsos: *Information Survival Threshold in Sensor and P2P Networks*. INFOCOM 2007: 1316-1324

C. Faloutsos (CMU)

 Christos Faloutsos, Tamara G. Kolda, Jimeng Sun: *Mining large graphs and streams using matrix and tensor tools*. Tutorial, SIGMOD Conference 2007: 1174

 T. G. Kolda and J. Sun. Scalable Tensor Decompositions for Multi-aspect Data Mining. In: ICDM 2008, pp. 363-372, December 2008.

- Jure Leskovec, Jon Kleinberg and Christos Faloutsos Graphs over Time: Densification Laws, Shrinking Diameters and Possible Explanations, KDD 2005 (Best Research paper award).
- Jure Leskovec, Deepayan Chakrabarti, Jon M. Kleinberg, Christos Faloutsos: *Realistic, Mathematically Tractable Graph Generation and Evolution, Using Kronecker Multiplication.* PKDD 2005: 133-145

- Jimeng Sun, Yinglian Xie, Hui Zhang, Christos Faloutsos. *Less is More: Compact Matrix Decomposition for Large Sparse Graphs*, SDM, Minneapolis, Minnesota, Apr 2007.
- Jimeng Sun, Spiros Papadimitriou, Philip S. Yu, and Christos Faloutsos, *GraphScope: Parameter -free Mining of Large Time-evolving Graphs* ACM SIGKDD Conference, San Jose, CA, August 2007

 Jimeng Sun, Dacheng Tao, Christos Faloutsos: *Beyond streams and graphs: dynamic tensor analysis*. KDD 2006: 374-383

- Hanghang Tong, Christos Faloutsos, and Jia-Yu Pan, *Fast Random Walk with Restart and Its Applications*, ICDM 2006, Hong Kong.
- Hanghang Tong, Christos Faloutsos, *Center-Piece Subgraphs: Problem Definition and Fast Solutions*, KDD 2006, Philadelphia, PA

 Hanghang Tong, Christos Faloutsos, Brian Gallagher, Tina Eliassi-Rad: Fast best
 effort pattern matching in large attributed graphs. KDD 2007: 737-746

# Joint papers with LLNL

- Keith Henderson, Tina Eliassi-Rad, Spiros Papadimitriou, Christos Faloutsos: HCDF: A Hybrid Community Discovery Framework. SDM 2010:754-765
- Hanghang Tong, Yasushi Sakurai, Tina Eliassi-Rad, Christos Faloutsos: Fast mining of complex time-stamped events. CIKM 2008:759-768
- Jimeng Sun, Charalampos E. Tsourakakis, Evan Hoke, Christos Faloutsos, Tina Eliassi-Rad: Two heads better than one: pattern discovery in time-evolving multi-aspect data. Data Min. Knowl. Discov. (DATAMINE) 17(1) :111-128 (2008)

## Joint papers with LLNL

- Jimeng Sun, Charalampos E. Tsourakakis, Evan Hoke, Christos Faloutsos, Tina Eliassi-Rad: Two Heads Better Than One: Pattern Discovery in Time-Evolving Multi-aspect Data. ECML /PKDD 2008:22
- Duen Horng Chau, Christos Faloutsos, Hanghang Tong, Jason I. Hong, Brian Gallagher, Tina Eliassi-Rad: GRAPHITE: A Visual Query System for Large Graphs. ICDM Workshops 2008:963-966

## Joint papers with LLNL

- Brian Gallagher, Hanghang Tong, Tina Eliassi
   Rad, Christos Faloutsos: Using ghost edges for classification in sparsely labeled networks. KDD 2008:256-264
- Hanghang Tong, Christos Faloutsos, Brian Gallagher, Tina Eliassi-Rad: Fast best-effort pattern matching in large attributed graphs. KDD 2007:737-746

# **Project info** www.cs.cmu.edu/~pegasus



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Tong, Hanghang

Thanks to: LLNL (DE-AC52-07NA27344, +) NSF, CTA-INARC; Yahoo (M45), IBM, SPRINT, INTEL, HP

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