

## UNIT 10B

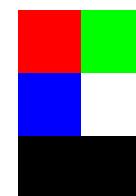
### Concurrency: Moore's Law Revisited & Sorting Networks

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## Review: Bitmap Images

- screen consists of individual pixels
  - pixel = picture elements
- arranged into rows and columns
  - projector 1024x768
  - 720p = 1280x720
  - 1080p = 1920x1080
- Bitmap as a 3-D Ruby Arrays



2 X 3 pixel image

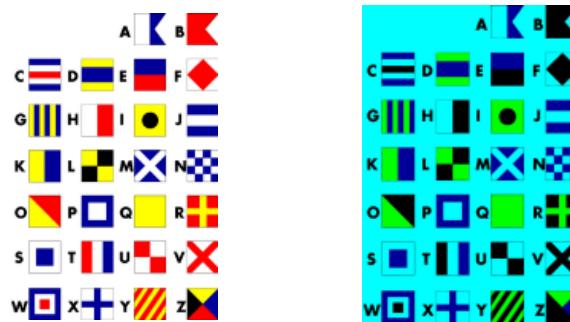
```
bitmap = [[[255,0,0], [0,255,0]],
           [[0,0,255], [255,255,255]],
           [[0,0,0], [0,0,0]]]
```

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# Example: Image Processing

Remove Red operation



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# Example: Image Processing

```
def remove_red(image)
    num_rows = image.length
    num_columns = image[0].length
    for row in 0..num_rows do
        for column in 0..num_columns do
            image[row][column][0] = 0
        end
    end
    return nil
end
```

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## Example: Image Processing

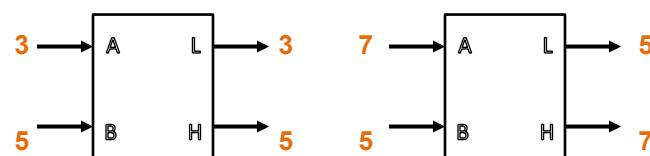
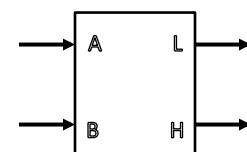
- What order are the pixels processed?
  - row by row, one pixel at a time
- Does this matter?
  - not really: all pixel computations are independent of one another
  - if we have multiple processors (cores), we could have each work on part of the image independently → faster results
  - Graphical Processing Units (GPU)

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## Example: Sorting Networks

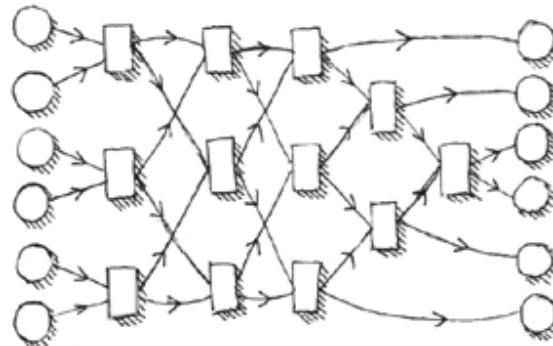
- Comparator
  - Input: A and B
  - Output:
    - If  $A \leq B$ , then  $L = A$  and  $H = B$
    - If  $A > B$ , then  $L = B$  and  $H = A$



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## Activity: Sorting Network Simulation



Input: [5, 1, 6, 3, 4, 2]

How many steps does this take . . . sequentially? concurrently?

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## Review: Merge Operation for Merge Sort

- Merge Operation
- Takes two sorted lists (a and b)
- Returns one sorted list containing elements of a and b
- Can we do this concurrently?  
How?

```
>> merge([27,49,84,91],  
        [17,32,53,63])  
=> [17,27,32,49,53,63,84,91]
```

```
def merge(a,b)  
    i, j = 0, 0  
    c = []  
    while i < a.length  
        and j < b.length do  
        if a[i] <= b[j] then  
            c << a[i]  
            i = i + 1  
        else  
            c << b[j]  
            j = j + 1  
        end  
    end  
    return c + a[i..-1]  
           + b[j..-1]
```

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## An Observation

- Merge with Odd and Even Elements Marked

```
>> merge([27, 49, 84, 91, 92, 93],[17, 32, 53, 63, 95, 98])
```

```
=> [17, 27, 32, 49, 53, 63, 84, 91, 92, 93, 95, 98]
```

- elements initially at even indices
- elements initially at odd indices

- Do you see a pattern?

- How many even/odd elements are in result[0..i]?

- In result[0..i]:

- always, at least as many even as odd
- always, at most two more even than odd
- when i is even, there is exactly one more even than odd

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## A Strategy for Merging

### Procedure for Merging a and b

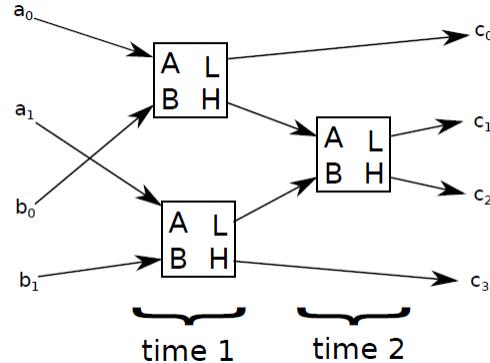
- Parameters: two sorted lists a and b      Result: one sorted list c
  - Split a into **even\_a** and **odd\_a**
  - Split b into **even\_b** and **odd\_b**
  - Recursively, merge **even\_a** and **even\_b** into **even\_c**
  - Recursively, merge **odd\_a** and **odd\_b** into **odd\_c**
  - interleave **even\_c** and **odd\_c** to get an almost-sorted c
  - swap neighbors, as necessary, to completely sort c

```
a = 27 49 84 91 b = 17 32 53 63
even_a = 27 84 odd_a = 49 91 even_b = 17 53 odd_b = 32 63
even_c = 17 27 53 84 odd_c = 32 49 63 91
c = 17 32 27 49 53 63 84 91
c = 17 27 32 49 53 63 84 91
```

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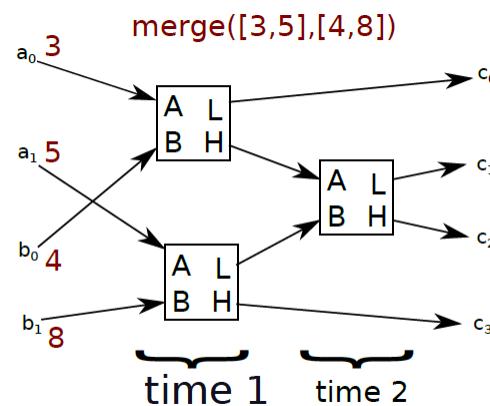
## 2 X 2 Merge Network



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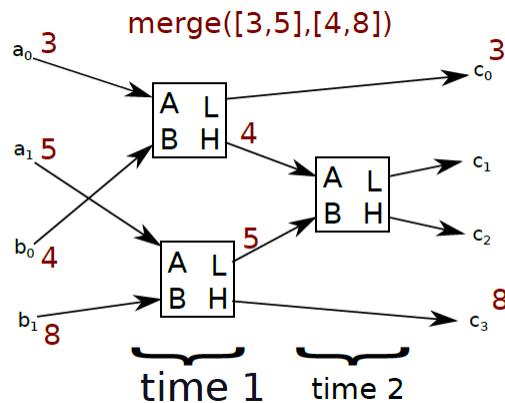
## 2 X 2 Merge Network



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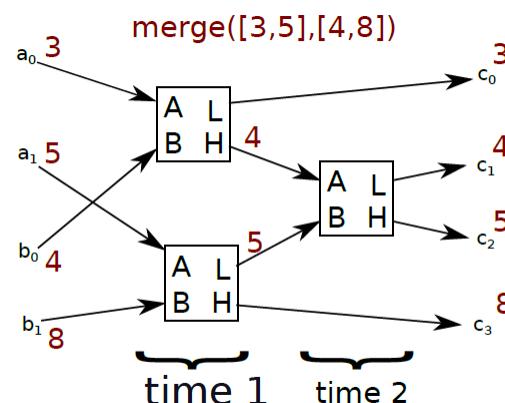
## 2 X 2 Merge Network



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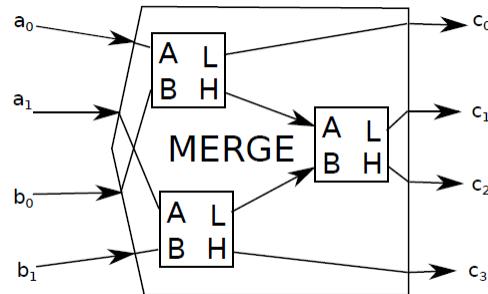
## 2 X 2 Merge Network



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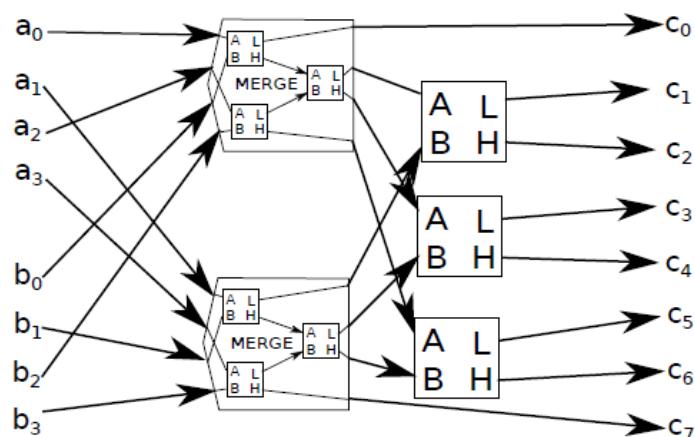
## 2 X 2 Merge Network Abstraction



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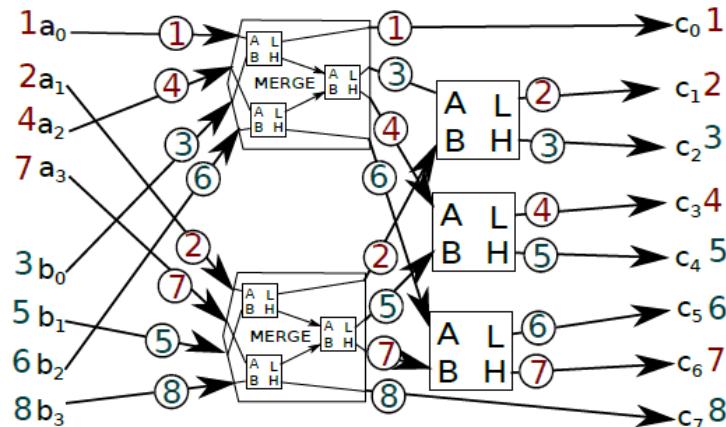
## 4 X 4 Odd-Even Merge



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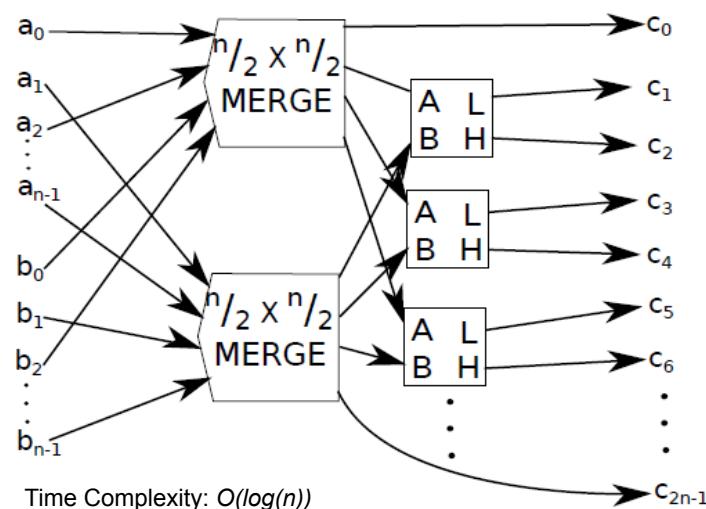
## 4 X 4 Odd-Even Merge



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## $n \times n$ Odd-Even Merge



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## Summary

- Multi-cores allow us to think about computation as a concurrent process.
- Some applications are naturally “parallel” and can be split up into smaller subproblems that are solved independently by individual processors/cores.
  - image processing
  - sorting