

Mining Billion-Node Graphs: Patterns and influence propagation

Christos Faloutsos

CMU

Thank you!

- Sinan Aral
- Foster Provost
- Arun Sundararajan

- Shirley Lau

Our goal:

Open source system for mining huge graphs:

PEGASUS project (PEta GrAph mining System)

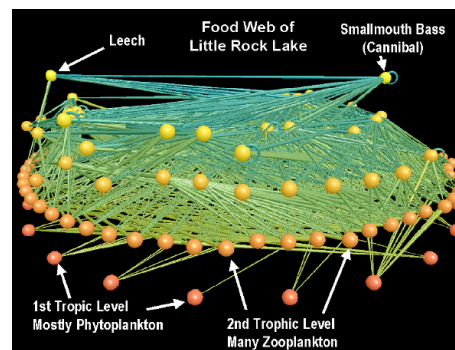
- www.cs.cmu.edu/~pegasus
- code and papers



Outline

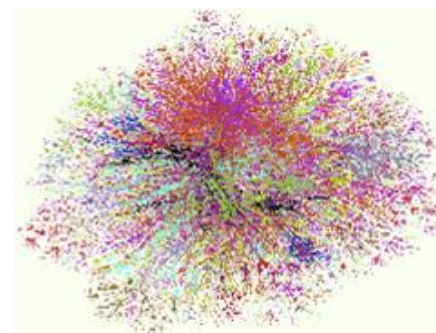
- ➔ • Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
- Conclusions

Graphs - why should we care?



Food Web
[Martinez '91]

Recommendation
systems

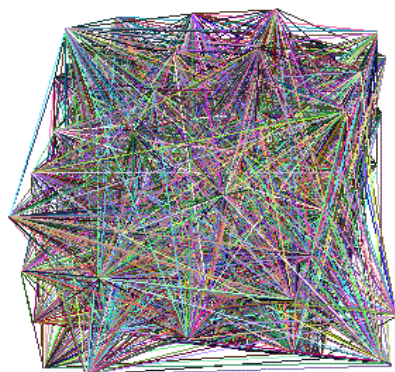


Internet Map
[lumeta.com]

Outline

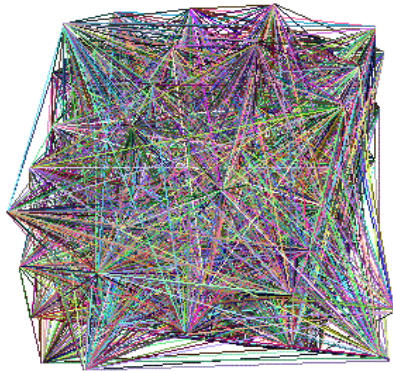
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 - Triangles
 - Diameter
 - ‘Eigenspokes’
 - Phonenumber duration
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Problem #1 - network and graph mining



- What does the Internet look like?
- What does FaceBook look like?
- What is ‘normal’/‘abnormal’?
- which patterns/laws hold?

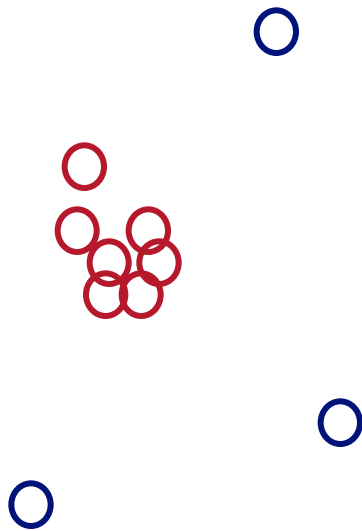
Problem #1 - network and graph mining



- What does the Internet look like?
- What does FaceBook look like?
- What is ‘normal’/‘abnormal’?
- which patterns/laws hold?
 - BIG DATA helps: finds patterns that would be ‘invisible’

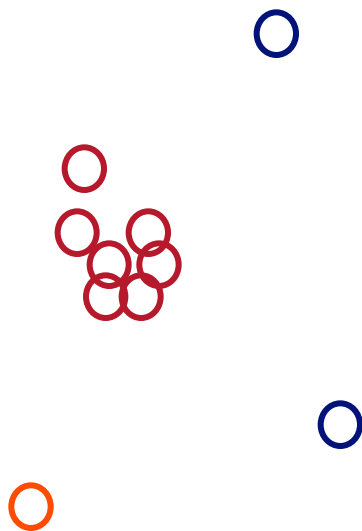
Typical viewpoint

- ‘Signal’ and
- noise

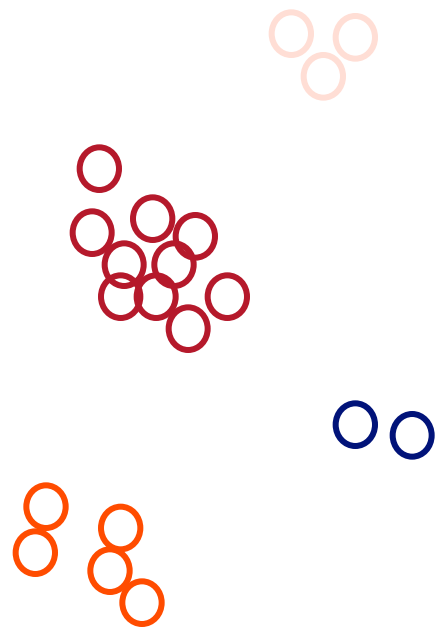


MORE REALISTIC viewpoint

- ‘Signal’ and
- Weaker signal



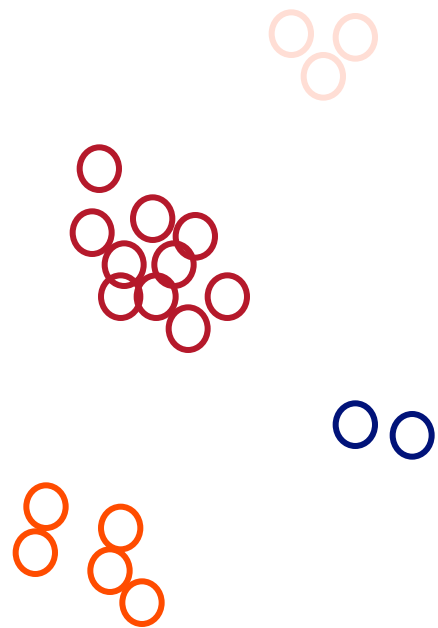
MORE REALISTIC viewpoint



- ‘Signal’ and
- Weaker signal and
- Even weaker signal
- ...

BIG DATA helps

MORE REALISTIC viewpoint



- ‘Signal’ and
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**BIG DATA helps
(and sampling may
hurt)**

Graph mining

- Are real graphs random?

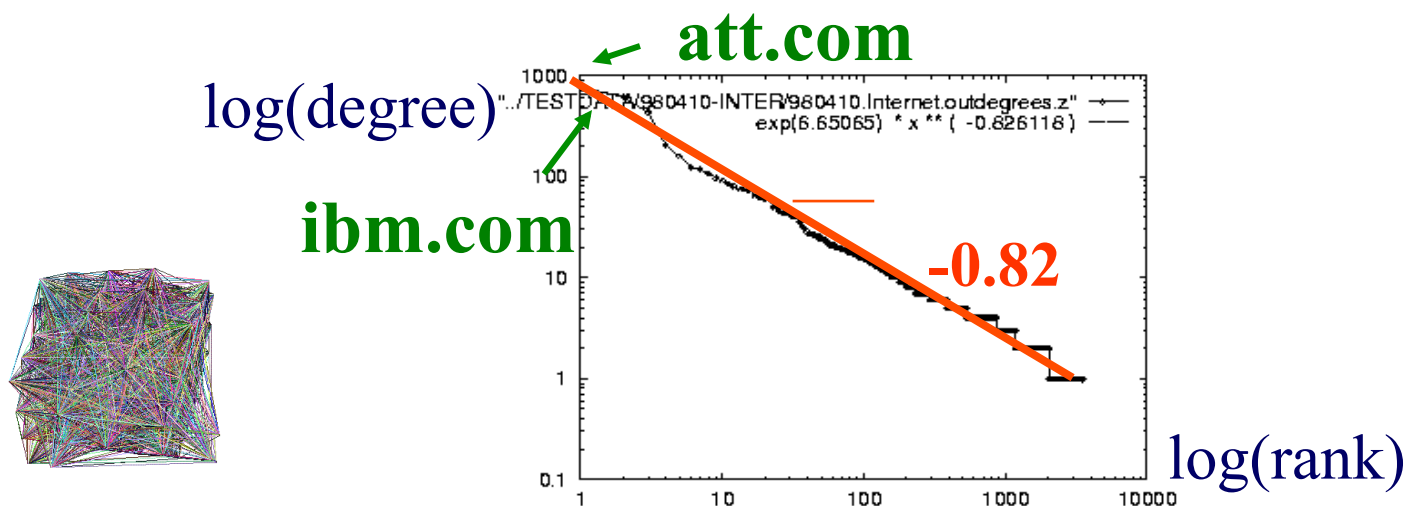
Laws and patterns

- Are real graphs random?
- A: NO!!
 - Diameter (small, and decreasing!)
 - in- and out- degree distributions (skewed/PL)
 - # triangles (skewed)
 - other (surprising) patterns
- So, let's look at the data

Solution# S.1

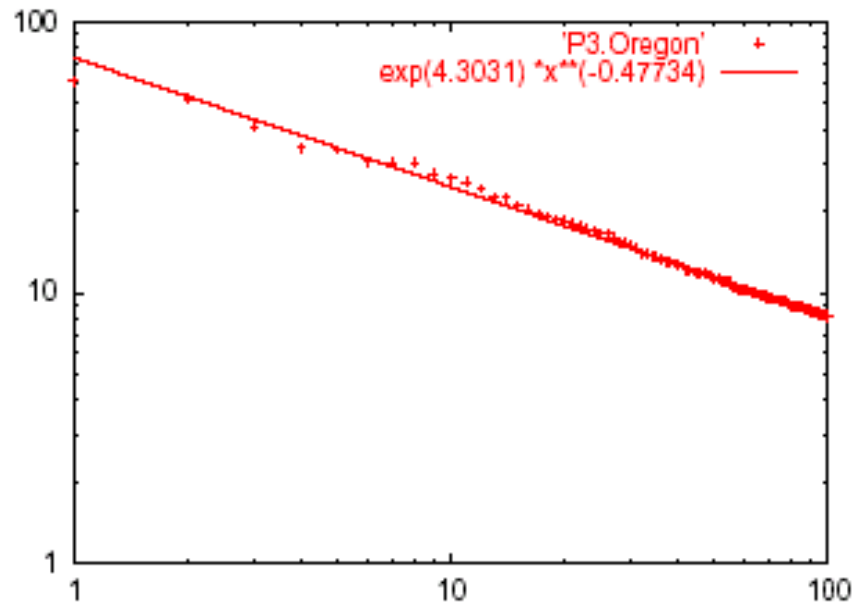
- Power law in the degree distribution [SIGCOMM99]

internet domains



Solution# S.2: Eigen Exponent E

Eigenvalue



Exponent = slope

$$E = -0.48$$

May 2001

Rank of decreasing eigenvalue

- A2: power law in the eigenvalues of the adjacency matrix



Real Graph Patterns

	unweighted	weighted
static	<p>P01. Power-law degree distribution [Faloutsos et. al. '99, Kleinberg et. al. '99, Chakrabarti et. al. '04, Newman '04]</p> <p>P02. Triangle Power Law [Tsourakakis '08]</p> <p>P03. Eigenvalue Power Law [Siganos et. al. '03]</p> <p>P04. Community structure [Flake et. al. '02, Girvan and Newman '02]</p> <p>P05. Clique Power Laws [Du et. al. '09]</p>	<p>P12. Snapshot Power Law [McGlohon et. al. '08]</p>
dynamic	<p>P06. Densification Power Law [Leskovec et. al. '05]</p> <p>P07. Small and shrinking diameter [Albert and Barabási '99, Leskovec et. al. '05, McGlohon et. al. '08]</p> <p>P08. Gelling point [McGlohon et. al. '08]</p> <p>P09. Constant size 2nd and 3rd connected components [McGlohon et. al. '08]</p> <p>P10. Principal Eigenvalue Power Law [Akoglu et. al. '08]</p> <p>P11. Bursty/self-similar edge/weight additions [Gomez and Santonja '98, Gribble et. al. '98, Crovella and Bestavros '99, McGlohon et. al. '08]</p>	<p>P13. Weight Power Law [McGlohon et. al. '08]</p> <p>P14. Skewed call duration distributions [Vaz de Melo et. al. '10]</p>

[RTG: A Recursive Realistic Graph Generator using Random Typing](#)

Leman Akoglu and Christos Faloutsos. *ECML PKDD'09*.



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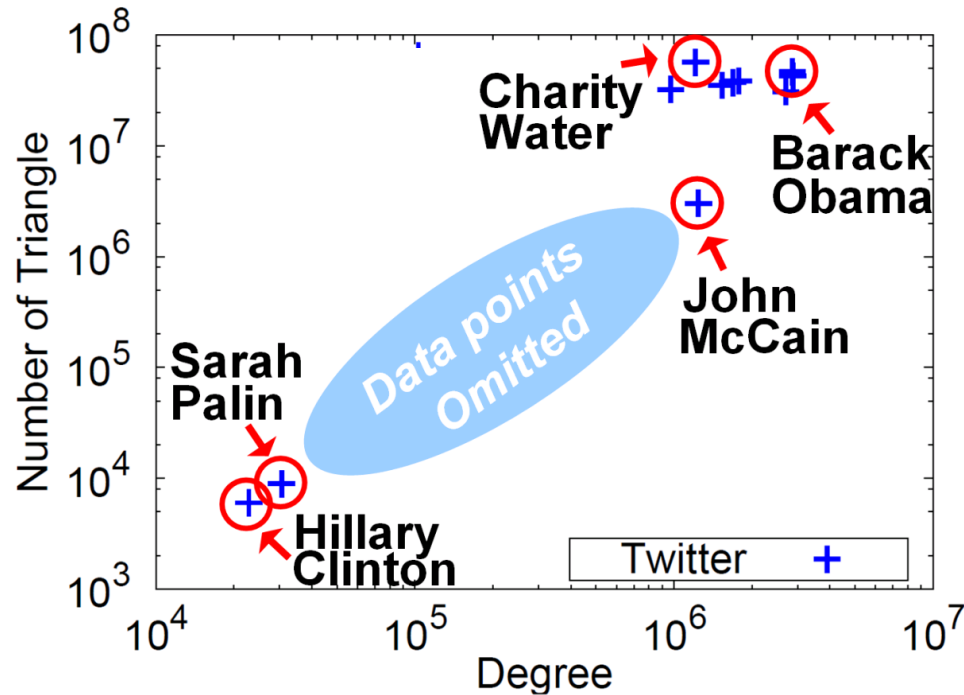
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Triangle counting for large graphs?

Anomalous nodes in Twitter (~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]

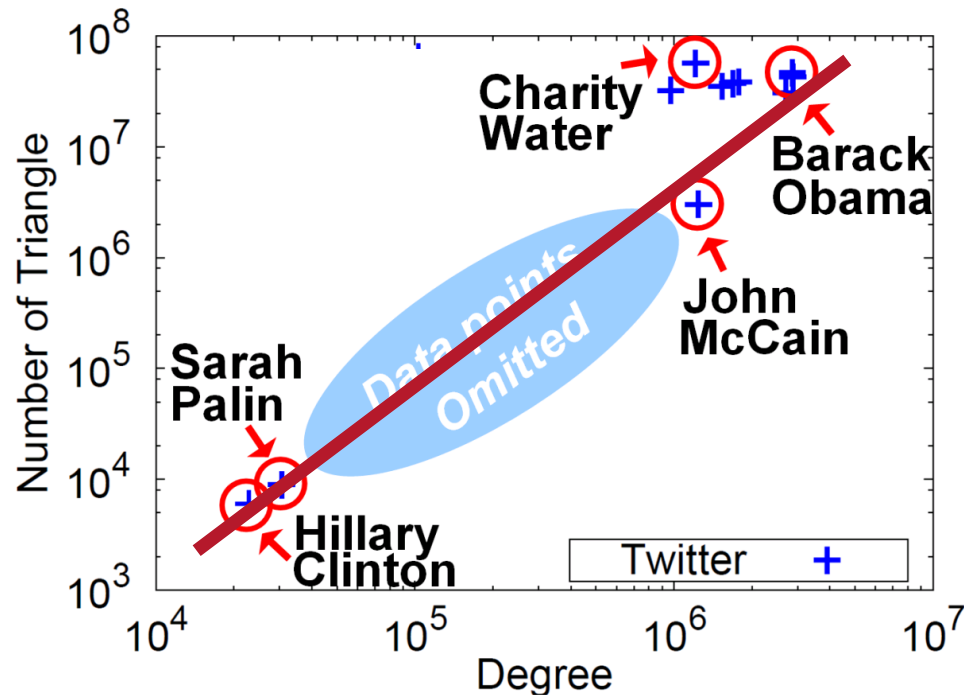
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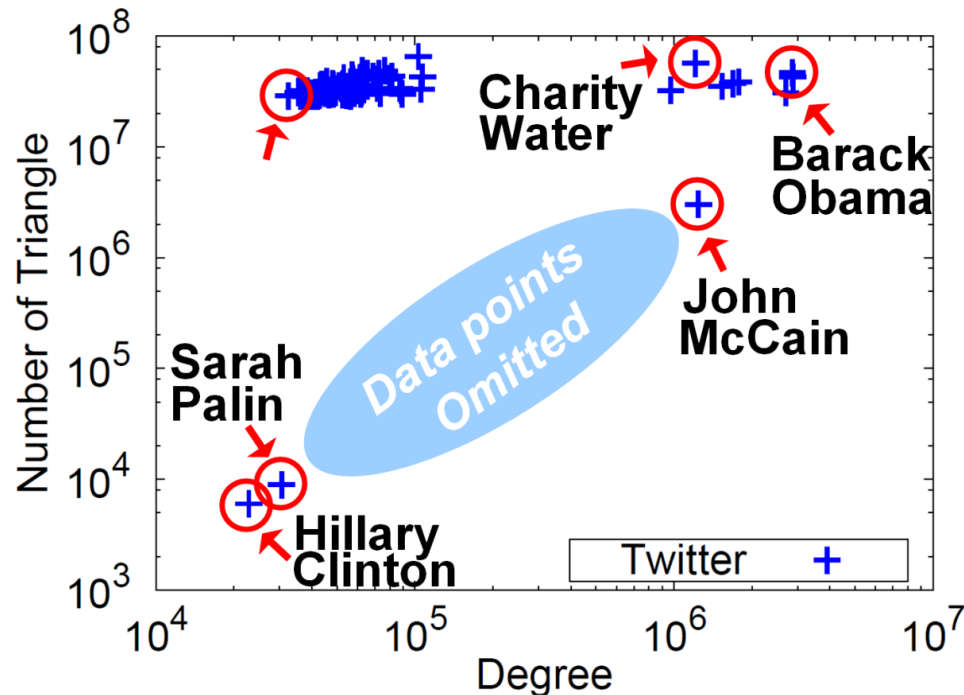
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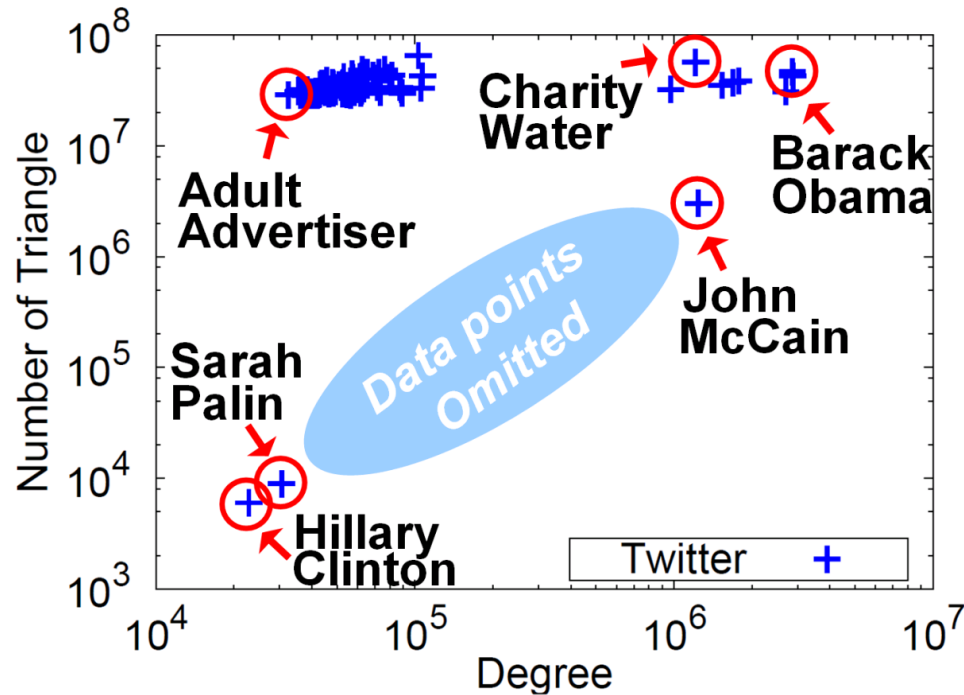
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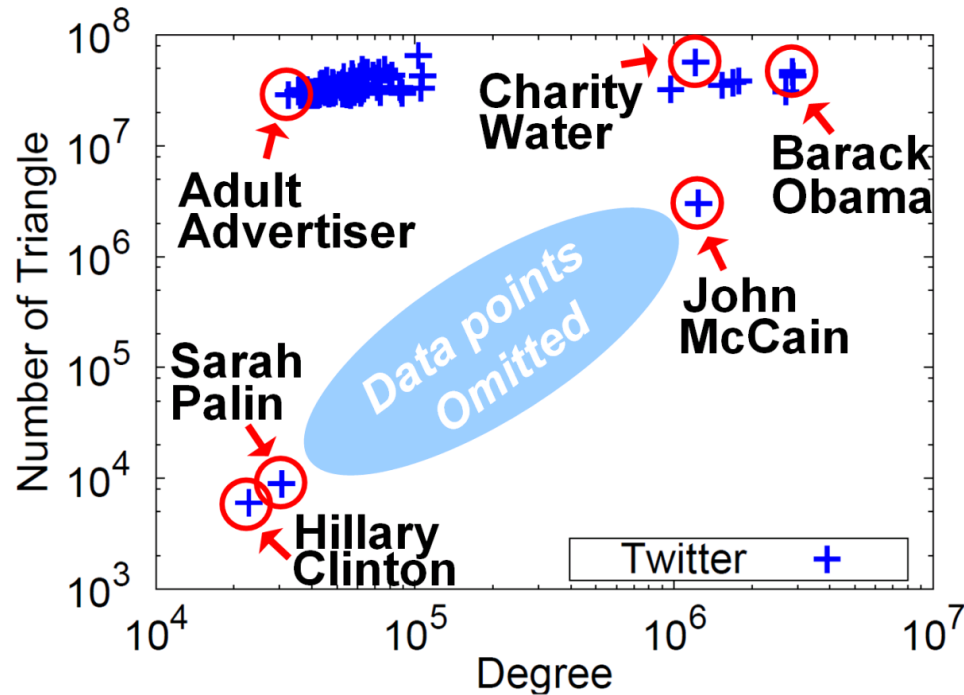
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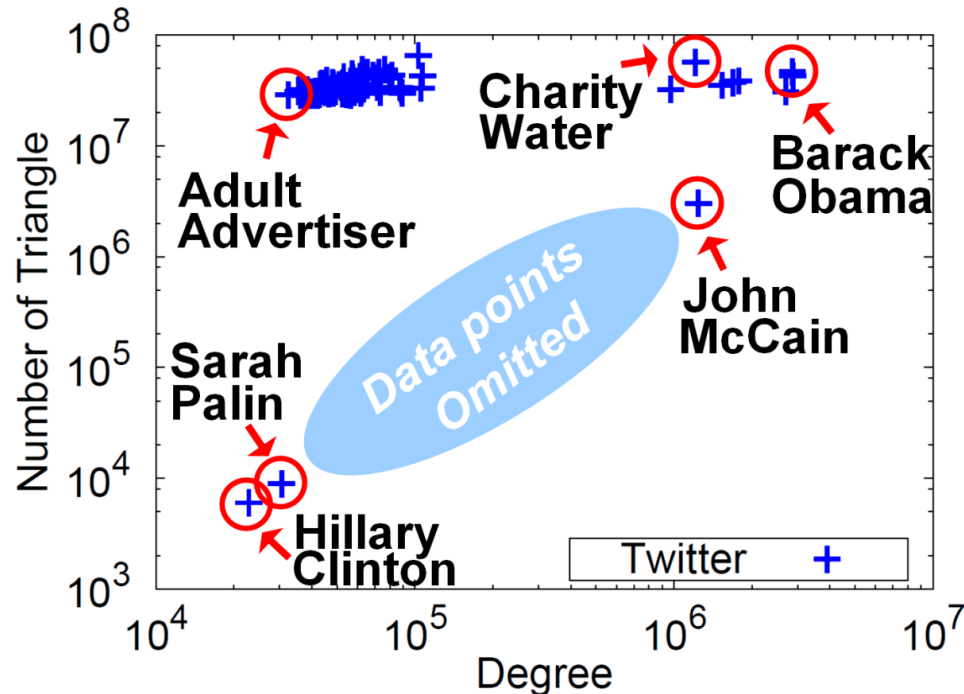
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Triangle counting for large graphs?



Q: How to compute # triangles in B-node graph? ($O(d_{\max}^{** 2})$)?

Triangle counting for large graphs?



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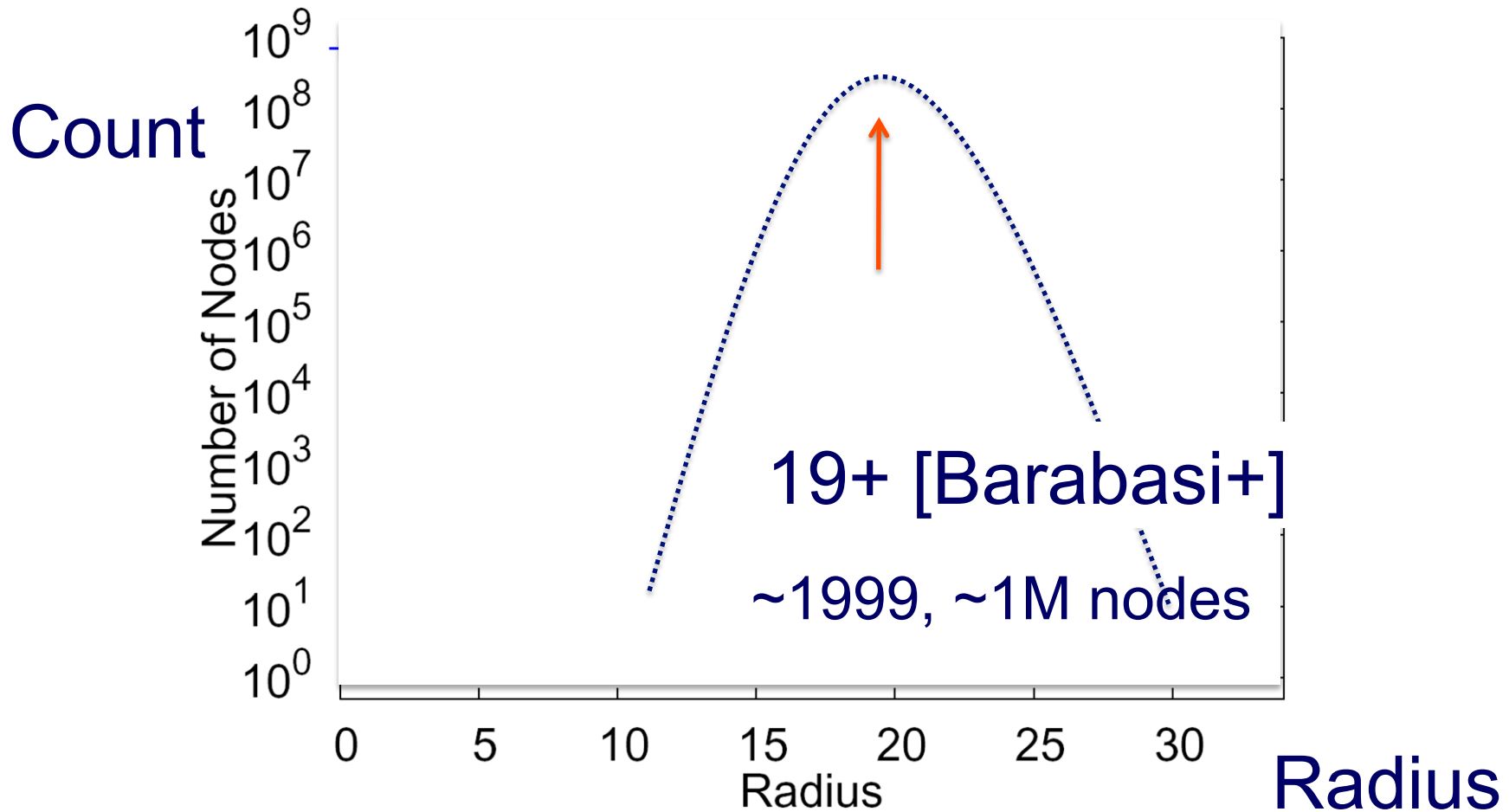
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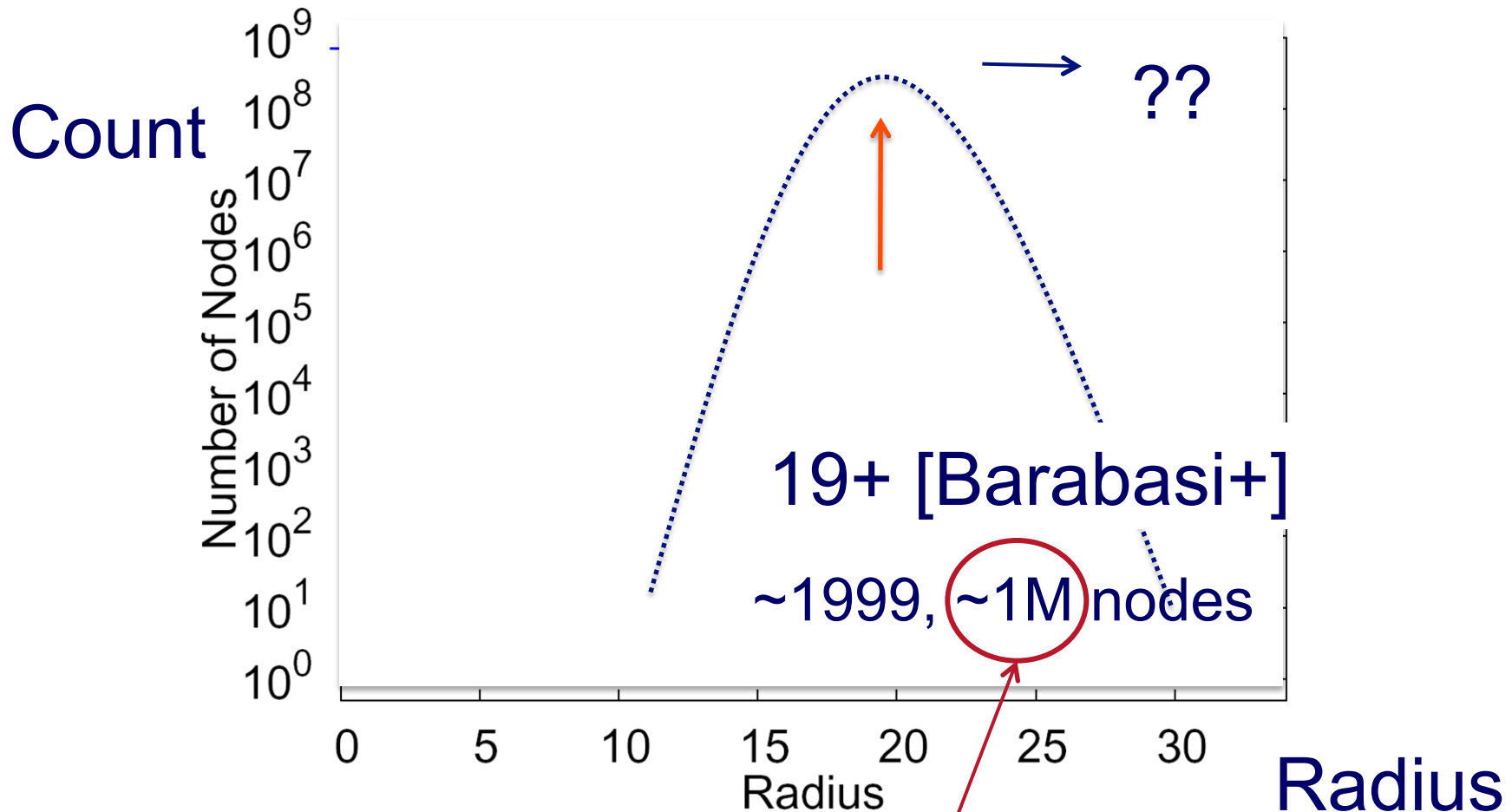


HADI for diameter estimation

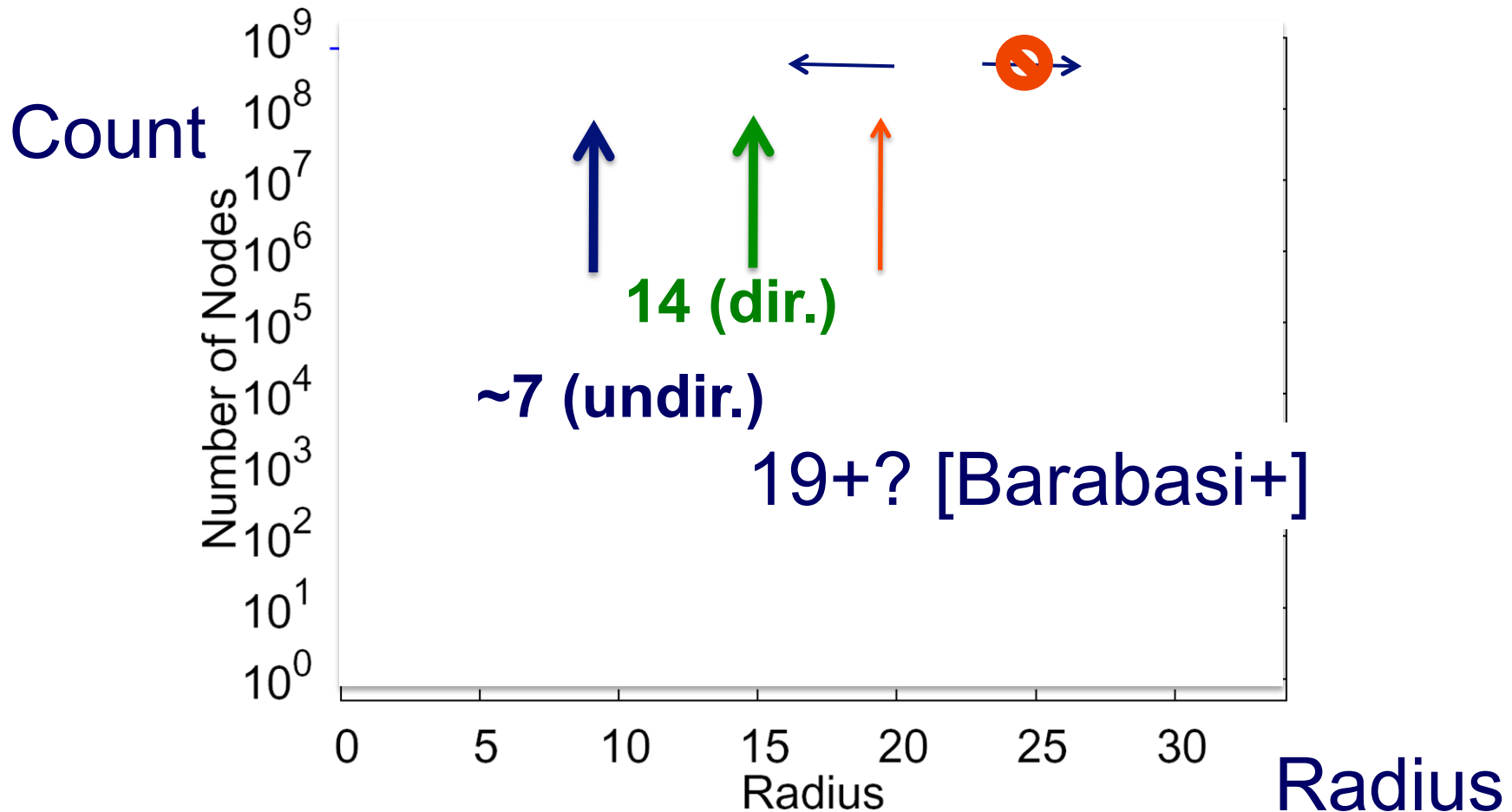
- *Radius Plots for Mining Tera-byte Scale Graphs* **U Kang**, Charalampos Tsourakakis, Ana Paula Appel, Christos Faloutsos, Jure Leskovec, SDM'10
- Naively: diameter needs $O(N^2)$ space and up to $O(N^3)$ time – **prohibitive** ($N \sim 1B$)
- Our HADI: linear on E ($\sim 10B$)
 - Near-linear scalability wrt # machines
 - Several optimizations \rightarrow 5x faster



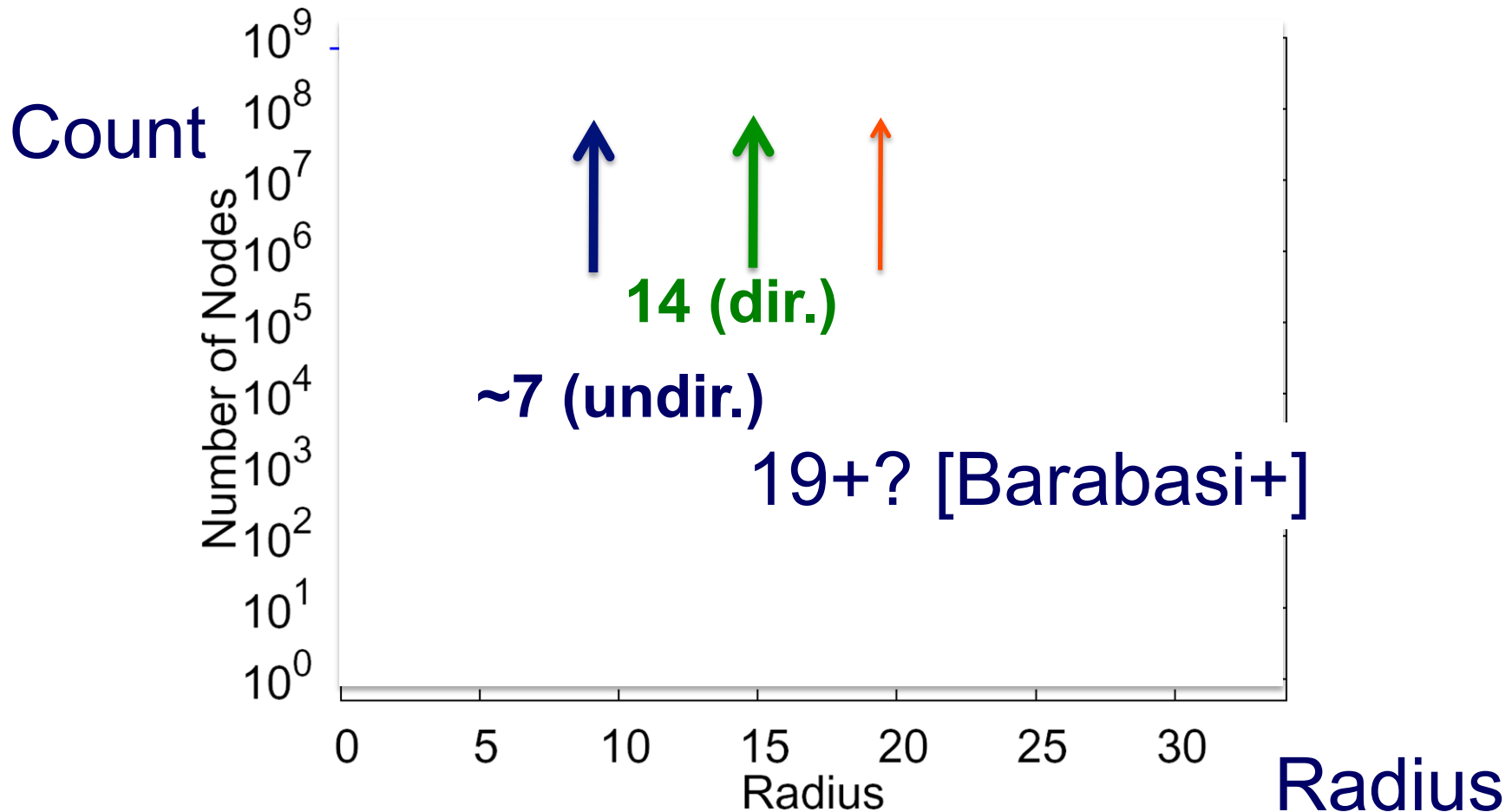




- YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)
- Largest publicly available graph ever studied.

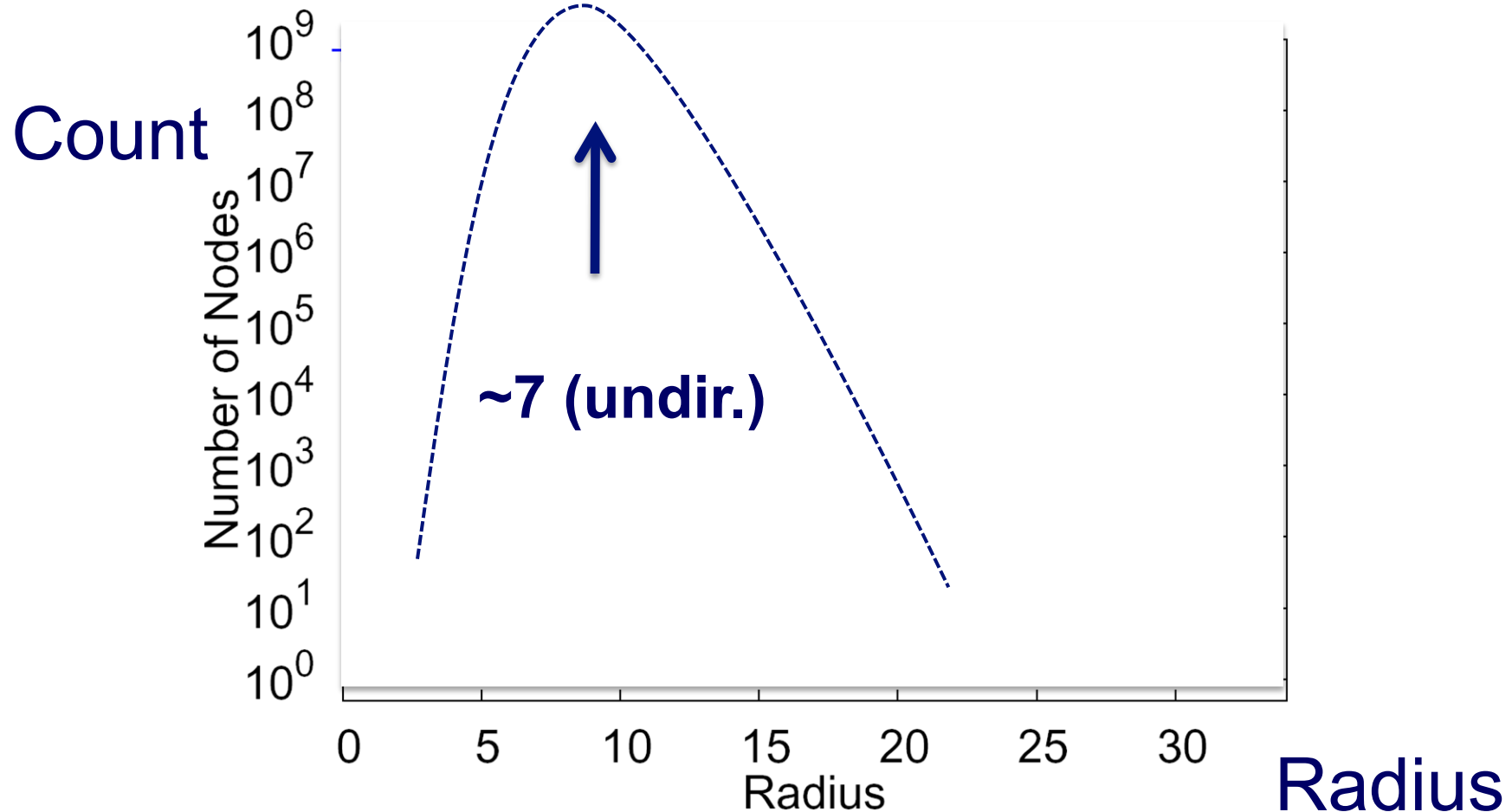


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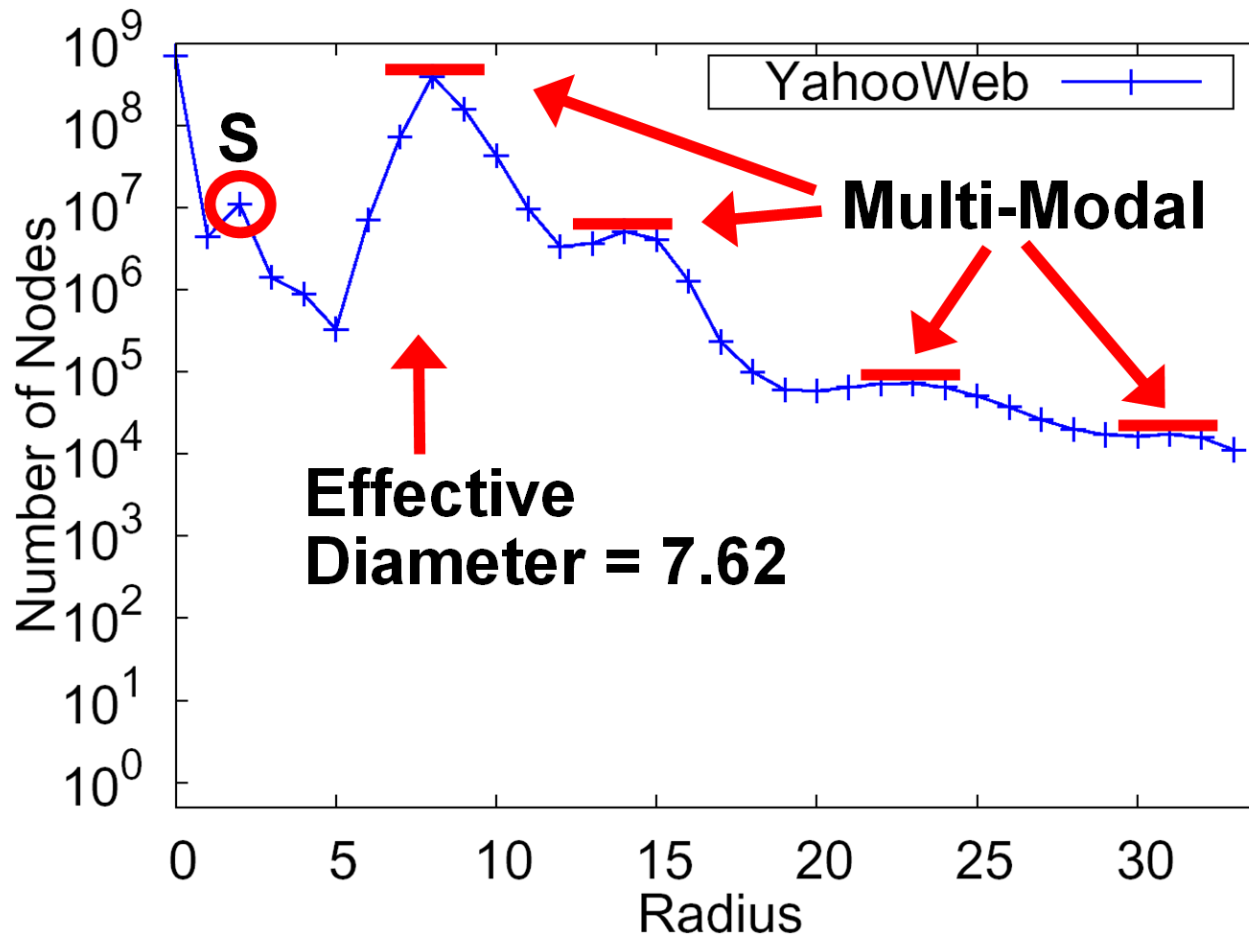


YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

- 7 degrees of separation (!)
- Diameter: shrunk

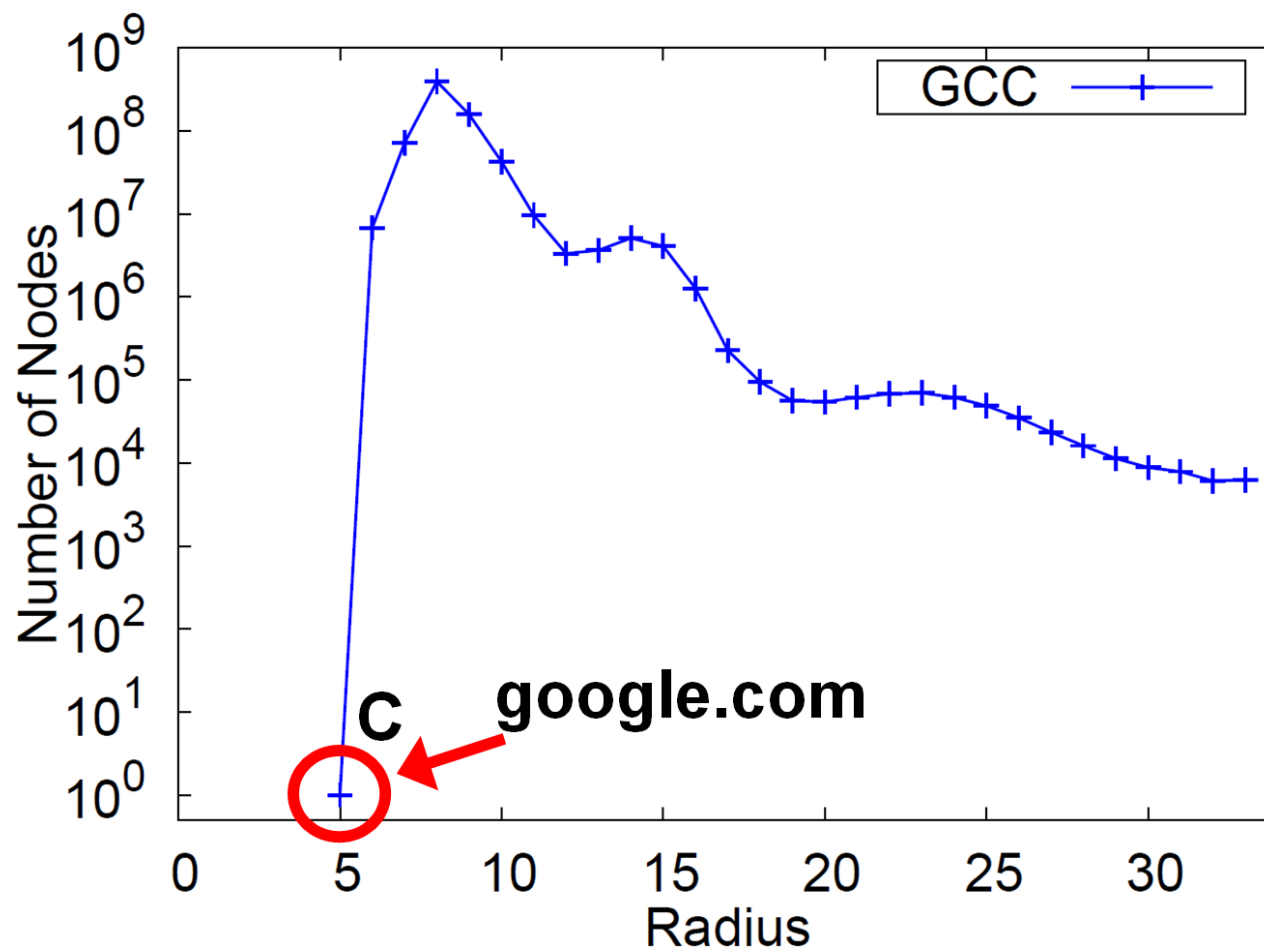


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Q: Shape?

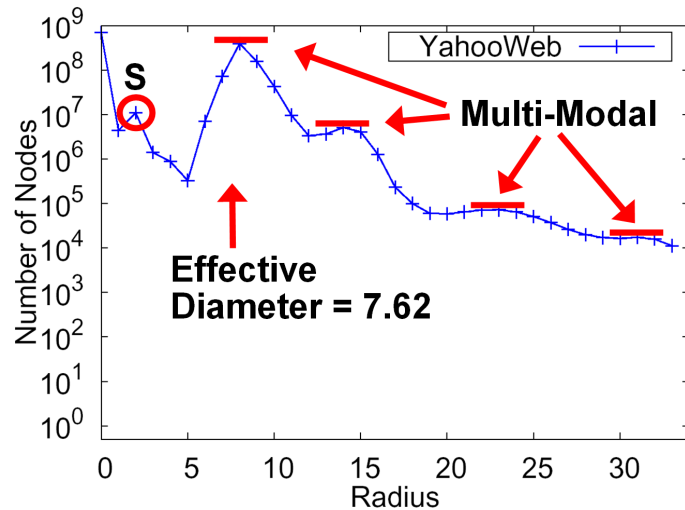


YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

- effective diameter: surprisingly small.
- Multi-modality (?!)

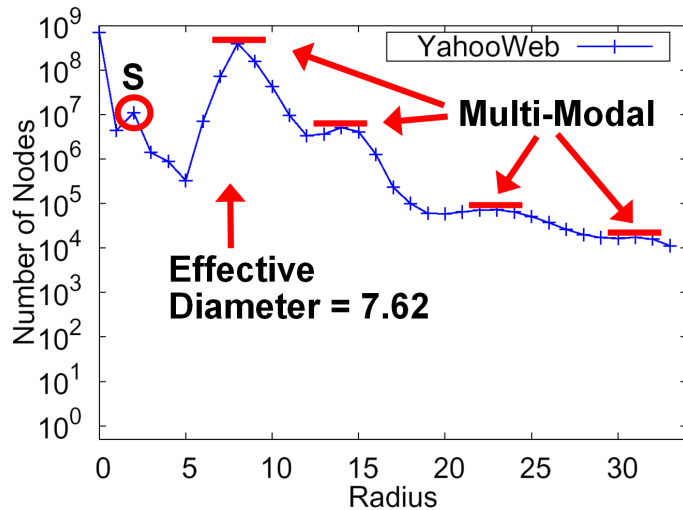


Radius Plot of **GCC** of YahooWeb.

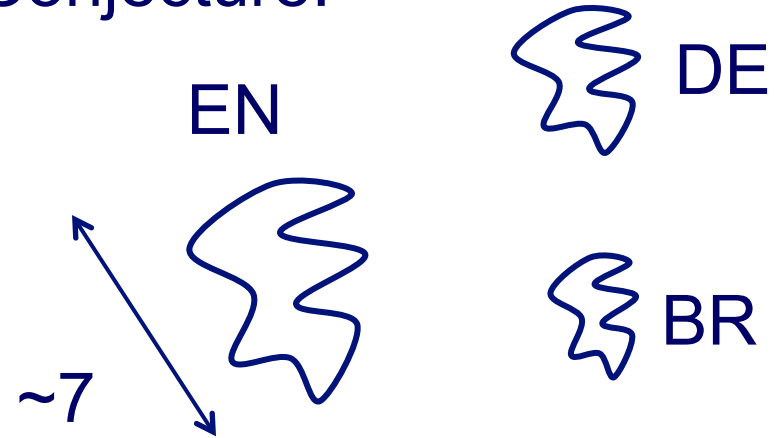


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- effective diameter: surprisingly small.
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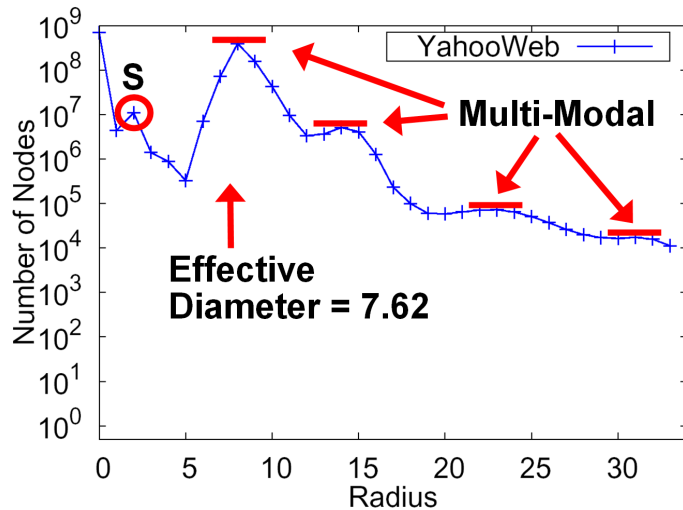


Conjecture:

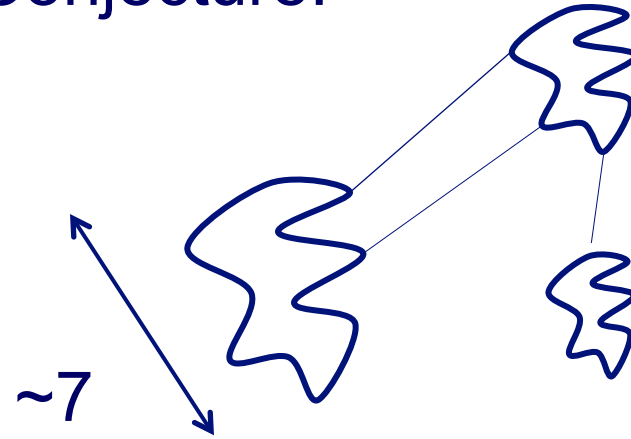


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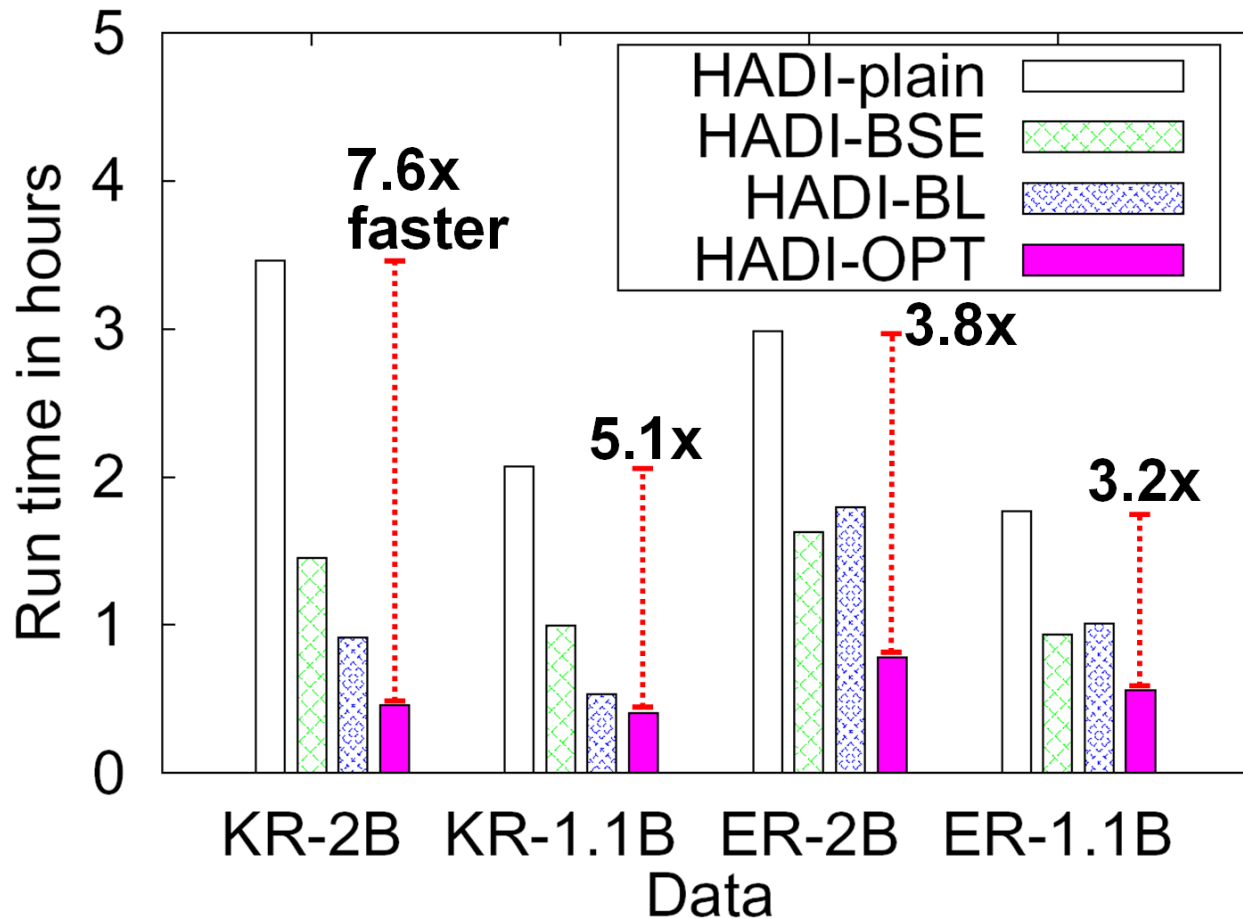
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Conjecture:



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Running time - Kronecker and Erdos-Renyi
Graphs with billions edges.

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EigenSpokes

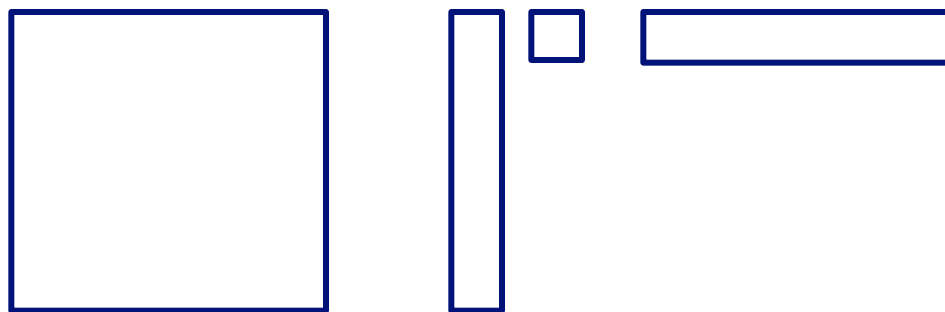


B. Aditya Prakash, Mukund Seshadri, Ashwin Sridharan, Sridhar Machiraju and Christos Faloutsos: *EigenSpokes: Surprising Patterns and Scalable Community Chipping in Large Graphs*, PAKDD 2010, Hyderabad, India, 21-24 June 2010.

EigenSpokes

- Eigenvectors of adjacency matrix
 - equivalent to singular vectors (symmetric, undirected graph)

$$A = U\Sigma U^T$$



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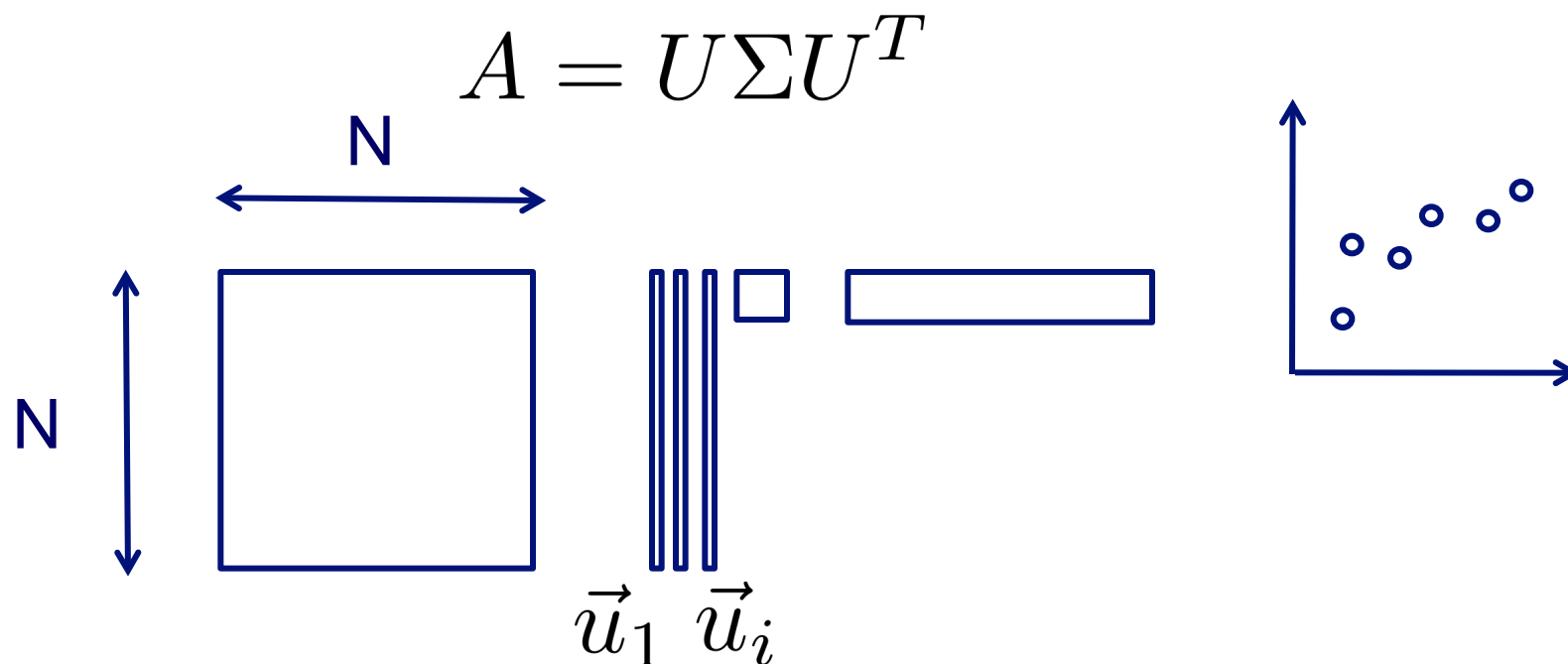
N

N

\vec{u}_1 \vec{u}_i

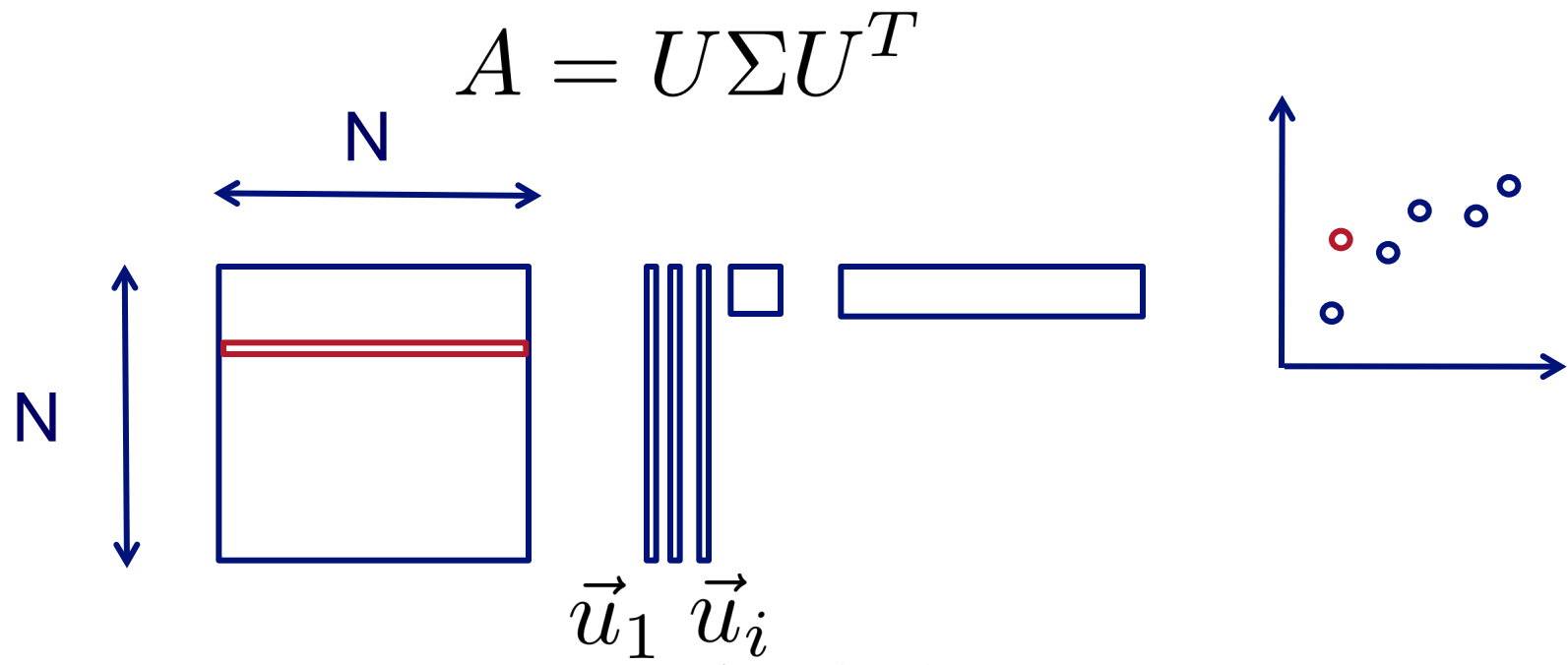
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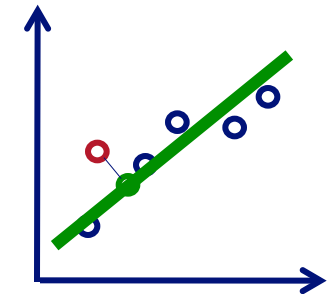
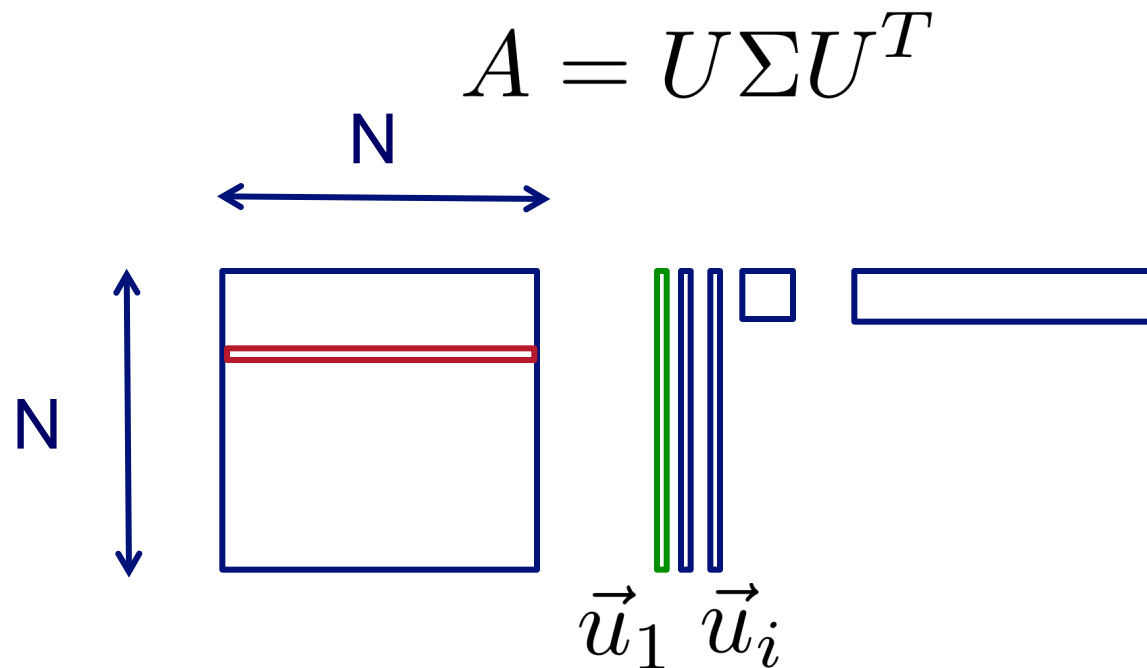
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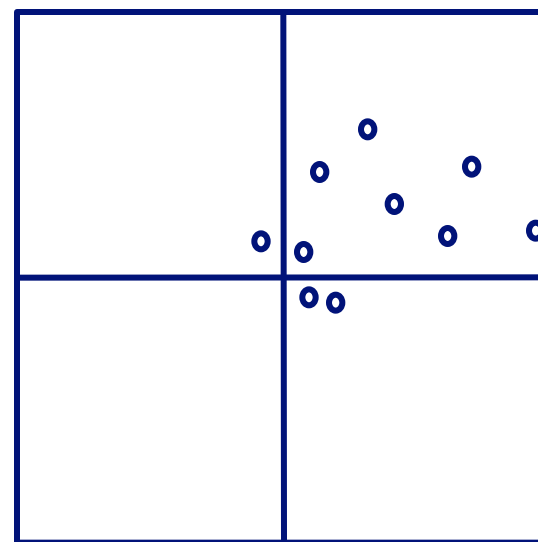
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EigenSpokes

- EE plot:
- Scatter plot of scores of u_1 vs u_2
- One would expect
 - Many points @ origin
 - A few scattered ~randomly

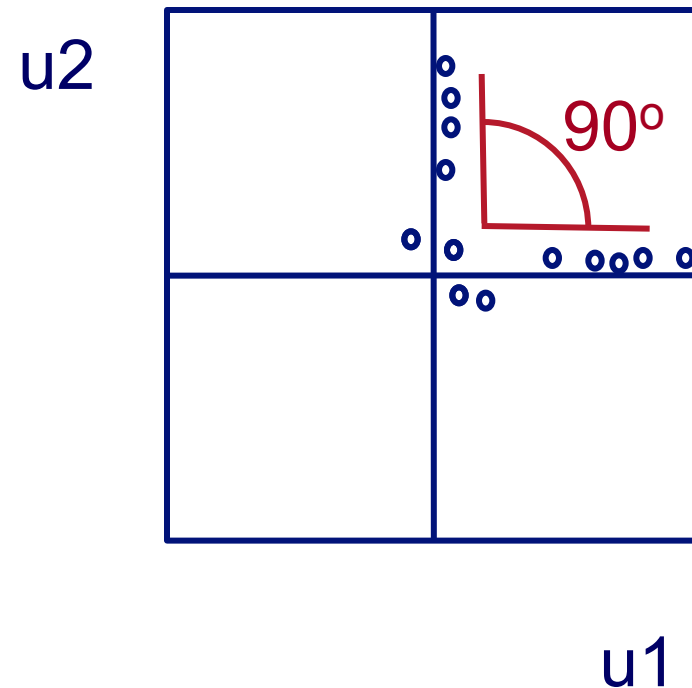
2nd Principal component
 u_2



u_1
1st Principal component

EigenSpokes

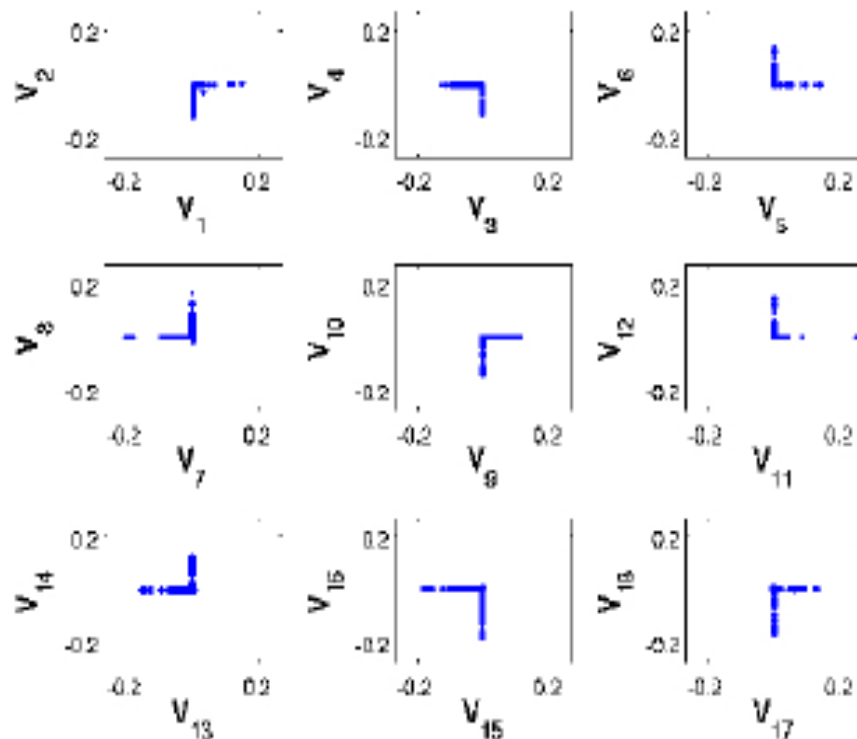
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EigenSpokes - pervasiveness

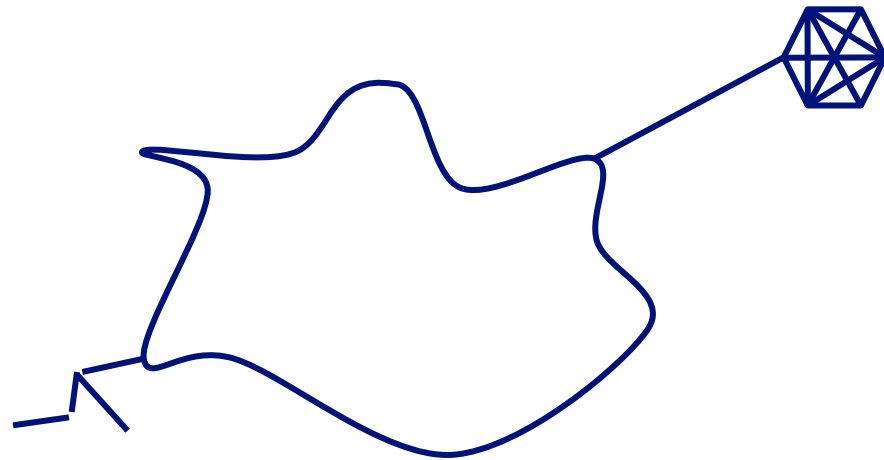
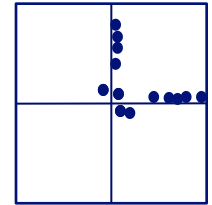
- Present in mobile social graph
 - across time and space

- Patent citation graph



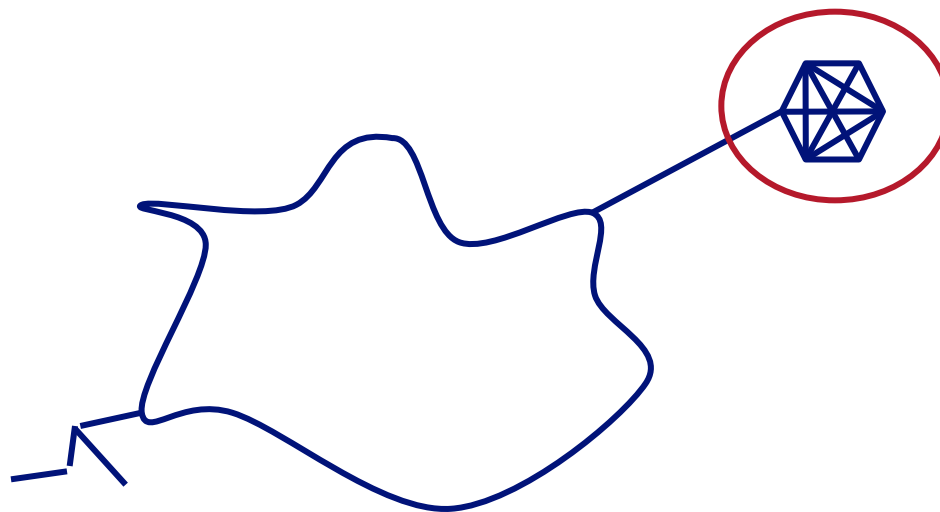
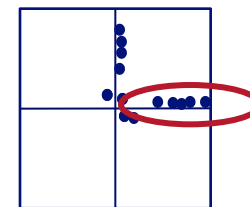
EigenSpokes - explanation

Near-cliques, or near-bipartite-cores, loosely connected



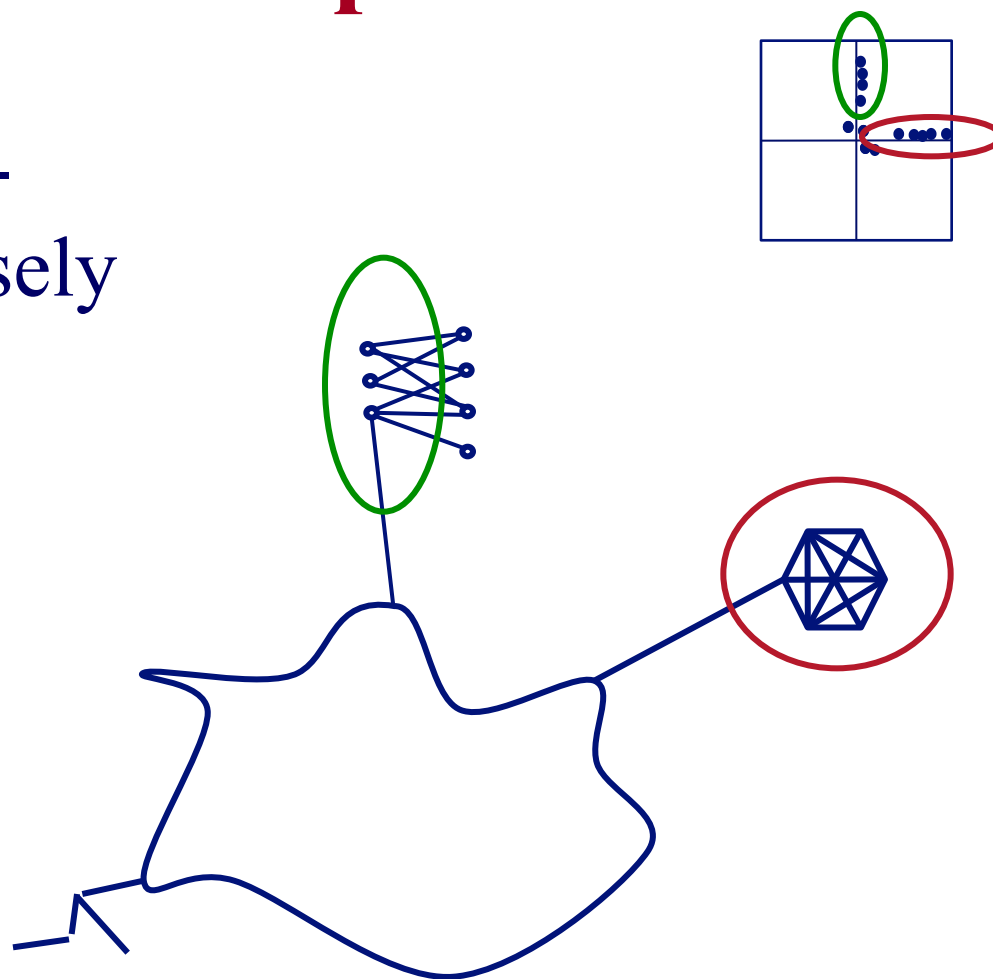
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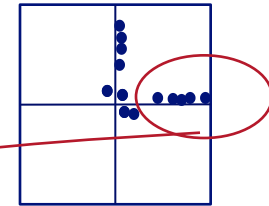
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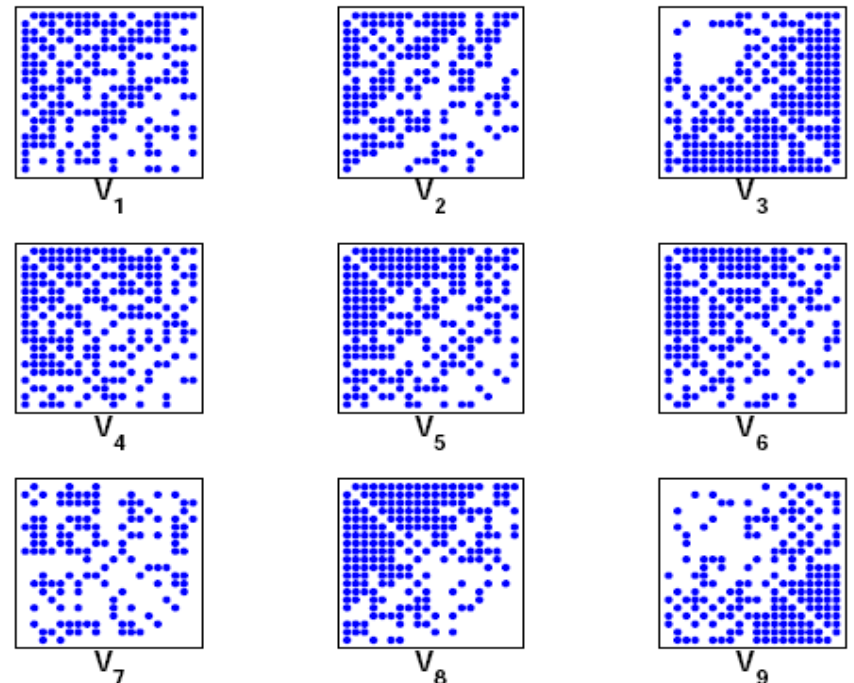


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spy plot of top 20 nodes



So what?

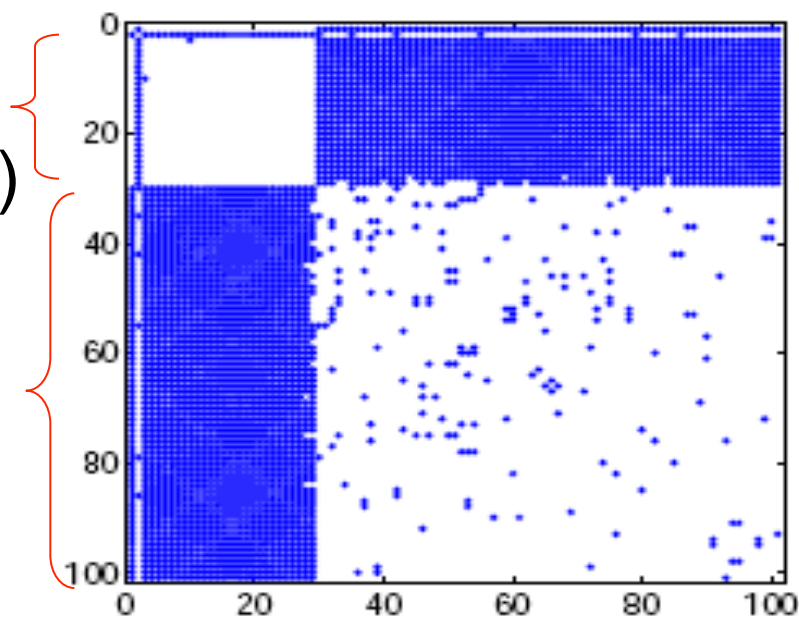
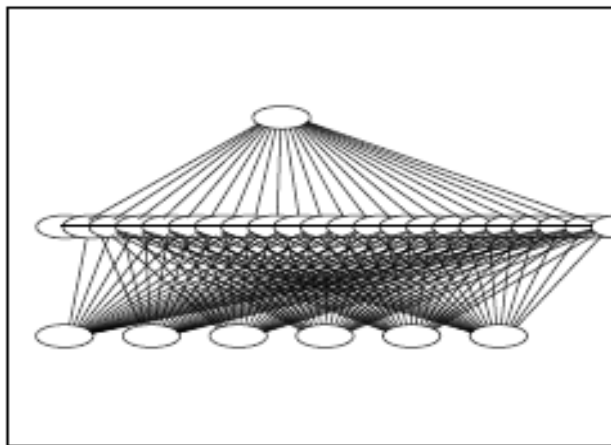
- Extract nodes with high *scores*
- high connectivity
- Good “communities”

Bipartite Communities!

patents from
same inventor(s)

`cut-and-paste'
bibliography!

magnified bipartite community



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Duration of phonecalls

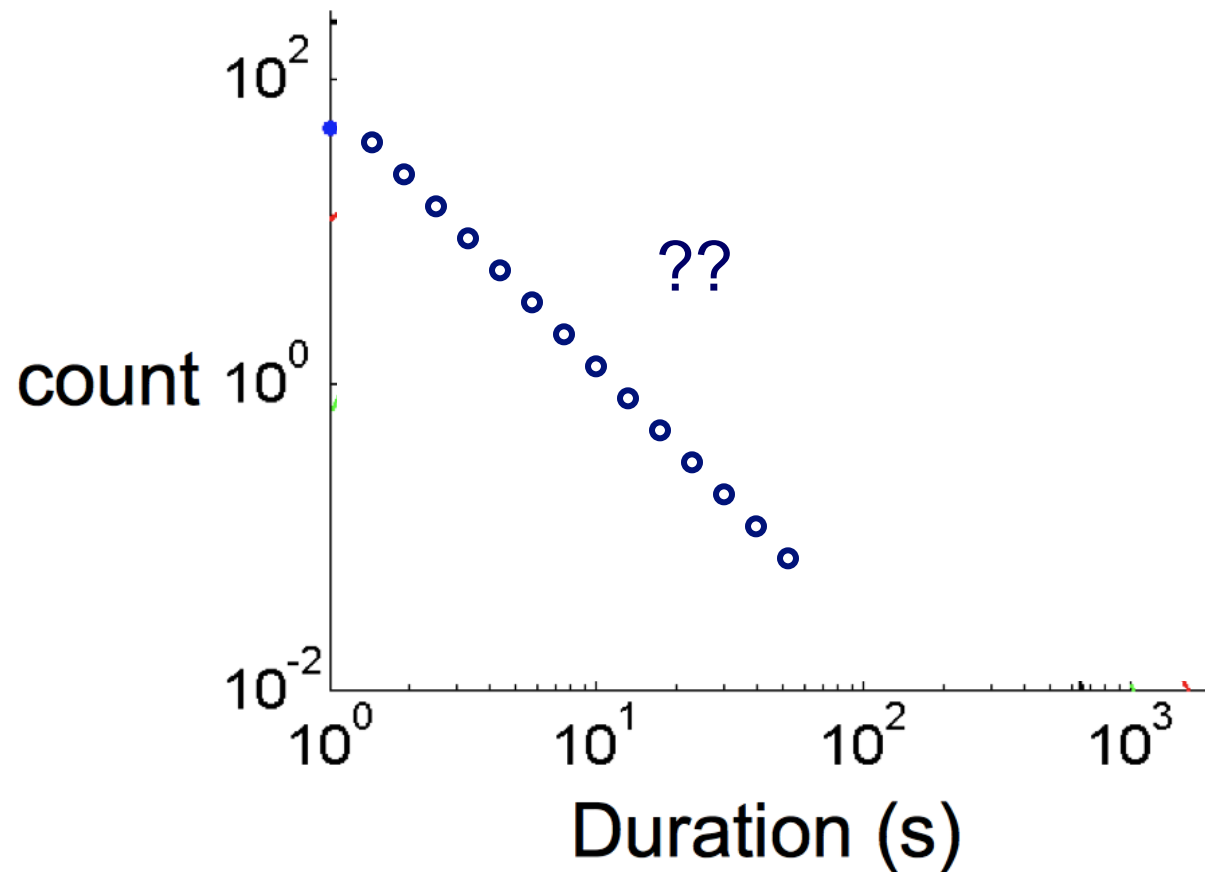
*Surprising Patterns for the Call
Duration Distribution of Mobile
Phone Users*



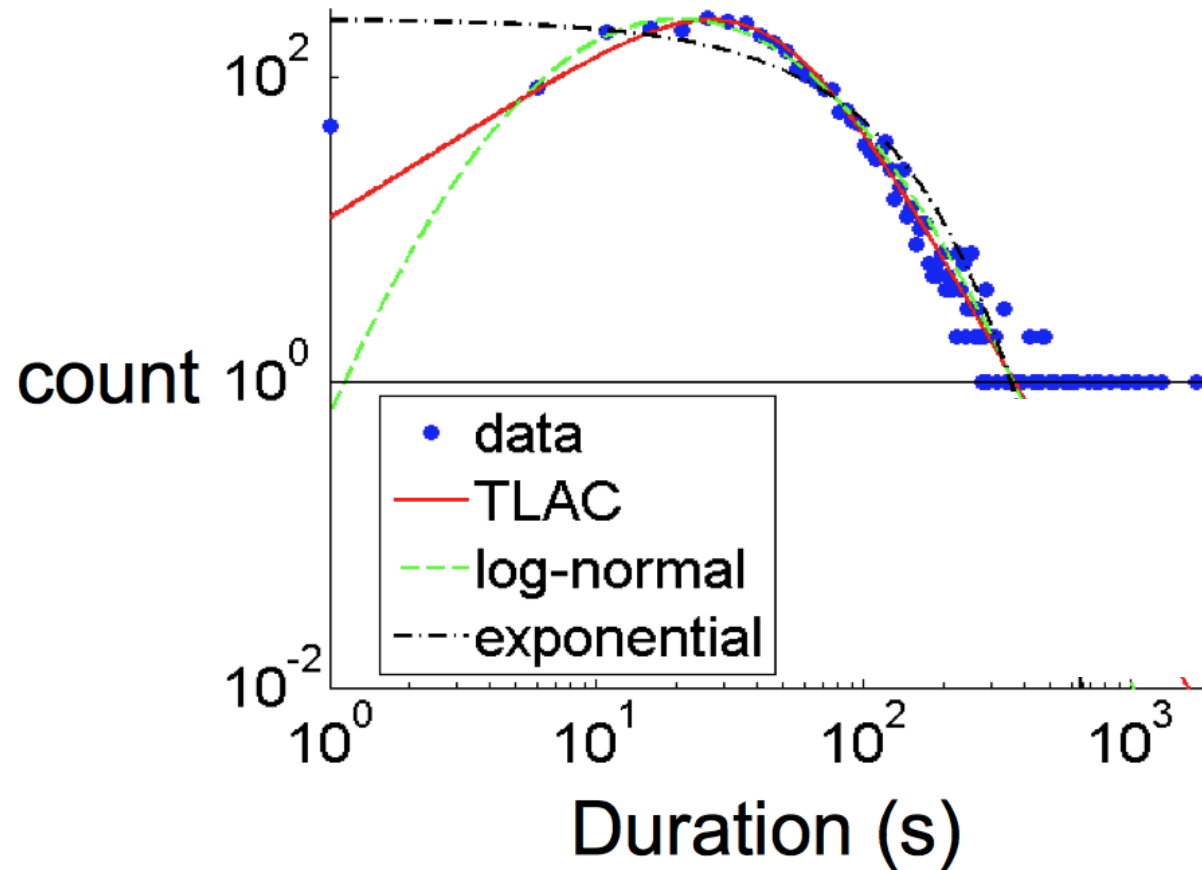
Pedro O. S. Vaz de Melo, Leman
Akoglu, Christos Faloutsos, Antonio
A. F. Loureiro

PKDD 2010

Probably, power law (?)

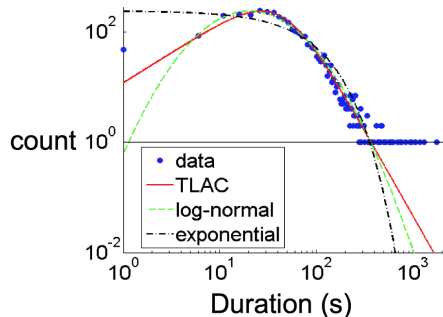


No Power Law!?



'TLaC: Lazy Contractor'

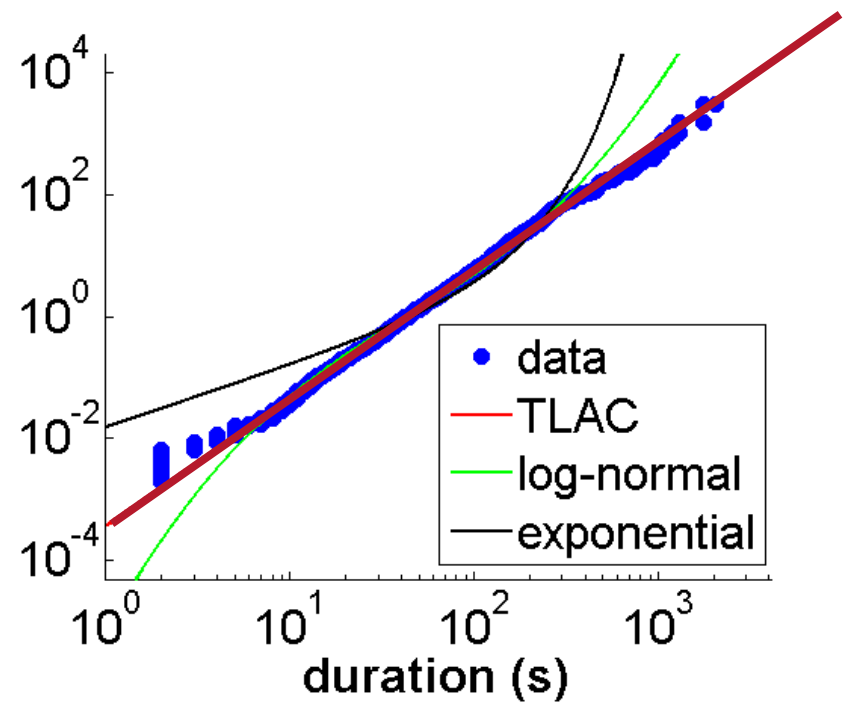
- The longer a task (phonecall) has taken,
- The even longer it will take



Odds ratio=

Casualties($<x$):
Survivors($\geq x$)

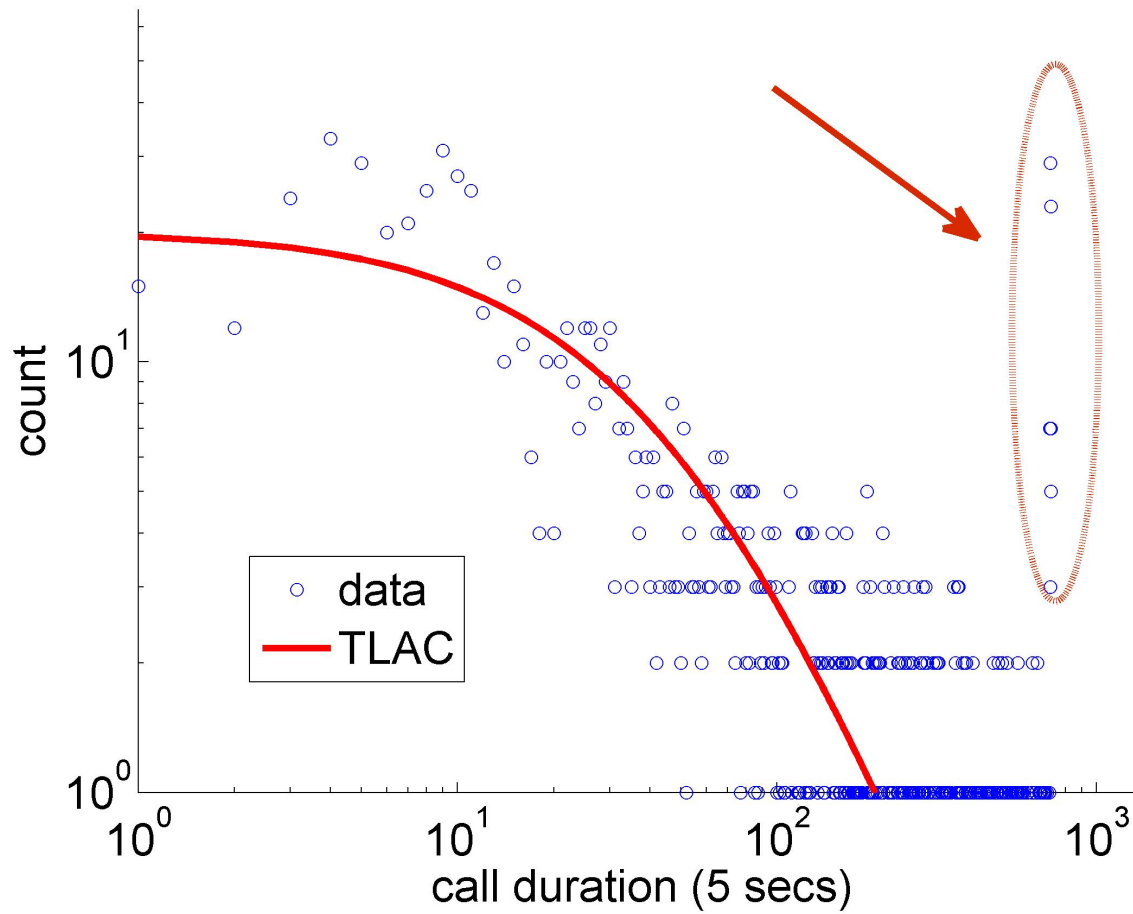
== power law



Data Description

- Data from a private mobile operator of a large city
 - 4 months of data
 - 3.1 million users
 - more than 1 billion phone records
- Over 96% of ‘talkative’ users obeyed a TLAC distribution (‘talkative’: >30 calls)

Outliers:



Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
 - ...
 - ‘Eigenspokes’
 - Phonecall duration
 - ➔ – Connected components
- Problem#2: Tools
- Conclusions

Generalized Iterated Matrix Vector Multiplication (GIMV)

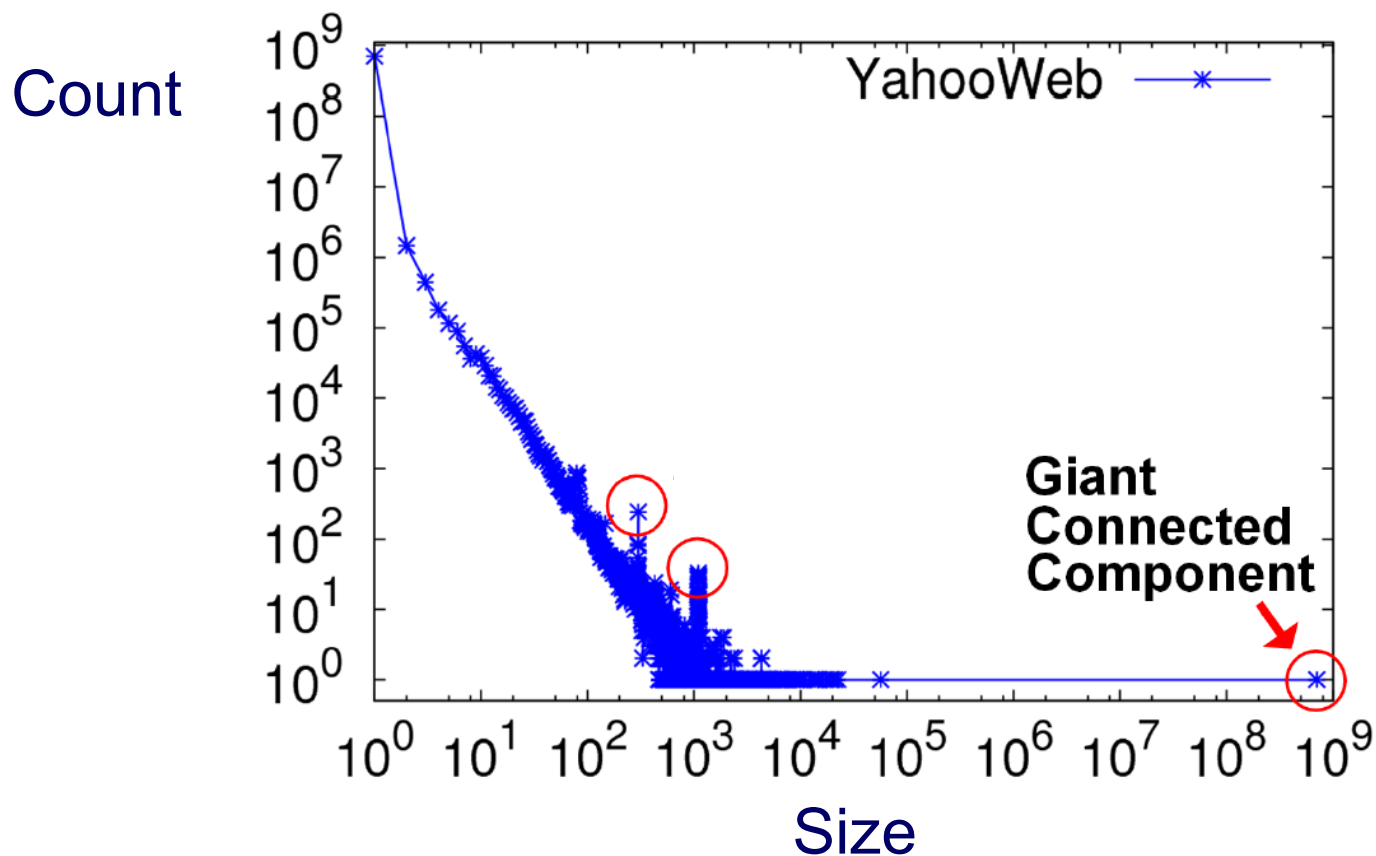
*PEGASUS: A Peta-Scale Graph Mining
System - Implementation and Observations.*

U Kang, Charalampos E. Tsourakakis,
and Christos Faloutsos.

(ICDM) 2009, Miami, Florida, USA.
Best Application Paper (runner-up).

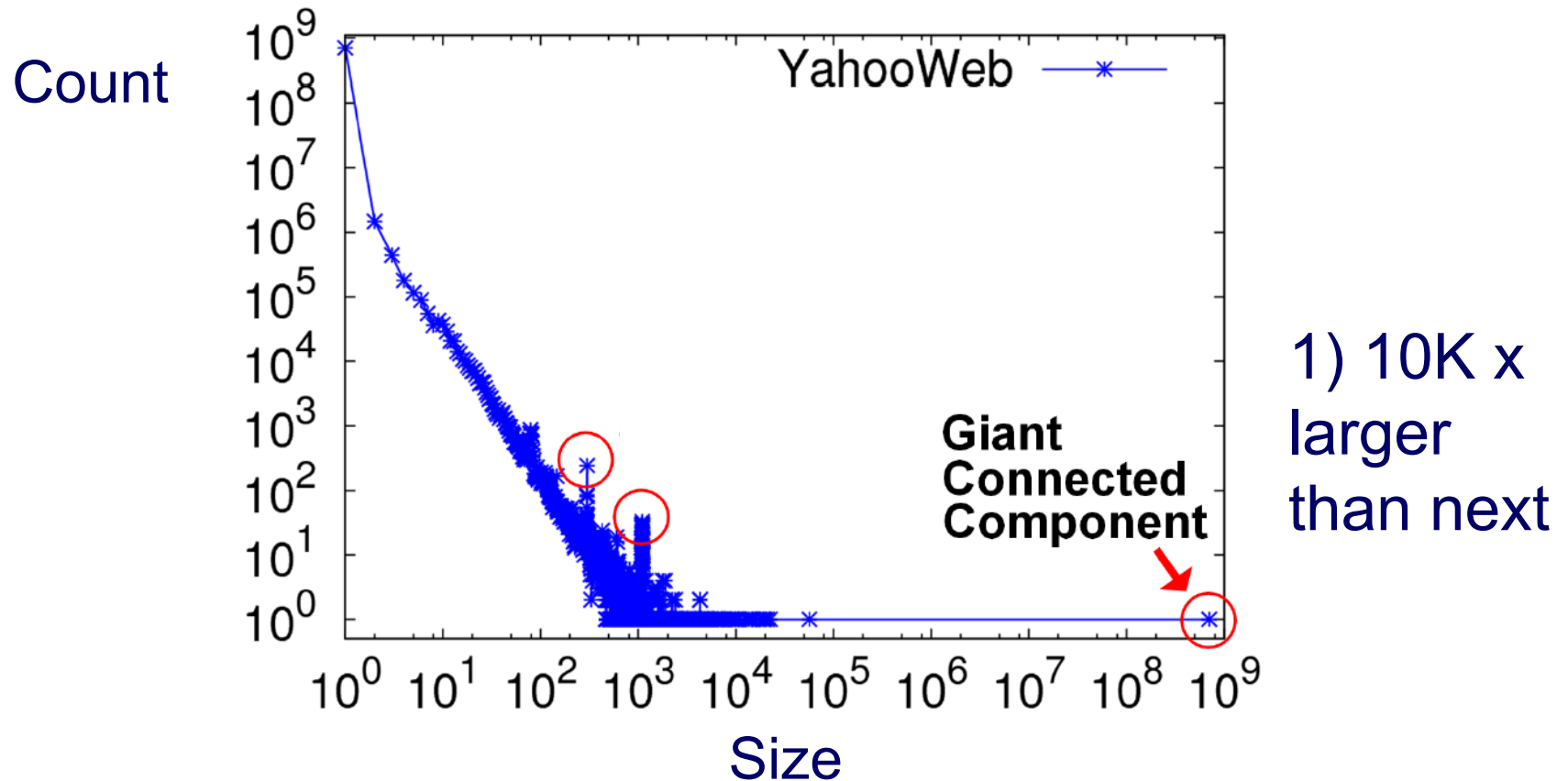
Example: GIM-V At Work

- Connected Components – 4 observations:



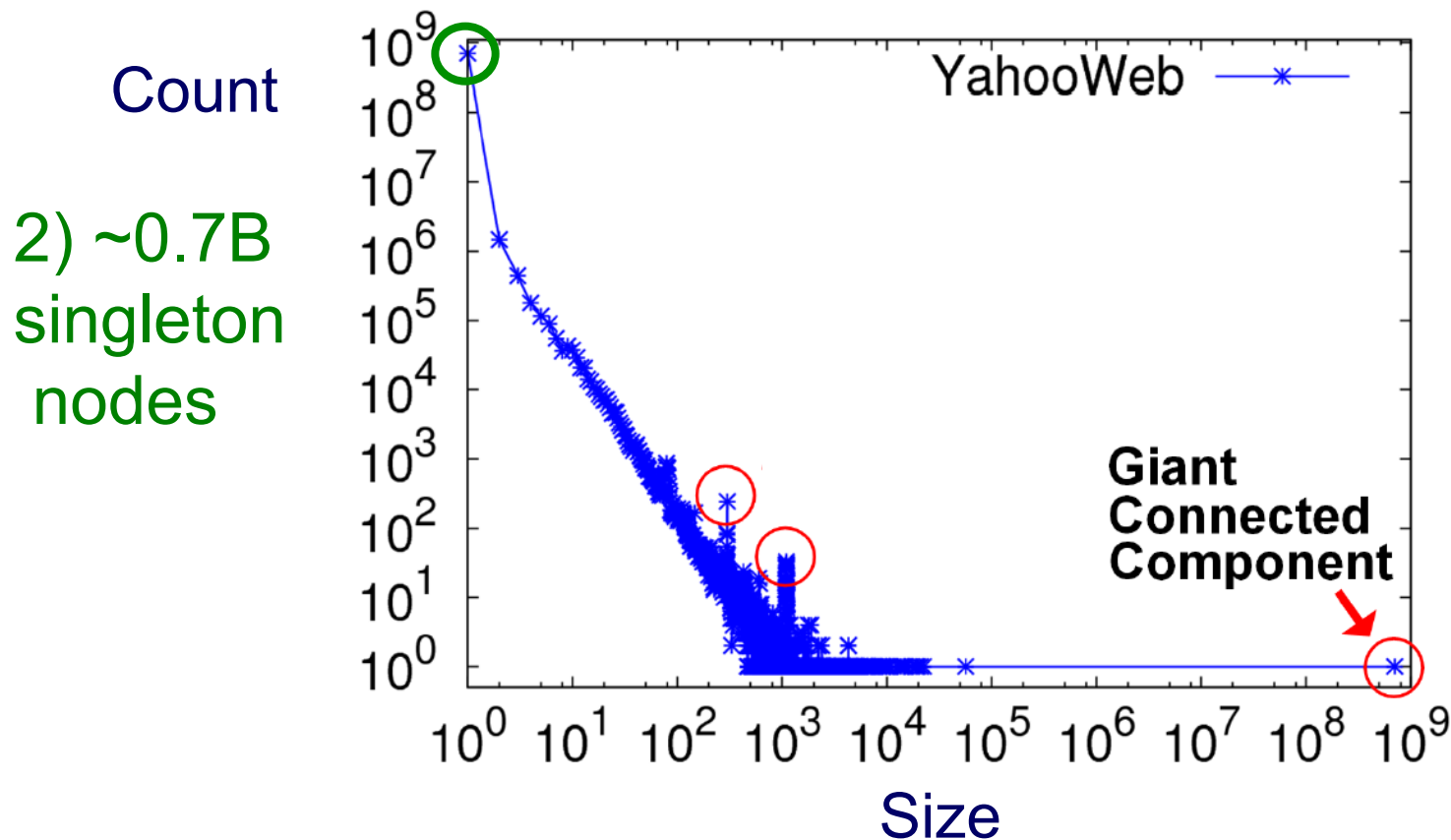
Example: GIM-V At Work

- Connected Components



Example: GIM-V At Work

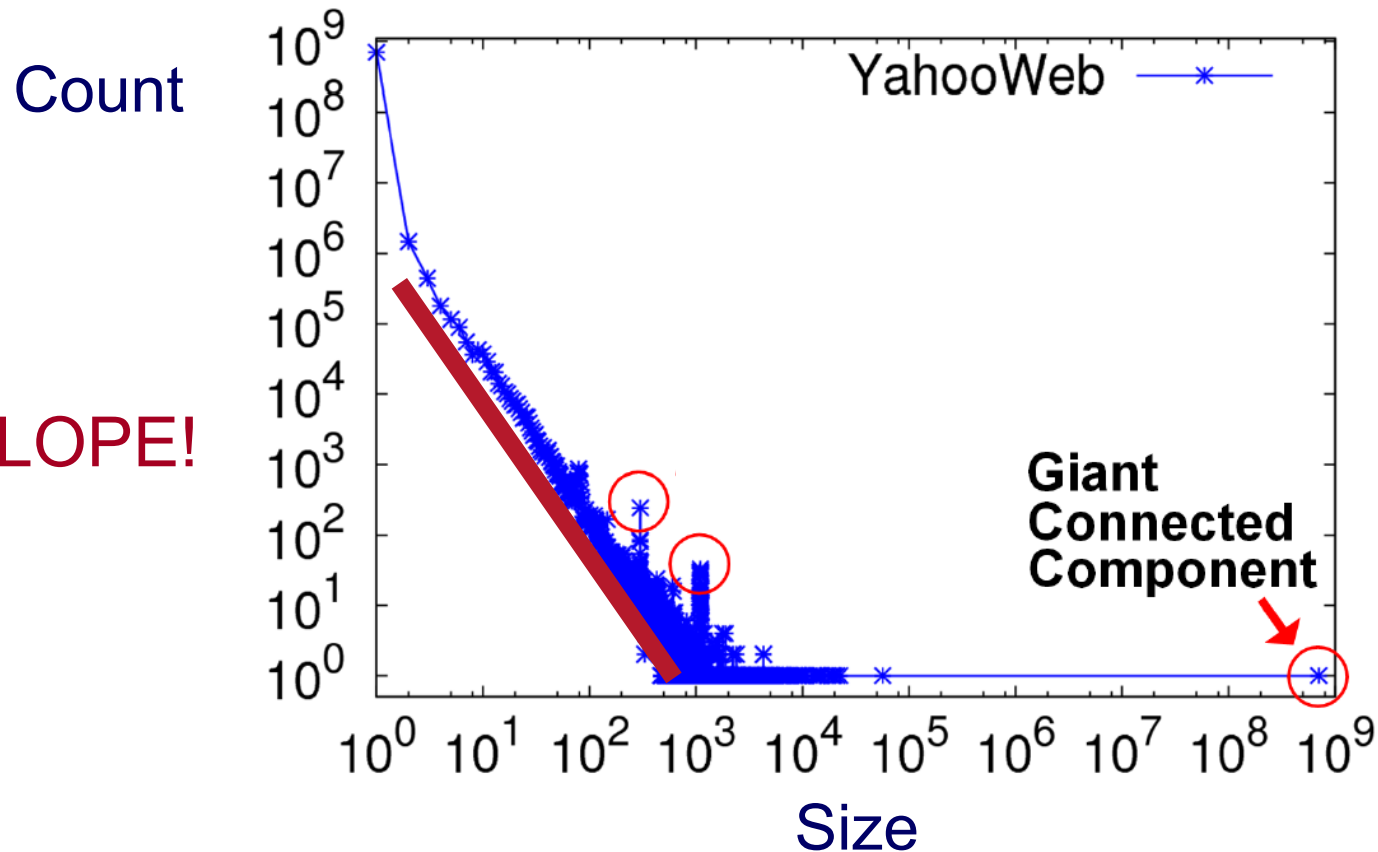
- Connected Components



Example: GIM-V At Work

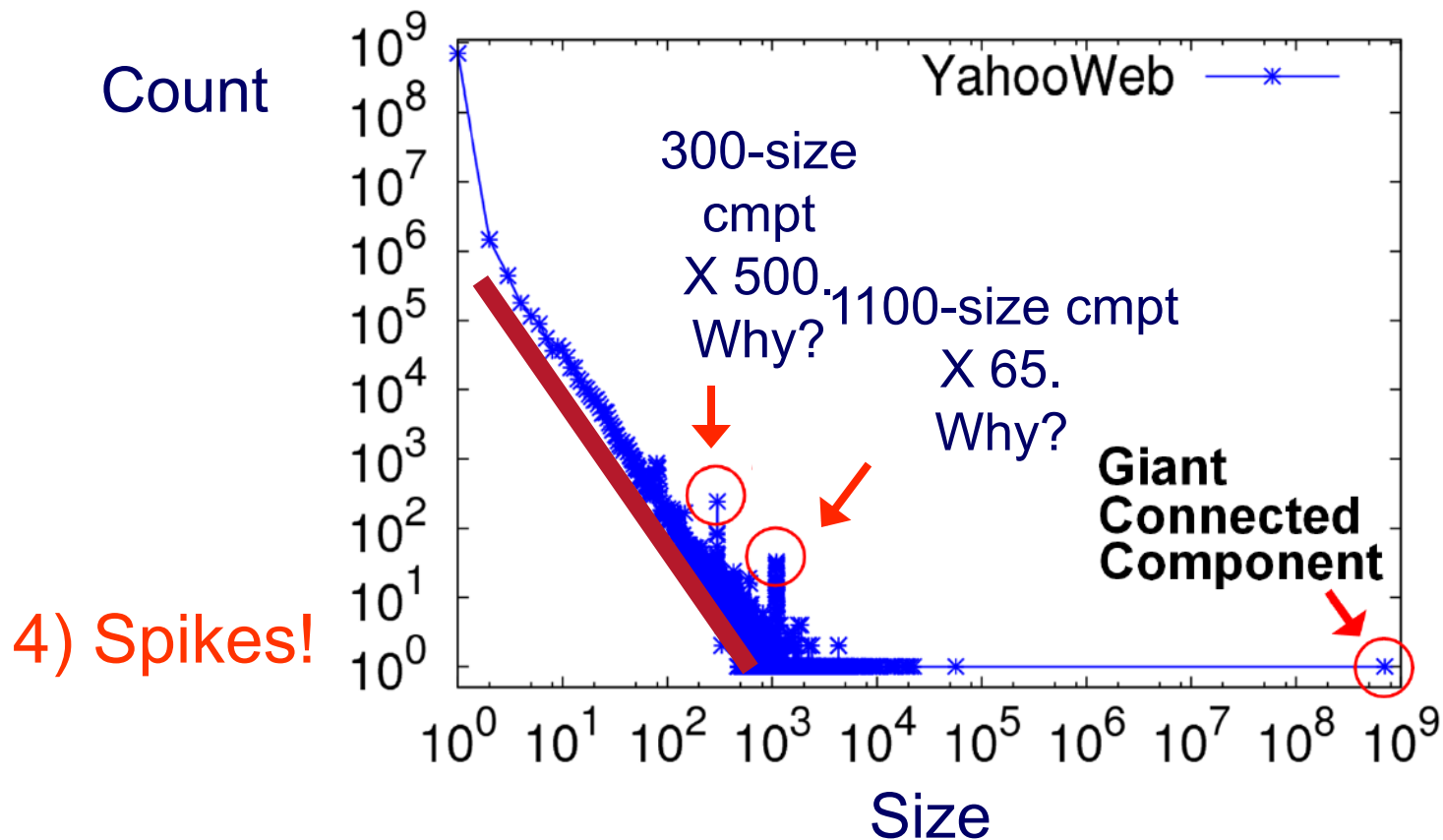
- Connected Components

3) SLOPE!



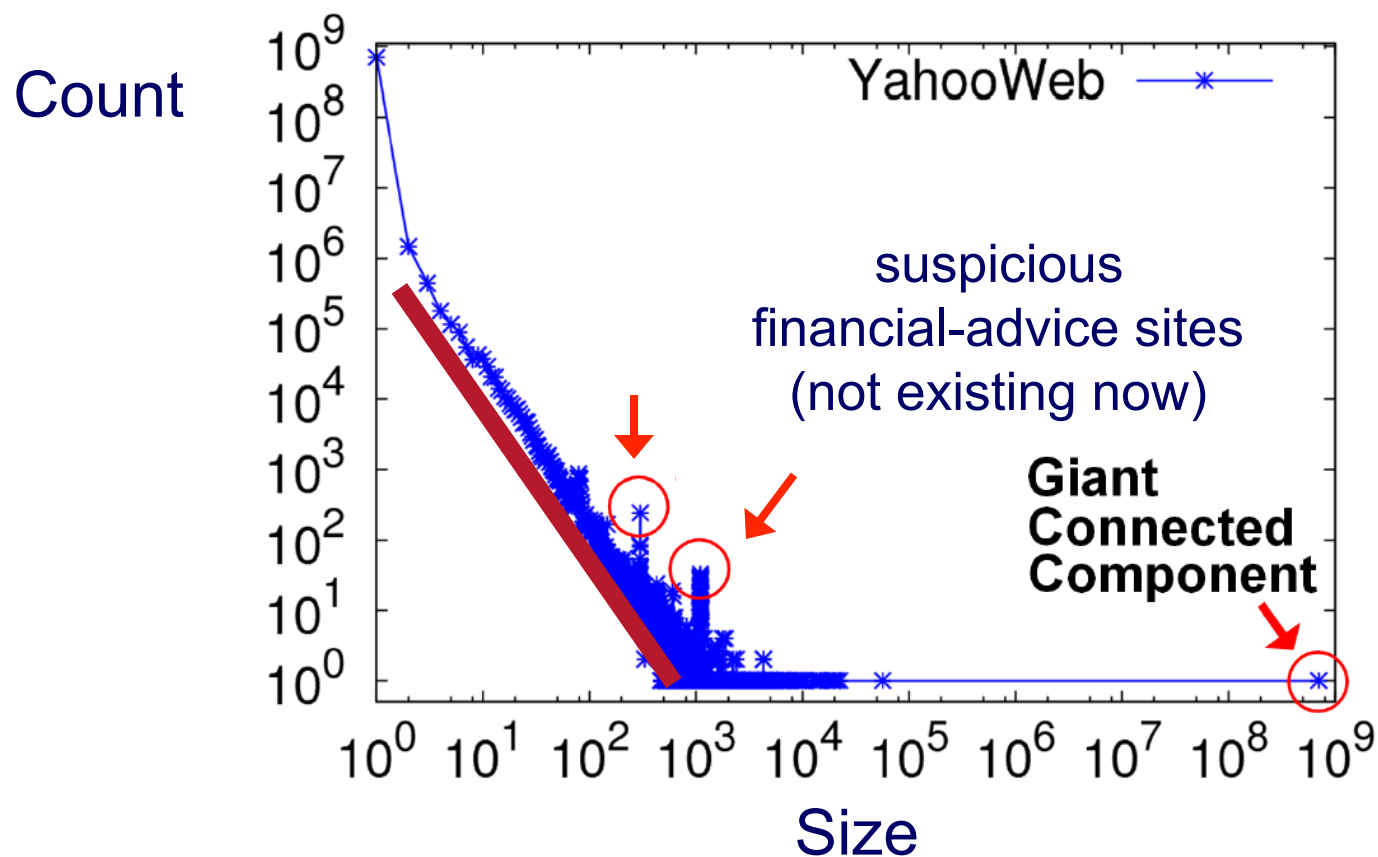
Example: GIM-V At Work

- Connected Components



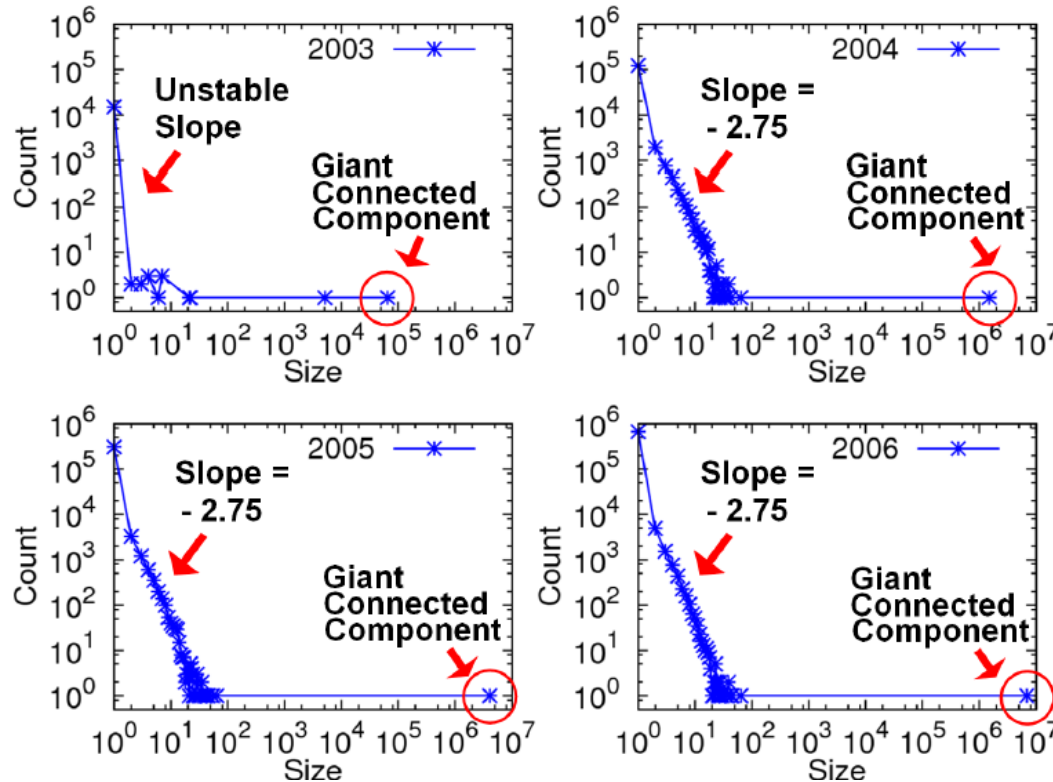
Example: GIM-V At Work

- Connected Components



GIM-V At Work

- Connected Components over Time
- **LinkedIn: 7.5M nodes and 58M edges**



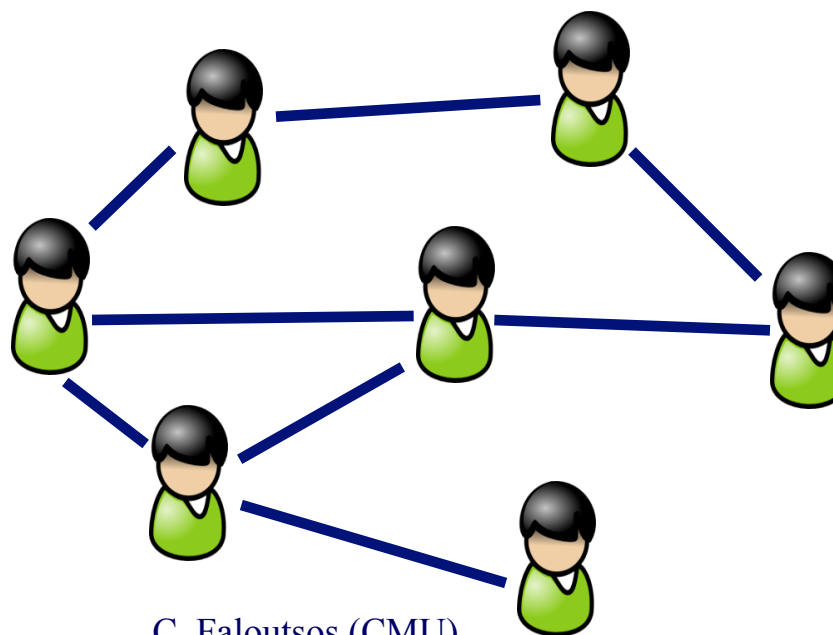
Stable tail slope
after the gelling point

Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
 - ➔ – Immunization
 - BP
 - visualization
- Conclusions

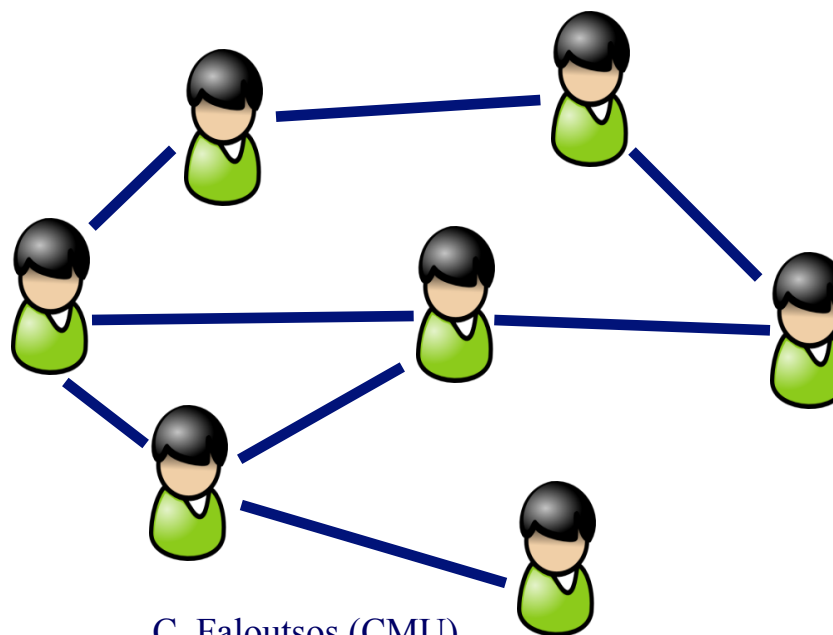
Immunization and epidemic thresholds

- Q1: which nodes to immunize?
- Q2: will a virus vanish, or will it create an epidemic?



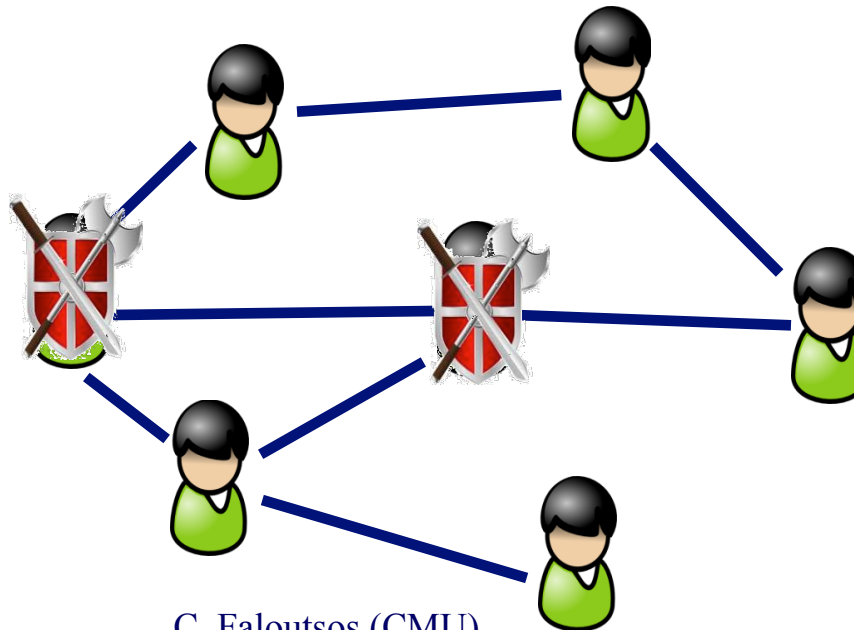
Q1: Immunization:

- Given
 - a network,
 - k vaccines, and
 - the virus details
- Which nodes to immunize?



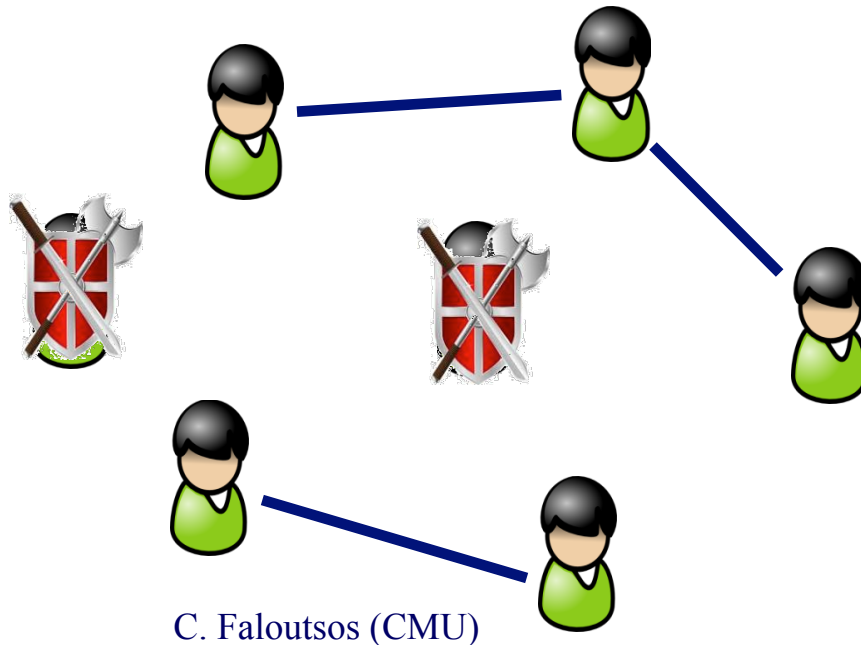
Q1: Immunization:

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Q1: Immunization:

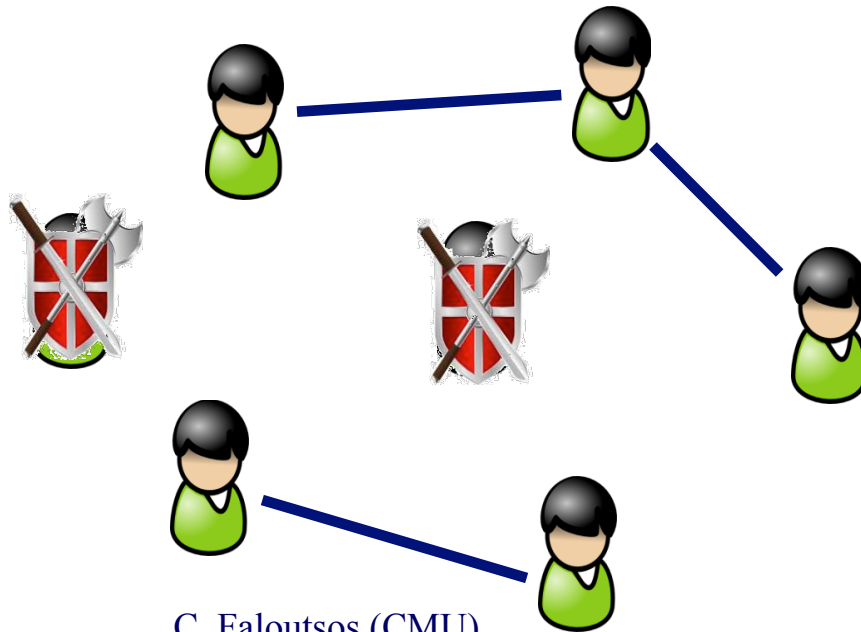
- Given
 - a network,
 - k vaccines, and
 - the virus details
- Which nodes to immunize?



Q1: Immunization:

- Given
 - a network,
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- Which nodes to immunize?

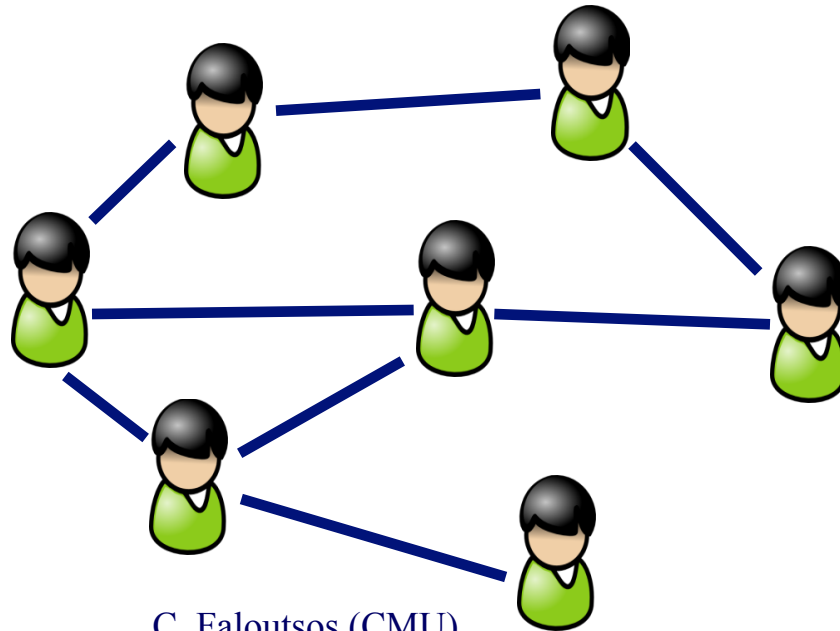
A: immunize the ones that maximally raise the 'epidemic threshold'
[Tong+, ICDM'10]



Q2: will a virus take over?

- Flu-like virus (no immunity, 'SIS')
- Mumps (life-time immunity, 'SIR')
- Pertussis (finite-length immunity, 'SIRS')

β : attack prob
 δ : heal prob



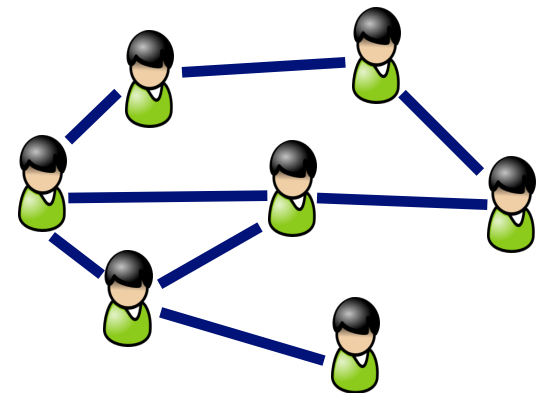
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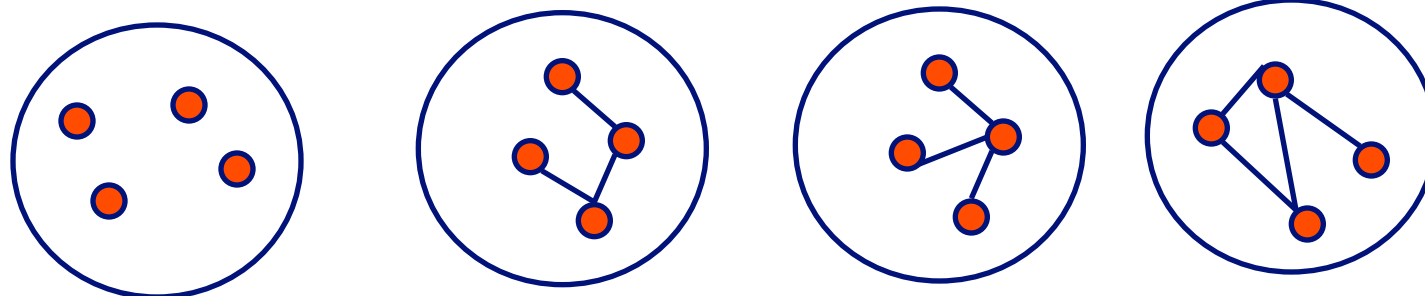
A: depends on connectivity
(avg degree? Something else?)



Epidemic threshold τ

What should τ depend on?

- avg. degree? and/or highest degree?
- and/or variance of degree?
- and/or third moment of degree?
- and/or diameter?



Epidemic threshold - SIS

- [Theorem] We have no epidemic, if

$$\beta/\delta < \tau = 1/\lambda_{1,A}$$

Epidemic threshold - SIS

- [Theorem] We have no epidemic, if

recovery prob. $\beta/\delta < \tau = 1/\lambda_{1,A}$ epidemic threshold

attack prob. β/δ largest eigenvalue of adj. matrix A

The diagram shows the inequality $\beta/\delta < \tau = 1/\lambda_{1,A}$ enclosed in a blue box. A blue arrow points from the text 'recovery prob.' to the δ in the denominator. Another blue arrow points from 'attack prob.' to the β in the numerator. A blue arrow points from 'epidemic threshold' to the τ . A red arrow points from 'largest eigenvalue of adj. matrix A ' to the $\lambda_{1,A}$ term.

Proof: [Wang+03] (for **SIS=flu only**)

Epidemic threshold - SIS

- [Theorem] We have no epidemic, if

$$\beta/\delta < \tau = 1/\lambda_{1,A}$$

**What about other V.P.M.?
(SIR, SIRS, etc?)**

Proof: [Wang+03] (for SIS=flu only)



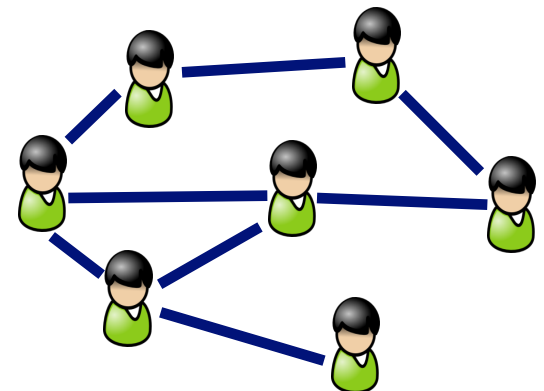
Theorem:

- For **all** typical virus propagation models (flu, mumps, pertussis, HIV, etc)
- The **only** connectivity measure that matters, is

$$1/\lambda_1$$

the first eigenvalue of the
adj. matrix

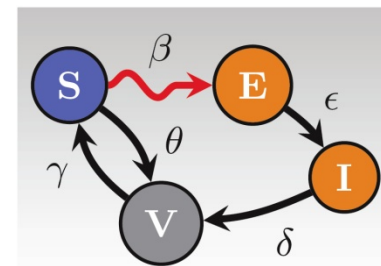
[Prakash+, '10, arxiv]





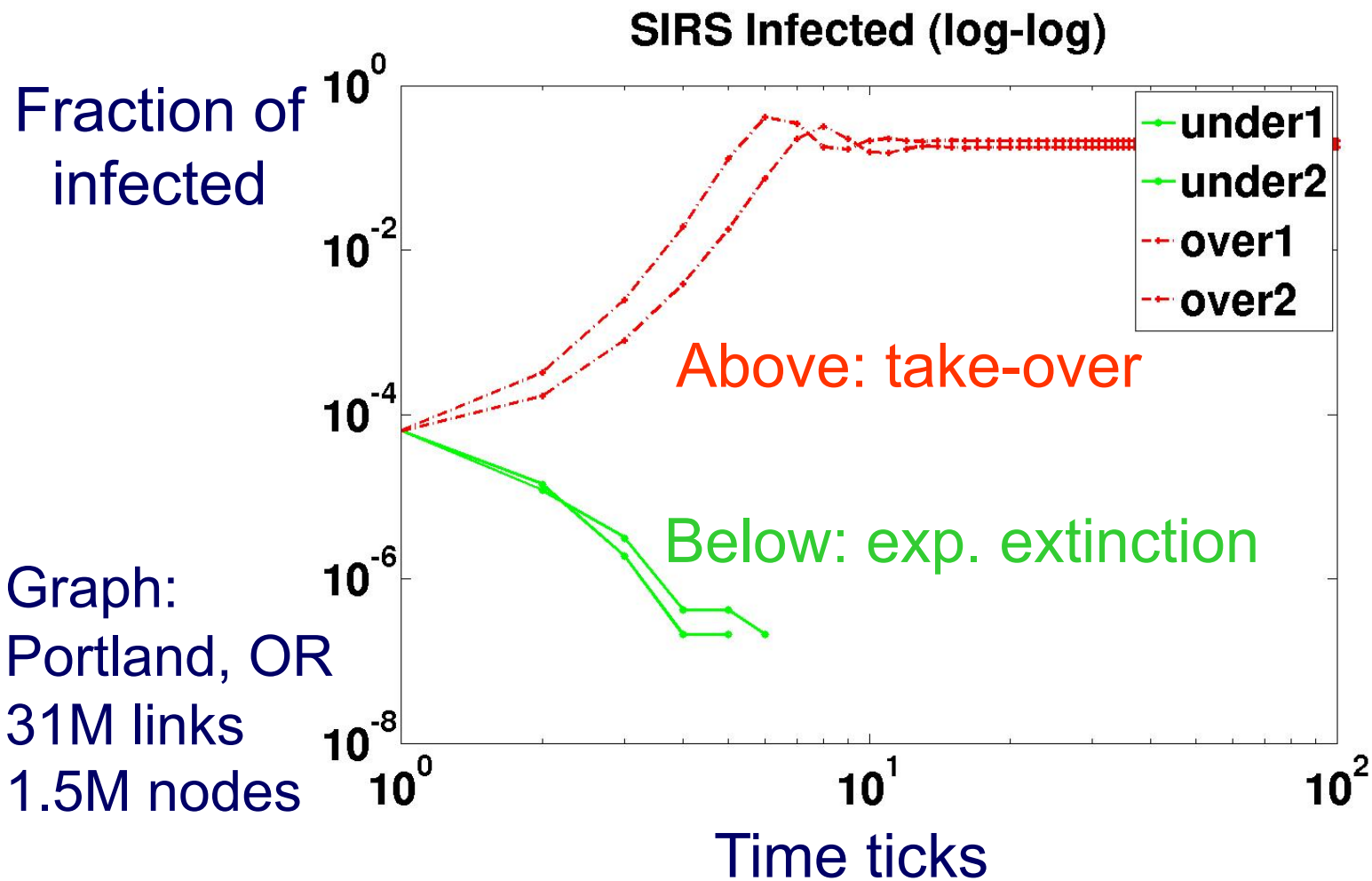
Thresholds for some models

- $s = \text{effective strength}$
- $s < 1$: *below threshold*



Models	Effective Strength (s)	Threshold (tipping point)
SIS, SIR, SIRS, SEIR	$s = \lambda \cdot \left(\frac{\beta}{\delta} \right)$	$s = 1$
SIV, SEIV	$s = \lambda \cdot \left(\frac{\beta\gamma}{\delta(\gamma + \theta)} \right)$	
$SI_1I_2V_1V_2$ (H.I.V.)	$s = \lambda \cdot \left(\frac{\beta_1v_2 + \beta_2\varepsilon}{v_2(\varepsilon + v_1)} \right)$	

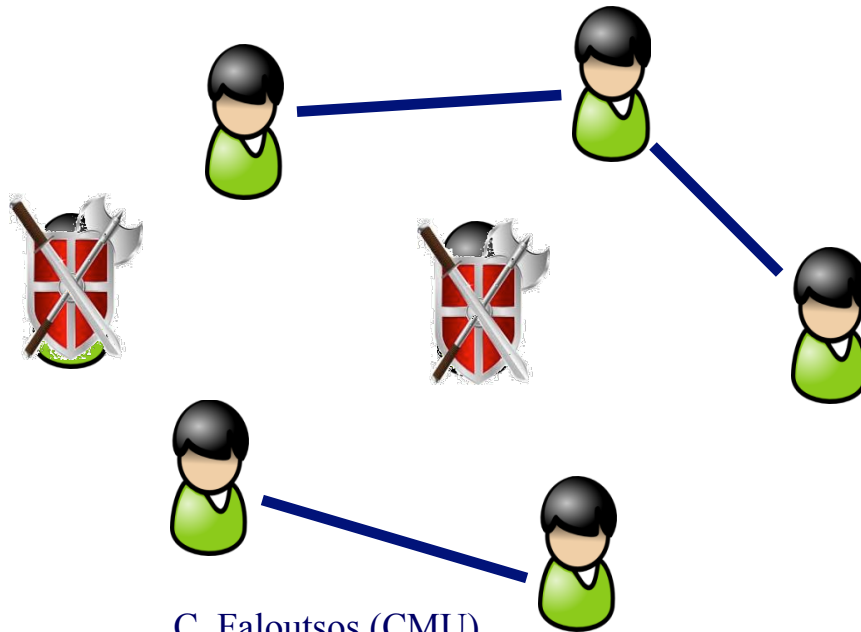
A2: will a virus take over?



Q1: Immunization:

- Given
 - a network,
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 - the virus details
- Which nodes to immunize?

A: immunize the ones that maximally raise the `epidemic threshold'
[Tong+, ICDM'10]

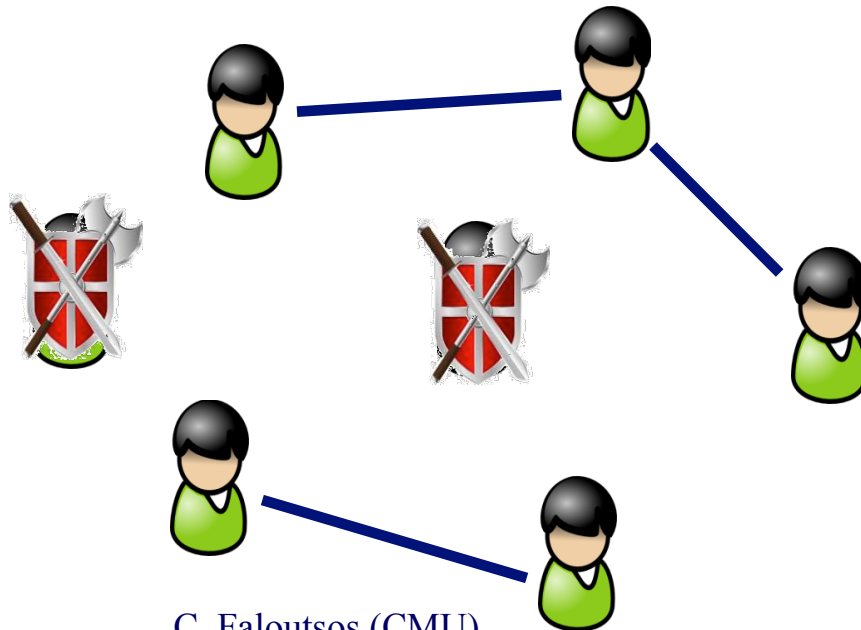


Q1: Immunization:

- Given
 - a network,
 - k vaccines, and
 - the virus details
- Which nodes to immunize?

A: immunize the ones that

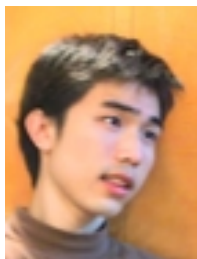
**Max eigen-drop $\Delta\lambda$
For any virus!**



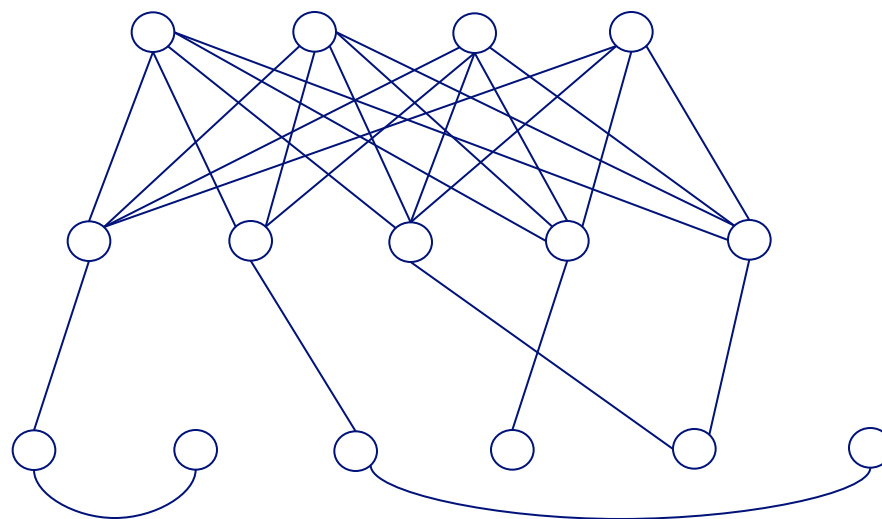
Outline

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- Conclusions

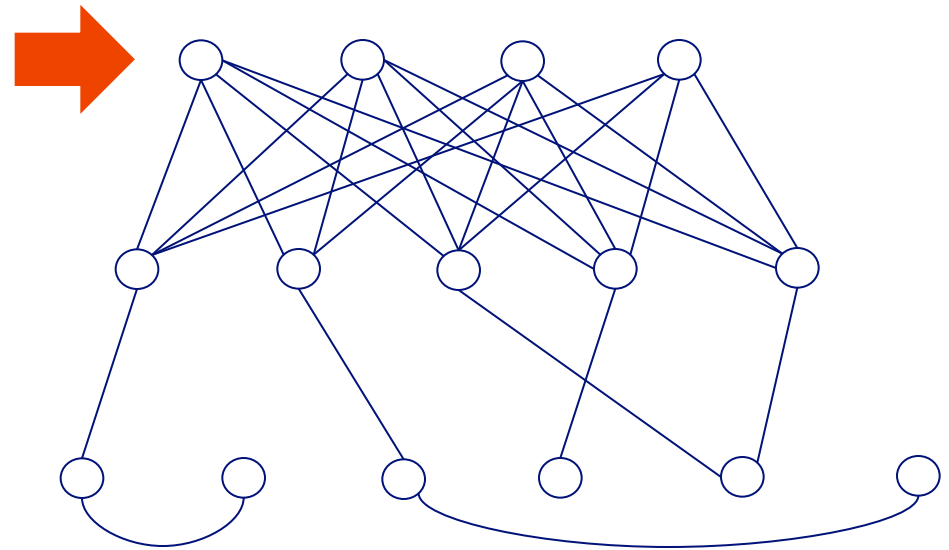
E-bay Fraud detection



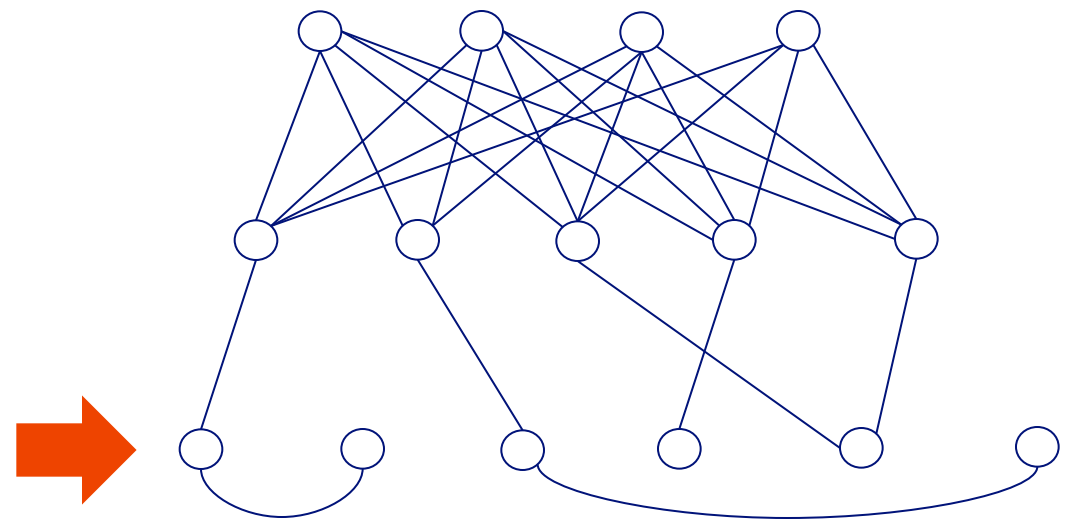
w/ Polo Chau &
Shashank Pandit, CMU
[www'07]



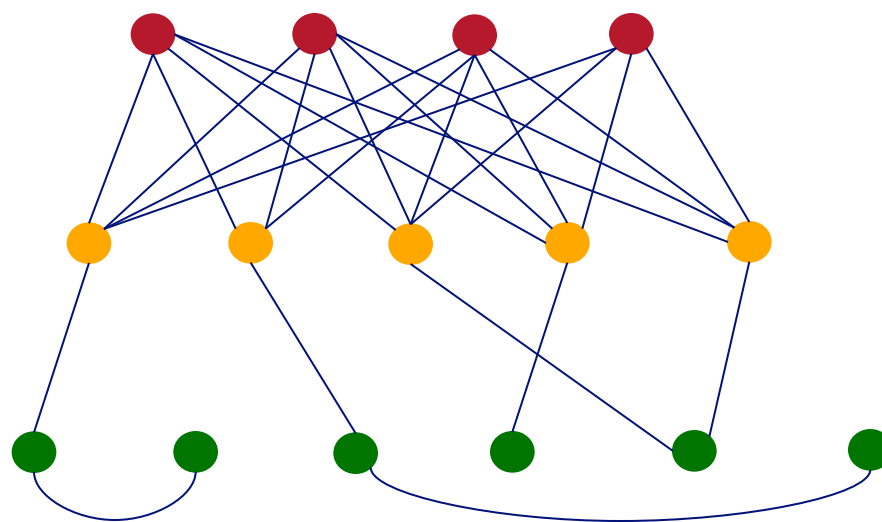
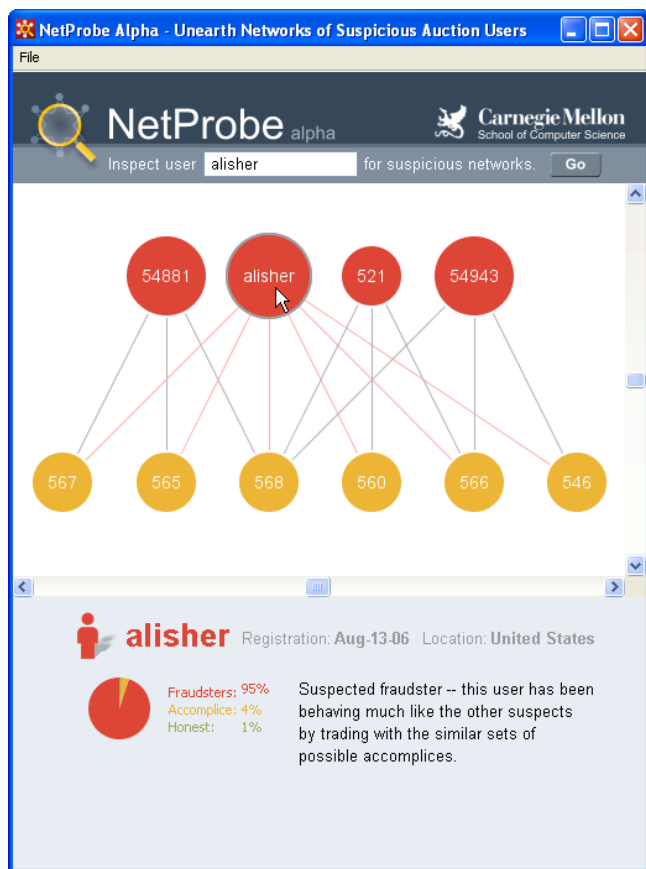
E-bay Fraud detection



E-bay Fraud detection



E-bay Fraud detection - NetProbe



Popular press



The Washington Post

Los Angeles Times

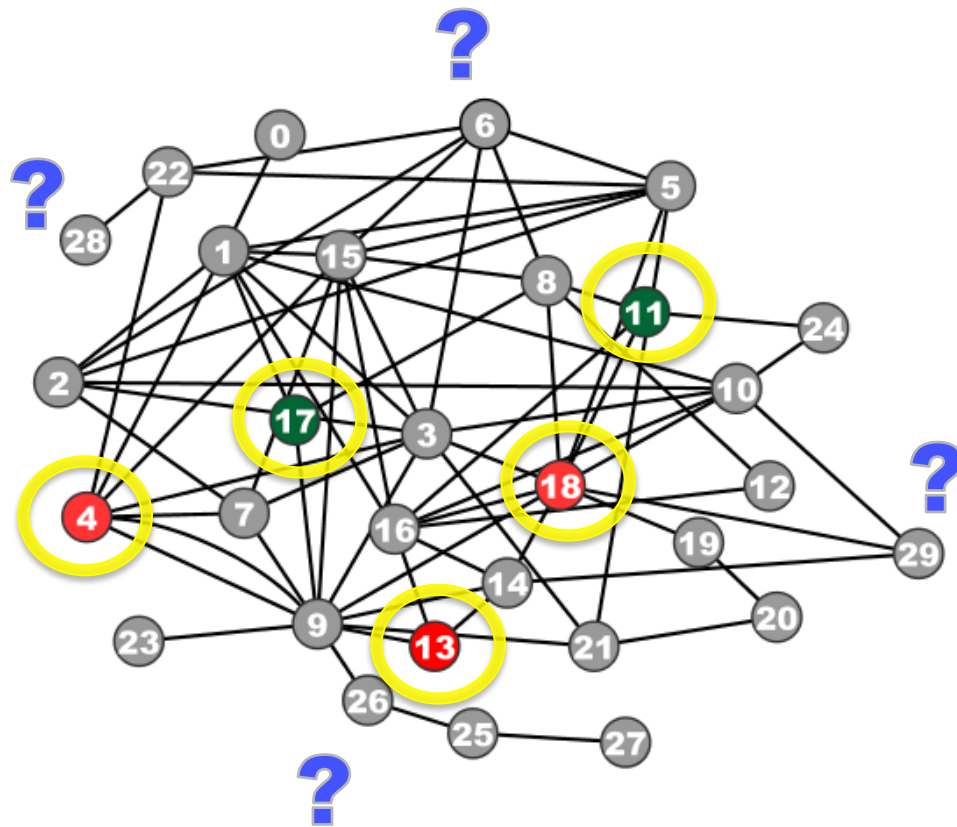
And less desirable attention:

- E-mail from ‘Belgium police’ (‘copy of your code?’)

Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
 - Immunization
 - ➔ – BP - theory
 - visualization
- Conclusions

Guilt-by-Association Techniques



Given:

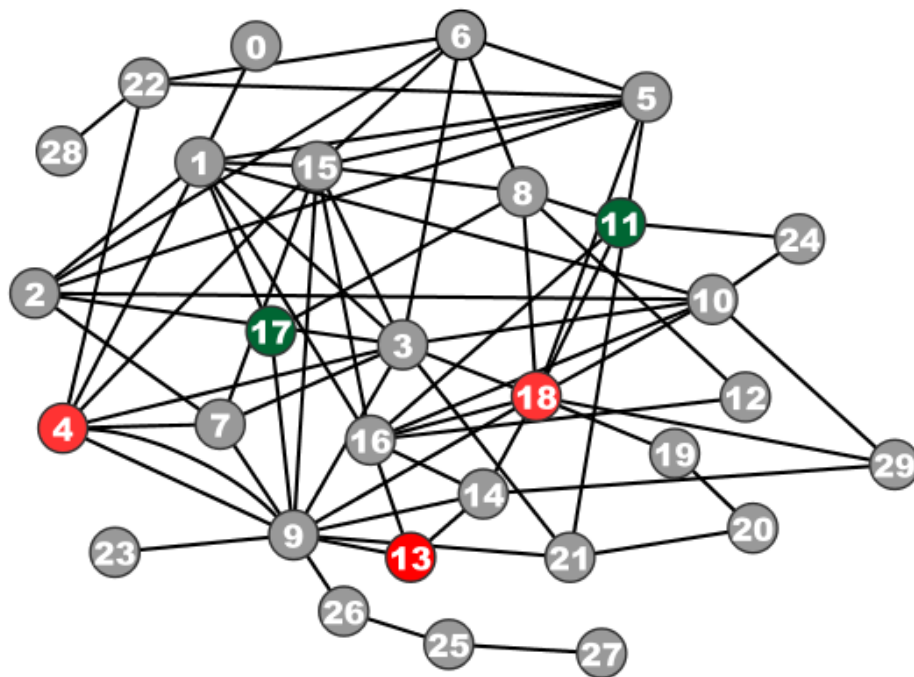
- graph and
- few labeled nodes

Find: class (red/green)
for rest nodes

Assuming: network
effects (homophily/
heterophily)

Correspondence of Methods

Random Walk with Restarts (**RWR**) Google
Semi-supervised Learning (**SSL**)
Belief Propagation (**BP**) Bayesian

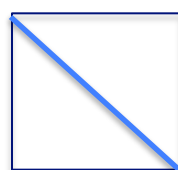
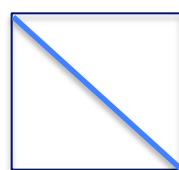




Correspondence of Methods

Random Walk with Restarts (**RWR**) \approx
 Semi-supervised Learning (**SSL**) \approx
 Belief Propagation (**BP**)

Method	Matrix		unknown	=	known
RWR	$[\mathbf{I} - c \mathbf{A} \mathbf{D}^{-1}]$	\times	\mathbf{x}	=	$(1-c)\mathbf{y}$
SSL	$[\mathbf{I} + a(\mathbf{D} - \mathbf{A})]$	\times	\mathbf{x}	=	\mathbf{y}
FABP	$[\mathbf{I} + a \mathbf{D} - c' \mathbf{A}]$	\times	\mathbf{b}_h	=	ϕ_h



$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$



$$\begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$$

Unifying Guilt-by-Association Approaches: Theorems and Fast Algorithms. Danai Koutra, et al *PKDD'11*

Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
 - Immunization
 - BP
 - ➔ – visualization
- Conclusions

Apolo

Making Sense of Large Network Data:
Combining Rich User Interaction & Machine Learning
CHI 2011, Vancouver, Canada



Polo Chau



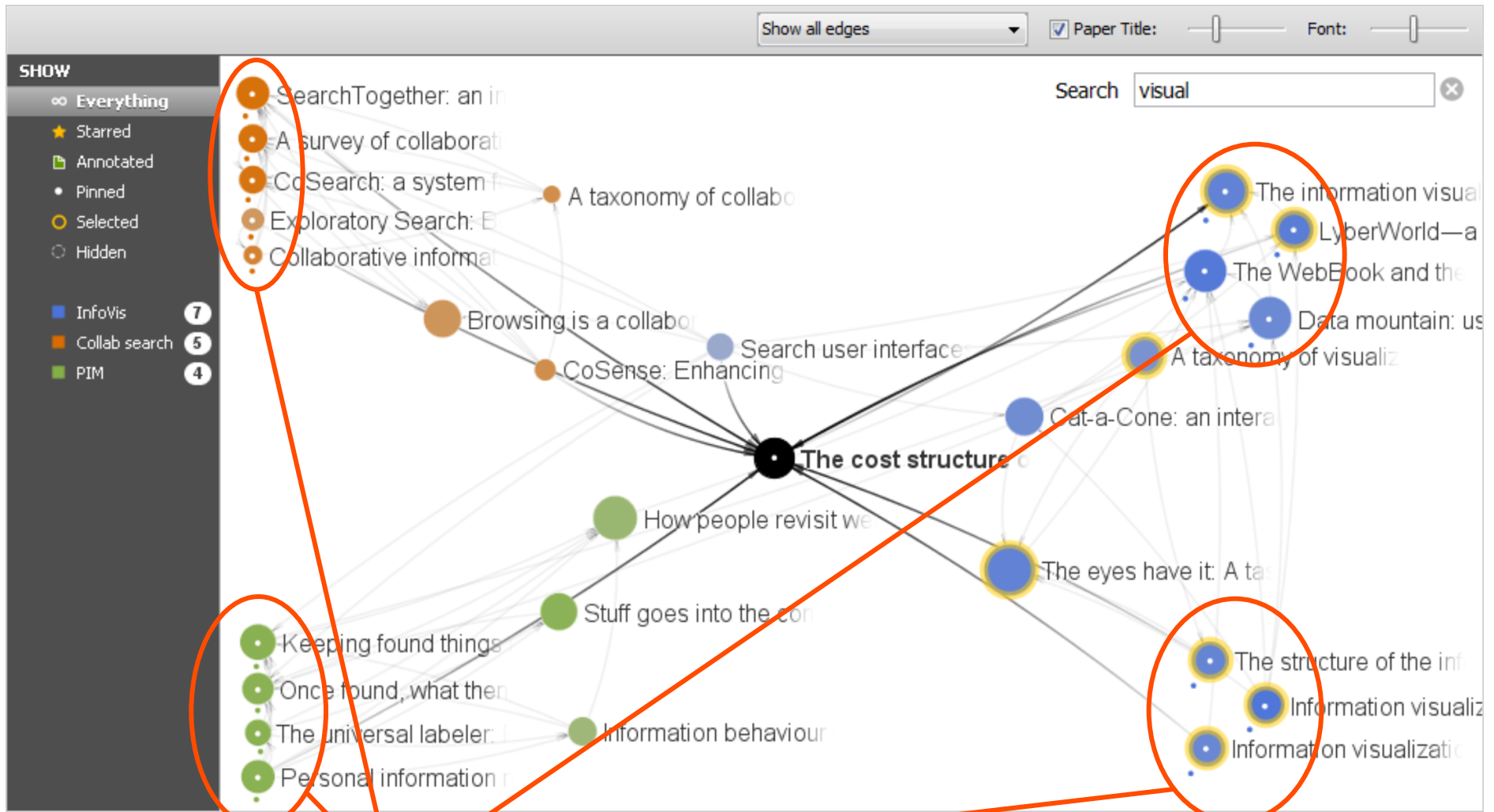
Prof. Niki Kittur



Prof. Jason Hong



Prof. Christos Faloutsos



Exemplars

Rest of the nodes are considered relevant (by BP); relevance indicated by color saturation.

C. Faloutsos (CMU) Note that BP supports multiple groups 100

Outline

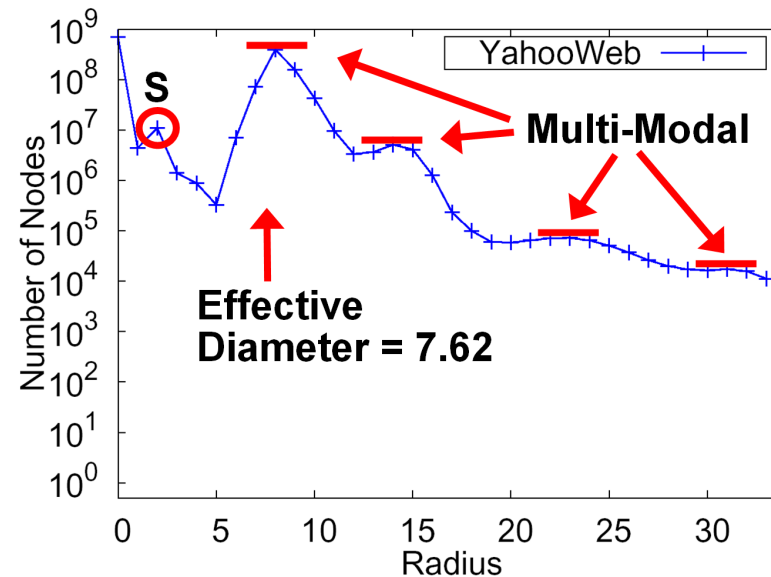
- Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
 - Immunization
 - BP
 - visualization
- ➔ • Conclusions

OVERALL CONCLUSIONS – low level:

- Several new **patterns** (eigenspokes, radius plot etc)
- New **tools** and theoretical results
 - belief propagation (\sim RWR \sim SSL)
 - Immunization: $\Delta \lambda$, for ‘any’ V.P.M.

OVERALL CONCLUSIONS – high level

- **BIG DATA:** -> patterns/outliers that are invisible otherwise



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- Leman Akoglu, Christos Faloutsos: *RTG: A Recursive Realistic Graph Generator Using Random Typing*. ECML/PKDD (1) 2009: 13-28
- Deepayan Chakrabarti, Christos Faloutsos: *Graph mining: Laws, generators, and algorithms*. ACM Comput. Surv. 38(1): (2006)

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- Deepayan Chakrabarti, Jure Leskovec, Christos Faloutsos, Samuel Madden, Carlos Guestrin, Michalis Faloutsos: *Information Survival Threshold in Sensor and P2P Networks*. INFOCOM 2007: 1316-1324

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- T. G. Kolda and J. Sun. *Scalable Tensor Decompositions for Multi-aspect Data Mining*. In: ICDM 2008, pp. 363-372, December 2008.

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- Jure Leskovec, Deepayan Chakrabarti, Jon M. Kleinberg, Christos Faloutsos: *Realistic, Mathematically Tractable Graph Generation and Evolution, Using Kronecker Multiplication*. PKDD 2005: 133-145

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- Jimeng Sun, Yinglian Xie, Hui Zhang, Christos Faloutsos. *Less is More: Compact Matrix Decomposition for Large Sparse Graphs*, SDM, Minneapolis, Minnesota, Apr 2007.
- Jimeng Sun, Spiros Papadimitriou, Philip S. Yu, and Christos Faloutsos, *GraphScope: Parameter-free Mining of Large Time-evolving Graphs* ACM SIGKDD Conference, San Jose, CA, August 2007

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- Jimeng Sun, Dacheng Tao, Christos Faloutsos: *Beyond streams and graphs: dynamic tensor analysis*. KDD 2006: 374-383

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- Hanghang Tong, Christos Faloutsos, and Jia-Yu Pan, *Fast Random Walk with Restart and Its Applications*, ICDM 2006, Hong Kong.
- Hanghang Tong, Christos Faloutsos, *Center-Piece Subgraphs: Problem Definition and Fast Solutions*, KDD 2006, Philadelphia, PA

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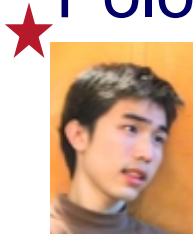
- Hanghang Tong, Christos Faloutsos, Brian Gallagher, Tina Eliassi-Rad: Fast best-effort pattern matching in large attributed graphs. KDD 2007: 737-746

Project info

www.cs.cmu.edu/~pegasus



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Polo



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Danae



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Aditya



Akoglu,
Leman

Kang, U

McGlohon,
Mary

Tong,
Hanghang

★ **Out, in '12**

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Google, INTEL, HP, iLab

OVERALL CONCLUSIONS – high level

- **BIG DATA:** -> patterns/outliers that are invisible otherwise

