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Sensor Data Mining: Similarity Search and Pattern Analysis

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Thanks

 Deepay Chakrabarti (CMU)
Prof. Dimitris Gunopulos (UCR) 
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Outline

- ➔ Motivation
- Similarity Search and Indexing
- DSP (Digital Signal Processing)
- Linear Forecasting
- Bursty traffic - fractals and multifractals
- Non-linear forecasting
- Conclusions

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Problem definition

- Given: one or more sequences
 $x_1, x_2, \dots, x_t, \dots$
 $(y_1, y_2, \dots, y_p, \dots$
...)
- Find
 - similar sequences; forecasts
 - patterns; clusters; outliers

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Motivation - Applications

- Financial, sales, economic series
- Medical
 - ECGs +; blood pressure etc monitoring
 - reactions to new drugs
 - elderly care

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Motivation - Applications (cont'd)

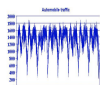
- ‘Smart house’
 - sensors monitor temperature, humidity, air quality
- video surveillance

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Motivation - Applications (cont'd)

- civil/automobile infrastructure
 - bridge vibrations [Oppenheim+02]
 - road conditions / traffic monitoring

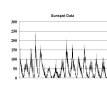


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Motivation - Applications (cont'd)

- Weather, environment/anti-pollution
 - volcano monitoring
 - air/water pollutant monitoring



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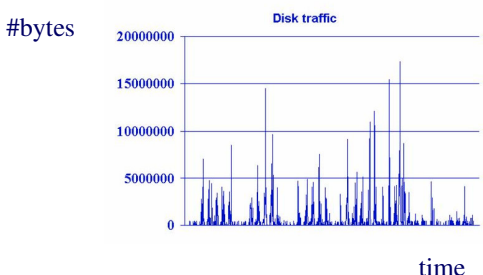
Motivation - Applications (cont'd)

- Computer systems
 - ‘Active Disks’ (buffering, prefetching)
 - web servers (ditto)
 - network traffic monitoring
 - ...

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Stream Data: Disk accesses



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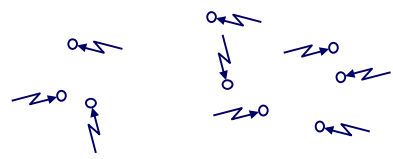
Settings & Applications

- One or more sensors, collecting time-series data

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Settings & Applications



Each sensor collects data $(x_1, x_2, \dots, x_p, \dots)$

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Settings & Applications

Some sensors 'report' to others or to the central site

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Settings & Applications

Goal #1:
Finding patterns
in a single time sequence

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Settings & Applications

Goal #2:
Finding patterns
in many time sequences

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Problem #1:

Goal: given a signal (e.g., #packets over time)
Find: patterns, periodicities, and/or compress

lynx caught per year
(packets per day;
temperature per day)

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Problem#2: Forecast

Given x_p, x_{t-1}, \dots , forecast x_{t+1}

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Problem#2': Similarity search

E.g., Find a 3-tick pattern, similar to the last one

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Problem #3:

- Given: A set of **correlated** time sequences
- Forecast 'Sent(t)'

Time Tick	sent	lost	repeated
1	40	20	20
2	55	25	25
3	75	35	25
4	45	20	30
5	55	25	20
6	65	30	25
7	80	40	30
8	75	35	35
9	60	25	35
10	50	25	30
11	45	25	25

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Differences from DSP/Stat

- Semi-infinite streams
 - we need on-line, 'any-time' algorithms
- Can not afford human intervention
 - need automatic methods
- sensors have limited memory / processing / transmitting power
 - need for (lossy) compression

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Important observations

Patterns, rules, forecasting and similarity indexing are closely related:

- To do forecasting, we need
 - to find patterns/rules
 - to find similar settings in the past
- to find outliers, we need to have forecasts
 - (outlier = too far away from our forecast)

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Important topics NOT in this tutorial:

- Continuous queries
 - [Babu+Widom] [Gehrke+] [Madden+]
- Categorical data streams
 - [Hatonen+96]
- Outlier detection (discontinuities)
 - [Breunig+00]
- Related (see D. Shasha's tutorial)

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Outline

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 - distance functions: Euclidean; Time-warping
 - indexing
 - feature extraction
- DSP
- ...

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Importance of distance functions

Subtle, but **absolutely necessary**:

- A 'must' for similarity indexing (-> forecasting)
- A 'must' for clustering

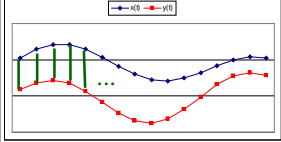
Two major families

- Euclidean and L_p norms
- Time warping and variations

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Euclidean and L_p



$$D(\bar{x}, \bar{y}) = \sum_{i=1}^n (x_i - y_i)^2$$

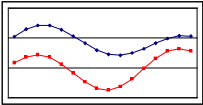
$$L_p(\bar{x}, \bar{y}) = \sum_{i=1}^n |x_i - y_i|^p$$

- L_1 : city-block = Manhattan
- L_2 = Euclidean
- L_∞

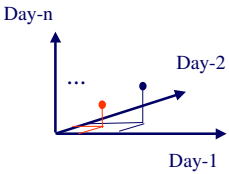
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Observation #1



- Time sequence -> n-d vector



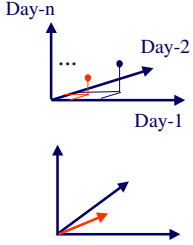
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Observation #2

Euclidean distance is closely related to

- cosine similarity
- dot product
- 'cross-correlation' function



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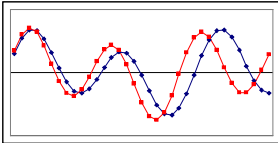
Time Warping

- allow accelerations - decelerations
 - (with or w/o penalty)
- THEN compute the (Euclidean) distance (+ penalty)
- related to the string-editing distance

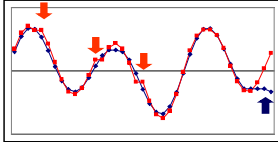
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Time Warping



'stutters':



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Time warping

Q: how to compute it?
 A: dynamic programming
 $D(i, j)$ = cost to match
 prefix of length i of first sequence x with prefix
 of length j of second sequence y

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Time warping **Time warping**

Thus, with no penalty for stutter, for sequences
 $x_1, x_2, \dots, x_i; \quad y_1, y_2, \dots, y_j$

$$D(i, j) = \|x[i] - y[j]\| + \min \begin{cases} D(i-1, j-1) & \text{no stutter} \\ D(i, j-1) & \text{x-stutter} \\ D(i-1, j) & \text{y-stutter} \end{cases}$$

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Time warping

- Complexity: $O(M*N)$ - quadratic on the length of the strings
- **Many** variations (penalty for stutters; limit on the number/percentage of stutters; ...)
- popular in voice processing [Rabiner+Juang]

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Other Distance functions

- piece-wise linear/flat approx.; compare pieces [Keogh+01] [Faloutsos+97]
- ‘cepstrum’ (for voice [Rabiner+Juang])
 - do DFT; take log of amplitude; do DFT again!
- Allow for small gaps [Agrawal+95]

See tutorial by [Gunopulos Das, SIGMOD01]

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Other Distance functions

- recently: parameter-free, MDL based [Keogh, KDD’04]

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Conclusions

Prevailing distances:

- Euclidean and
- time-warping

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 - feature extraction
- DSP
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Indexing

Problem:

- given a set of time sequences,
- find the ones similar to a desirable query sequence

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Price vs. day (1 to 365)

distance function: by expert

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Idea: 'GEMINI'

E.g., 'find stocks similar to MSFT'

Seq. scanning: too slow

How to accelerate the search?

[Faloutsos96]

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'GEMINI' - Pictorially

S1 vs. day (1 to 365)

Sn vs. day (1 to 365)

eg., std

$F(S1)$

eg., avg

$F(Sn)$

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GEMINI

Solution: Quick-and-dirty' filter:

- extract n features (numbers, eg., avg., etc.)
- map into a point in n -d feature space
- organize points with off-the-shelf spatial access method ('SAM')
- discard false alarms

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Examples of GEMINI

- Time sequences: DFT (up to 100 times faster) [SIGMOD94];
- [Kanellakis+], [Mendelzon+]

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Examples of GEMINI

Even on other-than-sequence data:

- Images (QBIC) [JIIS94]
- tumor-like shapes [VLDB96]
- video [Informedia + S-R-trees]
- automobile part shapes [Kriegel+97]

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Indexing - SAMs

Q: How do Spatial Access Methods (SAMs) work?

A: they group nearby points (or regions) together, on nearby disk pages, and answer spatial queries quickly ('range queries', 'nearest neighbor' queries etc)

For example:

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R-trees

Skip

- [Guttman84] eg., w/ fanout 4: group nearby rectangles to parent MBRs; each group -> disk page

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R-trees

Skip

- eg., w/ fanout 4:

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R-trees

Skip

- eg., w/ fanout 4:

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R-trees - range search?

Skip

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R-trees - range search?

Skip

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Conclusions

- Fast indexing: through GEMINI
 - feature extraction and
 - (off the shelf) Spatial Access Methods [Gaede+98]

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 - DFT, DWT, DCT (data independent)
 - SVD, etc (data dependent)
 - MDS, FastMap

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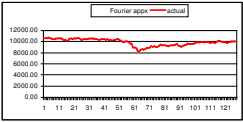
DFT and cousins

- very good for compressing real signals
- more details on DFT/DCT/DWT: later

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DFT and stocks

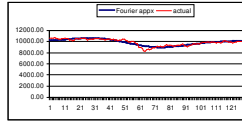
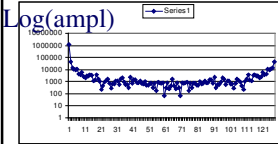


- Dow Jones Industrial index, 6/18/2001-12/21/2001

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DFT and stocks

- Dow Jones Industrial index, 6/18/2001-12/21/2001
- just 3 DFT coefficients give very good approximation

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SVD

- THE optimal method for dimensionality reduction
 - (under the Euclidean metric)

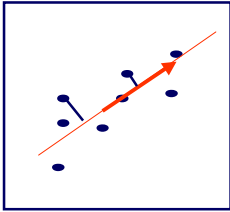
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Singular Value Decomposition (SVD)

- SVD (~LSI ~ KL ~ PCA ~ spectral analysis...)

day2



day1

LSI: S. Dumais; M. Berry
 KL: eg, Duda+Hart
 PCA: eg., Jolliffe
 Details: [Press+], [Faloutsos96]

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SVD

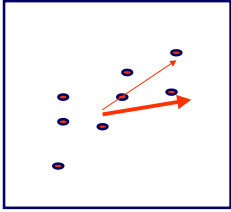
- Extremely useful tool
 - (also behind PageRank/google and Kleinberg's algorithm for hubs and authorities)
- But may be slow: $O(N * M * M)$ if $N > M$
- any approximate, faster method?

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SVD shortcuts

- random projections (Johnson-Lindenstrauss thm [Papadimitriou+ pods98])



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Random projections

- pick 'enough' random directions (will be ~orthogonal, in high-d!!)
- distances are preserved probabilistically, within epsilon
- (also, use as a pre-processing step for SVD [Papadimitriou+ PODS98])

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Feature extraction - w/ fractals Skip

- Main idea: drop those attributes that don't affect the intrinsic ('fractal') dimensionality [Traina+, SBBD 2000]
- i.e., drop attributes that depend on others (linearly or non-linearly!)

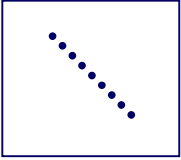
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Fractals Skip

Fractal dimension
= intrinsic dimension
~ degrees of freedom

Real data: often self-similar, with NON-INTEGER intrinsic dimension (!)



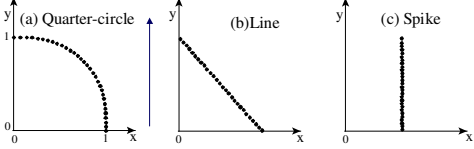
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Feature extraction - w/ fractals Skip

global FD=1

PFD~1



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MDS / FastMap

- but, what if we have NO points to start with?
(eg. Time-warping distance)
- A: Multi-dimensional Scaling (MDS) ;
FastMap

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MDS/FastMap

	O1	O2	O3	O4	O5
O1	0	1	1	100	100
O2	1	0	1	100	100
O3	1	1	0	100	100
O4	100	100	100	0	1
O5	100	100	100	1	0

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MDS

Multi Dimensional Scaling

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FastMap

- Multi-dimensional scaling (MDS) can do that, but in $O(N^2)$ time
- FastMap [Faloutsos+95] takes $O(N)$ time

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FastMap: Application

VideoTrails [Kobla+97]

scene-cut detection (about 10% errors)

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Conclusions - Practitioner's guide

Similarity search in time sequences

- 1) establish/choose distance (Euclidean, time-warping,...)
- 2) extract features (SVD, DWT, MDS), and use an SAM (R-tree/variant) or a Metric Tree (M-tree)
- 2') for high intrinsic dimensionalities, consider sequential scan (it might win...)

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Books

- William H. Press, Saul A. Teukolsky, William T. Vetterling and Brian P. Flannery: *Numerical Recipes in C*, Cambridge University Press, 1992, 2nd Edition. (Great description, intuition and code for SVD)
- C. Faloutsos: *Searching Multimedia Databases by Content*, Kluwer Academic Press, 1996 (introduction to SVD, and GEMINI)

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Part 2: DSP (Digital Signal Processing)

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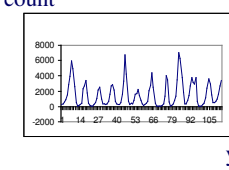
- ➔ • DFT
 - Definition of DFT and properties
 - how to read the DFT spectrum
- DWT
 - Definition of DWT and properties
 - how to read the DWT scalogram

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Introduction - Problem#1

Goal: given a signal (eg., packets over time)
Find: patterns and/or compress



lynx caught per year
(packets per day;
automobiles per hour)


year

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What does DFT do?

A: highlights the periodicities



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Skip

DFT: definition

- For a sequence x_0, x_1, \dots, x_{n-1}
- the **(n-point)** Discrete Fourier Transform is
- X_0, X_1, \dots, X_{n-1} :

$$X_f = 1/\sqrt{n} \sum_{t=0}^{n-1} x_t * \exp(-j2\pi tf/n) \quad f = 0, \dots, n-1$$

$(j = \sqrt{-1})$

$$x_t = 1/\sqrt{n} \sum_{f=0}^{n-1} X_f * \exp(+j2\pi tf/n) \quad \swarrow \text{inverse DFT}$$

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DFT: definition

- **Good news:** Available in **all** symbolic math packages, eg., in ‘mathematica’

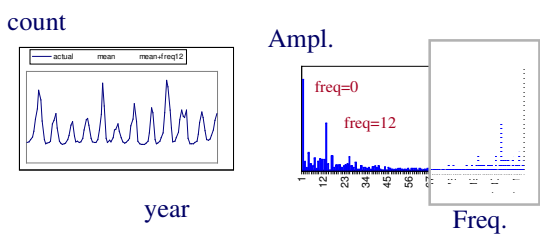
```
x = [1,2,1,2];
X = Fourier[x];
Plot[ Abs[X] ];
```

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DFT: Amplitude spectrum

Amplitude: $A_f^2 = \text{Re}^2(X_f) + \text{Im}^2(X_f)$



count

year

Ampl.

freq=0

freq=12

Freq.

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Outline

- Motivation
- Similarity Search and Indexing
- ➔ • DSP
- Linear Forecasting
- Bursty traffic - fractals and multifractals
- Non-linear forecasting
- Conclusions

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Outline

- Motivation
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 - Definition of DFT and properties
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 - DWT

➔

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DFT: Amplitude spectrum

Amplitude: $A_f^2 = \text{Re}^2(X_f) + \text{Im}^2(X_f)$

count

year

Ampl.

Freq.

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DFT: Amplitude spectrum

count

year

Ampl.

Freq.

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DFT: Amplitude spectrum

count

year

Ampl.

Freq.

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DFT: Amplitude spectrum

- excellent approximation, with only 2 frequencies!
- so what?

count

year

Ampl.

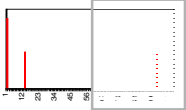
Freq.

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DFT: Amplitude spectrum

- excellent approximation, with only 2 frequencies!
- so what?
- A1: **(lossy) compression**
- A2: pattern discovery

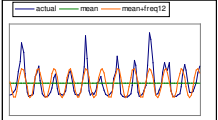


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DFT: Amplitude spectrum

- excellent approximation, with only 2 frequencies!
- so what?
- A1: (lossy) compression
- A2: **pattern discovery**



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DFT - Conclusions

- It spots periodicities (with the 'amplitude spectrum')
- can be quickly computed ($O(n \log n)$), thanks to the FFT algorithm.
- **standard** tool in signal processing (speech, image etc signals)
- (closely related to DCT and JPEG)

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Outline

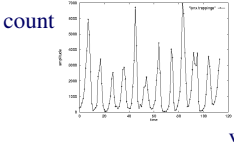
- Motivation
- Similarity Search and Indexing
- DSP
 - DFT
 - DWT
 - Definition of DWT and properties
 - how to read the DWT scalogram

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Problem #1:

Goal: given a signal (eg., #packets over time)
 Find: patterns, periodicities, and/or **compress**



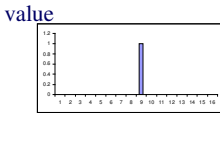
lynx caught per year
 (packets per day;
 virus infections per month)

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Wavelets - DWT

- DFT is great - but, how about compressing a spike?



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Wavelets - DWT

- DFT is great - but, how about compressing a spike?
- A: Terrible - all DFT coefficients needed!

The first plot shows a single vertical spike at time index 10 on a graph of value vs. time (1-16). The second plot shows the amplitude of the DFT coefficients, where the spike's energy is distributed across all 16 frequency bins.

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Wavelets - DWT

- DFT is great - but, how about compressing a spike?
- A: Terrible - all DFT coefficients needed!

The first plot is identical to the previous slide. The second plot shows the DWT coefficients, where the spike's energy is concentrated in a few low-frequency coefficients, demonstrating better compression.

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Wavelets - DWT

- Similarly, DFT suffers on short-duration waves (eg., baritone, silence, soprano)

The plot shows a complex waveform with varying frequencies and amplitudes over time, illustrating a signal where DFT would struggle to capture local features.

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Wavelets - DWT

- Solution#1: Short window Fourier transform (SWFT)
- But: how short should be the window?

The diagram shows a 4x4 grid of windows. The top-right and middle-left windows are shaded dark blue. To the right, a waveform is shown with a horizontal bar below it indicating the duration of the windows.

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Wavelets - DWT

- Answer: **multiple** window sizes! -> DWT

Time domain

freq

The diagram shows four representations: 1) Time domain: a single vertical line representing a single window size. 2) DFT: a grid with many horizontal lines, representing a single window size across all frequencies. 3) SWFT: a grid with a few horizontal lines, representing a short window size. 4) DWT: a grid with multiple horizontal lines of varying lengths, representing multiple window sizes.

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Haar Wavelets

- subtract sum of left half from right half
- repeat recursively for quarters, eight-ths, ...

The diagram shows the recursive construction of Haar wavelets. It starts with a single horizontal line, then shows a step function (difference between left and right halves), and then shows the resulting wavelet functions at different scales.

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Wavelets - construction

x0 x1 x2 x3 x4 x5 x6 x7

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Wavelets - construction

level 1 d1,0 s1,0 d1,1 s1,1

- + x0 x1 x2 x3 x4 x5 x6 x7

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Wavelets - construction

level 2 d2,0 s2,0

d1,0 s1,0 d1,1 s1,1

- + x0 x1 x2 x3 x4 x5 x6 x7

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Wavelets - construction

etc ...

d2,0 s2,0

d1,0 s1,0 d1,1 s1,1

- + x0 x1 x2 x3 x4 x5 x6 x7

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Wavelets - construction

Q: map each coefficient on the time-freq. plane

f

t

d2,0 s2,0

d1,0 s1,0 d1,1 s1,1

- + x0 x1 x2 x3 x4 x5 x6 x7

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Wavelets - construction

Q: map each coefficient on the time-freq. plane

f

t

d2,0 s2,0

d1,0 s1,0 d1,1 s1,1

- + x0 x1 x2 x3 x4 x5 x6 x7

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Haar wavelets - code

```

#!/usr/bin/perl
# expects a file with numbers
# and prints the dwt transform
# The number of time-ticks should be a power of 2
# USAGE
# haar.pl <filename>

my @vals=();
my @smooth; # the smooth component of the signal
my @diff; # the high-freq. component

# collect the values into the array @val
while(<@>){
    @vals = ( @vals , split );
}

my $len = scalar(@vals);
my $half = int($len/2);
while($half >= 1 ){
    for(my $i=0; $i< $half; $i++){
        $diff[$i] = ($vals[2*$i] - $vals[2*$i + 1]) / sqrt(2);
        print "d", $diff[$i];
        $smooth[$i] = ($vals[2*$i] + $vals[2*$i + 1]) / sqrt(2);
    }
    print "\n";
    @vals = @smooth;
    $half = int($half/2);
}
print "a", $vals[0], "\n"; # the final, smooth component
    
```

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Wavelets - construction

Observation1:
 '+' can be some weighted addition
 '-' is the corresponding weighted difference
 ('Quadrature mirror filters')

Observation2: unlike DFT/DCT,
 there are *many* wavelet bases: Haar, Daubechies-4, Daubechies-6, Coifman, Morlet, Gabor, ...

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Wavelets - how do they look like?

- E.g., Daubechies-4

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Wavelets - how do they look like?

- E.g., Daubechies-4

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Wavelets - how do they look like?

- E.g., Daubechies-4

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Outline

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Wavelets - Drill#1:

- Q: baritone/silence/soprano - DWT?

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Wavelets - Drill#1:

- Q: baritone/soprano - DWT?

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Wavelets - Drill#2:

- Q: spike - DWT?

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Wavelets - Drill#2:

- Q: spike - DWT?

0.00	0.00	0.71	0.00
0.00	0.50		
	-0.35		
	0.35		

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Wavelets - Drill#3:

- Q: weekly + daily periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: weekly + daily periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: weekly + **daily** periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: weekly + daily periodicity, + **spike** - DWT?

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Wavelets - Drill#3:

- Q: weekly + daily periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: DFT?

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Advantages of Wavelets

- Better compression (better RMSE with same number of coefficients - used in JPEG-2000)
- fast to compute (usually: $O(n)$!)
- very good for 'spikes'
- mammalian eye and ear: Gabor wavelets

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Overall Conclusions

- DFT, DCT spot periodicities
- DWT** : multi-resolution - matches processing of mammalian ear/eye better
- All three: powerful tools for **compression, pattern detection** in real signals
- All three: included in math packages - (matlab, 'R', mathematica, ... - often in spreadsheets!)

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Overall Conclusions

- DWT : very suitable for self-similar traffic
- DWT: used for summarization of streams [Gilbert+01], db histograms etc

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Resources - software and urls

- <http://www.dsptutor.freeuk.com/jsanalyser/FFTSpectrumAnalyser.html> : Nice java applets for FFT
- <http://www.relisoft.com/freeware/freq.html> voice frequency analyzer (needs microphone)

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Resources: software and urls

- *xwpl*: open source wavelet package from Yale, with excellent GUI
- <http://monet.me.ic.ac.uk/people/gavin/java/waveletDemos.html> : wavelets and scalograms

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Books

- William H. Press, Saul A. Teukolsky, William T. Vetterling and Brian P. Flannery: *Numerical Recipes in C*, Cambridge University Press, 1992, 2nd Edition. (Great description, intuition and code for DFT, DWT)
- C. Faloutsos: *Searching Multimedia Databases by Content*, Kluwer Academic Press, 1996 (introduction to DFT, DWT)

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Additional Reading

- [Gilbert+01] Anna C. Gilbert, Yannis Kotidis and S. Muthukrishnan and Martin Strauss, *Surfing Wavelets on Streams: One-Pass Summaries for Approximate Aggregate Queries*, VLDB 2001

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BREAK!

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Sensor Data Mining: Similarity Search and Pattern Analysis

Christos Faloutsos
CMU

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Part 3: Linear Forecasting

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Outline

- Motivation
- Similarity Search and Indexing
- DSP
- ➔ • Linear Forecasting
 - Bursty traffic - fractals and multifractals
 - Non-linear forecasting
 - Conclusions

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Forecasting

"Prediction is very difficult, especially about the future." - Nils Bohr

<http://www.hfac.uh.edu/MediaFutures/thoughts.html>

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Outline

- Motivation
- ...
- Linear Forecasting
 - ➔ – Auto-regression: Least Squares; RLS
 - Co-evolving time sequences
 - Examples
 - Conclusions

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Problem#2: Forecast

- Example: give x_{t-1}, x_{t-2}, \dots , forecast x_t

Time Tick	Number of packets sent
1	45
2	55
3	75
4	45
5	55
6	60
7	85
8	75
9	60
10	50

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Forecasting: Preprocessing

MANUALLY:
remove trends spot periodicities

time time

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Problem#2: Forecast

- Solution: try to express x_t as a linear function of the past: x_{t-2}, x_{t-2}, \dots (up to a window of w)

Formally:

$$x_t \approx a_1 x_{t-1} + \dots + a_w x_{t-w} + \text{noise}$$

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(Problem: Back-cast; interpolate)

- Solution - interpolate: try to express x_t as a linear function of the past AND the future: $x_{t+1}, x_{t+2}, \dots, x_{t+w_{future}}; x_{t-1}, \dots, x_{t-w_{past}}$ (up to windows of w_{past}, w_{future})
- EXACTLY the same algo's

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Linear Regression: idea

patient	weight	height
1	27	43
2	43	54
3	54	72
...
N	25	??

- express what we don't know (= 'dependent variable')
- as a linear function of what we know (= 'indep. variable(s)')

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Linear Auto Regression:

Time	Packets Sent(t)
1	43
2	54
3	72
...	...
N	??

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Linear Auto Regression:

Time	Packets Sent (t-1)	Packets Sent(t)
1	-	43
2	43	54
3	54	72
...
N	25	??

- lag $w=1$
- Dependent variable = # of packets sent ($S[t]$)
- Independent variable = # of packets sent ($S[t-1]$)

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Outline

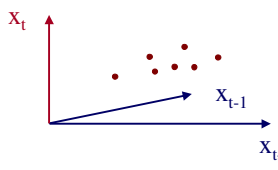
- Motivation
- ...
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 - Co-evolving time sequences
 - Examples
 - Conclusions

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More details:

- Q1: Can it work with window $w > 1$?
- A1: YES!

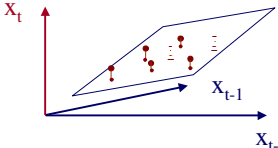


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More details:

- Q1: Can it work with window $w > 1$?
- A1: YES! (we'll fit a hyper-plane, then!)

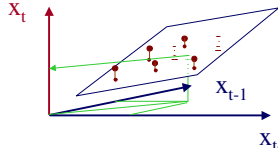


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More details:

- Q1: Can it work with window $w > 1$?
- A1: YES! (we'll fit a hyper-plane, then!)



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More details:

Skip

- Q1: Can it work with window $w > 1$?
- A1: YES! The problem becomes:

$$\mathbf{X}_{[N \times w]} \times \mathbf{a}_{[w \times 1]} = \mathbf{y}_{[N \times 1]}$$

- **OVER-CONSTRAINED**
 - \mathbf{a} is the vector of the regression coefficients
 - \mathbf{X} has the N values of the w indep. variables
 - \mathbf{y} has the N values of the dependent variable

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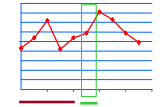
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More details:

Skip

- $\mathbf{X}_{[N \times w]} \times \mathbf{a}_{[w \times 1]} = \mathbf{y}_{[N \times 1]}$

Ind-var1 Ind-var-w



$$\begin{matrix} \text{time} \\ \downarrow \\ \begin{bmatrix} X_{11}, X_{12}, \dots, X_{1w} \\ X_{21}, X_{22}, \dots, X_{2w} \\ \vdots \\ X_{N1}, X_{N2}, \dots, X_{Nw} \end{bmatrix} \end{matrix} \times \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_w \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix}$$

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More details:

• $\mathbf{X}_{[N \times w]} \times \mathbf{a}_{[w \times 1]} = \mathbf{y}_{[N \times 1]}$

Ind-var1 Ind-var-w

time

$$\begin{bmatrix} X_{11}, X_{12}, \dots, X_{1w} \\ X_{21}, X_{22}, \dots, X_{2w} \\ \vdots \\ X_{N1}, X_{N2}, \dots, X_{Nw} \end{bmatrix}$$

$$\times \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_w \end{bmatrix} =$$

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix}$$

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More details

- Q2: How to estimate $a_1, a_2, \dots, a_w = \mathbf{a}$?
- A2: with Least Squares fit

$$\mathbf{a} = (\mathbf{X}^T \times \mathbf{X})^{-1} \times (\mathbf{X}^T \times \mathbf{y})$$

- (Moore-Penrose pseudo-inverse)
- \mathbf{a} is the vector that minimizes the RMSE from \mathbf{y}

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Even more details

- Q3: Can we estimate \mathbf{a} incrementally?
- A3: Yes, with the brilliant, classic method of 'Recursive Least Squares' (RLS) (see, e.g., [Yi+00], for details) - pictorially:

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Even more details

- Given:

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Even more details

← new point

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Even more details

RLS: quickly compute new best fit

← new point

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Even more details

- **Straightforward Least Squares**
 - Needs huge matrix (**growing** in size) $O(N \times w)$
 - Costly matrix operation $O(N \times w^2)$
- **Recursive LS**
 - Need much smaller, fixed size matrix $O(w \times w)$
 - Fast, incremental computation $O(1 \times w^2)$

$N = 10^6, \quad w = 1-100$

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Even more details

- Q4: can we 'forget' the older samples?
- A4: Yes - RLS can easily handle that $[Y_{i+00}]$:

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Adaptability - 'forgetting'

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Adaptability - 'forgetting'

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Adaptability - 'forgetting'

- RLS: can *trivially* handle 'forgetting'

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How to choose 'w'?

- goal: capture arbitrary periodicities
- with NO human intervention
- on a semi-infinite stream

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Answer:

- ‘AWSOM’ (Arbitrary Window Stream fOrecasting Method) [Papadimitriou+, vldb2003]
- idea: do AR on each wavelet level
- in detail:

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AWSOM

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AWSOM

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AWSOM - idea

$$W_{l,t} = \beta_{l,1}W_{l,t-1} + \beta_{l,2}W_{l,t-2} + \dots$$

$$W_{l,t+1} = \beta_{l,1}W_{l,t} + \beta_{l,2}W_{l,t-1} + \dots$$

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More details...

- Update of wavelet coefficients (incremental)
- Update of linear models (incremental; RLS)
- Feature selection (single-pass)
 - Not all correlations are significant
 - Throw away the insignificant ones (“noise”)

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Results - Synthetic data

- Triangle pulse
- Mix (sine + square)
- AR captures wrong trend (or none)
- Seasonal AR estimation fails

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Results - Real data

- Automobile traffic
 - Daily periodicity
 - Bursty “noise” at smaller scales
- AR fails to capture any trend
- Seasonal AR estimation fails

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Results - real data

- Sunspot intensity
 - Slightly time-varying “period”
- AR captures wrong trend
- Seasonal ARIMA
 - wrong downward trend, despite help by human!

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Complexity

Skip

- Model update
 - Space: $O(\lg N + mk^2) \approx O(\lg N)$
 - Time: $O(k^2) \approx O(1)$
- Where
 - N : number of points (so far)
 - k : number of regression coefficients; fixed
 - m : number of linear models; $O(\lg N)$

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Outline

- Motivation
- ...
- Linear Forecasting
 - Auto-regression: Least Squares; RLS
 - Co-evolving time sequences
 - Examples
 - Conclusions

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Co-Evolving Time Sequences

- Given: A set of **correlated** time sequences
- Forecast ‘**Repeated(t)**’

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Solution:

Q: what should we do?

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Solution:

Least Squares, with

- Dep. Variable: Repeated(t)
- Indep. Variables: Sent(t-1) ... Sent(t-w); Lost(t-1) ... Lost(t-w); Repeated(t-1), ...
- (named: 'MUSCLES' [Yi+00])

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B.II - Time Series Analysis Skip

Outline

- Auto-regression
- Least Squares; recursive least squares
- Co-evolving time sequences
- ➔ Examples
- Conclusions

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Examples - Experiments Skip

- Datasets
 - Modem pool traffic (14 modems, 1500 time-ticks; #packets per time unit)
 - AT&T WorldNet internet usage (several data streams; 980 time-ticks)
- Measures of success
 - Accuracy : Root Mean Square Error (RMSE)

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Accuracy - "Modem" Skip

Modem	AR	yesterday	MUSCLES
1	1.8	1.5	0.8
2	1.5	1.2	0.6
3	2.0	1.8	0.9
4	2.5	2.2	1.1
5	2.0	1.8	0.9
6	2.5	2.2	1.1
7	2.0	1.8	0.9
8	1.5	1.2	0.6
9	2.0	1.8	0.9
10	2.0	1.8	0.9
11	1.5	1.2	0.6
12	1.5	1.2	0.6
13	2.0	1.8	0.9
14	3.5	3.0	1.5

MUSCLES outperforms AR & "yesterday"

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Accuracy - "Internet" Skip

Streams	AR	yesterday	MUSCLES
1	0.8	0.7	0.4
2	0.7	0.6	0.3
3	0.8	0.7	0.4
4	0.7	0.6	0.3
5	0.8	0.7	0.4
6	0.7	0.6	0.3
7	0.8	0.7	0.4
8	0.7	0.6	0.3
9	0.8	0.7	0.4
10	0.7	0.6	0.3
11	0.8	0.7	0.4
12	0.7	0.6	0.3
13	1.2	1.1	0.5
14	1.3	1.2	0.6
15	1.2	1.1	0.5

MUSCLES consistently outperforms AR & "yesterday"

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B.II - Time Series Analysis Skip

Outline

- Auto-regression
- Least Squares; recursive least squares
- Co-evolving time sequences
- Examples
- ➔ Conclusions

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Conclusions - Practitioner's guide

- AR(IMA) methodology: prevailing method for linear forecasting
- Brilliant method of Recursive Least Squares for fast, incremental estimation.
- See [Box-Jenkins]
- very recently: AWSOM (no human intervention)

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Resources: software and urls

- MUSCLES: Prof. Byoung-Kee Yi:
<http://www.postech.ac.kr/~bkyi/>
or christos@cs.cmu.edu
- free-ware: 'R' for stat. analysis (clone of Splus)
<http://cran.r-project.org/>

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Books

- George E.P. Box and Gwilym M. Jenkins and Gregory C. Reinsel, *Time Series Analysis: Forecasting and Control*, Prentice Hall, 1994 (the classic book on ARIMA, 3rd ed.)
- Brockwell, P. J. and R. A. Davis (1987). *Time Series: Theory and Methods*. New York, Springer Verlag.

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Additional Reading

- [Papadimitriou+ vldb2003] Spiros Papadimitriou, Anthony Brockwell and Christos Faloutsos *Adaptive, Hands-Off Stream Mining* VLDB 2003, Berlin, Germany, Sept. 2003
- [Yi+00] Byoung-Kee Yi et al.: *Online Data Mining for Co-Evolving Time Sequences*, ICDE 2000. (Describes MUSCLES and Recursive Least Squares)

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Part 4: Bursty traffic and multifractals

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Outline

- Motivation
- Similarity Search and Indexing
- DSP
- Linear Forecasting
- ➔ • Bursty traffic - fractals and multifractals
- Non-linear forecasting
- Conclusions

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Outline

- Motivation
- ...
- Linear Forecasting
- Bursty traffic - fractals and multifractals
 - ➔ – Problem
 - Main idea (80/20, Hurst exponent)
 - Results

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Recall: Problem #1:

Goal: given a signal (eg., #bytes over time)
 Find: patterns, periodicities, and/or compress

Bytes per 30' (packets per day; earthquakes per year)

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Problem #1

- model bursty traffic
- generate realistic traces
- (Poisson does not work)

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Motivation

- predict queue length distributions (e.g., to give probabilistic guarantees)
- “learn” traffic, for buffering, prefetching, ‘active disks’, web servers

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Q: any ‘pattern’?

- Not Poisson
- spike; silence; more spikes; more silence...
- any rules?

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solution: self-similarity

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But:

- Q1: How to generate realistic traces; extrapolate; give guarantees?
- Q2: How to estimate the model parameters?

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Outline

- Motivation
- ...
- Linear Forecasting
- Bursty traffic - fractals and multifractals
 - Problem
 - ➔ – Main idea (80/20, Hurst exponent)
 - Results

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Approach

- Q1: How to generate a sequence, that is
 - bursty
 - self-similar
 - and has similar queue length distributions

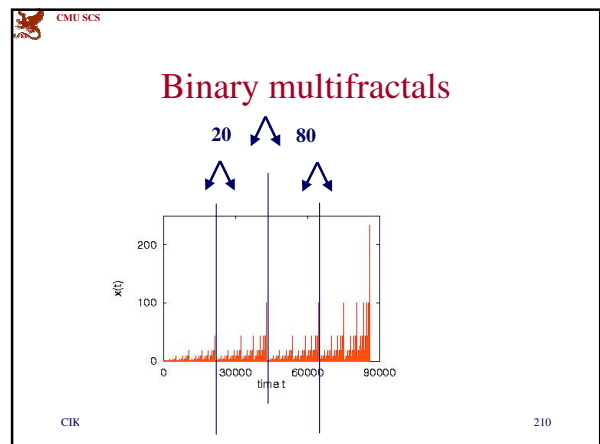
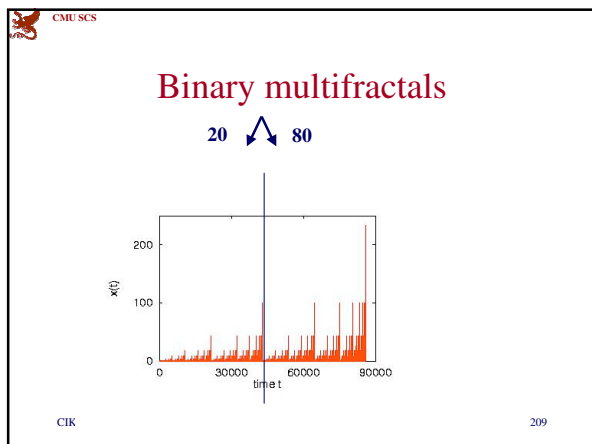
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Approach

- A: ‘binomial multifractal’ [Wang+02]
- ~ 80-20 ‘law’:
 - 80% of bytes/queries etc on first half
 - repeat recursively
- b : bias factor (eg., 80%)

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Parameter estimation

- Q2: How to estimate the bias factor b ?

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Parameter estimation

- Q2: How to estimate the bias factor b ?
- A: MANY ways [Crovella+96]
 - Hurst exponent
 - variance plot
 - even DFT amplitude spectrum! ('periodogram')
 - More robust: 'entropy plot' [Wang+02]

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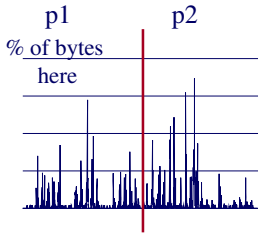
Entropy plot

- Rationale:
 - burstiness: inverse of uniformity
 - entropy measures uniformity of a distribution
 - find entropy at several granularities, to see whether/how our distribution is close to uniform.

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Entropy plot



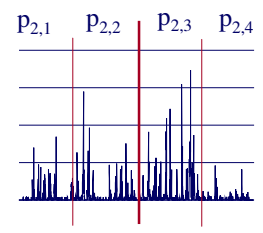
p_1 p_2
 % of bytes
 here

- Entropy $E(n)$ after n levels of splits
- $n=1$: $E(1) = -p_1 \log_2(p_1) - p_2 \log_2(p_2)$

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Entropy plot



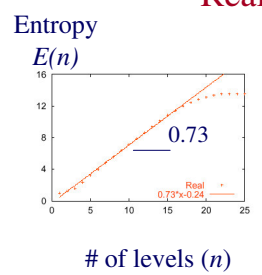
$P_{2,1}$ $P_{2,2}$ $P_{2,3}$ $P_{2,4}$

- Entropy $E(n)$ after n levels of splits
- $n=1$: $E(1) = -p_1 \log_2(p_1) - p_2 \log_2(p_2)$
- $n=2$: $E(2) = -\sum_i p_{2,i} \log_2(p_{2,i})$

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Real traffic



Entropy
 $E(n)$

0.73

0.73 * 0.24

of levels (n)

- Has linear entropy plot (-> self-similar)

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Observation - intuition:

Entropy $E(n)$

intuition: slope =
intrinsic dimensionality =
info-bits per coordinate-bit
– unif. Dataset: slope = 1
– multi-point: slope = 0

of levels (n)

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Entropy plot - Intuition

- Slope ~ intrinsic dimensionality (in fact, 'Information fractal dimension')
- = info bit per coordinate bit - eg

Dim = 1

Pick a point;
reveal its coordinate bit-by-bit -
how much info is each bit worth to me?

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Entropy plot

- Slope ~ intrinsic dimensionality (in fact, 'Information fractal dimension')
- = info bit per coordinate bit - eg

Dim = 1

↑ Is MSB 0?
'info' value = $E(1)$: 1 bit

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Entropy plot

- Slope ~ intrinsic dimensionality (in fact, 'Information fractal dimension')
- = info bit per coordinate bit - eg

Dim = 1

↑ Is MSB 0?
↑ Is next MSB = 0?

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Entropy plot

- Slope ~ intrinsic dimensionality (in fact, 'Information fractal dimension')
- = info bit per coordinate bit - eg

Dim = 1

Info value = 1 bit
= $E(2) - E(1)$ = slope!
↑ Is next MSB = 0?

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Entropy plot

- Repeat, for all points at same position:


Dim=0

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Entropy plot

- Repeat, for all points at same position:
- we need 0 bits of info, to determine position
- > slope = 0 = intrinsic dimensionality


Dim=0 


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Entropy plot

- Real (and 80-20) datasets can be in-between: bursts, gaps, smaller bursts, smaller gaps, at every scale

Dim = 1 

Dim=0 

0 < Dim < 1 

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(Fractals, again)

- What set of points could have behavior between point and line?

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Cantor dust

- Eliminate the middle third
- Recursively!

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Cantor dust



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Cantor dust

Dimensionality?
(no length; infinite # points!)
Answer: $\log 2 / \log 3 = 0.6$

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Some more entropy plots:

- Poisson vs real

Poisson: slope = ~ 1 \rightarrow uniformly distributed

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B-model

$E(n)$

- b-model traffic gives perfectly linear plot
- Lemma: its slope is $\text{slope} = -b \log_2 b - (1-b) \log_2 (1-b)$
- Fitting: do entropy plot; get slope; solve for b

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Outline

- Motivation
- ...
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- Bursty traffic - fractals and multifractals
 - Problem
 - Main idea (80/20, Hurst exponent)
 - Experiments - Results

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Experimental setup

- Disk traces (from HP [Wilkes 93])
- web traces from LBL
<http://repository.cs.vt.edu/lbl-conn-7.tar.Z>

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Model validation

- Linear entropy plots

(a) Disk Traces

(b) Web Traces

Bias factors b : 0.6-0.8
 smallest b / smoothest: nntp traffic

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Web traffic - results

- LBL, NCDF of queue lengths (log-log scales)

Prob(> l)

(a) lbl-all

(b) lbl-nntp

(c) lbl-smtp

(d) lbl-ftp

How to give guarantees? (queue length l)

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Web traffic - results

- LBL, NCDF of queue lengths (log-log scales)

Prob(> l)

20% of the requests will see queue lengths < 100

(queue length l)

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Conclusions

- Multifractals (80/20, 'b-model', Multiplicative Wavelet Model (MWM)) for analysis and synthesis of bursty traffic
- can give (probabilistic) guarantees

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Books

- Fractals: Manfred Schroeder: *Fractals, Chaos, Power Laws: Minutes from an Infinite Paradise* W.H. Freeman and Company, 1991 (Probably the BEST book on fractals!)

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Further reading:

- Crovella, M. and A. Bestavros (1996). Self-Similarity in World Wide Web Traffic, Evidence and Possible Causes. Sigmetrics.
- [ieeetn94] W. E. Leland, M.S. Taqqu, W. Willinger, D.V. Wilson, *On the Self-Similar Nature of Ethernet Traffic*, IEEE Transactions on Networking, 2, 1, pp 1-15, Feb. 1994.

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Further reading

- [Riedi+99] R. H. Riedi, M. S. Crouse, V. J. Ribeiro, and R. G. Baraniuk, *A Multifractal Wavelet Model with Application to Network Traffic*, IEEE Special Issue on Information Theory, 45. (April 1999), 992-1018.
- [Wang+02] Mengzhi Wang, Tara Madhyastha, Ngai Hang Chang, Spiros Papadimitriou and Christos Faloutsos, *Data Mining Meets Performance Evaluation: Fast Algorithms for Modeling Bursty Traffic*, ICDE 2002, San Jose, CA, 2/26/2002 - 3/1/2002.

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Part 5: chaos and non-linear forecasting

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Outline

- Motivation
- Similarity Search and Indexing
- DSP
- Linear Forecasting
- Bursty traffic - fractals and multifractals
- ➔ • Non-linear forecasting
- Conclusions

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Detailed Outline

- Non-linear forecasting
 - Problem
 - Idea
 - How-to
 - Experiments
 - Conclusions

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Recall: Problem #1

Value

Time

Given a time series $\{x_t\}$, predict its future course, that is, x_{t+1}, x_{t+2}, \dots

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How to forecast?

- ARIMA - but: linearity assumption
- ANSWER: 'Delayed Coordinate Embedding' = Lag Plots [Sauer92]

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General Intuition (Lag Plot)

Lag = 1,
k = 4 NN

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Questions:

- Q1: How to choose lag L ?
- Q2: How to choose k (the # of NN)?
- Q3: How to interpolate?
- Q4: why should this work at all?

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Q1: Choosing lag L

- Manually (16, in award winning system by [Sauer94])

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Q2: Choosing number of neighbors k

- Manually (typically ~ 1-10)

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Q3: How to interpolate?

How do we interpolate between the k nearest neighbors?

A3.1: Average

A3.2: Weighted average (weights drop with distance - how?)

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Q3: How to interpolate?

A3.3: Using SVD - seems to perform best ([Sauer94] - first place in the Santa Fe forecasting competition)

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Q4: Any theory behind it?

A4: YES!

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Theoretical foundation

- Based on the “Takens’ Theorem” [Takens81]
- which says that **long enough delay vectors can do prediction**, even if there are unobserved variables in the dynamical system (= diff. equations)

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Theoretical foundation

Example: Lotka-Volterra equations

$$\frac{dH}{dt} = r H - a H * P$$

$$\frac{dP}{dt} = b H * P - m P$$

H is count of prey (e.g., hare)
P is count of predators (e.g., lynx)

Suppose only P(t) is observed (t=1, 2, ...).

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Theoretical foundation

- But the delay vector space is a faithful reconstruction of the internal system state
- So prediction in **delay vector space** is as good as prediction in **state space**

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Detailed Outline

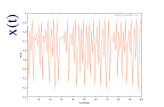
- Non-linear forecasting
 - Problem
 - Idea
 - How-to
 - ➔ – Experiments
 - Conclusions

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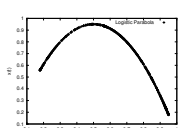
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Datasets

Logistic Parabola:
 $x_t = ax_{t-1}(1-x_{t-1}) + \text{noise}$
 Models population of flies [R. May/1976]



time



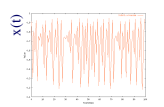
Lag-plot

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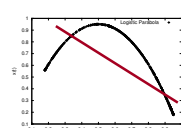
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Datasets

Logistic Parabola:
 $x_t = ax_{t-1}(1-x_{t-1}) + \text{noise}$
 Models population of flies [R. May/1976]



time



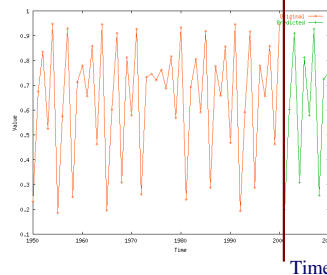
Lag-plot
ARIMA: fails

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Logistic Parabola

Our Prediction from here



Value

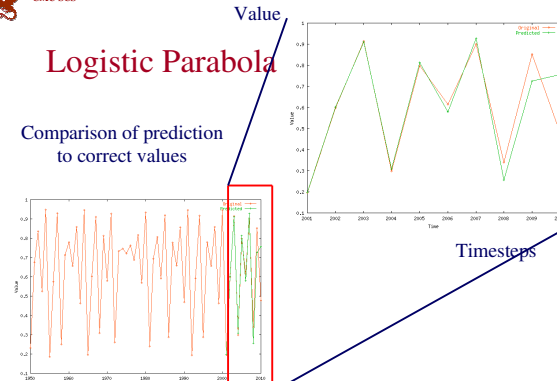
Timesteps

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Logistic Parabola

Comparison of prediction to correct values



Value

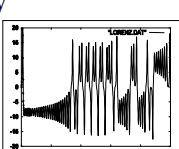
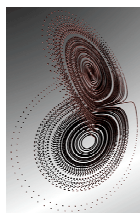
Timesteps

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Datasets

LORENZ: Models convection currents in the air

$$\begin{aligned} dx / dt &= a(y - x) \\ dy / dt &= x(b - z) - y \\ dz / dt &= xy - cz \end{aligned}$$



Skip

Value

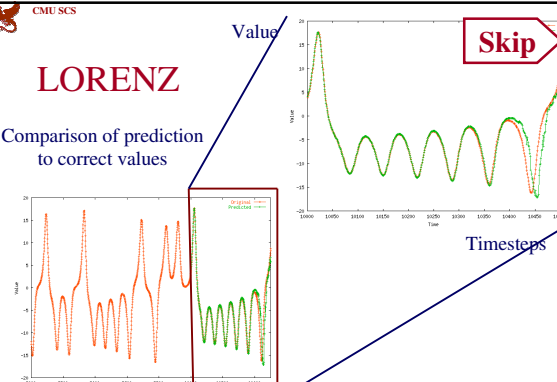
Timesteps

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LORENZ

Comparison of prediction to correct values



Value

Timesteps

Skip


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Value

Datasets

- LASER: fluctuations in a Laser over time (used in Santa Fe competition)



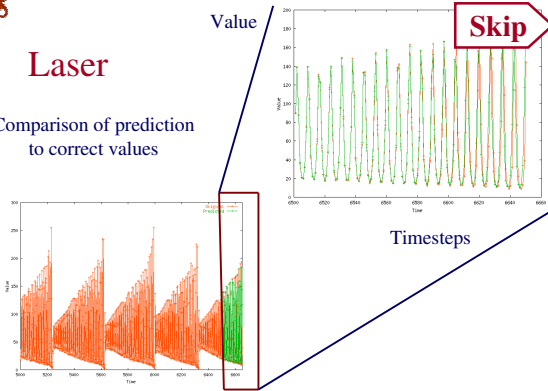
Time

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Laser

Comparison of prediction to correct values



Value

Timesteps

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Conclusions

- Lag plots for non-linear forecasting (Takens' theorem)
- suitable for 'chaotic' signals

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References

- Deepay Chakrabarti and Christos Faloutsos *F4: Large-Scale Automated Forecasting using Fractals* CIKM 2002, Washington DC, Nov. 2002.
- Sauer, T. (1994). *Time series prediction using delay coordinate embedding*. (in book by Weigend and Gershenfeld, below) Addison-Wesley.
- Takens, F. (1981). *Detecting strange attractors in fluid turbulence*. Dynamical Systems and Turbulence. Berlin: Springer-Verlag.

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References

- Weigend, A. S. and N. A. Gershenfeld (1994). *Time Series Prediction: Forecasting the Future and Understanding the Past*, Addison Wesley. (Excellent collection of papers on chaotic/non-linear forecasting, describing the algorithms behind the winners of the Santa Fe competition.)

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Overall conclusions

- Similarity search: **Euclidean/time-warping; feature extraction and SAMs**

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Overall conclusions

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- Non-linear forecasting: **lag-plots** (Takens)

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‘Take home’ messages

- Hard, but desirable query for sensor data: *‘find patterns / outliers’*
- We need **fast**, **automated** such tools
 - Many great tools exist (DWT, ARIMA, ...)
 - some are readily usable; others need to be made scalable / single pass/ automatic

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THANK YOU!



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