

# **Mining Large Graphs: Patterns, Anomalies, and Fraud Detection**

*Christos Faloutsos*

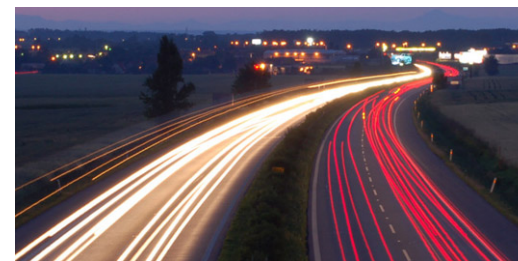
CMU

# Thank you!

- Dr. Yang Ou
- Prof. Shiqiang Yang
- Prof. Peng Cui
- Dr. Meng Jiang
- Chengxi
- Tianyang
- Kun
- Mingdong
- Daixin

# Roadmap

- ➔ • Introduction – Motivation
  - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
- Conclusions



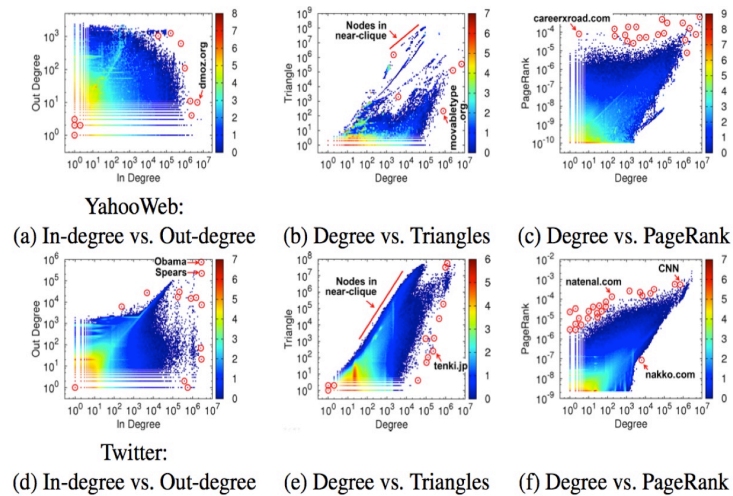
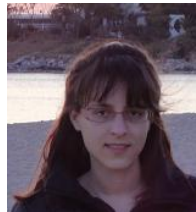
# Graphs - why should we care?



~1B nodes (web sites)  
~6B edges (http links)  
'YahooWeb graph'



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U Kang, Jay-Yoon Lee, Danai Koutra, and Christos Faloutsos. *Net-Ray: Visualizing and Mining Billion-Scale Graphs* PAKDD 2014, Tainan, Taiwan.

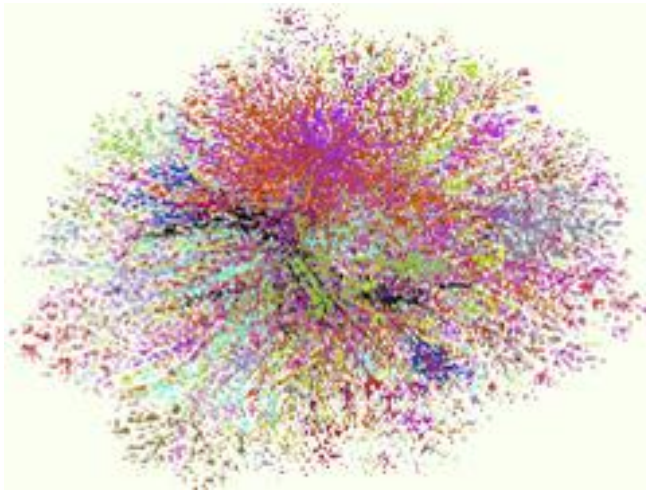
# Graphs - why should we care?



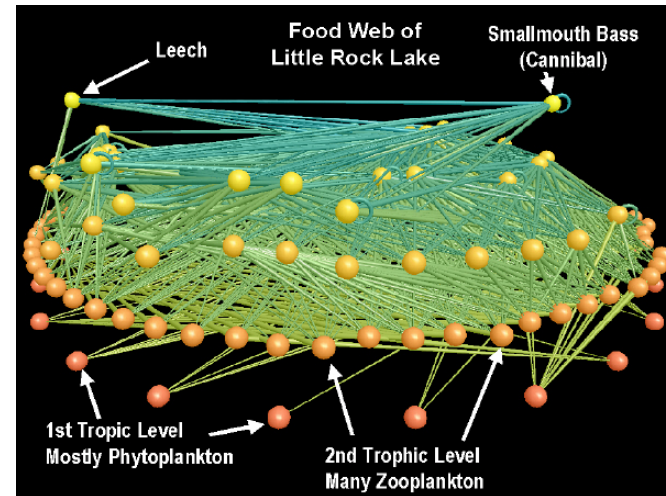
>\$10B; ~1B users



# Graphs - why should we care?



Internet Map  
[lumeta.com]



Food Web  
[Martinez '91]

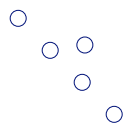
# Graphs - why should we care?

- web-log ('blog') news propagation
- computer network security: email/IP traffic and anomaly detection
- Recommendation systems
- ....
- Many-to-many db relationship -> graph

The Netflix logo is displayed in white capital letters on a red rectangular background.

# Motivating problems

- P1: patterns? Fraud detection?



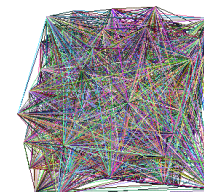
- P2: patterns in time-evolving graphs / tensors

destination



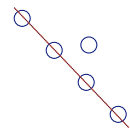
source

time



# Motivating problems

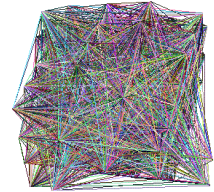
- P1: patterns? Fraud detection?



Patterns



anomalies



- P2: patterns in time-evolving graphs / tensors

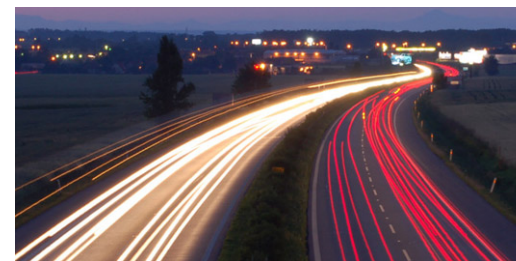
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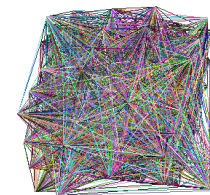
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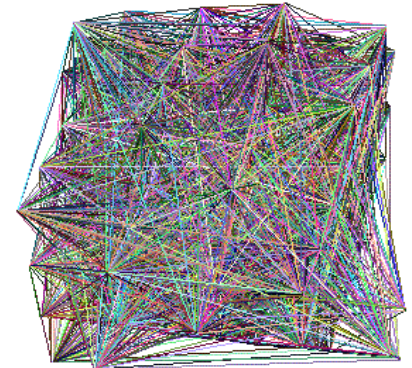


# Part 1: Patterns, & fraud detection



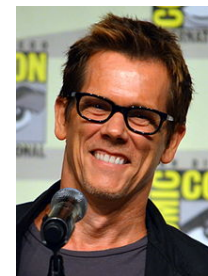
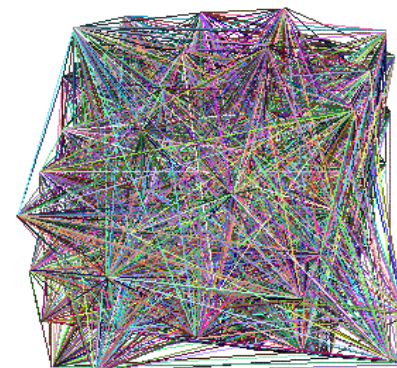
# Laws and patterns

- Q1: Are real graphs random?



# Laws and patterns

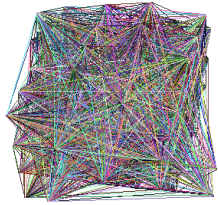
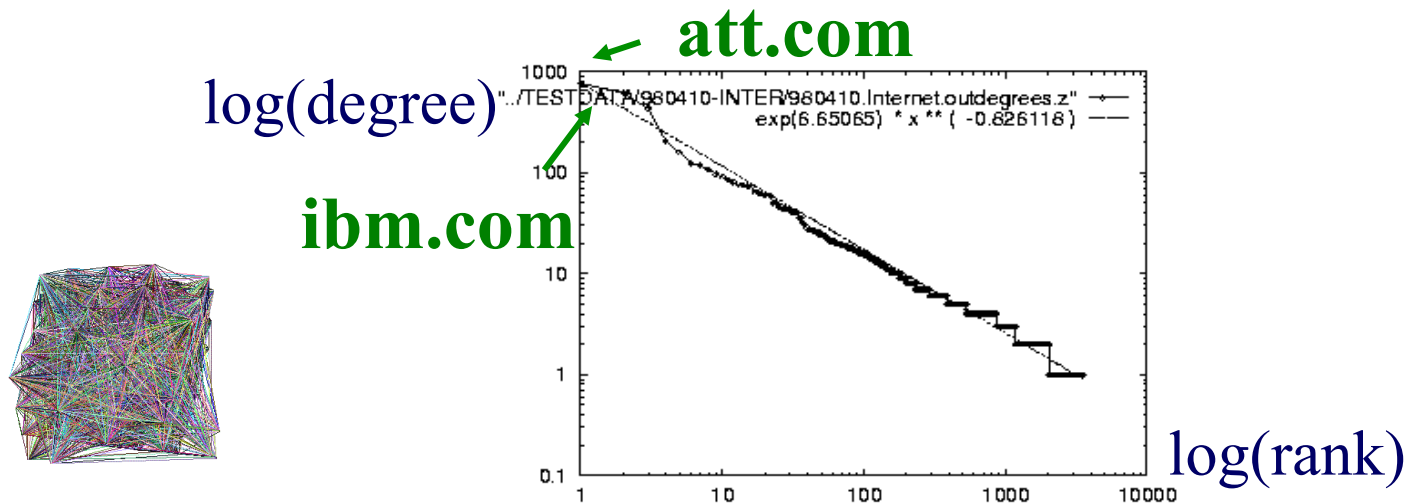
- Q1: Are real graphs random?
- A1: NO!!
  - Diameter ('6 degrees'; 'Kevin Bacon')
  - in- and out- degree distributions
  - other (surprising) patterns
- So, let's look at the data



# Solution# S.1

- Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

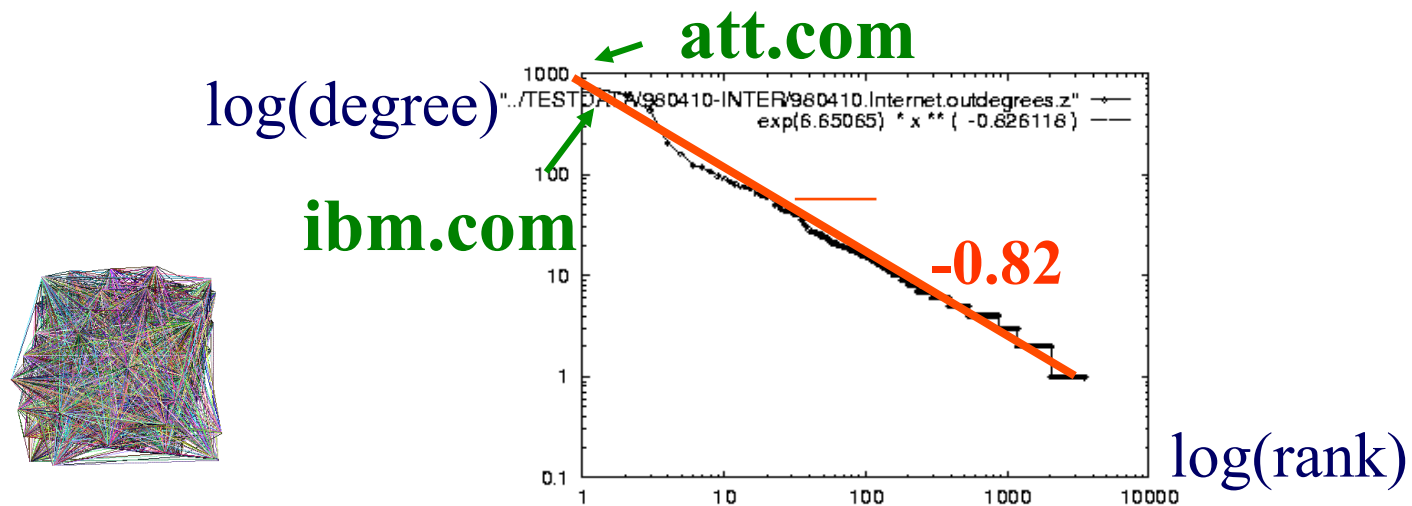
internet domains



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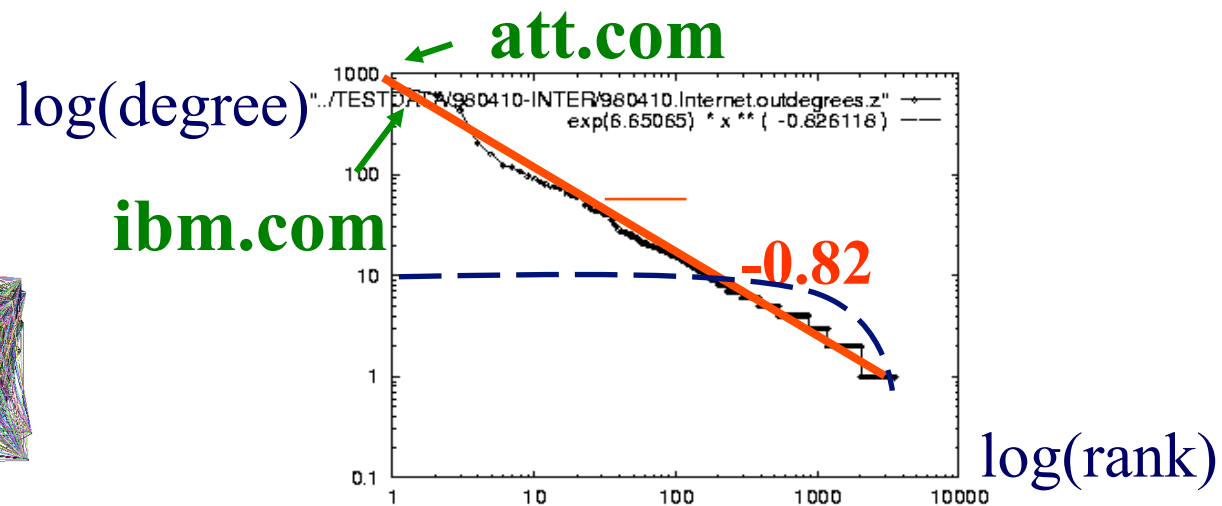
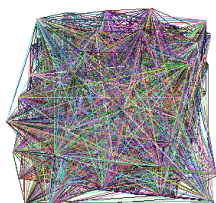
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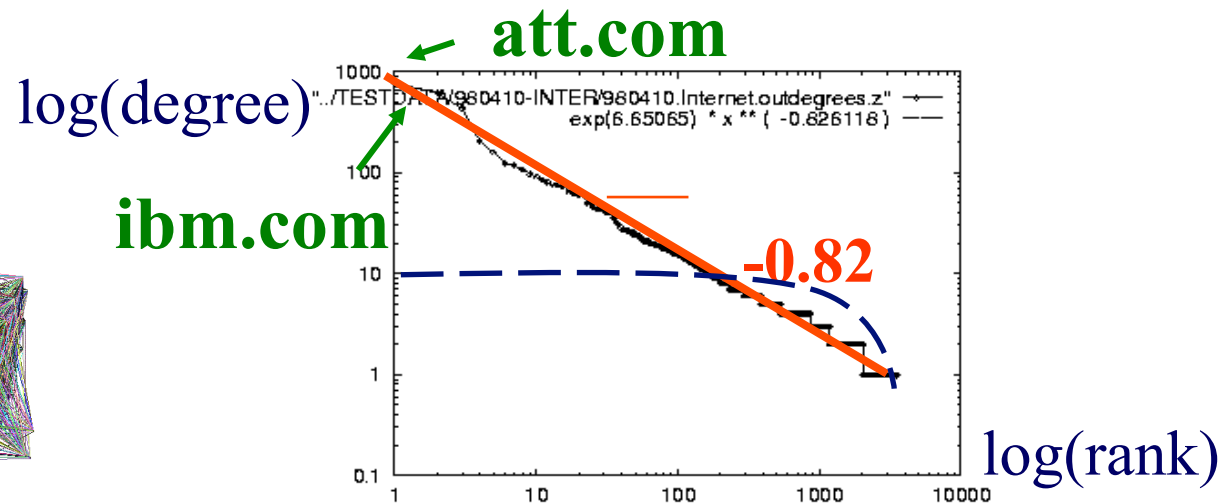
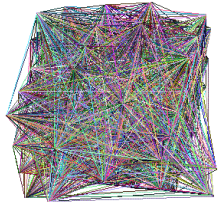
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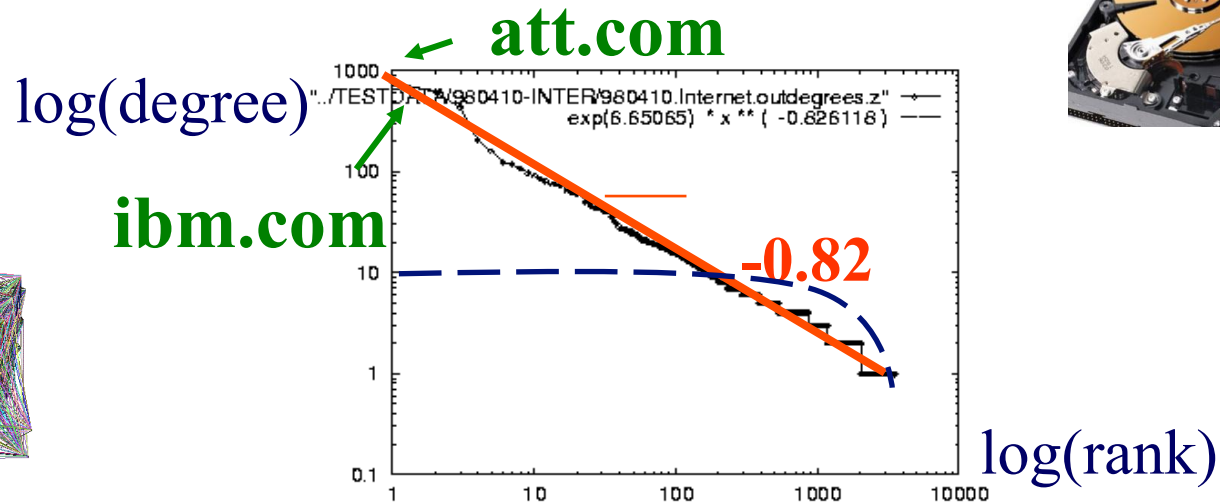
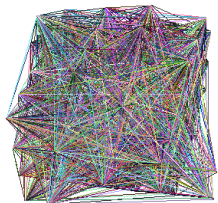
# Solution# S.1

- Q: So what?
- A1: # of two-step-away pairs: **internet domains**  
= friends of friends (F.O.F.)



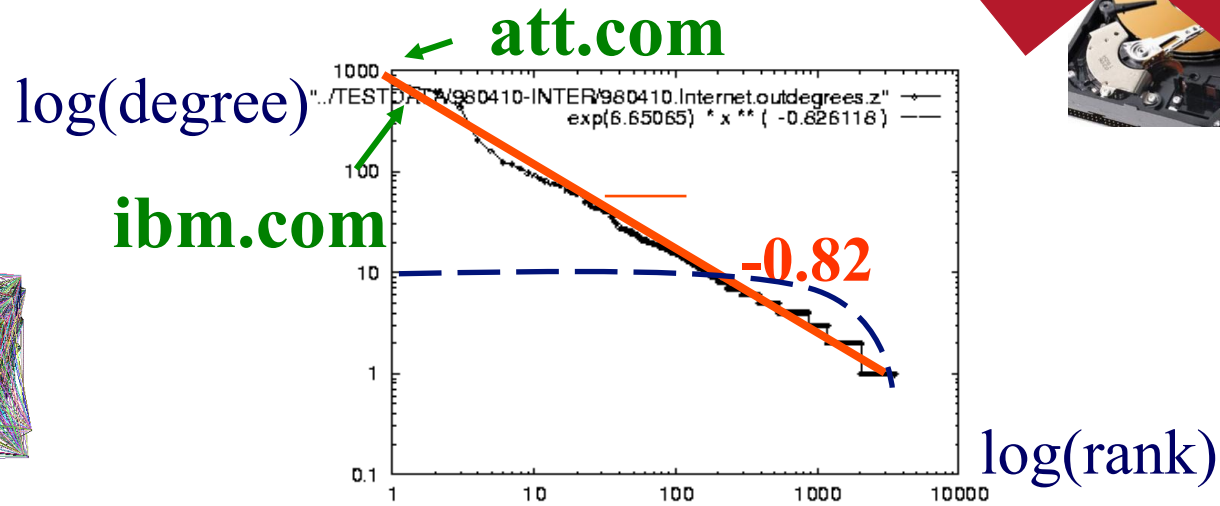
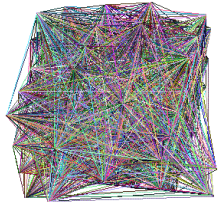
# Solution# S.1

- Q: So what? = friends of friends (F.O.F.)
- A1: # of two-step-away pairs:  $100^2 * N = 10$  Trillion internet domains



# Solution# S.1

- Q: So what?
- A1: # of two-step-away pairs:  $100^2 \times 100^2 = 10^8$  Trillion internet domains





# Gaussian trap

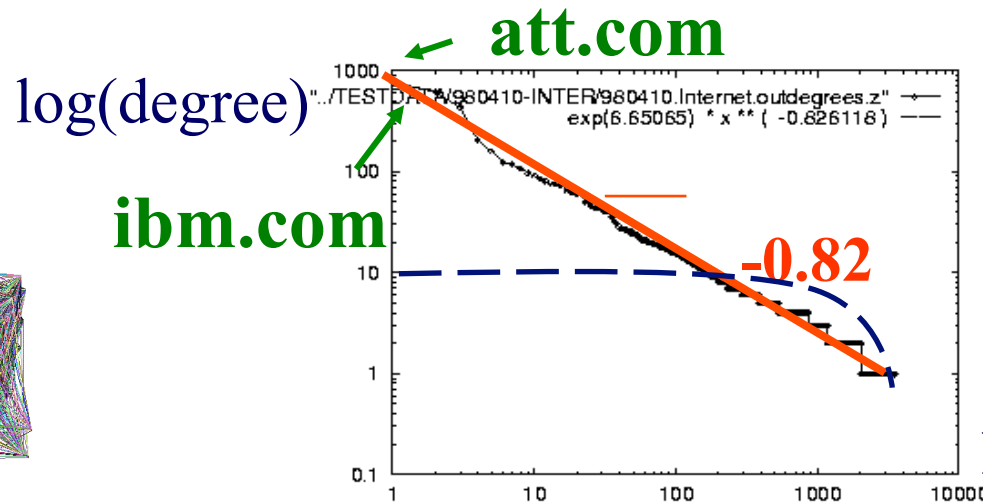
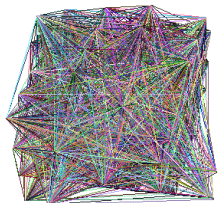
## Solution# S.1



- Q: So what? = friends of friends (F.O.F.)
- A1: # of two-step-away pairs:  $O(d_{\max}^2) \sim 10M^2$  internet domains



~0.8PB ->  
a data center(!)



# Gaussian trap

## Solution# S.1



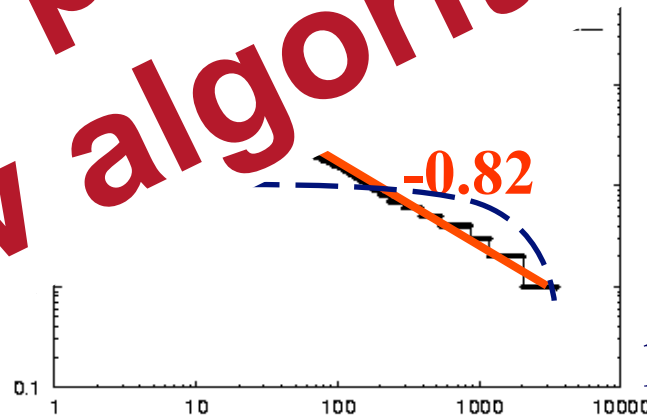
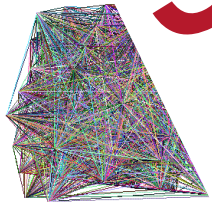
- Q: So what?
- A1: # of two-step-away inter

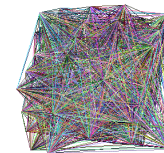
? ) ~  $10M^2$



~0.8PB ->  
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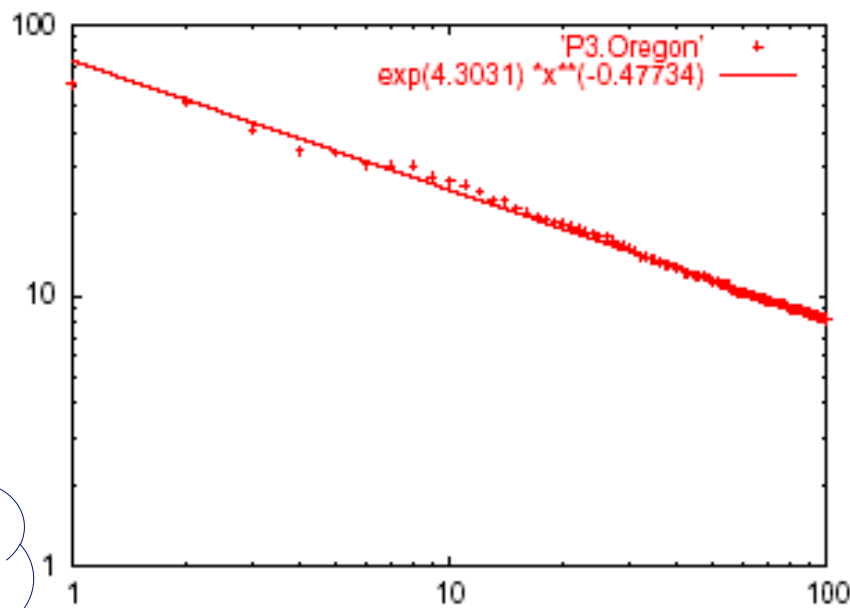
**Such patterns ->  
New algorithms**





# Solution# S.2: Eigen Exponent $E$

Eigenvalue



Exponent = slope

$$E = -0.48$$

$$\mathbf{A} \mathbf{x} = \lambda \mathbf{x}$$

Rank of decreasing eigenvalue

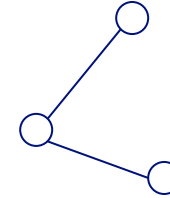
- A2: power law in the eigenvalues of the adjacency matrix ('eig()')

# Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
  - ➔ – Patterns: Degree; Triangles
  - Anomaly/fraud detection
  - Graph understanding
- Part#2: time-evolving graphs; tensors
- Conclusions

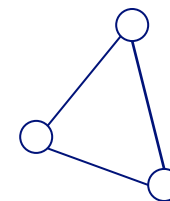


## Solution# S.3: Triangle ‘Laws’

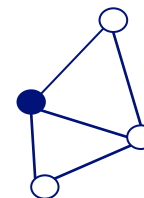


- Real social networks have a lot of triangles

## Solution# S.3: Triangle ‘Laws’



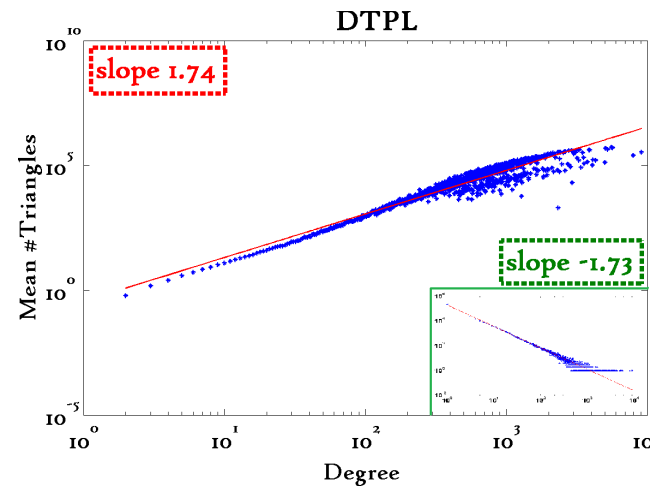
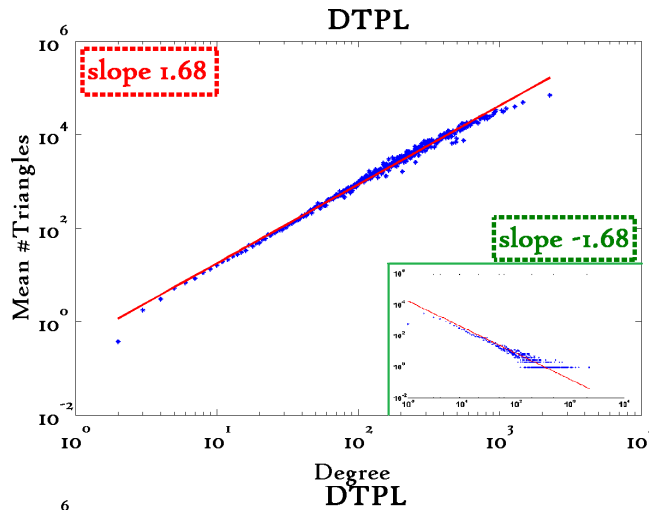
- Real social networks have a lot of triangles
  - Friends of friends are friends
- Any patterns?
  - 2x the friends, 2x the triangles ?



# Triangle Law: #S.3

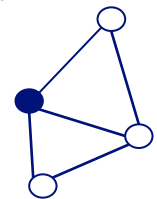
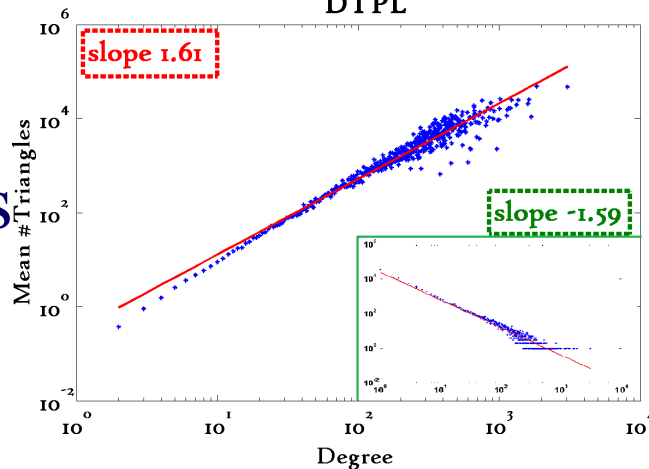
[Tsourakakis ICDM 2008]

Reuters



SN

Epinions



X-axis: degree  
 Y-axis: mean # triangles  
 $n$  friends  $\rightarrow \sim n^{1.6}$  triangles

# Triangle Law: Computations

[Tsourakakis ICDM 2008]



But: triangles are expensive to compute

(3-way join; several approx. algos) –  $O(d_{\max}^2)$

Q: Can we do that quickly?

A:



# Triangle Law: Computations

## [Tsourakakis ICDM 2008]



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Q: Can we do that quickly?

A: Yes!

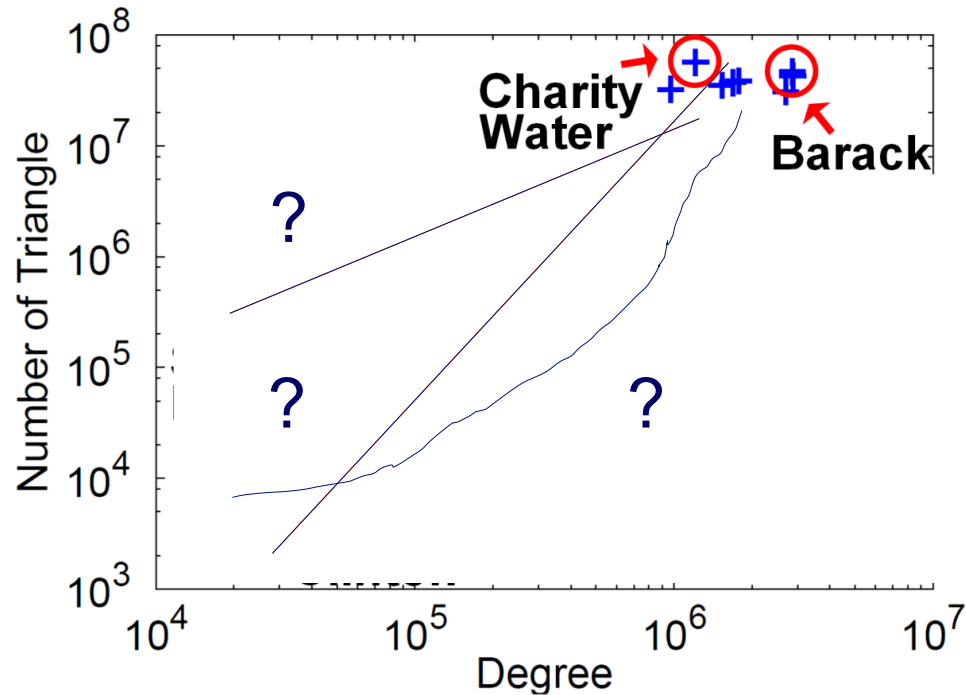
**#triangles =  $1/6 \text{ Sum} (\lambda_i^3)$**

(and, because of skewness (S2) ,

we only need the top few eigenvalues! -  $O(E)$

$$\mathbf{A} \mathbf{x} = \lambda \mathbf{x}$$

# Triangle counting for large graphs?

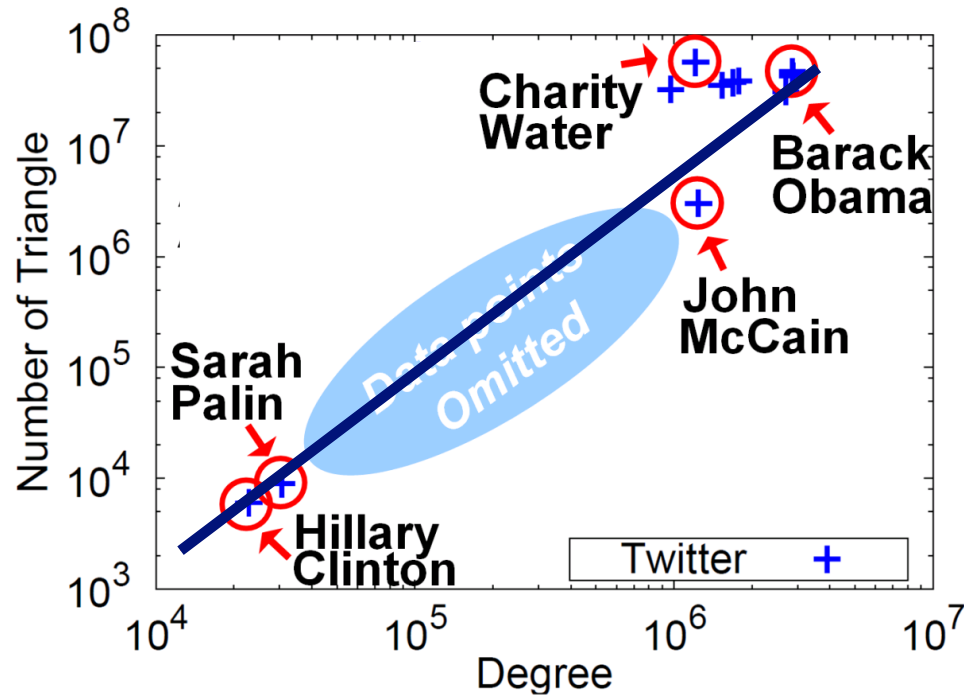


Anomalous nodes in Twitter (~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]



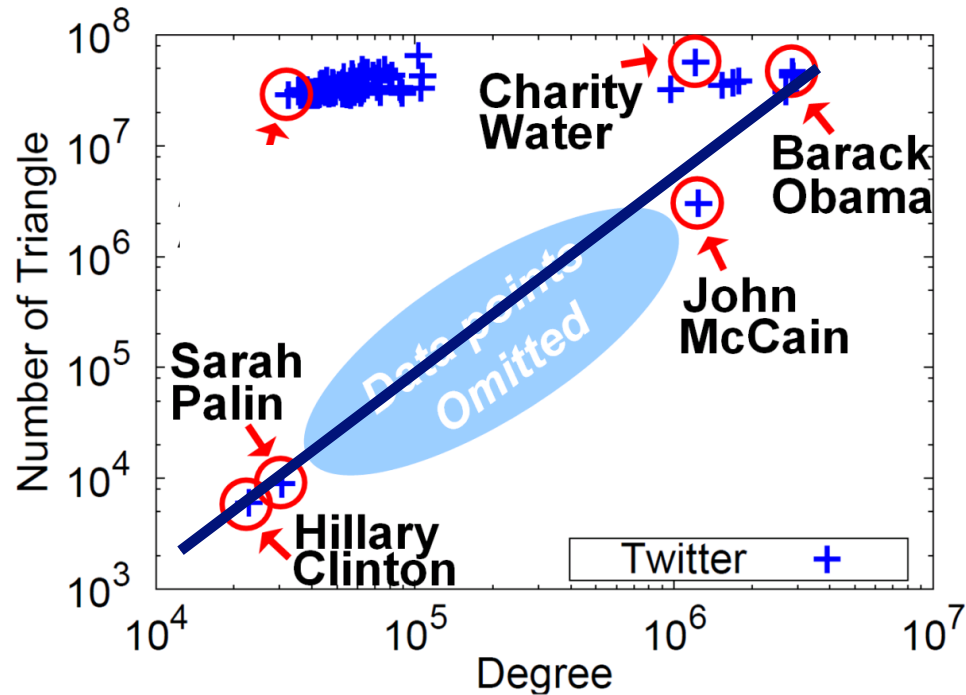
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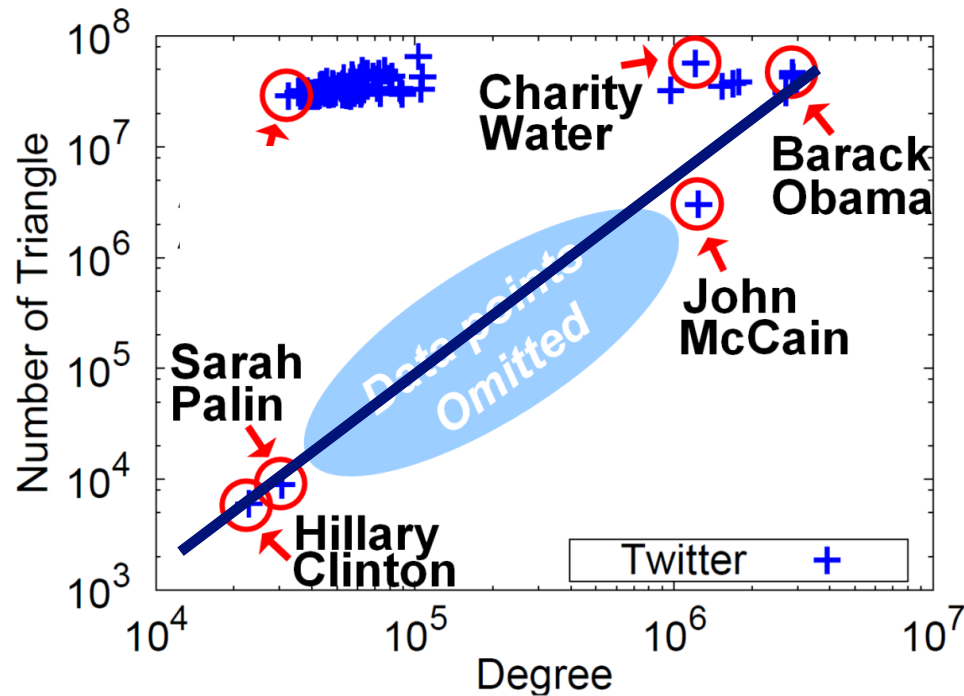
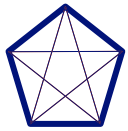
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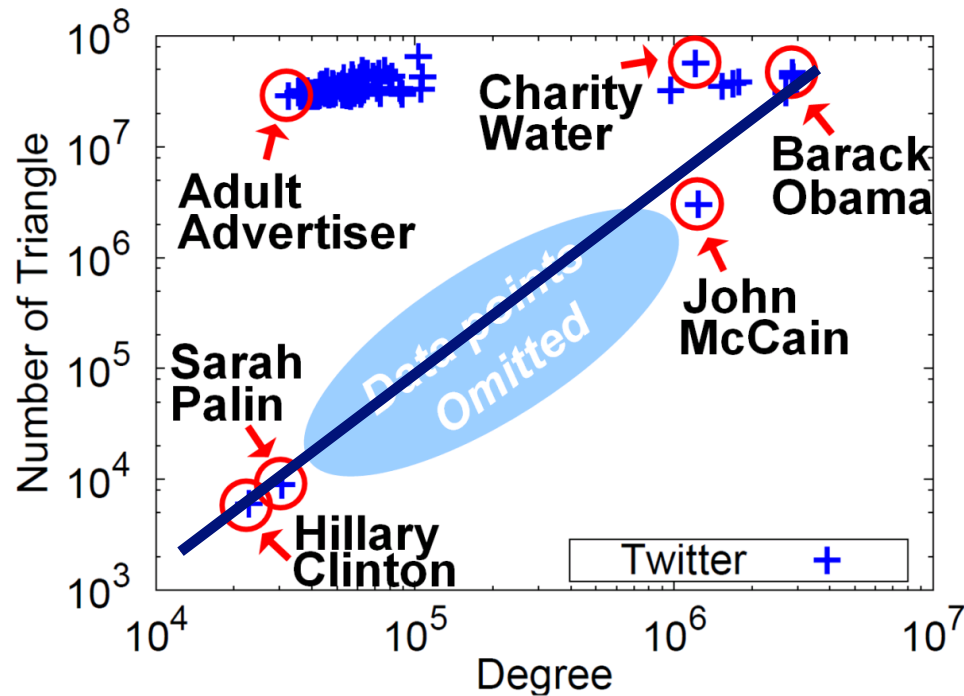
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# MORE Graph Patterns

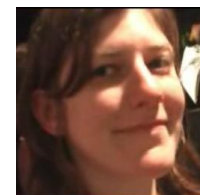
	Unweighted	Weighted
Static	<p> <b>L01.</b> Power-law degree distribution [Faloutsos et al. '99, Kleinberg et al. '99, Chakrabarti et al. '04, Newman '04]</p> <p> <b>L02.</b> Triangle Power Law (TPL) [Tsourakakis '08]</p> <p> <b>L03.</b> Eigenvalue Power Law (EPL) [Siganos et al. '03]</p> <p><b>L04.</b> Community structure [Flake et al. '02, Girvan and Newman '02]</p>	<p><b>L10.</b> Snapshot Power Law (SPL) [McGlohon et al. '08]</p>
Dynamic	<p><b>L05.</b> Densification Power Law (DPL) [Leskovec et al. '05]</p> <p><b>L06.</b> Small and shrinking diameter [Albert and Barabási '99, Leskovec et al. '05]</p> <p><b>L07.</b> Constant size 2<sup>nd</sup> and 3<sup>rd</sup> connected components [McGlohon et al. '08]</p> <p><b>L08.</b> Principal Eigenvalue Power Law (<math>\lambda_1</math>PL) [Akoglu et al. '08]</p> <p><b>L09.</b> Bursty/self-similar edge/weight additions [Gomez and Santonja '98, Gribble et al. '98, Crovella and</p>	<p><b>L11.</b> Weight Power Law (WPL) [McGlohon et al. '08]</p>

*RTG: A Recursive Realistic Graph Generator using Random Typing* Leman Akoglu and Christos Faloutsos. *PKDD'09*.

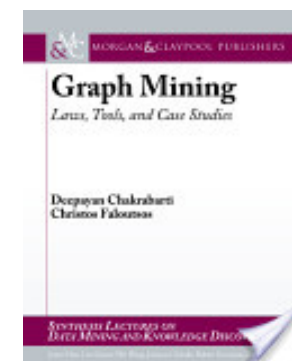
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- Mary McGlohon, Leman Akoglu, Christos Faloutsos. *Statistical Properties of Social Networks*. in "Social Network Data Analytics" (Ed.: Charu Aggarwal)



- Deepayan Chakrabarti and Christos Faloutsos, [\*Graph Mining: Laws, Tools, and Case Studies\*](#) Oct. 2012, Morgan Claypool.





# Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs



– Patterns



– Anomaly / fraud detection

- CopyCatch
- Spectral methods ('fBox')
- Belief Propagation

Patterns



anomalies

- Part#2: time-evolving graphs; tensors
- Conclusions

# Fraud

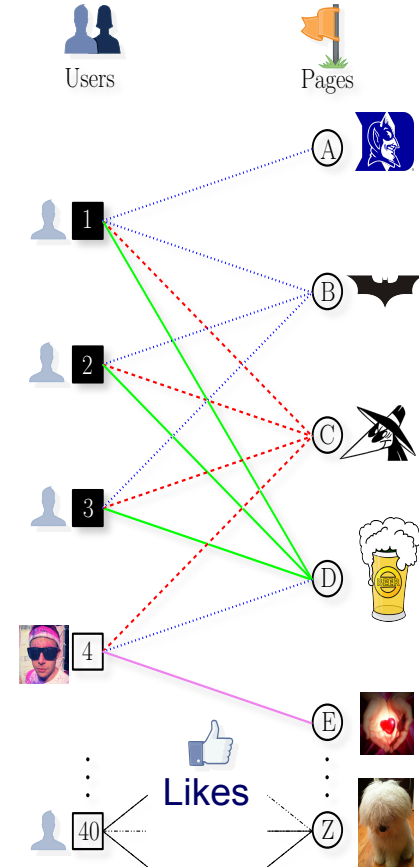
- Given
  - Who ‘likes’ what page, and when
- Find
  - Suspicious users and suspicious products



**CopyCatch: Stopping Group Attacks by Spotting Lockstep Behavior in Social Networks**, Alex Beutel, Wanhong Xu, Venkatesan Guruswami, Christopher Palow, Christos Faloutsos *WWW, 2013*.

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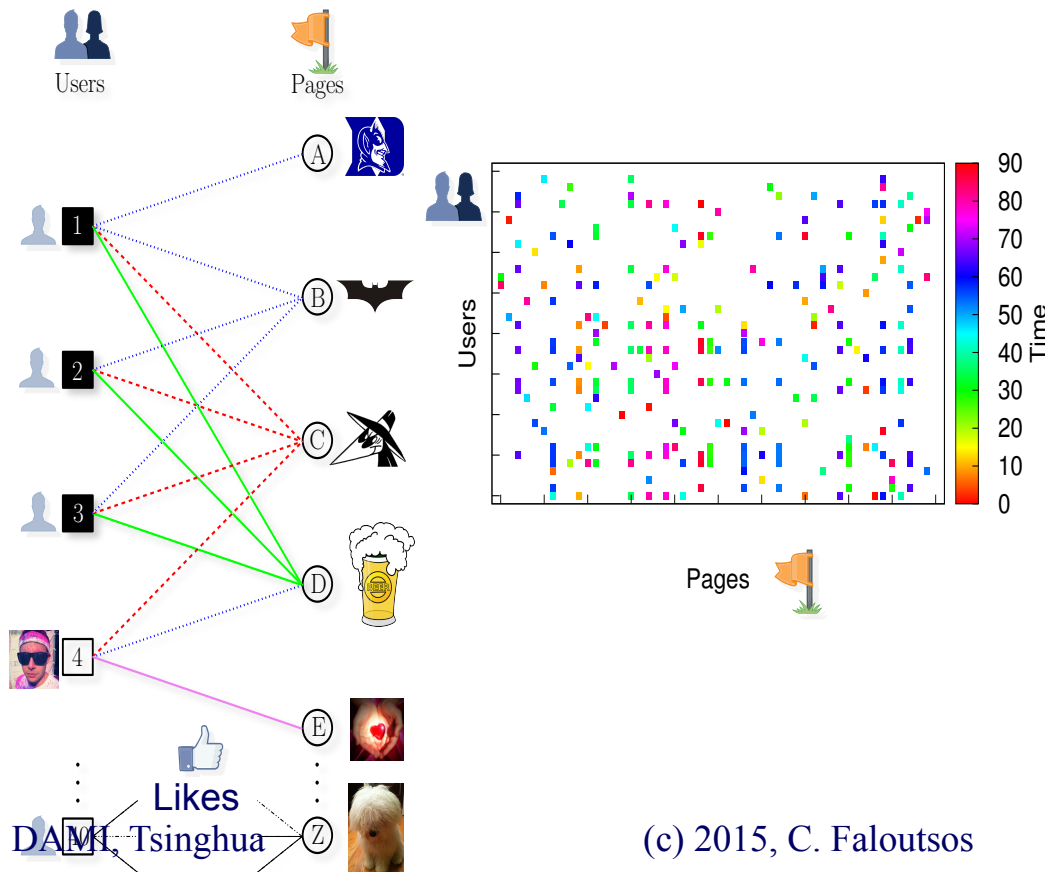
# Graph Patterns and Lockstep Behavior

Our intuition

## Behavior



- Lockstep behavior: Same Likes, same time



Users: 1, 2, 3, 4  
 Pages: A, B, C, D, E  
 Likes: DAM, Tsinghua, Z

(c) 2015, C. Faloutsos



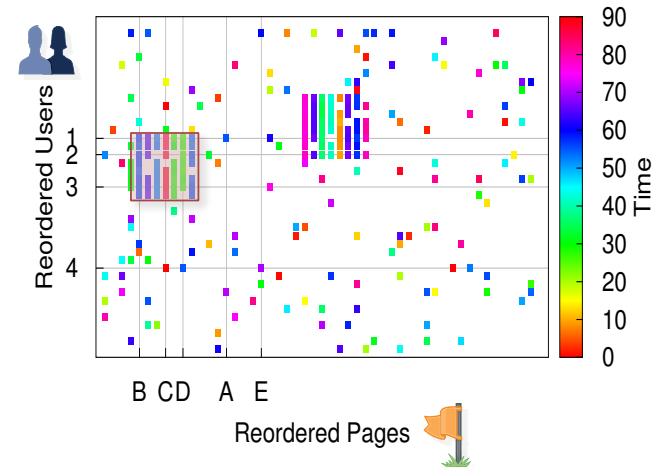
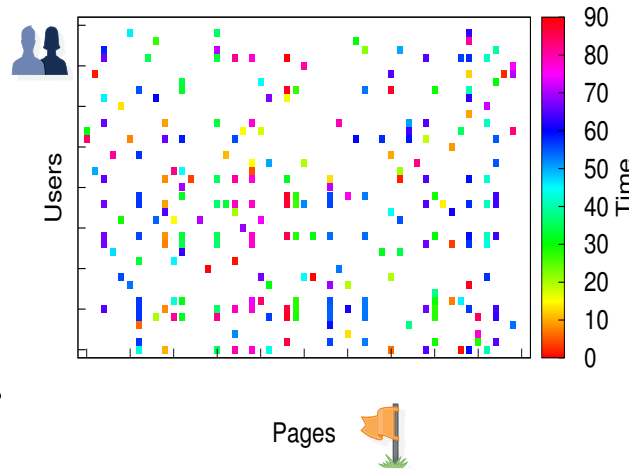
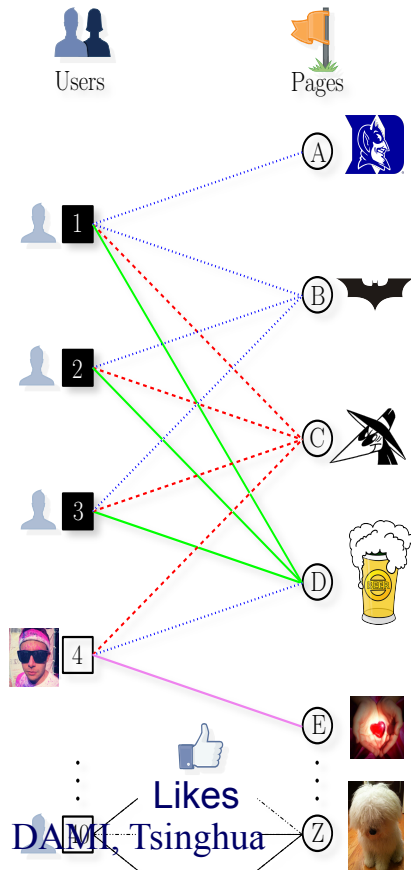
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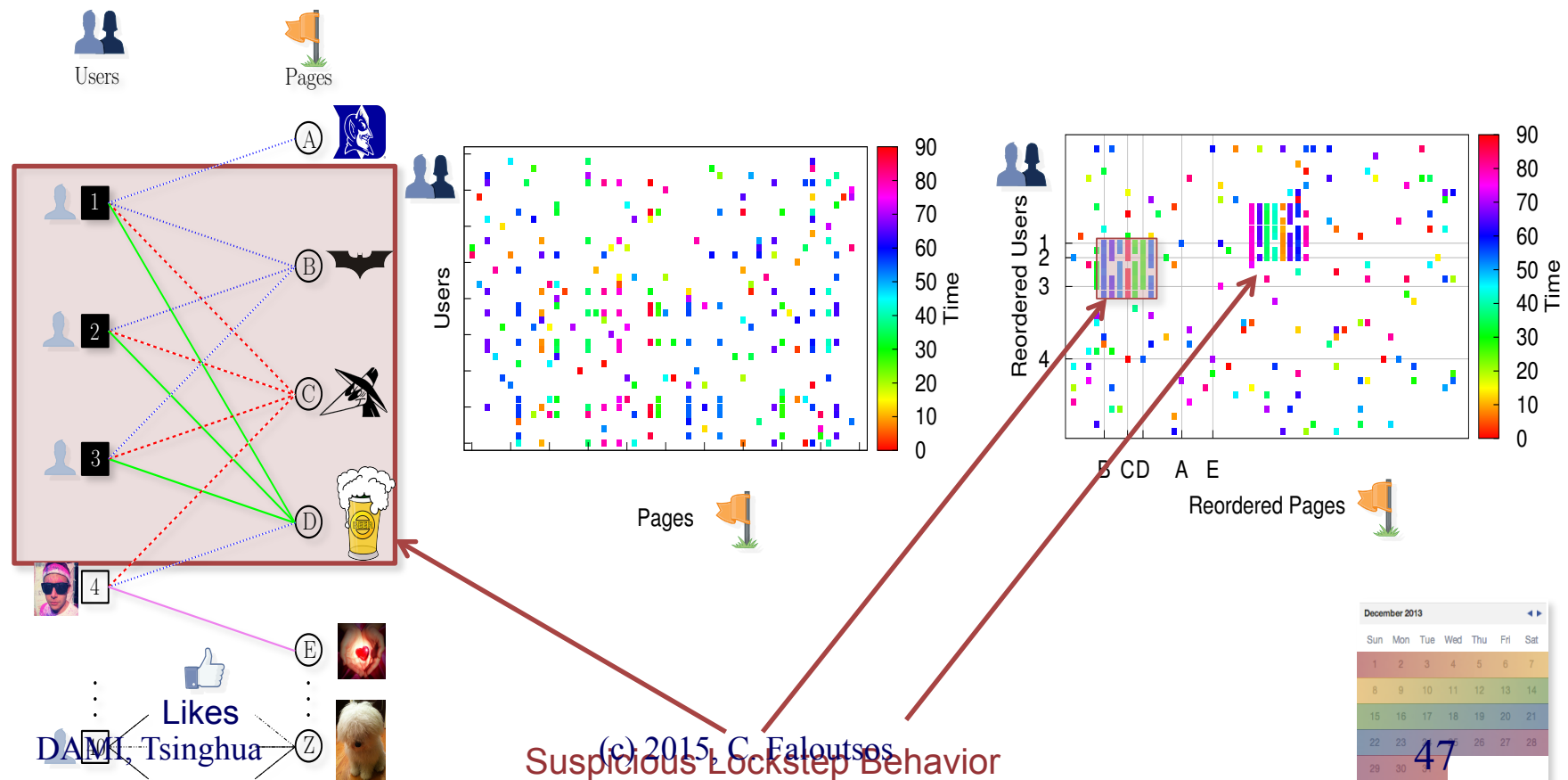
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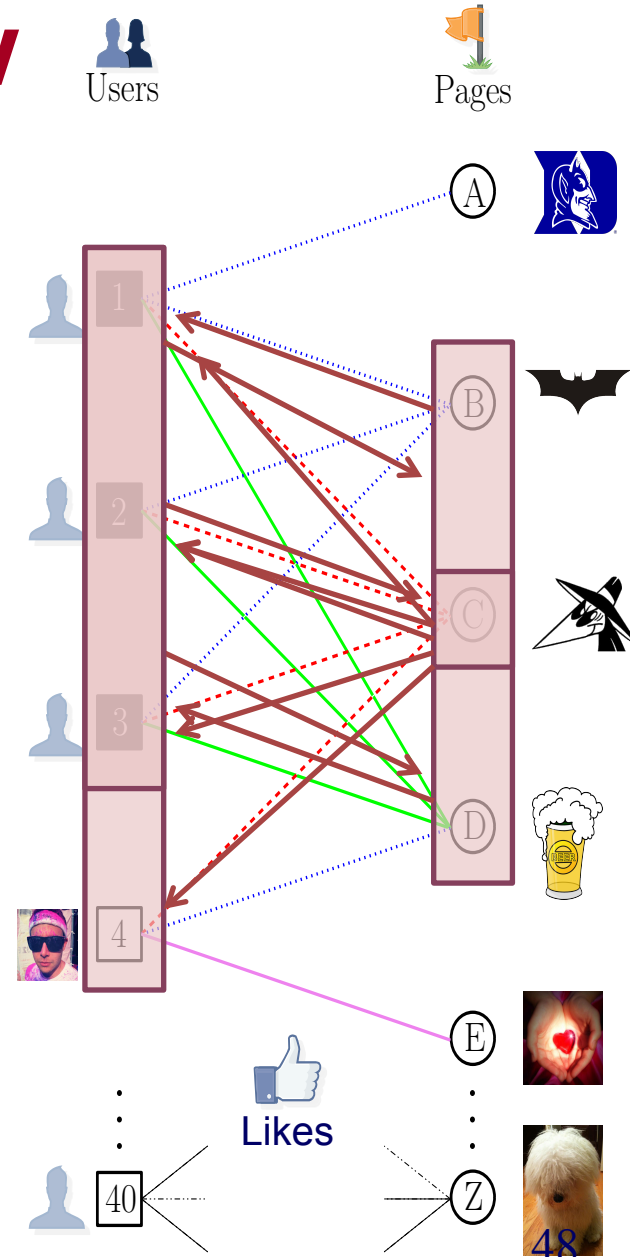
- Lockstep behavior: Same Likes, same time



(c) 2015, C. Faloutsos  
Suspicious Lockstep Behavior

# MapReduce Overview

- Use Hadoop to search for many clusters in parallel:
  - Start with randomly seed
  - Update set of Pages and center Like times for each cluster
  - Repeat until convergence



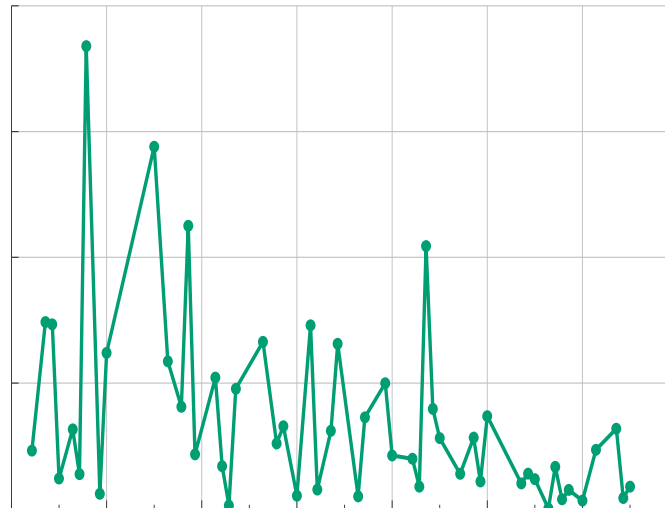
December 2013						
Sun	Mon	Tue	Wed	Thu	Fri	Sat
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28

# Deployment at Facebook

- *CopyCatch* runs regularly (along with many other security mechanisms, and a large Site Integrity team)

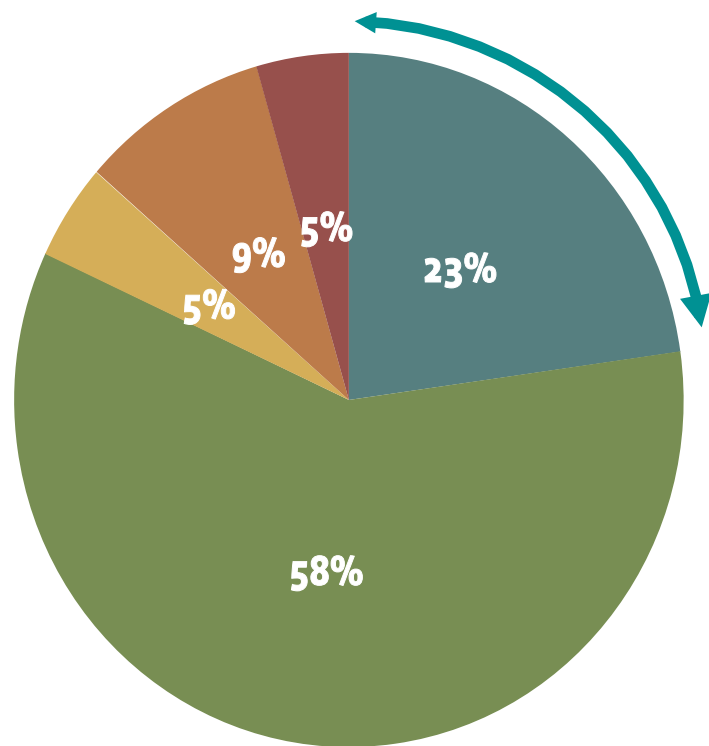
3 months of *CopyCatch* @ Facebook

#users  
caught



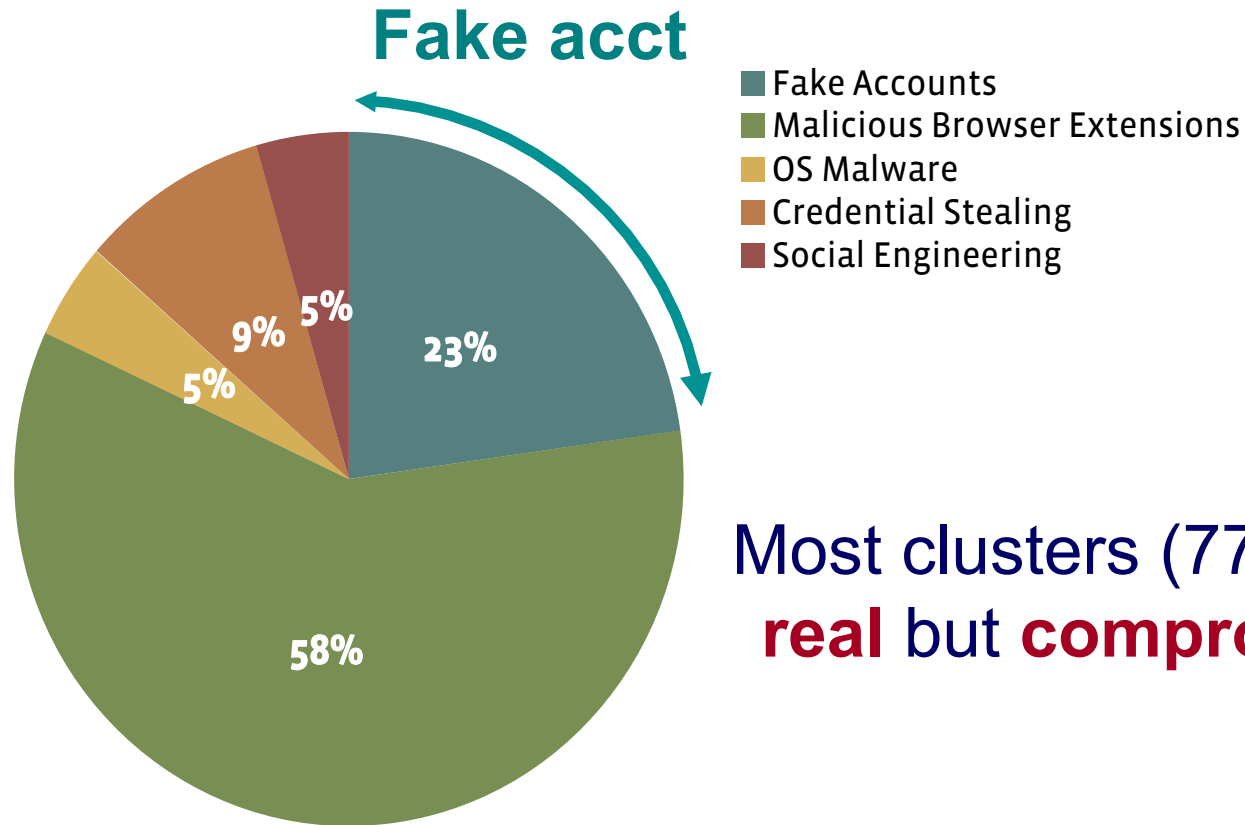


# Deployment at Facebook



Manually labeled 22 randomly selected *clusters* from February 2013

# Deployment at Facebook

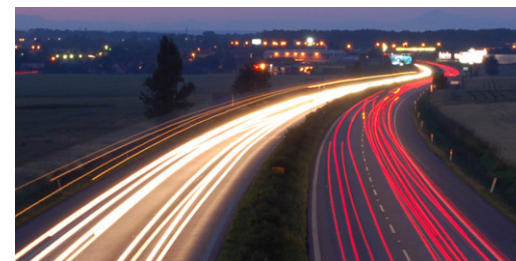


Most clusters (77%) come from **real but compromised** users

Manually labeled 22 randomly selected *clusters* from February 2013

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  - Patterns
  - Anomaly / fraud detection
    - CopyCatch
    - Spectral methods ('fBox')
    - Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions



# Problem: Social Network Link Fraud

Target: find “stealthy” attackers missed by other algorithms

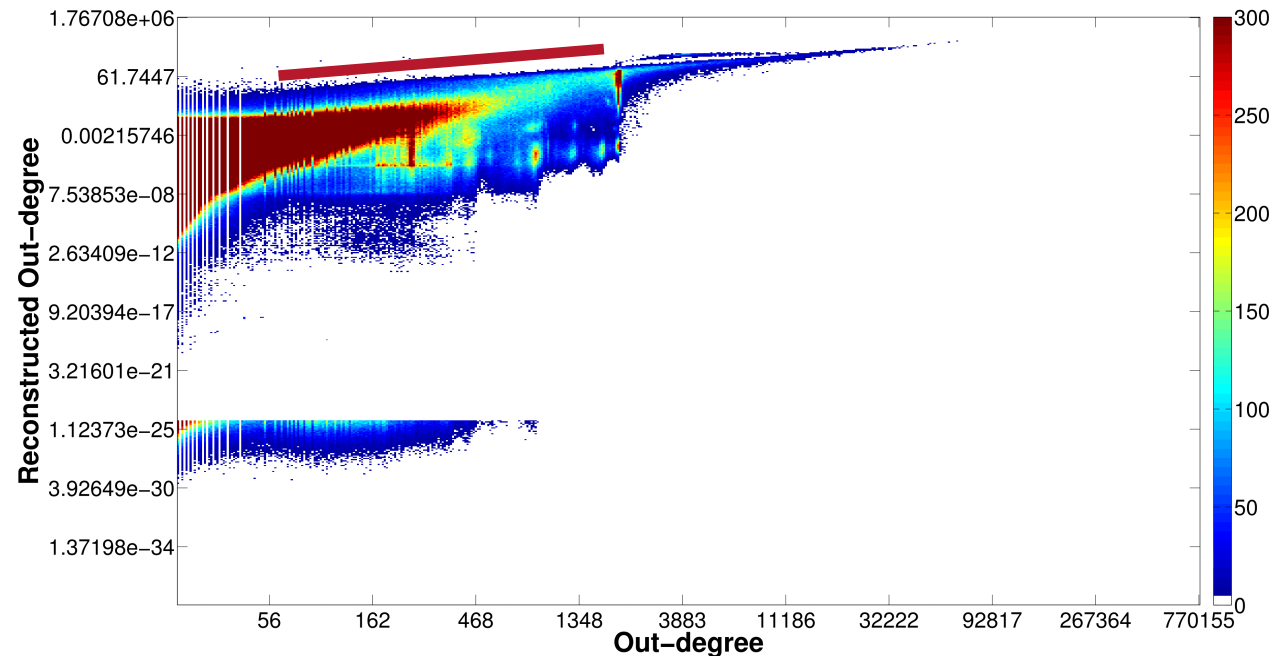


Clique

41.7M nodes  
1.5B edges



Bipartite  
core



# Problem: Social Network Link Fraud

Target: find “stealthy” attackers missed by other algorithms



Lekan Olawole Lowe @loweinc

26 Jul 09

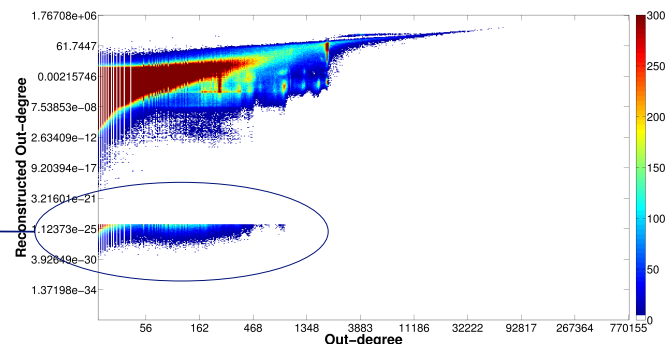
Sign up free and Get 400 followers a day using <http://tweeteradder.com>



Lekan Olawole Lowe @loweinc

26 Jul 09

Get 400 followers a day using <http://www.tweeterfollow.com>



**Takeaway:** use *reconstruction error* between true/latent representation!



Neil Shah, Alex Beutel, Brian Gallagher and Christos Faloutsos. *Spotting Suspicious Link Behavior with fBox: An Adversarial Perspective*. ICDM 2014, Shenzhen, China.

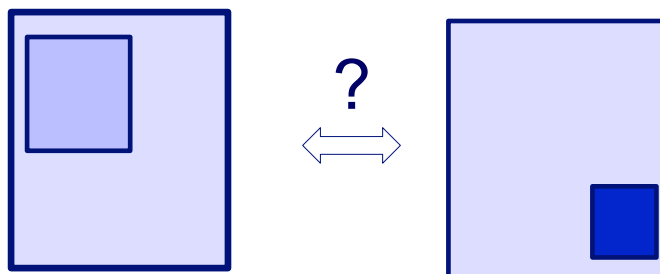
# Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
  - Patterns
  - Anomaly / fraud detection
    - CopyCatch
    - Spectral methods ('fBox', **suspiciousness**)
    - Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions

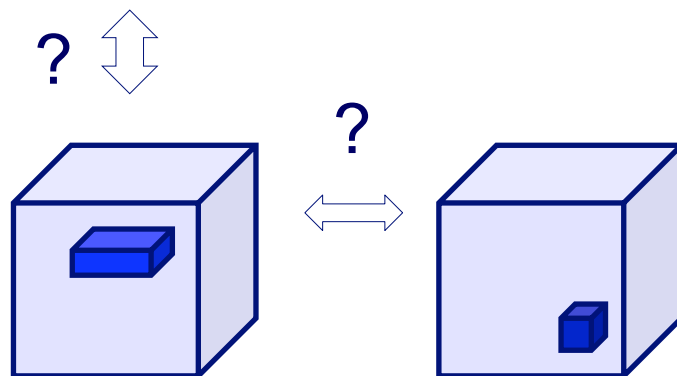


# Suspicious Patterns in Event Data

2-modes



$n$ -modes



A General Suspiciousness Metric for Dense Blocks in Multimodal Data, Meng Jiang, Alex Beutel, Peng Cui, Bryan Hooi, Shiqiang Yang, and Christos Faloutsos, *ICDM*, 2015.

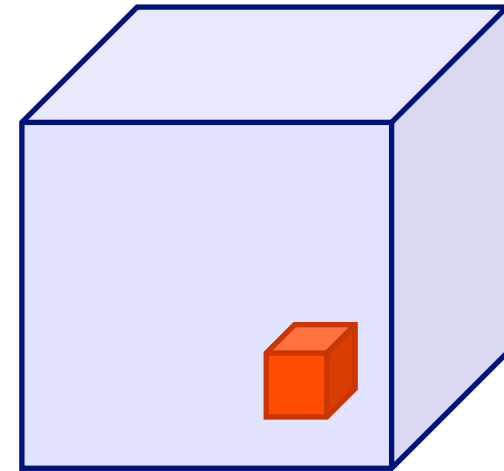
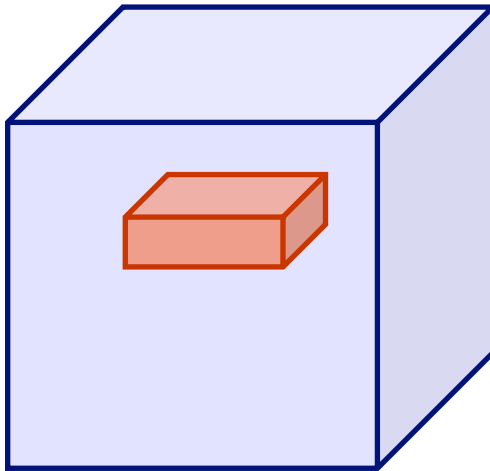
# Suspicious Patterns in Event Data

Which is more suspicious?

20,000 Users  
Retweeting same 20 tweets  
6 times each  
All in 10 hours

↔  
↔  
vs.  
↔

225 Users  
Retweeting same 1 tweet  
15 times each  
All in 3 hours  
All from 2 IP addresses



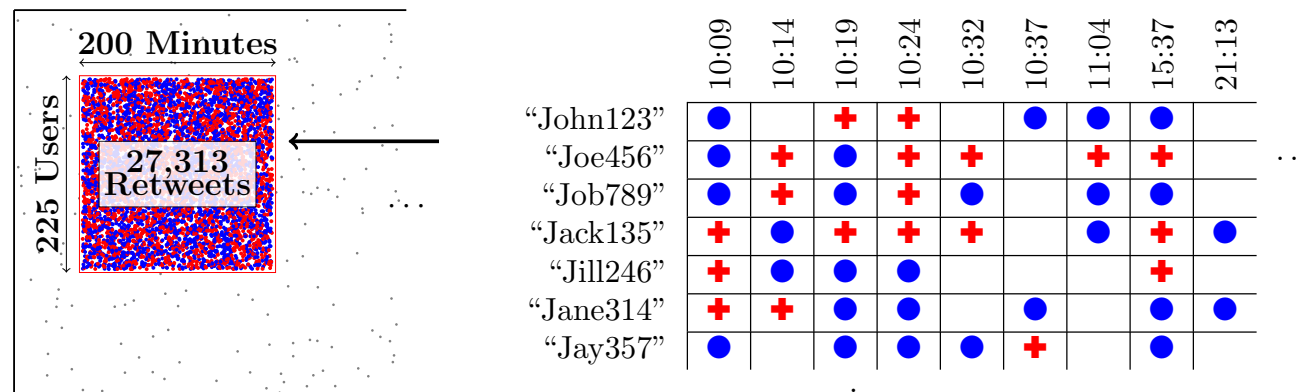
DAMI,

Answer: volume \*  $D_{KL}(p || p_{background})$

57



# Suspicious Patterns in Event Data

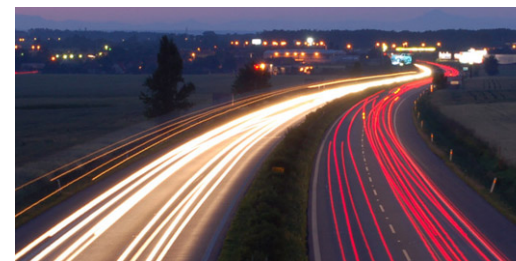


Retweeting: "Galaxy Note Dream Project:  
Happy Happy Life Traveling the World"

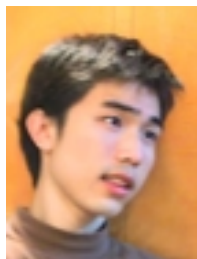
	#	User $\times$ tweet $\times$ IP $\times$ minute	Mass $c$	Suspiciousness
CROSSPOT	1	$14 \times 1 \times 2 \times 1,114$	41,396	1,239,865
	2	$225 \times 1 \times 2 \times 200$	27,313	777,781
	3	$8 \times 2 \times 4 \times 1,872$	17,701	491,323
HOSVD	1	$24 \times 6 \times 11 \times 439$	3,582	131,113
	2	$18 \times 4 \times 5 \times 223$	1,942	74,087
	3	$14 \times 2 \times 1 \times 265$	9,061	381,211

# Roadmap

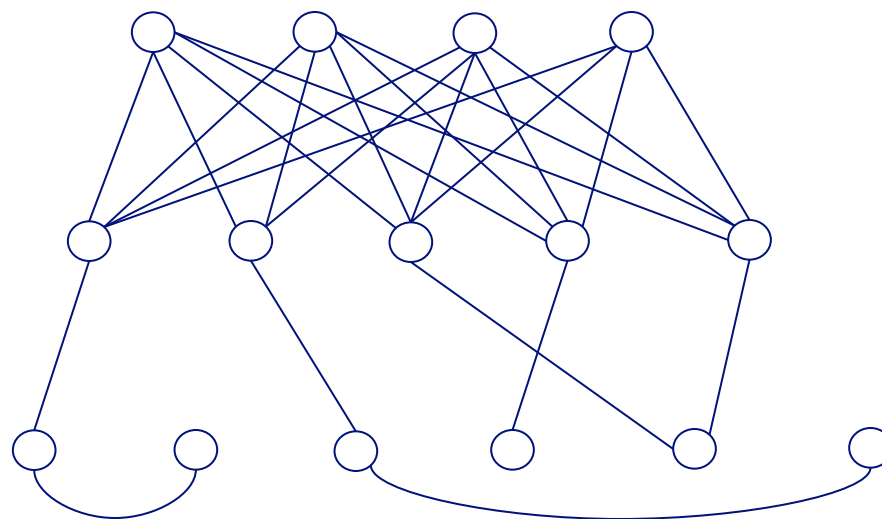
- Introduction – Motivation
- Part#1: Patterns in graphs
  - Patterns
  - Anomaly / fraud detection
    - CopyCatch
    - Spectral methods ('fBox')
    - Belief Propagation
- • Part#2: time-evolving graphs; tensors
- Conclusions



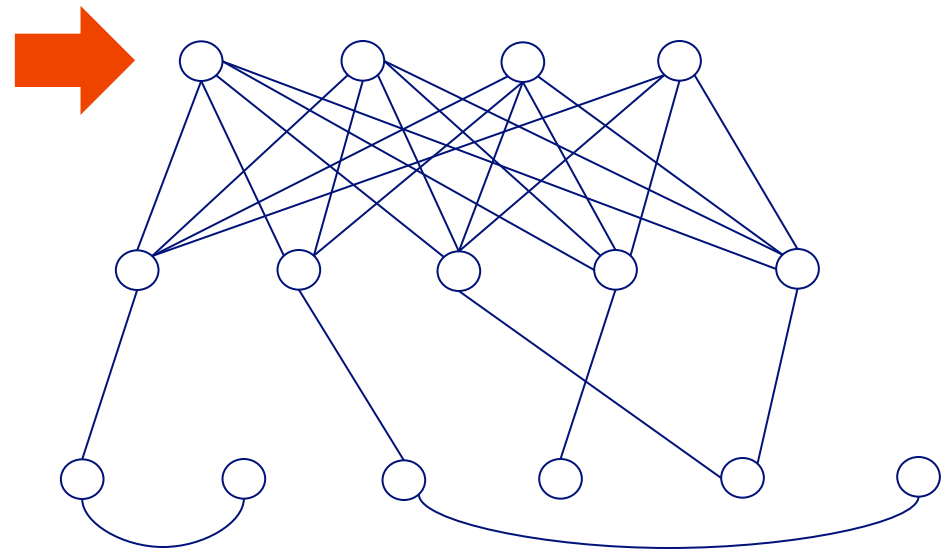
# E-bay Fraud detection



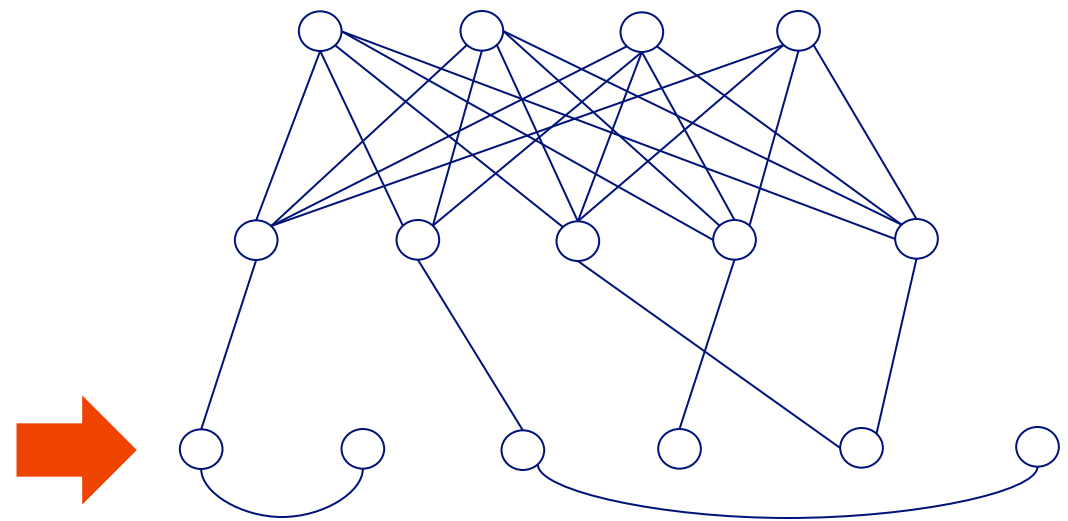
w/ Polo Chau &  
Shashank Pandit, CMU  
[www'07]



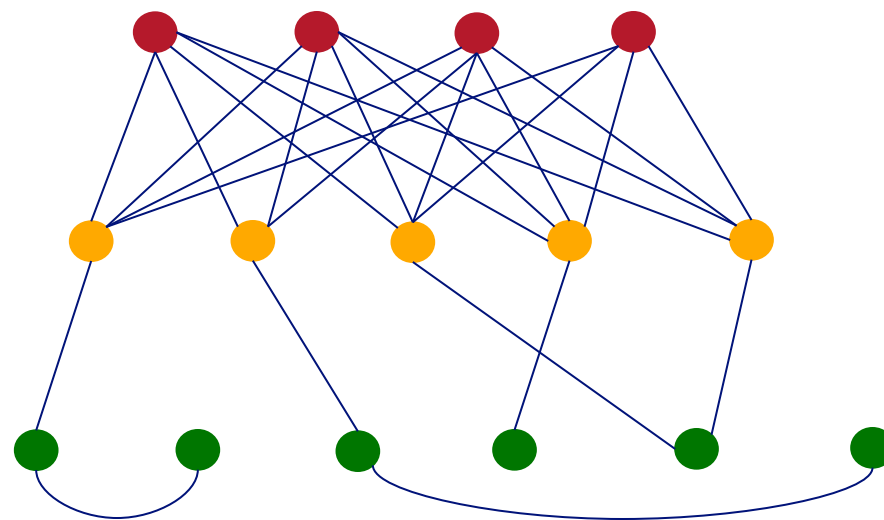
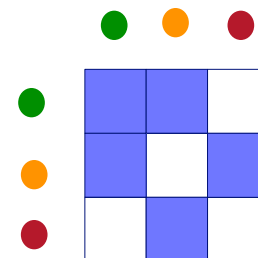
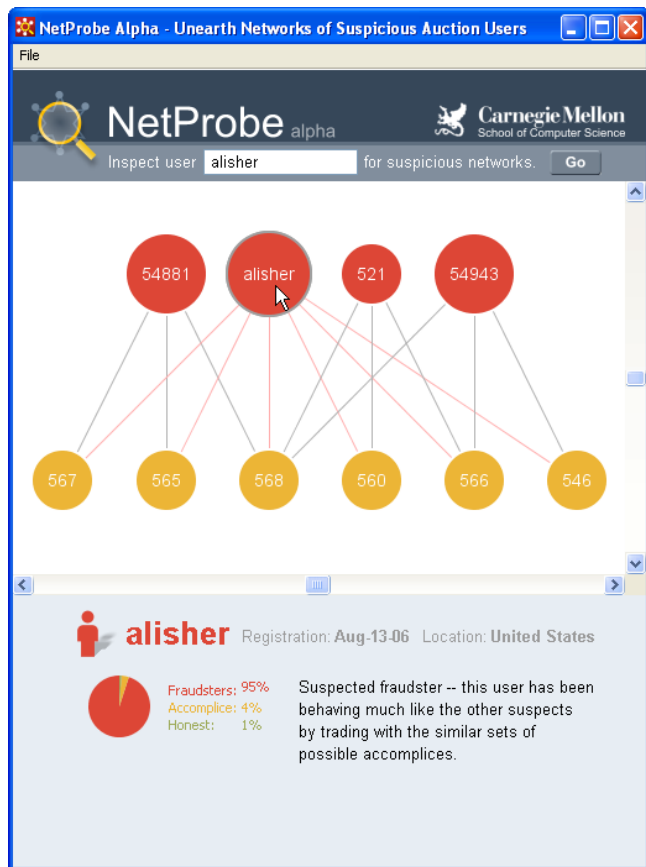
# E-bay Fraud detection



# E-bay Fraud detection



# E-bay Fraud detection - NetProbe



# Popular press



The Washington Post

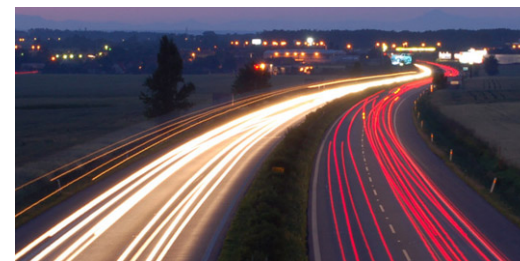
Los Angeles Times

And less desirable attention:

- E-mail from ‘Belgium police’ (‘copy of your code?’)

# Roadmap

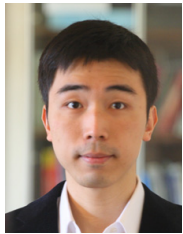
- Introduction – Motivation
- Part#1: Patterns in graphs
  - Patterns
  - Anomaly / fraud detection
    - CopyCatch
    - Spectral methods ('fBox')
    - Belief Propagation; antivirus app
- Part#2: time-evolving graphs; tensors
- Conclusions





# Polonium: Tera-Scale Graph Mining and Inference for Malware Detection

*SDM 2011, Mesa, Arizona*



**Polo Chau**

Machine Learning Dept



**Carey Nachenberg**

Vice President & Fellow



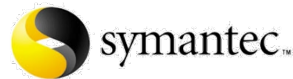
**Jeffrey Wilhelm**

Principal Software Engineer



**Adam Wright**

Software Engineer



**Prof. Christos Faloutsos**

Computer Science Dept

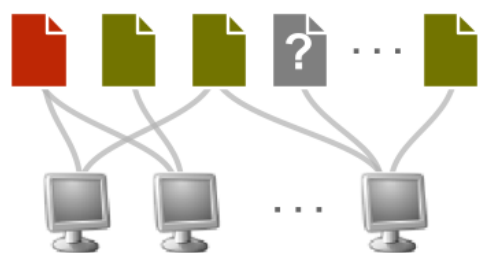
# Polonium: The Data



60+ terabytes of data *anonymously* contributed by participants of worldwide *Norton Community Watch* program

50+ million machines

900+ million executable files



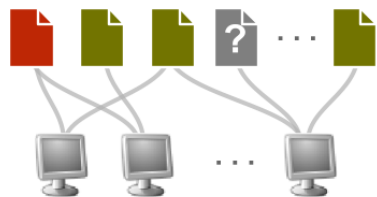
Constructed a machine-file bipartite graph (0.2 TB+)

1 billion nodes (machines and files)

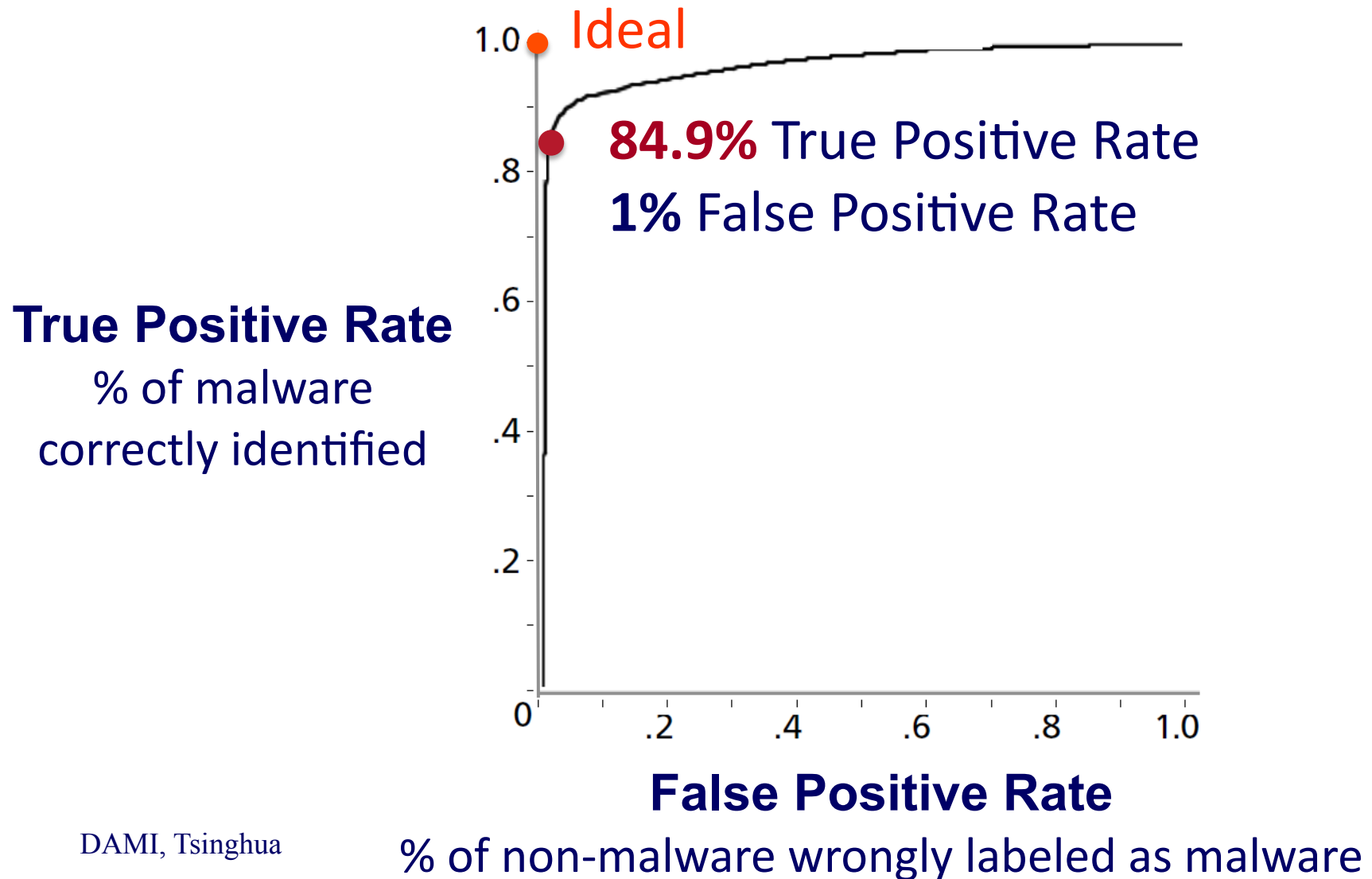
37 billion edges

## Polonium: Key Ideas

- Use **Belief Propagation** to propagate domain knowledge in machine-file graph to detect malware
- Use “**guilt-by-association**” (i.e., homophily)
  - E.g., files that appear on machines with many bad files are more likely to be bad
- **Scalability**: handles 37 billion-edge graph



# Polonium: One-Interaction Results



# Summary of Part#1

- \*many\* patterns in real graphs
  - Power-laws everywhere
  - Gaussian trap
    - Avg  $\ll$  Max
  - Long (and growing) list of tools for anomaly/fraud detection



Patterns



anomalies

# Roadmap

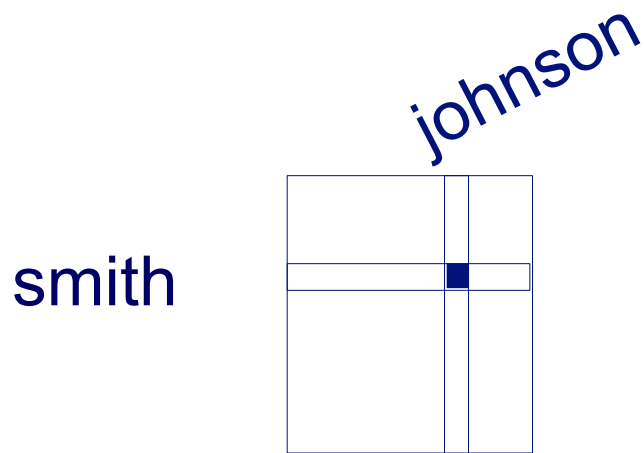
- Introduction – Motivation
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
  - ➔ – P2.1: time-evolving graphs
  - P2.2: with side information (‘coupled’ M.T.F.)
  - (Speed)
- Conclusions



# Part 2: Time evolving graphs; tensors

# Graphs over time -> tensors!

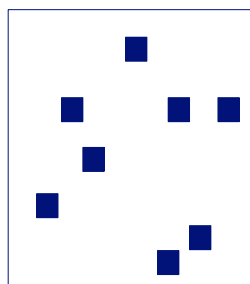
- Problem #2.1:
  - Given who calls whom, and when
  - Find patterns / anomalies





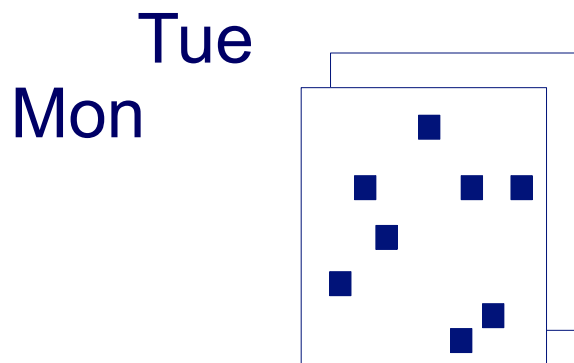
# Graphs over time $\rightarrow$ tensors!

- Problem #2.1:
  - Given who calls whom, and when
  - Find patterns / anomalies



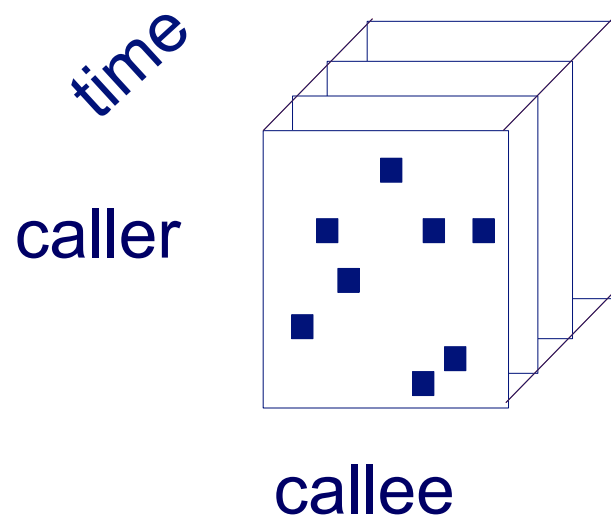
# Graphs over time -> tensors!

- Problem #2.1:
  - Given who calls whom, and when
  - Find patterns / anomalies



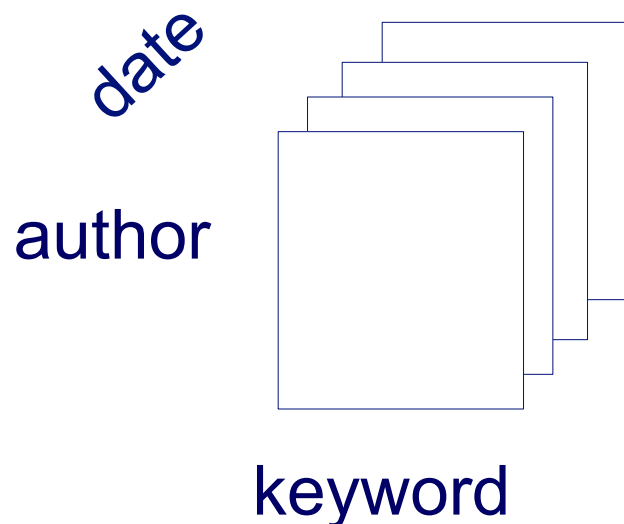
# Graphs over time -> tensors!

- Problem #2.1:
  - Given who calls whom, and when
  - Find patterns / anomalies



# Graphs over time -> tensors!

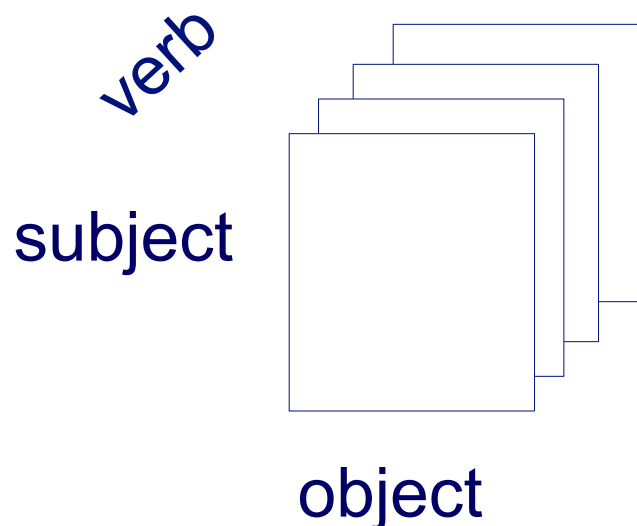
- Problem #2.1':
  - Given author-keyword-date
  - Find patterns / anomalies



**MANY** more settings,  
with  $>2$  'modes'

# Graphs over time -> tensors!

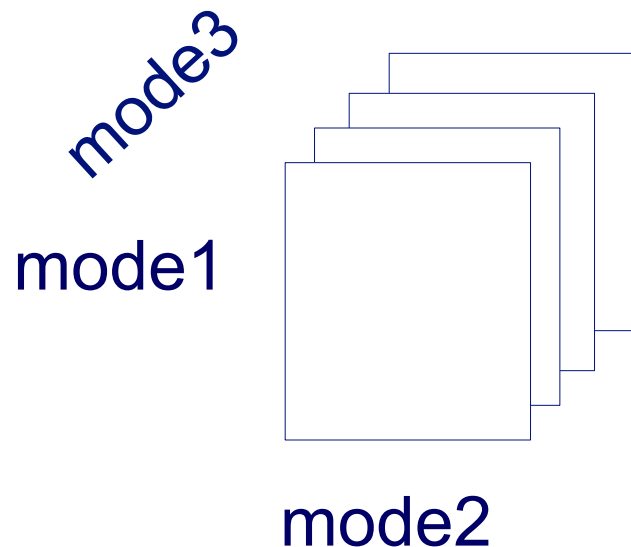
- Problem #2.1’’:
  - Given subject – verb – object facts
  - Find patterns / anomalies



**MANY** more settings,  
with  $>2$  ‘modes’

# Graphs over time -> tensors!

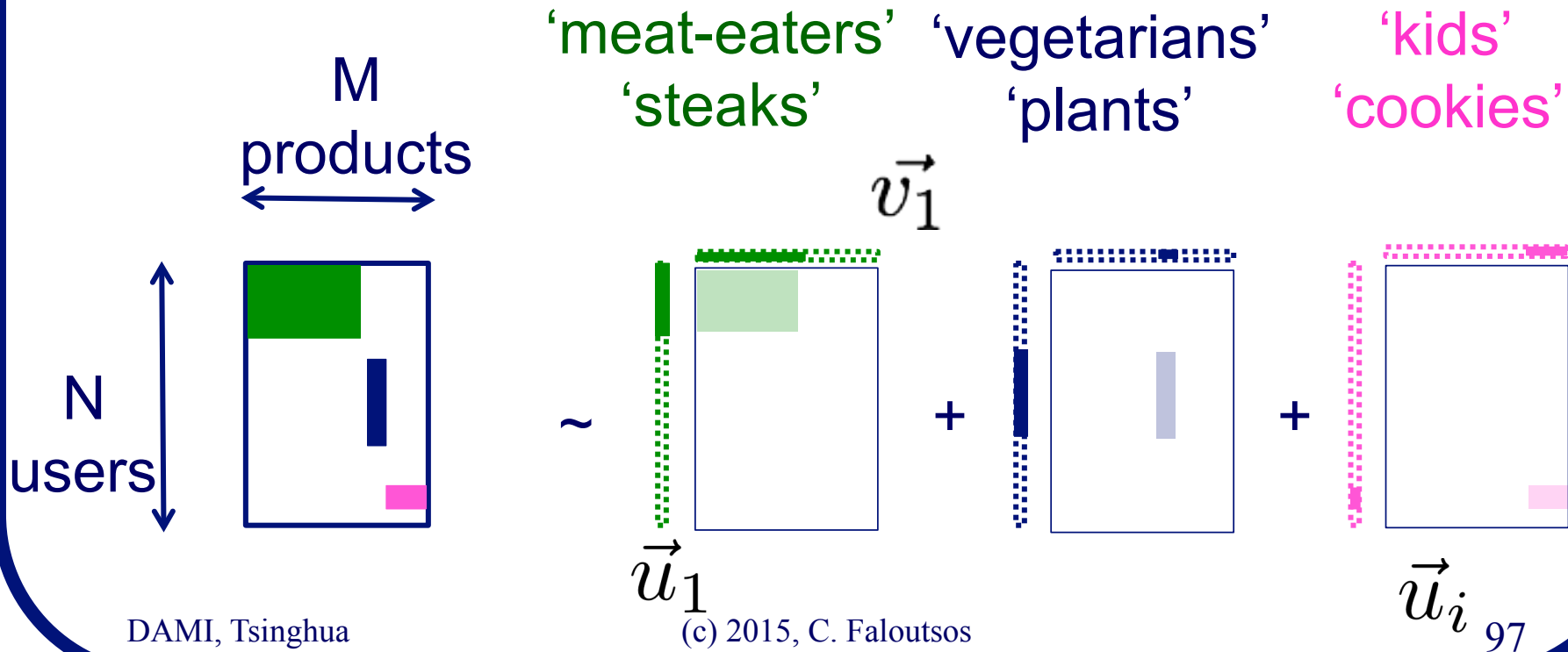
- Problem #2.1''':
  - Given <triplets>
  - Find patterns / anomalies



**MANY** more settings,  
with >2 'modes'  
(and 4, 5, etc modes)

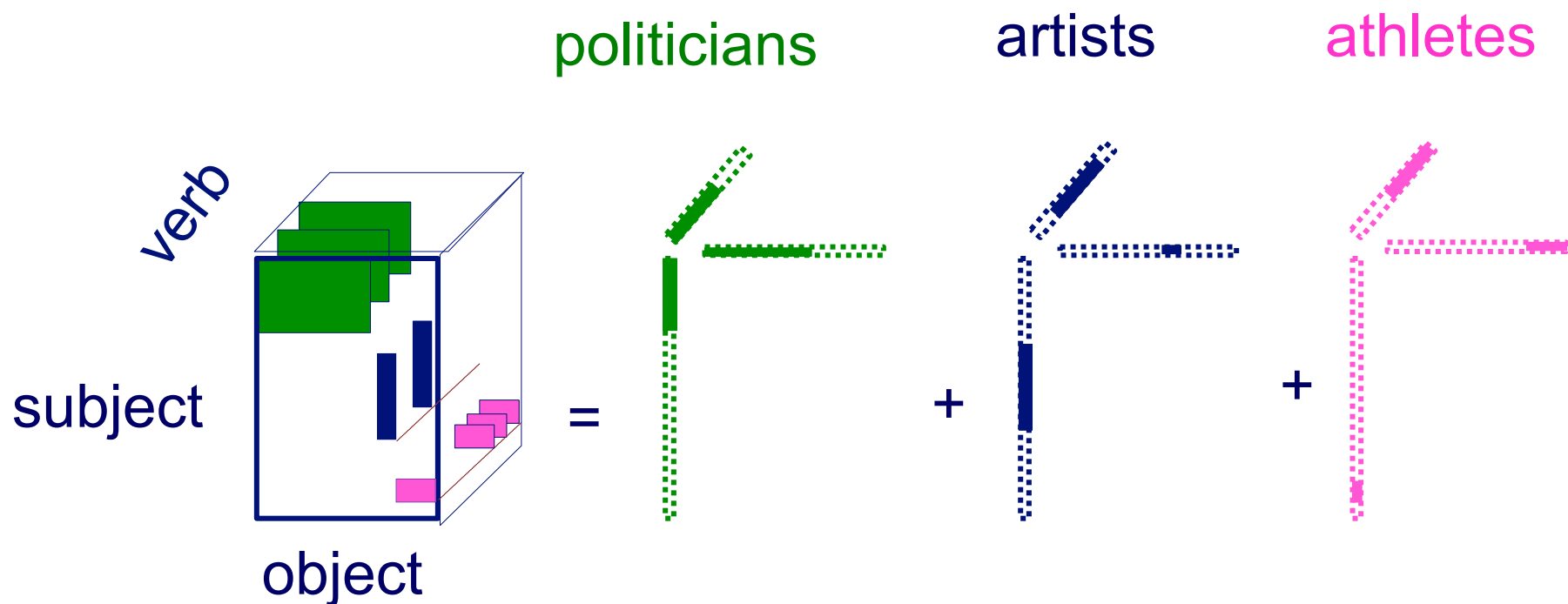
# Answer to both: tensor factorization

- Recall: (SVD) matrix factorization: finds blocks



# Answer to both: tensor factorization

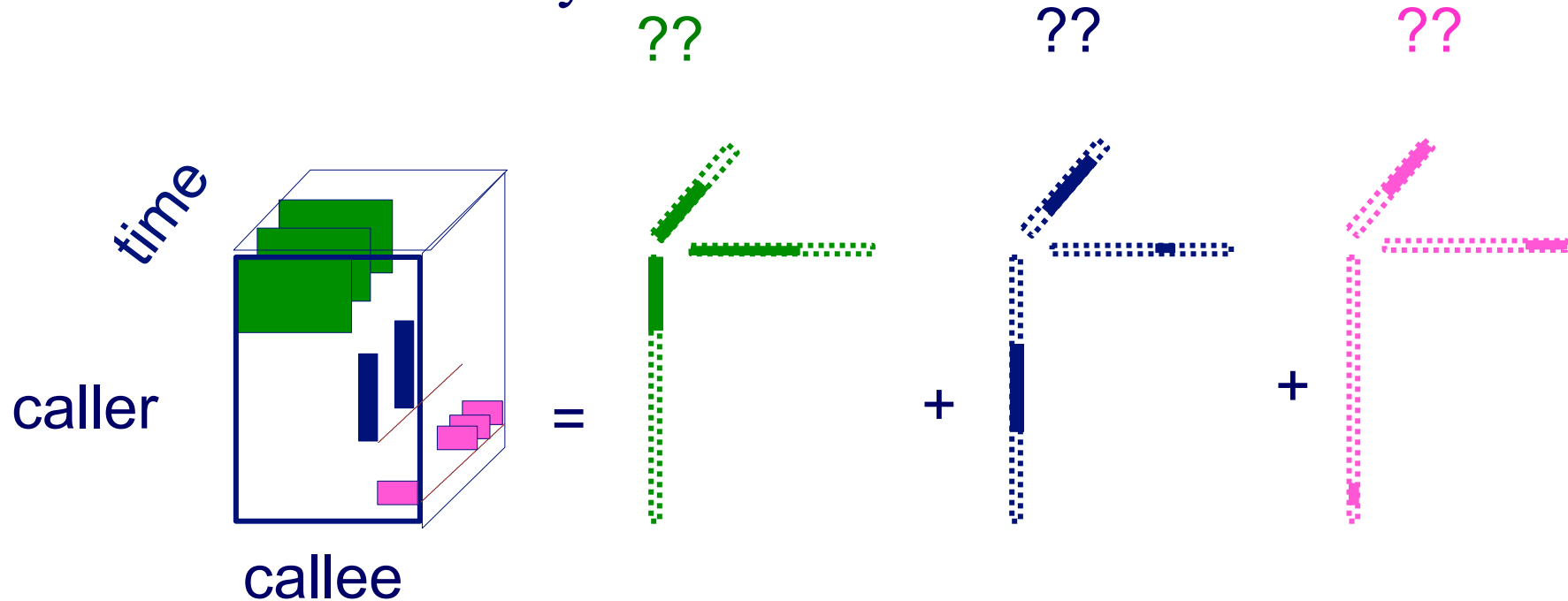
- PARAFAC decomposition



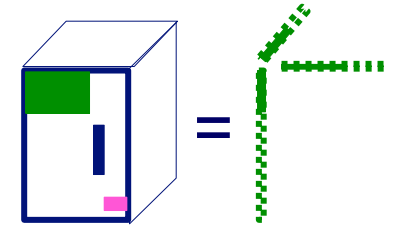


# Answer: tensor factorization

- PARAFAC decomposition
- Results for who-calls-whom-when
  - 4M x 15 days

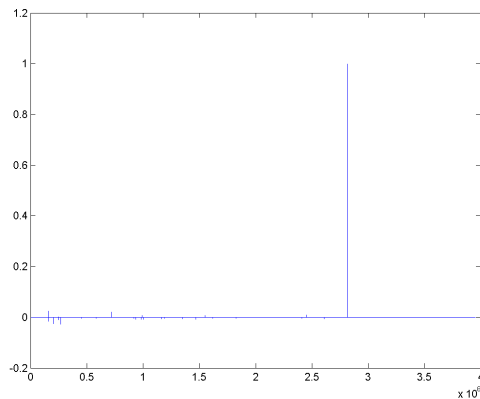


# Anomaly detection in time-evolving graphs

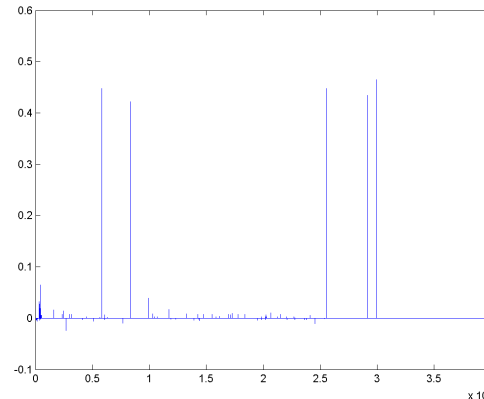


- Anomalous communities in phone call data:
  - European country, 4M clients, data over 2 weeks

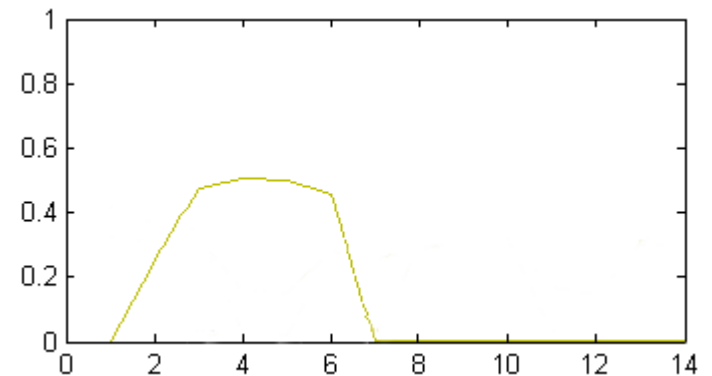
1 caller



5 receivers

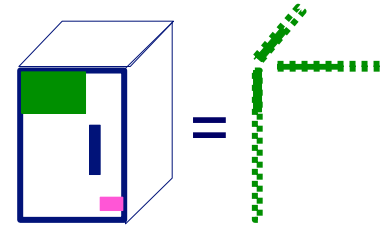


4 days of activity



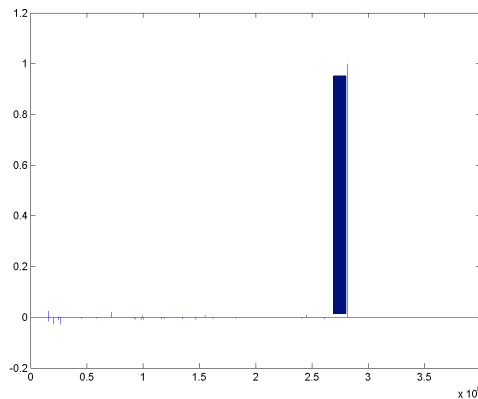
~200 calls to EACH receiver on EACH day!

# Anomaly detection in time-evolving graphs

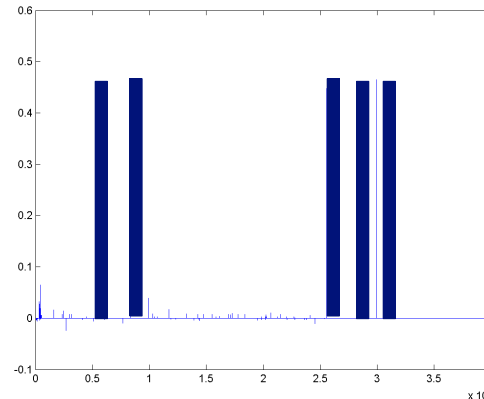


- Anomalous communities in phone call data:
  - European country, 4M clients, data over 2 weeks

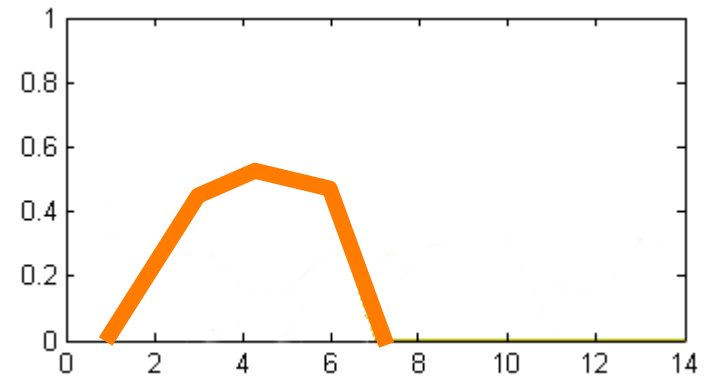
1 caller



5 receivers

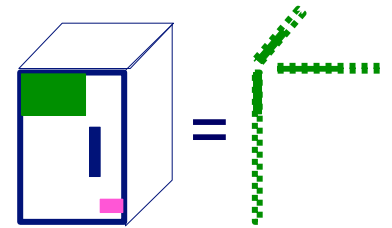


4 days of activity



~200 calls to EACH receiver on EACH day!

# Anomaly detection in time-evolving graphs



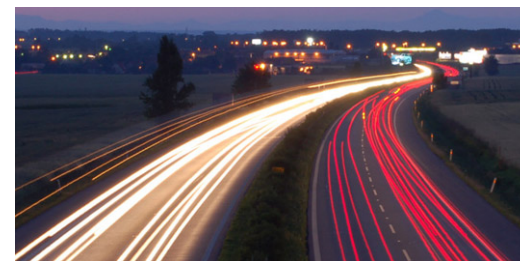
- Anomalous communities in phone call data:
  - European country, 4M clients, data over 2 weeks



**Miguel Araujo, Spiros Papadimitriou, Stephan Günnemann, Christos Faloutsos, Prithwish Basu, Ananthram Swami, Evangelos Papalexakis, Danai Koutra. *Com2: Fast Automatic Discovery of Temporal (Comet) Communities.* PAKDD 2014, Tainan, Taiwan.**

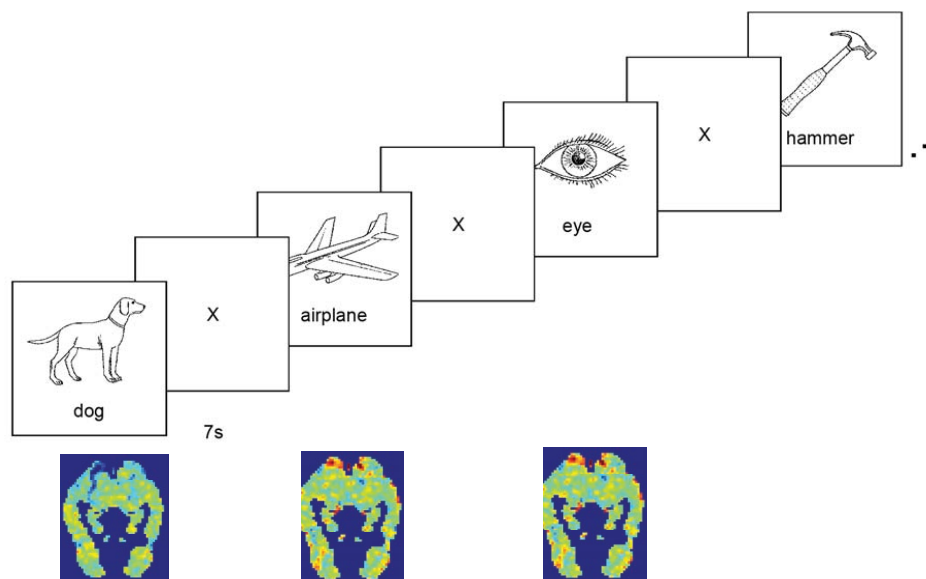
# Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
  - P2.1: Discoveries @ phonecall network
  - P2.2: Discoveries in neuro-semantic
  - (Speed)
- Conclusions



# Neuro-semantic

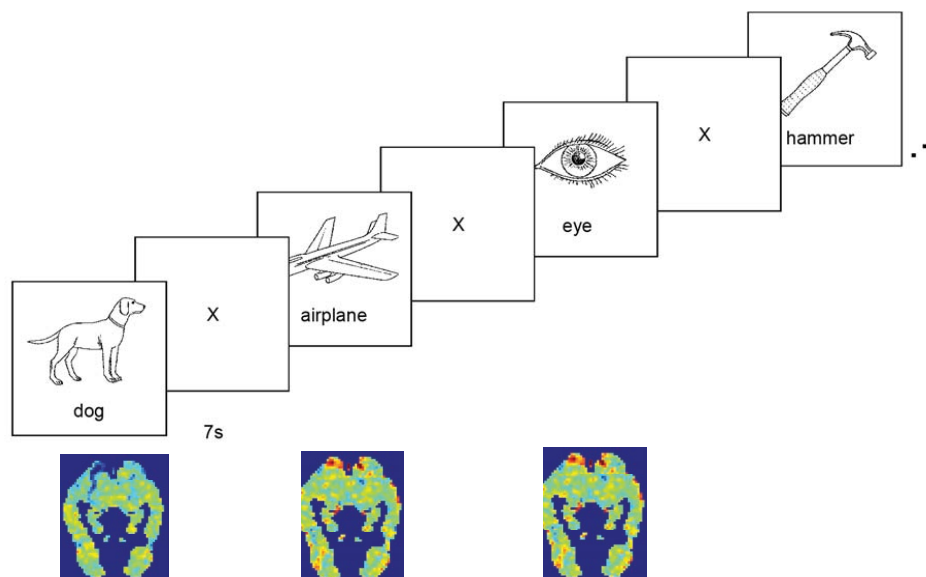
- **Brain Scan Data\***
  - 9 persons
  - 60 nouns
- **Questions**
  - 218 questions
  - ‘is it alive?’, ‘can you eat it?’



\*Mitchell et al. *Predicting human brain activity associated with the meanings of nouns*. Science, 2008. Data@ [www.cs.cmu.edu/afs/cs/project/theo-73/www/science2008/data.html](http://www.cs.cmu.edu/afs/cs/project/theo-73/www/science2008/data.html)

# Neuro-semantic

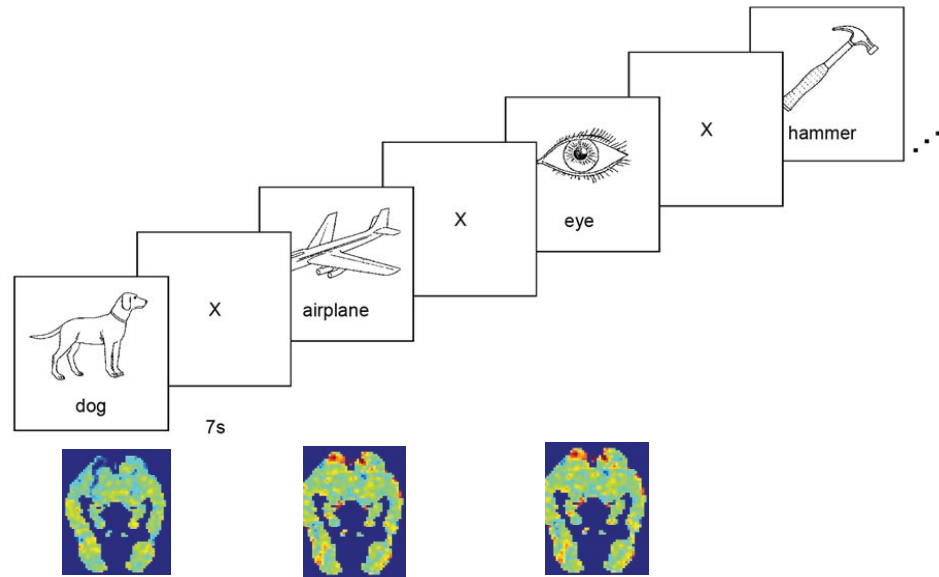
- **Brain Scan Data\***
  - 9 persons
  - 60 nouns
- **Questions**
  - 218 questions
  - 'is it alive?', 'can you eat it?'



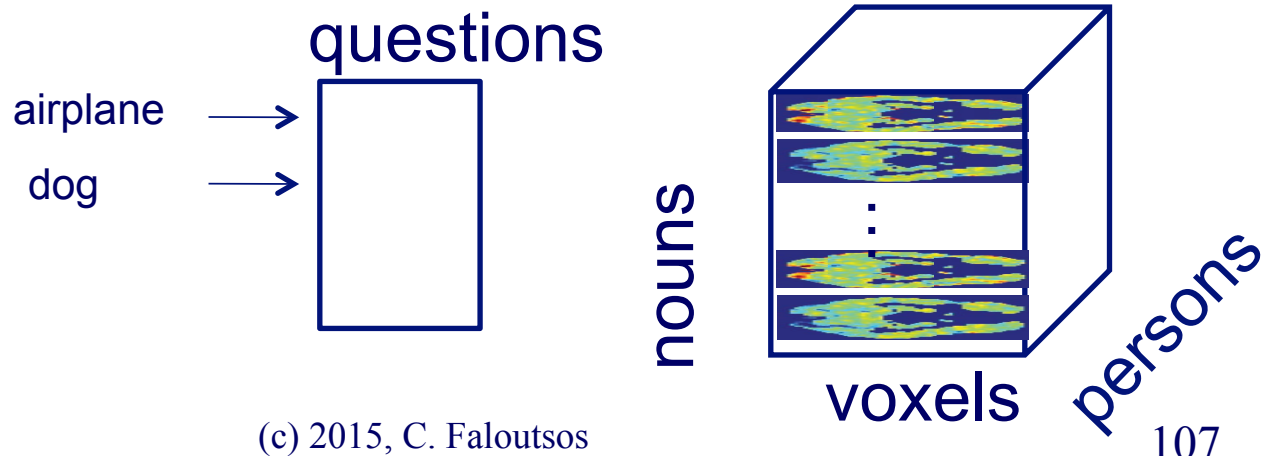
## Patterns?

# Neuro-semantic

- **Brain Scan Data\***
  - 9 persons
  - 60 nouns
- **Questions**
  - 218 questions
  - ‘is it alive?’, ‘can you eat it?’

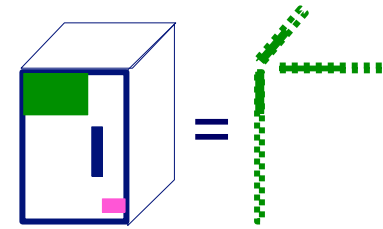


## Patterns?





# Neuro-semantic



## Nouns

beetle  
pants  
bee

## Questions

can it cause you pain?  
do you see it daily?  
is it conscious?

## Nouns

bear  
cow  
coat

## Questions

does it grow?  
is it alive?  
was it ever alive?

## Nouns

glass  
tomato  
bell

## Questions

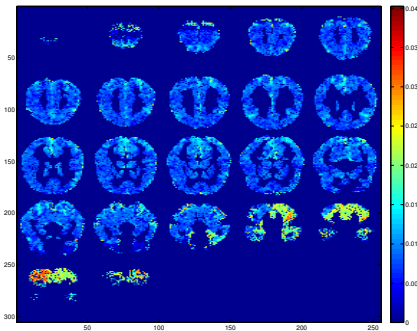
can you pick it up?  
can you hold it in one hand?  
is it smaller than a golfball?

## Nouns

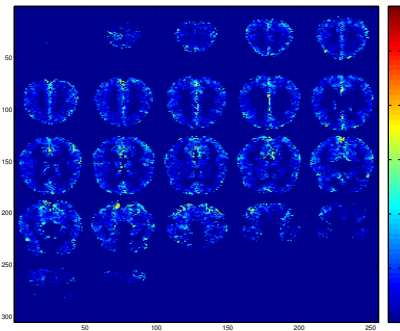
bed  
house  
car

## Questions

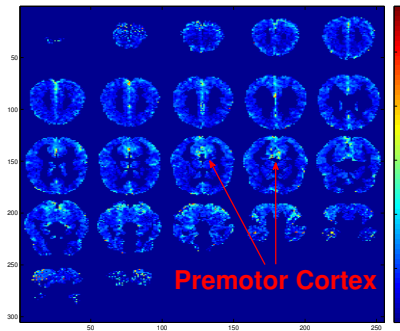
does it use electricity?  
can you sit on it?  
does it cast a shadow?



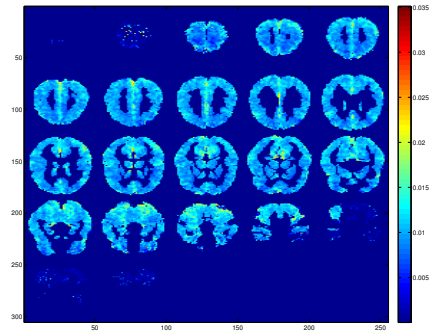
Group 1



Group 2

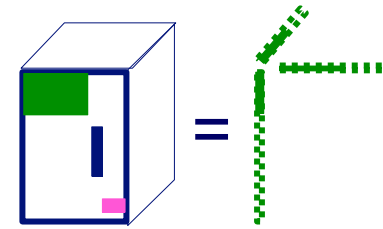


Group 3



Group 4

# Neuro-semantic



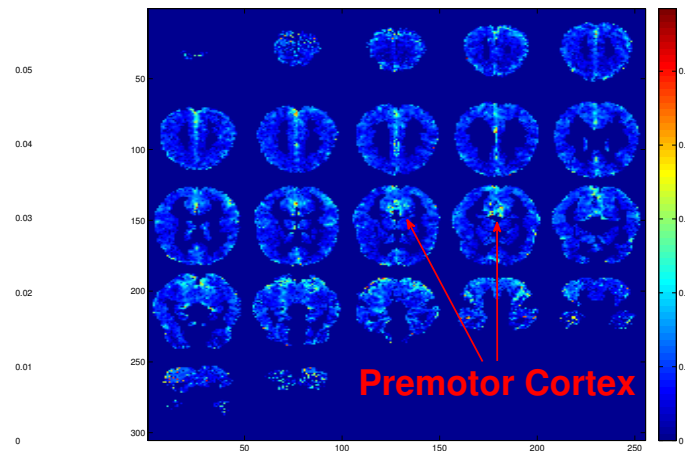
**Small items ->  
Premotor cortex**

## Nouns

glass  
tomato  
bell

## Questions

can you pick it up?  
can you hold it in one hand?  
is it smaller than a golfball?'



**Group 3**

# Neuro-semantic

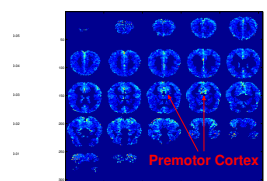
Small items ->  
Premotor cortex

## Nouns

glass  
tomato  
bell

## Questions

can you pick it up?  
can you hold it in one hand?  
is it smaller than a golfball?



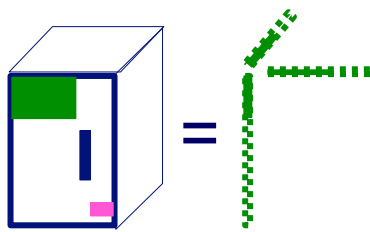
Group 3



Evangelos Papalexakis, Tom Mitchell, Nicholas Sidiropoulos,  
Christos Faloutsos, Partha Pratim Talukdar, Brian Murphy,  
*Turbo-SMT: Accelerating Coupled Sparse Matrix-Tensor  
Factorizations by 200x*, SDM 2014

## Part 2: Conclusions

- Time-evolving / heterogeneous graphs -> tensors
- PARAFAC finds patterns
- (GigaTensor/HaTen2 -> fast & scalable)

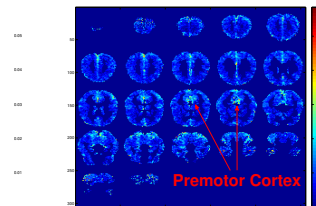


### Nouns

glass  
tomato  
bell

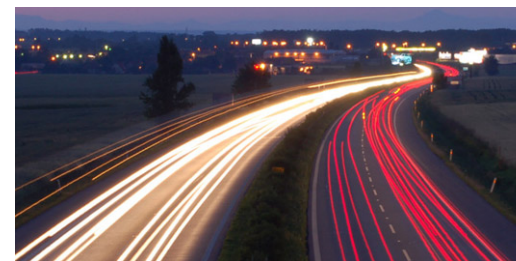
### Questions

can you pick it up?  
can you hold it in one hand?  
is it smaller than a golfball?



Group 3

# Roadmap



- Introduction – Motivation
  - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
- ➔ • Acknowledgements and Conclusions

# Thanks



**Microsoft**

*Disclaimer: All opinions are mine; not necessarily reflecting the opinions of the funding agencies*

Thanks to: NSF IIS-1247489, IIS-0705359, IIS-0534205, CTA-INARC; Yahoo (M45), LLNL, IBM, SPRINT, Google, INTEL, HP, iLab

# Cast



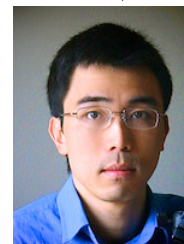
Akoglu,  
Leman



Araujo,  
Miguel



Beutel,  
Alex



Chau,  
Polo



Hooi,  
Bryan



Kang, U



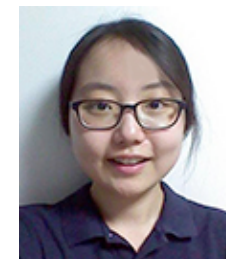
Koutra,  
Danai



Papalexakis,  
Vagelis




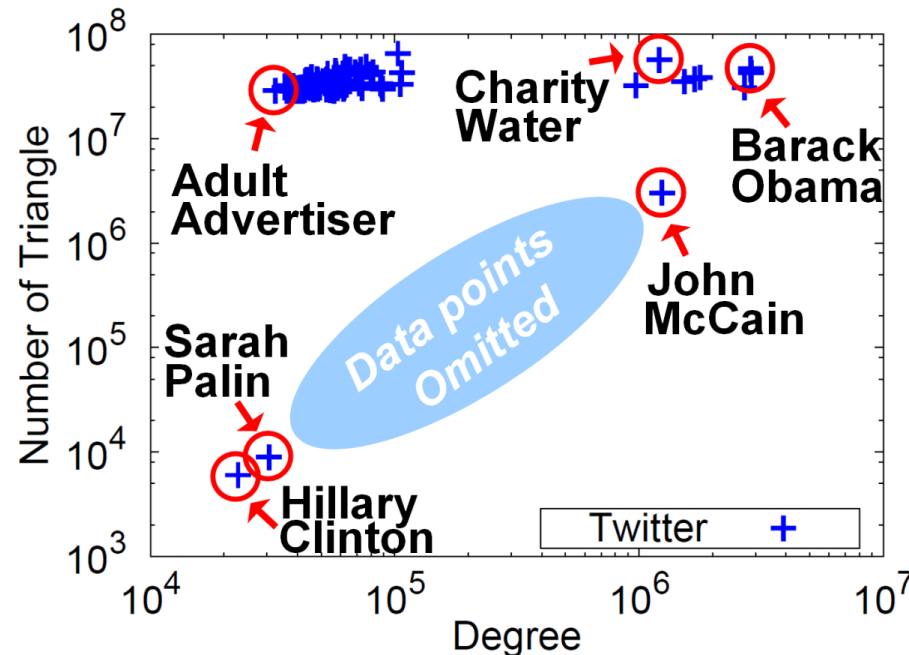
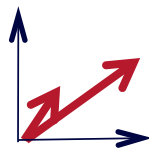
Shah,  
Neil



Song,  
Hyun Ah

# CONCLUSION#1 – Big data

- **Patterns**  **Anomalies**
- **Large datasets reveal patterns/outliers that are invisible otherwise**





# CONCLUSION#2 – tensors

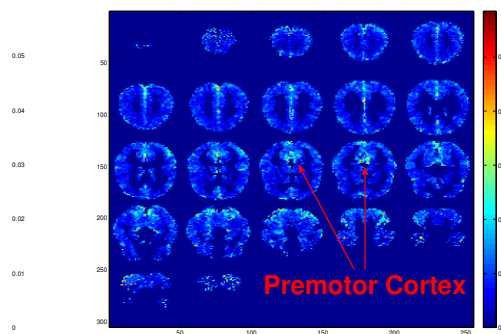
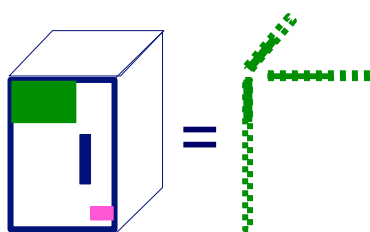
- powerful tool

## Nouns

glass  
tomato  
bell

## Questions

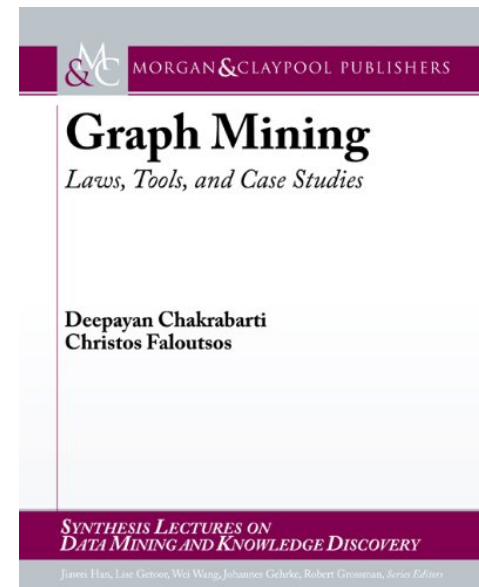
can you pick it up?  
can you hold it in one hand?  
is it smaller than a golfball?



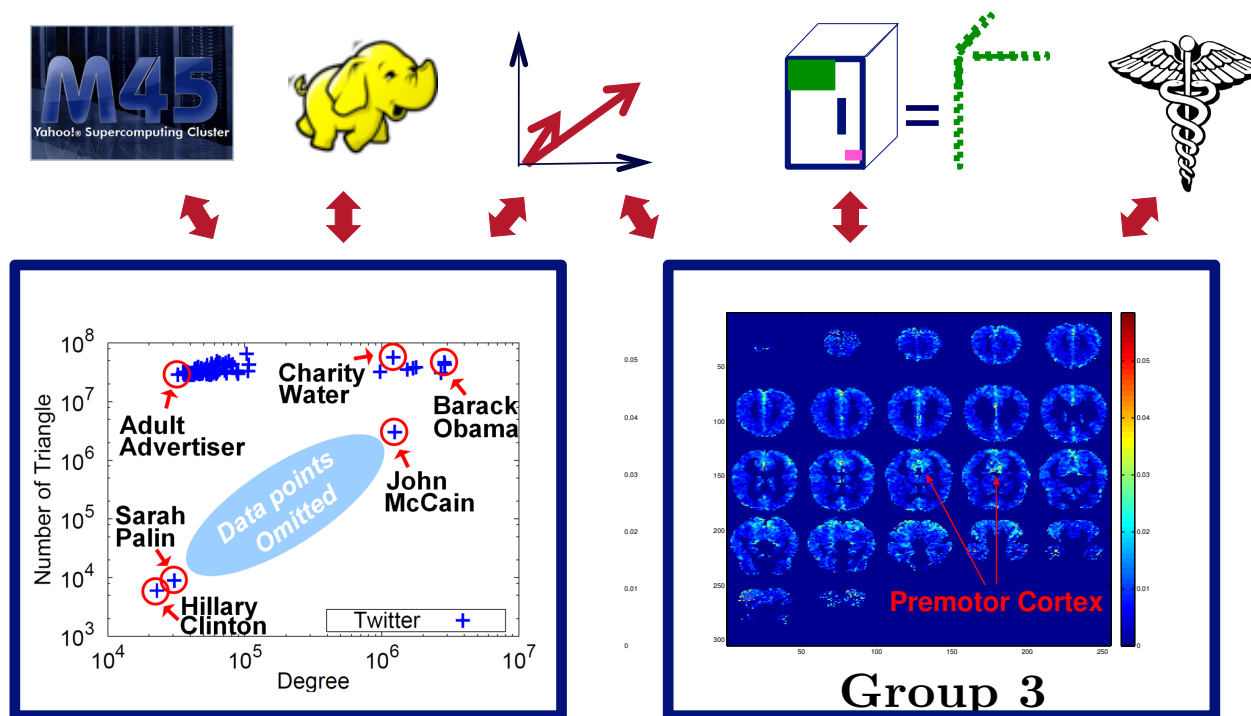
Group 3

# References

- D. Chakrabarti, C. Faloutsos: *Graph Mining – Laws, Tools and Case Studies*, Morgan Claypool 2012
- <http://www.morganclaypool.com/doi/abs/10.2200/S00449ED1V01Y201209DMK006>



# TAKE HOME MESSAGE: Cross-disciplinary



# Thank you!

## Cross-disciplinary

