

### 10-423/10-623 Generative AI

Machine Learning Department School of Computer Science Carnegie Mellon University

# Generative Adversarial Networks (GANs)

Matt Gormley Lecture 6 Feb. 5, 2024

### Reminders

- Homework 1: Generative Models of Text
  - Out: Thu, Jan 25
  - Due: Wed, Feb 7 at 11:59pm
- Matt's office hours on GCal

# MODEL: GENERATIVE ADVERSARIAL NETWORK (GAN)

### Stable Diffusion still can't explain GANs

Prompt: slide explaining Generative Adversarial Networks (GANs) for Intro to Machine Learning course, carefully designed, easy to follow

Negative Prompt: boring, unclear, nontechnical



Figure from https://stablediffusionweb.com/

A GAN consists of two deterministic neural network models:

 the Generator
takes a vector of random noise as input, and generates an image

### 2) the Discriminator

takes in an image classifies whether it is real (label 1) or fake (label 0)

### **Generator Model**

#### 1) the Generator

takes a vector of random noise as input, and generates an image

#### **Example Generator: DCGAN**

- An inverted CNN with four fractionallystrided convolution layers (not deconvolution)
- These fractional strides grow the size of the image from layer to layer
- The final layer has three channels for red/green/blue



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### **Discriminator Model**

#### **Example Discriminator: PatchGAN**

- Convolutional neural network
- Looks at each patch of the image and tries to predict whether it is real or fake
- Helps avoid producing blurry images



### 2) the Discriminator

takes in an image classifies whether it is real (label 1) or fake (label 0)

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### 2) the Discriminator

takes in an image classifies whether it is real (label 1) or fake (label 0)

In training, the GAN plays a two player minimax game:

- 1. the Generator tries to create realistic images to fool the Discriminator into thinking they are real
- 2. the Discriminator tries to identify the real images from the fake







Real/fake images from Huang et al. (2017)

Gaussian noise from https://physbam.stanford.edu/cs448x/old/Noise\_Review.html



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### **LEARNING FOR GANS**

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$$\max_{\phi} \log \left( D_{\phi}(\mathbf{x}^{(i)}) \right) + \log \left( 1 - D_{\phi}(G_{\theta}(\mathbf{z}^{(i)})) \right)$$
$$\min_{\theta} \log \left( 1 - D_{\phi}(G_{\theta}(\mathbf{z}^{(i)})) \right)$$

The discriminator is trying to maximize the likelihood of a binary classifier with labels {real = 1, fake = 0}, on the fixed output of the generator

The generator is trying to minimize the likelihood of its generated (fake) image being classified as fake, according to a fixed discriminator

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- 2. the Discriminator tries to identify the real images from the fake

- Objective function is a simple differentiable function
- We chose G and D to be differentiable neural networks

- Keep  $G_{\theta}$  fixed and backprop through  $D_{\phi}$
- Keep  $D_{\phi}$  fixed and backprop through  $G_{\theta}$



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- Training data consists of a collection of m unlabeled images x<sup>(1)</sup>, ..., x<sup>(m)</sup>
- Optimization is similar to block coordinate descent
- But instead of exactly solving the min/max problem, we take a step of mini-batch SGD

Algorithm 1 Minibatch stochastic gradient descent training of generative adversarial nets. The number of steps to apply to the discriminator, k, is a hyperparameter. We used k = 1, the least expensive option, in our experiments.

for number of training iterations do

#### for k steps do

- Sample minibatch of m noise samples  $\{z^{(1)}, \ldots, z^{(m)}\}$  from noise prior  $p_g(z)$ .
- Sample minibatch of m examples  $\{x^{(1)}, \ldots, x^{(m)}\}$  from data generating distribution  $p_{\text{data}}(x)$ .
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[ \log D\left( \boldsymbol{x}^{(i)} \right) + \log \left( 1 - D\left( G\left( \boldsymbol{z}^{(i)} \right) \right) \right) \right].$$

end for

- Sample minibatch of m noise samples  $\{z^{(1)}, \ldots, z^{(m)}\}$  from noise prior  $p_g(z)$ .
- Update the generator by descending its stochastic gradient:

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log\left(1 - D\left(G\left(\boldsymbol{z}^{(i)}\right)\right)\right).$$

#### end for

The gradient-based updates can use any standard gradient-based learning rule. We used momentum in our experiments.

### **Class-conditional GANs**

- Objective function is a simple differentiable function
- We chose G and D to be differentiable neural networks

Training alternates between:

- Keep  $G_{\theta}$  fixed and backprop through  $D_{\phi}$
- Keep  $D_{\phi}$  fixed and backprop through  $G_{\theta}$



Real/fake images from Huang et al. (2017)

### **SCALING UP THE MODEL SIZE**

# Scaling Up the Model Size



Fig. 5. Timeline of TTI model development, where green dots are GAN TTI models, blue dots are autoregressive Transformers and orange dots are Diffusion TTI models. Models are separated by their parameter, which are in general counted for all their components. Models with asterisk are calculated without the involvement of their text encoders.

# Scaling Up the Model Size

### The Pathways Autoregressive Text-to-Image (Parti) model:

- treat image generation as a sequence-tosequence problem
- text prompt is input to encoder
- sequence of image tokens is output of decoder
- ViT-VQGAN takes in the image tokens and generates a high-quality image



Two dogs running in a field

# Scaling Up the Model Size

**Prompt:** A portrait photo of a kangaroo wearing an orange hoodie and blue sunglasses standing on the grass in front of the Sydney Opera House holding a sign on the chest that says Welcome Friends!

#### Parti with different model sizes



## Watermarking & Attribution

#### • Watermarking

- A digital watermark allows one to identify when an image has been created by a model
- Most methods for image generation (GANs, VAEs, stable diffusion) can be augmented with watermarking
- Fake-image Detection
  - Goal: identify fakes even without a watermark
- Model Attribution
  - Identify which generative model created an image (e.g. Dalle-2 vs. SDXL)
  - Very successful (natural watermarks)
- Image Attribution
  - Goal: identify the source images that led to the generation of a new image
  - Extremely challenging



### SOCIETAL IMPACTS OF IMAGE GENERATION

# Societal Impacts of Image Generation

### Pros

- New tools for artists
- Faster creation of memes

### Cons

- Copyright infringement / loss of work for artists
- Societal decrease in creativity
- Potential to create dehumanizing content
- Fake news / false realities / increased difficulty of fact checking
- Not rooted in reality
- Video generation is around the corner

# DIFFUSION MODELS AND VARITIONAL AUTOENCODERS (VAES)

### **Diffusion Models**

- Next we will consider (1) diffusion models and (2) variational autoencoders (VAEs)
  - Although VAEs came first, we're going to dive into diffusion models since they will receive more of our attention
- The steps in defining these models is roughly:
  - Define a probability distribution involving Gaussian noise
  - Use a variational lower bound as an objective function
  - Learn the parameters of the probability distribution by optimizing the objective function
- So what is a variational lower bound?

### **DIRECTED GRAPHICAL MODEL**

### Three Types of Graphical Models

Directed Graphical Model Undirected Graphical Model

Factor Graph







### Bayesian Network

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$$p(X_1, X_2, X_3, X_4, X_5) = p(X_5 | X_3) p(X_4 | X_2, X_3) p(X_3) p(X_2 | X_1) p(X_1)$$

### Bayesian Network



- A Bayesian Network is a directed graphical model
- It consists of a graph **G** and the conditional probabilities **P**
- These two parts full specify the distribution:
  - Qualitative Specification: G
  - Quantitative Specification: P

### **Qualitative Specification**

- Where does the qualitative specification come from?
  - Prior knowledge of causal relationships
  - Prior knowledge of modular relationships
  - Assessment from experts
  - Learning from data (i.e. structure learning)
  - We simply prefer a certain architecture (e.g. a layered graph)

— ...

### **Quantitative Specification**

Example: Conditional probability tables (CPTs) for discrete random variables



P(a,b,c.d) = P(a)P(b)P(c|a,b)P(d|c)

a<sup>1</sup>b<sup>1</sup>

0.7

0.3

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 $a^{1}b^{0}$ 

0.9

0.1

### **Quantitative Specification**

Example: Conditional probability density functions (CPDs) for continuous random variables



### **Quantitative Specification**

Example: Combination of CPTs and CPDs for a mix of discrete and continuous variables



### **Observed Variables**

In a graphical model, shaded nodes are "observed", i.e. their values are given



### MARKOV MODEL

### Markov Model

- Markov assumption: for a sequence of random variables, the probability distribution over x<sub>t</sub> random variables is conditionally independent of x<sub>1</sub>,..., x<sub>t-2</sub> given x<sub>t-1</sub>
- Markov model: defines a joint distribution over a sequence of variables using a Markov assumption
- We can represent the Markov model as a directed graphical model

$$p(x_t \mid x_1, \dots, x_{t-1}) = p(x_t \mid x_{t-1})$$

$$p(x_1, \dots, x_T) = p(x_1) \prod_{t=2}^T p(x_t \mid x_{t-1})$$



### RNN as a DGM

### **UNDIRECTED GRAPHICAL MODELS**

### Three Types of Graphical Models

Directed Graphical Model Undirected Graphical Model

Factor Graph







### Undirected Graphical Models

Representation of both directed and undirected graphical models

### FACTOR GRAPHS

### Three Types of Graphical Models

Directed Graphical Model Undirected Graphical Model

Factor Graph







### Factor Graphs

### **Factor Graph**

(bipartite graph)

- variables (circles)
- factors (squares)



### Factor Graphs

### Factor Graph

(bipartite graph)

- variables (circles)
- factors (squares)



Each **random variable** can be assigned a **value** 

The collection of values for all the random variables is called an **assignment**.

### Factor Graphs

### **Factor Graph**

(bipartite graph)

- variables (circles)
- factors (squares)

Factors have local opinions about the assignments of their neighboring variables



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### How General Are Factor Graphs?

- Factor graphs can be used to describe
  - Markov Random Fields (undirected graphical models)
  - Conditional Random Fields
  - Bayesian Networks (directed graphical models)

### Factor Graph Notation



### Factors are Tensors

• Def: the arity of a <u>170 00</u> factor is the number s vppp.. Xg s vp pp of neighbors S •3 2 (variables) it has  $\psi_{\{1,8,9\}}$ prvp  $X_8$ .pp .1 2 • Factors: S ັvp pp  $\Psi_{\{2,7,8\}}$  $\psi_{\alpha}, \psi_{\beta}, \psi_{\gamma}, \ldots$  $X_7$ d V n р where  $\alpha, \beta, \gamma, \ldots \subseteq \{1, \ldots, n_n^{\mathbf{v}}\}$ 6 3  $\Psi_{\{3,6,7\}}$ 4 2 0.1  $X_6$ 3 1 3 р 1 Def: a unary factor **d** 0.1 8 0 touches one variables • Def: a binary factor  $X_l$  $\psi_{\{1,2\}}$  $X_3$  $X_2$  $\psi_{\{2,3\}}$  $\psi_{\{3,4\}}$ touches two variables V 3 n 4 • Def: a ternary factor p 0.1  $\psi_{\{1\}}$ touches three **d** 0.1 variables time flies like an ari

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### Factors are Tensors

- Factors must contain non-negative values -this ensures we have a valid probability distribution
- We also sometimes refer to factors as potential functions or potentials (like UGMs)





### Ex: Factor Graph over Binary Variables



### Locally Normalized vs. Globally Normalized

