Elaboration in L2

Recall the discussion about elaboration last recitation. The AST generated by your parser should reflect the source-code **syntactic** structure as closely as possible. You can then perform an elaboration pass to generate an AST that reflects the **semantic** structure of L2.

During L1, because all programs were simply a list of statements, they could for the most part be elaborated into seq and nop in a simple right-associative nesting:

$$s_1;\ s_2;\ s_3; \quad \Longrightarrow_{\text{elab}} \quad \texttt{seq}(s_1, \texttt{seq}(s_2, \texttt{seq}(s_3, \texttt{nop})))$$

The main tricky part of elaboration was handling declarations, for which our AST node $\texttt{decl}(x, \tau, s)$ contains s to clearly mark the scope of x. So if s_2 above was actually some declaration $\tau\ x$, the elaboration would instead be $\texttt{seq}(s_1, \texttt{decl}(x, \tau, \texttt{seq}(s_3, \texttt{nop})))$.

In L2 however, programs can get more complex. A block, which is a list of statements surrounded by braces, is itself a statement. Yet, our (post-elaboration) AST does not require an additional variant for blocks. We can represent them with only seq and nop.

Checkpoint 0

Write out the post-elaboration AST of the following program. Be careful about the nesting of seq's and decl's.

```
int main () {
  int a;
  {
    int b;
    b = 5;
    a = b;
  }
  int b;
  b = a;
  return b;
}
```

Solution:

```
decl(a, int,
  seq(
    decl(b, int,
      seq(assign(b, 5),
      seq(assign(a, b),
      nop))
    ),
    decl(b, int,
      seq(assign(b, a),
      seq(return(b),
      nop))
    )
  )
)
```

Of course, you are not required to elaborate in this specific manner. The way we have presented decl, seq, and nop makes it easier for us to define judgements for their static semantics, but it may affect the debugability of the post-elaboration AST in your compiler. You are free to not elaborate blocks and keep them as lists of statements.

Static Semantics of Initialization

For a C0 program to be valid, all variables must be declared and initialized before use. A compiler should confirm this property of a user program. To formally check this, we need to come up with a set of judgements and their associated inference rules. In class, we saw 2 different presentations of judgements that could achieve this. One of them used the following judgements:

- $\mathsf{use}(e, x)$: the variable x *might* be used when evaluating expression e.

- $\mathsf{def}(s, x)$: the variable x *must* be initialized after executing statement s.

- $\mathsf{live}(s, x)$: x *might* be used before initialization when executing s.

- $\mathsf{init}(s)$: all variables declared in s *must* be initialized before use in s.

While this presentation might be more intuitive, we will focus on another version which explicitly tracks the set of initialized variables. We denote a set of variables with δ and define the following two judgments:

- $\delta \vdash s \Rightarrow \delta'$

  Assuming all the variables in δ are defined when s is reached, no uninitialized variable will be referenced and after its execution all the variables in δ' will be defined.

- $\delta \vdash e$

  e will only reference variables defined in δ.

Here are some of the rules that define the judgement $\delta \vdash s \Rightarrow \delta'$:

$$\frac{}{\delta \vdash \mathtt{nop} \Rightarrow \delta} \qquad \frac{\delta \vdash s_1 \Rightarrow \delta_1 \quad \delta_1 \vdash s_2 \Rightarrow \delta_2}{\delta \vdash \mathtt{seq}(s_1, s_2) \Rightarrow \delta_2} \qquad \frac{\delta \vdash e}{\delta \vdash \mathtt{assign}(x, e) \Rightarrow \delta \cup \{x\}} \qquad \frac{\delta \vdash e \quad \delta \vdash s \Rightarrow \delta'}{\delta \vdash \mathtt{while}(e, s) \Rightarrow \delta}$$

$$\frac{\delta \vdash s \Rightarrow \delta'}{\delta \vdash \mathtt{decl}(y, \tau, s) \Rightarrow \delta' - \{y\}} \qquad \frac{\delta \vdash e}{\delta \vdash \mathtt{return}(e) \Rightarrow \{x \mid x \text{ in scope}\}}$$

In these judgments we have traded the complexity of traversing statements multiple times with the complexity of maintaining variables sets.

Checkpoint 1

Write the missing inference rule for $\delta \vdash \mathtt{if}(e, s_1, s_2) \Rightarrow \delta'$.

Solution:

$$\frac{\delta \vdash e \quad \delta \vdash s_1 \Rightarrow \delta_1 \quad \delta \vdash s_2 \Rightarrow \delta_2}{\delta \vdash \mathtt{if}(e, s_1, s_2) \Rightarrow \delta_1 \cap \delta_2}$$

Checkpoint 2

Using the inference rules as given, try to derive $\{\} \vdash s \Rightarrow \delta$ for the following program:

$$\mathsf{decl}(x, \mathtt{int}, \mathsf{seq}(\mathsf{assign}(x, 3), \mathsf{return}(x)))$$

Solution:

$$\frac{\dfrac{\dfrac{}{\{\} \vdash 3}}{\{\} \vdash \mathsf{assign}(x, 3) \Rightarrow \{x\}} \quad \dfrac{\dfrac{}{\{x\} \vdash x}}{\{\} \vdash \mathsf{return}(x) \Rightarrow \{x\}}}{\dfrac{\{\} \vdash \mathsf{seq}(\mathsf{assign}(x, 3), \mathsf{return}(x)) \Rightarrow \{x\}}{\{\} \vdash \mathsf{decl}(x, \mathtt{int}, \mathsf{seq}(\mathsf{assign}(x, 3), \mathsf{return}(x))) \Rightarrow \{\}}}$$

Unifying Static Semantics of Initialization and Typing

If you looked carefully earlier, or if you read the lecture notes, you'll notice that the rule for `return` is a bit strange, as it deals with scope in an informal way. The lecture notes suggest getting around this by also tracking a set γ of variables currently in scope. It turns out we can actually just use the typechecking context Γ that maps variables to types, as its domain $\operatorname{dom}\Gamma$ will be exactly the variables that are in scope. Incidentally, this means we can even combine it with the typing judgement for statements to create the following new judgment

$$\Gamma;\ \Delta \vdash s : [\tau] \Rightarrow \Delta'$$

The statement s

- is in the scope of the variables in Γ, which were *declared* with their corresponding types
- only uses *initialized* variables from Δ
- leaves the variables in Δ' *initialized* after execution
- returns a value of type τ if it returns

We can similarly define $\Gamma;\ \Delta \vdash e : \tau$ to mean "e uses only variables in Δ and has type τ given the context Γ". Here are some of the rules that define the judgement $\Gamma;\ \Delta \vdash s : [\tau] \Rightarrow \Delta'$:

$$\frac{\Gamma;\ \Delta \vdash s_1 : [\tau] \Rightarrow \Delta' \qquad \Gamma;\ \Delta' \vdash s_2 : [\tau] \Rightarrow \Delta''}{\Gamma;\ \Delta \vdash \mathsf{seq}(s_1, s_2) : [\tau] \Rightarrow \Delta''} \qquad\qquad \frac{}{\Gamma;\ \Delta \vdash \mathsf{nop} : [\tau] \Rightarrow \Delta}$$

$$\frac{\Gamma, x : \tau';\ \Delta \vdash s : [\tau] \Rightarrow \Delta'}{\Gamma;\ \Delta \vdash \mathsf{declare}(x, \tau', s) : [\tau] \Rightarrow \Delta' \setminus \{x\}}$$

$$\frac{\Gamma;\ \Delta \vdash e : \mathsf{bool} \qquad \Gamma;\ \Delta \vdash s_1 : [\tau] \Rightarrow \Delta' \qquad \Gamma;\ \Delta \vdash s_2 : [\tau] \Rightarrow \Delta''}{\Gamma;\ \Delta \vdash \mathsf{if}(e, s_1, s_2) : [\tau] \Rightarrow \Delta' \cap \Delta''}$$

$$\frac{\Gamma;\ \Delta \vdash e : \mathsf{bool} \qquad \Gamma;\ \Delta \vdash s : [\tau] \Rightarrow \Delta'}{\Gamma;\ \Delta \vdash \mathsf{while}(e, s) : [\tau] \Rightarrow \Delta}$$

Checkpoint 3

Write the missing inference rules for $\Gamma;\ \Delta \vdash \mathsf{assign}(x, e) : [\tau] \Rightarrow \Delta'$ and $\Gamma;\ \Delta \vdash \mathsf{return}(e) : [\tau] \Rightarrow \Delta'$.

Solution:

$$\frac{\Gamma(x) = \tau' \qquad \Gamma;\ \Delta \vdash e : \tau'}{\Gamma;\ \Delta \vdash \mathsf{assign}(x, e) : [\tau] \Rightarrow \Delta \cup \{x\}} \qquad\qquad \frac{\Gamma;\ \Delta \vdash e : \tau}{\Gamma;\ \Delta \vdash \mathsf{return}(e) : [\tau] \Rightarrow \operatorname{dom}\Gamma}$$

Checkpoint 4

Write the inference rule for $\Gamma;\ \Delta \vdash x : \tau$.

Solution: $\dfrac{\Gamma(x) = \tau \qquad x \in \Delta}{\Gamma;\ \Delta \vdash x : \tau}$

We have shown that it is quite possible, and not too inelegant, to implement static semantics for initialization and typing as a single judgement. It is up to you whether to do this in your own compiler – you could definitely check initialization and typing in separate passes.

Grab Bag of Hints

- For the expression `if (a < 0) if (b < 0) x = 4 else x = 5`, x is not assigned if $a \geq 0$ (`else` binds to the most recent `if`)

- You have to add support for Boolean variables now, and you will have to add support for pointers in lab 4. Plan ahead when making design decisions to support different types in type checking and instruction selection.

- We suggest adding support for a `-O0` flag that disables register allocation and places all temps on the stack. Interference bugs fail in subtle, hard to understand ways.

- You can step through your programs with gdb. Place a breakpoint with `break _c0_main`, then use `step` to advance the program.