

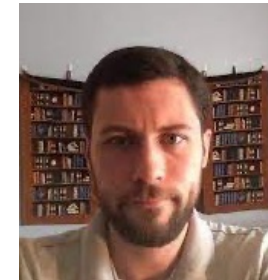
Anomaly detection in large graphs

Christos Faloutsos

CMU

Thank you!

- Badel Mbanga
- Clifton Denning
- Matthew Berezo



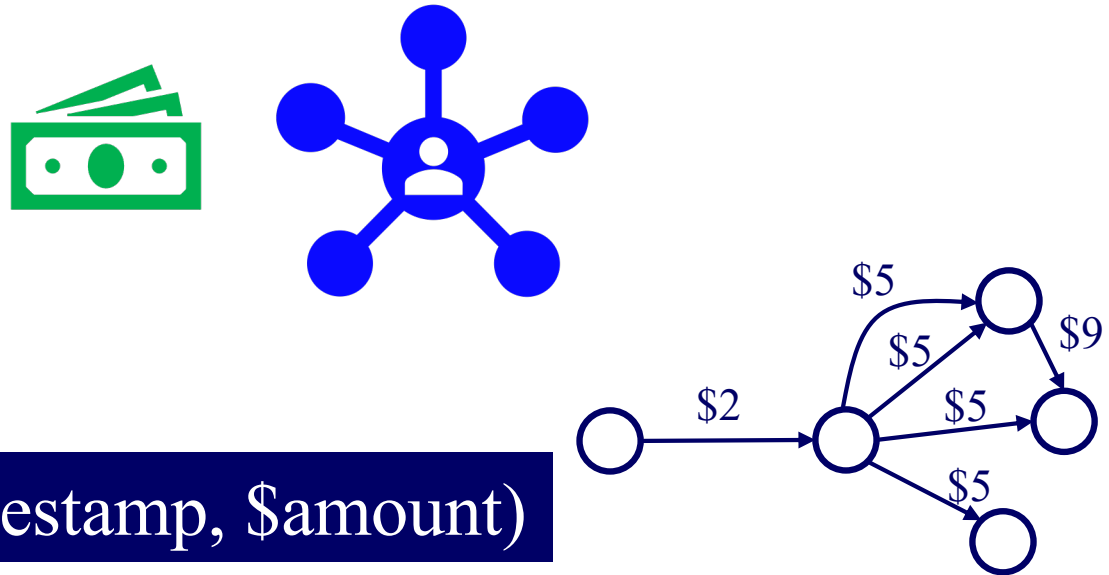
Roadmap

- ➔ • Introduction – Motivation
 - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
- Conclusions



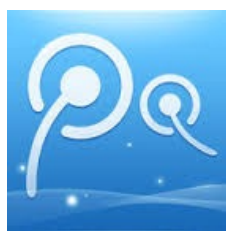
Graphs – why should we care?

PNC



(source, destination, timestamp, \$amount)

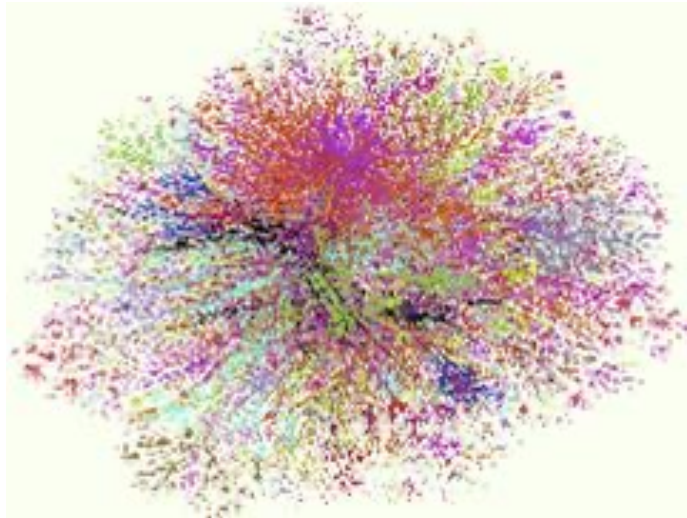
Graphs - why should we care?



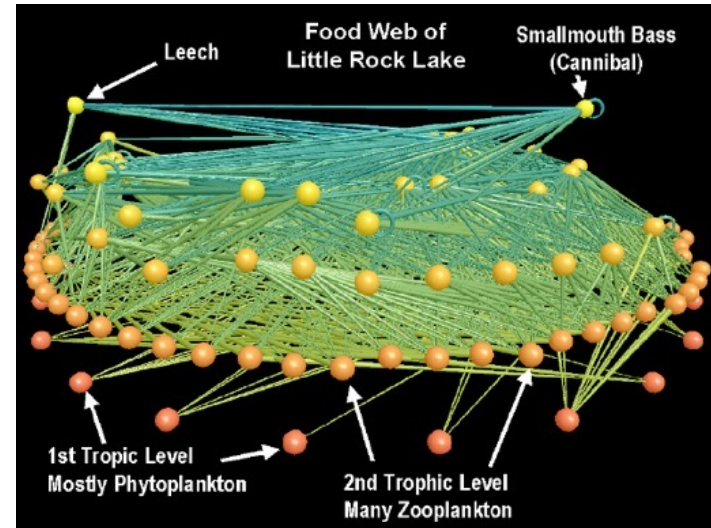
>\$10B; ~1B users



Graphs - why should we care?






Internet Map
[lumeta.com]



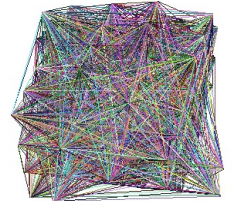
Food Web
[Martinez '91]

Graphs - why should we care?

- web-log ('blog') news propagation 
- computer network security: email/IP traffic and anomaly detection
- Recommendation systems 
- 
- Many-to-many db relationship -> graph

Motivating problems

- P1: patterns? Fraud detection?



- P2: patterns in time-evolving graphs / tensors

destination



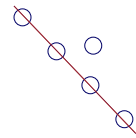
source

time



Motivating problems

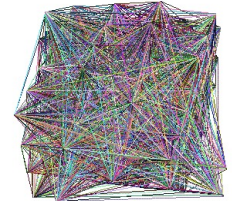
- P1: patterns? Fraud detection?



Patterns



anomalies



- P2: patterns in time-evolving graphs / tensors

destination



source

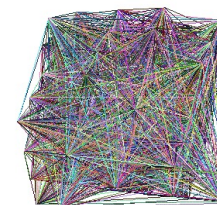
time



Roadmap

- Introduction – Motivation
 - Why study (big) graphs?
- ➔ • Part#1: Patterns & fraud detection
- Part#2: time-evolving graphs; tensors
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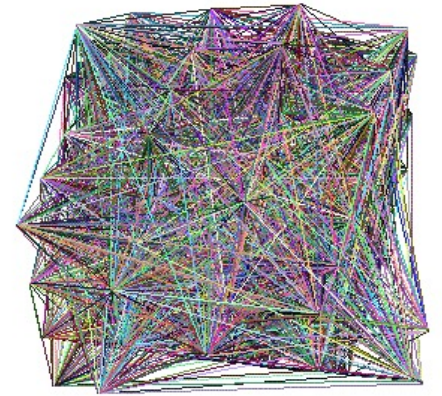




Part 1: Patterns, & fraud detection

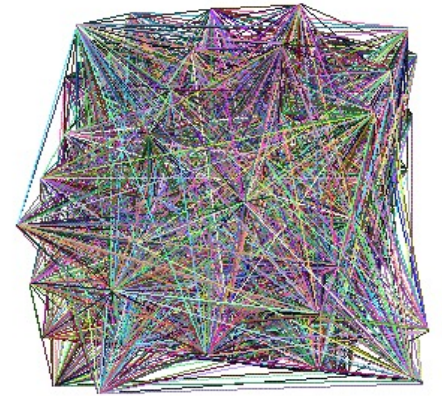
Laws and patterns

- Q1: Are real graphs random?



Laws and patterns

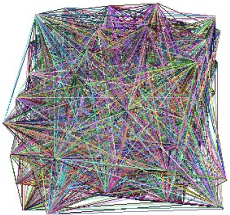
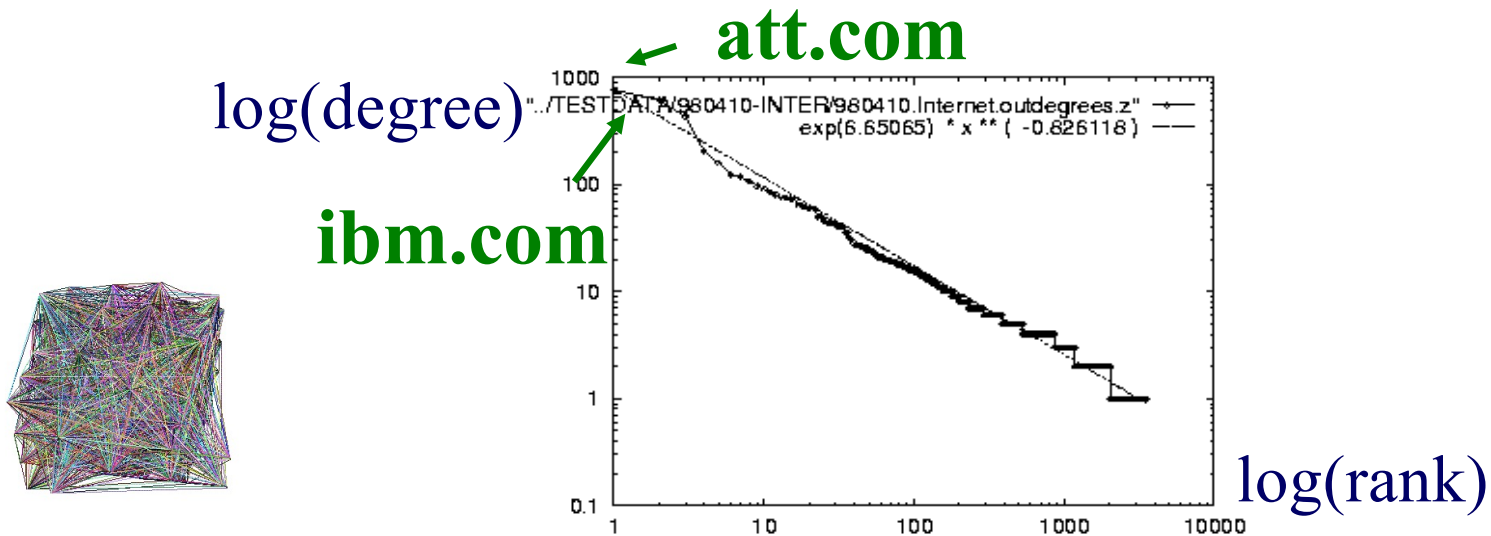
- Q1: Are real graphs random?
- A1: NO!!
 - Diameter ('6 degrees'; 'Kevin Bacon')
 - in- and out- degree distributions
 - other (surprising) patterns
- So, let's look at the data



Solution# S.1

- Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

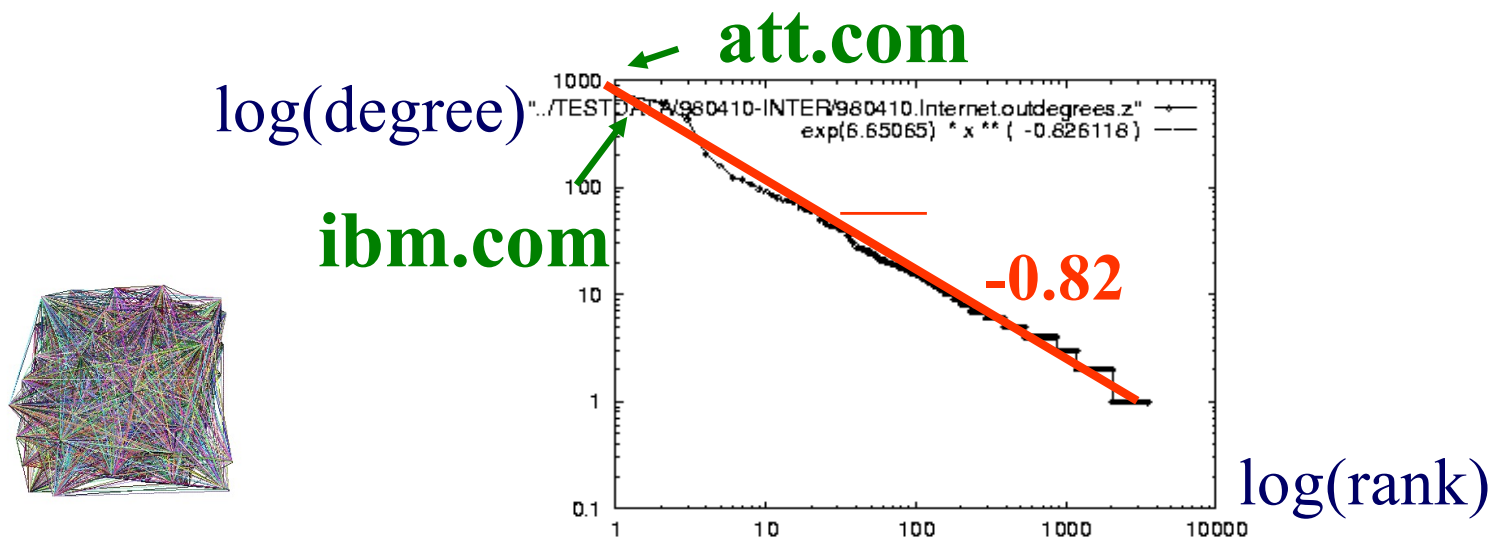
internet domains



Solution# S.1

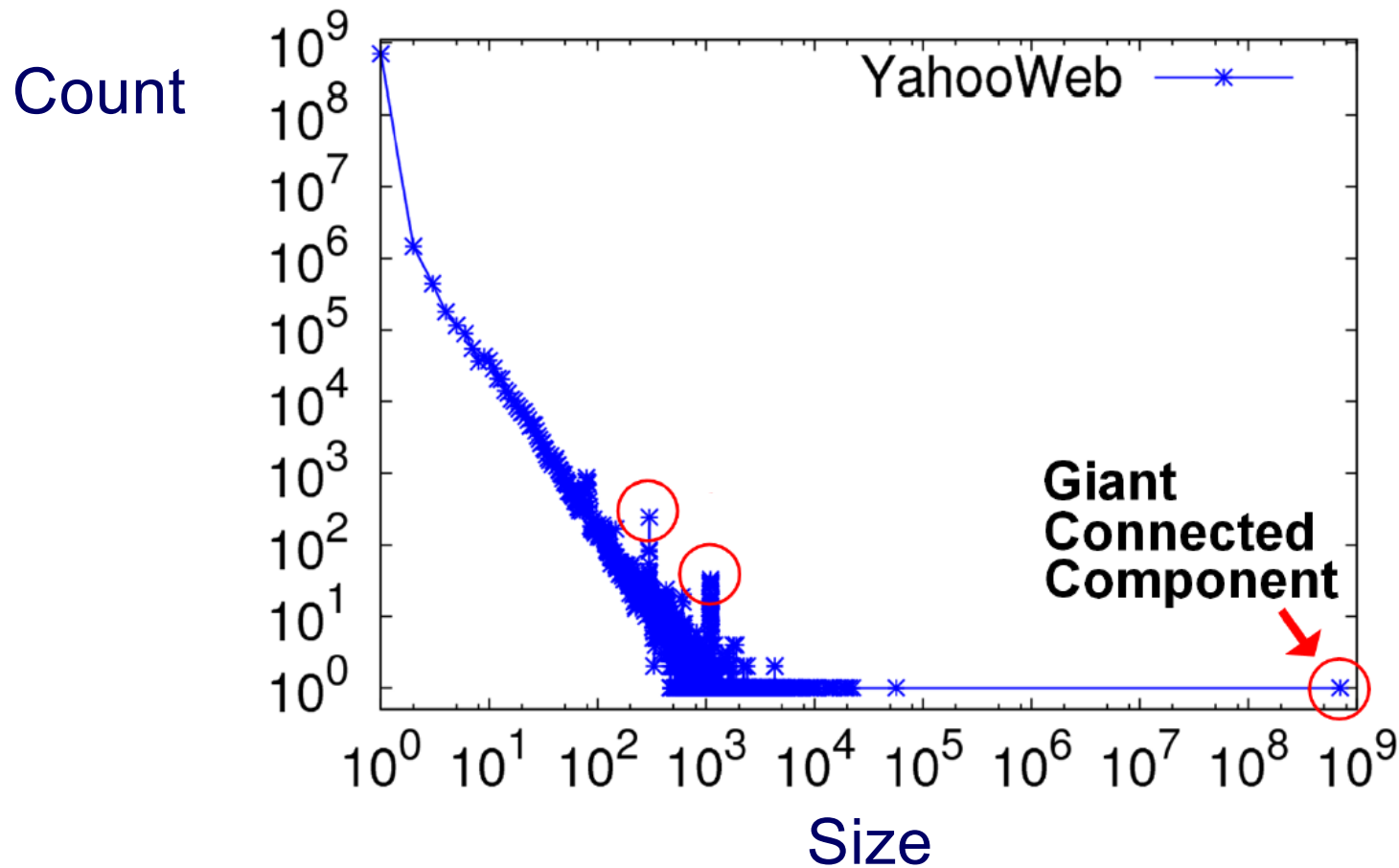
- Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

internet domains



S2: connected component sizes

- Connected Components – 4 observations:

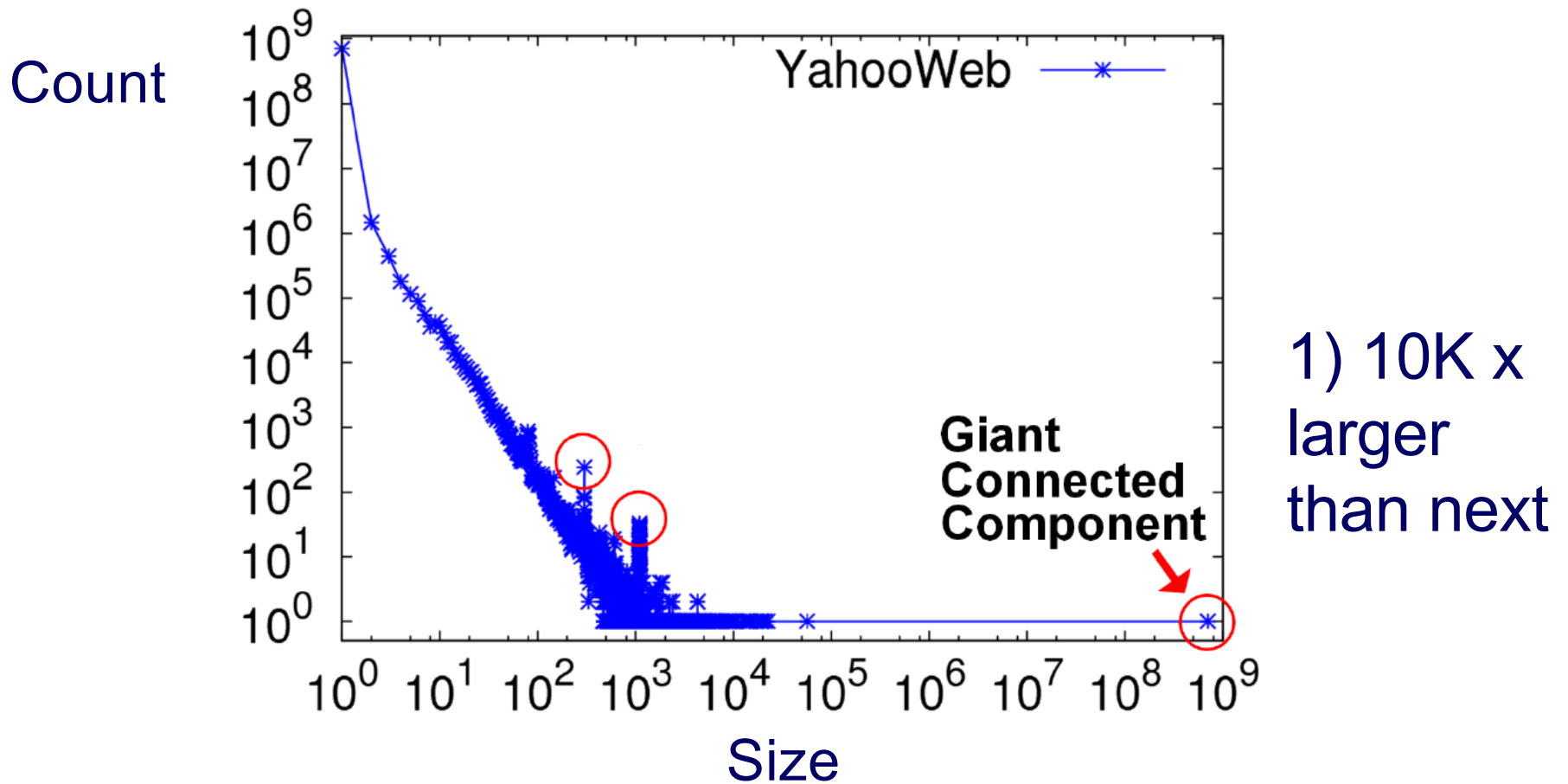


1.4B nodes
6B edges

S2: connected component sizes



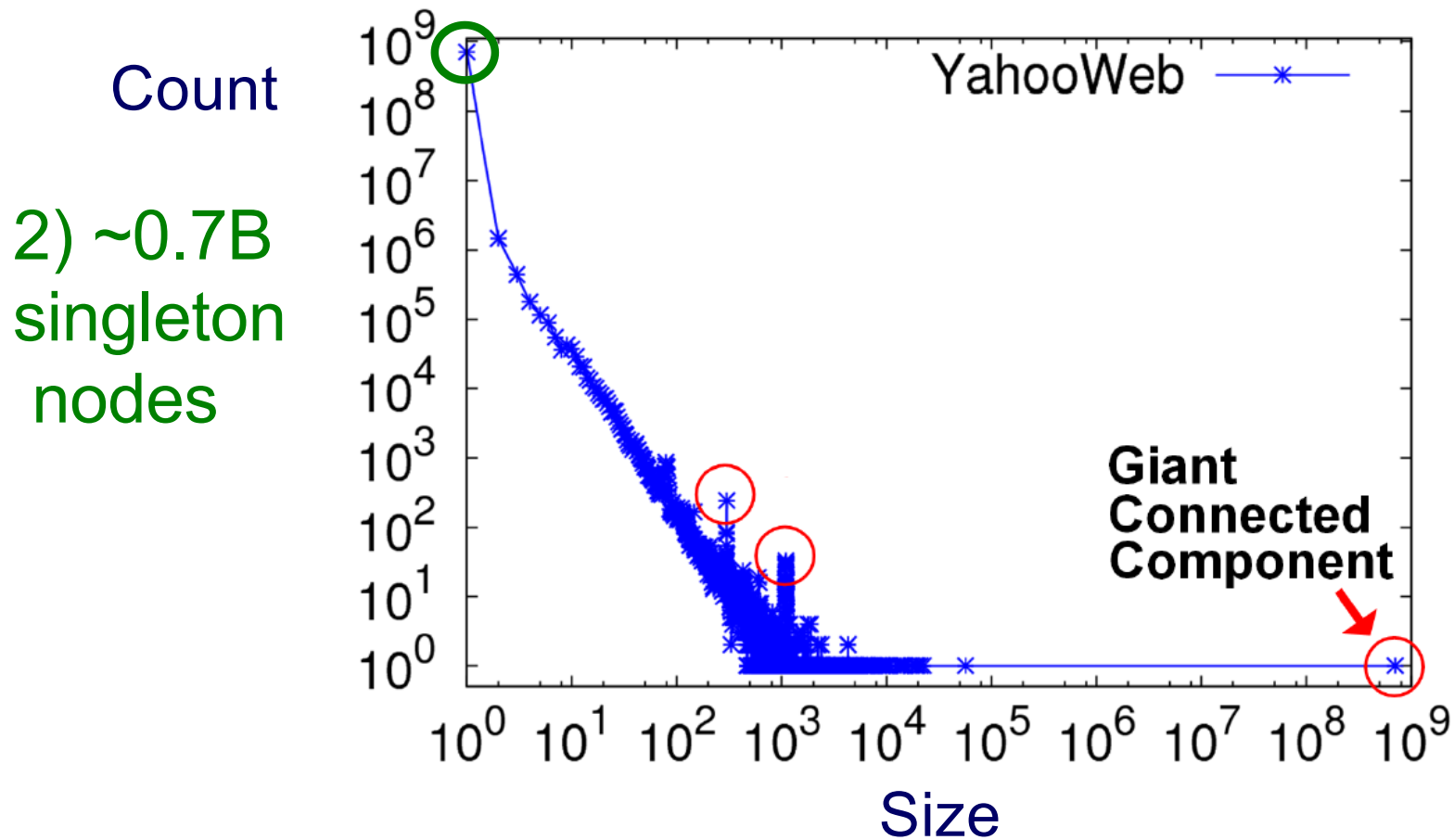
- Connected Components



S2: connected component sizes



- Connected Components

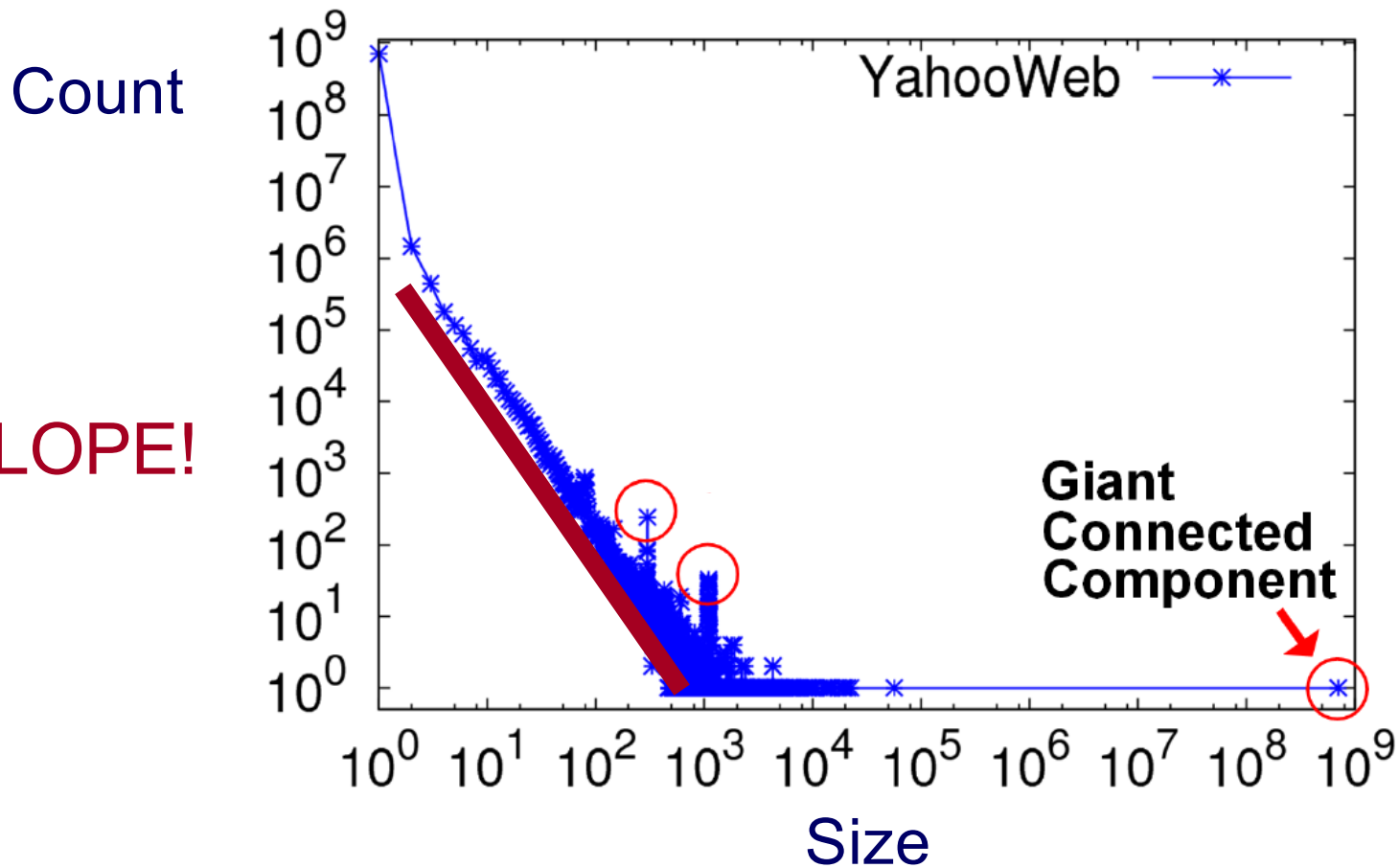


S2: connected component sizes



- Connected Components

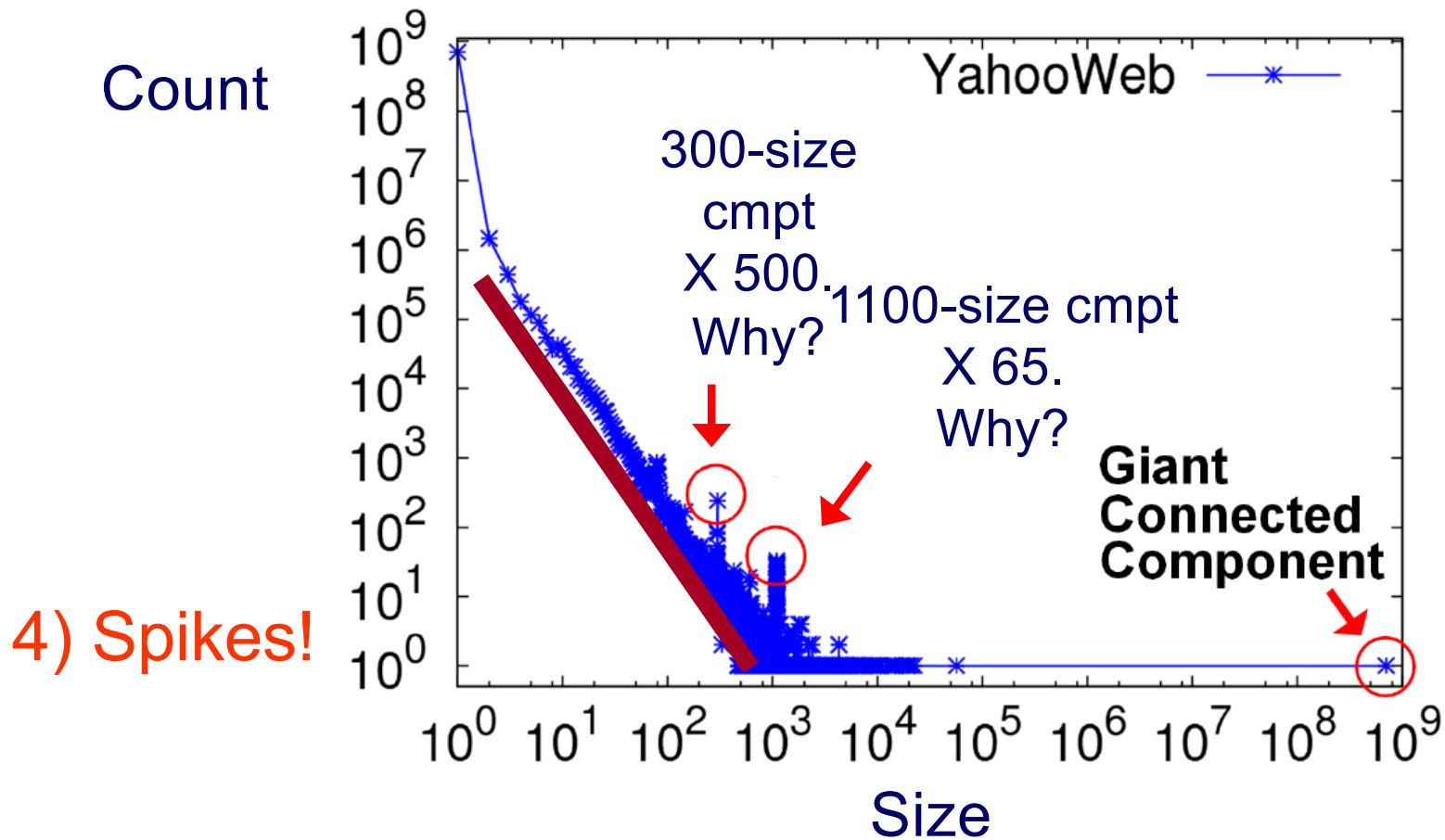
3) SLOPE!



S2: connected component sizes



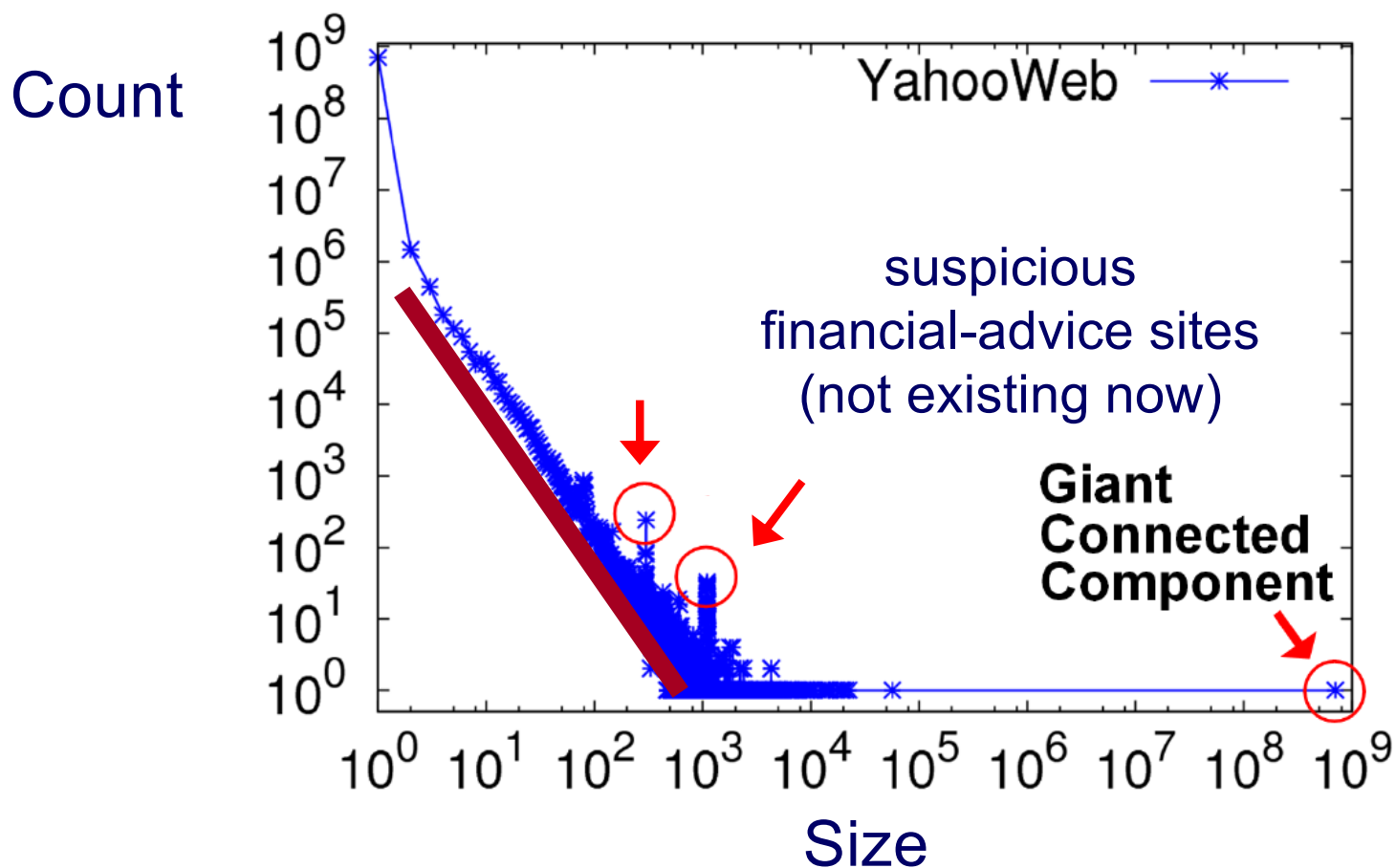
- Connected Components



S2: connected component sizes



- Connected Components

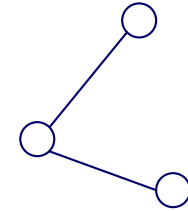


Roadmap



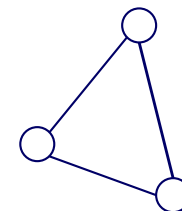
- Introduction – Motivation
- Part#1: Patterns in graphs
 - P1.1: Patterns: Degree; Triangles
 - P1.2: Anomaly/fraud detection
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Solution# S.3: Triangle ‘Laws’

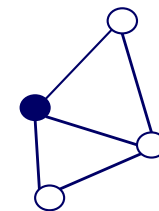


- Real social networks have a lot of triangles

Solution# S.3: Triangle ‘Laws’

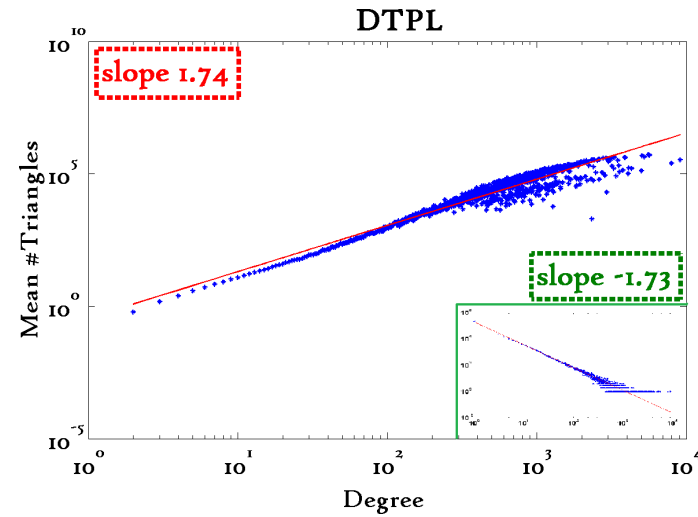
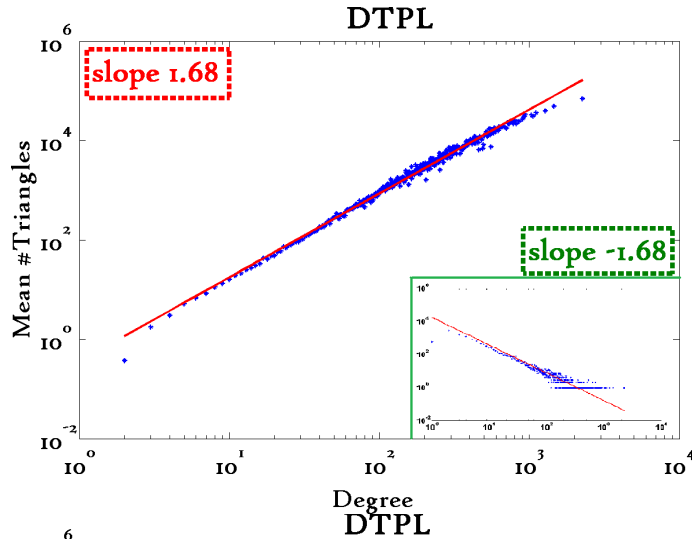


- Real social networks have a lot of triangles
 - Friends of friends are friends
- Any patterns?
 - 2x the friends, 2x the triangles ?



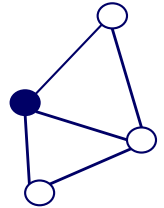
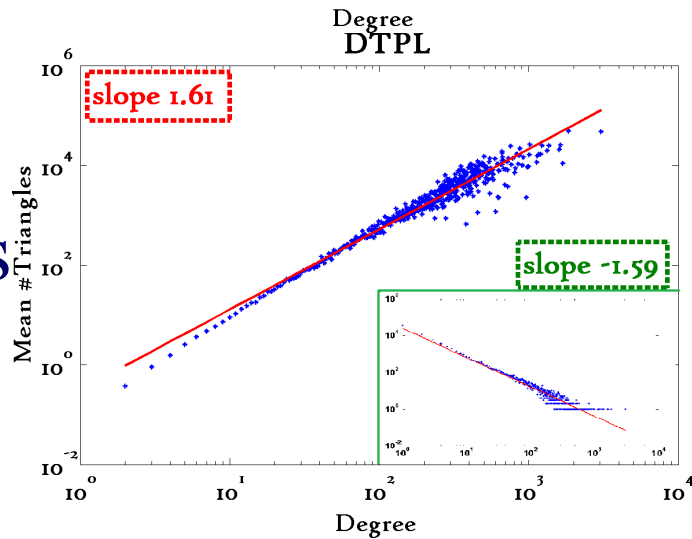
Triangle Law: #S.3 [Tsourakakis ICDM 2008]

Reuters



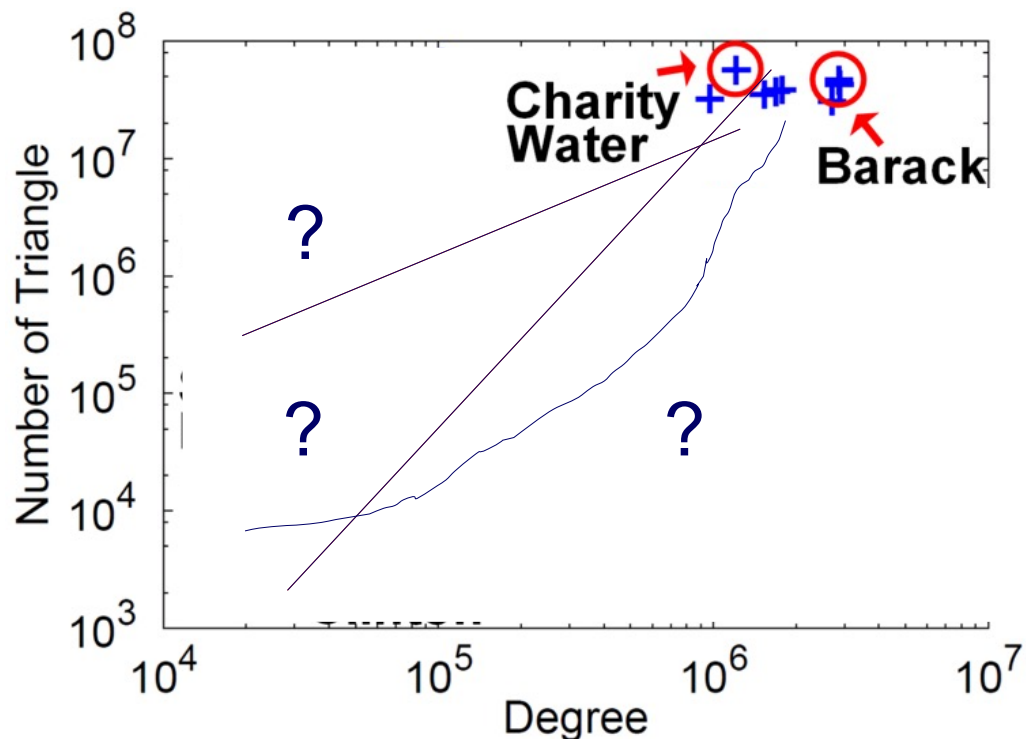
SN

Epinions



X-axis: degree
 Y-axis: mean # triangles
 n friends $\rightarrow \sim n^{1.6}$ triangles

Triangle counting for large graphs?

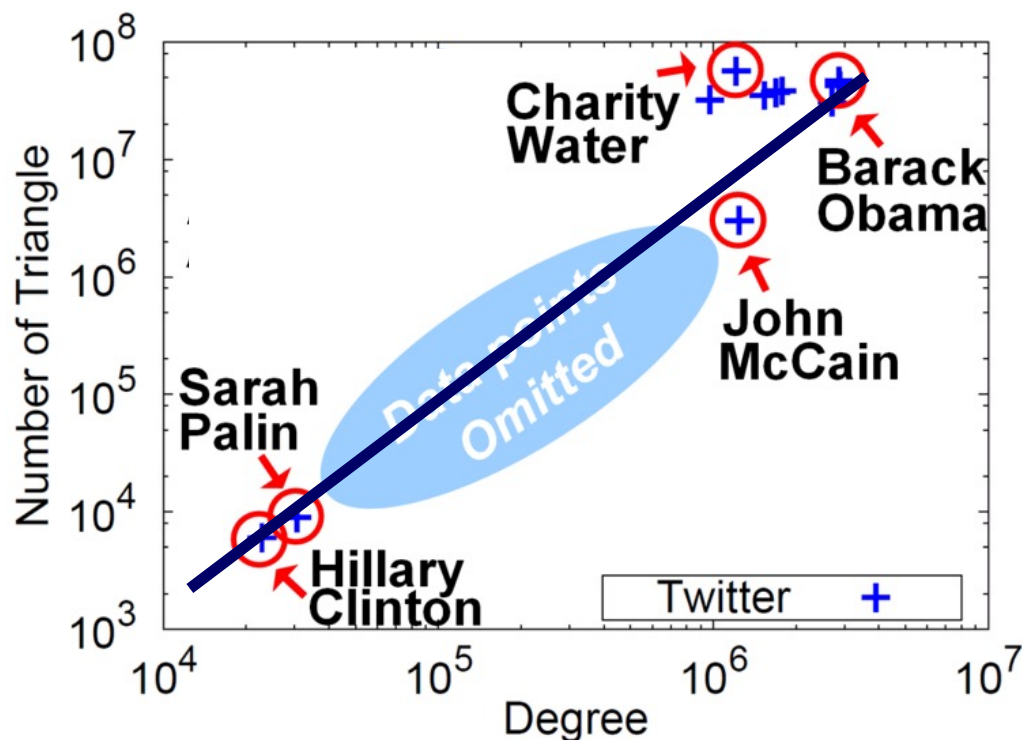


Anomalous nodes in Twitter (~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]



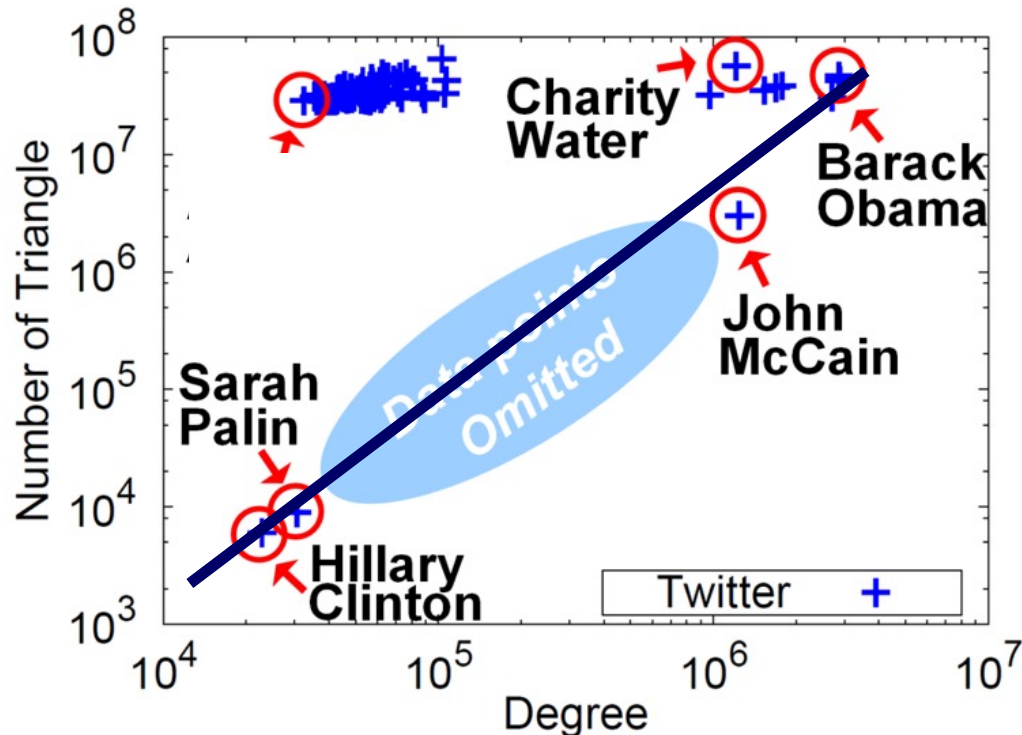
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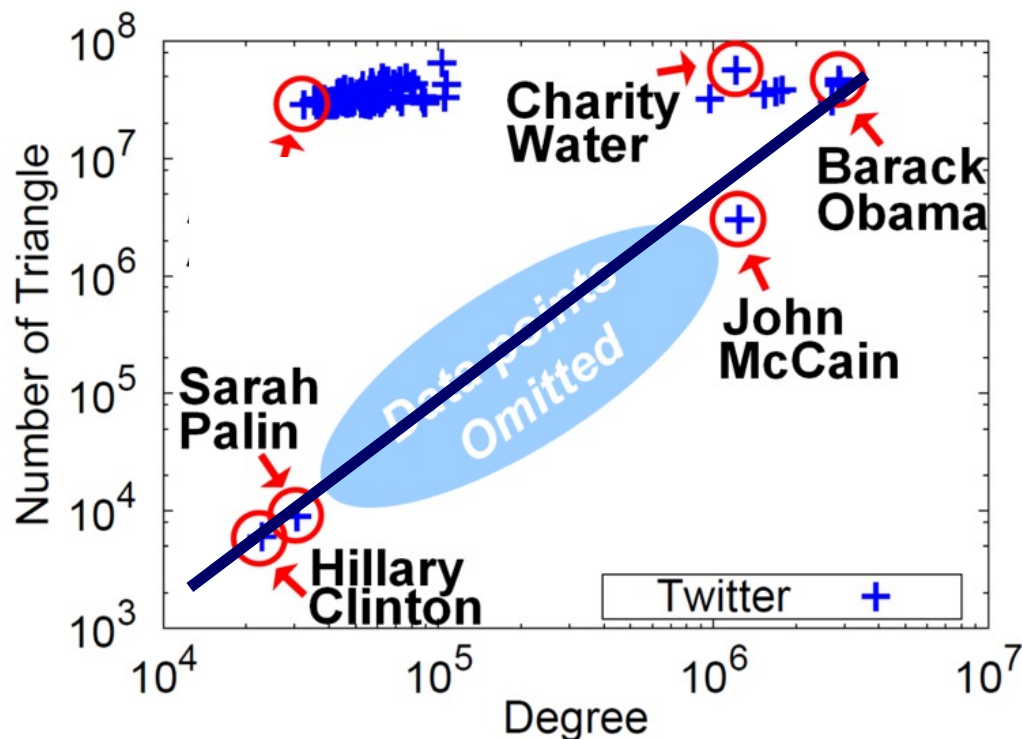
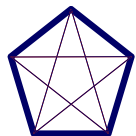
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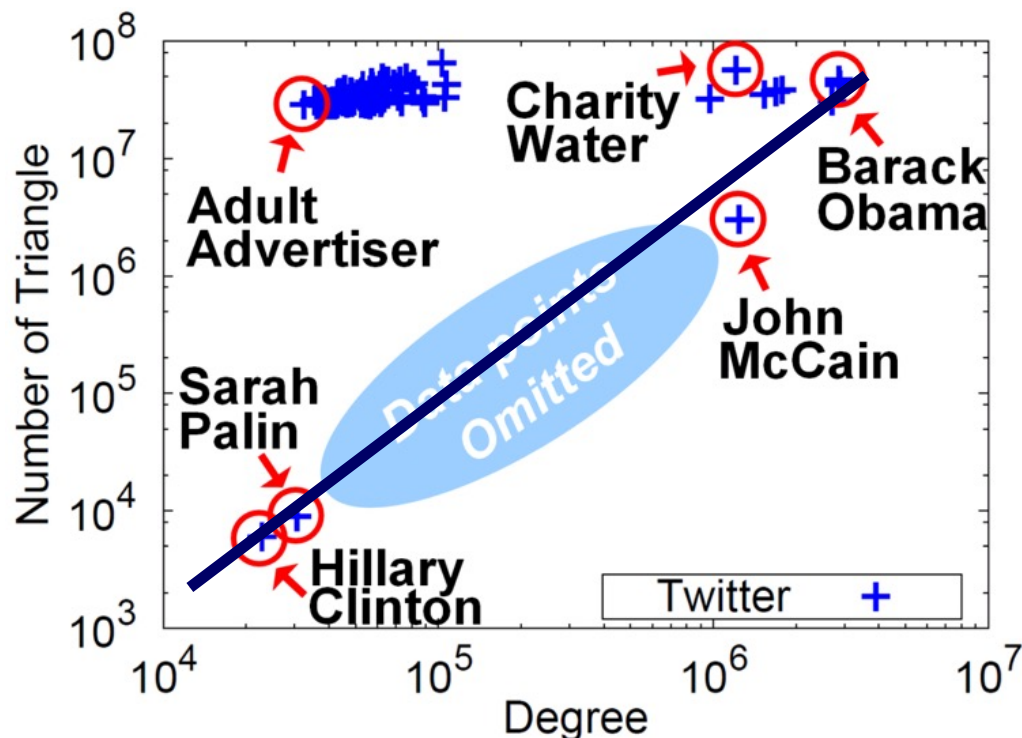
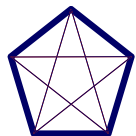
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Triangle counting for large graphs?



Anomalous nodes in Twitter (~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]

MORE Graph Patterns

	Unweighted	Weighted
Static	<p>L01. Power-law degree distribution [Faloutsos et al. '99, Kleinberg et al. '99, Chakrabarti et al. '04, Newman '04]</p> <p>L02. Triangle Power Law (TPL) [Tsourakakis '08]</p> <p>L03. Eigenvalue Power Law (EPL) [Siganos et al. '03]</p> <p>L04. Community structure [Flake et al. '02, Girvan and Newman '02]</p>	<p>L10. Snapshot Power Law (SPL) [McGlohon et al. '08]</p>
Dynamic	<p>L05. Densification Power Law (DPL) [Leskovec et al. '05]</p> <p>L06. Small and shrinking diameter [Albert and Barabási '99, Leskovec et al. '05]</p> <p>L07. Constant size 2nd and 3rd connected components [McGlohon et al. '08]</p> <p>L08. Principal Eigenvalue Power Law (λ_1PL) [Akoglu et al. '08]</p> <p>L09. Bursty/self-similar edge/weight additions [Gomez and Santonja '98, Gribble et al. '98, Crovella and</p>	<p>L11. Weight Power Law (WPL) [McGlohon et al. '08]</p>

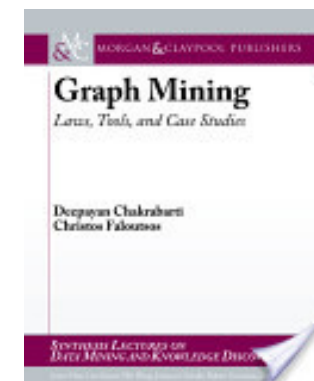
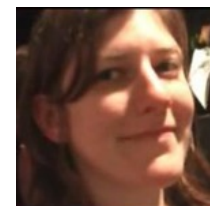
RTG: A Recursive Realistic Graph Generator using Random Typing Leman Akoglu and Christos Faloutsos. *PKDD'09*.

MORE Graph Patterns

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- Mary McGlohon, Leman Akoglu, Christos Faloutsos. *Statistical Properties of Social Networks*. in "Social Network Data Analytics" (Ed.: Charu Aggarwal)

- Deepayan Chakrabarti and Christos Faloutsos, [*Graph Mining: Laws, Tools, and Case Studies*](#) Oct. 2012, Morgan Claypool.



Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
 - P1.1: Patterns
 - ➔ – P1.2: Anomaly / fraud detection
 - No labels – spectral
 - With labels: Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions



Patterns



anomalies

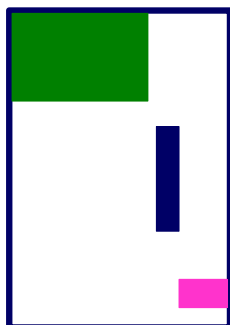
How to find ‘suspicious’ groups?

- ‘blocks’ are normal, right?



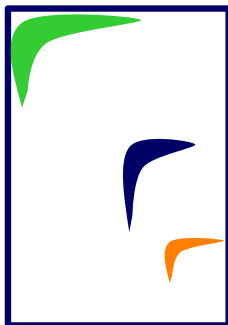
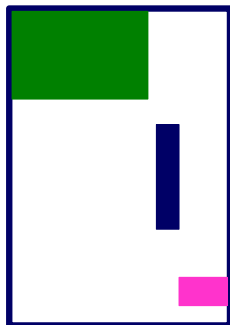
idols

fans



Except that:

- ‘blocks’ are normal, ~~right?~~
- ‘hyperbolic’ communities are more realistic [Araujo+, PKDD’14]

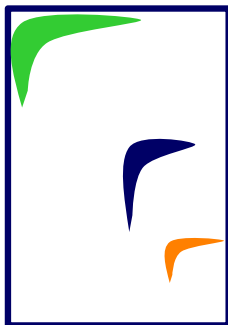
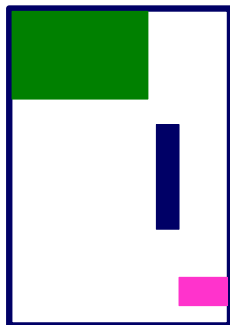


Except that:



- ‘blocks’ are usually **suspicious**
- ‘hyperbolic’ communities are more realistic
[Araujo+, PKDD’14]

Q: Can we spot blocks, easily?



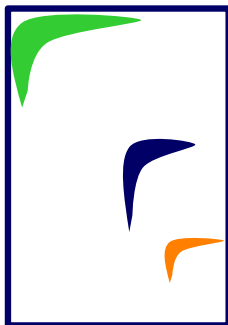
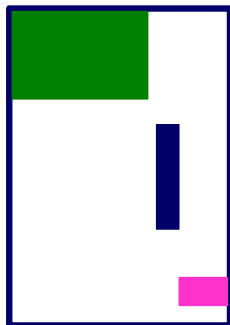
Except that:



- ‘blocks’ are usually **suspicious**
- ‘hyperbolic’ communities are more realistic
[Araujo+, PKDD’14]

Q: Can we spot blocks, easily?

A: Silver bullet: SVD!



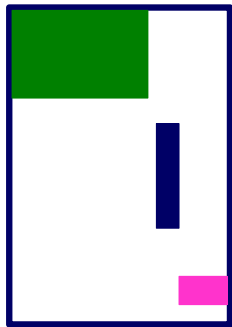
Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks



M
idols

N
fans

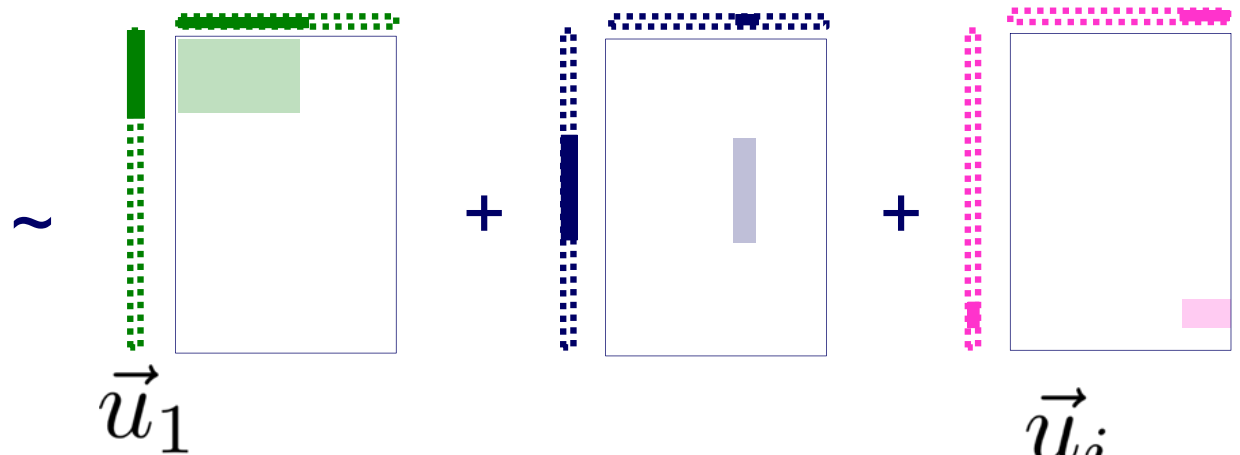


'music lovers'
'singers'

'sports lovers'
'athletes'

'citizens'
'politicians'

\vec{v}_1



\vec{u}_1

Christos Faloutsos

\vec{u}_i 38

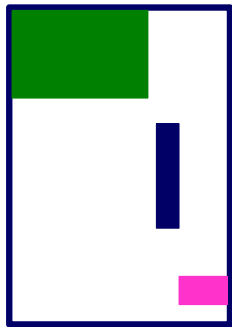
Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks



M
products

N
users

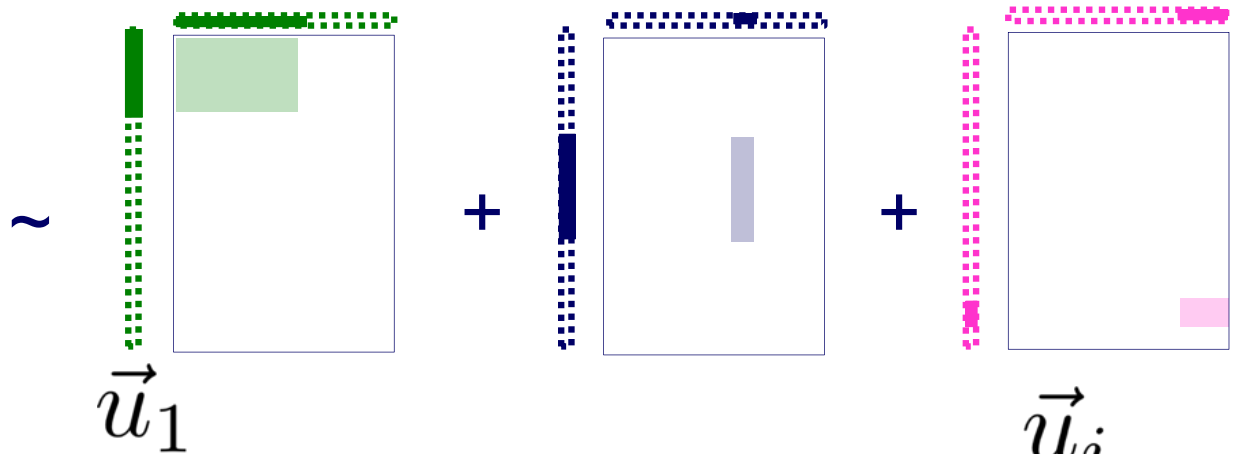


'meat-eaters'
'steaks'

\vec{v}_1

'vegetarians'
'plants'

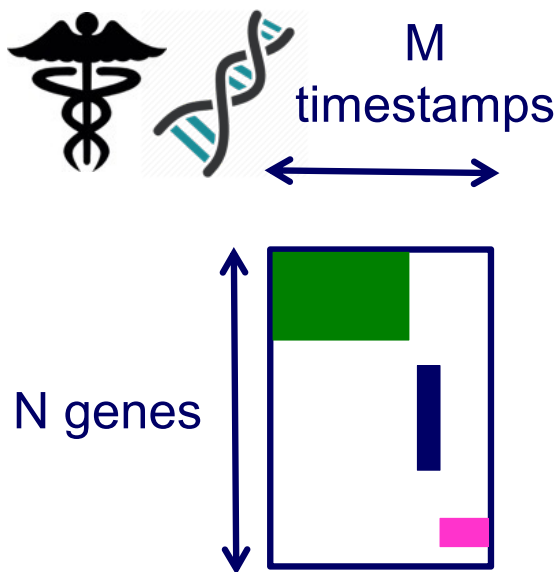
'kids'
'cookies'



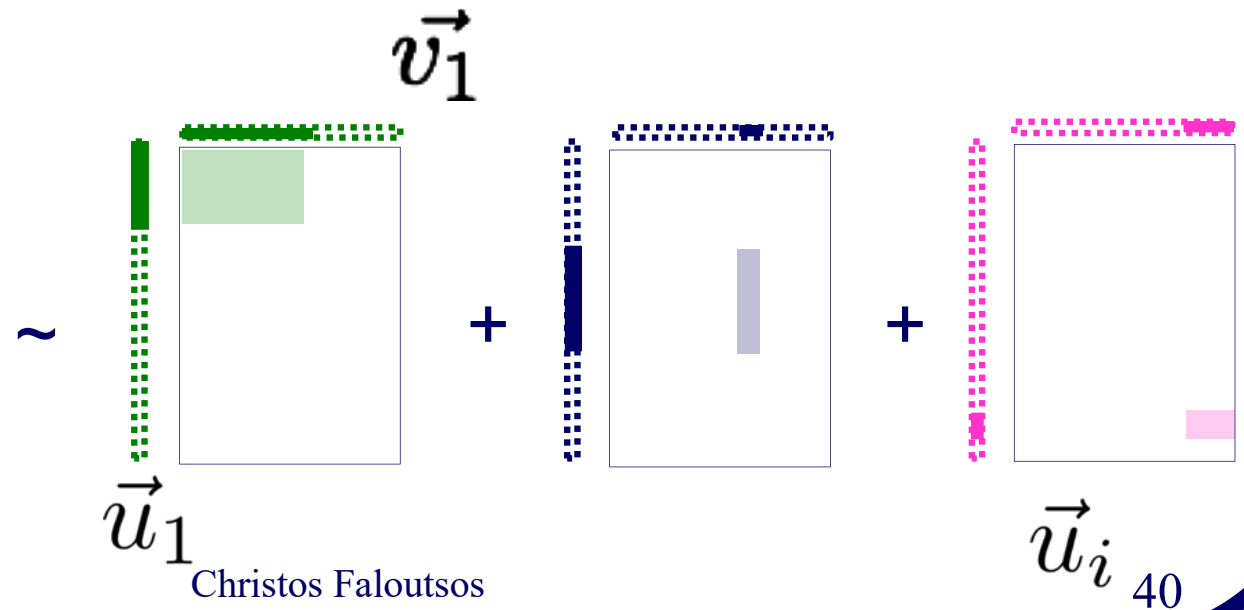
\vec{u}_i 39

Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks



'cancer' 'alzheimer' 'Parkinson'



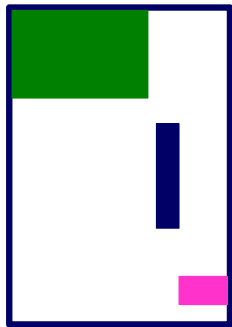
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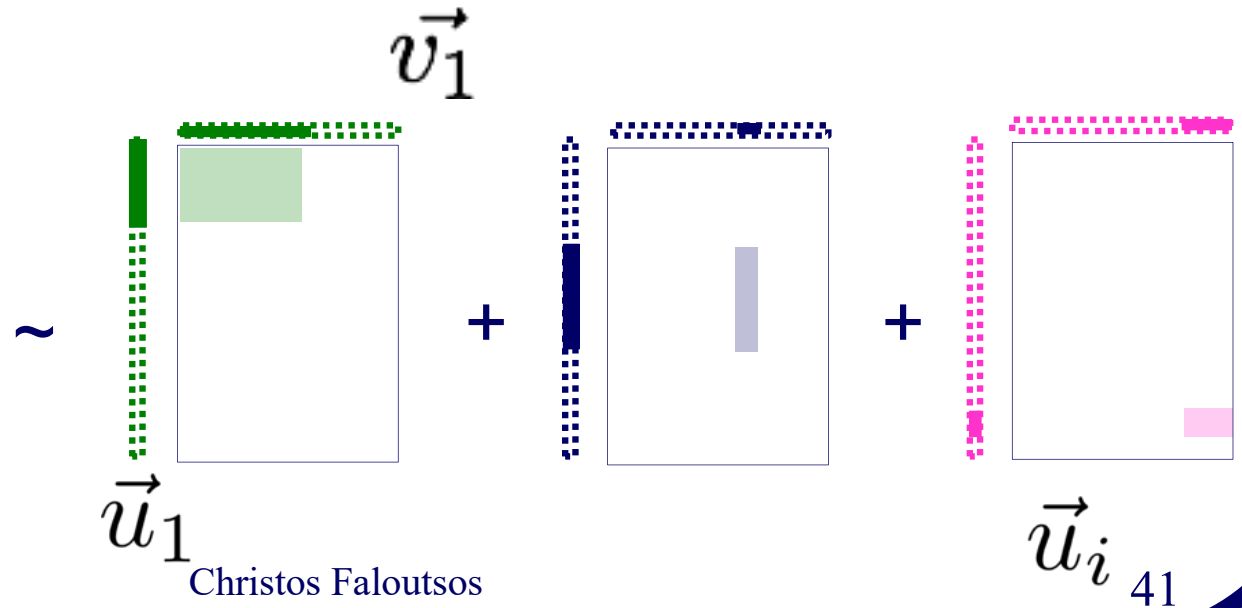


M
idols

N
fans



'music lovers' 'singers'
'sports lovers' 'athletes'
'citizens' 'politicians'



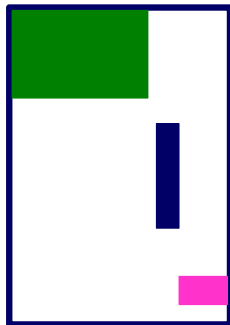
Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks



M
idols

N
fans



'music lovers'
'singers'

'sports lovers'
'athletes'

'citizens'
'politicians'

$$\sim \vec{u}_1 + \vec{v}_1 + \vec{u}_i$$

Christos Faloutsos

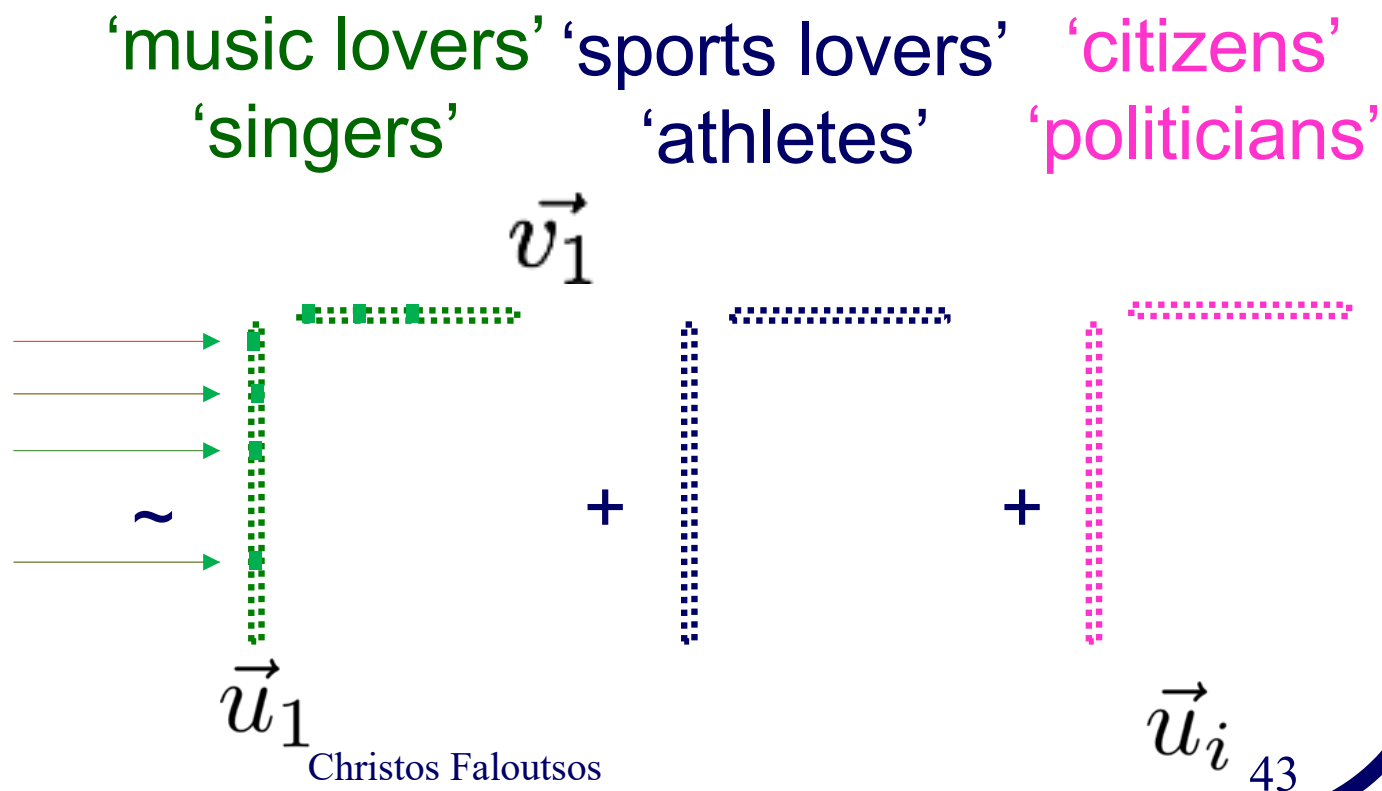
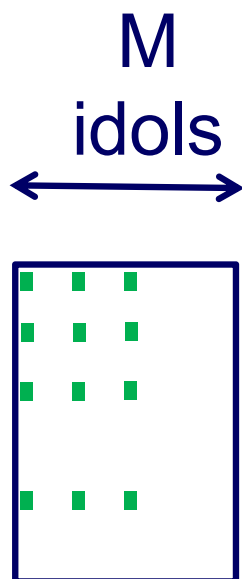
42

Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks **Even if shuffled!**



N
fans



Inferring Strange Behavior from Connectivity Pattern in Social Networks


PAKDD'14



Meng Jiang, Peng Cui, Shiqiang Yang (Tsinghua)
Alex Beutel, Christos Faloutsos (CMU)



Dataset

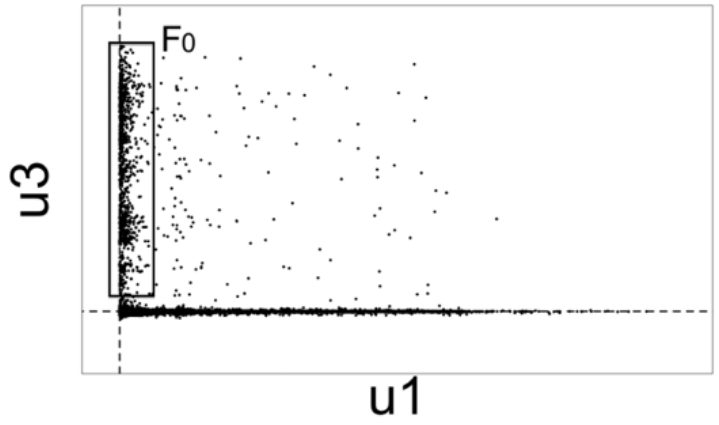
- Tencent Weibo 
- 117 million nodes (with profile and UGC data)
- 3.33 billion directed edges



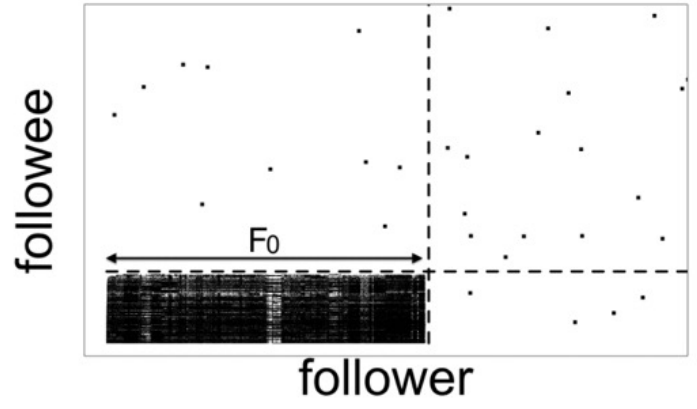
Real Data



“Rays”



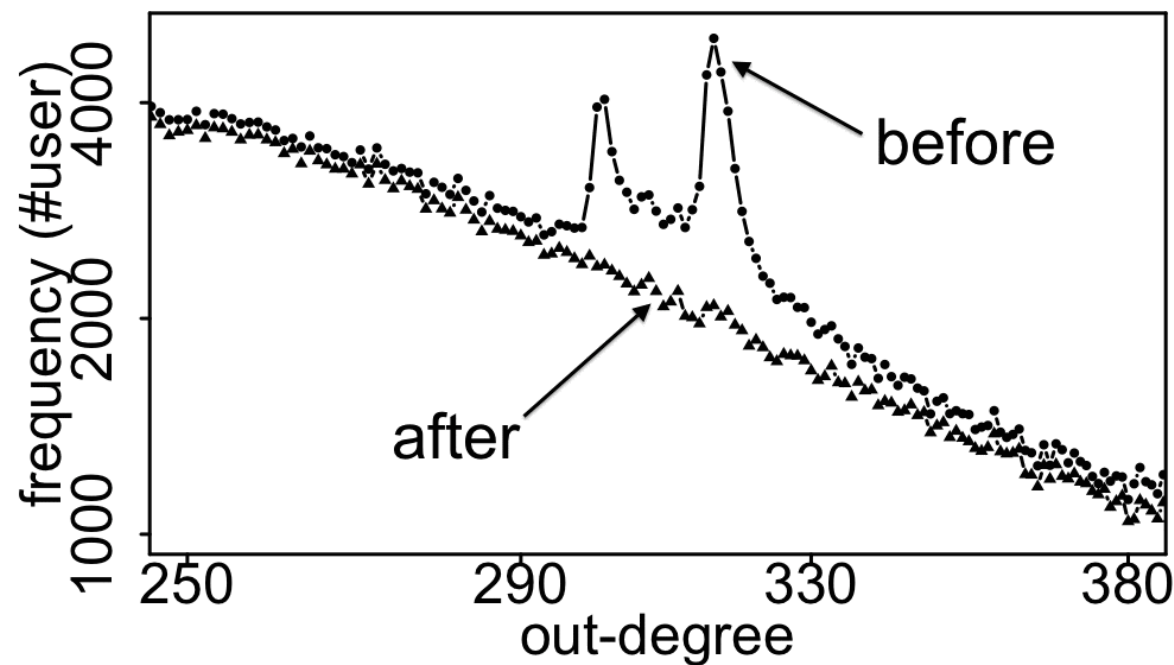
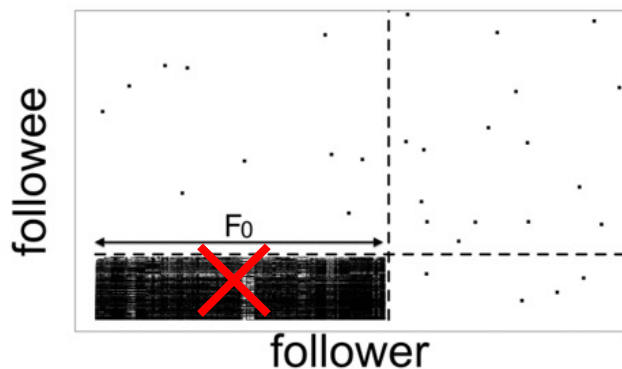
“Block”



Real Data



- Spikes on the out-degree distribution



Roadmap



- Introduction – Motivation
- Part#1: Patterns in graphs
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 - P1.2: Anomaly / fraud detection
 - No labels – spectral methods
 - No labels – **accounting application**
 - With labels: Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions



AutoAudit: Mining Accounting and Time-Evolving Graphs

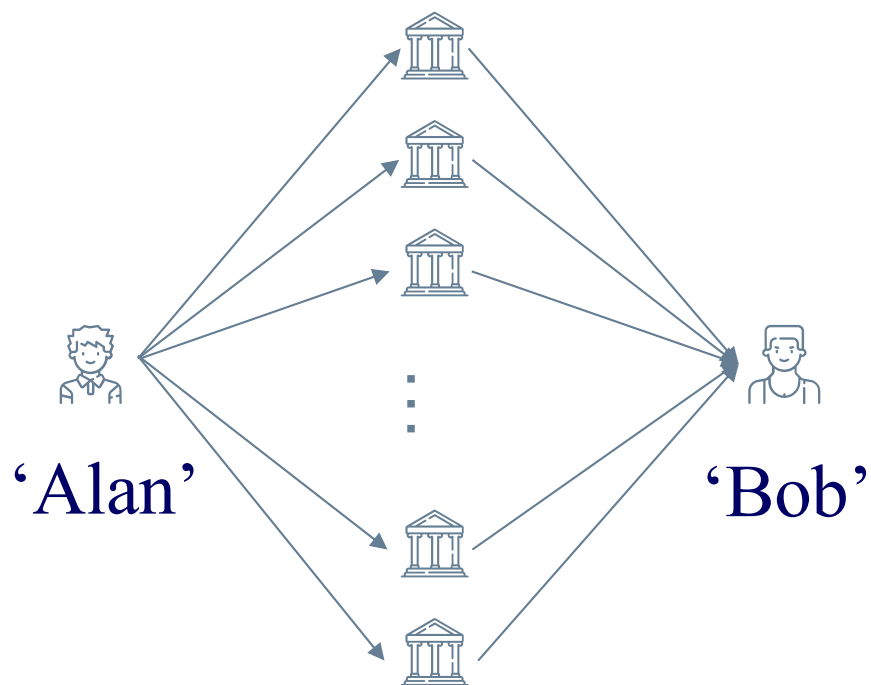
IEEE Big Data, 2020



Meng-Chieh Lee¹, Yue Zhao², Aluna Wang², Pierre Jinghong Liang²,
Leman Akoglu², Vincent S. Tseng¹, Christos Faloutsos²

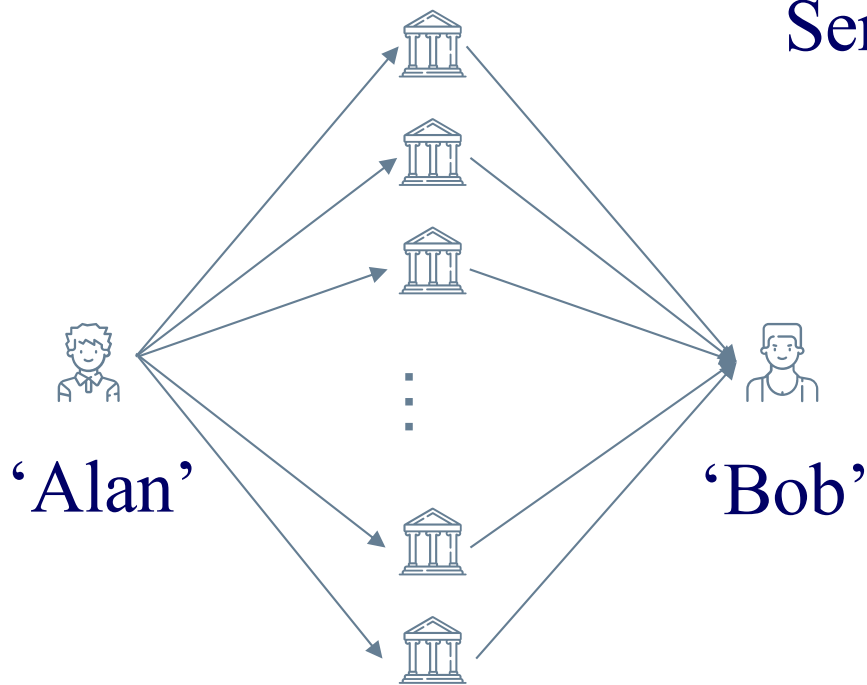


'Smurfing'



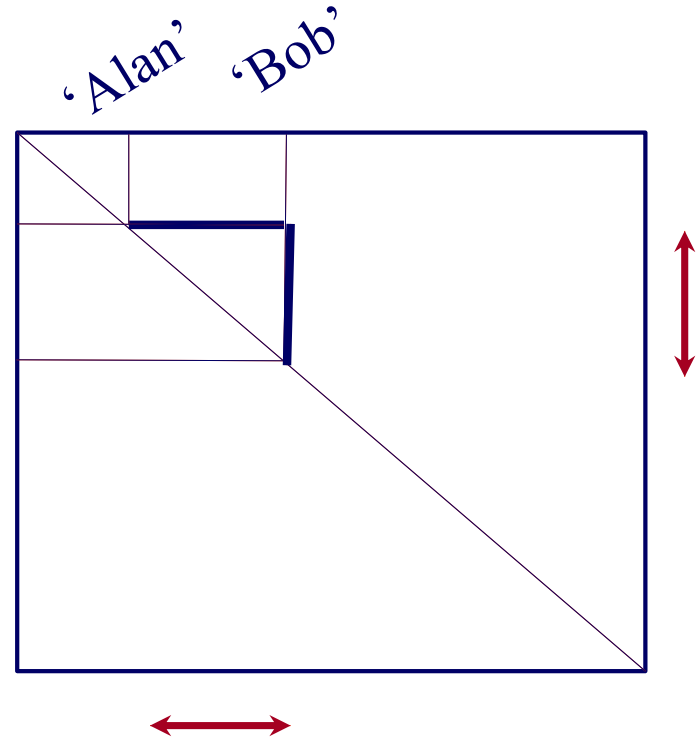
How to spot it?

'Smurfing'



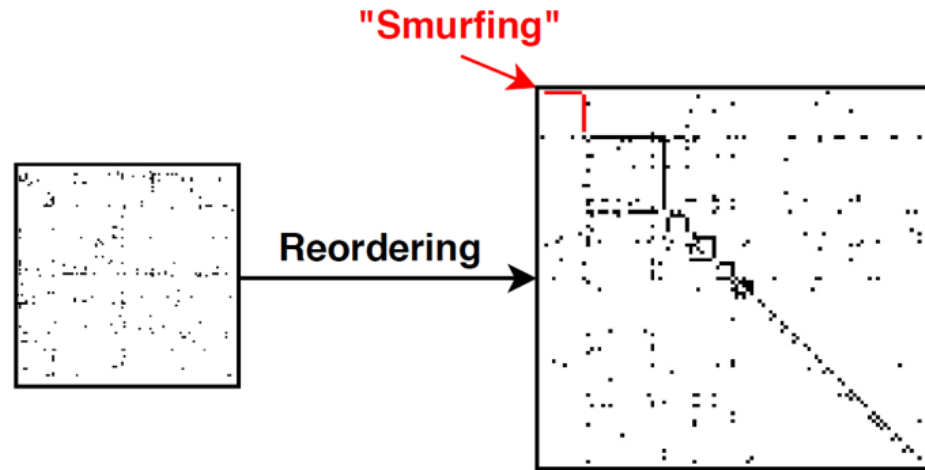
Receiver

Sender

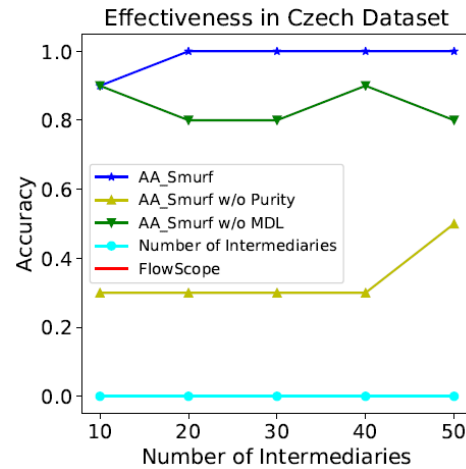
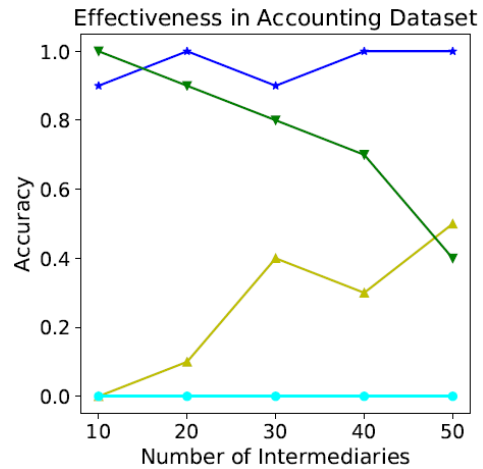


Reverse-'L' shape
(after careful re-ordering)

AutoAudit: Experiments



accuracy



← Ideal: 100%

Roadmap

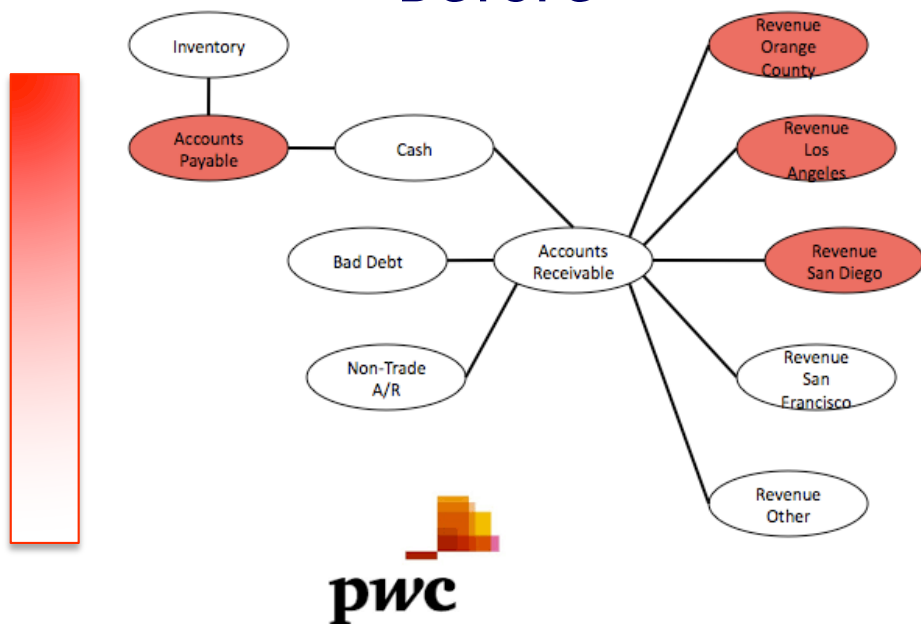
- Introduction – Motivation
- Part#1: Patterns in graphs
 - P1.1: Patterns
 - P1.2: Anomaly / fraud detection
 - No labels – spectral methods
 - No labels – dense subgraphs
 - With labels: Belief Propagation
- ➔
- Part#2: time-evolving graphs; tensors
- Conclusions



Network Effect Tools: SNARE

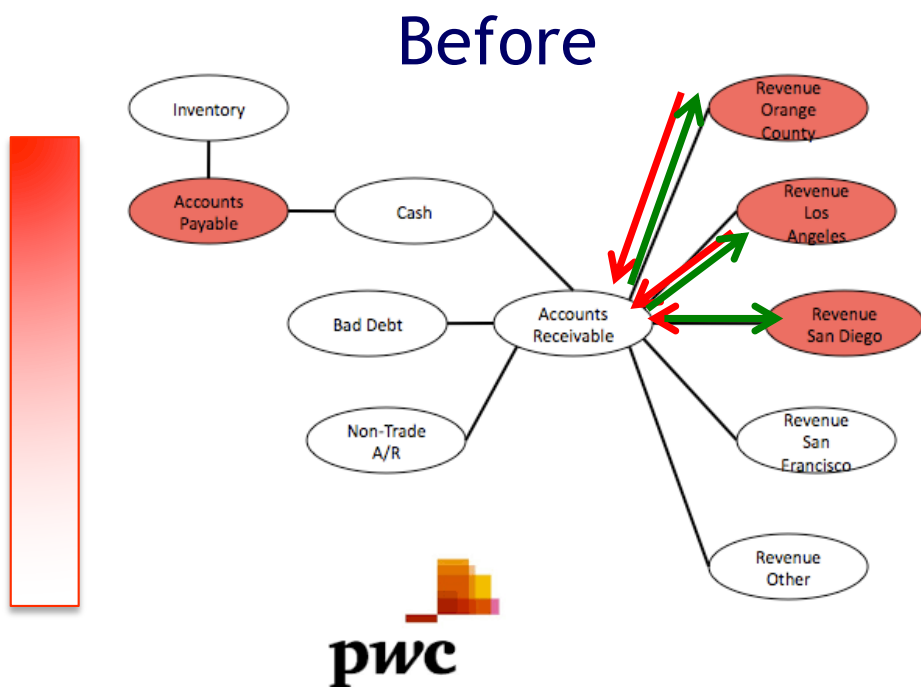
- Some accounts are sort-of-suspicious – how to combine weak signals?

Before



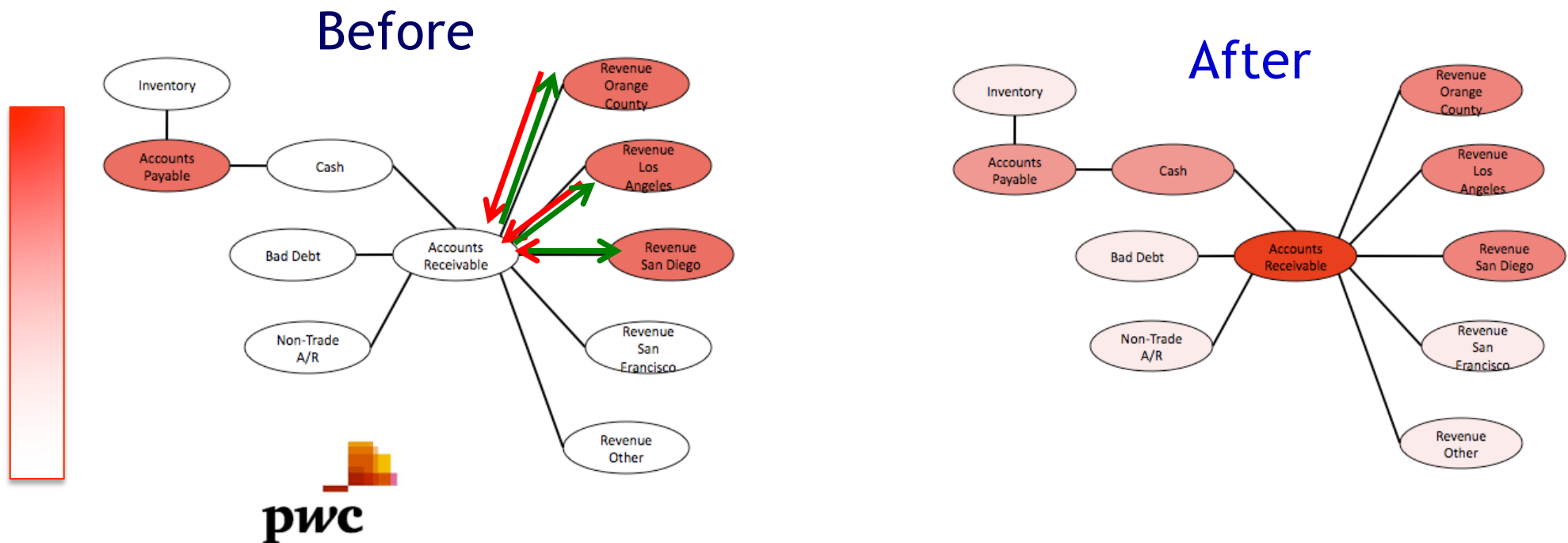
Network Effect Tools: SNARE

- A: Belief Propagation.



Network Effect Tools: SNARE

- A: Belief Propagation.

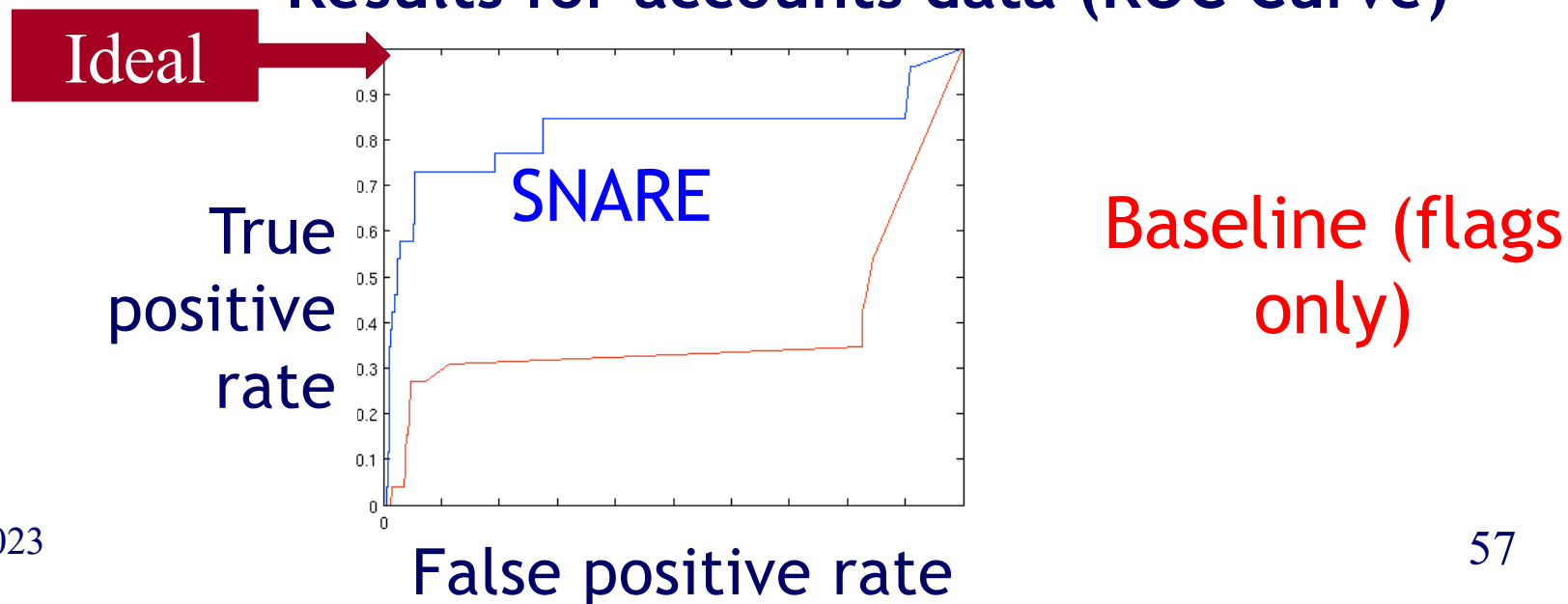


Mary McGlohon, Stephen Bay, Markus G. Anderle, David M. Steier, Christos Faloutsos: *SNARE: a link analytic system for graph labeling and risk detection*. KDD 2009: 1265-1274

Network Effect Tools: SNARE

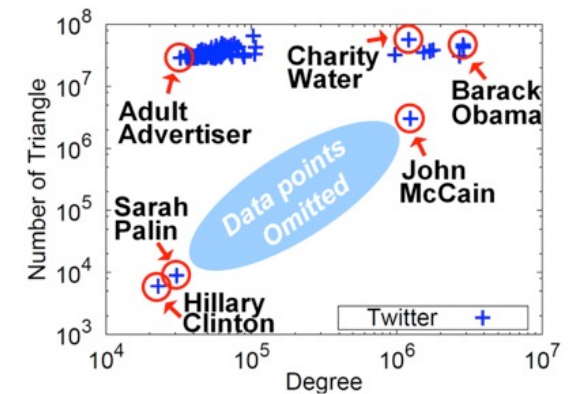
- Produces improvement over simply using flags
 - Up to 6.5 lift
 - Improvement especially for low false positive rate

Results for accounts data (ROC Curve)



Summary of Part#1

- **many** patterns in real graphs
 - Power-laws everywhere
 - Long (and growing) list of tools for anomaly/fraud detection



Patterns



anomalies

Roadmap

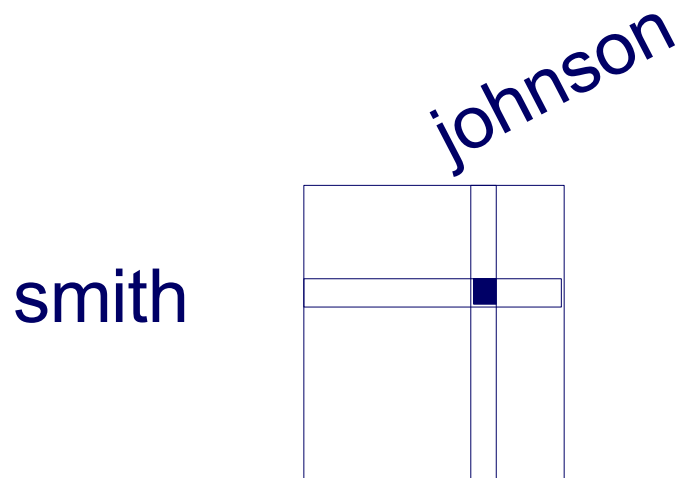
- Introduction – Motivation
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs
 - ➔ – P2.1: tools/tensors
 - P2.2: other patterns
- Conclusions



Part 2: Time evolving graphs; tensors

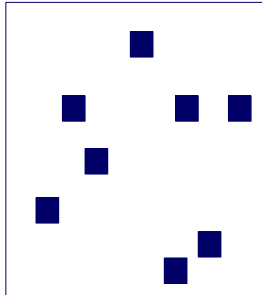
Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



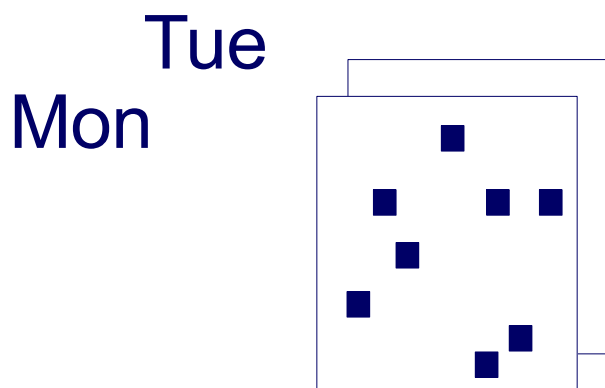
Graphs over time \rightarrow tensors!

- Problem #2.1:
 - Given who calls whom, and when
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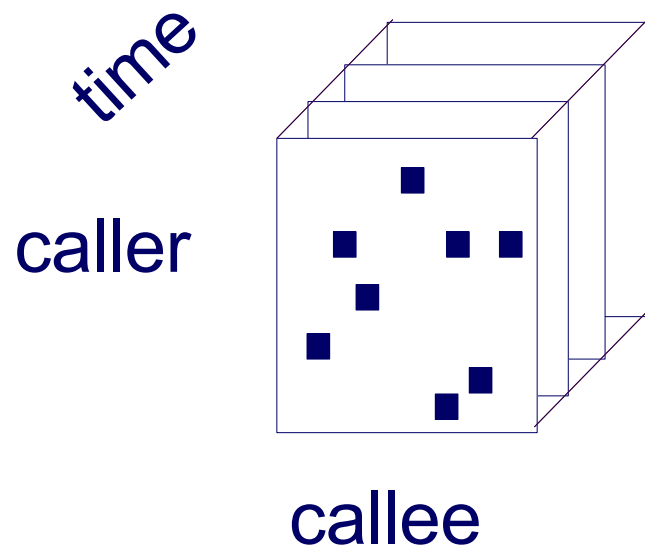
Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
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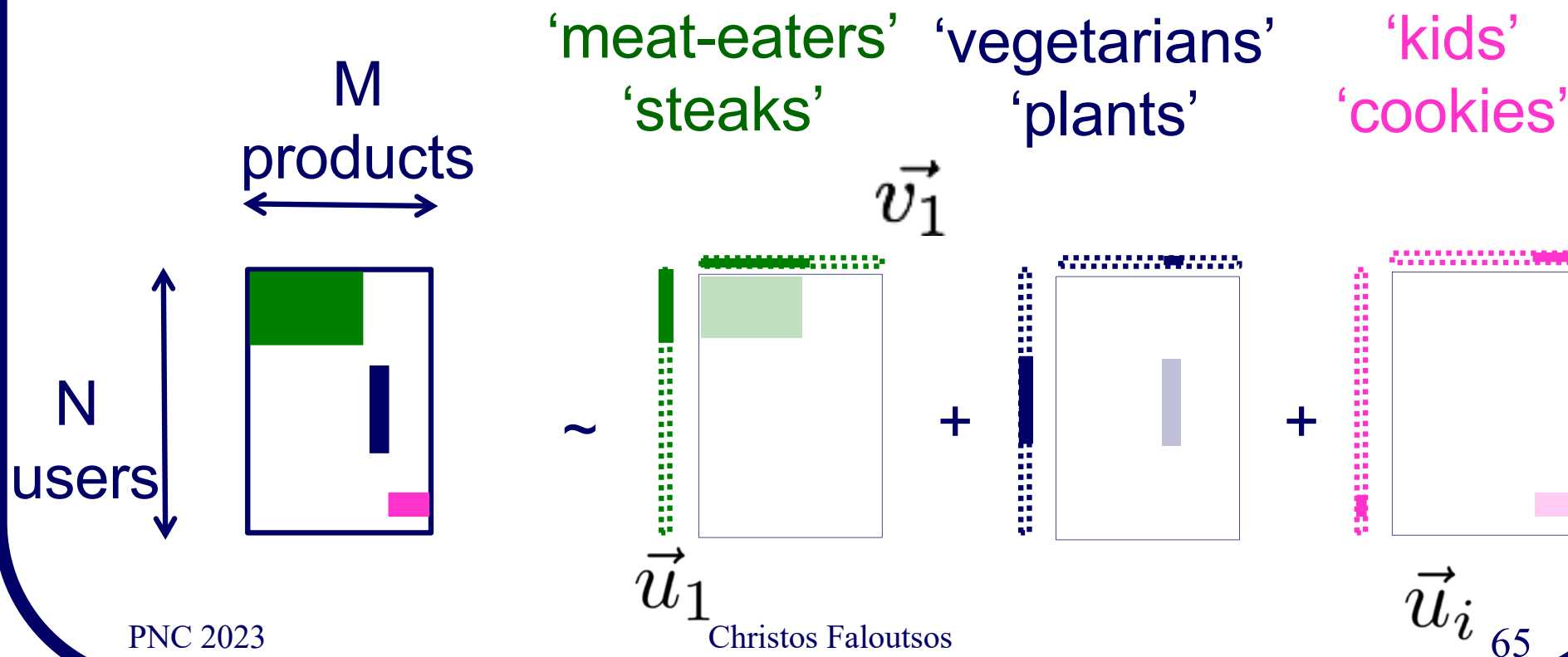
Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



Answer : tensor factorization

- Recall: (SVD) matrix factorization: finds blocks



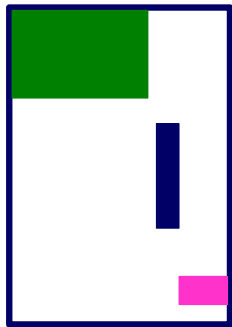
Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks



M
idols

N
fans

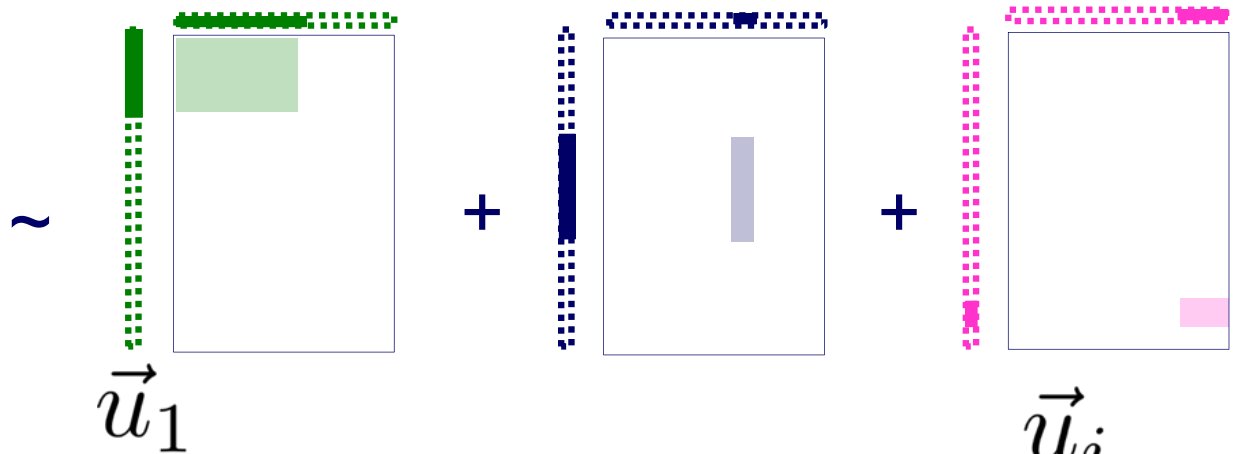


'music lovers'
'singers'

'sports lovers'
'athletes'

'citizens'
'politicians'

\vec{v}_1



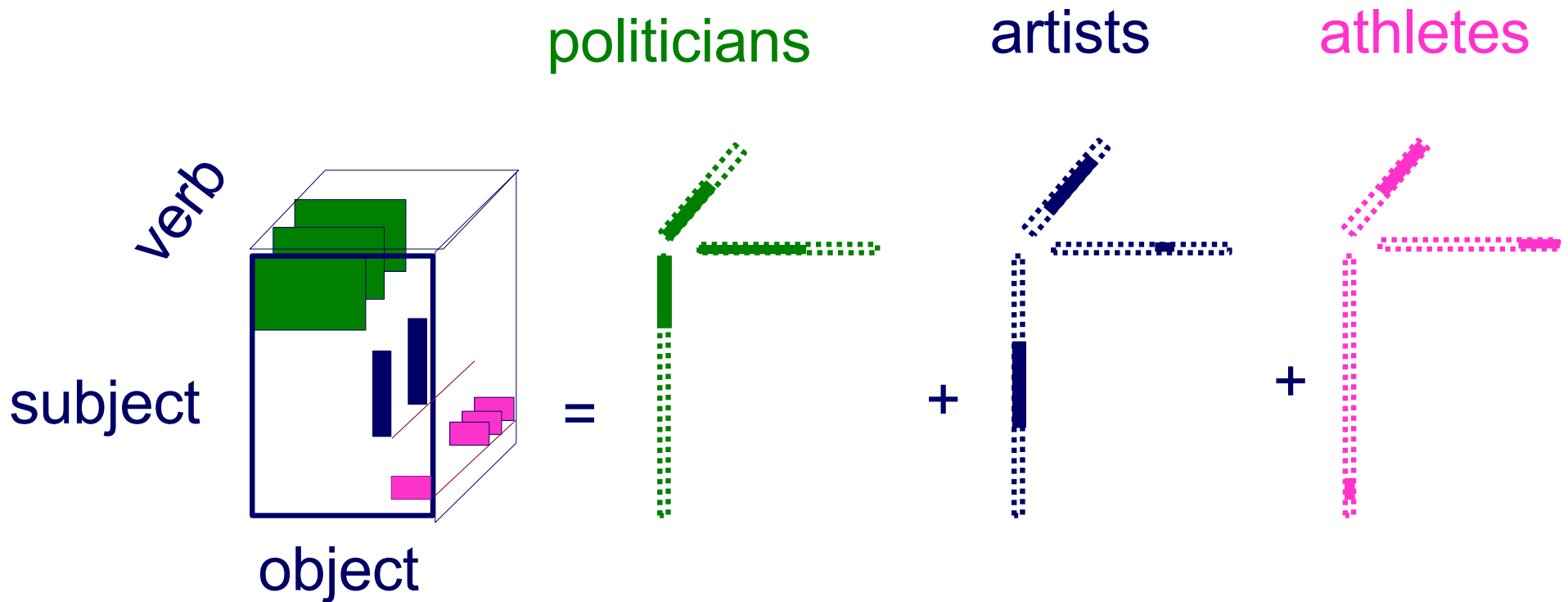
\vec{u}_1

Christos Faloutsos

\vec{u}_i 66

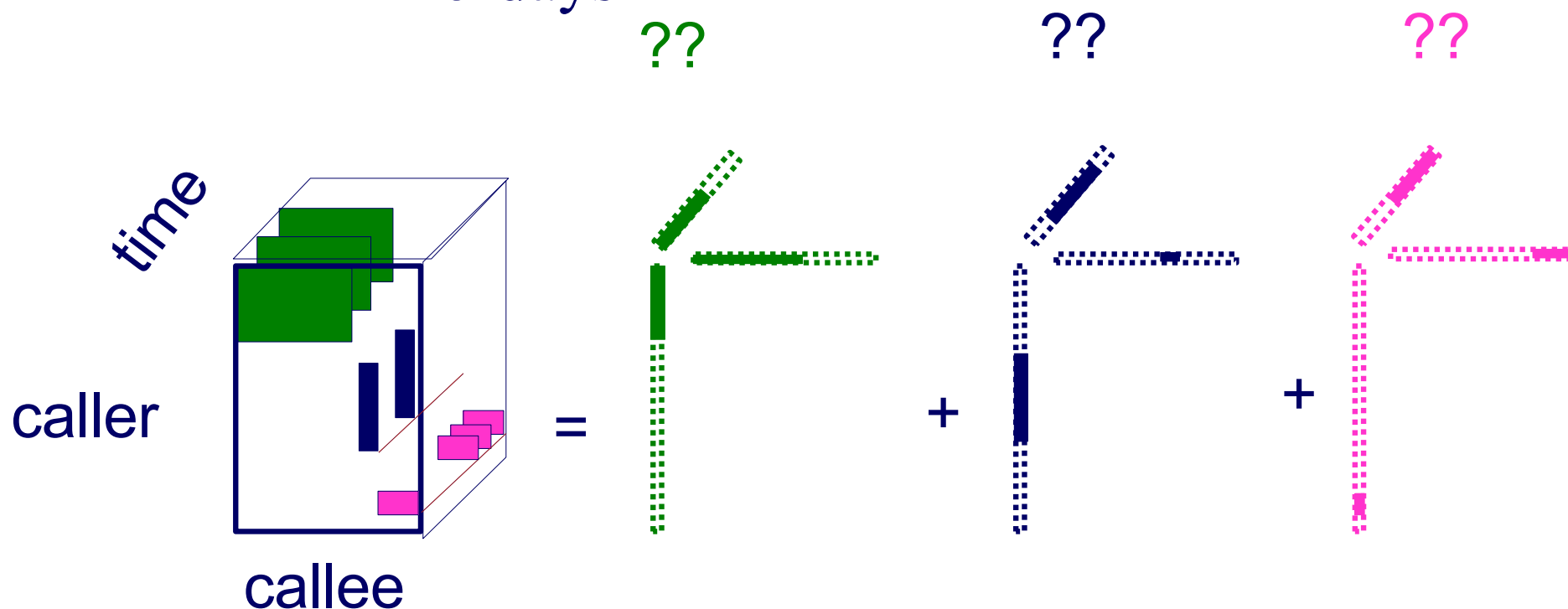
Answer: tensor factorization

- PARAFAC decomposition

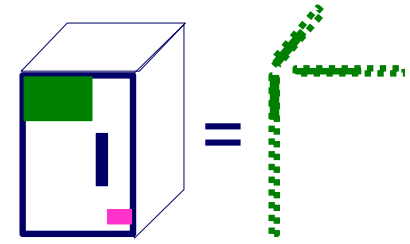


Answer: tensor factorization

- PARAFAC decomposition
- Results for who-calls-whom-when
 - 4M x 15 days

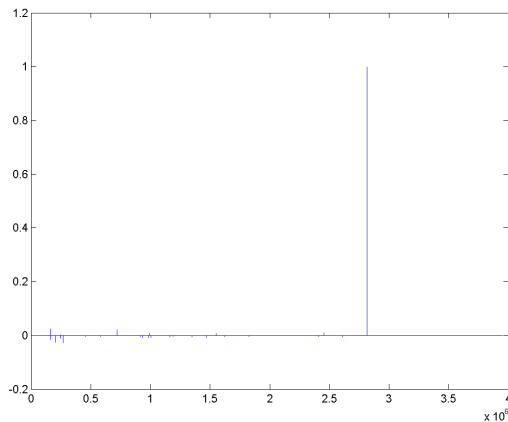


Anomaly detection in time-evolving graphs

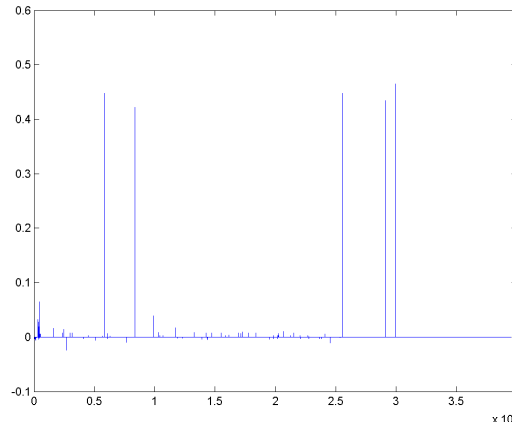


- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks

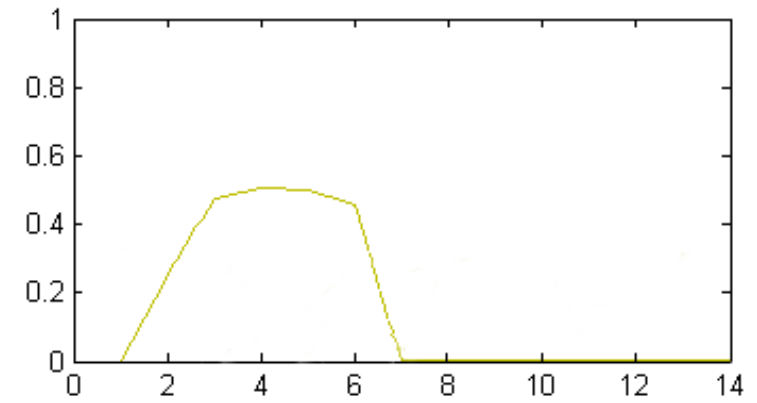
1 caller



5 receivers

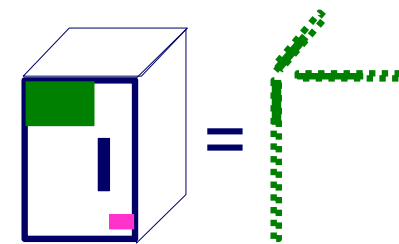


4 days of activity



~200 calls to EACH receiver on EACH day!

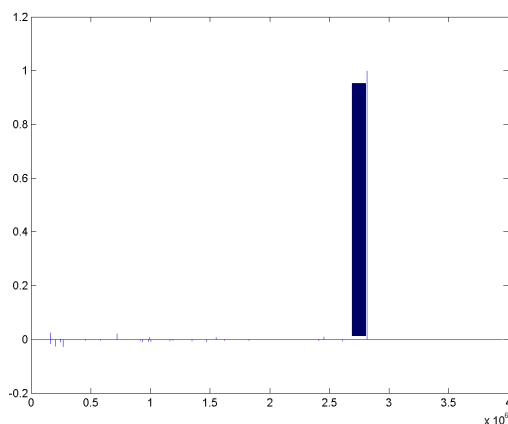
Anomaly detection in time-evolving graphs



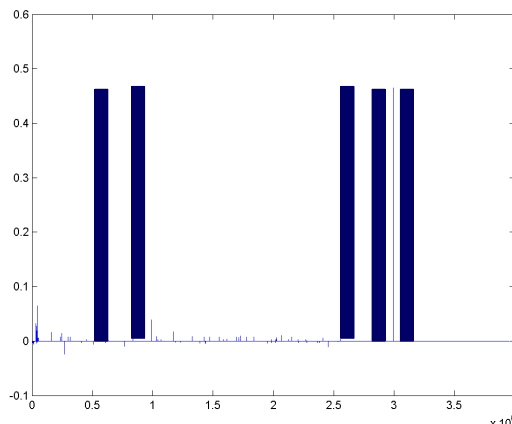
- Anomalous communities in phone call data:
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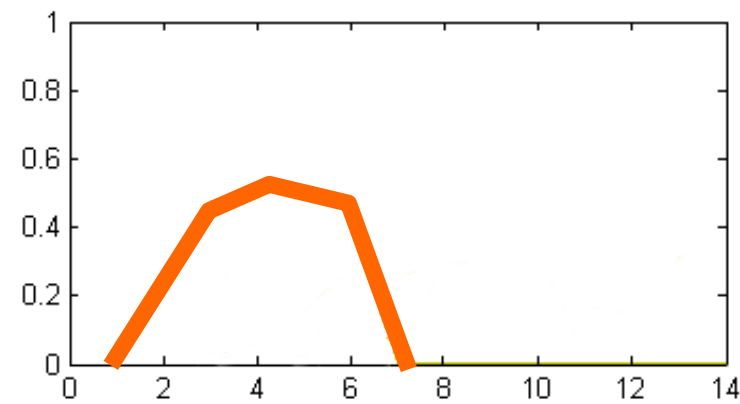
1 caller



5 receivers

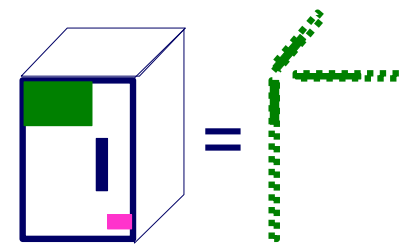


4 days of activity



~200 calls to EACH receiver on EACH day!

Anomaly detection in time-evolving graphs



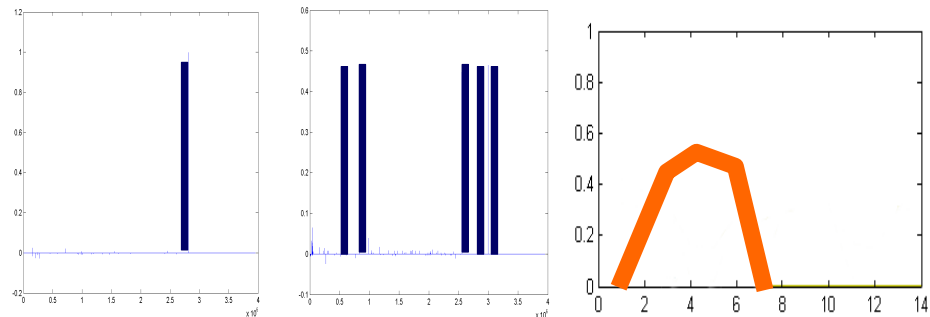
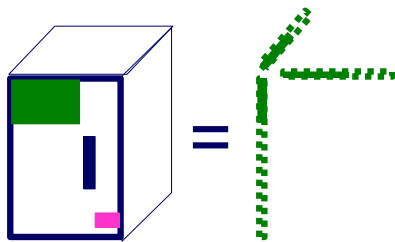
- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks



Miguel Araujo, Spiros Papadimitriou, Stephan Günnemann, Christos Faloutsos, Prithwish Basu, Ananthram Swami, Evangelos Papalexakis, Danai Koutra. *Com2: Fast Automatic Discovery of Temporal (Comet) Communities*. PAKDD 2014, Tainan, Taiwan.

Part 2: Conclusions

- Time-evolving / heterogeneous graphs \rightarrow tensors
- PARAFAC finds patterns
- Surprising temporal patterns



Roadmap

- Introduction – Motivation
 - Why study (big) graphs?
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- ➔ • Visualization
- Conclusions



TgraphSpot: Fast and Effective Anomaly Detection for Time-Evolving Graphs

IEEE BigData, 2022

Mirela Cazzolato^{1,2}, Saranya Vijayakumar¹, Xinyi Zheng¹,
Namyong Park¹, Meng-Chieh Lee¹, Pedro Fidalgo^{3,4},
Bruno Lages³, Agma J. M. Traina², Christos Faloutsos¹

CarnegieMellon



iscte

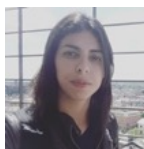
INSTITUTO
UNIVERSITÁRIO
DE LISBOA

Open source:

<https://github.com/mtcazzolato/tgraph-spot>

Video: <https://youtu.be/jI1adN-BQuo?t=1537>

Authors



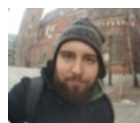
Mirela Cazzolato



Pedro Fidalgo



Saranya Vijayakumar



Bruno Lages



Xinyi Zheng



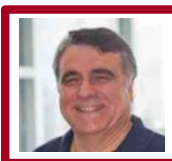
Agma Traina



Namyong Park

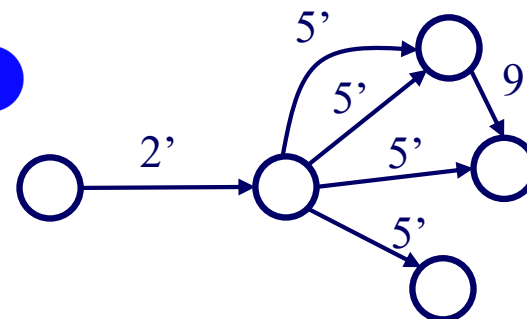
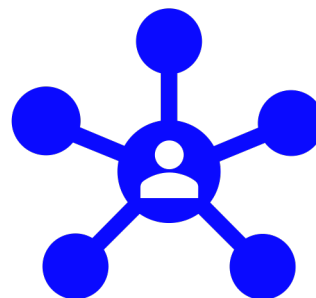


Meng-Chieh Jeremy Lee



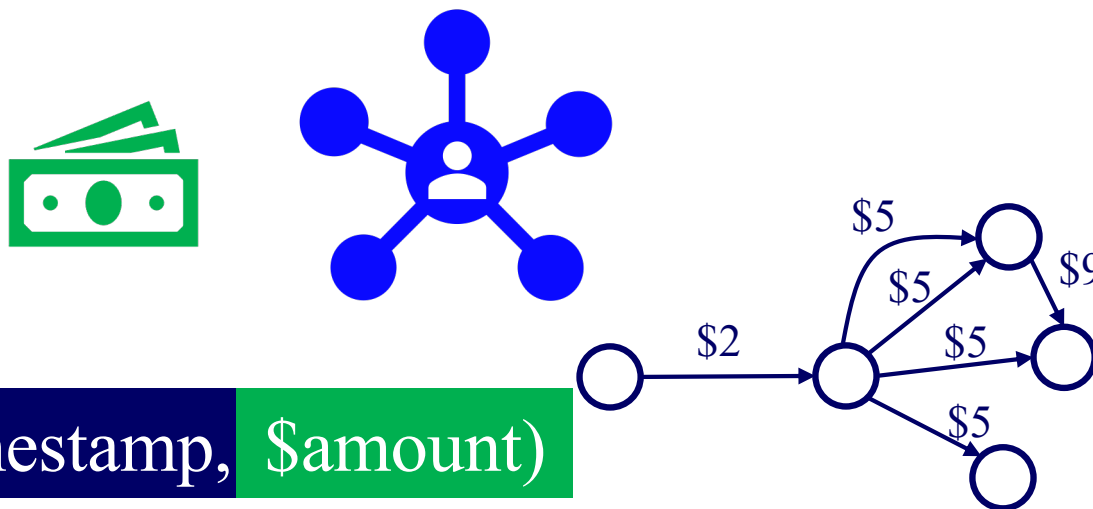
Christos Faloutsos

Problem definition



(source, destination, timestamp, duration)

Problem definition



(source, destination, timestamp, **\$amount**)

System Overview - current

Feature extraction

Extract features using t-graph

Enter input file path:
data/sample_raw_data.csv

Use example file

Selected file: data/sample_raw_data.csv

t-graph parameters

Select SOURCE column: source | Select MEASURE column: duration

Select DESTINATION column: destination | Select TIMESTAMP column: timestamp

Run t-graph

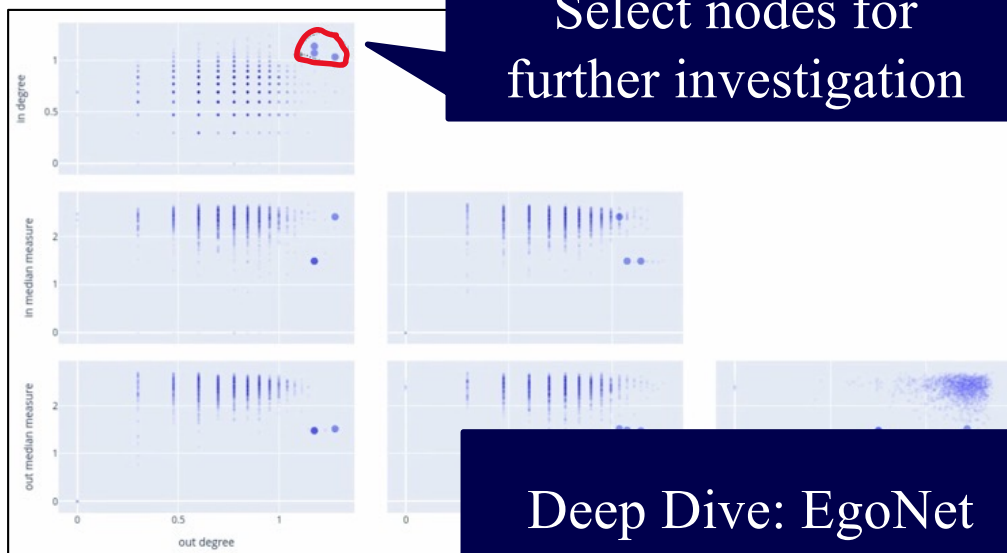
Finished extracting features. Check file 'data/features_nodevectors.csv'

Extracted features

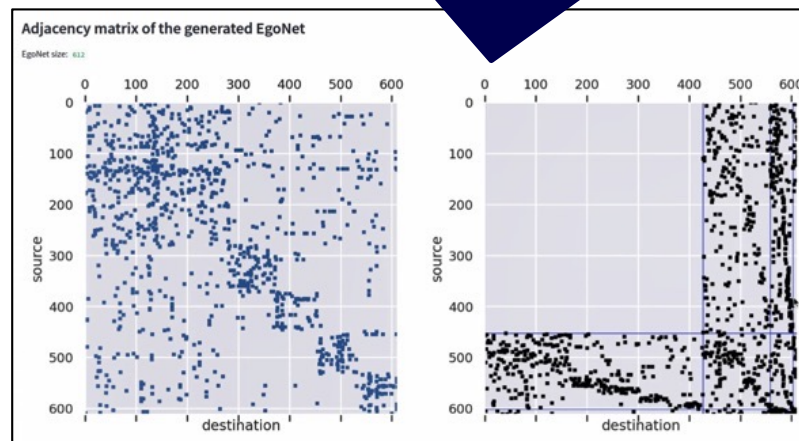
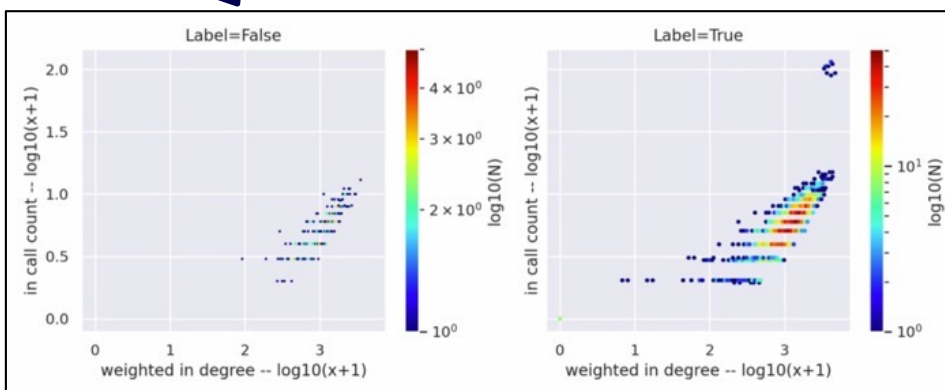
in_c	in_entropy	in_quantile_75	in_quantile_50	in_quantile_25
91,153.0000	0.0000	91,153.0000	91,153.0000	91,153.0000
65,572.0000	0.0000	65,572.0000	65,572.0000	65,572.0000
37,434.0000	1.1426	40,885.0000	48,009.0000	40,885.0000
25,179.0000	1.1793	32,413.0000	131,157.0000	32,413.0000

Feature extraction

Feature visualization



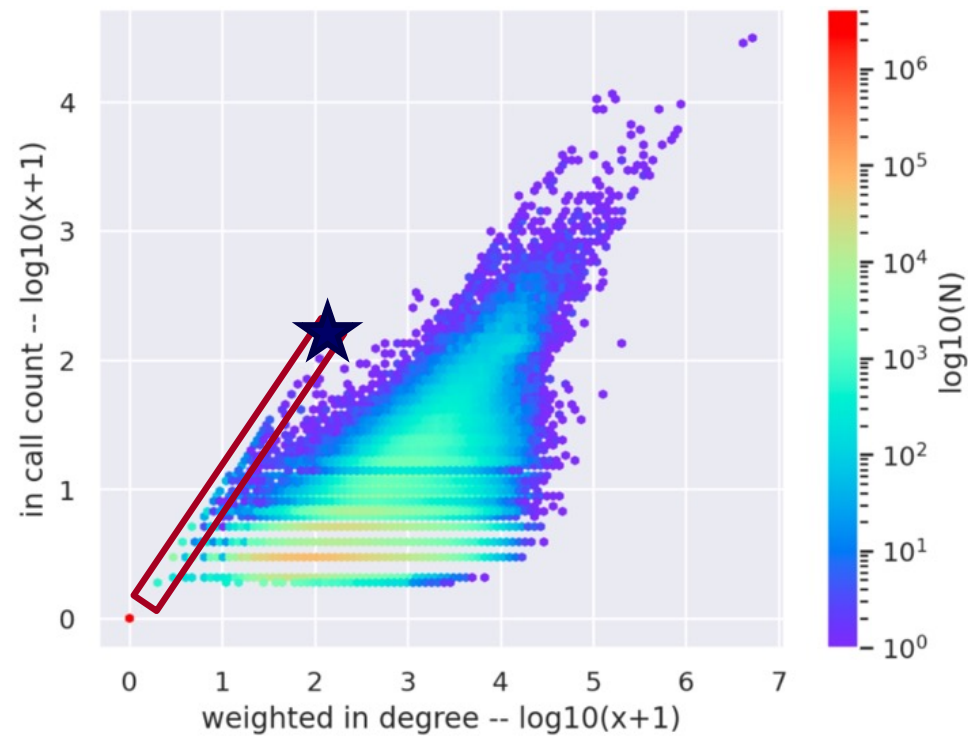
Deep Dive: EgoNet



Video: <https://youtu.be/jHladN-BQuo?t=1537>

Discovery #1

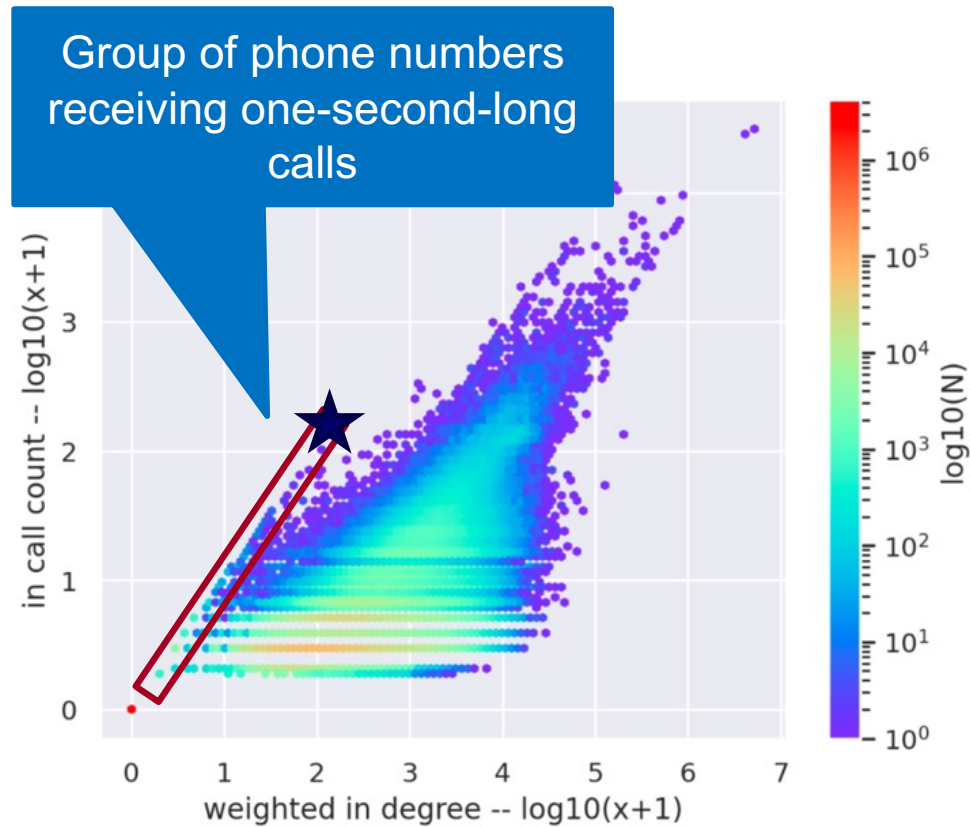
in-degree



Weighted in-degree (= in-seconds)

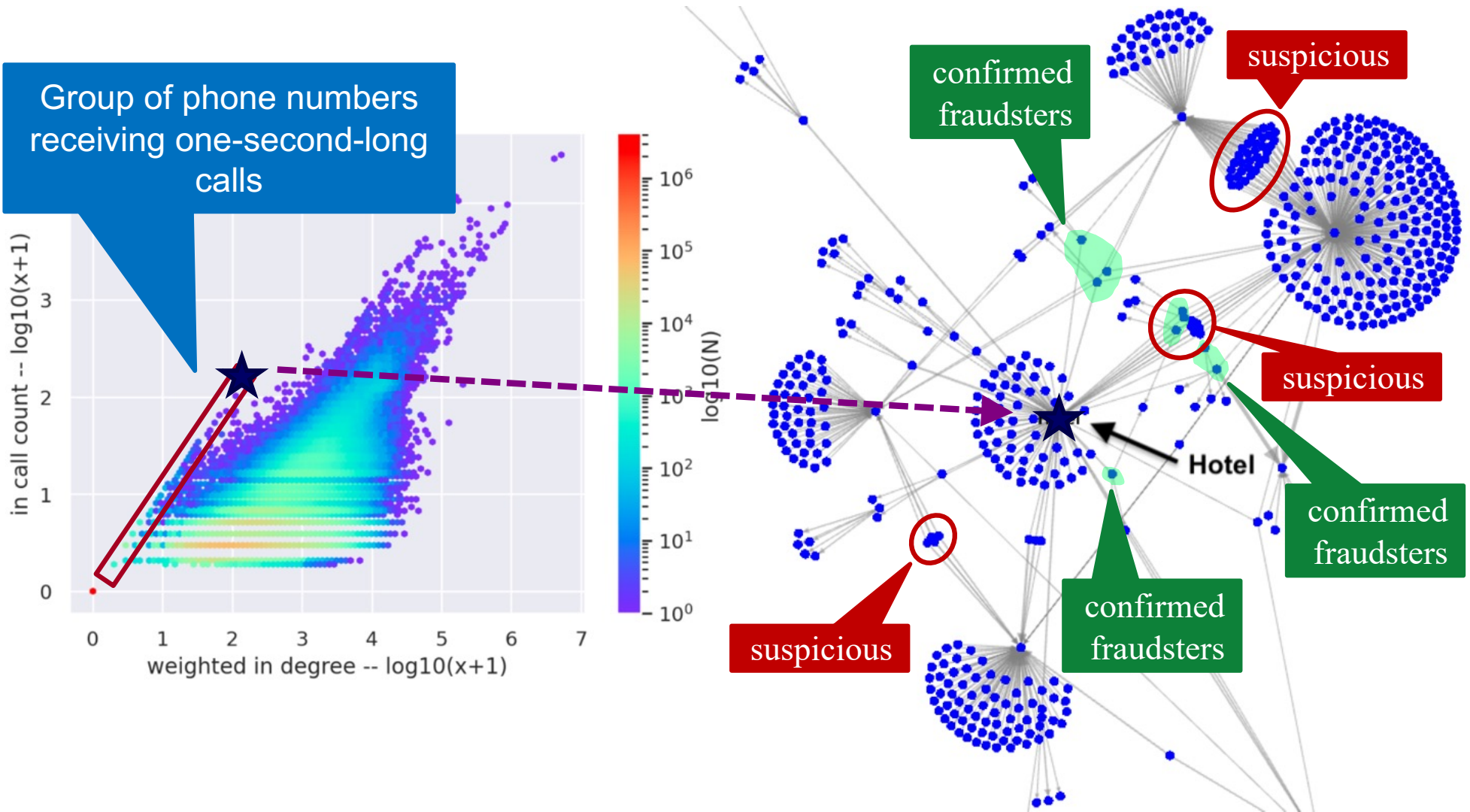
Discovery #1

100 in-calls
100 seconds



Discovery #1

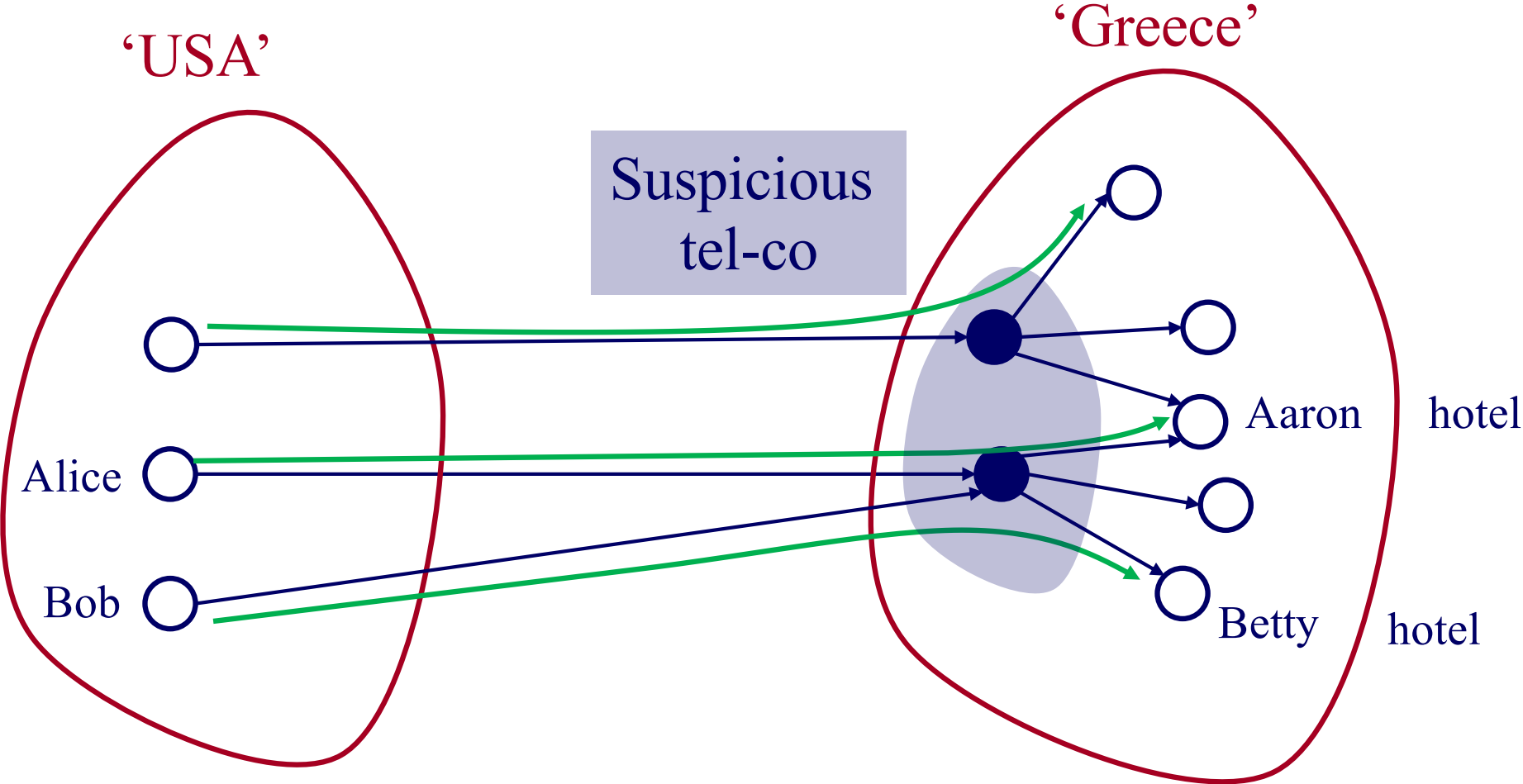
Group of phone numbers receiving one-second-long calls



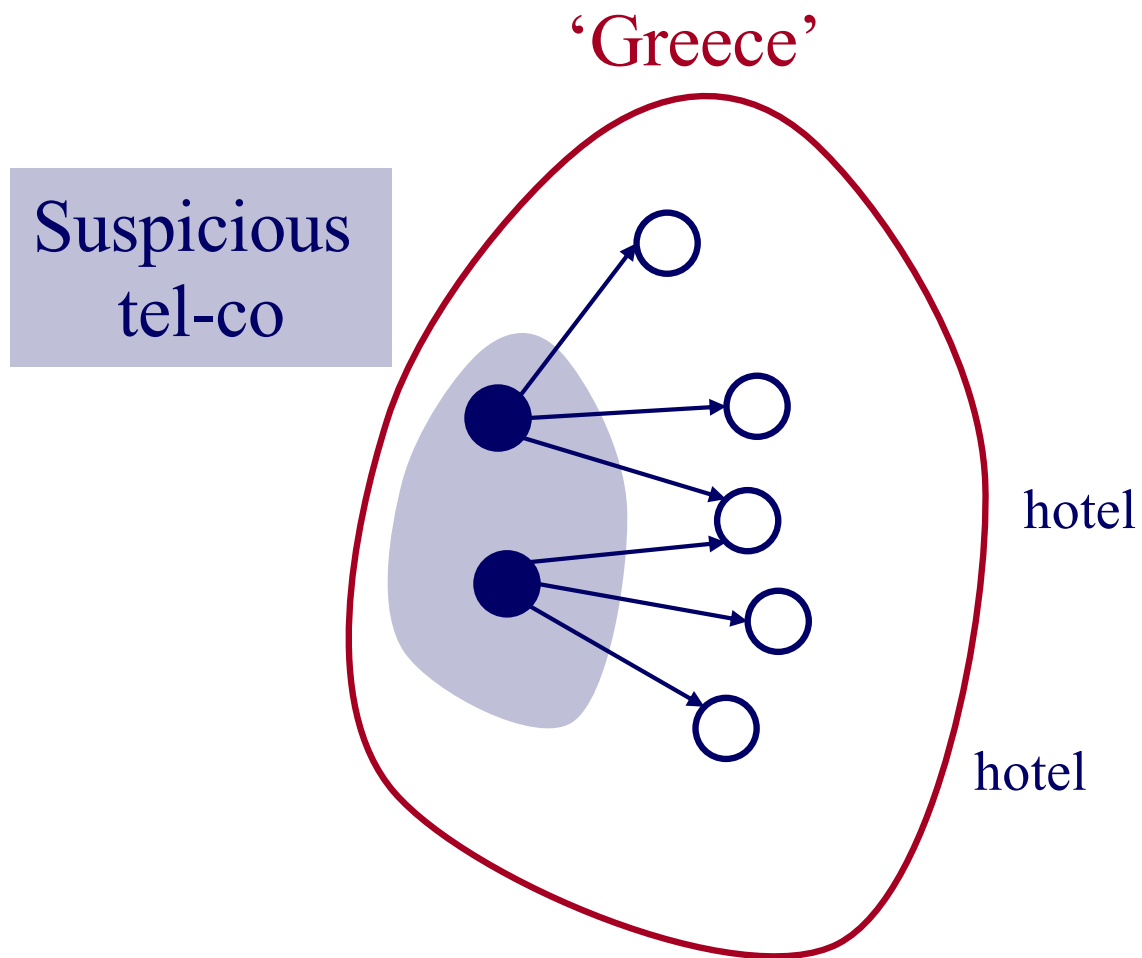
Q: Why?

- Q: Why would people call hotel-like numbers, for 1second?

A: 'international by-pass'



A: 'international by-pass'




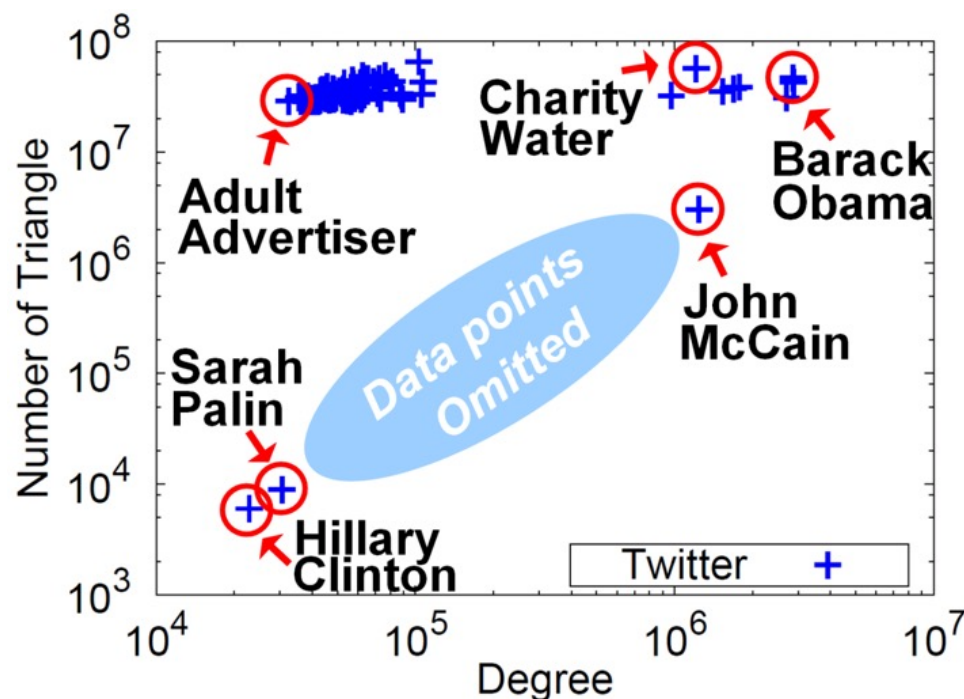
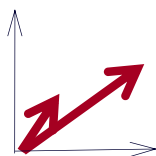
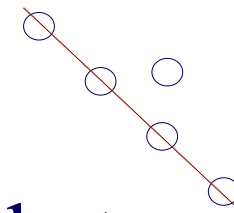
Roadmap

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- ➔ • Conclusions



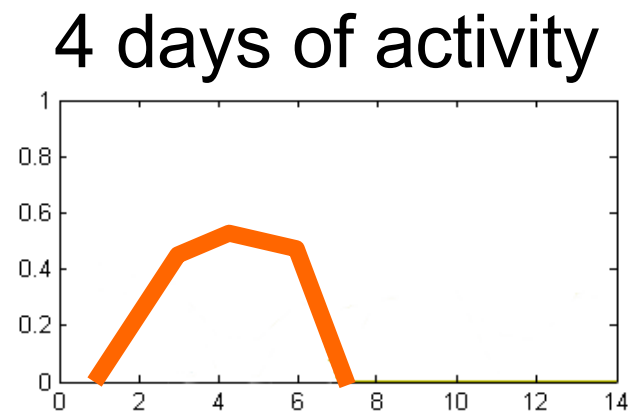
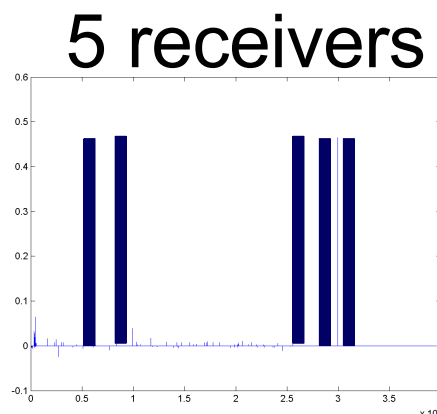
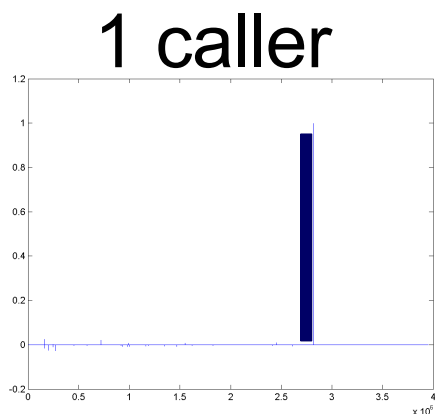
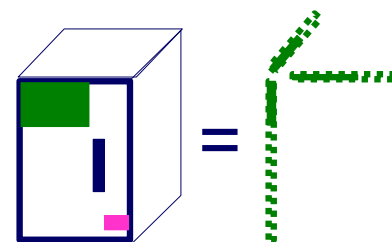
CONCLUSION#1 – Big data

- **Patterns**  **Anomalies**
- **Large datasets reveal patterns/outliers that are invisible otherwise**



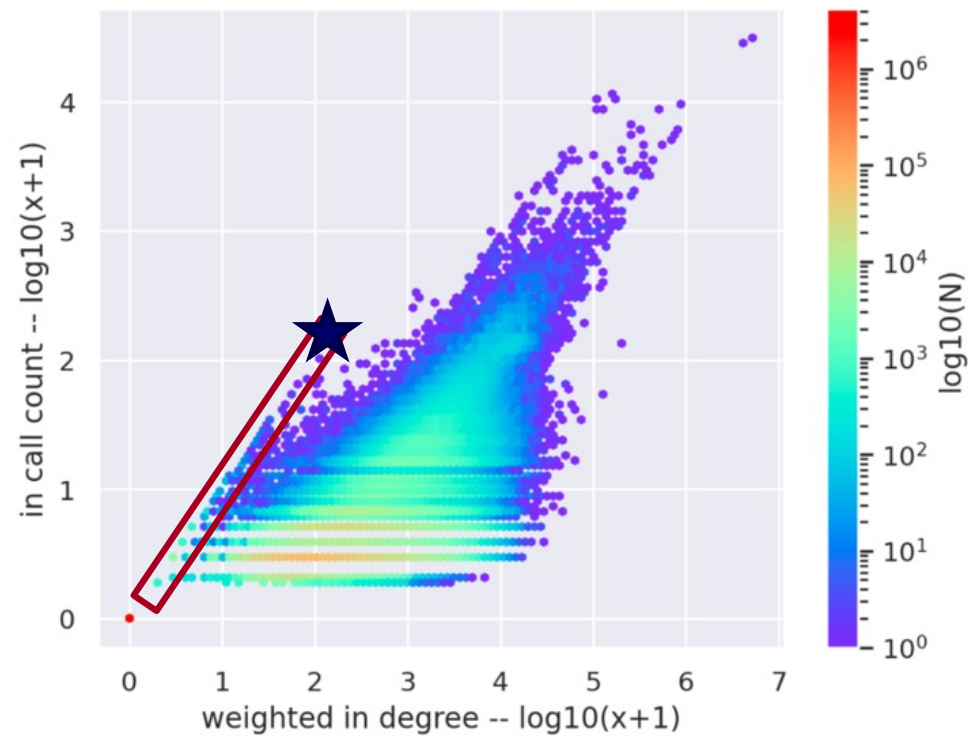
CONCLUSION#2 – tensors

- powerful tool



CONCLUSION#3 - visualization

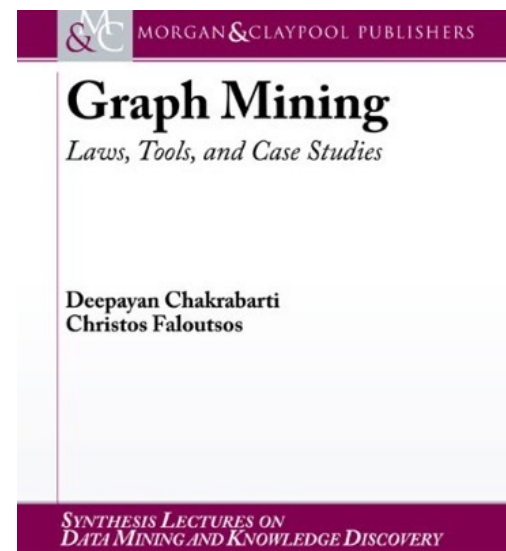
in-degree



Weighted in-degree (= in-seconds)

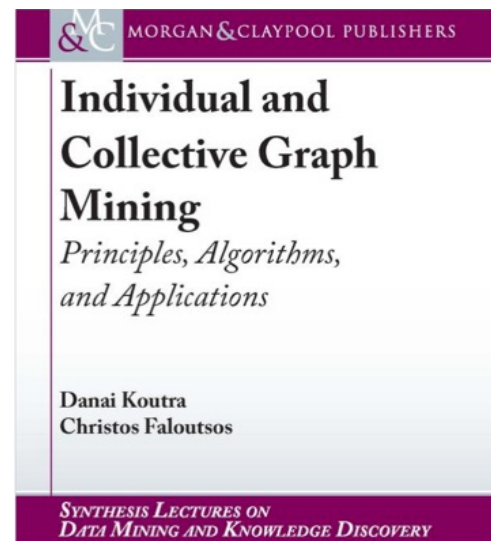
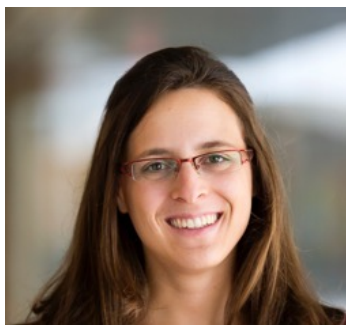
References

- D. Chakrabarti, C. Faloutsos: *Graph Mining – Laws, Tools and Case Studies*, Morgan Claypool 2012
- <http://www.morganclaypool.com/doi/abs/10.2200/S00449ED1V01Y201209DMK006>



References

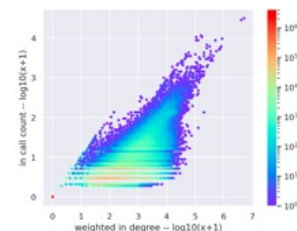
- Danai Koutra and Christos Faloutsos, *Individual and Collective Graph Mining: Principles, Algorithms, and Applications*, Morgan Claypool 2017
(<https://doi.org/10.2200/S00796ED1V01Y201708DMK014>)



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IEEE BigData, 2022

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Namyong Park¹, Meng-Chieh Lee¹, Pedro Fidalgo^{3,4},
Bruno Lages³, Agma J. M. Traina², Christos Faloutsos¹



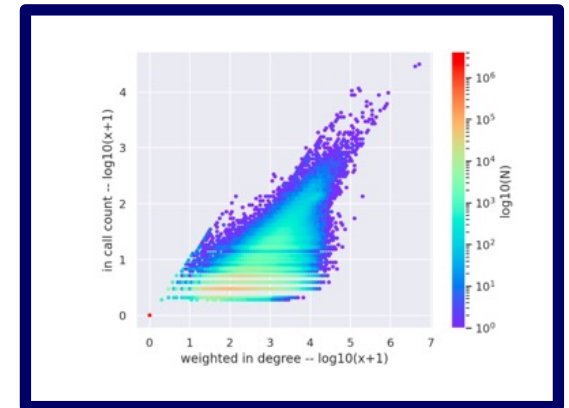
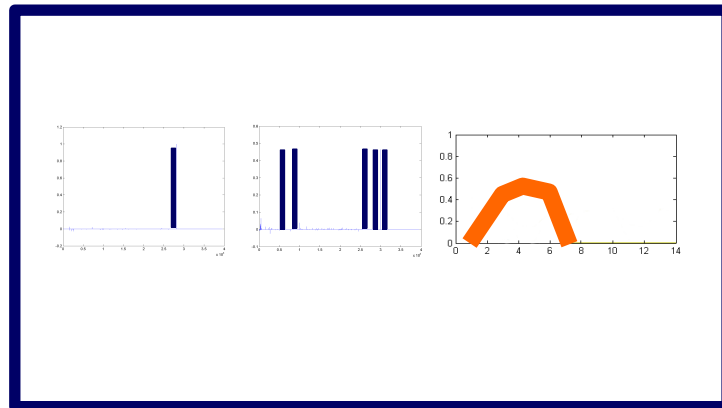
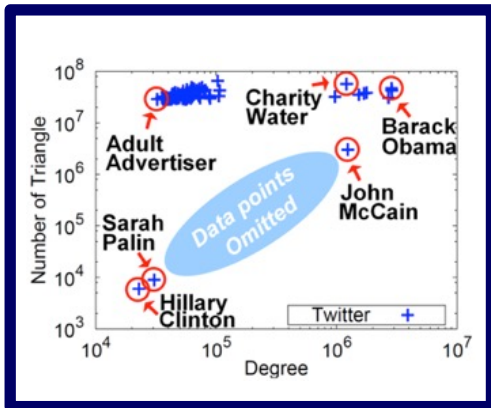
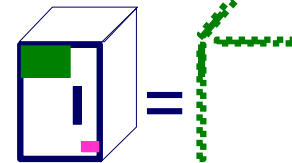
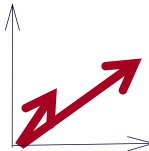
Open source:

<https://github.com/mtcazzolato/tgraph-spot>

Video: <https://youtu.be/jI1adN-BQuo?t=1537>

TAKE HOME MESSAGE:

Cross-disciplinarity



Thank you!

Cross-disciplinarity

